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**BOUNDARY-LAYER TRANSITION DETECTION IN  
CRYOGENIC WIND TUNNEL USING FLUORESCENT  
PAINTS.**

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# Applications of Temperature and Pressure Sensitive Paints

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## Summary

Luminescent molecular probes imbedded in a polymer binder form a temperature or pressure paint. On excitation by light of the proper wavelength, the luminescence, which is quenched either thermally or by oxygen, is detected by a camera or photodetector. From the detected luminescent intensity, temperature and pressure can be determined. The basic photophysics, calibration, accuracy and time response of a luminescent paints is described followed by applications in low speed, transonic, supersonic and cryogenic wind tunnels and in rotating machinery.

## Introduction

The use of luminescent molecular probes for measuring surface temperature and pressure on wind tunnel models and flight vehicles offers the promise of enhanced spatial resolution and lower costs compared to traditional techniques. These new sensors are called temperature-sensitive paint (TSP) and pressure-sensitive paint (PSP). Traditionally, arrays of thermocouples and pressure taps have been used to obtain surface temperature and pressure distributions. These techniques can be very labor-intensive and model/flight vehicle preparation costs are high when detailed maps of temperature and pressure are desired. Further, the spatial resolution is limited by the number of instrumentation locations chosen. By comparison, the TSP and PSP techniques provide a way to obtain simple, inexpensive, full-field measurements of temperature and pressure with much higher spatial resolution. Both TSP and PSP incorporate luminescent molecules in a paint which can be applied to any aerodynamic model surface. Figure 1 shows a schematic of a paint layer incorporating a luminescent molecule.

The paint layer is composed of luminescent molecules and a polymer binder material. The resulting 'paint' can be applied to a surface using a brush or sprayer. As the paint dries, the solvent evaporates and leaves behind a polymer matrix with luminescent molecules embedded in it. Light of the proper wavelength to excite the luminescent molecules in the paint is directed at the model and luminescent light of a longer wavelength is emitted by the molecules. Figure 2 shows the spectra for a typical luminescent ruthenium molecule. Using the proper filters, the excitation light and luminescent emission light can be separated and the intensity of the luminescent light can be determined using a

photodetector. Through the photo-physical processes known as thermal- and oxygen-quenching, the luminescent intensity of the paint emission is related to temperature or pressure. Hence, from the detected luminescent intensity, temperature and pressure can be determined.

The polymer binder is an important ingredient of a luminescent paint used to adhere the paint to the surface of interest. In some cases, the polymer matrix is a passive anchor. In other cases, however, the polymer may affect significantly the photophysical behavior of the paint through a complicated interaction between the luminescent molecules and the macro-molecules of the polymer. A good polymer binder should be robust enough to sustain skin friction and other forces on the surface of an aerodynamic model. Also, it must be easy to apply and repair to the surface in a smooth, thin film. For TSPs, many commercially available resins and epoxies can be chosen serve as polymer binders if they are not oxygen permeable and do not degrade the activity of the luminophore molecules. In contrast, a good polymer binder for a PSP must have high oxygen permeability besides being robust and easy to apply.

Two recent papers ( Liu et al. 1997 and Gouterman 1997 ) provide excellent reviews of the foundations and history of TSP and PSP and contain extensive reference lists.

## Measurement Systems

The measurement systems are the same for both TSPs and PSPs. The essential elements of the systems include illumination sources, optical filters, photodetectors and data acquisition/processing units. This section provides a brief description of two measurement systems: the CCD camera system and the laser scanning system. Intensity based measurements are considered first and then lifetime and multi-luminophore systems.

### CCD Camera System

The CCD camera system for luminescent paints is the most commonly used in aerodynamic testing. A schematic of this system is shown in Figure 3. The luminescent paint (TSP or PSP) is coated on the surface of the model. The paint is excited to luminesce by the illumination source, such as a lamp or a laser. The luminescent intensity image is filtered optically to eliminate the illuminating light and then captured by a CCD camera and transferred to a computer with a frame grabber board for image processing. Both

wind-on image (at temperature and pressure to be determined) and wind-off image (at a known constant temperature and pressure) are obtained. The ratio between the wind-on and wind-off images is taken after the dark current level image is subtracted from both images, yielding a relative luminescent intensity image. Using the calibration relations, the surface temperature and pressure distributions can be computed from the relative luminescent intensity image.

Selection of the appropriate illumination sources depends on the absorption spectrum of the paint and the optical access of the facility. The source must provide a large number of photons in the wavelength band of absorption. A variety of illumination sources are available. Lasers with fiber-optic delivery systems have been used in wind tunnel tests (Morris et al. 1993b, Crites 1993, Bukov et al. 1992, Engler et al. 1995). Other light sources reported in literature include a xenon arc light with a blue filter (McLachlan et al. 1993a), incandescent tungsten/halogen lamps (Dowgwillo et al. 1994) and fluorescent UV lamps (Liu et al. 1995a, 1995b). Morris et al. (1993a) and Crites (1993) discussed the characteristics of some illumination sources. For imaging the surface, scientific grade cooled CCD digital cameras can provide high intensity resolution (12 and 16 bits) and high spatial resolution (up to  $2048 \times 2048$  pixels). Since the scientific grade CCD camera exhibits good linearity and high signal-to-noise ratio (SNR), it is particularly suitable to quantitative luminescent intensity measurements.

A necessary step in data processing is taking the ratio between the wind-on luminescence image and the wind-off reference image at a known reference temperature and pressure. The image ratio process can eliminate the effects of spatial non-uniformity in illumination light, coating thickness, and luminophore concentration. However, since aerodynamic forces may cause model motion and deformation in high-speed wind tunnel tests, the wind-on image may not align with the wind-off image. The ratio between the non-aligned images leads to considerable errors in calculating temperature and pressure using the calibration relations. Also, some distinct flow characteristics, such as shocks, transition and separation locations, could be smeared. In order to correct this non-alignment, an image registration method was suggested by Bell and McLachlan (1996) and Donovan et al. (1993).

### **Laser Scanning System**

A laser scanning system for TSPs and PSPs is shown in Figure 4. A low power laser is focused to a small point and scanned over the surface of the model using computer controlled mirrors. The laser illumination excites the paint on the model and luminescence is detected by a low noise photodetector (e.g. a PMT). The photodetector signal is digitized with a high resolution A/D converter and processed to obtain temperature and pressure. The mirror is synchronized to the data acquisition so that the position of the laser spot on the model is accurately known.

Compared with the CCD camera system, it takes longer to obtain full-surface temperature and pressure distributions using the laser scanning system. However, this system has some advantages. (Hamner et al. 1994)

- (i) Luminescence is detected by a low noise photodetector. Before the analog output from the PMT is digitized, filtering and other SNR enhancement techniques are available to improve the measurement resolution. The signal is then digitized with a high resolution (12 to 24 bit) A/D converter. Additional noise reduction can be accomplished by using a lock-in amplifier if the laser intensity is modulated.
- (ii) The laser scanning system can be used for measurement in a facility where optical access is very limited and the CCD camera system is difficult to use.
- (iii) The system provides uniform illumination over the surface by scanning a single light spot.
- (iv) The system can be easily adapted for measurement of luminescent lifetime or phase shift if a pulsed laser or modulated laser is used.

### **Lifetime-based detection systems**

A promising method for making temperature and pressure measurements is to determine the luminescent lifetime of the paint rather than the luminescent intensity. Compared with the intensity-based method, the greatest advantage of this method is that the lifetime-temperature or -pressure relation is not dependent on illumination intensity. Therefore, the calibration relation is intrinsic for a particular paint and the image ratio process is not required. Also, the lifetime measurement is insensitive to luminophore concentration, paint thickness, photodegradation, tubid paint surface and dirty optical surfaces. The temperature and pressure can be directly obtained from the measured lifetime. The lifetime measurement technique in photochemistry is well-developed (Szmecinski and Lakowicz 1995, Papkovsky 1995). The basic configuration of this system is similar to either the CCD camera or the laser scanning system, except a pulsed excitation light is used. After each pulse, the luminescence decay is detected and acquired by a computer. Then, temperature or pressure is obtained by using the calibration relation. Using a lifetime detection system, Davies et al. (1995) measured the pressure distributions on a cylinder in subsonic flow and on a wedge at Mach 2. Comparison with data obtained by conventional pressure taps was favorable.

A frequency-domain method detects the phase angle between the luminescence emission and harmonically modulated excitation light. If the modulation frequency is fixed, the phase angle is a function of the lifetime and hence is dependent on temperature and pressure. The phase angle can be measured using a lock-in amplifier. Campbell et al. (1994) gave a calibration between phase angle and temperature for Ru(bpy)-Shellac paint at 100 kHz modulation frequency. A simple phase detection system using blue LED excitation was used to measure surface temperature on an electrically heated steel foil on which a

round air jet impinged (Campbell et al. 1994). Torgerson et al. (1996) measured the pressure distribution in a low-speed impinging jet using a laser scanning system with an optical modulator.

### Multi-Luminophore System

Use of the normal CCD camera or laser scanning system requires a ratio between the wind-on and wind-off luminescent images. This image ratio method inevitably causes inaccuracy in determining temperature and pressure because the image registration is never perfect. A two-color luminophore paint would eliminate the need for a wind-off reference image. Two-color luminescent TSP is made by combining a temperature-sensitive luminophore with a temperature-insensitive reference luminophore. Similarly, two-color luminescent PSP consists of a pressure-sensitive luminophore with a pressure-insensitive reference luminophore. The probe luminophore and reference luminophore can be excited by the same illumination. However, there is ideally no overlap between the emission spectra of the probe luminophore and reference luminophore such that two color luminescent images can be completely separated by optical filters. The ratio between these two color images can eliminate effects of spatial non-uniformity in illumination, paint thickness and luminophore concentration. Besides the aforementioned combinations, a temperature sensitive luminophore which is not quenched by oxygen can be combined with an oxygen sensitive luminophore. This dual luminophore temperature/pressure paint can be used for temperature correction in PSP measurement. Furthermore, a multi-color PSP can be developed to correct simultaneously the effects of both temperature variation and non-uniformities in lighting, paint thickness and concentration.

Some preliminary experiments indeed indicate that a two-color PSP can correct variations in illumination (Oglesby et al. 1995, Harris and Gouterman 1995). Three pressure sensitive paints with internal temperature sensitive luminophore have also been tested by Oglesby et al. (1996). Their results show that the dual luminophore paint enables point-by-point correction of temperature effects of PSP measurement. Only recently, a two-color PSP was used to measure pressure distribution in a low speed impinging jet (Torgerson et al. 1996).

### Temperature Sensitive Paints

This section will describe the photophysics, calibration, accuracy, time response of temperature sensitive paint.

#### Photophysics

For a TSP, it is assumed that the paint layer is not oxygen-permeable so that  $[O_2] = 0$ . Hence, the quantum yield is simply given by

$$\Phi = \frac{I}{I_a} = \frac{k_L}{k_L + k_D} = k_L \tau_0 \quad (1)$$

The deactivation term  $k_D$  may be decomposed into a temperature-independent part  $k_0$  and a temperature-dependent part  $k_1$  that is related to thermally activated intersystem crossing (i.e.  $k_D = k_0 + k_1$ ). The rate  $k_1$  can be assumed to have an Arrhenius form (Bennett and McCartin 1966, Schanze et al. (1997)

$$k_1 = C \exp(-E/RT) \quad (2)$$

where  $C$  is a constant,  $E$  is the Arrhenius activation energy,  $R$  is the universal gas constant and  $T$  is the thermodynamic temperature (in Kelvin).

The relation (1) can be approximately written in the simple Arrhenius form

$$\ln \frac{I(T)}{I(T_{ref})} = \frac{E}{R} \left( \frac{1}{T} - \frac{1}{T_{ref}} \right) \quad (3)$$

Theoretically speaking, the Arrhenius plot of  $\ln[I(T)/I(T_{ref})]$  versus  $1/T$  gives a straight line of slope  $E/R$ . Tests indicate that the simple Arrhenius relation does fit experimental data over a certain temperature range. However, for some paints, the data may not fully obey the simple Arrhenius relation over a wider range of temperature. As an alternative, the relation between the luminescence intensity and temperature can be expressed in a functional form

$$\frac{I(T)}{I(T_{ref})} = F(T/T_{ref}) \quad (4)$$

The empirical expression  $F(T/T_{ref})$  could be a polynomial, exponential or other functions to fit the experimental data over a certain temperature range. Both (3) and (4) are operational forms of the calibration relation for a TSP used for data reduction in practical applications.

#### TSP Calibration

In order to quantitatively measure temperature with the TSP coatings, a calibration relating luminescent intensity or lifetime to temperature is needed. A calibration rig consists of a temperature controlled sample and appropriate illumination source and luminescent detector.

Typical temperature dependencies of luminescent intensity are shown in Figure 5 for some TSPs. Several TSPs have high temperature sensitivity in cryogenic temperature range. Others can be used in a temperature range from -20 to 105 °C. Figure 6 gives a lifetime calibration of two TSPs.

#### Accuracy

The accuracy of the temperature measurement has been shown to depend primarily on calibration accuracy, but is in the range of 1 degree. ( see Liu et al. 1995b for a detailed analysis)

#### Time Response

There are two characteristic time scales that are related to the time response of the paint. One is the luminescent lifetime which represents an intrinsic physical limit for the achievable temporal resolution of the paint. Luminescent paint usually has a lifetime ranging from  $10^{-10}$  seconds to milliseconds. Another is the time scale of the thermal diffusion in the TSP layer. In a forced convection-dominated case, the thermal diffusion time can be expressed by  $\tau = \rho c \ell / h$ , where  $\rho$  is the density,  $c$  is the specific



heat,  $\ell$  is the paint thickness and  $h$  is the convection heat transfer coefficient. In general, the diffusion time is much larger than the lifetimes of most luminescent paints. Therefore, the time response of the luminescent paint is mainly limited by the diffusion processes for both TSP and PSP measurements.

Figure 7 shows the temperature response of the TSP paint subjected to the pulsed laser heating. (Liu et al., 1995c). The surface temperature increases rapidly after the pulsed laser beam is turned on and then gradually decays due to natural convection. By fitting the experimental data with the asymptotic solutions, it is found that  $\tau_1 = 0.25$  ms (heating) and  $\tau_2 = 25$  ms (cooling).

## TSP Applications

### Transition Detection

TSP has also been utilized as an approach to flow transition detection (Campbell 1994, McLachlan et al. 1993b). Since convective heat transfer is much higher in turbulent flow than in laminar flow, TSP can visualize the surface temperature difference between turbulent and laminar regions. In low speed wind tunnel tests, the model is typically heated or cooled to enhance temperature variation across the transition line. Using EuTTA-dope paint, Campbell et al. (1992, 1993) visualized transition patterns on a symmetric NACA 65<sub>4</sub>-021 airfoil in a low-speed wind tunnel. (Figure 8). Recently, cryogenic TSP systems have been developed at Purdue, the University of Florida NASA Langley and National Aerospace Laboratory (NAL), Japan. Several TSP formulations have been successfully used to detect transition on airfoils in a 0.1m transonic cryogenic wind tunnel at the NAL in Japan (Figure 9 from Asai et al. 1997a) and a 0.3m cryogenic wind tunnel at NASA-Langley (Figure 10 from Popernack et al.).

### Quantitative Heat Transfer

Global surface heat transfer mapping on a waverider model in Mach 10 flow has been obtained using EuTTA-dope paint (Liu et al. 1995b).

A thin Mylar insulating layer covered the windward side of the model, and EuTTA-dope paint was applied on the insulating layer. The temporal evolution of surface temperature distributions was obtained and then heat flux was calculated using a simple heat transfer model. Figure 11 shows a representative map of heat flux on the windward side of the waverider. The bright and dark regions correspond to high and low heat transfer, respectively. The low heat transfer region near the leading edge corresponds to laminar flow. Transition from laminar to turbulent flow can be easily identified by an abrupt change from low to high heat transfer. Figure 12 shows a typical heat transfer history. The TSP measurement is in good agreement with data obtained by thermocouples.

### Pressure Sensitive Paints

This section will describe the photophysics, calibration, accuracy, time response of pressure sensitive paint.

### Photophysics

PSP operation is based on the principle that certain fluorescent molecules are quenched by the presence of oxygen. In the molecules of interest, oxygen interacts with the excited molecules and the excess energy is transferred to the oxygen in a collisional process, with no photons being emitted. This process, known as oxygen quenching, is the basis for the pressure sensitive paint method.

According to Henry's law, oxygen concentration is proportional to the partial pressure of oxygen, which is proportional to static pressure. The result is that if there is a locally high pressure area, the fluorescent molecules will be quenched by oxygen.

The quenching process is governed by the Stern Volmer equation which can be written as a ratio of intensities in order to remove the effects of concentration, thickness and illumination variations.

$$\frac{I_{ref}}{I} = A(T) + B(T) \left( \frac{P}{P_{ref}} \right) \quad (5)$$

$I_{ref}$  = fluorescence intensity at reference condition

$P_{ref}$  = pressure at reference condition

$A(T), B(T)$  = Stern Volmer constants

The result is that an increasing pressure causes the intensity of the paint to decrease. In using equation 5, an intensity map must be acquired at a reference condition, typically a flow off or slow rotation where the pressure is a known constant across the surface.

In this version of the Stern Volmer equation, the coefficients  $A$  and  $B$  are functions of temperature.

$$A(T) = a_1 \left[ 1 + \frac{E_{nr}}{RT_{ref}} \left( \frac{T - T_{ref}}{T_{ref}} \right) \right],$$

$$B(T) = b_1 \left[ 1 + \frac{E_p}{RT_{ref}} \left( \frac{T - T_{ref}}{T_{ref}} \right) \right]$$

$E_{nr}$  = non-radiative activation energy

$E_p$  = polymer activation energy

$R$  = interaction distance

$a_1, b_1$  = constants

The temperature dependence of  $A$  is due to the thermal quenching as in TSP. The temperature dependence of  $B$  is due to the temperature dependence of diffusivity of the polymer binder. (Torgerson 1997, Schanze et al.)

### Calibration

Figure 13 shows Stern Volmer curves for various paints at room temperature. A calibration of Ru(ph<sub>2</sub>-phen) in GE RTV 118 at several temperatures is given in Figure 14 and for PtTFPP in polystyrene in Figure 15.

### Accuracy

To estimate the uncertainty of the PSP measurement with a scientific-grade CCD camera system, Morris et al. (1993a) conducted a series of calibration experiments focused on a proprietary PSP paint sample in a pressure vessel which controlled both the temperature and pressure. After

averaging a 32 sequential images to improve the SNR, they found that the minimum pressure resolution near atmospheric pressure (13 to 16 psia) is about  $\pm 0.05$  psid for their system. Note that the above uncertainty estimates do not contain the contributions from some major error sources such as the temperature effects and model displacement. The uncertainty of PSP measurements depends strongly on a systematic error source associated with the temperature dependence of the paint. An analysis by Sajben (1993) indicates that the temperature uncertainty dominates the PSP measurement errors. Another major error source is model motion between the wind on and wind off images. To date, it has been necessary to perform an in-situ calibration of the PSP using standard pressure taps on the model in order to obtain reasonable accuracy.

#### Time Response

Based on the transient solution of the diffusion equation, the oxygen diffusion time for a thin PSP coating is on the order of  $\tau = \ell^2 / D_m$ , where  $\ell$  is the coating thickness and  $D_m$  is the mass diffusivity of oxygen in the paint layer.

Baron et al. (1993) studied the time response to oxygen concentration changes of several PSPs using a pressure jump apparatus. The PSPs that they investigated are PtOEP in GP-197 and MAX-100 polymer binders and H<sub>2</sub>TFPP in Silica-W, Silica-B and TLC binders. They found that the response times for GP-197 and MAX-100 binder are 2.45 s and 0.4 s, respectively. The Silica-W and Silica-B show response times of 11 ms and 1.5 ms, respectively. The response time of the TLC is about 25  $\mu$ s. Recently, using a similar set-up, Carroll et al. (1996) measured the step response of three PSPs: a proprietary PSP from McDonnell Douglas, PtOEP on a white primer layer, and PtOEP in GP-197. For the McDonnell Douglas paint with thickness ranging from 13 to 35  $\mu$ m, the response time varies from 0.042 s to 0.42 s. The response time of PtOEP on a white primer layer is 45 ms. For PtOEP in GP-197, the response times are 1.4 s, 1.6 s and 2.6 s for the paint thickness of 22  $\mu$ m, 26  $\mu$ m and 32  $\mu$ m, respectively. Bukov et al. (1992) reported that a proprietary fast-responding PSP coating developed by TsAGI has a time constant of 5 ms. Clearly, the diverse time constants of various PSPs result from the effects of the different polymer diffusivity, coating thickness and structure of the paint.

### PSP Applications

Most of PSP measurements on aerodynamic models have been conducted in transonic and supersonic wind tunnels. Recently, the PSP technique has been used for pressure measurements in low-speed flows and rotating machinery.

#### Tests in Wind Tunnels

PSPs have been applied to pressure measurements in wind tunnel tests over a wide range of Mach numbers in order to examine the feasibility of this method. Kavandi et al. (1990) and McLachlan et al. (1993a) tested a two-dimensional airfoil (NACA-0012) over a Mach number range of 0.3 to 0.66. McLachlan et al. (1995a, 1995b) also

tested a large generic transport wing/body configuration in transonic Mach number from 0.7 to 0.9. The PSP data not only provide good quantitative chordwise pressure results, but also show complicated two-dimensional pressure maps that would be difficult to deduce from the usual discrete tap data. Some experiments conducted in the McDonnell Douglas Research Laboratories (Morris et al. 1993b) include pressure measurements on a generic wing/body model (Mach number = 2 and angle of attack = 8 degree), a model of a high performance fighter (Mach number = 1.2), and a two-dimensional converging/diverging nozzle. Sellers and Brill (1994) conducted a demonstration test of a PSP in the Arnold Engineering Development Center transonic wind tunnel for an aircraft model. Using fast-responding PSP coatings developed at TsAGI, Troyanovsky et al. (1993) carried out a semi-quantitative pressure visualization for a shock/body interaction in a Mach 8 shock tube with 0.1 s duration, and Borovoy et al. (1995) determined the pressure distributions on a cylinder at Mach 6 in a shock wind tunnel with about 40 ms duration. In general, the PSP technique works well in high Mach number subsonic flows and supersonic flows since static pressure change is typically large. Morris (1995) and Shimbo et al. (1997) measured the pressure on delta wings at low Mach numbers ranging from 0.05 to 0.2. These results indicate the low pressure regions induced by leading edge vortices.

Figure 16 shows a typical surface pressure map in the interaction of a cylinder mounted normal to a flat floor with a supersonic turbulent boundary layer at a freestream Mach number of 2.5. In this test carried out in the Purdue University supersonic wind tunnel, the incoming boundary layer thickness is 4 mm, the cylinder height is 15 mm, and the cylinder diameter is 4.8 mm. The PSP, Ru(ph<sub>2</sub>-phen) in GE RTV 118, was applied to the floor surface for pressure measurement. The pressure map clearly indicates a pressure rise induced by a bow shock ahead the cylinder and a low pressure region in the turbulent wake behind the cylinder.

#### Transonic Airfoil - Lifetime Method

The laser scanning method for pressure and temperature sensitive paints was demonstrated in the Boeing Company model transonic wind tunnel. (Torgerson 1997) The airfoil was 10% thick with a sharp leading edge and a small amount of camber. It had 19 pressure taps along the upper surface to compare with the pressures found from the paints. The laser used was a small air-cooled argon-ion laser. The beam was modulated using an electro-optic modulator, enabling the signal to be processed by a two phase lock-in amplifier. Both intensity and phase were recorded during the scan over the airfoil, so that a comparison between intensity and lifetime methods could be made. Results in Figure 17 show both methods compare favorably with the pressure tap data. The phase measurements have the advantage that wind off data is not required.

#### Cryogenic Pressure Paint

Recently, Asai et al. 1997b demonstrated the feasibility of using luminescent coatings for surface pressure measurements in a cryogenic wind tunnel. Calibrations of a

new anodized layer (Figures 18 and 19) show extremely high oxygen sensitivity. By injecting a small of oxygen (250 ppm) into the NAL transonic cryogenic tunnel excellent comparison between pressure taps and PSP was obtained for flow over a 14% circular-arc bump model. (Figure 20)

### Rotating Machinery

The PSP/TSP technique provides a promising tool for measuring surface pressure distributions on a high-speed rotating blade at a high spatial resolution. Instrumentation is particularly difficult in the rotating environment and the pressure taps weaken the structure of the rotating blade. Recently, a test was performed to measure the chordwise pressure distributions on the rotor blades of a high speed axial flow compressor shown in Figure 21 (Liu et al 1996b). TSP (Ru(bpy)-Shellac) and PSP (Ru(ph<sub>2</sub>-phen) in GE RTV 118) were applied to alternating blades. The TSP provided the temperature distributions on the blades for temperature correction of the PSP results. A scanning laser system was used for excitation and detection of luminescence. Both the TSP and PSP were excited with an Argon laser and luminescence was detected with a Hamamatsu PMT. The pressure map of Figure 22 shows a strong suction surface shock wave. Comparisons to CFD over a range of rotational speeds (Figure 23) show good correlation but require care in interpretation since the error in the PSP is ~.1 psia because an in-situ calibration was not possible. The same system was on used on an Allied Signal F109 gas turbine engine (Figure 24) giving the suction surface pressure map at 14000 rpm shown in Figure 25.

### Conclusion

The fundamentals and applications of the TSP and PSP techniques have been discussed in this paper. The TSP technique has been used not only to visualize surface flow features such as boundary layer transition, shocks and separation, but also to obtain quantitative surface temperature and heat transfer maps with good accuracy. Applications of the PSP technique are focused on surface pressure measurements on airfoils, generic wing-body models aircraft models and turbomachinery over a wide range of Mach numbers. The field mapping capability of the TSP and PSP techniques is able to provide information about complicated flow characteristics that cannot be easily acquired using more conventional methods. Much effort has being made to improve essential elements of the measurement system including paint formulation, illumination, imaging, and data acquisition/processing hardware and software. Many groups are working to extend and refine TSP and PSP measurements so they will become a routine procedure in aerodynamics testing.

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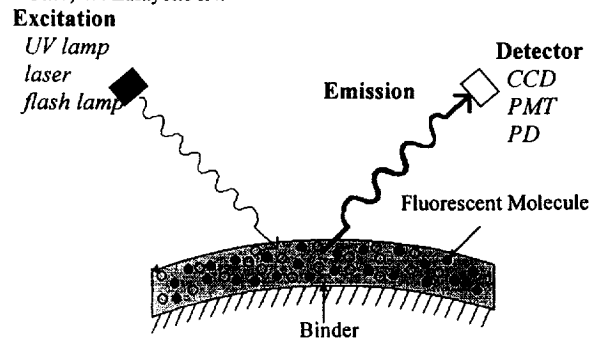


Figure 1: Schematic of TSP/PSP Layer

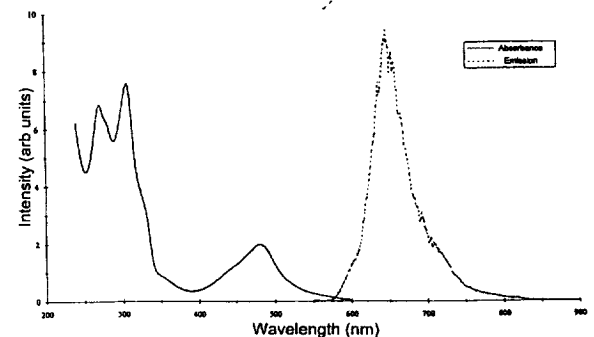


Figure 2: Excitation and Emission spectra of a Ruthenium based molecule

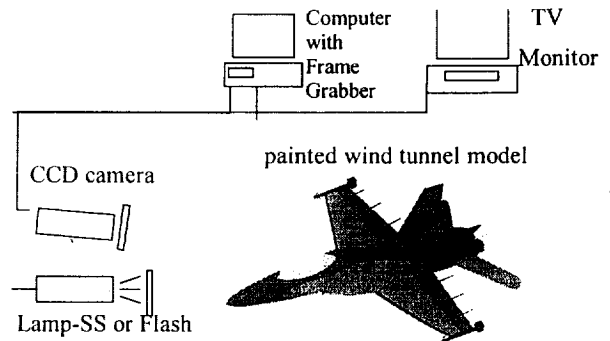


Figure 3: Schematic of CCD camera system

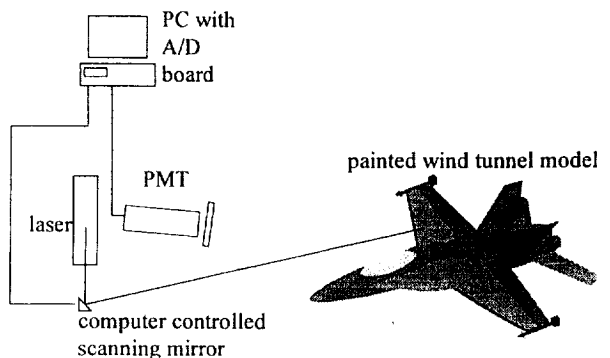


Figure 4: Schematic of laser scanning system

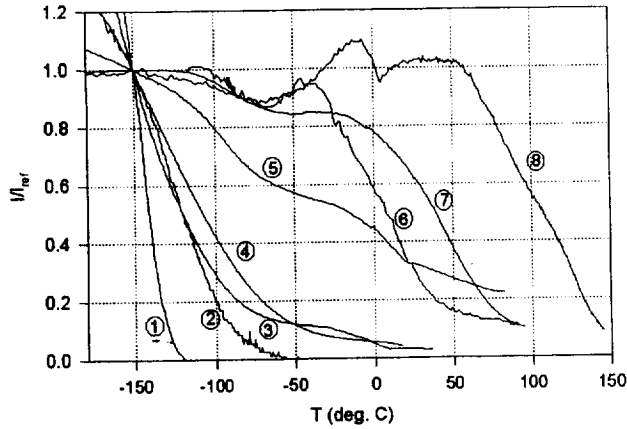


Figure 5. Temperature dependence of luminescence intensity for several TSP formulations: (1) Ru(trpy) in Ethanol/ Methanol, (2) Ru(trpy)(phtrpy) in GP-197, (3) Ru(VH127) in GP-197, (4) Ru(trpy) in Du Pont Chroma Clear, (5) Ru(trpy)/Zeolite in GP-197, (6) EuTTA in dope, (7) Ru(bpy) in Du Pont Chroma Clear, (8) Perylenedicarboximide in Sucrose Octaacetate. ( $T_{ref} = -150$  °C).

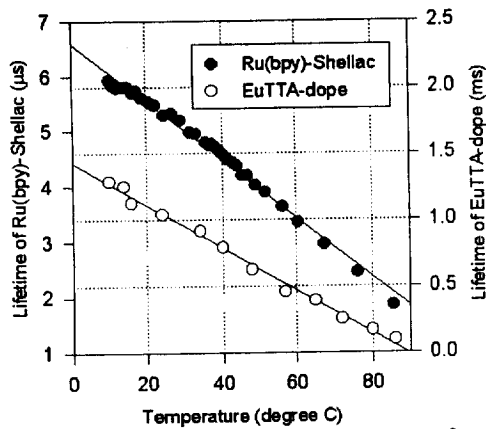


Figure 6 Lifetime-temperature relations for Ru(bpy)-Shellac and EuTTA-dope paints.

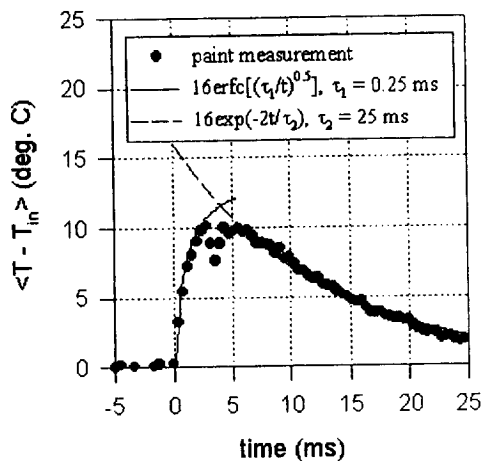


Figure 7 Temperature response of Ru(bpy)-Shellac paint to pulsed laser heating on steel foil.

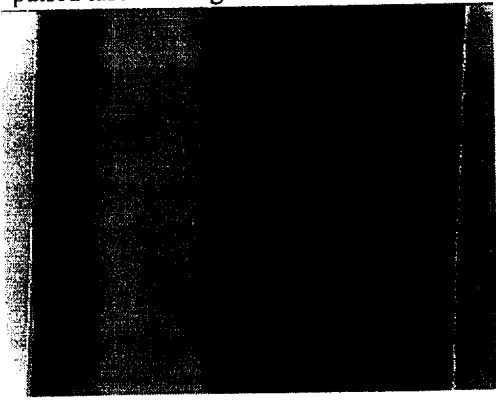


Figure 8. Transition at low speed on a NACA 65-021 Airfoil

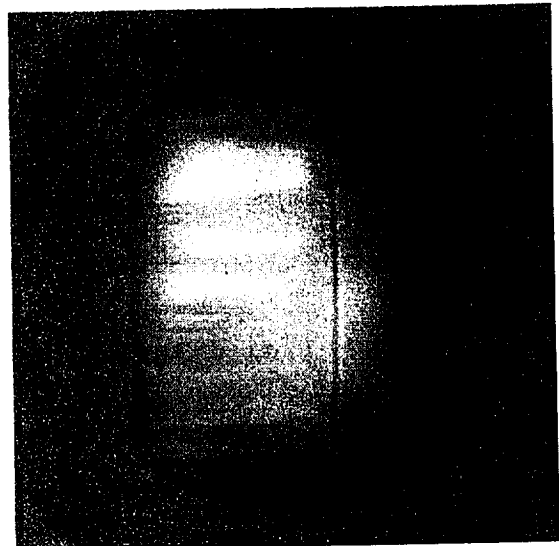


Figure 9. Transition on a NACA 64A021 at  $M=0.82$  and  $T=120$  K in NAL cryogenic wind tunnel.

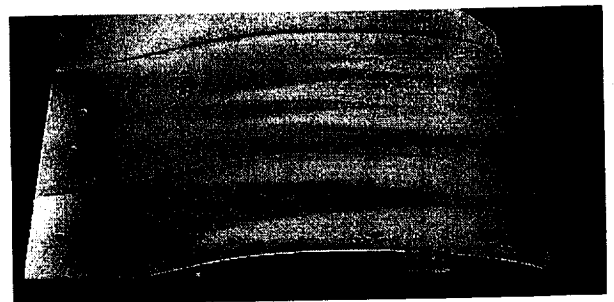


Figure 10. Transition on a HSNLF in the NASA .3 meter cryogenic wind tunnel.



Figure 11. Transition on a Waverider model at  $M=10$ .

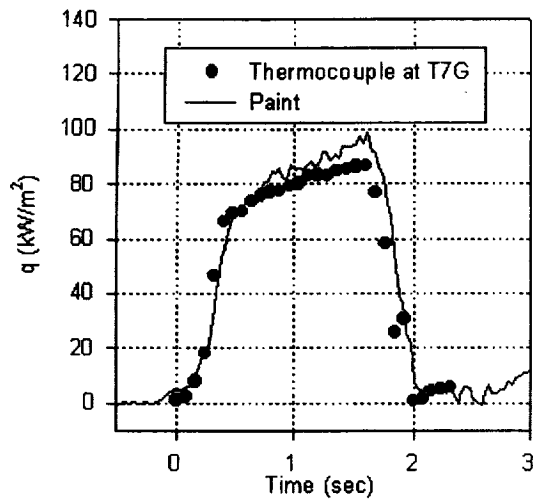


Figure 12 Heat transfer history on a Mach 10 waverider model at location T7G.

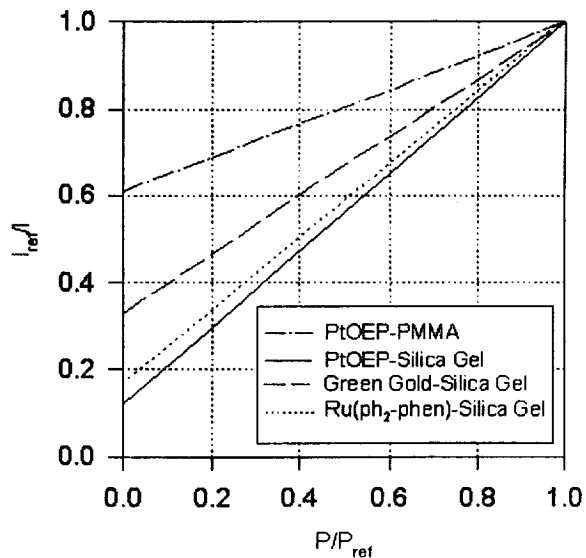


Figure 13 Stern-Volmer plots for several PSPs at ambient temperature (22 °C), where  $P_{ref}$  is the ambient pressure and  $I_{ref}$  is the luminescence intensity at ambient conditions.

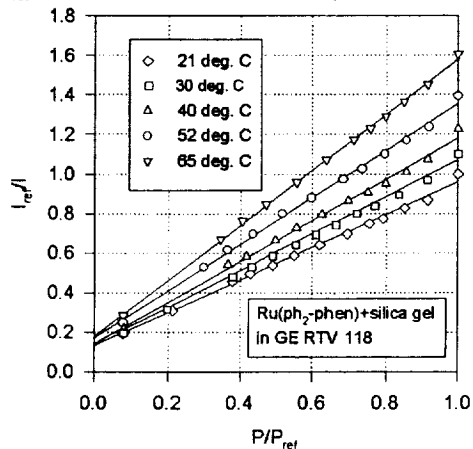


Figure 14. Calibration of Ruthenium based PSP.

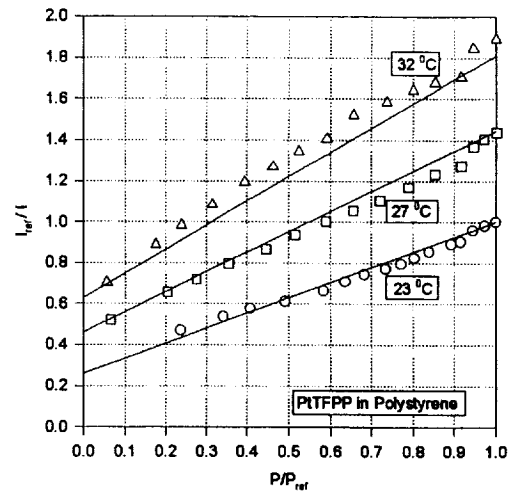


Figure 15. Calibration of PtTFPP pressure paint.

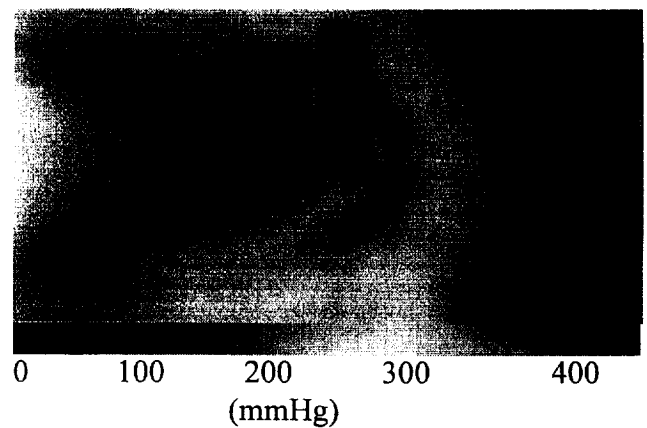


Figure 16. Pressure map for cylinder/boundary layer interaction at  $M=2.5$ .

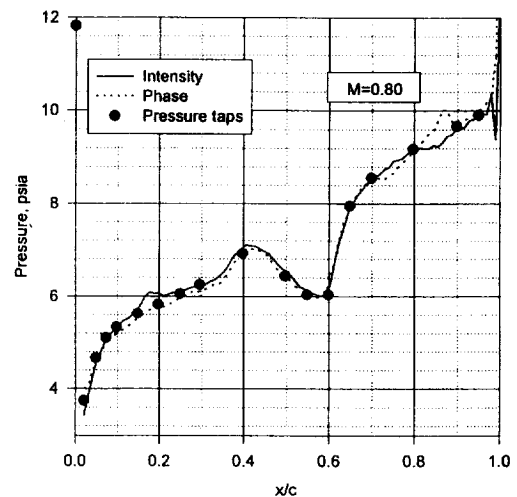


Figure 17. Pressure distribution on a transonic airfoil using both intensity and lifetime based methods.

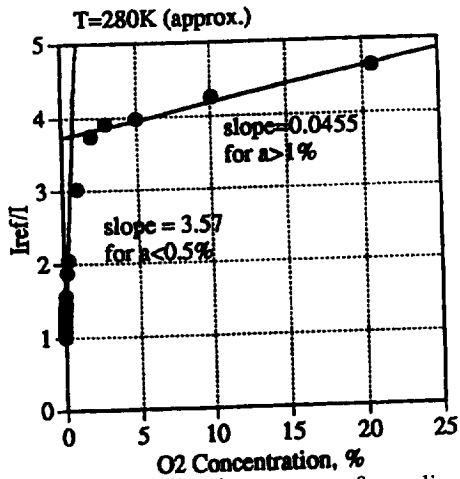


Figure 18. Calibration curve of anodized luminescent coating.

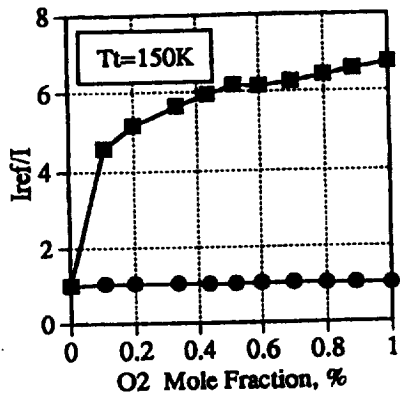


Figure 19. Calibration curve at cryogenic temperature.

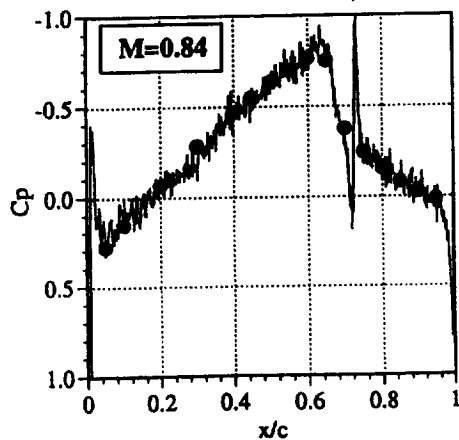


Figure 20. Comparison of luminescent paint and pressure tap data at  $T= 100K$ .

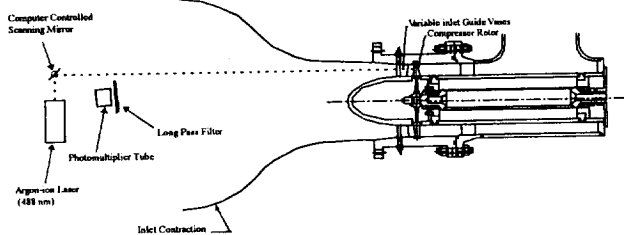


Figure 21. Transonic compressor rig with laser scanning system

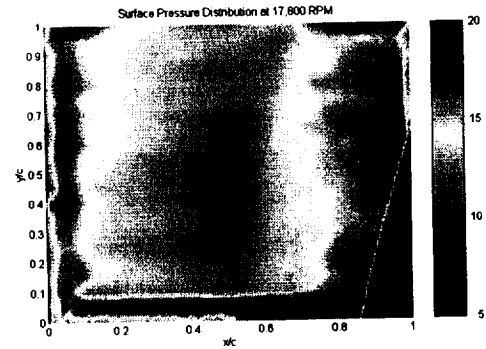


Figure 22. Compressor blade suction surface pressure map at 17,800 rpm (scale in psia).

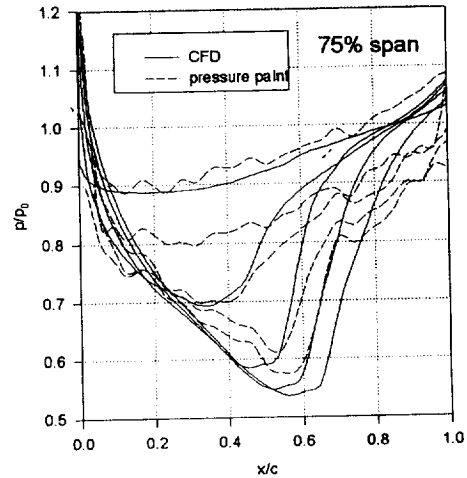


Figure 23. Comparison of PSP data and CFD results.

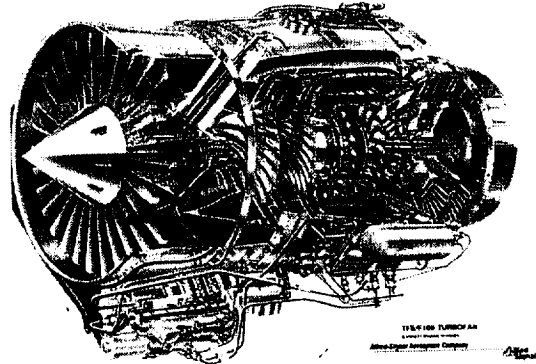


Figure 24. Allied F109 turbofan engine.

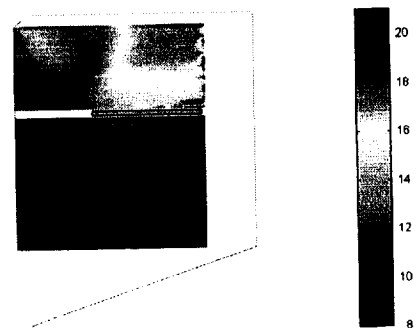


Figure 25. Fan blade pressure distribution at 14,000rpm  
(scale in psia).



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# Anodized Aluminum Pressure Sensitive Paint in a Cryogenic Wind Tunnel

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## KEYWORDS

Pressure-Sensitive Paint, Anodized Aluminum, Cryogenic Wind Tunnel

## ABSTRACT

Anodized aluminum pressure-sensitive paint has been used to measure the surface pressure distributions of wind tunnel models in a cryogenic wind tunnel. A thin, uniform anodized aluminum layer was directly coated onto the wind tunnel models by an electrochemical process. The resulting coating has an extremely high oxygen sensitivity for very low mole fractions of oxygen in the working gas (~150ppm). Numerous types of anodized aluminum PSPs were calibrated to optimize the sensitivity and the uniformity and to prevent the aging of anodized aluminum PSP. The luminophore deposition affected the sensitivity, and the phosphoric acid modification improved the uniformity and reduced the aging. To demonstrate this technology, a flat model and a 14% thick circular arc bump model were tested in the 0.1m Transonic Cryogenic Wind Tunnel at NAL. Surface pressure distributions on the models were clearly captured.

## INTRODUCTION

Pressure-sensitive paint (PSP) measures the surface pressure distributions of wind tunnel models.

This technology is based on a photophysical phenomena known as oxygen quenching. Currently, PSP is applied to aircraft development wind tunnel testing. Using PSP, surface pressure distributions over the entire surface of a wind tunnel model can be obtained using a standard imaging camera and imaging processing techniques. However, one can say that the potential of the paint technology has not been fully exploited. One of the challenging areas to apply PSP is the use in a cryogenic wind tunnel. The idea of the cryogenic wind tunnel was developed at NASA Langley<sup>1</sup> to operate at high Reynolds number flows by lowering the working gas temperature by the continuous injection of liquid nitrogen. Hence, the working gas is practically pure nitrogen. In addition, a normal PSP cannot be used at cryogenic temperatures, since the oxygen quenching hardly occurs because of the low oxygen permeation in a normal PSP binder.

Asai<sup>2</sup> developed a new type of PSP which uses anodized aluminum as a binder. This PSP is extremely sensitive to oxygen since the luminophore is directly attached on the porous wall opened to the working gas. This new type of PSP is called anodized aluminum pressure sensitive paint (AA-PSP).

In our previous papers<sup>3,4</sup>, the surface pressure measurements in a cryogenic wind tunnel using AA-PSP were discussed. Successful results were obtained for some AA-PSPs, showing the correspondence between pressure distributions from AA-PSP and from pressure taps. However, AA-PSP has not been fully developed. Uniformity was not reliably obtained, and the luminescent intensity and the sensitivity were changed by the day (aging).

In this paper, four factors of AA-PSPs, which are the anodization process, materials, phosphoric acid modification, and aging, are considered. Experimental results from a flat model and a 14% thick circular arc bump model tests in the 0.1m Transonic Cryogenic Wind Tunnel at National Aerospace Laboratory (NAL) are also presented.

## BACKGROUND

### Theory

The relationship between the luminescent intensity and the surface pressure of the wind tunnel model can be described by the Stern-Volmer equation. The original Stern-Volmer equation is,

$$\frac{I_0}{I} = 1 + K_q [O_2] \quad (1)$$

where,  $I_0$  is the luminescent intensity without the oxygen quencher,  $I$  is the luminescent intensity, and  $K_q$  is the Stern-Volmer quenching constant.  $[O_2]$  is the oxygen concentration, which is proportional to the partial pressure of oxygen,  $p_{[O_2]}$ . In addition,  $p_{[O_2]}$  and the static pressure of the working gas,  $p$ , can be related by the mole fraction of oxygen,  $\bar{\phi}_{O_2}$ , which is a constant in the atmosphere (21%) but varies in a cryogenic wind tunnel. Equation (1) is rewritten as

$$\frac{I_0}{I} = 1 + K \bar{\phi}_{O_2} p_{[O_2]} \quad (2)$$

where  $K$  is the quenching constant with respect to  $p_{[O_2]}$ . The luminescent intensities can be related to the static gas pressures from equation (2).

One way to set the reference is to use an image with no-wind condition (wind-off condition).

However, it is impossible to obtain a wind-off condition in a cryogenic wind tunnel since the test gas

is cooled by the continuous injection of liquid nitrogen. An alternate way to set the reference is to use a low-speed condition. Taking a ratio between a low-speed condition and a wind-on condition, one can obtain the Stern-Volmer equation,

$$\frac{I_{ref}}{I} = A + B \frac{p_{[O_2]}}{p_{[O_2]ref}} \quad (3)$$

where  $A = \frac{1}{1 + K\phi_{O_2}p_{[O_2]ref}}$  and  $B = \frac{K\phi_{O_2}p_{[O_2]ref}}{1 + K\phi_{O_2}p_{[O_2]ref}}$ .

The coefficients A and B can be obtained by subjecting the PSP coating to a series of known partial pressures of oxygen.

### Anodized Aluminum PSP (AA-PSP)

Anodized aluminum PSP (AA-PSP) uses anodized aluminum as a binder, and the luminophore is directly deposited on the anodized aluminum surface. The anodized aluminum is created from aluminum by an electrochemical process known as anodization. Hence, an aluminum model surface becomes the anodized aluminum surface by anodization. Spraying is not required to coat PSP onto the wind tunnel model for AA-PSP. By the anodization technique, a uniform AA-PSP coating can be obtained.

Anodized aluminum has micropores, 20 to 100nm in diameter, distributed on the surface. Since the anodized layer grows inward to the model surface, the thickness increase of the model surface is less than the anodized layer thickness.

### *Sensitivity*

Stern-Volmer plots of AA-PSP show non-linearity, which can be fit with Freundlich isotherm,

$$\frac{I_{ref}}{I} = A + B \left( \frac{p_{[O_2]}}{p_{[O_2]ref}} \right)^{\gamma} \quad (4)$$

Since the Stern-Volmer plot is non-linear, we used the slope at  $p_{[O_2]}/p_{[O_2]ref}=1$  to represent the pressure sensitivity,  $\sigma$ , such as,

$$\sigma = \left. \frac{\Delta(I_{ref}/I)}{\Delta(p_{[O_2]}/p_{[O_2]ref})} \right|_{p_{[O_2]}/p_{[O_2]ref}=1} \quad (5)$$

### *Uniformity*

In our previous experiments, some AA-PSPs had spatial variations in Stern-Volmer constants. This means that the same calibration constants cannot be used to convert pressures from the luminescent intensity image at different spatial points. Uniformity of the calibration constants at different points on the AA-PSP model was necessary to obtain the pressure distributions.

### *Aging*

The luminescent intensity and the sensitivity were lowered by aging, which occurs to AA-PSP within one day. One day after the experiment, for example, the luminescent intensity was changed by 10% for one of the AA-PSPs in previous experiments.

## DESCRIPTION OF EXPERIMENTS

### AA-PSP Conditions

The following four factors were considered for their effect on the sensitivity, uniformity, and aging.

#### *1. Anodization Process (Pretreatment)*

The anodized aluminum layer is prepared from an aluminum surface pretreatment and anodization<sup>5</sup>. Although the pretreatment is important to prepare the anodized aluminum layer, its influence on the pressure sensitivity has not been evaluated. The pretreatment requires mechanical polishing or electrochemical polishing which dissolves the aluminum surface to remove the microscopic bumps. Mechanical polishing, electropolishing, and non-polishing were considered.

#### *2. Material (Alloy)*

Pure aluminum is usually used for anodizing aluminum, however, pure aluminum is soft and expensive to use as a wind tunnel model. The cost of aluminum alloy is much less than that of pure aluminum. For aluminum alloys, some impurities are mixed to increase the strength. However, the impurities cause pits, which are locally dissolved holes, on the anodized aluminum surface. Pure aluminum, 2024 aluminum alloy, and 5052 aluminum alloy were used for preparing AA-PSP models.

#### *3. Luminophore Deposition*

Two types of luminophore depositions, electrochemical deposition and the dipping deposition, were considered. Electrochemical deposition was used in the previous experiments. For this deposition, the AA-PSP model surface was negatively charged to attract the anionized luminophore. We developed another way to deposit luminophore called the dipping deposition. For this deposition, AA-PSP models were just dipped into a luminophore-dichloromethane solution. In both depositions, bathophen ruthenium was used as a luminophore.

#### *4. Anodized Layer Modification*

The anodized aluminum layer consists of three types of layers (Figure 1)<sup>6</sup>. We assumed that aging occurs on the anodized aluminum surface. Hence, the outer cell layer was dissolved by phosphoric acid ( $H_3PO_4$ ) to compare two different anodized aluminum surfaces. Figure 2 (a) and (b) show SEM (Scanning Electron Microscope) pictures of unmodified and  $H_3PO_4$  modified anodized aluminum surfaces. These surfaces were prepared from non-polished, pure aluminum. The micropores became wide and the outer cell layer was removed for  $H_3PO_4$  modified surface (Figure 2 (b)).

Table 1 shows a list of AA-PSP conditions employed in present experiments.

### Cryogenic Wind Tunnel Facility

To demonstrate the capability of AA-PSP to measure the surface pressures of wind tunnel models, experiments were conducted in the 0.1m Transonic Cryogenic Wind Tunnel (0.1m TCWT) at NAL<sup>7</sup>. This facility is a closed-circuit, fan-driven wind tunnel operated with cryogenic nitrogen as the working gas. The maximum stagnation pressure is 200kPa with the stagnation temperature ranging from 90K to 200K. The test section is 0.1m square and is equipped with slotted top and bottom walls of 4% porosity and solid side walls.

Figure 3 shows a schematic diagram of the experimental setup. The cryogenic wind tunnel is operated by controlling both the liquid nitrogen injection and the gaseous nitrogen exhaust. Oxygen gas was injected through a strut located just downstream of the test section. A small amount of the exhaust gas was sampled and fed into a Zirconia ( $\text{ZrO}_2$ ) oxygen sensor to monitor the mole fractions of oxygen in the flow. The Zirconia sensor was calibrated prior to each run using a standard gas with known oxygen concentration.

### Optical Equipment and Model

Figure 4 represents a schematic of the optical setup. The wind tunnel model was installed on one side of the wall of the wind tunnel test section. The optical access is gained through a 70mm diameter observation window on the opposite side of the wall. AA-PSP was excited by a Xenon light with a band pass filter ( $475\pm 50\text{nm}$ ). A dichroic mirror was used to separate the luminescence from the excitation light. The luminescence from the AA-PSP was detected by a digital camera with a cooled CCD. This camera has a 12-bit intensity resolution and  $1000 \times 1018$  spatial resolution. An infrared rejection filter (900nm) and a red long pass filter (620nm) were placed over the camera lens.

In the present experiment, two types of models, a flat model and a 14% circular arc bump model, were used. A Flat model has six removable strips, which are 5mm wide and 50mm chord, mounted on one side of the wall of the test section (Figure 5 (a)). An arc bump model is a 14% thick circular arc bump with 50mm chord with 16 static pressure taps on the centerline. Four removable 8mm wide strips are mounted in spanwise locations (Figure 5 (b)). AA-PSP was applied onto the removable strips for both models. Tap pressures were measured by an electric pressure scanner located outside the tunnel.

### Test Conditions

#### *1 Flat Model Tests*

Flat model tests were conducted prior to the arc bump model tests. The objective of this test was to optimize the sensitivity of AA-PSP, so that the pressure distributions on the wind tunnel model were not necessary. The anodization process, materials, and the luminophore deposition were considered. AA-PSP1 through AA-PSP6 is listed in Table 1. The partial pressures of oxygen on the flat model were changed by controlling the mole fractions of oxygen in the working gas ranging from 4ppm to 500ppm. The Mach number was kept at 0.40 and the stagnation temperature and the stagnation pressure were set as 100K and 190kPa, respectively.

#### *2 Arc Bump Model Tests*

14% circular arc bump models were employed to obtain the pressure distributions. A low-speed condition was taken as a reference and the Mach number of the flow was changed from 0.40 to 0.84. The mole fractions of oxygen was fixed at 150ppm, and the stagnation temperature and the stagnation pressure were kept at 100K and 190kPa, respectively.

The phosphoric acid modification was considered for uniformity and aging.

## RESULTS AND DISCUSSION

### Flat Model Tests

#### *Sensitivity*

Figure 6 shows the Stern-Volmer plots of AA-PSP1 through AA-PSP6. Each AA-PSPs has combinations of polishings, materials, and luminophore depositions. The main factor affecting the sensitivity was the luminophore deposition. The difference in materials and the difference in polishings did not change the sensitivity as much as the luminophore deposition. Taking 14Pa of the partial pressure of oxygen as a reference, the sensitivity was determined from equation (5). Higher sensitivity was obtained by the AA-PSP with the dipping deposition. The sensitivity was 0.40 to 0.53 for the AA-PSP with the dipping deposition and 0.13 with the electrochemical deposition.

#### Arc Bump Model Tests

From flat model results, non-polished, pure aluminum was used for preparing AA-PSP models. The AA-PSPs with the electrochemical deposition (AA-PSP7) and with the dipping deposition (AA-PSP8) were applied on arc bump model surfaces. To consider the uniformity and the aging, AA-PSP with the phosphoric acid modification and dipping deposition (AA-PSP9) was also applied.

#### Uniformity

Figure 7 (a) through (c) shows Stern-Volmer plots near pressure tap locations for AA-PSP7, AA-PSP8, and AA-PSP9. The partial pressure of oxygen at 14Pa was used as a reference. The partial pressures of oxygen on the model were changed by controlling the mole fractions of oxygen at Mach 0.40. It is clear that uniformity was not obtained for AA-PSP8. On the other hand, AA-PSP7 and AA-PSP9 were uniform. However, low sensitivity was obtained for AA-PSP7 because of the electrochemical deposition. Uniformity was obtained for the high sensitivity AA-PSP by using the phosphoric acid modification.

#### Pressure Distribution

We used *in situ* calibration to convert the luminescent intensity image to pressures. The calibration curves were obtained from pressure tap measurements and the luminescent intensity image at corresponding tap locations on AA-PSP. A low-speed image (Mach 0.40) was taken as a reference. Figure 8 (a) shows *in situ* calibration curves of AA-PSP7 and AA-PSP8 models at  $M=0.82$ . Linear lines could fit to all *in situ* calibration curves, which indicates that temperature effects were negligible. Since the model surface is fairly isothermal in a cryogenic flow, we can use a single calibration curve for the entire surface of the model. Using these calibration curves, pressure coefficient,  $C_p$ , distributions were obtained from luminescent intensity images.  $C_p$  distributions of AA-PSP7 model had larger noise than that of AA-PSP8 model because of lower sensitivity (Figure 8(b)).  $C_p$  distributions of AA-PSP8 model did not correspond to the pressure tap measurements because of the poor uniformity (Figure 8(c)). Both the uniformity and high sensitivity are necessary to obtain high signal to noise pressure distributions.

The Mach number was changed from 0.75 to 0.84 for AA-PSP9 model. Using the *in situ* calibration curves shown in Figure 9 (a),  $C_p$  distributions of AA-PSP9 model were obtained at different Mach numbers (Figure 9 (b) through (e)). At  $M=0.82$  and 0.84, the shock wave strength and locations were clearly identified. The main source of error comes from errors in the calibration. Other error sources, such as camera shot noise, are much smaller. The error bars were estimated from the calibration error, and shown at 20%, 50%, and 85% of the chord (Figure 9 (b) through (e)).

#### Aging

Figure 10 (a) and (b) show  $C_p$  distributions of (a) AA-PSP9 and (b) AA-PSP7 models after six days from the previous arc bump model test. It is clear that AA-PSP7, which was not modified by phosphoric acid, was totally aged. Aging was reduced by the phosphoric acid modification. This

suggests that the outer cell layer causes aging, since it was reduced by removing the outer layer.

## CONCLUSIONS

- 1) Different types of AA-PSP were evaluated. The difference in the pretreatment and the difference in aluminum materials did not affect the sensitivity. Aluminum alloys can be used to increase the strength and to reduce the cost of the model.
- 2) The luminophore deposition changed the sensitivity. The dipped deposition method gave higher sensitivity than the electrochemical deposition method.
- 3) Uniformity was improved and the aging was reduced by the phosphoric acid modification. This suggests that aging occurs at the outer cell layer of the anodized aluminum surface.
- 4) With the uniformity and high sensitivity, AA-PSP can be used as a pressure sensor in cryogenic wind tunnel tests. Using the intensity image taken at a low speed condition as a reference, surface pressure distributions over the arc bump model were obtained. The AA-PSP data agreed with pressure tap data. The pressure jump due to a shock wave was clearly identified at transonic Mach numbers.

## ACKNOWLEDGEMENTS

This work has been done as an international collaboration between Purdue University, USA, and National Aerospace Laboratory (NAL), Japan. The authors wish to thank Science and Technology Agency (STA), Japan, and the NASA Langley Research Center, USA, for their support of this work. The authors would like to thank Prof. H. Masuda at Tokyo Metropolitan University for his advice on how to prepare anodized aluminum layers, and H. Kanda at NAL for his supports in optical setups.

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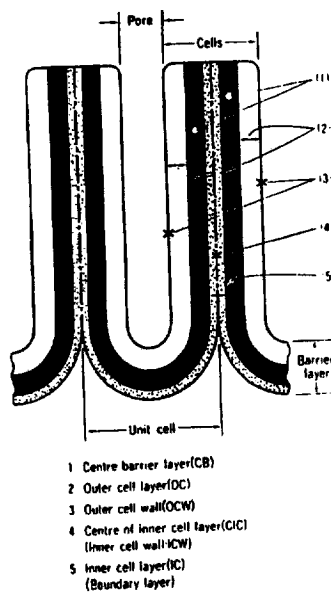


Figure 1 Composition of micropore (obtained from Wada, K.<sup>6</sup>).

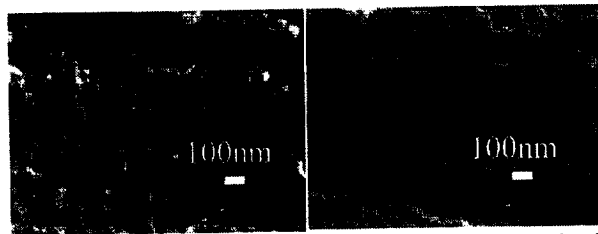


Figure 2 SEM pictures of (a) unmodified and of (b) phosphoric acid modified anodized aluminum surfaces.

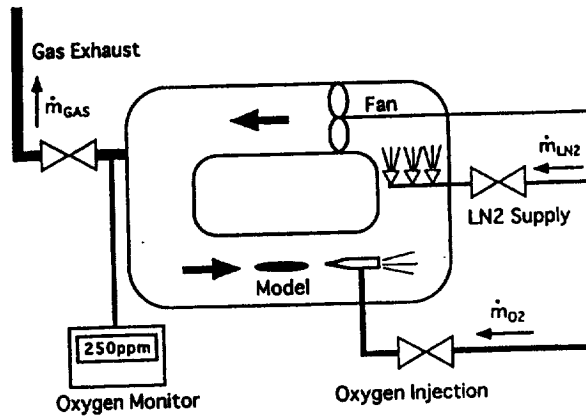


Figure 3 Schematic diagram of experimental setup in NAL 0.1m Transonic Cryogenic Wind Tunnel.

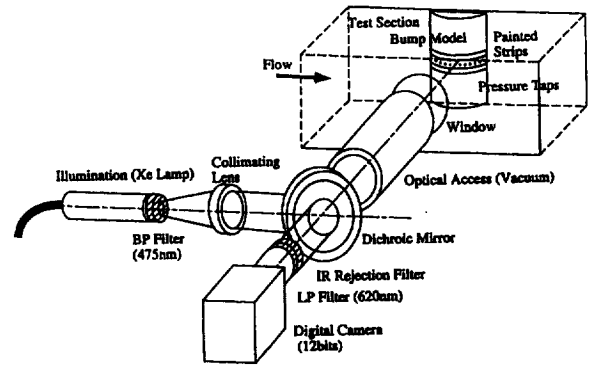


Figure 4 Schematic of optical setup in NAL 0.1m Transonic Cryogenic Wind Tunnel.

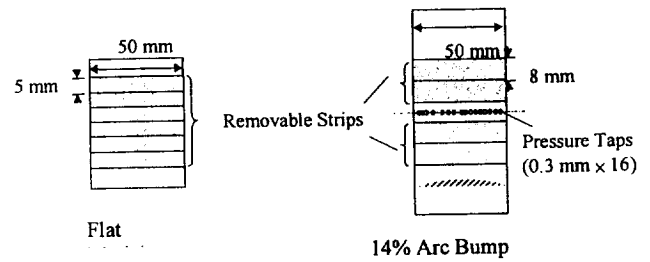


Figure 5 Schematic of (a) a flat model and (b) a 14% thick arc bump model.

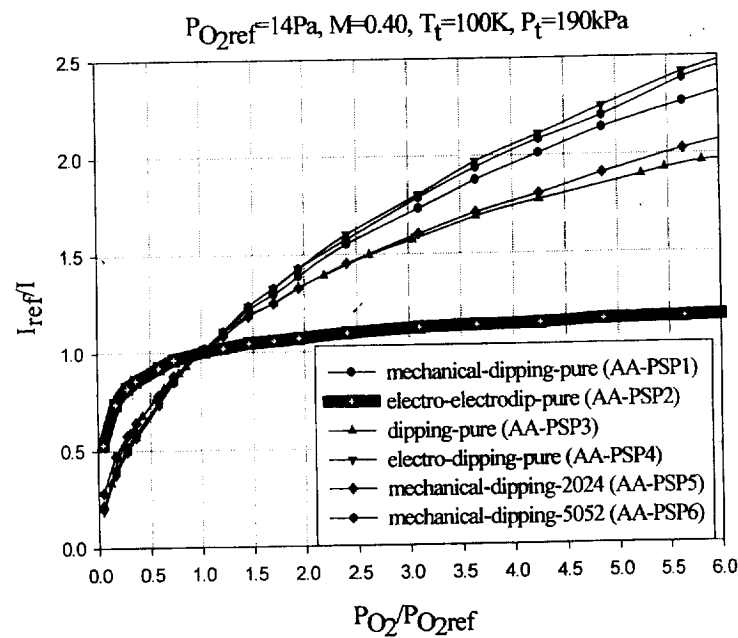


Figure 6 Stern-Volmer curves of different AA-PSPs (flat model tests).

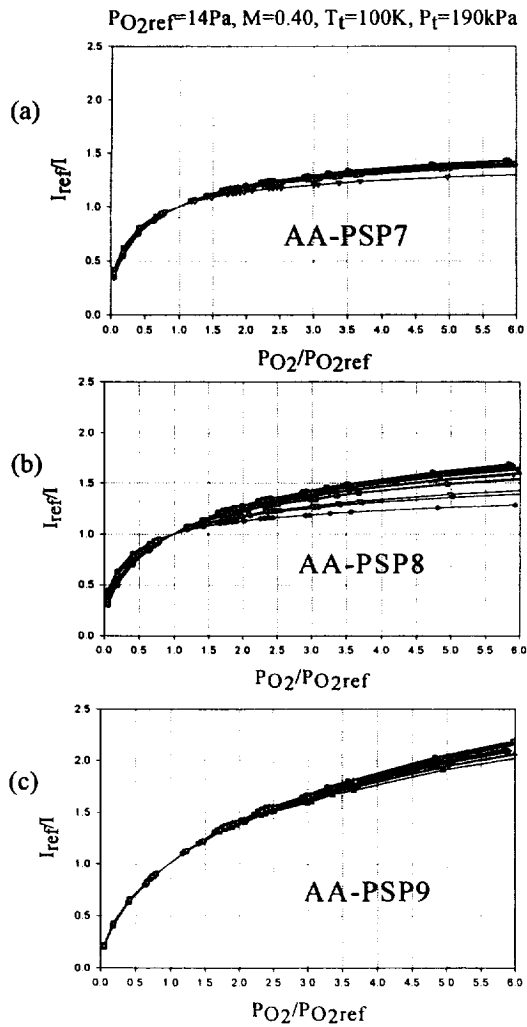


Figure 7 Stern-Volmer curves of different AA-PSPs near pressure tap locations (arc bump model tests).

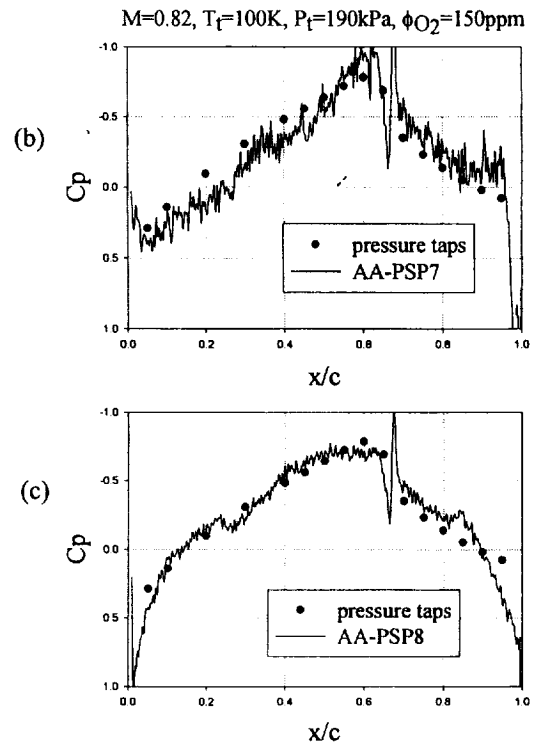
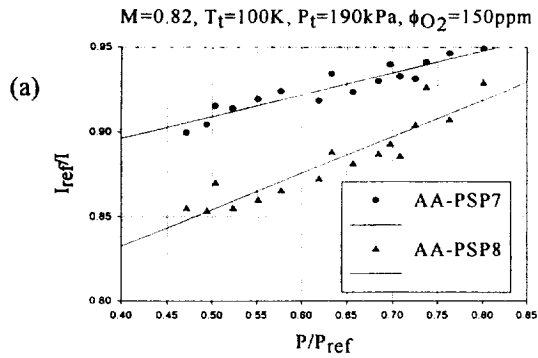
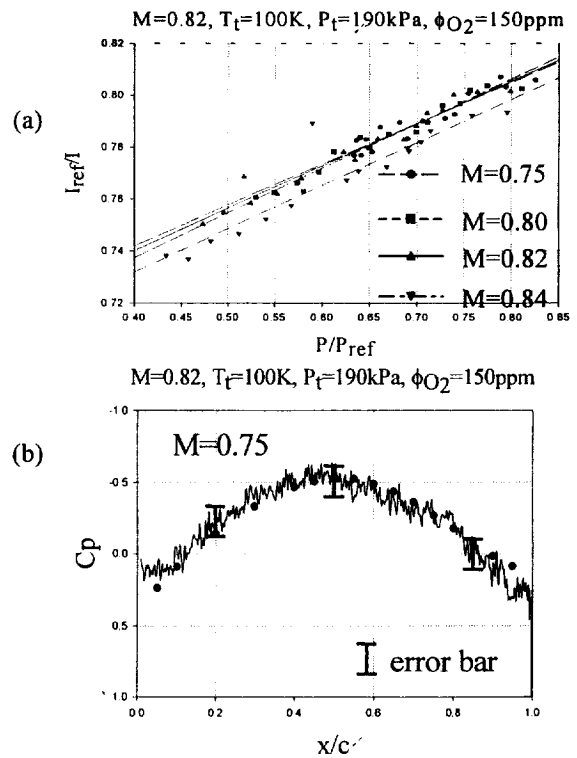


Figure 8 *in situ* calibration curves and  $C_p$  distributions for AA-PSP7 and AA-PSP8 at  $M=0.82$ .



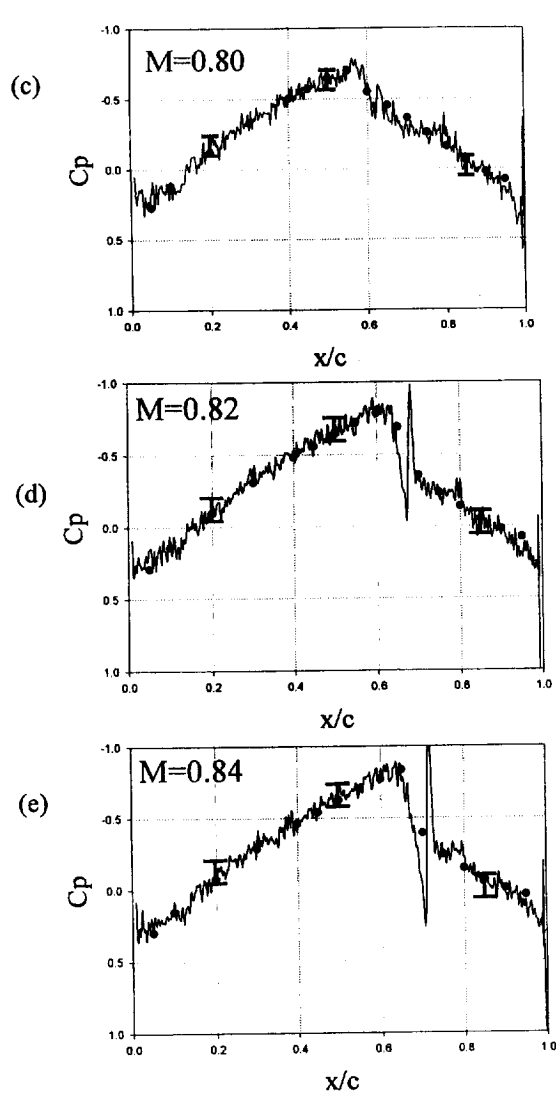


Figure 9 *in situ* calibration curves and  $C_p$  distributions of AA-PSP9 at different Mach numbers.

Table 1 Anodized Aluminum PSP conditions

| AA-PSP | Test           | Pretreatment    | Material      | Deposition      | Modification |
|--------|----------------|-----------------|---------------|-----------------|--------------|
| 1      | Flat Model     | mechanical      | pure aluminum | dipping         | no           |
| 2      | Flat Model     | electrochemical | pure aluminum | electrochemical | no           |
| 3      | Flat Model     | none            | pure aluminum | dipping         | no           |
| 4      | Flat Model     | electrochemical | pure aluminum | dipping         | no           |
| 5      | Flat Model     | mechanical      | 2024 alloy    | dipping         | no           |
| 6      | Flat Model     | mechanical      | 5052 alloy    | dipping         | no           |
| 7      | Arc Bump Model | none            | pure aluminum | electrochemical | no           |
| 8      | Arc Bump Model | none            | pure aluminum | dipping         | no           |
| 9      | Arc Bump Model | none            | pure aluminum | dipping         | yes          |

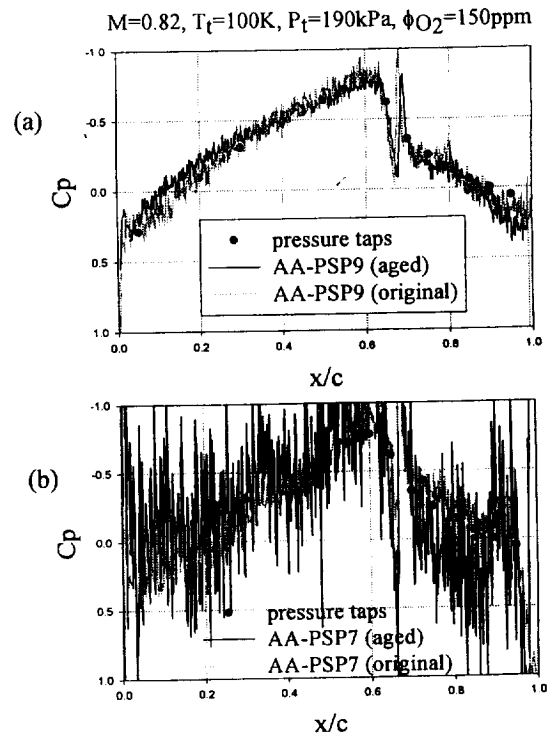


Figure 10 Aging of (a) AA-PSP9 and (b) AA-PSP7 (after 6 days in the wind tunnel).

# POROUS POLYMER/CERAMIC COMPOSITES FOR LUMINESCENCE-BASED TEMPERATURE AND PRESSURE MEASUREMENT

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## ABSTRACT

Porous Polymer/ceramic films were processed via tape casting. Upon doping with luminescent molecules such as platinum(II) octaethylporphine and [Ru(4,7-diphenyl-1,10-phenanthroline)<sub>3</sub>]Cl<sub>2</sub>, the films were used as pressure sensors, yielding a Stern-Volmer constant of A ranging from 0.02 to 0.61. These films also exhibited very fast response times (~1 ms). Tape cast films doped with Rhodamine B were used as temperature sensors under cryogenic conditions. The temperature sensitivity of the doped films increased with increasing Rhodamine B concentration.

## INTRODUCTION

Recently, luminescence-based sensors for temperature and pressure measurement have received a great deal of attention for aerodynamics applications [1-3]. These sensors, based on the phenomena of oxygen and thermal luminescence quenching, potentially provide inexpensive, non-intrusive, high resolution pressure and temperature mapping of aerodynamic model surfaces.

Pressure sensors typically consist of a luminescent molecule (luminophore) housed in a polymer binder [4]. When exposed to radiation of the proper wavelength, the luminophore will be excited to a singlet state. It may return to its ground state by emitting a photon of a longer wavelength. Certain luminophores can transfer excited state energy to a quencher molecule, such as O<sub>2</sub>, that has diffused into the sensor from the environment, causing a radiationless transition to the ground state. This phenomenon is known as oxygen quenching. The rate at which these two relaxation processes compete is dependent on the partial pressure of oxygen, with a higher oxygen pressure quenching the molecules more effectively. By filtering the excitation radiation from the emission radiation, photodetection of oxygen quenching makes pressure measurement possible. Oxygen quenching generally follows a Stern-Volmer relationship:

$$\frac{I_{ref}}{I} = A + B \left( \frac{P}{P_{ref}} \right)^{\gamma} \quad (1)$$

where A, B, and  $\gamma$  are constants.  $I_{ref}$  and  $P_{ref}$  are a reference intensity and pressure, respectively. These reference values correct for non-uniformities in excitation illumination, luminophore deposition, and photodetector sensitivity.

While polymers are mechanically robust, their effectiveness as a housing medium for luminophores is limited by material properties such as O<sub>2</sub> permeability (permeability representing the product of the diffusivity and the solubility). A low O<sub>2</sub> solubility will decrease

the sensitivity  $\left( \frac{d \left( \frac{I_{ref}}{I} \right)}{d \left( \frac{P}{P_{ref}} \right)} \right)$  of the sensor, while a low O<sub>2</sub> diffusivity will lengthen the response time

of the sensor to changes in O<sub>2</sub> pressure [1]. Several polymers have a high O<sub>2</sub> solubility:

However, most also display a low O<sub>2</sub> diffusivity, thus limiting the overall effectiveness of the sensor.

If a luminophore could be adsorbed or bonded to a porous surface, it would produce a sensor that would have a very fast response time to changes in oxygen pressure. Porous polymer membranes are commercially available, but are costly to apply for large-scale wind tunnel tests. Ceramic films provide a low cost alternative; however, due to challenges in processing ceramic films to conform to surfaces for aerodynamic testing, as well as their inherent brittle behavior, ceramics have yet to find widespread use as luminophore housings for luminescent pressure sensors.

Tape casting is a widely used process for preparing ceramic substrates for electronic packaging [6]. Prior to firing, tape cast films are composed of ceramic powder held together with a polymeric binder. Tape cast films are good candidates to house luminophores for luminescent pressure sensors. The films are porous, which may shorten response time, yet they are mechanically robust due the polymer, facilitating handling, and providing a film that will withstand the stresses of aerodynamic testing.

Tape casting may also be used to process luminescent temperature sensors by using luminophores that are sensitive to their thermal environment. The luminophore is again excited by absorption of a photon. The excited molecule deactivates through the emission of a photon. A rise in temperature of the luminescent molecule will increase the probability that the molecule will return to the ground state by a vibrational (radiationless) process. This is known as thermal quenching, and may be expressed in functional form as:

$$\frac{I(T)}{I(T_{ref})} = F(T/T_{ref}) \quad (2)$$

where  $F(T/T_{ref})$  is an empirical expression that may be a polynomial, or another function best fitting the experimental data.

While there are several effective temperature sensors near room temperature, few luminophores have exhibited temperature sensitivity at cryogenic temperatures (120-200 K) [1,5]. The sensors currently used exhibit sensitivity over only a small temperature range, making tests in cryogenic wind tunnels more difficult [5].

## EXPERIMENTAL PROCEDURE

Ceramic/polymer composite films were processed from an aqueous suspension of ceramic powder via tape casting. The suspension was prepared by dispersing Al<sub>2</sub>O<sub>3</sub> (Reynolds Aluminum Co., specific surface area=8.5 m<sup>2</sup>/g) in water (83 wt% Al<sub>2</sub>O<sub>3</sub>) using a polyelectrolyte surfactant (D-3021, Rohm & Haas). The suspension was ball-milled for one hour to eliminate agglomerates, and subsequently mixed with 7.5 wt% (relative to the suspension) of a poly(acrylic) binder emulsion (B-1035, Rohm & Haas). The suspension was cast onto a silicone-coated Mylar<sup>TM</sup> sheet (Richard E. Mistler, Inc.) using a doctor blade to form films ranging in thickness from 0.1-0.2 mm.

Two different luminophores were used in this study, platinum(II) octaethylporphine (PtOEP) (Porphyrin Products) dissolved in toluene, and [Ru(4,7-diphenyl-1,10-phenanthroline)<sub>3</sub>]Cl<sub>2</sub> (Ru(dpp)Cl<sub>2</sub>) (GFS Chem.) dissolved in methanol. Tape cast coupon samples were dipped into the luminophore solutions, and subsequently dried in air. The individual components of the tape cast composites were also prepared for calibration. The polymeric binder was cast onto Mylar<sup>TM</sup> via a doctor blade technique and allowed to dry. Coupons were again cut and dipped into the two luminophore solutions. The Al<sub>2</sub>O<sub>3</sub> powder was pressed in a die at 5000 psi, and the resulting porous powder compact was dipped into the luminophore solutions and dried in air.

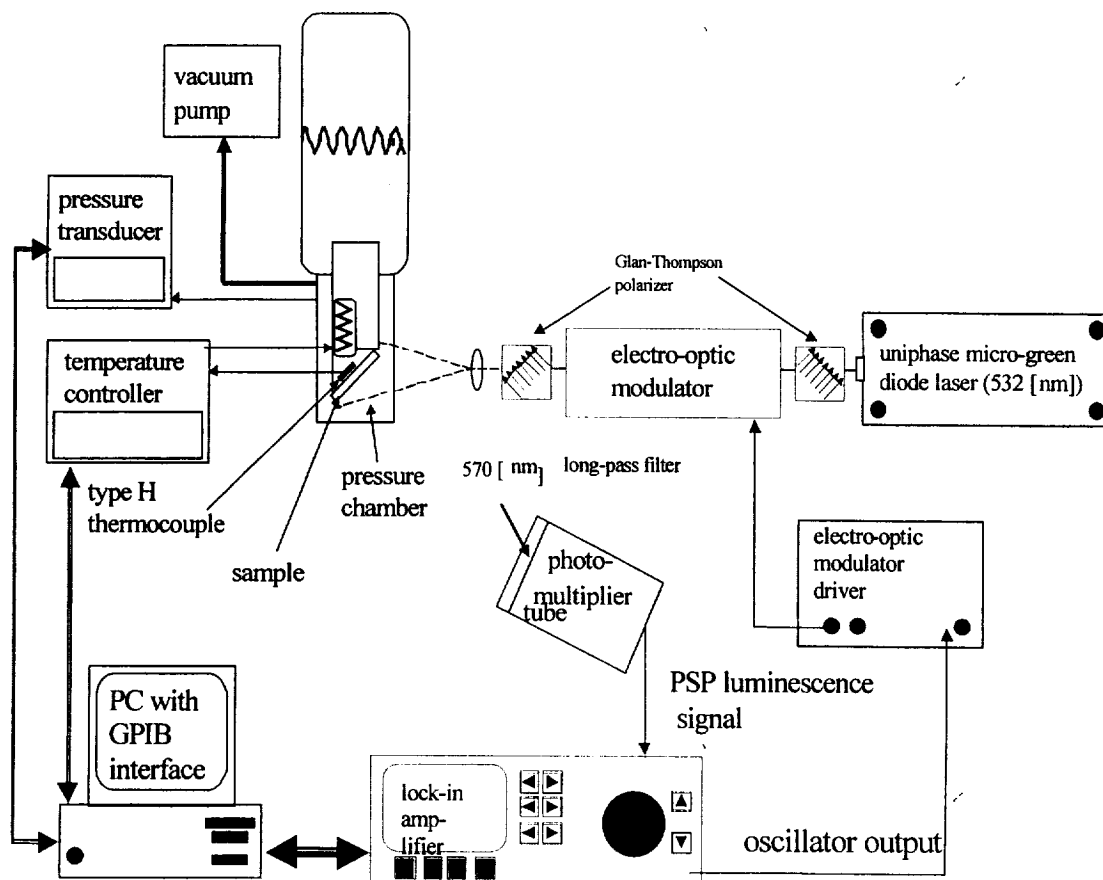


Figure 1. Apparatus used for pressure calibrations.

For the temperature sensors, tape cast coupons were dipped into solutions of Rhodamine B (RhB) (Aldrich) dissolved in methanol, and subsequently dried in air. To vary the amount of RhB in a given sample, coupons were prepared using RhB solution concentrations ranging from  $2.09 \times 10^{-4}$  to 0.02 molar.

The experimental apparatus used to calibrate the pressure sensors is shown in Figure 1. The sample is enclosed in a test chamber with optical access, and the chamber pressure is controlled by a vacuum pump and monitored by an absolute pressure gauge. Dry air (21%  $O_2$ ) of varying absolute pressure is fed into the chamber, and the partial pressure of oxygen in the calibration chamber is determined by combining the pressure measurement from the absolute pressure gauge and the test gas composition.

Measurements of the pressure sensor's luminescent intensity were made using phase sensitive detection. The sample was illuminated with 532 nm radiation from a 50 mW Uniphase Micro-Green diode laser. The laser radiation was passed through an electro-optic modulator which was driven by a sinusoidal reference from a lock-in amplifier resulting in a modulated illumination signal for the sample. The luminescent signal from the sample was collected through a 570 nm long pass filter onto a photo-multiplier tube. The photo-multiplier tube signal was demodulated by the lock-in amplifier using a 1-second integration time. The bandwidth narrowing characteristics of the phase sensitive detection scheme resulted in improved signal to noise ratio, and improved accuracy in the sensor calibrations. The entire calibration process was controlled by a LabView<sup>TM</sup>-based data acquisition program on a personal computer.

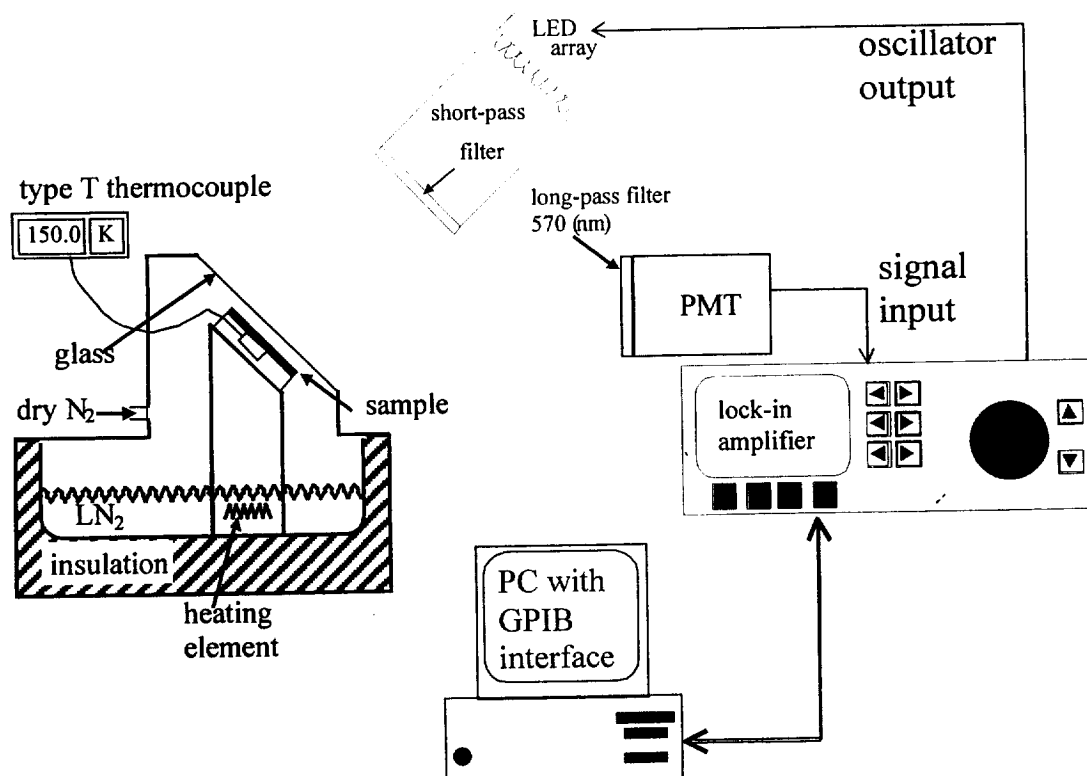


Figure 2. Apparatus used for temperature sensor calibrations.

The experimental apparatus used to calibrate the temperature sensors in the cryogenic range is shown in Figure 2. The temperature sensor was placed on a copper rod rising from a liquid nitrogen bath. A type T thermocouple was placed between the sensor and the copper rod. Good thermal contact between the sensor, thermocouple, and copper rod was ensured by the use of thermal grease. The sensor and bath were enclosed in a small chamber allowing optical access through a single window. Dry nitrogen was bled through the enclosure to prevent water from condensing on the paint sample. Accurate measurements of the luminescent intensity of the sensor were accomplished using phase sensitive detection. The sensor was excited with sinusoidally modulated illumination from a green LED array. The luminescent signal from the sensor was collected through a 570 nm long pass filter onto a photo-multiplier tube. The photo-multiplier tube signal was again demodulated by the lock-in amplifier with a 1-second integration time.

## RESULTS AND DISCUSSION

The tape cast films exhibited excellent mechanical properties. They were flexible and scratch resistant. They have successfully withstood the stresses that are seen in sonic jet impingement experiments, wind tunnel tests, and flight tests for *in-situ* pressure measurements.

Stern-Volmer plots for tape cast films doped with either the PtOEP or Ru(dpp)Cl<sub>2</sub> are shown in Figure 3. Films doped with PtOEP exhibited greater pressure sensitivity (larger slope) compared to films doped with Ru(dpp)Cl<sub>2</sub>. When the luminophores were housed in the binder alone, they exhibited the same behavior as the tape cast film. However, the pressure sensitivity of luminophores housed in Al<sub>2</sub>O<sub>3</sub> powder compacts differed significantly from the tape cast

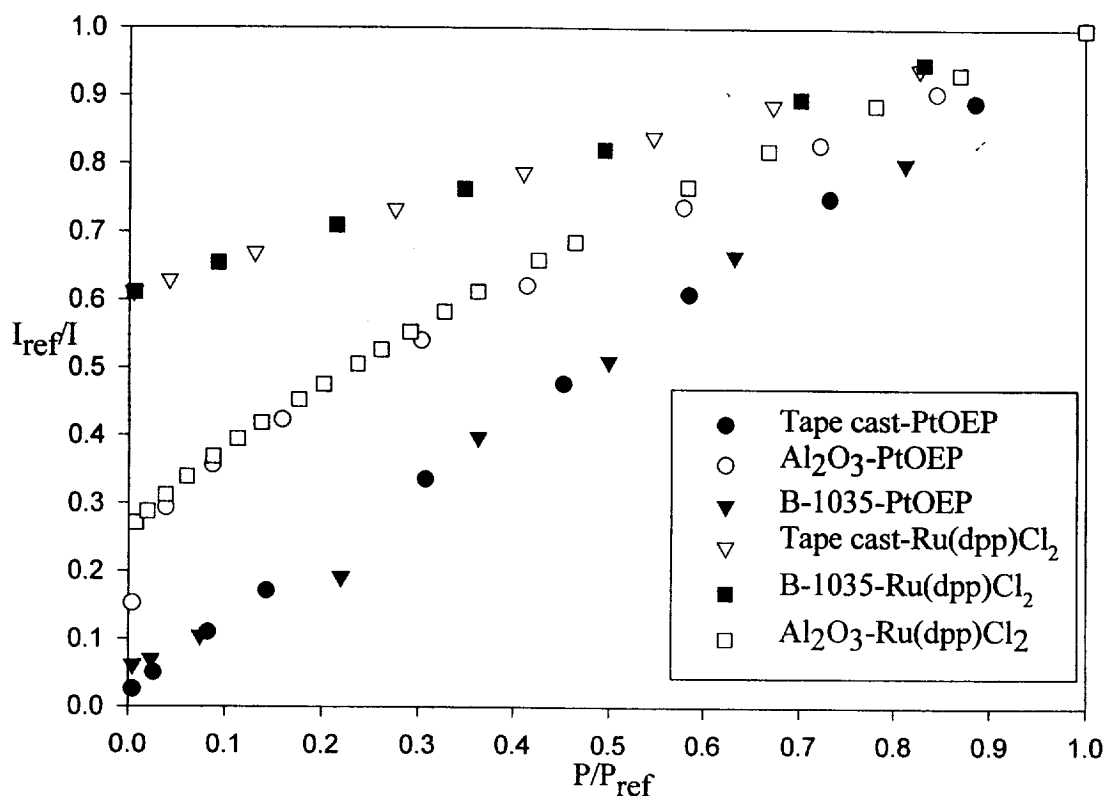


Figure 3. Stern-Volmer data for tape cast components and films doped with different luminophores.

films. When housed in  $Al_2O_3$  powder compacts, PtOEP and  $Ru(dpp)Cl_2$  exhibited similar pressure sensitivity. Compared to the powder compact with the same luminophore, the PtOEP tape cast film exhibited a greater pressure sensitivity, while the  $Ru(dpp)Cl_2$  tape cast film had a lower pressure sensitivity. This implies that the polymer plays a dominant role in determining the pressure sensitivity characteristics of the tape cast films. Preliminary measurements indicated that the tape cast films exhibited response times on the order of 1 ms. Microtomed cross sections of the tape cast films showed that there is a continuous interconnecting network of pore channels throughout the film. This may account for the observed rapid response times, because the porosity provides a fast diffusion path for oxygen.

Tape cast temperature sensors of varying RhB concentration were calibrated over a broad range of cryogenic temperatures (Fig. 4). At low RhB concentrations, the films were nearly insensitive to temperature variations, while at higher concentrations, the films showed good temperature sensitivity. However, the luminescent intensity of the sensor decreased both with increasing temperature due to more available vibrational modes for radiationless deactivation, and with increasing RhB concentration due to self-quenching effects. A larger luminescent intensity facilitates data acquisition by increasing photodetection efficiency. Therefore, the effective range of a temperature sensor depends on both the temperature sensitivity and the luminescent intensity. The film with intermediate RhB concentration exhibited an effective operating range of 130-260 K while the higher concentration had a range of 130-210 K. While the temperature sensitivity of the intermediate concentration was less than that of the highest concentration sensor, it still exhibited sufficient thermal quenching for data acquisition purposes.



**CRYOGENIC TEMPERATURE- AND PRESSURE-  
SENSITIVE FLUORESCENT PAINTS**

**A Thesis  
Submitted to the Faculty  
of  
Purdue University  
by  
Richard German Erausquin Jr.**

**In Partial Fulfillment of the  
Requirements for the Degree  
of  
Master of Science in Aeronautics and Astronautics**

**December 1998**

To my wonderful wife, Heather.  
Her willingness to assume the greater burdens of family  
and work have enabled the achievement of this goal.  
Words alone cannot convey my appreciation for the  
patience and love she has shown over the years.

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## ABSTRACT

Erausquin, Richard G. Jr. M.S.A.A., Purdue University, December 1998. Cryogenic Temperature- and Pressure- Sensitive Fluorescent Paints. Major Professor: John P. Sullivan.

The use of pressure- and temperature-sensitive fluorescent paints to make aerodynamic measurements has been well documented. The present work describes the extension of that research into the realm of cryogenic wind tunnel testing. Cryogenic wind tunnels are capable of simulating in-flight transonic Reynolds Numbers by lowering the operating temperature of the working gas to near liquid nitrogen temperatures. While this process enables testing in a dynamically similar flow, there are inherent difficulties in obtaining measurements. The use of pressure- and temperature-sensitive paints in cryogenic wind tunnels offers better economics and simplicity in measurement. The objective of this research is the development of pressure- and temperature-sensitive paints that function under the conditions experienced in a cryogenic wind tunnel. The problems associated with the extension of paint technology into the cryogenic realm are discussed and methods for preparing different coatings examined. These coating preparation methods include increasing pressure-paint layer porosity using previously untried methods of surface depositing luminescent molecules that alleviate poor diffusivity at cryogenic conditions. Issues associated with molecular properties and the ability to change those properties in an effort to design temperature-sensitive paints that respond with better sensitivity over specific temperature ranges are investigated. Apparatus for conducting cryogenic calibrations of pressure- and temperature-sensitive paints are described and calibrations conducted. Results of these calibrations show temperature response can be slightly affected by molecular design of luminescent molecules and that paint layers can be created that show sensitivity to oxygen concentration in the low temperature and low oxygen conditions found in cryogenic wind tunnels.

## CHAPTER 1: INTRODUCTION

In recent years, temperature-sensitive paints (TSP's) and pressure-sensitive paints (PSP's) have attracted much attention in the aerospace community. These paints are commonly composed of a luminescent compound and a binder. A luminescent compound is one that adsorbs radiative energy (light) of a particular wavelength and emits light of a slightly longer wavelength. Through the photophysical phenomena of thermal and oxygen quenching of luminescence, emission intensity of the paint can be related to temperature and pressure. Hence from the detected luminescence intensity, temperature or pressure on the painted surface can be determined. In general, emission intensity increases with decreasing temperature and decreasing oxygen concentration.

Currently, TSP's and PSP's are being applied to aircraft development and wind tunnel testing. Much success in obtaining temperature and pressure maps on wind tunnel model surfaces has been documented. These paints can be used to generate high-resolution temperature and pressure maps, detect boundary layer transition, and examine shock/boundary layer interactions.

Temperature measurements on wind tunnel models can sometimes incorporate a large number of thermocouples or similar measurement devices. These are complex systems that are expensive to instrument and do not yield continuous temperature distributions. On the other hand, temperature-sensitive paint measurements are fairly simple, inexpensive, and can yield full surface temperature maps.

Pressure-sensitive paints similarly offer several advantages over traditional methods of measuring pressure distributions on wind tunnel models. Pressure taps are complex and expensive (~\$200 per tap) to install on wind tunnel models, cannot give continuous pressure distributions, and aerodynamics and structural dynamics of the model can be seriously altered by the modifications required for pressure tap installation. Using PSP's alleviates all of these concerns. The continuous distributions obtained from PSP's allow for better comparisons with computational results and data rates are much higher than conventional techniques which increases efficiency of wind tunnel usage.

One recent, and very challenging, extension of the paint technology has been its application in cryogenic wind tunnel testing. Cryogenic wind tunnel technology was developed at NASA Langley as a means of simulating high Reynolds number flows. By cooling the wind tunnel test gas to near liquid nitrogen ( $\text{LN}_2$ ) temperature, significant increases in Reynolds number can be obtained. Full-scale flight Reynolds numbers have been obtained with sub-scale models in cryogenic wind tunnel facilities such as the National Transonic Facility (NTF), European Transonic Wind Tunnel Facility (ETW), and the 0.1-m Transonic Cryogenic Wind Tunnel at The National Aerospace Laboratory (NAL) in Japan. Typically, these wind tunnels operate at temperatures in the range of 90 to 180 K. Naturally, these types of facilities are expensive to operate and the conditions limit tunnel access. Cryogenic TSP's and PSP's require limited access and less tunnel operating time, thus reducing the cost. Like room temperature paints, they are also easier to implement than current techniques.

There are many challenges in the development of cryogenic TSP's and PSP's. The environment is very harsh, thus adversely affecting the coating. The extremely low temperatures have been observed to severely decrease diffusion of oxygen into the commonly used polymer binders for PSP's. Brittleness of the binder also becomes a major concern at these temperatures because any cracking or flaking of the binder would destroy the coating. In addition, most work with TSP's has concentrated on temperatures near room temperature. Compounds that are temperature sensitive under cryogenic conditions are difficult to obtain. Another concern with cryogenic PSP's is the need for molecular oxygen in the working gas to serve as a quencher. The problem that arises is that since the working gas in a cryogenic wind tunnel is pure nitrogen, oxygen needs to be added to the flow. Injecting large amounts of oxygen is, however, not permissible from the standpoints of safety and cost. Thus, only small concentrations of oxygen are allowed to exist in the working gas, yielding a necessity for highly sensitive PSP coatings.

Once a coating has been found to respond to temperature or pressure it must be calibrated to obtain a relation between emission intensity and temperature or pressure. Under room temperature conditions, this is a fairly straightforward process. Calibrations

under cryogenic conditions, however, require the use of specialized test stands designed specifically for that purpose. The design of such test stands, calibration methods, and calibration results for cryogenic TSP's and PSP's are presented herein.

Another interesting aspect of the luminescent molecules is that recent photophysical theory has suggested that temperature response can be affected by the molecular structure itself. Through modification of currently utilized luminescent molecules, the region of temperature over which the luminophore shows a response can be changed. It has also been postulated that the sensitivity can also be affected. Attempts have been made to create temperature sensitive molecules that exhibit a response over a specific region of temperature with a high sensitivity.

## CHAPTER 2: LITERATURE REVIEW

Thermal and oxygen quenching of luminescence has been observed since as early as 1931<sup>1</sup>, however it has not been until the past two decades that luminescent molecules have seen widespread use as temperature and oxygen sensors. Two driving forces in the development of these sensors have been the areas of biosensing and aerodynamics.

In the realm of biosensing, much effort has been made in the area of luminescent oxygen sensors. Papkovsky<sup>2</sup> created a prototype fiber-optic intensity-based oxygen sensor using a derivative of PtOEP. Shriver-Lake, et. al.<sup>3</sup> adapted a biosensor to utilize dyes excited above 600 nm and coupled easily to proteins to enable easy detection of blood toxins. A low cost instrument based on light-emitting diodes and photodiodes was created by Trettnak, et. al.<sup>4</sup> Another interesting quality of Trettnak's device was that the flow-through cell was thermally stabilized to alleviate temperature effects on the luminescent molecules. In the ultimate application, Poole et. al.<sup>5</sup> demonstrated the measurement of microvascular plasma  $P_{O_2}$  in vivo in a rat's costal diaphragm. While many of these sensors use intensity-based methods, biomedical researchers have also investigated fluorescence lifetime or phase based methods of making oxygen measurements. Szmecinski and Lackowicz<sup>6</sup> describe their method for externally modulating excitation light sources to enable measurements based on lifetime methods. Lifetime and phase methods in biosensing have also been investigated by Holst et. al.<sup>7</sup> and Keeffe et. al.<sup>8</sup> Another interesting aspect of Keeffe's work was that the luminescent molecule was immobilized in a Sol-gel matrix, a previously untried binder in aerodynamics circles. Another interesting investigation of binder effects from the biosensing community is the work of He et. al.<sup>9</sup> In this work, He examines the effects of entrapping a Ruthenium based complex in a silicone polymer binder.

Much of the early success of luminescent paints in aerodynamics came from temperature-sensitive paints. Campbell, et. al.<sup>10</sup> calibrated many aromatic hydrocarbon and transition metal based TSP's. The calibrated paints were then used to perform steady state and unsteady heat transfer measurements on subsonic, supersonic, and hypersonic models. Heat transfer in a shock-turbulent boundary layer interaction, heat transfer on a



wall shear flow, and heat transfer of an excited circular impinging jet were measured using temperature-sensitive paints by Liu<sup>11</sup>. More recently, work by Shen and Schanze<sup>12</sup> has focused on the actual synthesis of new temperature-sensitive paints that can be designed to respond over certain regions of temperature by choice of ligand structure.

Pressure-sensitive paints have been used in numerous aerodynamic measurements. Kavandi, et. al.<sup>13</sup> conducted measurements on a 2-D NACA 0012 airfoil. McDonnell Douglas conducted tests on a generic wing/body model at Mach 2, a Mach 1.2 high performance fighter, and a converging-diverging nozzle<sup>14</sup>. McDonnell Douglas<sup>15</sup> and Torgerson<sup>16</sup> (of Purdue University) have also made efforts at PSP measurements in low speed flows. In a very challenging extension of the technique, pressure measurements on the fan blades of rotating machinery have been made using PSP's by Burns<sup>17</sup> and Torgerson<sup>16</sup>. An excellent review of both TSP's and PSP's is given by Liu, et. al.<sup>24</sup>

To date, very little work has been done in implementing TSP's and PSP's under cryogenic conditions. Campbell<sup>10</sup> calibrated many different compounds and discovered a number of excellent TSP's that function in the cryogenic range. Cryogenic TSP's were used by Asai, et. al. to detect boundary-layer transition in a cryogenic wind tunnel over a temperature range of 90 to 150 K in both subsonic and transonic flows<sup>18</sup>. In cooperation with this research, Asai et. al. produced and tested a new coating technique for obtaining PSP measurements in a cryogenic wind tunnel<sup>19</sup>. Using this new coating, accurate resolution of the pressure distribution on a circular arc bump model was accomplished. Oglesby et. al. have also conducted cryogenic PSP experiments with this new type of coating and have noted marked divergence from traditional linear Stern-Volmer response<sup>20</sup>. It should be noted that non-linear Stern-Volmer responses have been noted for various paints containing  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$ <sup>21</sup> and Platinum Porphyrin complexes<sup>22</sup>. These PSP's exhibit a downward curve in the Stern-Volmer response at lower oxygen concentrations, thus exhibiting higher sensitivity at these low partial pressures. As previously noted, this is desirable in the low oxygen environment of a cryogenic wind tunnel.

### CHAPTER 3: THEORY

The photophysical processes behind the behavior of TSP's and PSP's have been thoroughly presented in literature, but will be covered for completeness. On the macro scale, a luminescent molecule is embedded in a polymer binder and placed on the surface to be measured. Absorbing a photon of light of a particular wavelength excites the luminescent molecules. In the process of returning to the ground state, the luminescent molecules emit photons of Stokes shifted light. The general term for the emitted light is luminescence. This process is depicted below in Figure 3.1, and a typical absorption and emission spectra is shown in Figure 3.2.

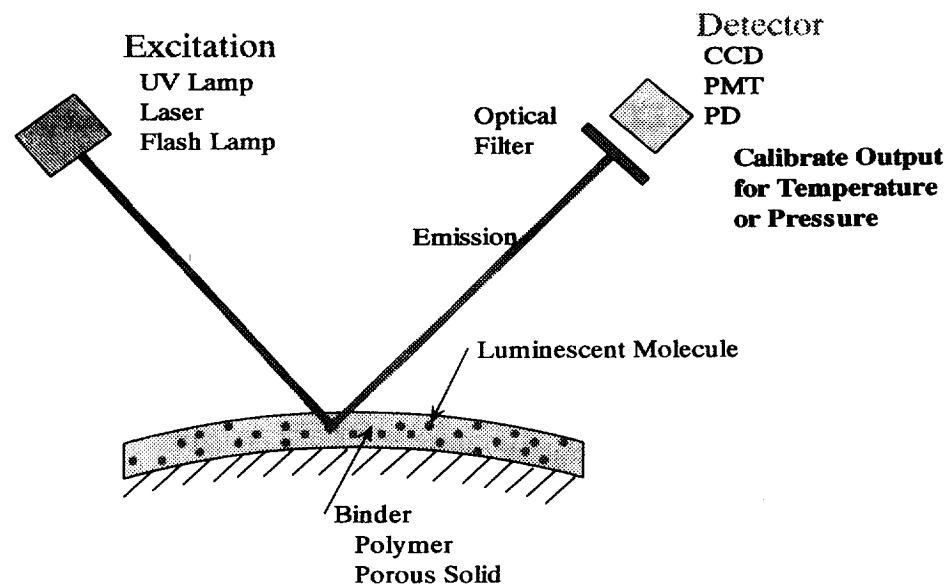


Figure 3.1: Luminescent Paint Layer

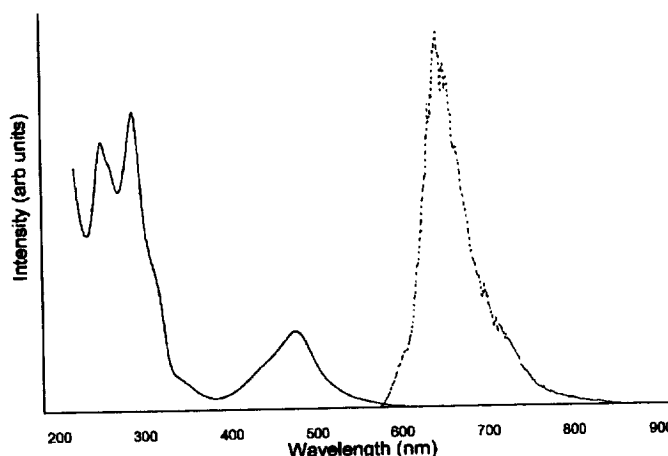


Figure 3.2: Absorption and Emission Spectrum for  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$

### 3.1 Electrochemical Theory

On a molecular scale, once the photon is adsorbed, an electron jumps from the singlet ground state  $S_0$  to the excited state  $S_i$  ( $i > 1$ ). Within picoseconds, the excited state relaxes to the lowest excited singlet state  $S_1$  through radiationless internal conversion. There is a small possibility that an intersystem crossing from  $S_1$  to the  $T_1$  triplet state may occur at this point, otherwise the electron remains in the  $S_1$  state for a short period of time. Once the electron is in either the lowest excited singlet or triplet state, the remaining excess energy must be dissipated in order for the electron to transition back to the ground state  $S_0$ . It is at this point, where a distinction is drawn as to what process happens next: fluorescence, phosphorescence, or radiationless deactivation (quenching). All of these processes are illustrated below in Figure 3.3.

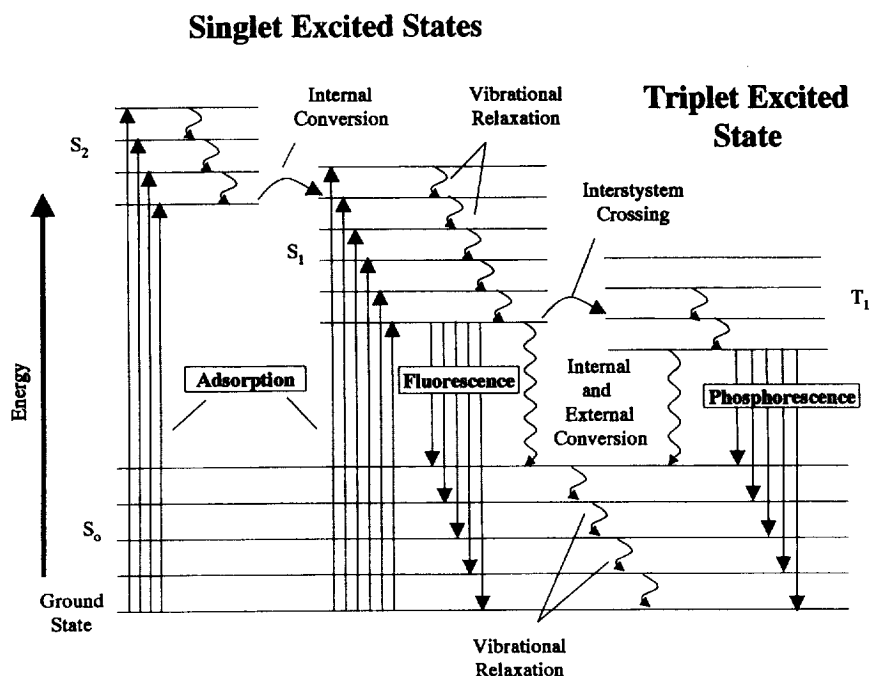


Figure 3.3: Energy Level Diagram

Electrons remaining in the  $S_1$  excited state can do so for only a short period of time. In order to relax to the singlet ground state, the excess energy must be dissipated. This is accomplished through the emission of a photon of light of a longer wavelength than the excitation light. The emission of a photon during a transition from  $S_1$  to  $S_0$  is called fluorescence. The other method of transitioning from  $S_1$  to  $S_0$  is through internal or external conversion, commonly known as quenching. When a molecule is quenched, the  $S_1$  to  $S_0$  transition occurs without the emission of a photon of light.

If an intersystem crossing from the first singlet excited state to the first triplet excited state occurs prior to relaxation to the ground state, a slightly different process takes place. As with transitions from the first singlet excited state, energy is dissipated through the emission of a photon of light of a longer wavelength than the excitation light, or through a radiationless deactivation process. The light emitted in the  $T_1$  to  $S_0$  transition is called phosphorescence. The difference between fluorescence and phosphorescence comes from the fact that transitions into the triplet excited state involve a spin flip of the electron. Phosphorescence occurs much less than fluorescence because the transition

from the excited triplet state to the ground singlet state is spin forbidden according to the Pauli Principle and thus exhibits a longer lifetime than a singlet excitation. It should be noted that second- and third-row transition metals exhibit a spin-orbit coupling where effects of the heavy metal atom can lead to a loss of distinction between singlet and triplet states.<sup>23</sup> In TSP's and PSP's the radiationless deactivation processes are of interest. Radiationless deactivation, or quenching, can occur through thermal or oxygen quenching of the molecule.

### 3.1.1 Molecular Structure

The luminophores used in this research are based on second and third row transition metals. A metal atom is bonded to a ligand molecule. The ligand is a molecule based on benzene structures. The structure of the bond between the metal and ligand is a major factor in determining temperature sensitivity. As an example of one of these atoms, a 2-D figure of the [Ru(trpy)] molecule is shown below. In three dimensions another trpy ligand molecule is bonded to the Ru opposite and perpendicularly out of plane with the trpy ligand shown below.

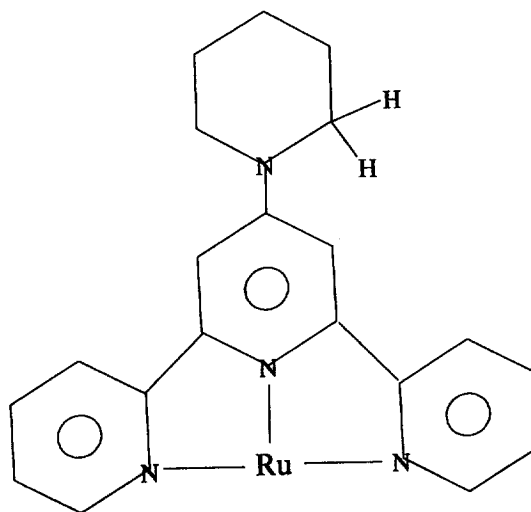


Figure 3.4: Structure of the [Ru(trpy)] molecule

An anion is added to neutralize the charge of the luminescent molecule. Anion quenching has been noted in some molecules, however it does not exhibit a large effect. The size of the anion used determines the solubility of the luminescent molecule and thus effects the kind of solvent used or whether or not the molecule dissolves directly into certain polymer binders.

### 3.1.2 Thermal Quenching

Thermal quenching of luminescence is based on the metal-to-ligand bond as mentioned in Section 3.1.1. At higher temperatures, the metal-to-ligand bond begins to elongate and shrink in a spring-like fashion. As temperature increases, more energy is lost to this vibration. Statistically, a system containing molecules experiencing energy loss due to this vibration can be modeled using Boltzman statistics. Figure 3.5 below shows the model used to describe a molecule's entry into the theoretical quenching state.

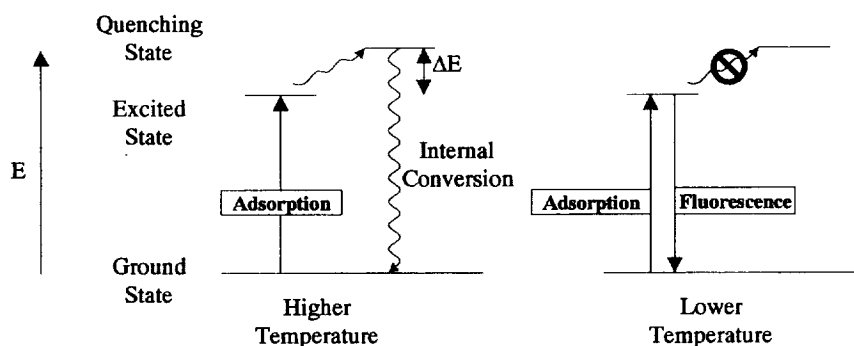


Figure 3.5: Quenching State Model

At higher temperatures, enough excess energy exists to allow some of the molecules to transition into the quenching state. Once in the quenching state, the molecule goes through a non-radiative internal conversion to return to the ground state. At lower temperatures, not enough excess energy exists to enter the quenching state thus the molecule must transition to the ground state by emitting excess energy in the form of a

photon of light (fluorescence). It is the Boltzman statistics that describe the rate constant  $k_D$ , used in Section 3.2.

From this discussion, it should be apparent that the properties of the metal-to-ligand bond have a large effect on rate parameters. These effects are controlled by the type of bond and bond angle. Stronger bonds allow for less rigidity, thus adversely effecting vibrations between the metal and ligand. Bond angle effects the distribution of molecular orbitals, thus effecting the energy gap,  $E$ , between the excited state and quenching state.

### 3.1.3 Oxygen Quenching

Oxygen quenching of luminescence is an entirely separate process from thermal quenching. The unexcited valence electrons in an  $O_2$  molecule naturally exist in the degenerate triplet state. When two electrons inhabit a degenerate triplet state in a molecule they have the same spin. When an  $O_2$  molecule in the triplet state comes in close proximity to an excited luminescent molecule in the triplet state (see 3.1), the electrons of opposite spin undergo a simultaneous transfer between the  $O_2$  molecule and the luminophore. This process returns the luminophore to the ground state, thus quenching the fluorescence, and returns the oxygen molecule to the singlet state.

It should be noted that singlet  $O_2$  is very reactive and may cause a destructive reaction with nearby luminescent molecules. This is the cause of photodegradation in pressure-sensitive paints (see 7.1.1 for a complete discussion). Metal porphyrin complexes like PtOEP are very susceptible to reactions with singlet  $O_2$ , transition metals are not as likely to react.

## 3.2 Quantitative Theory

The entire photophysical process is best quantified through the quantum yield (quantum efficiency) of luminescence  $\Phi$ .

$$\Phi = \frac{\text{rate of luminescence emission}}{\text{rate of excitation}} = \frac{I}{I_a} \quad (3.1)$$

where  $I$  is the luminescence intensity and  $I_a$  is the adsorption intensity. In the steady-state condition, the quantum yield in the presence of the quencher,  $[O_2]$ , is given by the following model:

$$\Phi = \frac{I}{I_a} = \frac{k_L}{k_L + k_D + k_Q [O_2]} = k_L \tau \quad (3.2)$$

where  $k_L$  is the rate constant for luminescence emission,  $k_D$  is the rate constant for deactivation and is temperature dependent,  $k_Q$  is the rate constant for quenching,  $[O_2]$  is the local concentration of oxygen, and  $\tau$  is the lifetime of the excited molecule, given by:

$$\tau = 1/(k_L + k_D + k_Q [O_2]) \quad (3.3)$$

Thus the process of thermal quenching affects quantum yield through  $k_D$ , and oxygen quenching affects quantum yield through the dependence on  $[O_2]$  and  $k_Q$ . Dividing (3.2) by the maximum luminescence intensity  $I_o$  at  $[O_2]=0$  yields the Stern-Volmer equation:

$$\frac{I_o}{I} = 1 + k_Q \tau_o [O_2] = 1 + K_Q [O_2] \quad (3.4)$$

where  $\tau_o$  is simply the rate constant at  $[O_2]=0$  and  $K_Q$  is the product of  $k_Q$  and  $\tau_o$ . Since  $[O_2]$  is proportional to the oxygen partial pressure,  $p_{[O_2]}$ , equation (3.4) can be written:

$$\frac{I_o}{I} = 1 + K p_{[O_2]} \quad (3.5)$$

where  $K$  is the quenching constant with respect to  $p_{[O_2]}$ . For a constant mole fraction of oxygen in the gas, the partial pressure of oxygen can be related to the local static pressure by:

$$p = \bar{\Phi}_{o_2} P_{[O_2]} \quad (3.6)$$

where  $p$  is the local static pressure and  $\bar{\Phi}_{o_2}$  is the mole fraction of oxygen in the working gas. The mole fraction is 0.21 for air and can be varied in a cryogenic wind tunnel. Using equations (3.5) and (3.6) an expression for the sensitivity of the luminescent coating to static pressure can be obtained:



$$\frac{\Delta\left(\frac{I_0}{I}\right)}{\Delta p} = K\bar{\Phi}_{[O_2]} \quad (3.7)$$

From equation (3.7) it can be noted that the sensitivity of a paint with quenching constant  $K$  will decrease with decreasing mole fraction. Thus in a cryogenic wind tunnel where the mole fraction of oxygen is low in the nitrogen-based cryogenic working gas, a paint with large quenching constant,  $K$ , is needed.

By using the ratio of  $I_0/I$ , spatial nonuniformities in the coating thickness, uneven luminophore concentration, and non-uniform excitation light are ratioed out of the result. It is however, very difficult to obtain a zero oxygen condition, even in a cryogenic wind tunnel where residual oxygen in the liquid nitrogen can have a large effect on the emitted intensity from these very sensitive PSP's. This problem can be alleviated by taking equation (3.4) at intensity  $I$  and ratioing it with an intensity measured at a known reference condition,  $I_{ref}$ . Factoring out adsorption intensity  $I_a$  yields the functional form of the Stern-Volmer equation shown below:

$$\frac{I_{ref}}{I} = A(T) + B(T) \frac{P_{[O_2]}}{P_{[O_2]_{ref}}} = a(T) + b(T) \frac{P}{P_{ref}} \quad (3.8)$$

$$A(T) + B(T) = a(T) + b(T) = 1$$

where  $A$  and  $B$  are experimentally determined coefficients,  $I$  is the measured intensity,  $I_{ref}$  is a reference intensity,  $p_{[O_2]}$  is the oxygen partial pressure, and  $p_{[O_2]_{ref}}$  is a reference partial pressure. Due to the temperature dependence of the oxygen permeability of the binder and  $k_D$  ( $\tau_o$ ), the coefficients  $A$  and  $B$  are temperature dependent thus requiring surface temperature to be known. The constants  $A$  and  $B$  can be determined through the following relation and experimental determination of the constants  $a_1$  and  $b_1$  in the following<sup>16</sup>:

$$A = a_1 \left[ 1 + \frac{E_{nr}}{RT_{ref}} \left( \frac{T - T_{ref}}{T_{ref}} \right) \right]$$

$$B = b_1 \left[ 1 + \frac{E_p}{RT_{ref}} \left( \frac{T - T_{ref}}{T_{ref}} \right) \right] \quad (3.9)$$

where  $E_{nr}$  is the non-radiative activation energy,  $E_p$  is the polymer activation energy,  $R$  is the interaction distance,  $T$  is the surface temperature in K,  $T_{ref}$  is the reference temperature in K, and  $a_1$  and  $b_1$  are experimentally determined constants. These constants can be obtained through a calibration where oxygen partial pressures are varied (or static pressure of a constant oxygen mole fraction gas is varied) at known constant temperature. Equation (3.8) can be more generally expressed as a power series expansion on the partial pressure ratio to account for some non-linear effects, however the second order polynomial expression has been shown to be sufficiently accurate to this point.

For TSP's, the assumption of a non oxygen-permeable paint allows  $[O_2]$  to be set to zero in equation (3.2) yielding:

$$\Phi = \frac{I}{I_a} = \frac{k_L}{k_L + k_D} = k_L \tau_0 \quad (3.10)$$

As noted previously, the rate constant  $k_D$  is temperature dependent. It can be decomposed into a temperature-independent part and temperature-dependent part,  $k_D = k_0 + k_1$ . The thermal deactivation rate  $k_1$  can be assumed as the Arrhenius form<sup>24</sup>:

$$k_1 = C \exp\left(-\frac{E}{RT}\right) \quad (3.11)$$

where  $C$  is a pre-exponential constant,  $E$  is the Arrhenius activation energy,  $R$  is the universal gas constant, and  $T$  is the thermodynamic temperature in Kelvin. Substituting equation (3.11) into (3.10) and then subtracting the inverse of equation (3.10) at absolute zero from the inverse of equation (3.10) at temperature  $T$  yields the following:

$$\frac{I_a}{I(T)} - \frac{I_a}{I(0)} = A k_L^{-1} \exp\left(-\frac{E}{RT}\right) \quad (3.12)$$

The adsorption intensity  $I_a$  can be excluded from the above expression by dividing (3.12) by the reference intensity  $I_{ref}$  at a known constant temperature  $T_{ref}$  yielding:

$$\ln \frac{I(T)[I(0) - I_{ref}(T_{ref})]}{I_{ref}(T_{ref})[I(0) - I(T)]} = \frac{E}{R} \left( \frac{1}{T} - \frac{1}{T_{ref}} \right) \quad (3.13)$$

Since  $I(0)$  is much larger than  $I(T)$  and  $I_{ref}(T_{ref})$  it follows that:

$$\frac{[I(0) - I_{ref}(T_{ref})]}{[I(0) - I(T)]} \approx 1.0 \quad (3.14)$$

and

$$\ln \frac{I(T)}{I_{ref}(T_{ref})} = \frac{E}{R} \left( \frac{1}{T} - \frac{1}{T_{ref}} \right) \quad (3.15)$$

Thus theoretically speaking, a plot of the log of the intensity ratio versus  $(1/T - 1/T_{ref})$  yields a straight line of slope  $E/R$ . Since the ratioing process corrects for non-uniformities, the slope of the Arrhenius plot can be used to compare the sensitivity of respective temperature paints.

While the linear relation holds for many luminescent compounds in solution, some compounds in rigid matrices show non-linearities over certain temperature ranges. Alternatively, the temperature dependence can be expressed in a functional form:

$$\frac{I(T)}{I_{ref}(T)} = F(T/T_{ref}) \quad (3.16)$$

The functional form could be a polynomial, exponential, or other function that fits the experimental data over a certain temperature range.

## CHAPTER 4: PAINT COMPOSITION, PREPARATION, AND MEASUREMENT TECHNIQUES

### 4.1 Paint Composition and Preparation Techniques

A TSP or PSP is generally composed of two components, a luminescent molecule and binder. Some new methods of attaching luminescent molecules to surfaces have also been investigated in order to make more sensitive cryogenic PSP's.

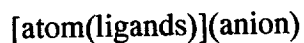
#### 4.1.1 Luminescent Molecules

The luminescent molecules calibrated in this research were based on second- and third-row transition metals. These metals readily undergo the addition or subtraction of electrons to produce different oxidation states, which makes them attractive as photoredox reagents<sup>23</sup>. Their likelihood to donate electrons to electron-accepting substituents is desired because this has been shown to increase quantum yield and excited state lifetime<sup>36</sup>. Another positive attribute of the transition metals is that they are naturally structured to carry out photochemical reactions using visible light<sup>23</sup>.

For temperature-sensitive paint research, emphasis was placed on the [Ru(trpy)<sub>2</sub>] family of luminescent molecules. This family exhibits very intense emissions at low temperatures and are nearly fully quenched at room temperature<sup>25</sup>. Thus, they are an excellent choice for temperature sensors under cryogenic conditions. The structure of [Ru(trpy)<sub>2</sub>] molecules offers several advantages significant to this research. Various [Ru(trpy)<sub>2</sub>] molecules can be easily synthesized with different ligands<sup>36</sup>. As noted in Section 3.1.1, the dynamics of the metal-to-ligand bond and the electron donating or accepting characteristics of the ligand<sup>36</sup> have a significant effect on the temperature sensitivity of the luminescent molecule. This includes the rate constant and region of temperature over which the molecule responds. A main effort in this research was to calibrate [Ru(trpy)<sub>2</sub>] type molecules with various ligands to determine if the response could be "tuned". This would enable the synthesis of molecules specifically designed to respond with high sensitivity in a specific region of temperature.

For cryogenic pressure-sensitive paint research, the emphasis was placed more on the binder than on the luminescent molecule. The reasoning being that the permeability of the binder has a significant effect on the response of the paint (see discussion in section 4.1.3). Thus, three luminescent molecules known to exhibit good sensitivity at lower oxygen concentrations were chosen for this research. The first,  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  has been used for many different measurements at room temperature and has a good record of accomplishment. The other two luminescent molecules chosen were Platinum porphyrins, Pt(meso-tetra fluorophenyl) Porphyrin (PtTFPP) and Pt(octa-ethyl) Porphyrin (PtOEP). Both have been observed to exhibit non-linear Stern-Volmer behavior in a rigid matrix, but this non-linear behavior exhibits greater sensitivity at lower oxygen partial pressures. As noted previously, good quenching behavior at low oxygen partial pressures is needed for cryogenic wind tunnel measurements.

With the exception of the porphyrin complexes, a standard nomenclature has been used throughout this document to describe the luminescent molecules. The nomenclature is of the following form:



#### 4.1.2 Temperature-sensitive Paint Preparation

The preparation of temperature-sensitive paint layers is generally a simple process. Two essential ingredients are required, the luminescent molecule and the binder used to hold the luminescent molecules to the surface. While some luminescent molecules will dissolve directly into certain polymers, in general it is necessary to first dissolve the luminescent molecules into a solvent, then mix with a binder which is also soluble in the solvent used. After the paint is mixed it can be applied to the surface on which a temperature measurement is desired. The solvent typically fully evaporates before the polymer is completely dry, leaving a layer where the luminescent molecules are suspended within the polymer matrix.

Generally, polymer binders are used to attach the luminescent molecules to the surface. Polymer binders are typically chosen because of their ability to form thin layers

and their solubility in common organic solvents. Different binders have been shown to have contrasting effects on adsorption and emission spectra, luminescent intensity (lifetime) and temperature dependence<sup>35</sup>. Binder choice is often the result of experience plus trial and error. Another concern in choosing a binder for TSP measurements is oxygen permeability. Since both oxygen and temperature quench luminescent molecules, it is desirable to de-couple the effects. This is easily accomplished in TSP's by choosing a binder that has low oxygen permeability.

The mixture may be applied to the surface using a variety of methods. The two most common application methods are spray and dipping. Spraying the paint onto the surface using an airbrush produces a thin, fairly uniform coating. This is desirable so that non-uniformity in the layer does not adversely effect the measurements. Dipping the surface into the paint solution and slowly withdrawing it produces thin films. Uniformity depends on the rate at which the surface is withdrawn from the paint mixture and on surface adhesion properties. In general, this method produces coatings uniform to the eye and acceptable for conducting measurements.

As this research is focused on TSP's operating in the cryogenic temperature range, it is necessary to examine what effects cold temperatures have on paint layers. The main concern is that the layer will become too brittle and crack at the extremely cold temperatures. Whether or not the layer will crack is dependent on the amount of contraction the material suffers with lowering temperature and the thickness of the layer. Experience has shown that thicker layers tend to crack more than thinner layers under the same cryogenic conditions. The overall likelihood of a layer to crack is difficult to quantify, thus trial and error generally identifies which particular binders are best to use and how thick the coating should be.

#### 4.1.3 Pressure-sensitive Paint Preparation

In general, the PSP molecule is absorbed into a polymer binder, which is highly oxygen permeable, and applied to the surface being measured. This is completed in a similar manner to that used to mix and apply TSP's. Factors such as test environment and response time influence the choice of molecule and binder. As with TSP's, the

binder can affect a luminescent molecules absorption and emission spectra, luminescent intensity (lifetime) and temperature dependence.

Generally, binders with higher diffusivity produce more sensitive PSP's with faster response times. Baron et al<sup>26</sup>. suggest fast responding coatings based on silica coatings applied to aluminum plates or a commercial porous silica thin-layer chromatography (TLC) plates. These types of coatings have been used to measure pressure distributions in impinging jets<sup>27</sup> and rotating propeller blades<sup>28</sup>. Torgerson et. al.<sup>29</sup> have used less porous binders such as GE 118 RTV and model airplane dope to make measurements on a low speed impinging jet. GE RTV 118 mixed with silica particles was used as a binder for  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  in high-speed axial compressor fan blade pressure distribution measurements<sup>30</sup>. While the most sensitive response is obtained with silica coatings, these are often difficult to apply to wind tunnel models. RTV based binders can be more easily sprayed onto the model, but tend to be less permeable to oxygen.

Oxygen permeability of the layer becomes an even larger issue at the low temperatures being investigated for this work. Permeability of gaseous oxygen into the paint layer is obtained from the following relation:

$$P = P_o e^{-E/kT} \quad (4.1)$$

where P is the coefficient of permeability, E is the thermal activation energy, k is Boltzman's constant, and T is temperature in Kelvin. It can be seen from equation (4.1) above that permeability will decrease exponentially with decreasing temperature.

Because permeability becomes so low at cryogenic temperatures, methods of increasing permeability needed to be found. Some of the low temperature effects on permeability of the RTV and GP-197 based paints have been alleviated by adding large amounts of silica to the paint mixture. While this increases the porosity of the binder, it also has an adverse effect on the ductility of the paint layer. In addition, several new methods of depositing the luminescent molecules onto the surface using little or no polymer were examined. Those methods are outlined in the following sections.

#### 4.1.3.1 Anodized Aluminum

To alleviate some of the poor effects of low temperature on binders, a new method of depositing the luminescent molecule onto the model was developed by Asai et. al<sup>31</sup>. In this method, an electrochemical anodizing process is used to produce a thin layer of porous alumina containing a luminophore. Aluminum and lead strips are placed in a bath of 20% (by concentration) sulfuric acid and 10 Volts (~0.6 A) placed across the two strips with the positive lead attached to the aluminum and the negative lead to the Pb. The voltage is applied to the two strips for approximately 10 to 30 minutes. Next the luminescent molecule is dissolved in a bath of Ethanol and the two strips are placed in the Ethanol bath with the aluminum surface to be coated facing the lead strip. A voltage of 20 Volts (~0.01A) is then placed across the two strips with the negative lead attached to the aluminum and the positive lead attached to the Pb. The voltage is applied for 5 to 10 minutes depending on the desired coating thickness. The resulting coating is very uniform, tough, and has an extremely high sensitivity to oxygen at cryogenic temperatures.

#### 4.1.3.2 Hydrothermal Coating

A coating method in which a thin coating of polymer and titania can be created through hydrothermal crystallization<sup>32</sup> was tried. This offers the possibility of creating a coating with high quantum yield. Since only a small weight percent of polymer is required, this coating also offers the possibility of minimizing the cryogenic effects on the polymer. To create the mixture, the polymer (Kraton D1102 shell / polystyrene-polybutadiene co-polymer) is dissolved in toluene. Next, a titanium precursor (titanium diisopropoxide bis(ethyl acetoacetate)) is added. The ratio of TiO<sub>2</sub> to polymer in the final coating is controlled at this step. The mixture is applied to a surface which is subsequently dipped into a solution of water and a luminophore ([Ru(ph<sub>2</sub>-phen)<sub>3</sub>] in this case) where a hydrolyzing process takes place, forming the coating containing TiO<sub>2</sub>, polymer, and luminescent molecule. The ratio of TiO<sub>2</sub> to polymer can vary significantly, however 80/20 and 99/1 were tested in this research.



#### 4.1.3.3 Sol-gel

The Sol-gel process is used to produce high quality glasses and ceramics<sup>33</sup>. In optical sensors, silica or titania is commonly used in the production of the Sol-gel layer. These glasses are produced through a process of hydrolysis and condensation polymerization of the metal alkoxide solution containing the silica or titania. Following this, a temperature program is undertaken to control the densification process. Through selection of process parameters, a microporous glass can be produced. This structure can be used as a support matrix for the luminophores, which are added to the precursor solution. This structure grows around the luminescent molecules and encapsulates them in a nanometer-scale cage-like structure small enough to hold the luminescent molecule, yet large enough to allow the quenching reagent (oxygen) to pass through.

#### 4.1.3.4 Tape Casting

Tape casting is a commonly used method of producing extremely thin layers of ceramic powders<sup>34</sup>. Again, some polymer is needed but considerably less polymer is in the coating than in traditional paints. To create a tape cast coating, a backing is passed through a bath containing a solution of aqueous ceramic slurry with polymer emulsion as shown below in Figure 4.1.

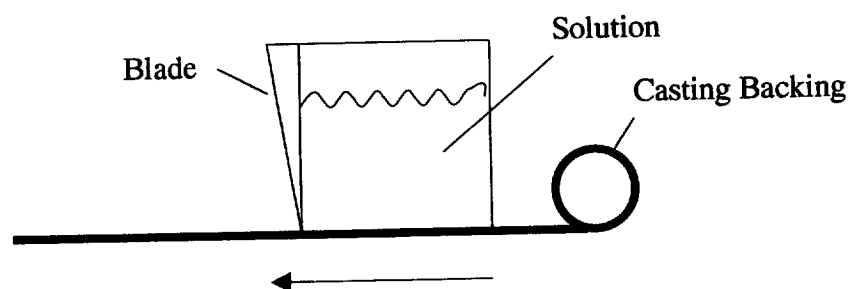


Figure 4.1: Tape Casting Method

The blade controls the thickness of the layer as the backing passes out of the solution. The solution then dries onto the backing. Final coatings can be approximately 0.5 mm thick. Once the coating is dry, it can be dipped into a solution containing a dissolved luminophore, which is soaked into the coating.

#### 4.1.3.5 Porous Filters

Certain filters may retain their porosity under cryogenic temperatures. Soaking luminescent molecules into the filters creates a PSP that retains its porosity under cryogenic conditions. The choice of filters is primarily a trial and error process. Two such paints were tested in this work.

### 4.2 Measurement Techniques

Two possible measurements can be used to relate to temperature or pressure in a TSP or PSP coating. Both are acquired in similar manners. The first is based on the intensity of the emitted light from the paint. The second involves AC measurement of the lifetime or phase of the emitted light.

#### 4.2.1 Intensity Based

Measurement of fluorescent intensity is currently the most common method of gathering experimental data from temperature- and pressure-sensitive paints. Blue or UV lamps are used to excite the paint and fluorescent emissions are collected with a CCD camera or photodetector and PC based frame digitizer board. For paint calibration, integrated measurements using a photodetector are used to relate intensity on a small painted surface to temperature or pressure.

For full surface mapping a CCD camera is used to take an image of the entire surface. The digitized image is then processed to get pixel intensities and flow-off and flow-on images are divided to remove non-uniformities in paint thickness and lighting. This ratio is then converted to temperature or pressure readings based on calibration data, yielding a temperature or pressure map of the entire surface. Resolutions of 8 bits and 640X480 pixels are available in standard CCD cameras, however resolutions of 16 bits are available in more expensive cooled, scientific CCD arrays. The biggest disadvantage to this method is that model movement can cause displacement between the flow-off and flow-on images. This problem is commonly alleviated by the use of image mapping and spatial transformations.

Improved resolution and noise characteristics can be achieved through the use of a laser scanning system. Instead of taking an image of the entire surface, a focused laser spot is scanned over the surface, exciting the paint. A low noise photo-multiplier tube or photo-diode is used to measure the emission intensity at each spot in the scan. After amplifying and filtering, the signal is digitized with a high resolution A/D converter. Through the use of computer controlled scanning mirrors or a rotary stage, the scan area and resolution can be user-specified. An added advantage is that the laser provides fairly uniform excitation intensity, while variations can be easily monitored.

#### 4.2.2 Lifetime Based

By modulating the intensity of the excitation light, fluorescence decay curves can be recorded. Typically several curves are recorded and averaged using a digital oscilloscope or A/D board. An exponential curve can then be fitted to the data and the lifetime calculated. The advantage to using lifetime measurements is that the measurements are independent of luminophore concentration and lighting effects. There is however, a disadvantage when using a laser scanning system in conjunction with this method. The disadvantage is that a large amount of computing time is required to fit a curve to each data point on the surface.

A related method that requires less computing time is measurement of phase. Similar to lifetime measurements, the excitation intensity is modulated but the phase shift between the excitation and fluorescence signals is measured instead of decay. This measurement can be easily completed using a lock-in amplifier and has the added advantage of rejection of AC noise at frequencies other than the frequency of the modulation. Torgerson<sup>29</sup> notes that for systems with small pressure changes (i.e. low speed aerodynamic tests), signal-to-noise ratio can be significantly increased through the use of the scanning system with a lock-in amplifier. By modulating the laser beam, producing an AC fluorescent signal, and making use of the lock-in amplifier, electrical bandwidth can be decreased to well below 1 Hz, increasing the signal-to-noise ratio. The other method used to increase signal-to-noise ratio is to increase the excitation intensity, however care must be taken not to photodegrade the paint. Many popular luminescent compounds, such as the porphyrin family, are highly susceptible to photodegradation.

## CHAPTER 5: TEMPERATURE CALIBRATIONS

In order to make effective surface temperature measurements using temperature-sensitive paint, a calibration relating the surface temperature to paint emission intensity must be performed. The apparatus used to perform these calibrations is shown in Figure 5.1. Each sample consisted of a temperature-sensitive paint applied to an aluminum block (1" x 1" x 0.25"). A 0.125" diameter hole was drilled in the block, parallel to and near the painted surface, for the temperature probe. These samples were then placed on the sample stand and illuminated with light of the correct wavelength to excite the fluorescence.

### 5.1 Calibration Apparatus

The calibration rig consists of five basic components: an excitation source, a sample stand, an intensity measurement system, a thermometer to measure sample temperature, and a personal computer (PC) to collect the data. Details concerning the specific components are given in the following sections and a diagram of the entire system is shown in Figure 5.1.

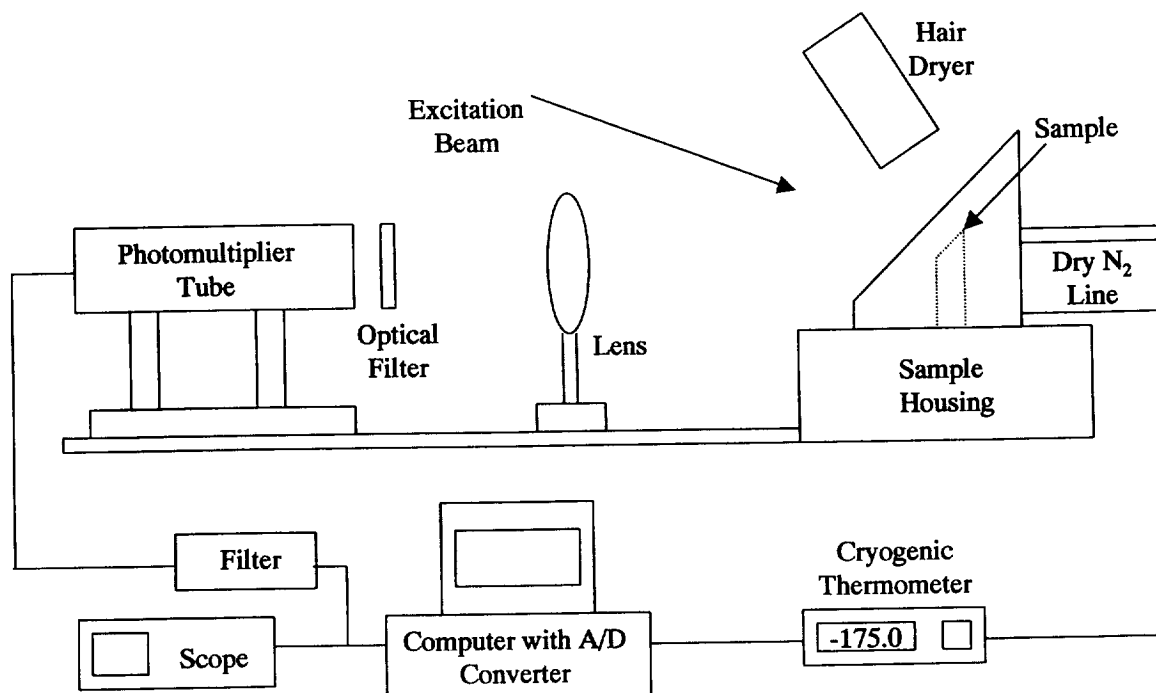


Figure 5.1: Temperature Calibration System

#### 5.1.1 Excitation Source

Paints were excited using either an Argon ion (Ar+) laser or Ultraviolet (UV) light. The UV lamp was a 100-watt mercury arc lamp equipped with a filter. The lamp had a peak emission at 365 nm and little radiation at other wavelengths. In the case of Ar+ laser excitation, either an air-cooled or a water-cooled Argon ion (Ar+) laser was used. The air-cooled laser is a low power (5 mW), multiline (515, 488, and 457 nm) Ar+ laser. The water-cooled Ar+ laser has 5 watts peak power and emissions at various peaks with 488 nm (blue-green) and 514 nm (green) being the strongest.

#### 5.1.2 Sample Stand

Since the area of interest in these experiments was the response of temperature-sensitive paints under cryogenic temperatures, a sample stand capable of attaining temperatures between  $-180^{\circ}\text{C}$  and room temperature was required. A stand capable of

operating in this temperature range was used in previous investigations by Campbell<sup>35</sup> and was used again for these experiments. The design of the stand is shown below in Figure 5.2.

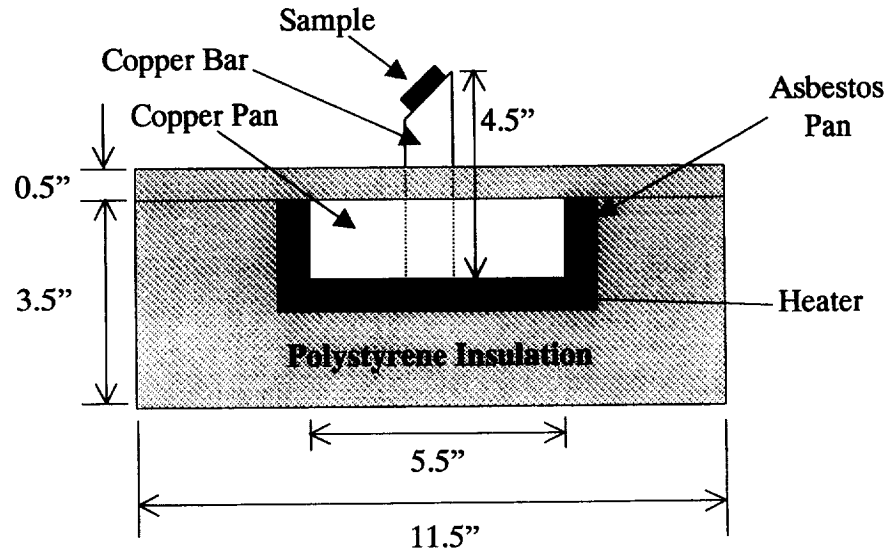


Figure 5.2: Cross Section of Sample Stand

The test stand consists of a 5.5" x 5.5" x 1.5" copper pan with a solid copper bar welded perpendicular to the pan's bottom. The copper bar has a diameter of 1" and is approximately 4.5" tall. It is cut at a 45° angle at its top and a small ledge is bolted to the bar allowing the sample block to rest on the sloped surface.

Underneath the pan rests a 3" diameter heating pad attached to the copper with heat sink compound. The copper fixtures rest inside another pan (6.5" x 6.5" x 2.25") consisting of asbestos blocks with fiberglass insulation placed between the copper and asbestos. The assembly of copper and asbestos rests inside a square hole recessed into a large block of polystyrene insulation. Another block of polystyrene with a small hole for the copper bar is placed over the copper pan. This block also contains a hole for pouring liquid nitrogen into the copper pan. The gaps between the polystyrene sheets are sealed with duct tape along the edges.

To isolate the sample from room air to allow cooling to near liquid nitrogen temperature, a housing of aluminum with a glass window sits atop the polystyrene box surrounding the copper bar and sample. The housing is sealed to the top of the box with duct tape. A line from a nitrogen bottle was attached to the back of the housing in order to purge the box of air prior to each calibration, eliminating the possibility of icing or condensation occurring on the sample surface. In addition, the glass window was heated with hot air from a hair dryer to prevent fogging at the low temperatures.

### 5.1.3 Emission Intensity Measurement

The intensity of the paint's fluorescent emissions was measured using a Photomultiplier tube (PMT) from EMI corporation. The light emitted from the sample was collected by a large lens and the image focused onto the PMT through a long-pass glass/interference optical filter. The filter cut-off frequency was determined by the wavelength of the particular paint's emission. Filters utilized in this research had cut-off frequencies of 550, 580, or 600 nm. The output of the PMT was passed through a Wavetech model 452 low pass digital filter with cut-off set to 30 Hz. This setting reduced any higher frequency fluctuations such as 60 Hz line noise. The output was connected to a PC equipped with a 12-bit analog-to-digital (A/D) board (DAS-1600).

### 5.1.4 Sample Temperature Measurement

Sample temperature was monitored using an Omega CY7-SD7 cryogenic silicon diode sensor and Omega CYD-208 cryogenic thermometer. The sensor was soldered onto a 0.125" copper wire which fit into the hole on the sample drilled near the painted surface. The sensor was connected to the thermometer with 32 gage copper wires, purchased from Omega (CYW4-32-25). The PC read the temperature from the thermometer through a serial port connection.

### 5.1.5 Data Collection

Calibration data was collected using a PC via a Quick Basic Program. The program reads voltage from the PMT via an A/D board and reads sample temperature through the serial port.

### 5.1.6 Calibration Procedure

First, a trickle flow of nitrogen gas through the calibration rig is initiated. This purges ambient air from the rig to avoid condensation or icing on the sample. Next, the sample is cooled to approximately  $-175^{\circ}\text{C}$  by filling the copper pan with liquid nitrogen through the liquid nitrogen pouring hole in the top of the calibration rig. Once the sample is at its coldest temperature, the emitted fluorescence will be at the highest and the PMT supply voltage can be set to yield the highest resolution. After ensuring the PMT is within the linear detection range, the PMT is covered and the Quick Basic program is used to obtain a reading of the DC offset of the PMT. After this, the PMT is uncovered and the program takes data points (temperature, PMT output voltage) at regular intervals as the sample warms from liquid nitrogen temperature to room temperature. As sample warming slows, a current is applied to the heating pad to increase the rate of warming until the calibration ends.

## 5.2 Calibration Results

A total of 26 paints were made and calibrated during this research. Plots of the calibration results are included in Appendix A. Two plots are presented for each paint: relative intensity versus temperature and an Arrhenius plot. Since experimental data is usually presented as an intensity ratio, presenting calibration data as an intensity ratio versus temperature gives direct insight when deciding what paint to use in an experiment based on the calibration data. Campbell<sup>35</sup> found that comparisons of paint sensitivity could be made by comparing the slopes of intensity ratio versus temperature for various paints. For each paint a useful range of sensitivity is identified. The useful range is determined by identifying the temperature region where the paint exhibits sharp intensity



changes with temperature (i.e. the largest slope). A linear regression was performed over the useful range of each paint and a regression line is marked on each intensity ratio plot in Appendix A.

### 5.2.1 General Results

Fluorescent compounds based on Copper, Platinum, Rhodium, Ruthenium, and Osmium were tested. Emphasis was placed on the  $[\text{Ru}(\text{trpy})_2]$  family of compounds because they have been shown to be temperature dependent in the region of interest by Campbell<sup>35</sup> and Maestri et. al.<sup>36</sup> and derivatives with larger Stokes shifts into the red could be formulated<sup>36</sup>. A discussion of the different Ruthenium compounds is given in section 5.2.2. Early in this research the binder of choice was determined to be DuPont Chromaclear® due to its low oxygen diffusivity and good surface adhesion at cryogenic temperatures.

For the purpose of comparison, the average slope of each paint's intensity ratio versus temperature over its useful range was calculated by linear regression. Plots of the calibration data can be found in Appendix A. The useful range and intensity ratio slope of each paint are tabulated below in Table 5.1.

Table 5.1: Intensity Ratio Slope Data for Calibrated TSP's

| Paint                                                                                   | Fig. | Useful Range (°C) | Intensity Ratio Slope ( $\Delta(I/I_{ref})/\Delta T$ ) | Comments             |
|-----------------------------------------------------------------------------------------|------|-------------------|--------------------------------------------------------|----------------------|
| [Cu(ph <sub>2</sub> -phen) <sub>2</sub> ](PF <sub>6</sub> ) <sub>2</sub> in GP-197      | A.1  | -150 to -80       | -0.0073                                                | Calibration Failed   |
| PtPFPP in CC                                                                            | A.2  | 45 to 100         | -0.0107                                                | Easily photodegraded |
| PtPFPP in Polyurethane                                                                  | A.3  | 0 to 75           | -0.0062                                                | Easily photodegraded |
| [Rh(bzq) <sub>2</sub> Cl] <sub>2</sub> in CC                                            | A.4  | -175 to -130      | -0.0191                                                |                      |
| [Rh(bzq) <sub>2</sub> (phen)](PF <sub>6</sub> ) in CC                                   | A.5  | -100 to -50       | -0.0107                                                |                      |
| [Ru(bipy) <sub>3</sub> ](DS) <sub>2</sub> in CC                                         | A.6  | 0 to 75           | -0.0096                                                |                      |
| [Ru(bipy) <sub>3</sub> ](TFPB) <sub>2</sub> in CC                                       | A.7  | 0 to 75           | -0.0095                                                |                      |
| [Ru(ph <sub>2</sub> -phen) <sub>3</sub> ](DS) <sub>2</sub> in CC                        | A.8  | 20 to 90          | -0.0077                                                |                      |
| [Ru(trpy)] in CC                                                                        | A.9  | -175 to -85       | -0.0112                                                |                      |
| [Ru(trpy)(4'-C <sub>6</sub> F <sub>5</sub> -trpy)](NO <sub>3</sub> ) <sub>2</sub> in CC | A.10 | -175 to -50       | -0.0081                                                |                      |
| [Ru(trpy)(4'-Cl-trpy)](Cl <sub>2</sub> ) in CC                                          | A.11 | -175 to -50       | -0.0106                                                |                      |
| [Ru(trpy)(4'-NC-trpy)](NO <sub>3</sub> ) <sub>2</sub> in CC                             | A.12 | -150 to -50       | -0.0078                                                |                      |
| [Ru(phtrpy)(Cltrpy)](NO <sub>3</sub> ) <sub>2</sub> in CC                               | A.13 | -175 to -50       | -0.0093                                                |                      |
| [Ru(trpy)(4'-TfO-trpy)](NO <sub>3</sub> ) <sub>2</sub> in CC                            | A.14 | -175 to -50       | -0.0101                                                |                      |
| [Ru(trpy)(MeStrpy)](NO <sub>3</sub> ) <sub>2</sub> in CC                                | A.15 | -175 to -75       | -0.0105                                                |                      |
| [Ru(trpy) <sub>2</sub> (NO <sub>2</sub> Phtrpy)](PF <sub>6</sub> ) in CC                | A.16 | -175 to -75       | -0.0087                                                | Not very stable      |
| [Ru(trpy)(phtrpy)](PF <sub>6</sub> ) <sub>2</sub> in GP-197                             | A.17 | -175 to -50       | -0.0114                                                |                      |
| [Ru(trpy)(phtrpy)](PF <sub>6</sub> ) <sub>2</sub> in CC                                 | A.18 | -150 to -100      | -0.0142                                                |                      |
| [Ru(trpy)(ppd-trpy)](TFPB) <sub>2</sub> in CC                                           | A.19 | -175 to -50       | -0.0097                                                |                      |
| [Ru(trpy)(phyphen)](TFPB) <sub>2</sub> in CC                                            | A.20 | -175 to -50       | -0.0090                                                |                      |
| [Ru(trpy)(SO <sub>2</sub> Me-trpy)](PF <sub>6</sub> ) <sub>2</sub> in CC                | A.21 | -175 to -75       | -0.0104                                                |                      |
| [Ru(trpy) <sub>2</sub> ](DS) <sub>2</sub> in CC                                         | A.22 | -150 to -75       | -0.0122                                                | Calibration Failed   |
| [Ru(trpy) <sub>2</sub> ](TFPB) <sub>2</sub> in CC                                       | A.23 | -170 to -75       | -0.0114                                                |                      |
| [Ru(ppd-trpy) <sub>2</sub> ](TFPB) <sub>2</sub> in CC                                   | A.24 | -175 to -75       | -0.0149                                                |                      |
| [Os(trpy) <sub>2</sub> ](PF <sub>6</sub> ) <sub>2</sub> in CC                           | A.25 | 0 to 75           | -0.0041                                                |                      |
| [Ru(trpy)(Vh127)](PF <sub>6</sub> ) <sub>2</sub> in GP-197                              | A.26 | -175 to -75       | -0.0154                                                |                      |

In general, the Ruthenium and Rhodium compounds exhibited the best response in the temperature range of interest. Compounds based on these two elements exhibited sensitivity from  $-175\text{ }^{\circ}\text{C}$  to  $-75$  or  $-50\text{ }^{\circ}\text{C}$ . While  $[\text{Cu}(\text{ph}_2\text{-phen})_2](\text{PF}_6)_2$  exhibited sensitivity at  $-150\text{ }^{\circ}\text{C}$ , it had a small useful range and comparatively poor intensity ratio slope. Osmium compounds with both terpyridine and bipyridene ligands were tested but only  $[\text{Os}(\text{trpy})_2](\text{PF}_6)_2$  was calibratable. It was desirable to test Osmium based compounds since they can be excited by red laser light and emit in the infra-red range of the spectrum. While a paint that could be excited by a relatively cheap red laser was desired, the useful range was above  $0^{\circ}\text{C}$  and the intensity ratio slope was very poor. The Platinum Porphyrin compounds also did not exhibit temperature sensitivity in the desired temperature range.  $[\text{Rh}(\text{bzq})_2\text{Cl}]_2$  exhibited a large intensity ratio slope over a fairly small useful range ( $-175^{\circ}\text{C}$  to  $-130^{\circ}\text{C}$ ) while  $[\text{Rh}(\text{bzq})_2(\text{phen})](\text{PF}_6)$  had a similar but shifted useful range ( $-100\text{ }^{\circ}\text{C}$  to  $-50\text{ }^{\circ}\text{C}$ ) which was outside our desired temperature range. Overall, the  $\text{Ru}(\text{trpy})$  based compounds showed the best intensity ratio slope over good useful ranges.

### 5.2.2 $[\text{Ru}(\text{trpy})_2]$ based compounds

The objective in investigating various  $[\text{Ru}(\text{trpy})_2]$  based compounds was to obtain a compound which exhibited a response similar to the response of  $[\text{Ru}(\text{trpy})(\text{VH-127})](\text{PF}_6)_2$ , which was received from Thummel at the University of Houston. While the VH-127 compound exhibits a very good temperature response in cryogenic conditions, it is very hard to synthesize while the other  $\text{Ru}(\text{trpy})$  compounds calibrated here were relatively easy to synthesize. By using various ligands as electron donating or electron accepting groups, the “activation” temperature of the luminescent response to temperature could be moved and hopefully designed. All compounds were synthesized by C. Cunningham of the Purdue University chemistry department and were mixed into paints and calibrated using the calibration apparatus described in section 5.1. Figure 5.3 below shows a comparison of several of the synthesized compounds.

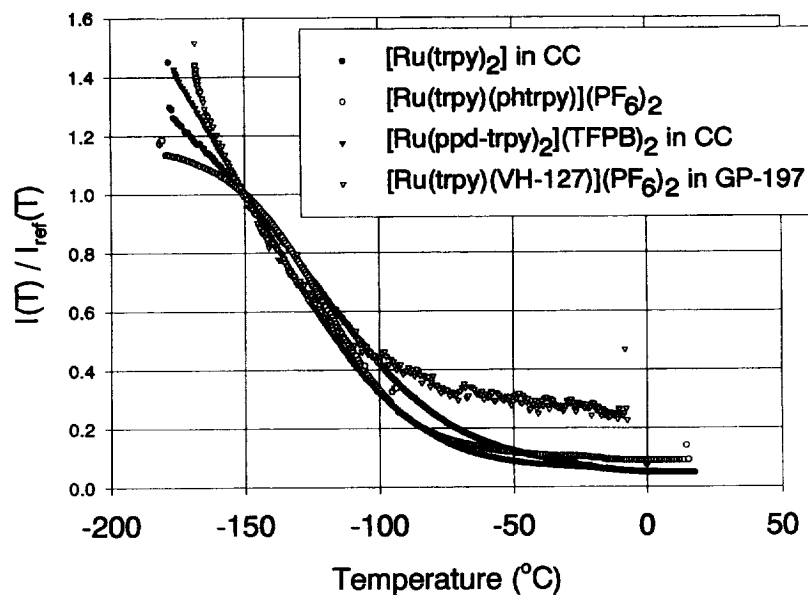


Figure 5.3: Comparison of Ru(trpy) based paints

As can be seen from the above plot and the slopes in Table 5.1, the response of the paints to temperature is very similar for these compounds. As expected,  $[\text{Ru}(\text{trpy})_2]$  has the shallowest slope, while changing the ligand structure produced steeper slopes. While the increases in slope were not as significant as hoped, most interesting is that the response and intensity ratio slope of  $[\text{Ru}(\text{ppd-trpy})_2](\text{PF}_6)_2$  were very similar to that of  $[\text{Ru}(\text{trpy})(\text{VH-127})](\text{PF}_6)_2$  which met our goal as  $[\text{Ru}(\text{ppd-trpy})_2](\text{PF}_6)_2$  is simpler to synthesize. The major difference between these two compounds was that the  $[\text{Ru}(\text{trpy})(\text{VH-127})](\text{PF}_6)_2$  exhibited a linear Arrhenius response while the  $[\text{Ru}(\text{ppd-trpy})_2](\text{PF}_6)_2$  did not. This however does not affect the researcher's ability to calibrate and fit a function to the paint's response. Other Ruthenium based compounds produced good responses in the temperature region of interest with useful sensitivity, but slopes were shallower than that of  $[\text{Ru}(\text{ppd-trpy})_2](\text{PF}_6)_2$ .

### 5.2.3 Effects of Polymer Binders

In chemistry circles, the luminescence of transition metal complexes is typically studied in solution. The effect of a solid matrix on fluorescent compounds is a very complex question and is beyond the current scope. In the interest of completeness, some of the effects are illustrated with the current data.

As previously noted, the mobility of the metal-to-ligand bonds affects the vibrational energy of the bonds. Suspension in a rigid matrix restricts this mobility. Through this restriction the vibrational energy associated with vibrational (temperature) quenching is limited, reducing the sensitivity of the compound to changes in temperature. Interactions between different polymer binders and luminescent molecules have different effects on the mobility of the metal-to-ligand bonds, producing different results. This is illustrated by Figure 5.4 and Figure 5.5 below.

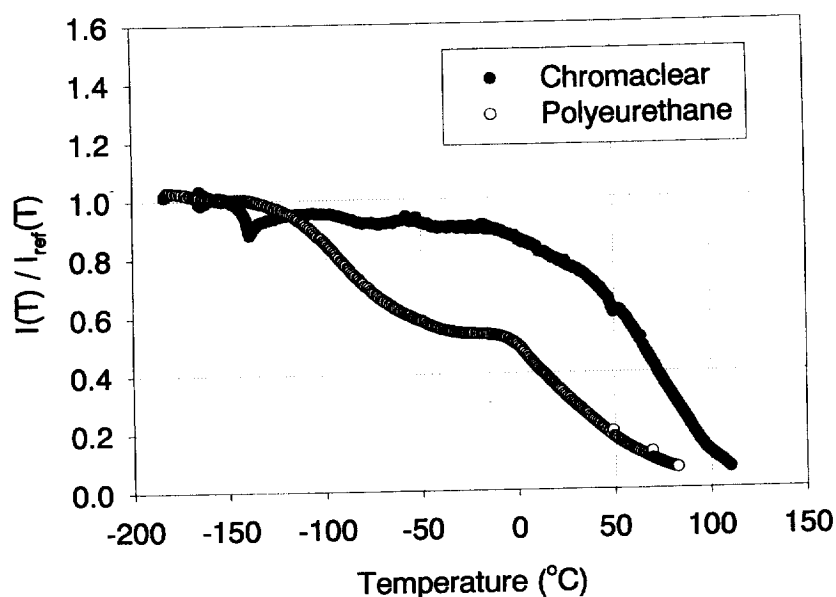


Figure 5.4: Effects of Polymer binder on PtPFPP

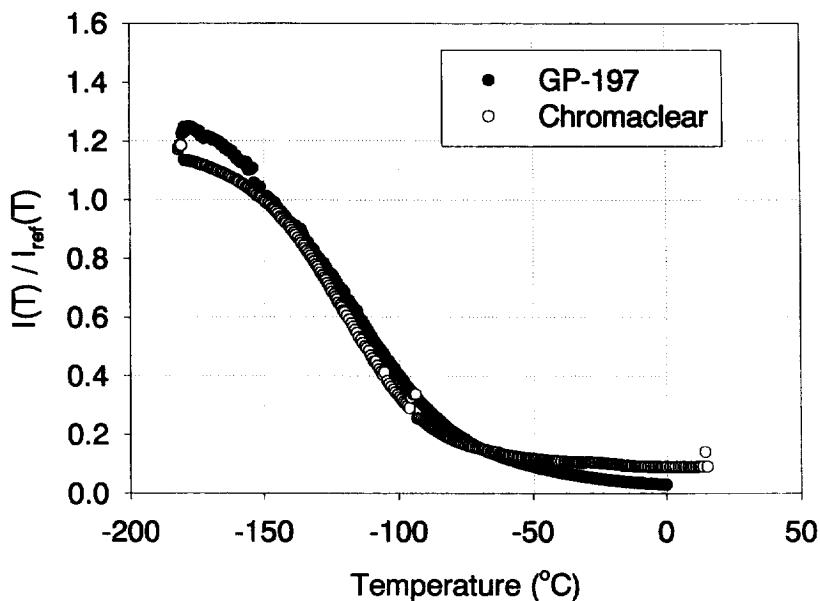


Figure 5.5: Effects of Polymer Binder on  $[\text{Ru}(\text{trpy})(\text{phtrpy})](\text{PF}_6)_2$

While the calibration results for PtPFPP in Chromaclear® and Polyurethane were significantly different, there was only a slight difference seen between  $[\text{Ru}(\text{trpy})(\text{phtrpy})](\text{PF}_6)_2$  in Chromaclear® and in GP-197. Thus, it should be noted that if one compound does not respond well in one binder, it may respond better in another (or vice versa). In this research it was decided to use one suitable binder and test different luminescent molecules in that binder.

Another interesting note is that the Arrhenius plots (see appendix A) are not linear for most of these paints. As noted in Chapter 3, theory states that the response of the paint should be linear when plotted in the Arrhenius form. With the exception of  $[\text{Rh}(\text{bzq})_2](\text{Cl}_2)$  and  $[\text{Ru}(\text{trpy})(\text{VH-127})](\text{PF}_6)_2$ , it can be seen from Figures A.1-A.26 that many of the Arrhenius plots are non-linear over certain temperature ranges, notably the cryogenic. While this does not hinder the ability of the researcher to calibrate and fit a curve to the intensity data, it does indicate that other processes are affecting the response of the paint. One possible explanation of this could be effects of the binder. Increased

rigidity of the polymer matrix at cryogenic temperatures could affect the molecular vibrations that produce the temperature response.

### 5.3 Application – Boundary Layer Transition Detection in Cryogenic Wind Tunnel

Two cryogenic temperature-sensitive paints found during Campbell's research<sup>35</sup> were applied to a NACA 64-A012 laminar airfoil placed in the 0.1-m Transonic Cryogenic Wind Tunnel at NAL, Japan. Testing was conducted by Asai, et. al.<sup>18</sup> and is presented here to illustrate one application of cryogenic temperature-sensitive paints.

#### 5.3.1 Wind Tunnel and Experimental Setup

The 0.1-m Transonic Cryogenic Wind Tunnel is a closed-circuit, fan-driven wind tunnel operated with cryogenic nitrogen as the working gas. The tunnel has a maximum stagnation pressure of 200 Pa and stagnation temperatures can range from 90 K to 200 K. The test section is a 0.1 m square. A simple schematic showing the operation of the 0.1-m Transonic Cryogenic Wind Tunnel is shown below in Figure 5.6 and the optical system is shown in Figure 5.7.

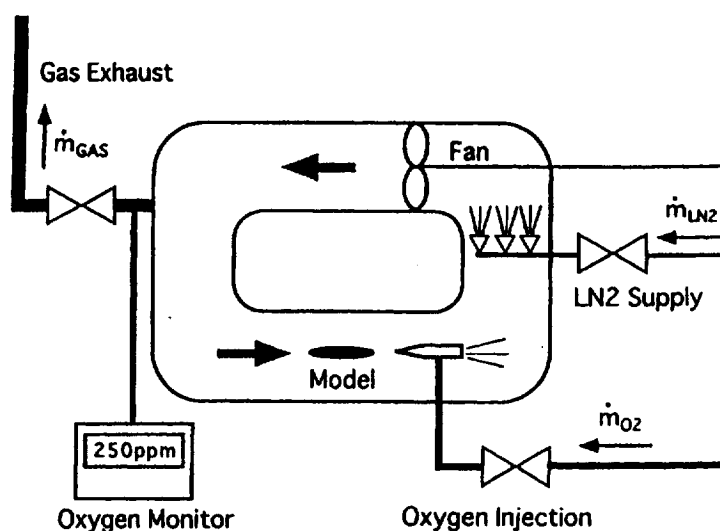


Figure 5.6: NAL 0.1-m Transonic Cryogenic Wind Tunnel Operation

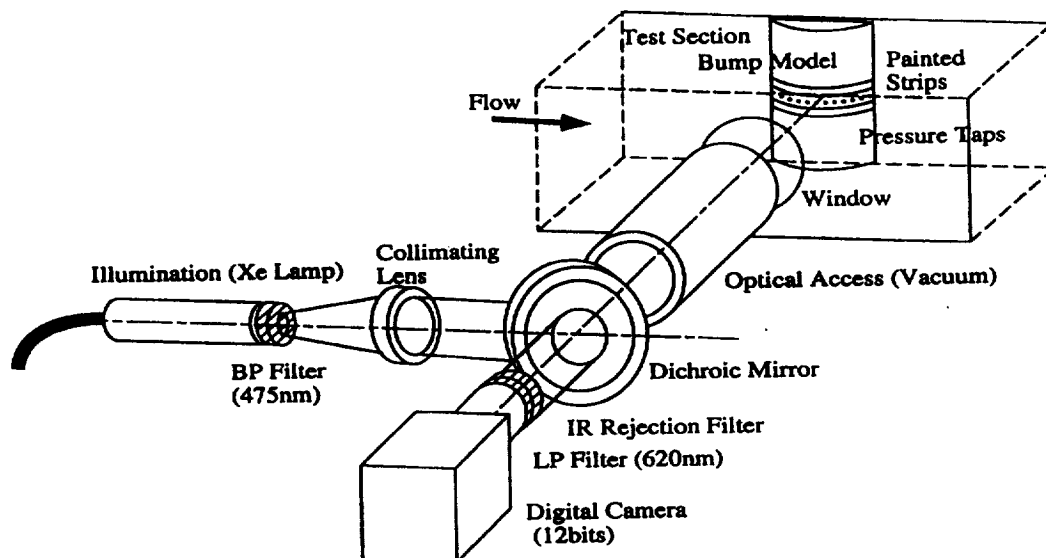


Figure 5.7: Optical System

A 300 W Xenon lamp with a light guide, band pass filter (470  $\pm$  50 nm), and a collating lens made up the excitation source. A dichroic mirror was used to separate paint emission from excitation light and a digital camera was used to measure the emission intensity of the paint.

### 5.3.2 Experiment and Results

[Ru(trpy)<sub>2</sub>] in GP-197 and [Ru(trpy)(VH-127)] in GP-197 were applied to the airfoil. The Xenon lamp was used to excite the paint and images of the surfaces were recorded by the CCD camera. Two methods of enhancing the surface temperature signatures between the laminar and turbulent regions were used. The two methods were actively cooling or heating either the tunnel flow or model substrate. A sample image of the data obtained in this experiment is shown below.



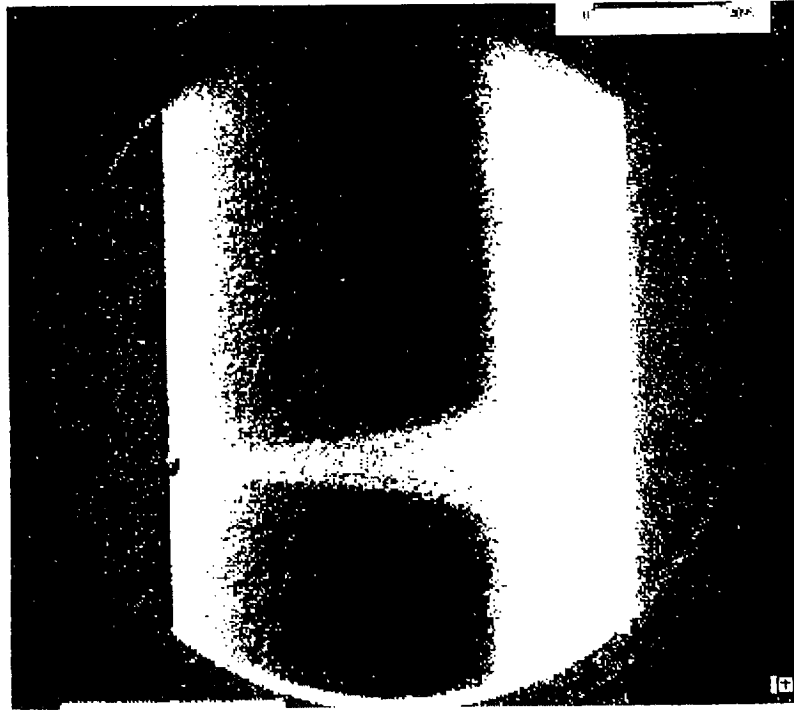


Figure 5.8: Transition on NACA 64-A012

The boundary layer transition is easily visualized in the above figure. The dark areas are laminar flow regions (low heat transfer) and the light areas are turbulent flow regions (high heat transfer). The boundary layer trip approximately 40 % up the chord is also clearly visible.

## CHAPTER 6: PRESSURE CALIBRATIONS

Since measurements using Pressure-sensitive Paints (PSP's) under cryogenic temperatures had never been attempted prior to the inception of this work, simple initial experiments were conducted to determine if PSP's responded under cryogenic temperatures. Once it was determined that PSP's did respond cryogenically, a calibration relating the surface pressure to paint emission intensity needed to be performed in order to be able to make effective surface pressure measurements using pressure-sensitive paint. The apparatus used to perform these calibrations is shown in Figure 6.1, and it should be noted that the overall system is very similar to that used for temperature-sensitive paint calibrations. The main difference is that a more unique sample stand was necessary. As in the cryogenic temperature-sensitive paint calibrations, each sample consisted of a pressure-sensitive paint applied to an aluminum block (1" x 1" x 0.25"). These samples were placed in a modified cryostat and illuminated with light of the correct wavelength to excite the fluorescence.

### 6.1 Initial Feasibility Experiments

Initially it was not known if the pressure-sensitive paints would respond under cryogenic conditions. Thus, a simple experiment was conducted on various paints to see if they would respond. The sample stand used for temperature-sensitive paint calibrations (see Figure 5.2) was modified by adding a copper tube coiled around inside the liquid nitrogen pan. One end of the copper tube opened onto the sample and the other end was connected to a supply of dry oxygen gas. The sample was cooled as described in section 5.1.6 and then oxygen was allowed to flow through the copper tube, which cooled the gas, and then onto the surface of the sample. Visual inspection was made to determine if any observable change in emission intensity occurred. This was done repeatedly as the sample warmed up and the temperature at which a response was

observed was recorded. The results of these initial experiments are shown below in Table 6.1.

Table 6.1: Results of Initial Cryogenic PSP Experiments

| Compound                                                                                                       | yes/<br>no | Notes                                            |
|----------------------------------------------------------------------------------------------------------------|------------|--------------------------------------------------|
| [Ru(ph <sub>2</sub> -phen) <sub>3</sub> ] in Dope                                                              | no         |                                                  |
| [Ru(ph <sub>2</sub> -phen) <sub>3</sub> ] in GE 118                                                            | no         | Responded above 200 K                            |
| [Ru(ph <sub>2</sub> -phen) <sub>3</sub> ] in GE 118 + silica gel (dipped)                                      | yes        | Responded above 150 K                            |
| [Ru(ph <sub>2</sub> -phen) <sub>3</sub> ] in GE 118 + silica gel (Toluene as solvent)                          | yes        | Responded above 150 K                            |
| [Ru(ph <sub>2</sub> -phen) <sub>3</sub> ] in GE 118 + silica gel particles (less than in prev sample) on Mylar | yes        | Responded above 150 K.                           |
| [Ru(ph <sub>2</sub> -phen) <sub>3</sub> ] in GE 118 + silica gel particles on Mylar                            | yes        | Above 125 K                                      |
| [Ru(ph <sub>2</sub> -phen) <sub>3</sub> ] in GP-197                                                            | no         | Responded above 235 K                            |
| [Ru(ph <sub>2</sub> -phen) <sub>3</sub> ] in GP-197 + lots of silica                                           | yes        | Showed response at 90 K                          |
| PtTFPP in GP-197                                                                                               | no         | Responded above 180 K                            |
| PtOEP in GP-197                                                                                                | no         | Responded above 250 K                            |
| PtOEP in GP-197 + lots of silica gel                                                                           | yes        | Responded above 90 K. Very sensitive.            |
| PtOEP in GP-197 + lots of silica gel (dipped)                                                                  | yes        | Responded above 90 K. Very sensitive.            |
| [Ru(ph <sub>2</sub> -phen) <sub>3</sub> ] on Porex Porous Polyethylene                                         | no         |                                                  |
| PtOEP on Porous Polyethylene                                                                                   | yes        | Responded above 125 K.                           |
| [Ru(bipy) <sub>3</sub> ](DS) <sub>2</sub> on TLC                                                               | yes        | Responded above 110 K.                           |
| [Ru(ph <sub>2</sub> -phen) <sub>3</sub> ] on TLC                                                               | yes        | Responded above 90 K. Very sensitive             |
| PtOEP on Polystyrene                                                                                           | yes        | Responded above 125 K. Not a very good response. |
| PtOEP in GP-197 soaked into ceramic #1                                                                         | yes        | Responded above 125 K.                           |
| PtOEP in GP-197 soaked into ceramic #10                                                                        | no         | Responded above 180 K.                           |
| PtOEP in GP-197 soaked into ceramic #2                                                                         | yes        | Responded above 125 K.                           |
| PtOEP in GP-197 soaked into ceramic #3                                                                         | yes        | Responded above 130 K                            |
| PtOEP in GP-197 soaked into ceramic #4                                                                         | yes        | Responded above 140 K.                           |
| PtOEP in GP-197 soaked into ceramic #5                                                                         | yes        | Responded above 150 K.                           |
| PtOEP in GP-197 soaked into ceramic #6                                                                         | yes        | Responded above 175 K.                           |
| PtOEP in GP-197 soaked into ceramic #7                                                                         | yes        | Responded above 140 K.                           |
| PtOEP in GP-197 soaked into ceramic #8                                                                         | yes        | Responded above 160 K.                           |
| PtOEP in GP-197 soaked into ceramic #9                                                                         | yes        | Responded above 125 K.                           |
| PtOEP in GP-197 soaked into filter paper                                                                       | yes        | Responded above 150 K.                           |

Several significant observations can be made from the above results. Notably that paints using polymer binders from common room temperature PSP's showed no response at the desired conditions (below 150 K). The addition of silica gel to certain binders (GE RTV and GP-197) improved observed response by lowering the temperature at which a response was first observed. Finally, no ceramic binders worked in the region of interest.

## 6.2 Calibration Apparatus

The cryogenic pressure-sensitive paint calibration rig consists of eight basic components: an excitation source, a modified cryostat, an emission intensity measurement system, a temperature measurement and control system, an absolute pressure measurement and control system, the test gas, a vacuum pump, and a personal computer (PC) to collect the data. Details concerning the specific components are given in the following sections and a diagram of the entire system is shown in Figure 6.1.

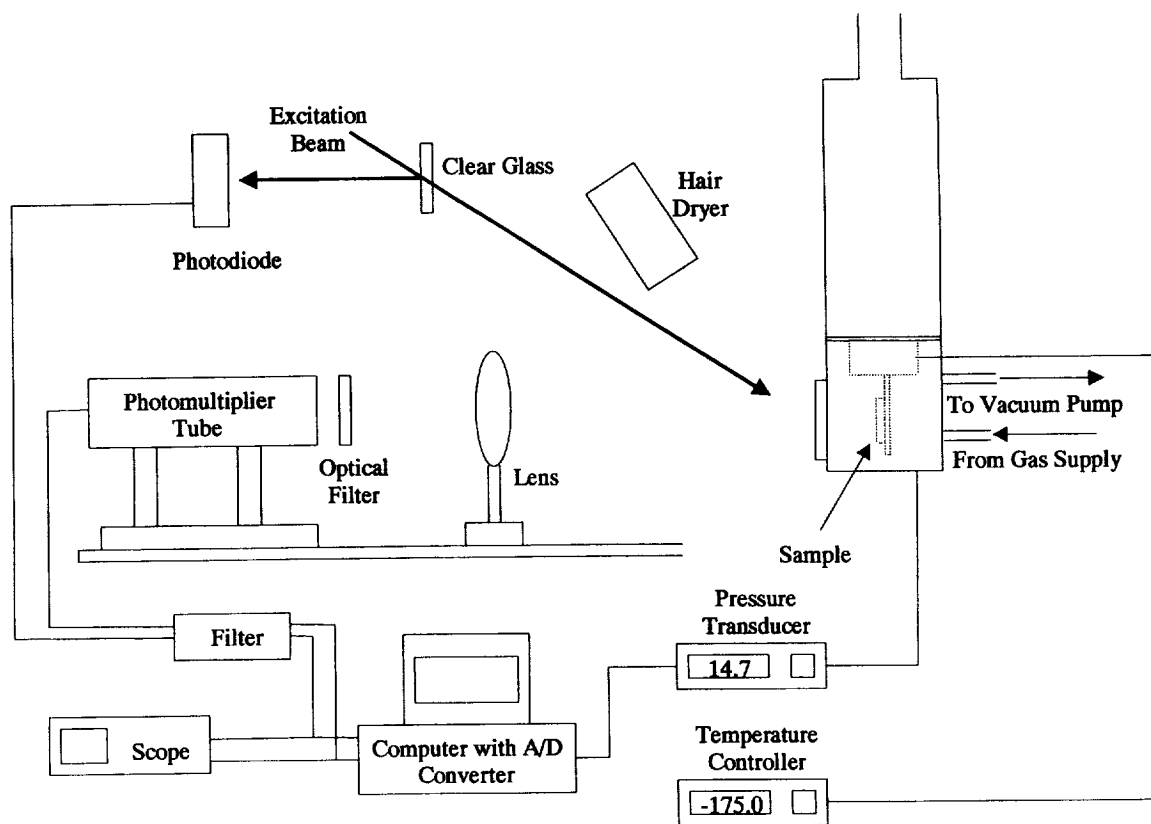


Figure 6.1: Pressure Calibration System

### 6.2.1 Excitation Source

Paints were excited using either an Argon (Ar<sup>+</sup>) laser or frequency doubled yag laser. In the case of Ar<sup>+</sup> laser excitation, either an air-cooled or water-cooled Argon ion (Ar<sup>+</sup>) laser was used. The air-cooled laser is a low power (5 mW), multiline (515, 488, and 457 nm) Ar<sup>+</sup> laser. The water-cooled Ar<sup>+</sup> laser has 5 watts peak power and emissions at various peaks with 488 nm (blue-green) and 514 nm (green) being the strongest. The frequency doubled yag has 50 mW peak power with emission at 532 nm.

Excitation source intensity was measured using a Nu systems model 2001 photodiode and recorded on the PC through an A/D board. The excitation light was reflected off a piece of clear glass and focused onto the photodiode. This measurement was used to correct calibration data for fluctuations in the intensity of the excitation source.

### 6.2.2 Modified Cryostat

In addition to operating at cryogenic temperatures, the test stand for the cryogenic pressure-sensitive paints had to be a sealed vessel so that partial pressure of oxygen could be controlled. A modified Keltran PF cryostat was used for this purpose. The modified cryostat is shown below in Figure 6.2.

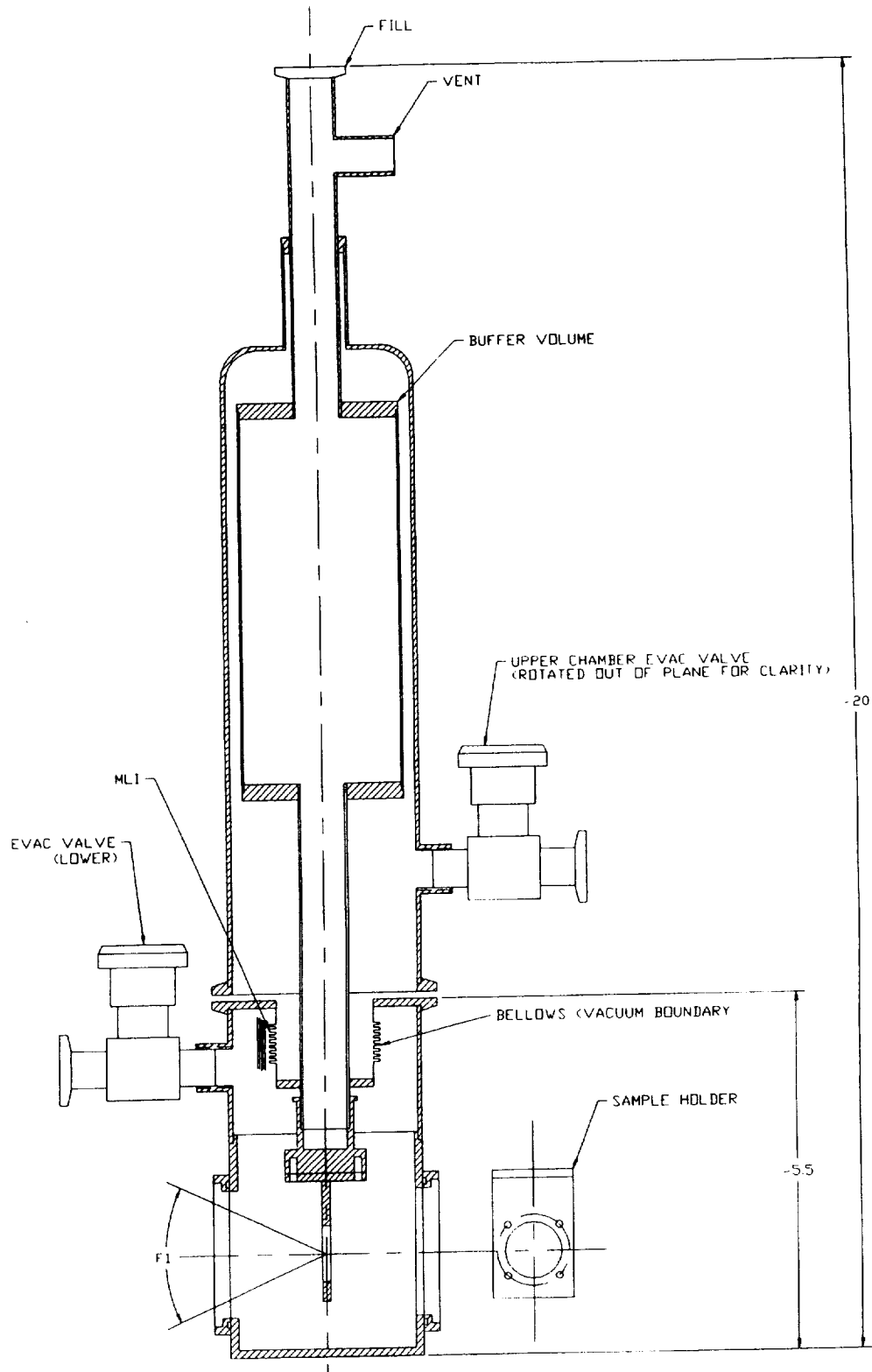


Figure 6.2: Modified Keltran PF Cryostat



Liquid nitrogen is used to cool the device to cryogenic temperatures and is contained in the buffer volume. In most standard cryostats, experiments are conducted solely under vacuum, thus the vacuum insulation jacket surrounding the buffer volume is simply extended around the sample holder so that one evacuation valve is needed to evacuate the entire unit. For our purpose however, it is necessary to fill the space surrounding the test sample with a gas mixture containing oxygen. Because the surface of the buffer volume is always near liquid nitrogen temperature ( $\sim 77$  K), any oxygen in a gas surrounding the buffer volume would condense on the surface of the buffer since the condensation temperature of oxygen ( $\sim 90$  K at 14.7 PSI) is above that of nitrogen. In addition, the presence of a gas in the system significantly increases the heat transfer to the outside, reducing test time available at cryogenic conditions. Thus, it was necessary to modify the basic design of the cryostat to better suit our requirements. The solution was to introduce a bellows between the buffer volume area of the cryostat and the test chamber area containing the sample (see Figure 6.2), thus separating the liquid nitrogen storage portion from the actual test chamber where gas would be introduced into the unit. Two valves were added to the lower portion to allow for filling and evacuation of test gasses.

There is one window on the lower portion allowing optical access to the sample, which is mounted on the copper sample holder. The sample holder is attached to the base of the lower tube leading from the buffer volume, allowing liquid nitrogen to come in direct contact with the sample holder. Aluminum sample blocks with the PSP paint on one surface are attached to the sample holder with an aluminum bracket and four screws. The interior of the test chamber has been finished with black paint to reduce reflected excitation light from inside the test chamber.

Sample temperature is controlled through two devices, the variable temperature displacer and Nichrome wire heater. The variable temperature displacer is a stopper of specific diameter inserted into the tube leading from the liquid nitrogen buffer volume to the top of the sample holder. Its purpose is to restrict the flow of nitrogen onto the top of the sample holder, thus slowing the cooling process, reducing heat transfer, and slowing evaporation of liquid nitrogen coming into contact with the hotter sample holder. As liquid nitrogen trickles past the variable temperature displacer, the sample mount and

sample (which is thermally attached to the holder) cool down. A Nichrome wire heater is wrapped around the upper portion of the sample holder to introduce heat into the system and raise the temperature of the sample and holder. There is also an RTD temperature sensor in the top of the sample holder. The heater and RTD are attached to a temperature controller, which applies current to the heater when the temperature from the RTD becomes lower than the desired set point. In order to conserve liquid nitrogen, it is desirable to have the smallest possible flow rate past the displacer while still cooling at a sufficient rate to maintain the desired cryogenic temperature. Several displacers are used, each sized for use over a specific range of cryogenic temperatures (i.e. one for use above 100 K, one for use above 150 K, etc.). With use of the proper displacer and proper filling procedures (see Section 6.2.9), desired temperatures can be maintained for several hours. Actual test time is much less since gas is repeatedly introduced into the test chamber, significantly increasing heat transfer out of the unit thus increasing the rate of liquid nitrogen depletion. Under continuous calibrations, the unit can remain at temperature for approximately ½ hour when using the proper displacer and procedures.

### 6.2.3 Emission Intensity Measurement

The emission intensity of the paints was measured using a Photomultiplier tube (PMT) from EMI corporation. The light emitted from the sample was collected by a large lens and the image focused onto the PMT through a long-pass glass/interference optical filter. The filter cut-off frequency was determined by wavelength of the particular paint's emission. PMT output was passed through a 30 Hz cutoff low pass digital filter to eliminate any higher frequency fluctuations such as 60 Hz line noise. The output of the digital filter was connected to a PC equipped with a 12-bit analog-to-digital (A/D) converter board (DAS-1800).

### 6.2.4 Sample Temperature Measurement and Control

Sample temperature was controlled using an Omega CN-76000 temperature controller. The controller used an RTD located above the sample holder to measure the

temperature of the sample mount assembly. It was assumed that the aluminum sample block was in thermal equilibrium with the copper sample mount assembly and thus the RTD temperature was equal to the sample surface temperature. To control temperature, the CN-76000 provided a reference signal to the Nichrome wire heater power supply, which activated a relay that closed the circuit to send current through the heater. Use of the controller in conjunction with a properly sized liquid nitrogen displacer enabled sample temperature to be controlled to within  $\pm 2^{\circ}\text{C}$ .

### 6.2.5 Pressure Measurement and Control

Absolute pressure in the test chamber was measured with an Omega PX-142 absolute pressure transducer in conjunction with an Omega DP-41 indicator. The transducer was capable of measuring 0-15 PSI absolute pressure with a 1 % F.S. error. The DP-41 indicator was connected to the data collection PC through a RS-485 serial port connection.

Test chamber pressure is controlled using the valve panel depicted below in Figure 6.3. Vacuum can be pulled on the cryostat vacuum jacket by opening ball valve 1. Once vacuum exists in the vacuum jacket, it can be sealed by the valve on the cryostat itself and by closing ball valve 1. Vacuum can be pulled in the cryostat test chamber by opening ball valves 2, 3, and 4 and the needle valve. The test gas enters the chamber through the lower line and valve system. With ball valve 4 open and slightly opening then closing the needle valve, small changes in test chamber pressure can be produced. See section 6.2.9 for a complete description of the operation of the valves to produce the desired environments in the test chamber.

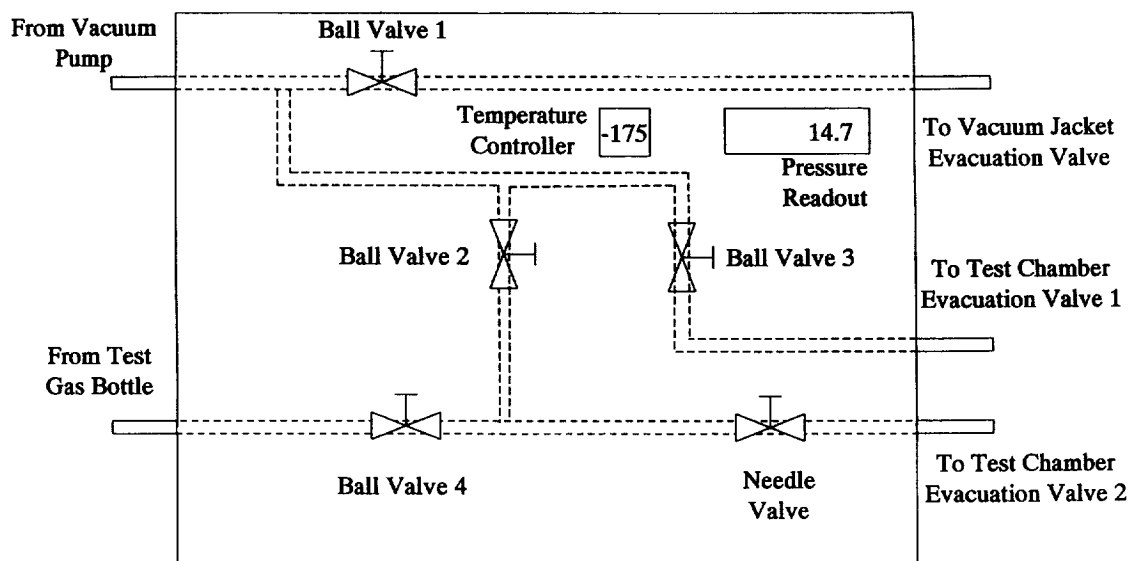


Figure 6.3: Valve Control Panel

#### 6.2.6 Data Collection

Calibration data was collected using a PC via LabView® software. The computer reads voltage from the PMT and voltage from the photodiode via DAS-1800 A/D board and reads pressure from the DP-41 indicator via the serial port. Each data point is taken manually with the LabView® program. All data points for the test are corrected for laser intensity fluctuations and displayed graphically by the program in intensity ratio form.

#### 6.2.7 Test Gasses

In order to calibrate cryogenic PSP's under the low oxygen partial pressures that are encountered in cryogenic wind tunnel testing, specialized test gasses were needed in order to achieve accurate resolution in the region of interest. These specialized gasses were dry mixtures of oxygen and nitrogen. The gasses available were 100 PPM, 250 PPM, 500 PPM, 0.1 %, 0.5 %, 1.0 %, and 2.0 % oxygen with the balance nitrogen, and dry air (21 % oxygen). Each gas was used to calibrate each sample between vacuum and 14.7 PSI. This allowed for proper resolution of the low partial pressures seen in cryogenic wind tunnel tests where oxygen concentrations are between 100 and 1000 PPM.

### 6.2.8 Vacuum Pump

An Edwards E2M0.7 rotary vacuum pump was used to evacuate the test chamber of the cryostat. The pumping capacity of the pump is  $1.1 \text{ m}^3/\text{hr}$  and the lowest observed pressures in the test chamber were less than 0.1 PSI.

### 6.2.9 Calibration Procedure

First, the test section is purged and evacuated several times with dry nitrogen using the procedure described below, to remove any ambient moisture or oxygen. Following the final purge, the test section is evacuated and the cryostat lower chamber evacuation valves closed (see Figure 6.2). The temperature controller is set to a value lower than 88 K so that the heater does not turn on during the cool down process. Next, liquid nitrogen is poured into the fill hole through a funnel until liquid is seen to be steadily streaming from the vent. At this point filling is stopped until the cryostat reaches its lowest temperature of approximately 88 K (about five minutes). Then more liquid is poured in to replace that evaporated during the final stage of the cool down. Once the buffer volume is full, the variable temperature displacer is inserted through the fill hole and adjusted so that it rests approximately 0.25 inches above the top of the sample holder (see Figure 6.2). This will slow the flow of liquid nitrogen to the top of the sample holder, allowing for slower rates of cooling while under constant temperature control.

With the sample at its lowest temperature and the cryostat readied for the test, the hair dryer is activated to alleviate condensation on the window, which may arise when the test gas is in the chamber. The temperature controller is set to the desired temperature and heating begins until the set point is reached and temperature control initiated. Then, the desired test gas is connected to the valve panel. Once above oxygen condensation temperature ( $\sim 90 \text{ K}$ ), ball valves 2 and 3 and the needle valve (see Figure 6.3) are now opened to attain vacuum in the lines leading to the cryostat, allowing the cryostat lower evacuation valves to be opened. Next, the needle valve is set to a slightly open position and ball valves 2 and 3 are closed and ball valve 4 opened to allow test gas to flow into

the test chamber until a pressure of ~14.7 PSI is attained. Ball valve 4 is then closed. Next ball valves 2 and 3 are opened again to pump out the gas in the chamber. This purge process is completed 4-5 successive times, leaving the chamber at vacuum. This ensures the composition of the residual gas inside the test chamber is indeed the intended composition. It should be noted that the test gasses should be used in order from lowest oxygen concentration to highest so as to have the paint at it's brightest intensity at the start of the calibration. The PMT supply voltage is then set to yield the highest resolution and a dark current data point is taken.

With the desired temperature attained and the test section at vacuum (with any residual gas being of the proper composition), the calibration can begin. With all panel valves in the closed position, ball valve 4 is opened so that test gas pressurizes the system up to the needle valve. An initial data point is taken, followed by the slight opening then closing of the needle valve to increase the pressure in the test section. A new data point is then taken and the process continued until the desired ending pressure is achieved (typically ~14.7 PSI).

Following this, the test chamber is evacuated as described above and the next desired test gas is connected to the valve panel. The chamber is purged 4-5 successive times as described above and the next calibration can be completed. The overall process can be continued until all test gases have been calibrated or the liquid nitrogen in the buffer volume is exhausted, whichever comes first. If the liquid nitrogen needs to be re-filled prior to having tested all gases, the test chamber should be brought to vacuum, closed off at the cryostat lower evacuation valves and the temperature controller disengaged. Following this, the liquid nitrogen can be refilled as described above without having to change any settings of additional electronic equipment such as the PMT. It should also be noted that care should be taken not to expose sensitive equipment, such as the PMT, to excess light while refilling the liquid nitrogen. Another important consideration is to make every effort to conserve the liquid nitrogen in the buffer volume. Time at cryogenic temperatures can be extended by always topping off the LN<sub>2</sub> level after the cryostat has reached it's coldest temperature and also keeping the test chamber at vacuum as much as possible so as to reduce heat transfer to the outside.

### 6.3 Calibration Results

A total of 22 paints were fashioned and calibrated during this research. Some paints were chosen as a result of the initial feasibility tests, others were synthesized using new methods in an effort to get the luminescent molecules deposited on the surface using little or no polymer. Because the binder was observed to have a large impact on PSP performance, results are organized by binder. In some cases, several different luminescent molecules were tested using the same type of binder. Although some results show non-linear behavior, data is plotted in the generally accepted Stern-Volmer form. The presentation in the following sections focuses primarily on the region of interest in cryogenic wind tunnel testing. More specifically, the region of interest includes temperatures of 150 K and 100 K and oxygen partial pressures between 0 and 100 Pa. Calibration data for oxygen partial pressures up to those found in the standard atmosphere can be found in Appendix B.

#### 6.3.1 Anodized Aluminum

[Ru(ph<sub>2</sub>-phen)<sub>3</sub>] was deposited on the surface of pure aluminum and 2024 aluminum alloy using the anodizing process described in Section 4.1.3.1. Coatings were prepared by Hirotaka Sakaue of the Purdue University Aerospace Sciences Lab. Both coatings exhibited non-linear behavior and comparison of the room temperature response of the two paints shows that the coating on pure aluminum appears to exhibit better sensitivity, as shown below in Figure 6.4.

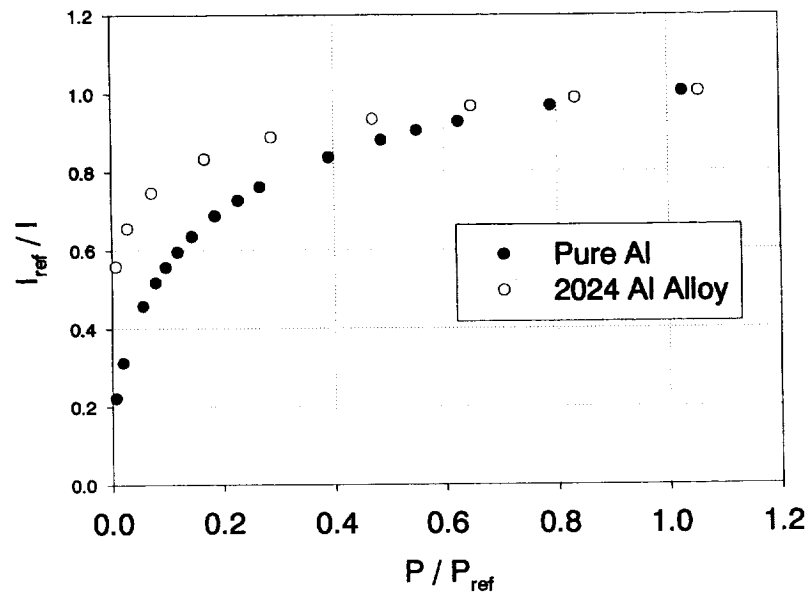


Figure 6.4: Stern-Volmer Response of Anodized Aluminum Paints

The data above was taken at room temperature using atmospheric pressure in PSI as the reference condition.

Under cryogenic conditions, examination of the overall response (shown in Appendix B) shows that the coating on the 2024 Alloy appears to respond better than pure aluminum at 150 K and the responses are the same at 100 K. This is contrary to comparisons made at standard conditions. Comparisons of the two responses in the region of interest for cryogenic wind tunnel testing are shown below in Figure 6.5 and Figure 6.6.



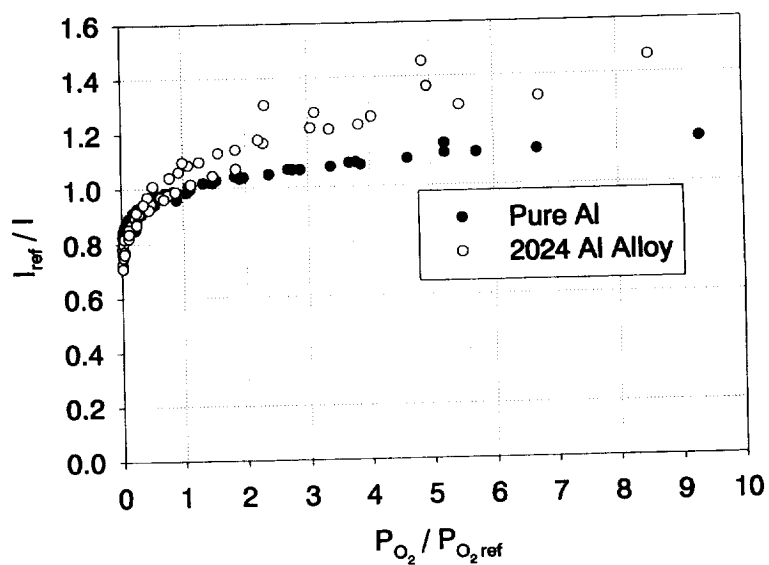


Figure 6.5: Comparison of Anodized Coatings at 150 K

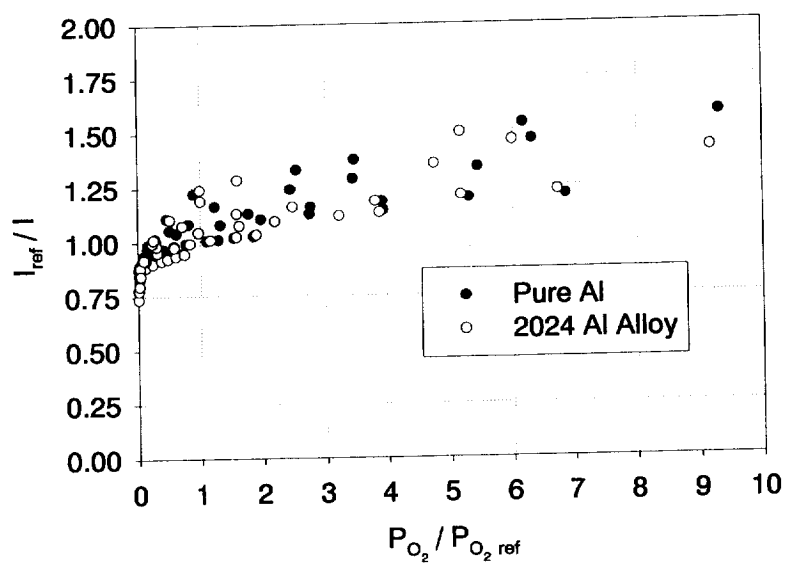


Figure 6.6: Comparison of Anodized Coatings at 100 K

In both figures, reference conditions are taken at an oxygen partial pressure of 14.0 Pa. At 150 K, the coating on the 2024 alloy shows approximately two times the sensitivity as the coating on the pure aluminum. At 100 K, there is no discernable difference between the two coatings, as the data is too noisy to give any insight into the response at this temperature.

### 6.3.2 GE RTV/Silica Gel

Luminescent coatings using GE RTV have been used in the past by several researchers<sup>16,17</sup>. The preliminary experiments described in Section 6.1 showed that paints with GE 110 RTV as the binder responded to oxygen at cryogenic temperatures when silica gel particles were added to the mixture. It was postulated that the addition of the silica gel increases the diffusivity of the coating. Using  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  or PtTFPP as the sensor, paints with increasing concentrations of silica gel particles were tested. The specific binders tested were:

- 5 mg  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$ /5 mL RTV/0.5 g silica gel
- 5 mg  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$ /5 mL RTV/1.0 g silica gel
- 5 mg  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$ /5 mL RTV/2.5 g silica gel
- 10 mg PtTFPP/5 mL RTV/2.0 g silica gel

None of the coatings responded in the range of interest for cryogenic wind tunnel testing.

While none of the luminescent coatings responded at cryogenic conditions, the coatings did respond at temperatures above  $-60^\circ\text{C}$ . Although not cryogenic, this temperature range is of interest for conducting in-flight pressure measurements. A comparison of the response for the  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$ /5 ml RTV/X g Silica Gel coatings is shown below in Figure 6.7.

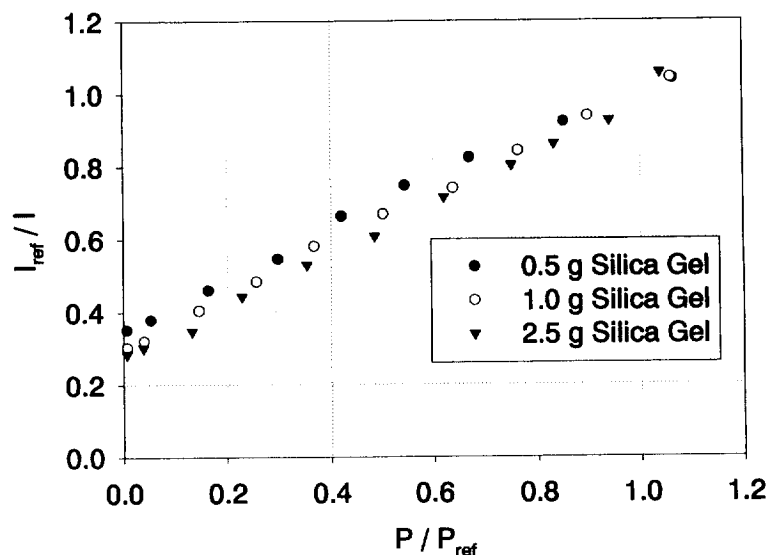


Figure 6.7: Comparison of  $[\text{Ru}(\text{ph}_2\text{-phen})_3]/5 \text{ mL RTV}/X \text{ g Silica Gel Paints}$

The above figure is in Stern-Volmer form with reference conditions taken at standard atmospheric pressure. The calibrations were done using air as the test gas at a temperature of  $-30^\circ\text{C}$ . The figure indicates that the addition of silica gel particles to the binder causes a small increase in the slope of the response. It should also be noted that the addition of silica gel causes the coating to become more powdery and harder to keep attached to the surface. Matrix calibrations for each paint at  $-30$ ,  $-20$ ,  $-15$ , and  $25^\circ\text{C}$  are given in Appendix B. Another concern with this paint was hysteresis. The paints did not appear to return to their starting intensity once the test chamber was evacuated following calibration. Further investigation revealed that the paints apparently had a slow desorption rate of oxygen and that the  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  based paints would indeed return to the starting intensity after 2-3 minutes under vacuum. Adsorption of oxygen seemed to be a much faster process with responses registering within 10 seconds of the introduction of additional gas. A coating of PtTFPP/5 mL RTV/2.0 g silica gel was also tested, but exhibited a much slower desorption rate ( $\sim 15 \text{ min}$ ) and was deemed unusable.

### 6.3.3 GP-197/Silica Gel

While preliminary experiments showed that coatings using GP-197 as a binder were not very sensitive under cryogenic conditions, the addition of silica gel to the mixture appeared to dramatically increase the sensitivity. The following GP-197/silica gel coatings were prepared and tested under cryogenic conditions:

- 5 mg  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  / 10 mL GP-197/1.0 g silica gel
- 5 mg  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  / 10 mL GP-197/2.0 g silica gel
- 5 mg PtTFPP / 10 mL GP-197/2.0 g silica gel
- 6 mg PtOEP / 10 mL GP-197 / 2.0 g silica gel

Comparison plots in the region of interest are shown below in Figure 6.8 and Figure 6.9. Intensity data are normalized to 1.0 at an oxygen partial pressure of 14.0 Pa.

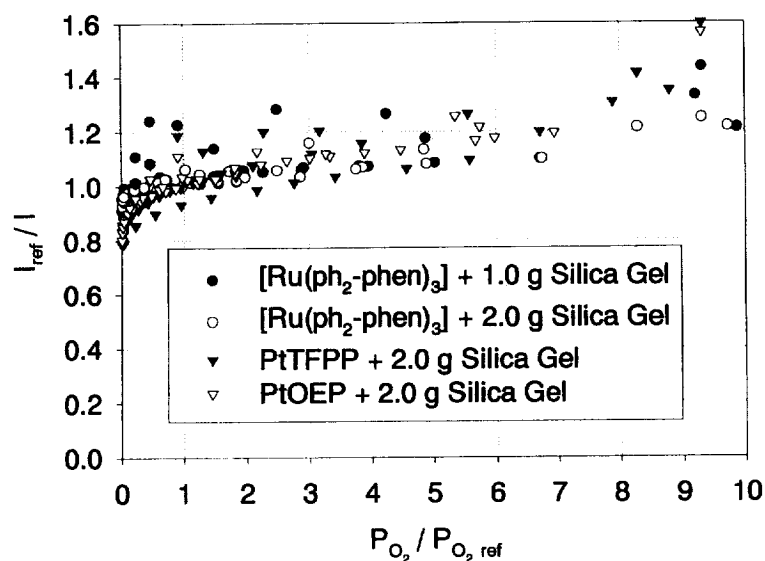


Figure 6.8: Comparison of GP-197/Silica Gel Coatings at 150 K

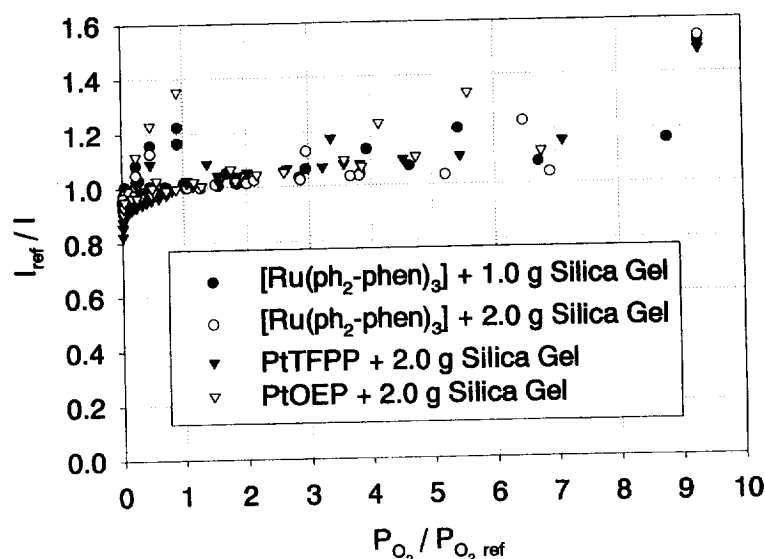


Figure 6.9: Comparison of GP-197/Silica Gel Coatings at 100 K

At both temperatures, no discernable differences can be observed. Resolution is generally too poor for these coatings to be useful. Information from the full range of pressure tested (see Appendix B) shows that these paints could be useful over a much larger range of partial pressures, but cannot provide the proper resolution over the small range needed in cryogenic wind tunnel testing.

#### 6.3.4 Hydrothermal Coating

Two luminescent paints were prepared by Aaron Scroggin of the Purdue University Materials Engineering Department using the hydrothermal coating method described in Section 4.1.3.2. Both used  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  as the luminescent pressure sensing molecule. One coating used 99%  $\text{TiO}_2$  and 1% polymer, the other 80%  $\text{TiO}_2$  and 20% polymer. Figure 6.10 below is a Stern-Volmer comparison of the two coatings at room temperature. Data is normalized to 1.0 at 14.7 PSI.

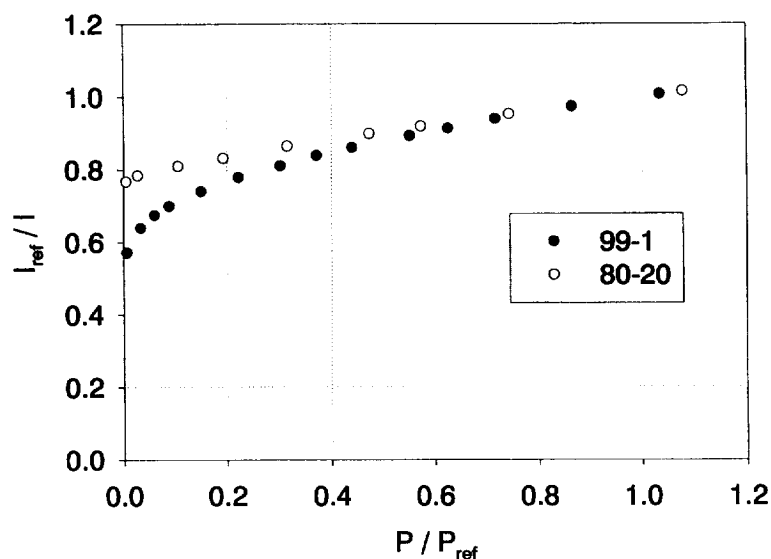


Figure 6.10: Comparison of Hydrothermal Coatings at Room Temperature

It can be seen from Figure 6.10 that slope of the response increases with decreasing amounts of polymer. Unfortunately, when tested at 150 K the coating containing 20% polymer did not respond and the coating with 1% polymer only showed a 5% drop in intensity between vacuum and atmospheric pressure air. Thus, neither coating could be considered further for use as a cryogenic PSP.

### 6.3.5 Polystyrene

Attempts were made to create paints using polystyrene as the binder. Coatings using  $[Ru(ph_2-phen)_3]$  in polystyrene and PtTFPP in polystyrene were created. The coating containing  $[Ru(ph_2-phen)_3]$  did not respond to oxygen at all. The PtTFPP/polystyrene coating showed the following response to air at room temperature (data is normalized to 1.0 at 14.7 PSI).

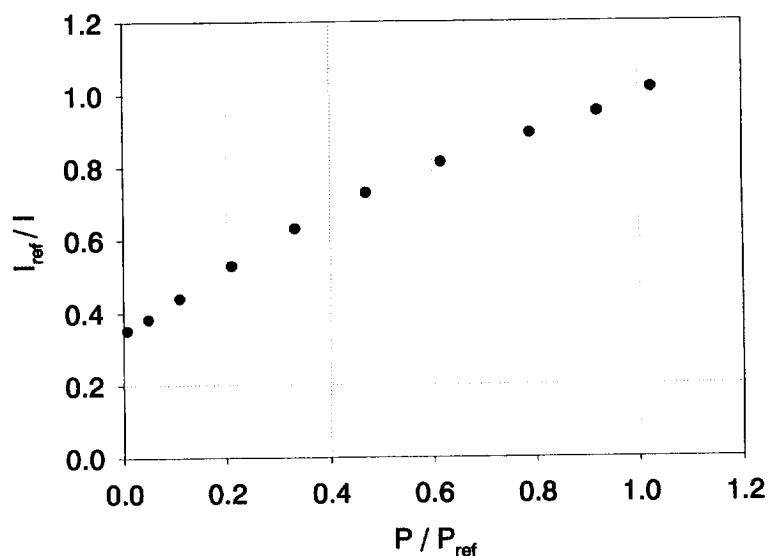


Figure 6.11: Stern-Volmer Response for PtTFPP/polystyrene in Air at 25 °C

The response follows the Stern-Volmer theory well and shows good sensitivity between vacuum and 15 PSI air. The coating, however, did not show any response to oxygen below a temperature of  $-25$  °C and showed no temperature response below a temperature of  $-50$  °C. Thus, this paint was of no use as a cryogenic PSP or TSP.

### 6.3.6 Sol Gel

Samples of  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  in a Sol Gel binder were obtained from Jeff Jordan of Innovative Scientific Solutions, Incorporated (ISSI). Room temperature calibrations in air yielded the following Stern-Volmer response normalized to 1.0 at 14.7 PSI.

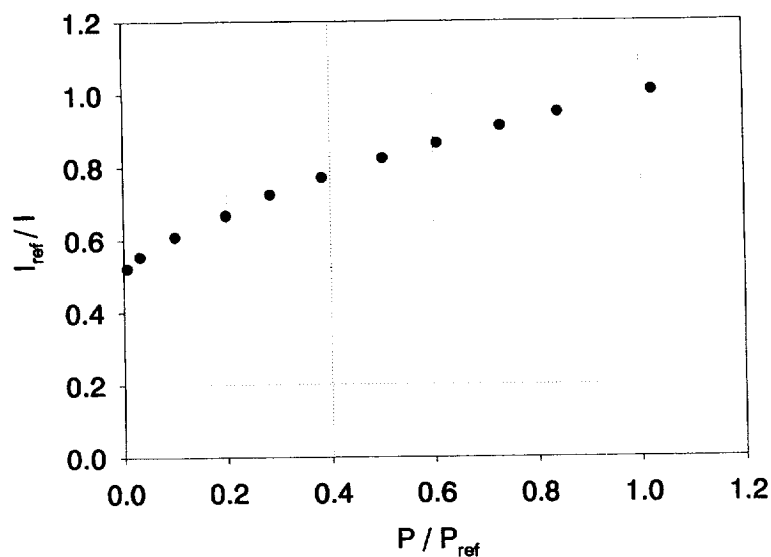


Figure 6.12: Stern-Volmer Response of  $[Ru(ph_2-phen)_3]$  in Sol Gel (25 °C, air)

This result agreed with similar tests on the sample conducted at ISSI. The sample however, did not respond to oxygen at temperatures below  $-70$  °C.

### 6.3.7 Tape Casting

The Tape Casting method described in Section 4.1.3.4 was used to create PSP's using  $[Ru(ph_2-phen)_3]$  or PtTFPP as the luminescent molecule. These coatings were prepared by A. Scroggin of the Purdue University Materials Engineering Department. Room temperature calibrations in air yielded the following responses.



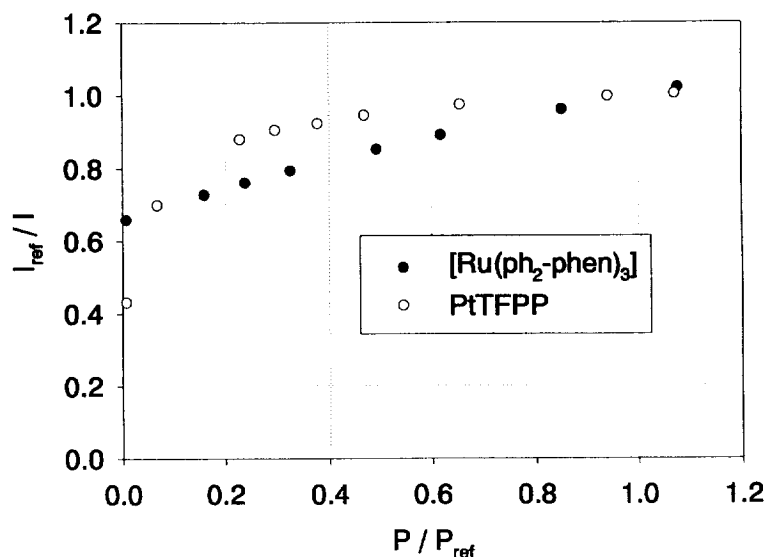


Figure 6.13: Stern-Volmer Responses of Tape Cast PSP's (25 °C, air)

While the  $[Ru(ph_2-phen)_3]$ /Tape Cast paint shows a linear response, the PtTFPP/Tape Cast paint is highly non-linear below  $P/P_{ref}=0.2$ .  $[Ru(ph_2-phen)_3]$ /Tape Cast shows no response to oxygen below  $-30$  °C. PtTFPP/Tape Cast showed a 20% intensity drop between vacuum and 15 PSI air at 150 K and a 30% intensity drop at 200 K. While this response could be observed and calibrated, the paint is of little use in cryogenic wind tunnel testing as proper resolution of the low oxygen partial pressures cannot be obtained.

### 6.3.8 Thin-Layer Chromatography Plate

Based on results of the initial feasibility experiments,  $[Ru(ph_2-phen)_3]$ , PtTFPP, and PtOEP where each soaked into standard grade Thin-Layer Chromatography (TLC) plates and calibrated under cryogenic conditions. Room temperature calibrations in air yielded the following results for these three paints.

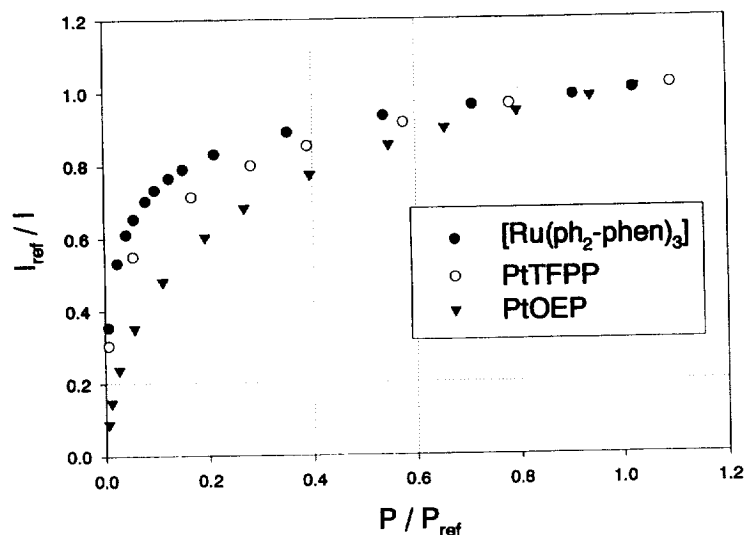


Figure 6.14: Stern-Volmer Response for TLC Based Paints (25 °C, air)

As can be seen above, all three paints show non-linear Stern-Volmer responses. PtOEP shows the steepest slope at low concentrations and  $[Ru(ph_2-phen)_3]$  shows the shallowest. All three paints responded well under cryogenic conditions and Figure 6.15 and Figure 6.16 below show comparisons of the three paints at 150 and 100 K respectively in the region of interest for cryogenic wind tunnel testing.

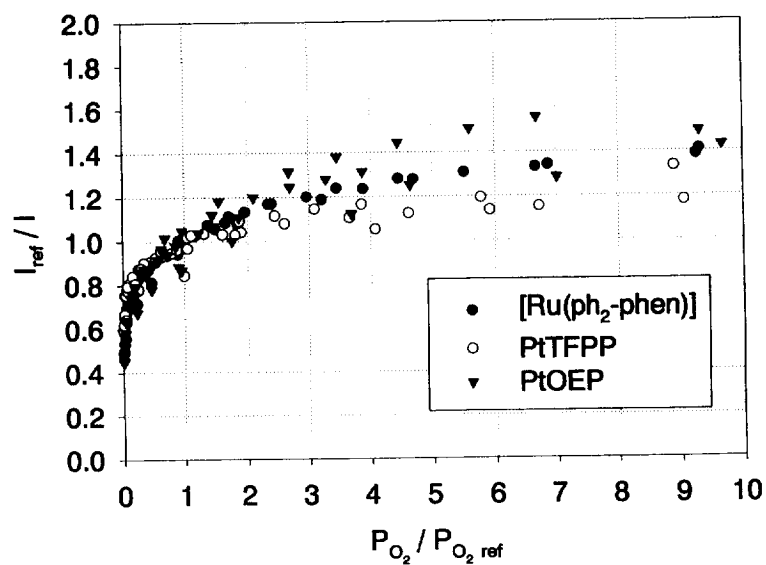


Figure 6.15: Comparison of TLC Based Paints at 150 K

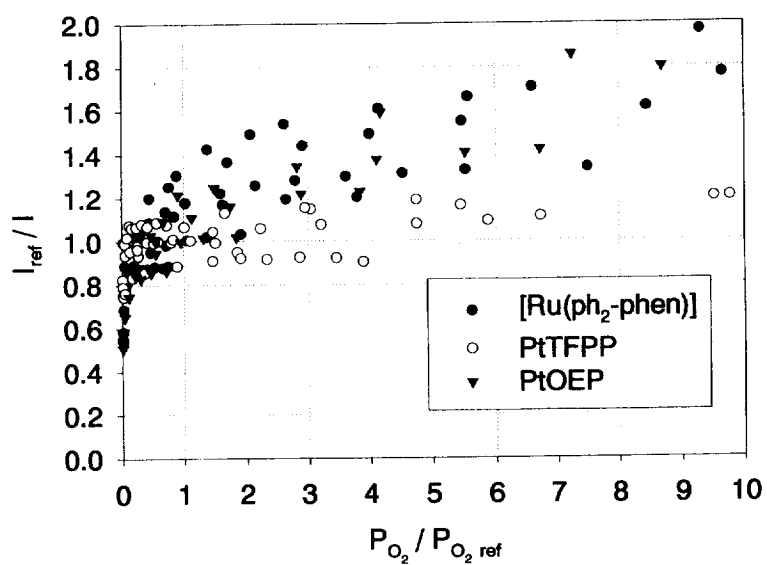


Figure 6.16: Comparison of TLC Based Paints at 100 K

At 150 K, PtOEP/TLC exhibits the largest intensity change over the region of interest. Followed by  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  and PtTFPP. At 100 K, no discernable trends can be observed.

### 6.3.9 Filter Paper

Based on results of the initial feasibility experiments,  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$ , PtTFPP, and PtOEP were each soaked into Whatman filter paper #1 (cat # 1001 042) and calibrated under cryogenic conditions. Room temperature calibrations in air yielded the following results for these three paints.

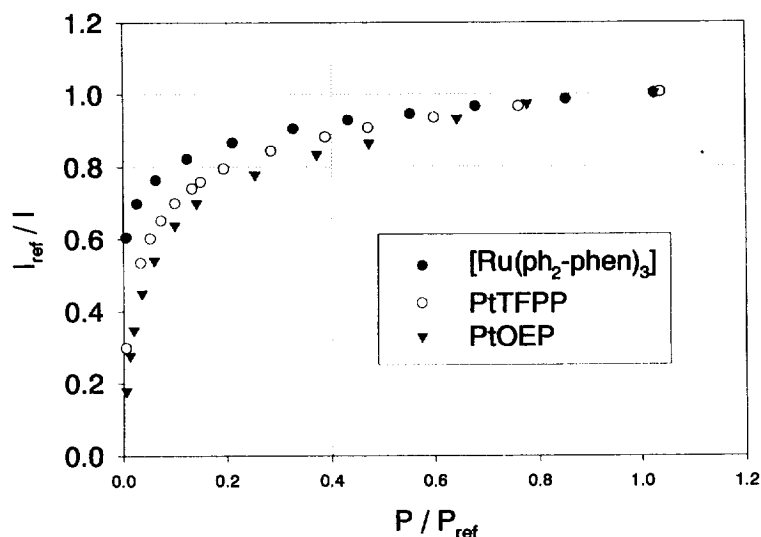


Figure 6.17: Stern-Volmer Responses for Filter Paper Based Paints (25 °C, air)

As with the TLC based paints, the filter paper based paints all show non-linear Stern-Volmer responses under room temperature conditions. PtOEP shows the steepest response at low pressures and  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  shows the shallowest. All three paints responded well under cryogenic conditions. Figure 6.18 and Figure 6.19 below show comparisons of the responses at 150 and 100 K respectively.

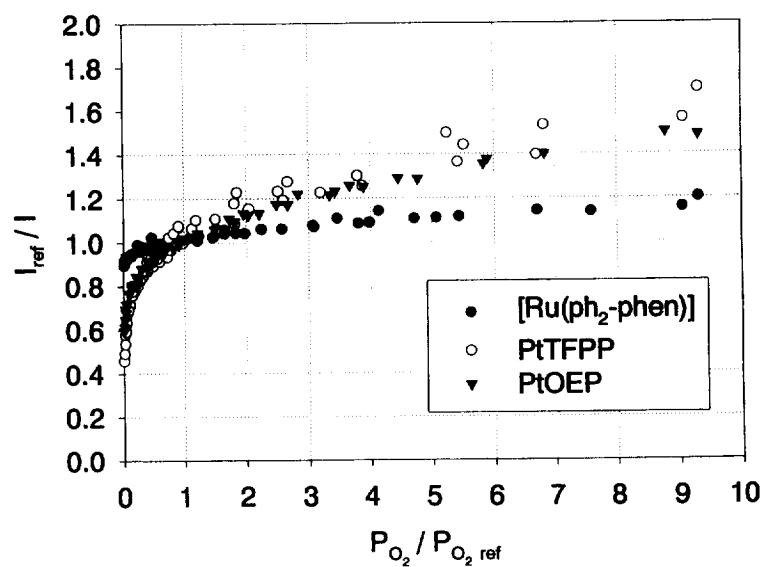


Figure 6.18: Response of Filter Paper Based Paints at 150 K

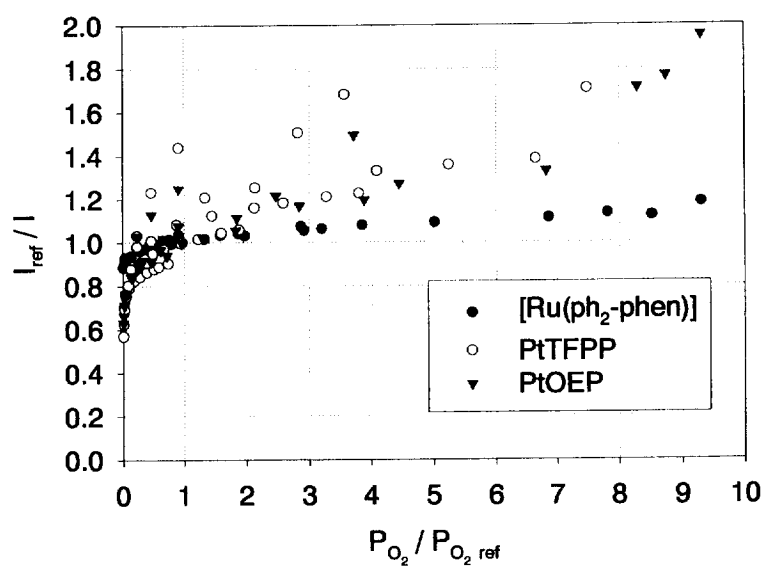


Figure 6.19: Response of Filter Paper Based Paints at 100 K

At 150 K, the PtOEP and PtTFPP paints responded with the steepest slopes and the  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  was considerably shallower. No information could be derived from the response at 100 K.

### 6.3.10 Porous Polyethylene

Attempts were made to create paints using Porex X-7744 porous polyethylene filters. These particular filters had 7  $\mu\text{m}$  pores.  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  did not respond to oxygen when soaked into this material, but PtTFPP did respond at temperatures above  $-75^\circ\text{C}$ . This made it a good possibility for use as a flight test paint, as static temperatures at cruising altitudes are above this temperature. Figure 6.20 below shows a matrix calibration for PtTFPP in Porex for the temperature regime found at a cruising altitude of approximately 20-30,000 ft.

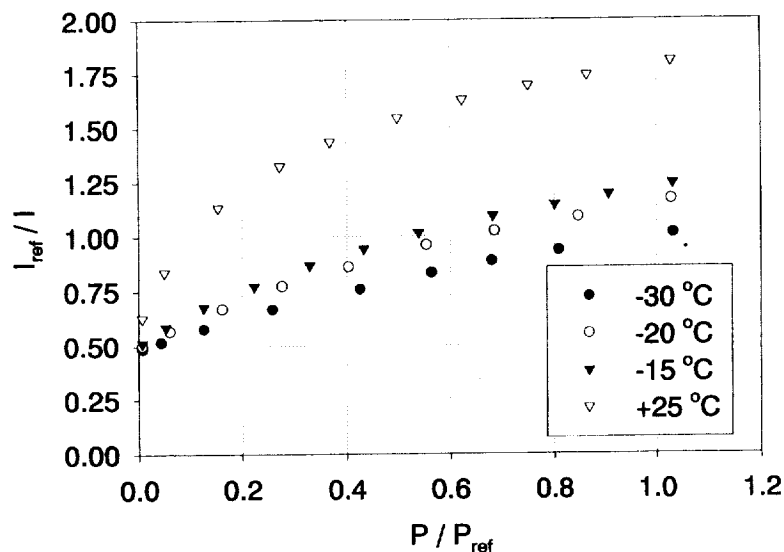


Figure 6.20: Matrix Calibration for PtTFPP in Porex Porous Polyethylene

### 6.3.11 Non-Collapse of Data at 100 K

Of the paints in the preceding sections which responded to oxygen under cryogenic conditions, none proved calibratable at 100 K while several were successfully calibrated at 150 K. A more detailed plot of the calibrations for  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  on TLC at 150 K and 100 K are shown below in Figure 6.21 and Figure 6.22.

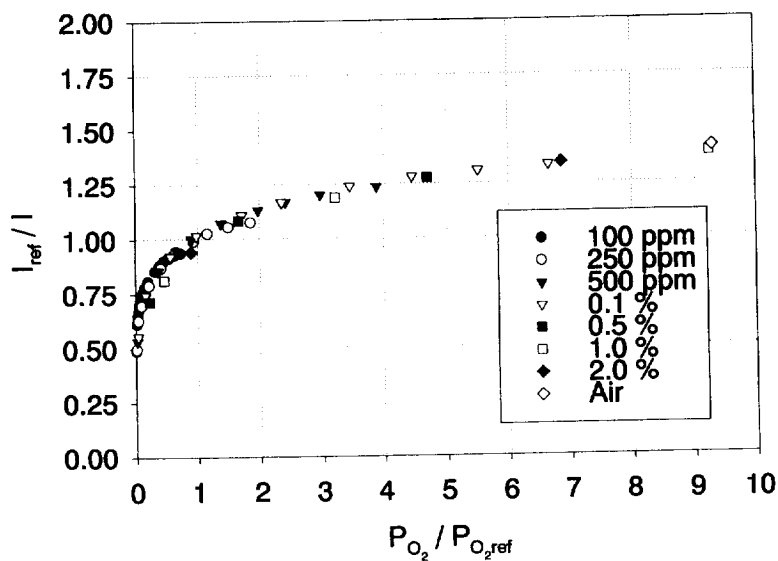


Figure 6.21:  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  on TLC – 150 K

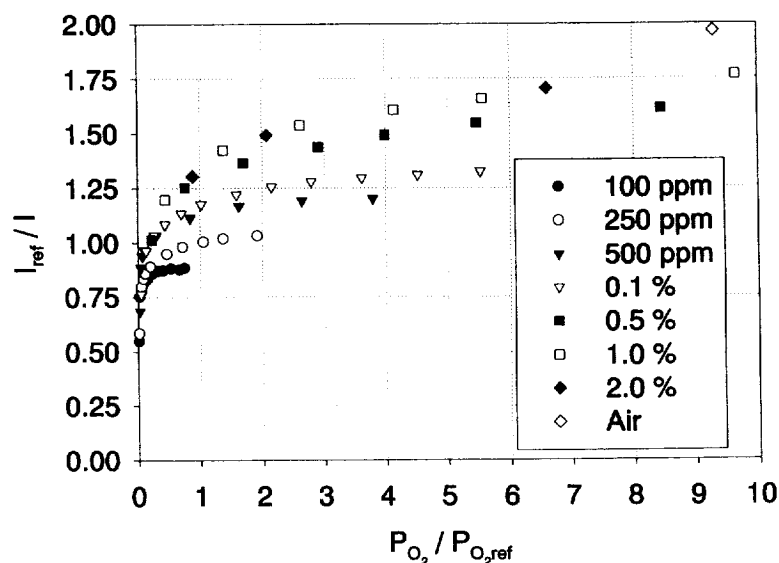


Figure 6.22:  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  on TLC – 100 K

As described in section 5.1.6, different test gasses are used to resolve the small regions of partial pressure that are of interest in cryogenic wind tunnel testing. As discussed in section 3.2, theoretically, the data from different test gasses should collapse onto the same curve when plotted in Stern-Volmer form. The above figures show the data from each test gas. The data at 150 K collapses but the data does not collapse at 100 K. This phenomena was observed in all paints that responded to oxygen in this temperature range. The trend seen in the above data was observed even though individual test gas calibrations yielded repeatable results when normalized to the same reference conditions, as shown below in Figure 6.23. The data is from an anodized sample at 100 K in a 78 % nitrogen, 2 % oxygen gas mixture and is normalized to 1.0 at 14.7 psi static pressure.



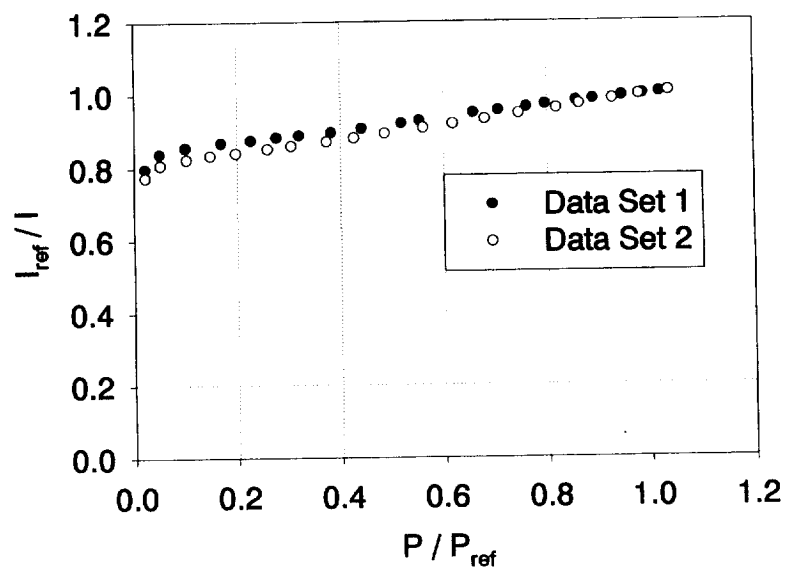


Figure 6.23: Repeated Calibration of Anodized Aluminum, 100 K, 2 %  $O_2$

As an illustration to show this phenomena is not limited by luminophore and binder, Figure 6.24 and Figure 6.25 below show calibration results for PtTFPP on Filter Paper. Additional results are given in Appendix B.

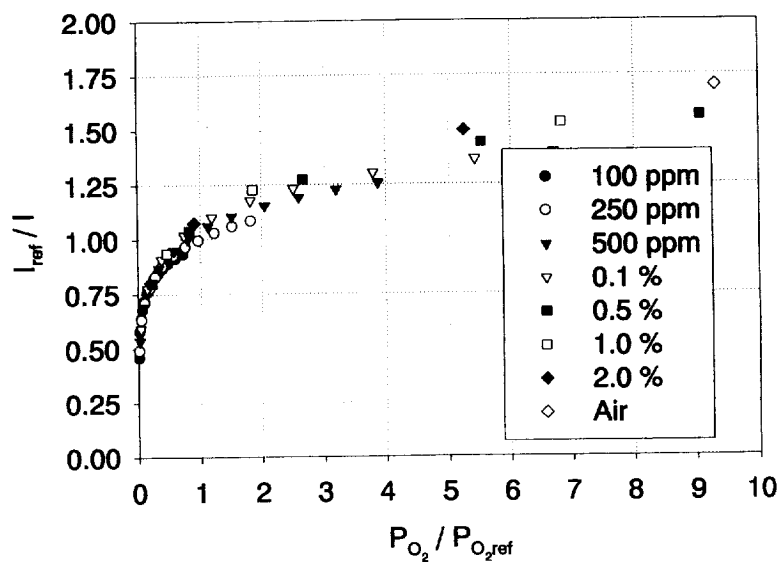


Figure 6.24: PtTFPP on Filter Paper – 150 K

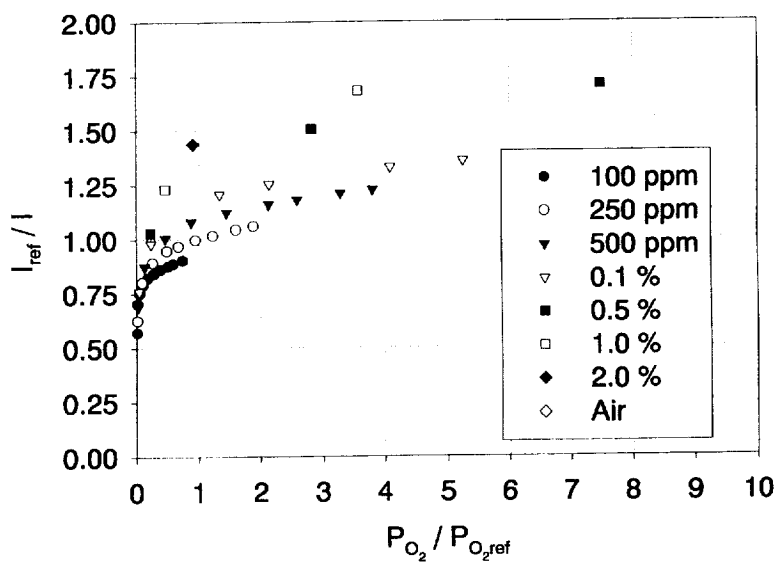


Figure 6.25: PtTFPP on Filter Paper – 100 K

This phenomena has also been observed by researchers at NASA Langley Research Center<sup>20</sup>. There is currently no explanation for this phenomena, however theories include nitrogen adsorption and occupation of quenching sites, condensation phenomena, or anomalies in the porous surface.

#### 6.4 Application – PSP Data in NAL 0.1-m Transonic Cryogenic Wind Tunnel

Several of the cryogenic PSP's discovered during this research were tested in the 0.1-m Transonic Cryogenic Wind Tunnel at the National Aerospace Laboratory (NAL) in Japan<sup>19</sup>. A description of the wind tunnel and operating conditions was given in section 5.3.1. The paints were applied to strips on a circular arc bump model in the wind tunnel. The model had an array of pressure taps along the mid-chord. Oxygen injection provided the quencher for the PSP's. Quencher concentration was monitored using a  $\text{ZrO}_2$  oxygen sensor. Figure 6.26 below shows an *a priori* calibration of  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  in Anodized Aluminum at the 16 pressure tap locations.

##### *a priori* Wind Tunnel Calibration

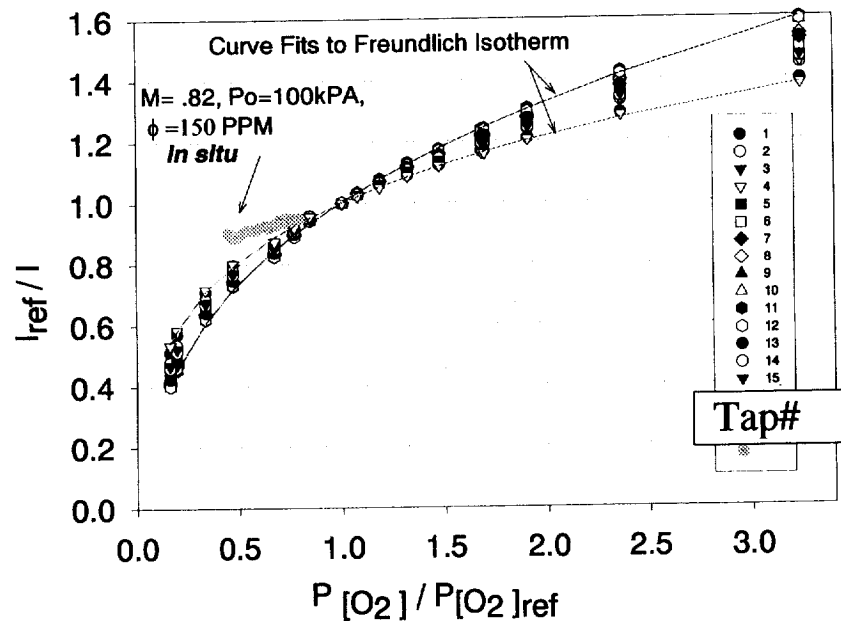


Figure 6.26: *a priori* calibration of  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  in Anodized Aluminum

A  $C_p$  distribution over the bump is shown below in Figure 6.27.

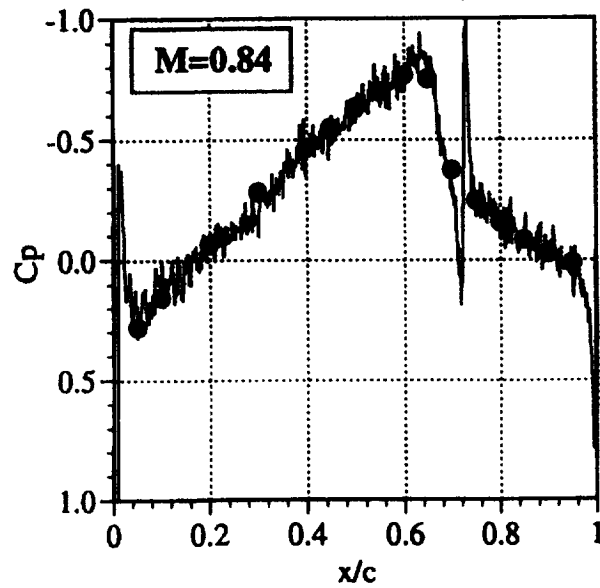


Figure 6.27:  $C_p$  Distribution Obtained from  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  on Anodized Al

The spike at approximately  $0.7 x/c$  is the shadowgraph of the shock wave on the surface of the model. The dots represent pressure data from taps at the corresponding location. From the figure it is seen that the paint data and pressure tap data agree well.

## CHAPTER 7: SOURCES OF ERROR

The accuracy of TSP and PSP measurements depend generally on photochemical properties of the paint and the measurement system used. The error sources can be classified in 2 groups:

- 1) Errors resulting from Photochemical and Photophysical properties of the paint
  - a) Photodegradation
  - b) Hysteresis
- 2) Measurement System Errors
  - a) Unstable illumination source
  - b) Photodetector Noise/Dark Current Effects
  - c) Non-linearity of photodetector response
  - d) Wavelength overlap between illumination source and optical filters
  - e) Leakage of atmospheric air into the test stand

Photodetector noise and illumination intensity fluctuations are random in nature, the remaining sources or error are systematic and must be procedurally addressed. A complete error analysis is difficult to obtain due to the many different components utilized in a TSP or PSP measurement system, however various sources of error can be individually addressed and minimized through proper procedures.

### 7.1 Errors Resulting From Photochemical and Photophysical Properties

#### 7.1.1 Photodegradation

Photodegradation of a luminescent paint occurs when the emission light intensity of the paint decreases with exposure time to illumination light. It is dependent upon illumination intensity, exposure time, and the properties of the luminescent molecule itself. Photodegradation is caused by destructive reactions between singlet state  $O_2$

molecules produced during the quenching process and the luminescent molecules. The Porphyrin family is very sensitive to singlet  $O_2$ , but molecules based on transition metals are not as sensitive.

Previous work<sup>11</sup> has shown that the calibration data for paints exhibiting various degrees of photodegradation roughly collapse onto the same curve through normalization. While this is true, photodegrading a paint is still undesirable since the emission intensity may fall below useful levels for detection. Since photodegradation results from exposure to singlet  $O_2$ , it can be significantly diminished in TSP's when using a binder with low oxygen permeability, which is already desirable. In addition, using minimal amounts of excitation light and limiting exposure time can diminish the effects of photodegradation.

### 7.1.2 Hysteresis

Hysteresis, or repeatability, occurs when calibration data does not match for consecutive calibrations. The causes of hysteresis vary depending on the type of coating being tested.

#### 7.1.2.1 Temperature Hysteresis

Hysteresis in TSP's is mainly a function of the glass transition temperature,  $T_g$ <sup>37</sup>. When temperature of the polymer binder exceeds the glass transition temperature, the matrix undergoes a non-reversible transition from a relatively brittle glassy state to a soft and rubbery state. This transition effects the temperature dependence of the luminescent paint<sup>11</sup>. Either maintaining a temperature below the glass transition of the binder or pre-heating the binder to a temperature above  $T_g$  prior to calibration can eliminate the effects of temperature hysteresis. Depending on calibration conditions, either method of eliminating temperature hysteresis was used in this research.

#### 7.1.2.2 Pressure Hysteresis

Hysteresis in PSP's can be caused by several factors. Glass transition causes hysteresis much the same as in TSP's and was avoided in the same manner as outlined in

the above section. In addition, moisture can soak into the coatings containing silica and cause hysteresis. The water molecules occupy quenching sites on the surface that could otherwise be inhabited by a quencher. This decreases the paint's intensity and changes the calibration. Typically paints containing silica must be stored in dry conditions (in a desiccator for example) and used within 72 hours before significant effects of moisture adsorption are observed. Similar aging effects have been observed with the anodized coatings, but this has not been directly correlated with moisture.

As a check for hysteresis which may have occurred during the calibration, room temperature calibrations in air were performed prior to and after exposure of each paint to cryogenic conditions. No significant changes in response were observed in any of the paints. Figure 7.1 below is an example of one of these checks. The calibration is for PtOEP on TLC plate at room temperature. Data is normalized to an intensity ratio of 1.0 at 14.7 psi static pressure. As can be seen from the data below, only small variations in the response were observed.

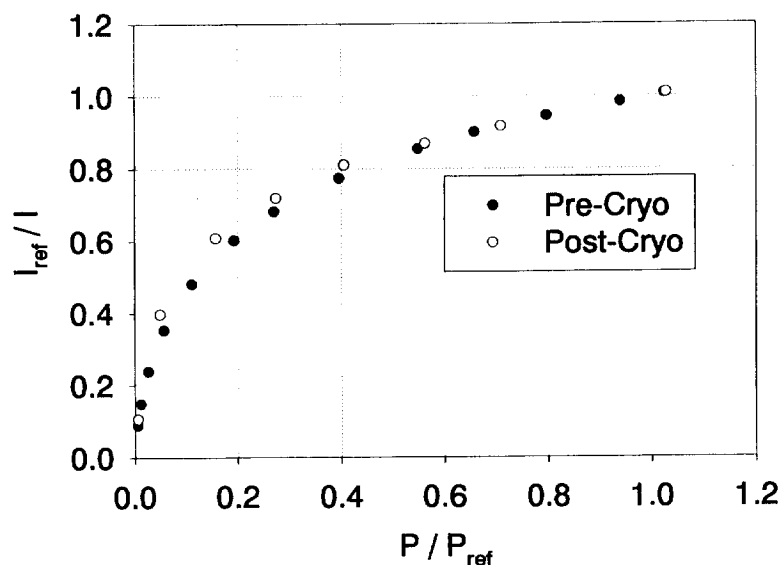


Figure 7.1: Hysteresis Check for PtOEP/TLC

As an additional check for hysteresis at low oxygen concentrations, the test chamber was purged repeatedly with nitrogen and brought to vacuum prior to and after each PSP calibration. Intensities were noted and if any significant differences ( $> 3\%$ ) were detected, calibrations were repeated until repeatability was observed. Additionally, pre- and post-cryogenic exposure calibrations were conducted and results compared to observe if any hysteresis effects occurred. It was noted that some paints, such as those using GE RTV + silica gel binders, exhibited very low rates of desorption of oxygen while at cryogenic conditions. While these paints returned to the initial intensity after a significant time period ( $>15$  min), the effect could be mistaken for hysteresis.

## 7.2 Measurement System Errors

### 7.2.1 Unstable Illumination Source

Fluctuations in the illumination source can cause associated fluctuations in emitted luminescence from the paint. In most cases in this research, the laser illumination sources had intensity fluctuations of less than  $1.0\%$ , which was stable enough to not affect measurements. Since PSP's often exhibit less sensitivity to oxygen compared to TSP's sensitivity to temperature changes, laser emission was monitored and recorded for PSP calibrations. Fluctuations in laser intensity were corrected for by dividing each paint intensity reading by the associated laser emission intensity for that reading. For TSP calibrations, laser power was simply monitored for significant variations ( $> 1.0\%$ ) where possible.

### 7.2.2 Photodetector Noise/Dark Current Effects

In addition to signal noise, there are two major sources of noise in photomultiplier tubes, shot noise and Johnson noise. Shot noise (dark noise) originates from the individual photons which eventually impact the PMT anode and is associated with the



thermionic component of dark current<sup>38</sup>. The rms noise current from shot noise is given by:

$$I_{rms} = \mu(2ei_d B)^{1/2} \quad (7.1)$$

where  $\mu$  is the photomultiplier gain,  $e$  is the charge on the electron,  $i_d$  is the dark emission current from the photocathode, and  $B$  is the bandwidth of the observation.

Johnson noise is thermal noise associated with the load resistance of the PMT and is given by the following:

$$I_{rms} = (4kTB/R)^{1/2} \quad (7.2)$$

where  $k$  is Boltzman's constant,  $T$  is the temperature in Kelvin,  $R$  is the load resistance, and  $B$  is the bandwidth of the observation.

From equation (7.2) it can be seen that the Johnson noise is dependent on the square root of the load resistance, assuming temperature is fairly constant. It has been shown that a load resistance of 50 ohms or greater will reduce the Johnson noise to a point where the shot noise (dark noise) far exceeds the Johnson noise<sup>38</sup>.

Signal noise can be modeled with the following equation:

$$I_{rms} = \mu(2ei_s B)^{1/2} \quad (7.3)$$

where  $\mu$  is the photomultiplier gain,  $e$  is the charge of an individual electron,  $i_s$  is the signal current, and  $B$  is the bandwidth of the measurement.

Noting that there is no correlation between shot noise and noise in the signal current, the noises may be added by summing their squares, yielding a total rms noise current of:

$$I_{rms} = \mu[2e(i_d + i_s)B]^{1/2} \quad (7.4)$$

In all cases, the PMT was operated at detection levels above that of the dark current, thus signal noise was the main contribution to overall noise. Regardless, digital low-pass filtering of the signal and averaging of A/D readings reduced both signal noise and shot noise in the system.

While dark current noise has minimal effects on the value of rms voltage readings, it can effect calculations of slope when using ratios to plot calibration data. Thus, dark current readings were taken at the start of each calibration and the rms voltage subtracted

from each reading prior to ratioing. Dark current rms voltage values were typically on the order of 1,000 times less than the signal voltage levels.

### 7.2.3 Non-linearity of Photodetector Response

Care must be taken when using a PMT to operate the device within its linear response range and also to not saturate the device. Linearity of the response is a function of incident light and supply voltage. As long as there is sufficient incident light and the supply voltage is set to an acceptable level, the response will be linear. This was checked prior to each calibration by reducing incident light by one half and observing if the voltage from the PMT dropped by approximately half. This test also will show if the device is saturated, as the signal would drop less than half. In addition, incident light can be slightly increased to see if signal increases, indicating the device is not saturated.

### 7.2.4 Wavelength Overlap Between Illumination Source and Optical Filters

All optical filters allow "bleed through" of wavelengths beyond the cut-off frequency of the filter. This could cause the PMT to detect some intensity associated with excitation light, which has passed through the optical filter. Care must be taken to use paints with sufficient Stokes shift to effectively filter out the excitation source intensity. Each excitation source and filter combination was tested by illuminating a piece of bare aluminum and checking the photodetector signal compared to a dark reading. In all cases, the effect of overlap was found to be negligible.

### 7.2.5 Leakage of Atmospheric Air Into the Test Stand

Since paints are sensitive to both oxygen and temperature, leakage of additional oxygen into the test stand can affect calibration results. The effects of leakage were not considered significant in temperature calibrations as the binders were relatively impermeable to oxygen and a trickle flow of nitrogen was maintained through the test stand.

Leakage, however, becomes a significant source of error for pressure calibrations especially since some of the paints being tested were highly sensitive under cryogenic conditions. Thus leakage of atmospheric air ( $[O_2]=21\%$ ) into the test chamber where much lower oxygen concentrations are present, can produce substantial changes in paint intensity. For example, the most sensitive PSP in this work showed a 60% change in intensity ratio over a 0.018 PSI change in oxygen partial pressure. Simple calculations using Dalton's Law shows that only 0.014 PSI leakage of atmospheric air into the test chamber could produce a 10% change in emission intensity. This amount of pressure increase is well within the measurement error of most pressure transducers and is thus considered undetectable without the purchase of expensive equipment. In lieu of purchasing better equipment, a simple test was conducted to observe any leakage effects. The most sensitive paint (PtOEP/filter paper) was placed in the test rig under vacuum at 150 K. The system was sealed by closing the proper valves on the control panel, just as it would be in a normal calibration. Paint intensity was monitored for a period of 10 minutes. The results are shown below in Figure 7.2.

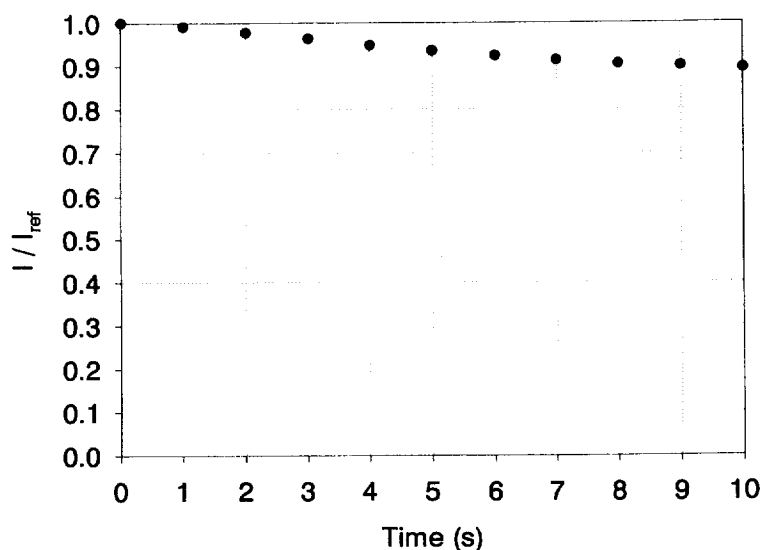


Figure 7.2: Intensity change in PtOEP/Filter Paper due to leakage

As can be seen from the figure, paint intensity changed by 10% over the 10 minute period, thus some leakage was assumed to exist. Using the calibration results for that paint, the leak rate is found to be 0.0014 PSI/min. Since data is taken with several test gasses and the test chamber purged between each test, the time scale of interest is the time it takes to conduct measurements with each test gas. It takes approximately 5 minutes to take data with each test gas, thus we are interested in the measurement error due to leakage over this period of time. Assuming leak rate remains constant throughout the 5 minute period, the error at the end of the 5 minutes is 5%. As outlined in section 5.1.6, measurements with each test gas start at vacuum and end near atmospheric pressure. Since the leak rate will decrease as the pressure differential between the test chamber and atmosphere decreases, the actual error is less.

## CHAPTER 8: CONCLUSIONS AND RECOMMENDATIONS

While the use of temperature- and pressure-sensitive paints to make surface temperature and pressure measurements on aerodynamic models is well documented at near standard atmospheric conditions, little work has been done to extend this application to cryogenic wind tunnel testing. The objective of this research is to prove that extension possible through the design and calibration of temperature- and pressure-sensitive paints that respond under cryogenic conditions. Results indicate that extension of the technology into cryogenic wind tunnel testing is plausible and calibrations conducted under these conditions have been presented.

Many cryogenic temperature-sensitive paints were calibrated and found to respond in the region of interest for cryogenic testing (-175 to -50 °C). The [Ru(trpy)<sub>2</sub>] family of luminescent molecules was found to yield high intensity paints with excellent sensitivity in the region of interest. Through changes in the ligand structure of the basic [Ru(trpy)<sub>2</sub>] molecule, variations in slope and response range were obtained. The [Ru(ppd-trpy)<sub>2</sub>](PF<sub>6</sub>)<sub>2</sub> molecule was found to exhibit a 33% increase in response slope over the basic [Ru(trpy)<sub>2</sub>] molecule and responded over approximately the same temperature range. The response of this molecule was very similar to the response of [Ru(trpy)(VH-127)](PF<sub>6</sub>)<sub>2</sub> (commonly considered the best response in this temperature region), but the [Ru(ppd-trpy)<sub>2</sub>](PF<sub>6</sub>)<sub>2</sub> molecule is much simpler and cheaper to synthesize. While the effects of the polymer binder were not a focus, they were outlined and illustrated.

While many pressure-sensitive paint formulations were tested under cryogenic conditions, only a few responded with reasonable sensitivity and resolution under the limited oxygen concentrations found in a cryogenic wind tunnel. These paints produced good data at 150 K, but no good responses were observed at 100 K. The paints that did respond well included the anodized paint layers and paints using TLC plate or filter paper as the binder. The anodized and TLC paints showed a 20-40% intensity change over the region of interest while the filter paper paints showed the same magnitude of change with the exception of PtTFPP/filter paper and PtOEP/filter paper which exhibited a 60%

intensity change. Although efforts were made to minimize the amount of polymer, none of the paints containing any type of polymer in the binder exhibited sensitivity under cryogenic conditions. However, porous polyethylene, tape cast, and RTV/silica gel paints were found to be good candidates for PSP's that operate in the temperature regions encountered during in-flight PSP measurements and should be considered for use in flight tests.

It is recommended that further investigation of porous surfaces be undertaken in an effort to understand the phenomena observed in PSP response at 100 K and also to expand binder choices beyond the limited options found in this research. Experiments to determine the nature of the 100 K response should also be conducted in an effort to explain and understand the origin of this behavior.

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## APPENDIX A: TEMPERATURE CALIBRATION DATA

This appendix is a compilation of the temperature-sensitive paint calibration data produced during the course of this research. This appendix contains two tables and 26 figures. Table A.1 contains information concerning the formulation of the paint mixtures that were calibrated for this research. It should be noted that the amount of solvent used to dissolve the luminescent compound prior to mixing with the polymer binder is not critical. Only enough solvent to fully dissolve the compound is required. The solvent then evaporates into the atmosphere as the paint dries after application. Also, some compounds dissolved directly into the binder and no solvent was required. The choice of a base coat was dictated by two factors, adhesiveness of the binder to the metal and optical requirements. White base coats were used in order to allow more emitted light to be reflected back to the collection optics. Trial and error determined if a particular binder would better adhere to certain base coats. Table A.2 shows the excitation light and filters used in each calibration. Choice of excitation wavelength and filtration was dependent on the excitation and emission spectrum of each luminescent molecule and also on required excitation intensity. Figures A.1-A.26 show the results of each calibration. The top plot is intensity ratio versus temperature and the bottom plot is the Arrhenius form of the results. In all cases, the reference conditions were taken at  $-150\text{ }^{\circ}\text{C}$ . A line representing the results of a linear regression over the useful range of sensitivity for each paint is shown on each intensity ratio plot.

Table A.1: TSP Paint Mixtures

| Paint<br>( $\langle$ compound $\rangle$ In $\langle$ binder $\rangle$ )                 | Amount of<br>Fluorophore<br>(mg) | Amount of<br>Binder<br>(mL) | Solvent       | Basecoat        |
|-----------------------------------------------------------------------------------------|----------------------------------|-----------------------------|---------------|-----------------|
| [Cu(ph <sub>2</sub> -phen) <sub>2</sub> ](PF <sub>6</sub> ) <sub>2</sub> in GP-197      |                                  |                             |               | None            |
| PtPFPP in CC                                                                            | 100                              | 25                          | Acetone       | Chroma Base     |
| PtPFPP in Polyurethane                                                                  | 100                              | 20                          | Acetone       | Chroma Base     |
| [Rh(bzq) <sub>2</sub> Cl] <sub>2</sub> in CC                                            | 50                               | 25                          | Acetonitrile  | Chroma Base     |
| [Rh(bzq) <sub>2</sub> (phen)](PF <sub>6</sub> ) in CC                                   | 50                               | 25                          | Acetonitrile  | Chroma Base     |
| [Ru(bipy) <sub>3</sub> ](DS) <sub>2</sub> in CC                                         |                                  |                             | Ethyl Alcohol | White Car Paint |
| [Ru(bipy) <sub>3</sub> ](TFPB) <sub>2</sub> in CC                                       |                                  |                             | None          | Chroma Base     |
| [Ru(ph <sub>2</sub> -phen) <sub>3</sub> ](DS) <sub>2</sub> in CC                        |                                  |                             | Ethyl Alcohol | Chroma Base     |
| [Ru(trpy)] in CC                                                                        | 20                               | 15                          | Acetone       | Chroma Base     |
| [Ru(trpy)(4'-C <sub>6</sub> F <sub>5</sub> -trpy)](NO <sub>3</sub> ) <sub>2</sub> in CC | 6                                | 20                          | Acetonitrile  | Chroma Base     |
| [Ru(trpy)(4'-Cl-trpy)](Cl <sub>2</sub> ) in CC                                          | 8                                | 22                          | Acetonitrile  | Chroma Base     |
| [Ru(trpy)(4'-NC-trpy)](NO <sub>3</sub> ) <sub>2</sub> in CC                             | 13                               | 22                          | Acetonitrile  | Chroma Base     |
| [Ru(phtrpy)(Cltrpy)](NO <sub>3</sub> ) <sub>2</sub> in CC                               | 6                                | 40                          | Acetonitrile  | Chroma Base     |
| [Ru(trpy)(4'-TfO-trpy)](NO <sub>3</sub> ) <sub>2</sub> in CC                            | 12                               | 20                          | Acetonitrile  | Chroma Base     |
| [Ru(trpy)(MeStrpy)](NO <sub>3</sub> ) <sub>2</sub> in CC                                | 17                               | 20                          | Acetonitrile  | Chroma Base     |
| [Ru(trpy) <sub>2</sub> (NO <sub>2</sub> (Phtrpy))](PF <sub>6</sub> ) in CC              |                                  |                             | Acetone       | Chroma Base     |
| [Ru(trpy)(phtrpy)](PF <sub>6</sub> ) <sub>2</sub> in GP-197                             |                                  |                             | None          | White Car Paint |
| [Ru(trpy)(phtrpy)](PF <sub>6</sub> ) <sub>2</sub> in CC                                 |                                  |                             | Acetone       | Chroma Base     |
| [Ru(trpy)(ppd-trpy)](TFPB) <sub>2</sub> in CC                                           | 11                               | 15                          | Acetone       | Chroma Base     |
| [Ru(trpy)(phyphen)](TFPB) <sub>2</sub> in CC                                            | 10                               | 11                          | Acetone       | Chroma Base     |

Table A.1: TSP Paint Mixtures (cont.)

|                                                                          |    |    |               |              |
|--------------------------------------------------------------------------|----|----|---------------|--------------|
| [Ru(trpy)(SO <sub>2</sub> Me-trpy)](PF <sub>6</sub> ) <sub>2</sub> in CC | 10 | 15 | Acetone       | Chroma Base  |
| [Ru(trpy) <sub>2</sub> ](DS) <sub>2</sub> in CC                          |    |    | Ethyl Alcohol | Chroma Base  |
| [Ru(trpy) <sub>2</sub> ](TFPB) <sub>2</sub> in CC                        |    |    | Ethyl Alcohol | Chroma Base  |
| [Ru(ppd-trpy) <sub>2</sub> ](TFPB) <sub>2</sub> in CC                    | 8  | 10 | Acetone       | Chroma Base  |
| [Os(trpy) <sub>2</sub> ](PF <sub>6</sub> ) <sub>2</sub> in CC            | 28 | 15 | Acetone       | Chroma Base  |
| [Ru(trpy)(Vh127)](PF <sub>6</sub> ) <sub>2</sub> in GP-197               | 5  | 13 | Acetone       | White Krylon |

Table A.2: TSP Calibration Settings

| Paint<br>(<compound> In <binder>)                                                       | Excitation         |              | Optical Filter |                 |
|-----------------------------------------------------------------------------------------|--------------------|--------------|----------------|-----------------|
|                                                                                         | Wavelength<br>(nm) | Power<br>(W) | Type           | Cut-off<br>(nm) |
| [Cu(ph <sub>2</sub> -phen) <sub>2</sub> ](PF <sub>6</sub> ) <sub>2</sub> in GP-197      | 488                |              | LP             | 550             |
| PtPFPP in CC                                                                            | 488                | 0.005        | LP             | 600             |
| PtPFPP in Polyurethane                                                                  | 488                | 0.005        | LP             | 600             |
| [Rh(bzq) <sub>2</sub> Cl] <sub>2</sub> in CC                                            | UV lamp            |              | LP             | 450             |
| [Rh(bzq) <sub>2</sub> (phen)](PF <sub>6</sub> ) in CC                                   | UV lamp            |              | LP             | 450             |
| [Ru(bipy) <sub>3</sub> ](DS) <sub>2</sub> in CC                                         | 476                | 0.05         | LP             | 550             |
| [Ru(bipy) <sub>3</sub> ](TFPB) <sub>2</sub> in CC                                       | 488                | 0.13         | LP             | 550             |
| [Ru(ph <sub>2</sub> -phen) <sub>3</sub> ](DS) <sub>2</sub> in CC                        | 488                | 0.18         | LP             | 550             |
| [Ru(trpy)] in CC                                                                        | 488                | 0.12         | LP             | 550             |
| [Ru(trpy)(4'-C <sub>6</sub> F <sub>5</sub> -trpy)](NO <sub>3</sub> ) <sub>2</sub> in CC | 488                | 0.005        | LP             | 550             |
| [Ru(trpy)(4'-Cl-trpy)](Cl <sub>2</sub> ) in CC                                          | 488                | 0.005        | LP             | 550             |
| [Ru(trpy)(4'-NC-trpy)](NO <sub>3</sub> ) <sub>2</sub> in CC                             | 488                | 0.005        | LP             | 550             |
| [Ru(phtrpy)(Cltrpy)](NO <sub>3</sub> ) <sub>2</sub> in CC                               | 488                | 0.005        | LP             | 550             |
| [Ru(trpy)(4'-TfO-trpy)](NO <sub>3</sub> ) <sub>2</sub> in CC                            | 488                | 0.005        | LP             | 550             |
| [Ru(trpy)(MeStrpy)](NO <sub>3</sub> ) <sub>2</sub> in CC                                | 488                | 0.005        | LP             | 550             |
| [Ru(trpy) <sub>2</sub> (NO <sub>2</sub> (Phtrpy))](PF <sub>6</sub> ) in CC              | 488                |              | LP             | 550             |
| [Ru(trpy)(phtrpy)](PF <sub>6</sub> ) <sub>2</sub> in GP-197                             | 488                |              | LP             | 550             |
| [Ru(trpy)(phtrpy)](PF <sub>6</sub> ) <sub>2</sub> in CC                                 | 488                |              | LP             | 550             |
| [Ru(trpy)(ppd-trpy)](TFPB) <sub>2</sub> in CC                                           | 488                | 0.005        | LP             | 550             |
| [Ru(trpy)(phyphen)](TFPB) <sub>2</sub> in CC                                            | 488                | 0.005        | LP             | 550             |
| [Ru(trpy)(SO <sub>2</sub> Me-trpy)](PF <sub>6</sub> ) <sub>2</sub> in CC                | 488                | 0.005        | LP             | 550             |
| [Ru(trpy) <sub>2</sub> ](DS) <sub>2</sub> in CC                                         | 488                | 0.005        | LP             | 550             |
| [Ru(trpy) <sub>2</sub> ](TFPB) <sub>2</sub> in CC                                       | 488                | 0.005        | LP             | 550             |
| [Ru(ppd-trpy) <sub>2</sub> ](TFPB) <sub>2</sub> in CC                                   | 488                | 0.005        | LP             | 550             |
| [Os(trpy) <sub>2</sub> ](PF <sub>6</sub> ) <sub>2</sub> in CC                           | 632                | 0.01         | LP             | 700             |
| [Ru(trpy)(Vh127)](PF <sub>6</sub> ) <sub>2</sub> in GP-197                              | 488                | 0.005        | LP             | 550             |

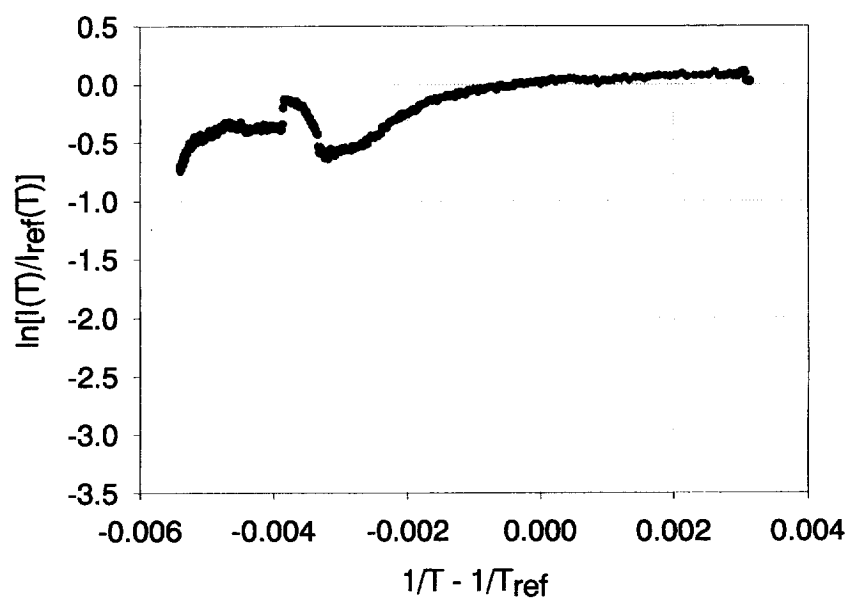
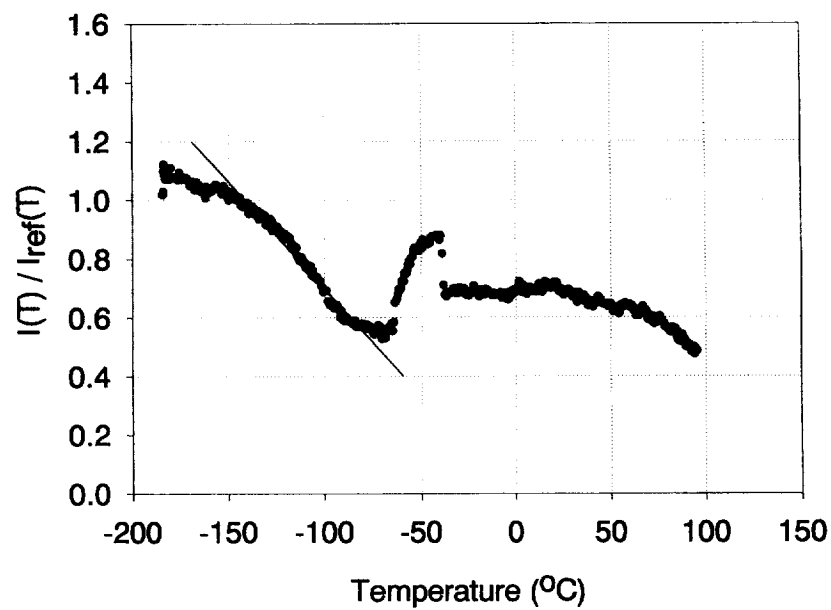


Figure A.1:  $[\text{Cu}(\text{ph}_2\text{-phen})_2](\text{PF}_6)_2$  in GP-197

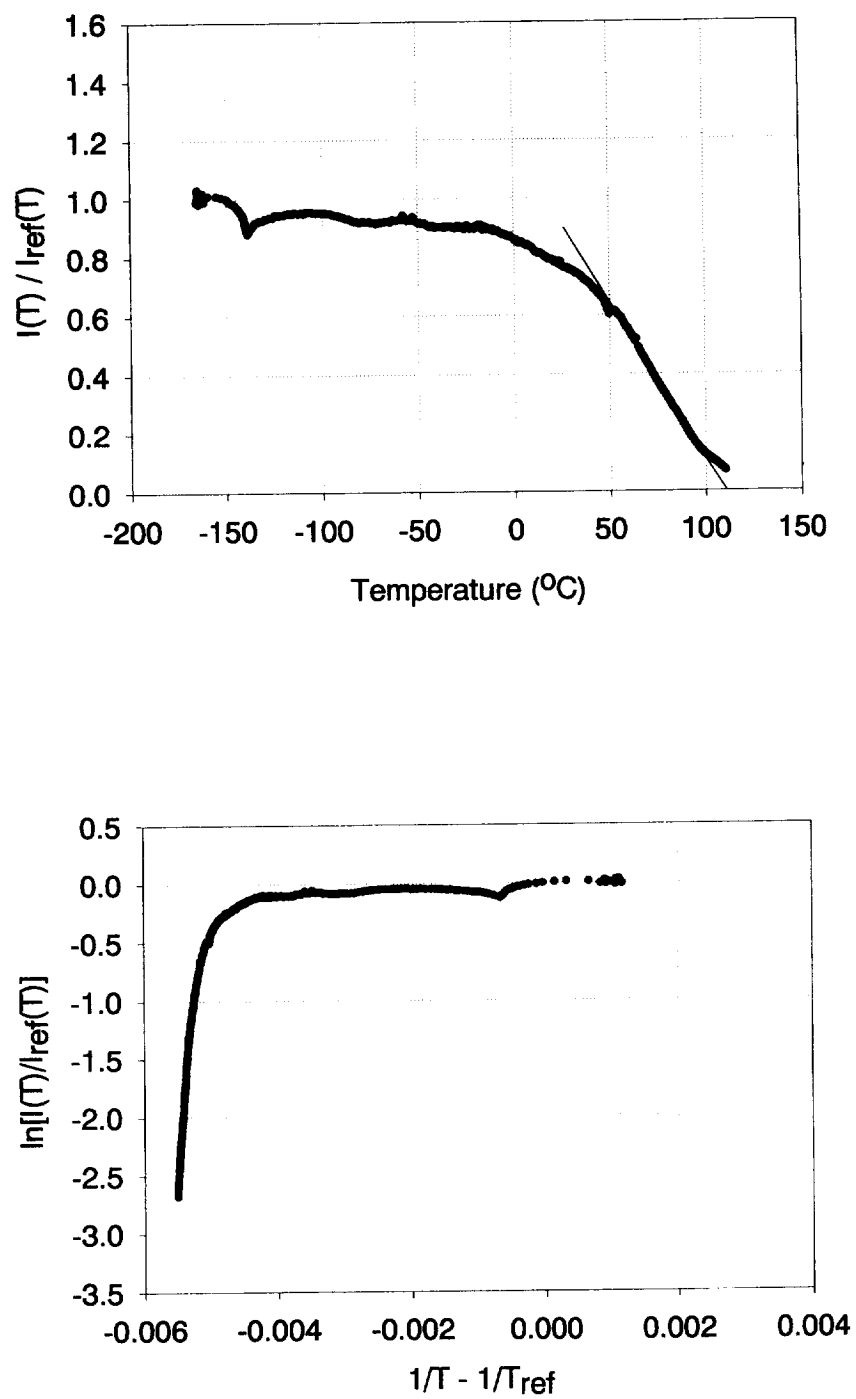


Figure A.2: PtPFPP in CC

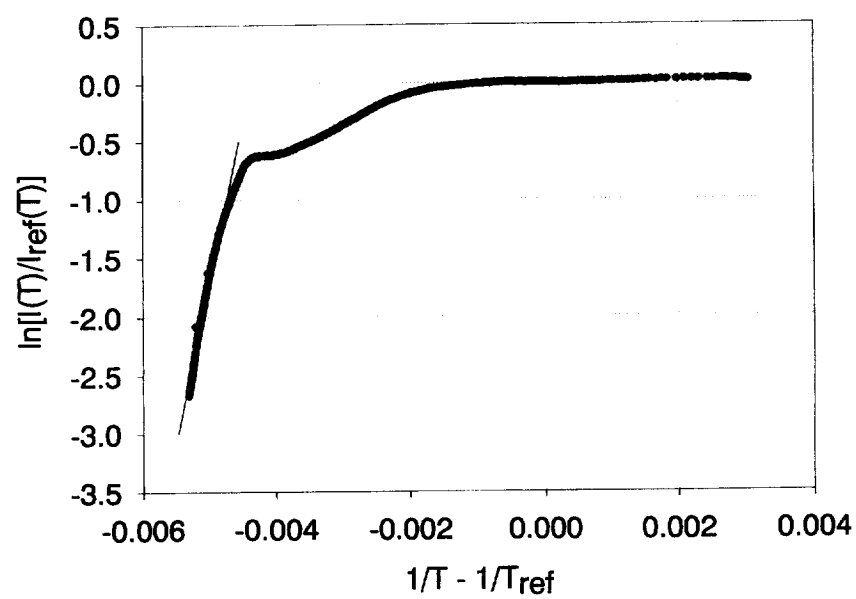
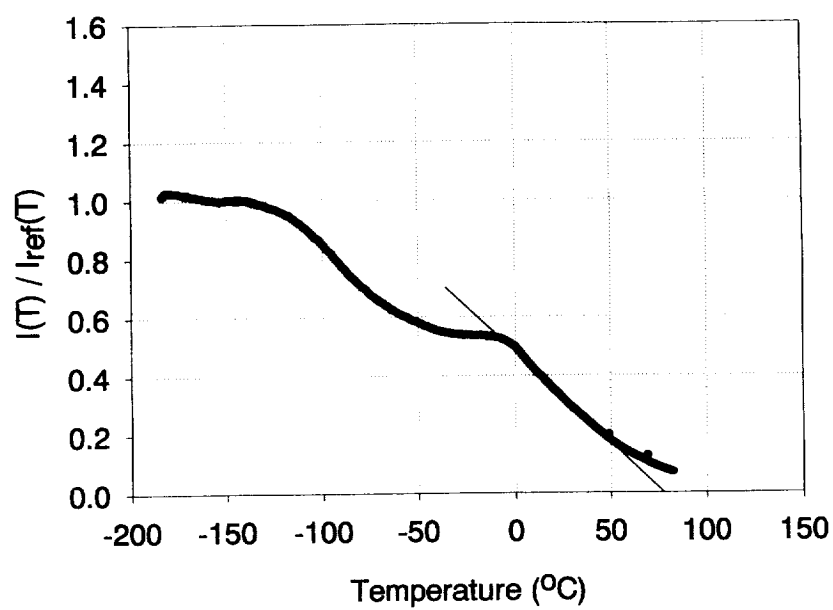


Figure A.3: PtPFPP in Polyurethane



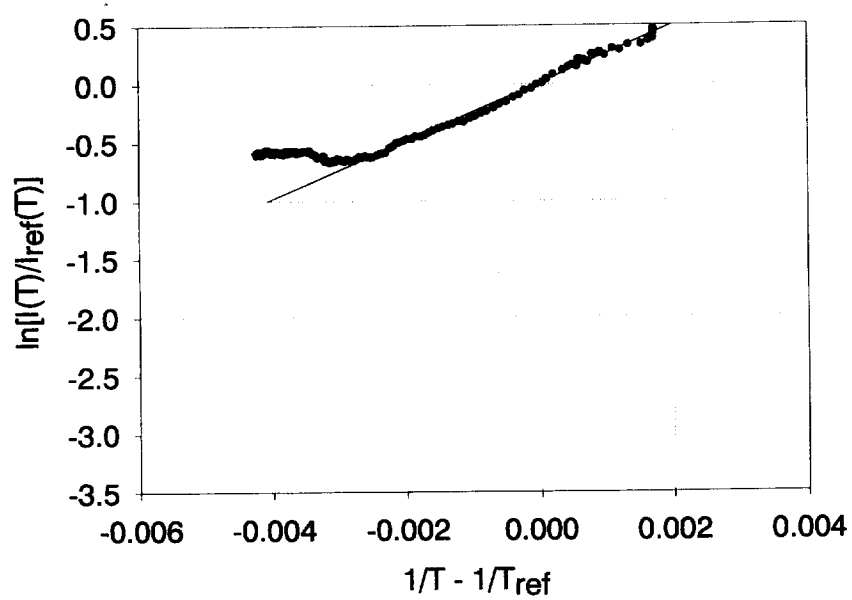
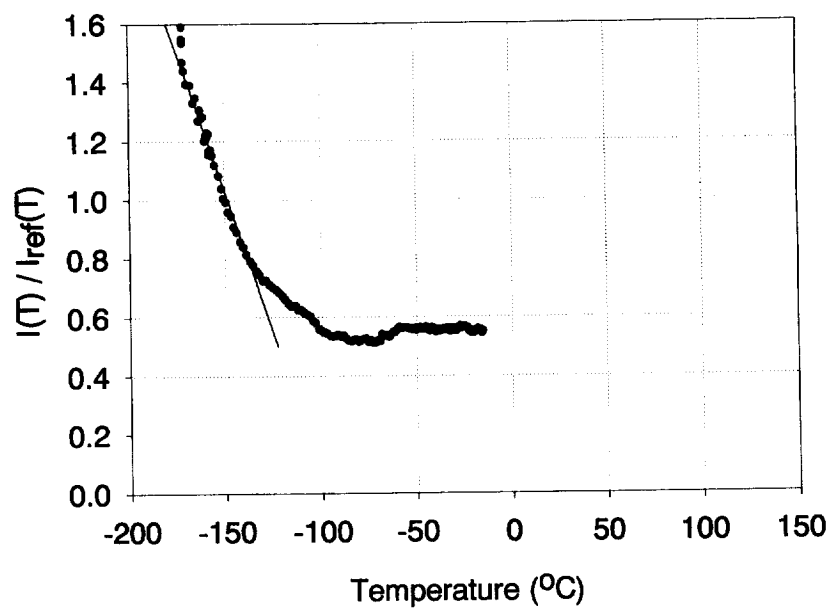


Figure A.4:  $[\text{Rh}(\text{bzq})_2\text{Cl}]_2$  in CC

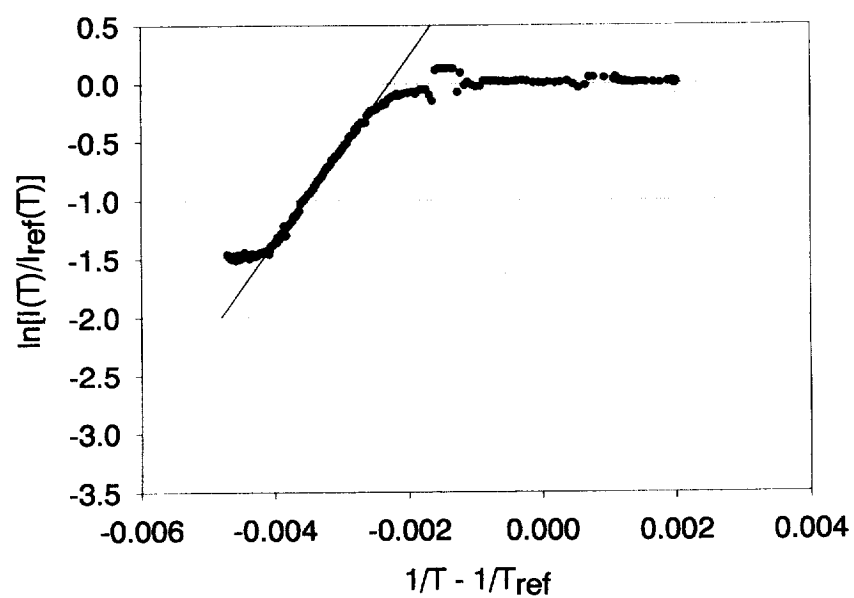
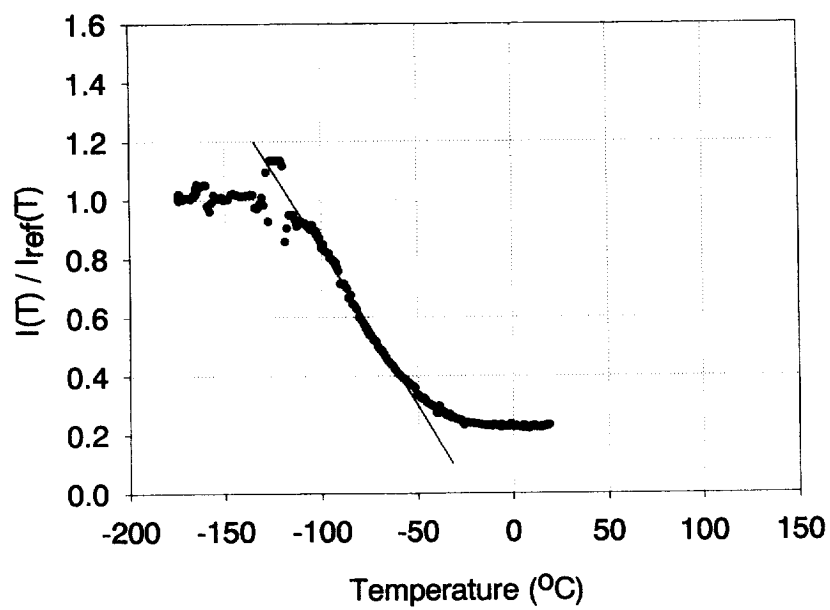
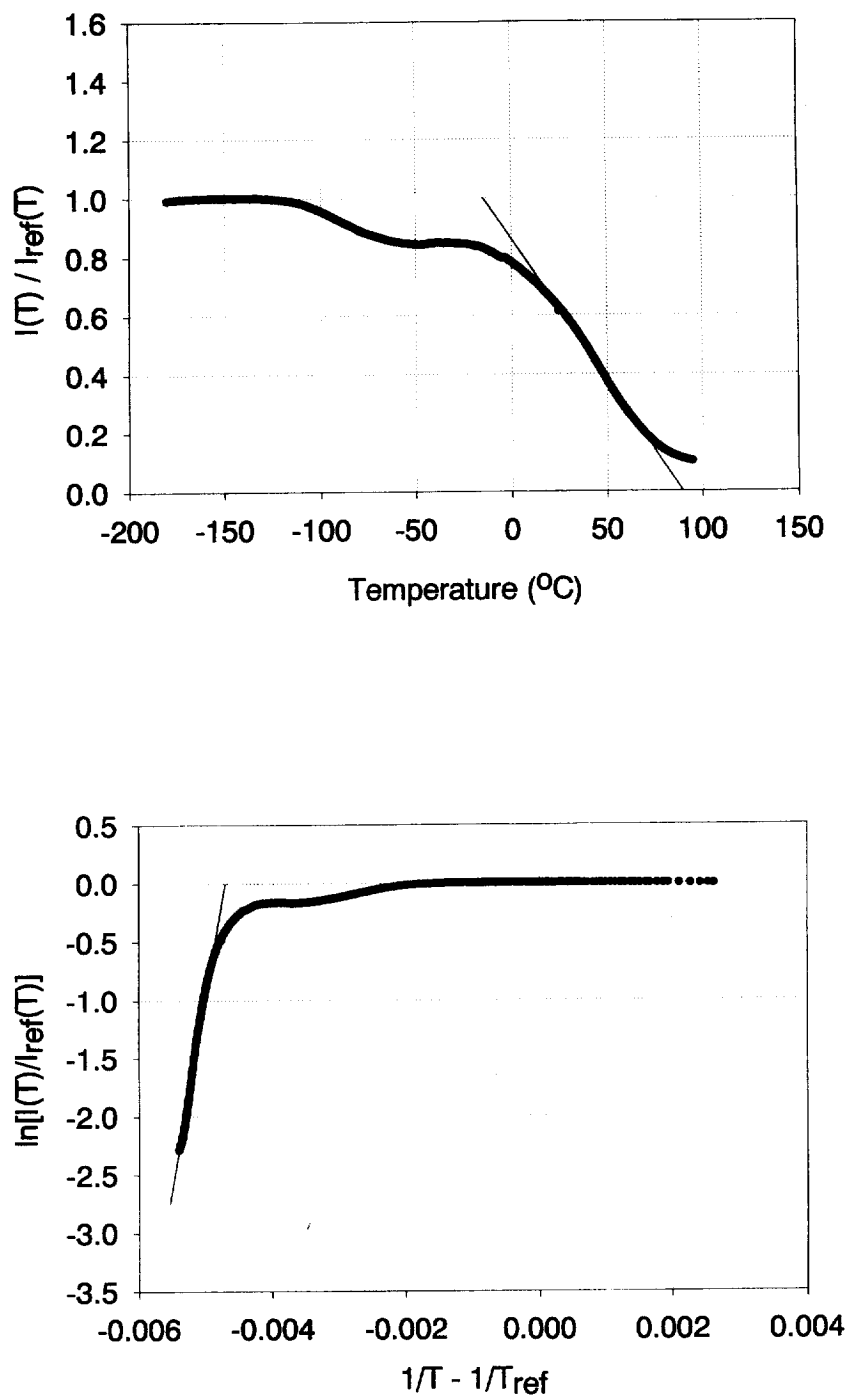


Figure A.5:  $[\text{Rh}(\text{bzq})_2(\text{phen})](\text{PF}_6)$  in CC

Figure A.6:  $[\text{Ru}(\text{bipy})_3](\text{DS})_2$  in CC

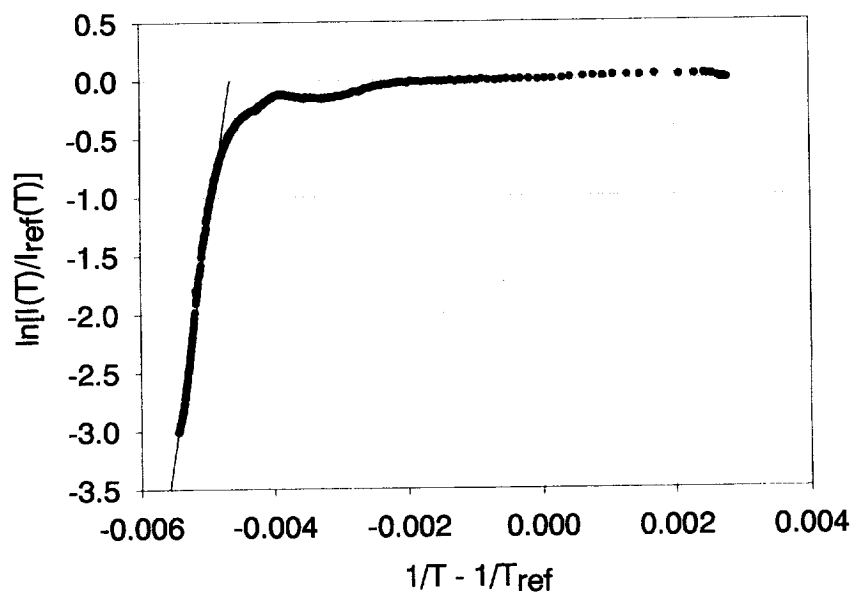
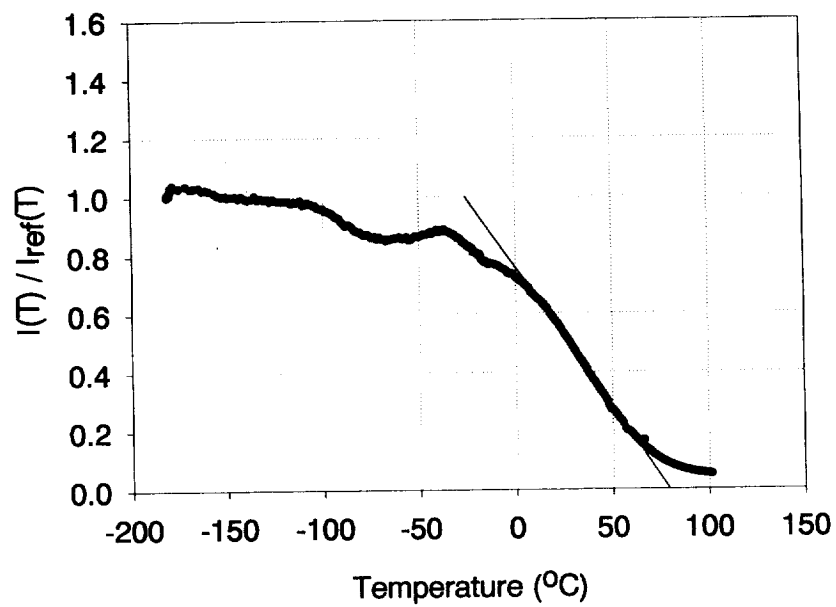


Figure A.7:  $[\text{Ru}(\text{bipy})_3](\text{TFPB})_2$  in CC

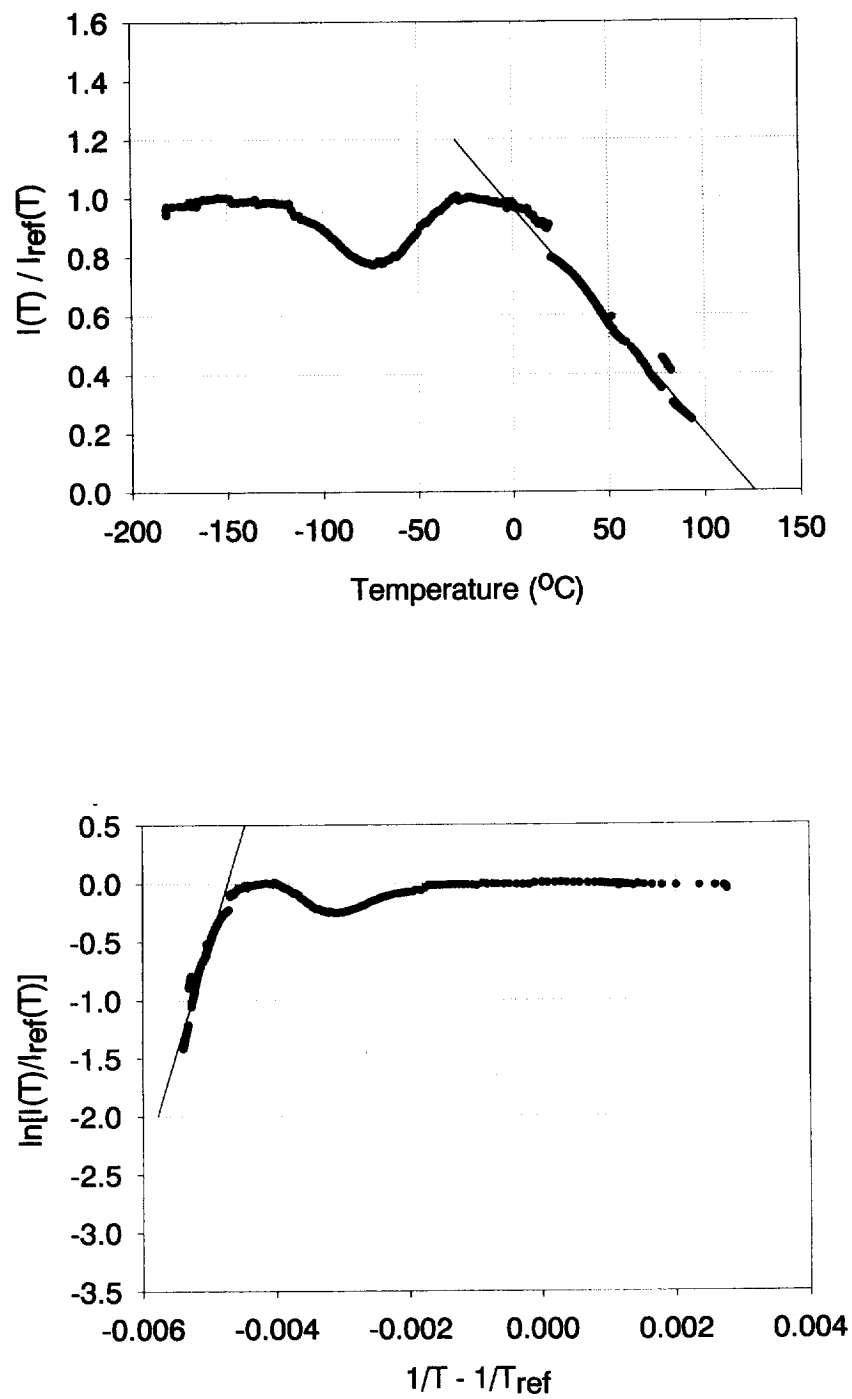


Figure A.8:  $[\text{Ru}(\text{ph}_2\text{-phen})_3](\text{DS})_2$  in CC

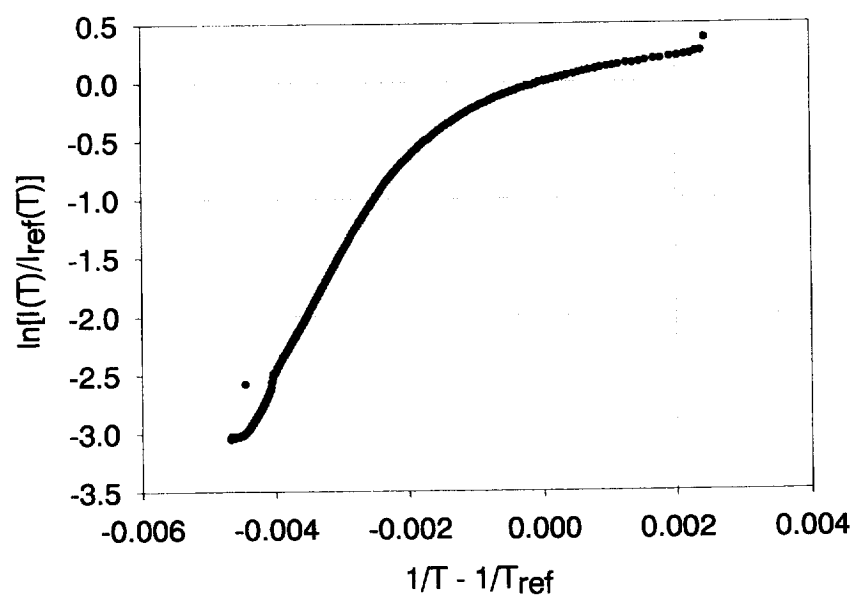
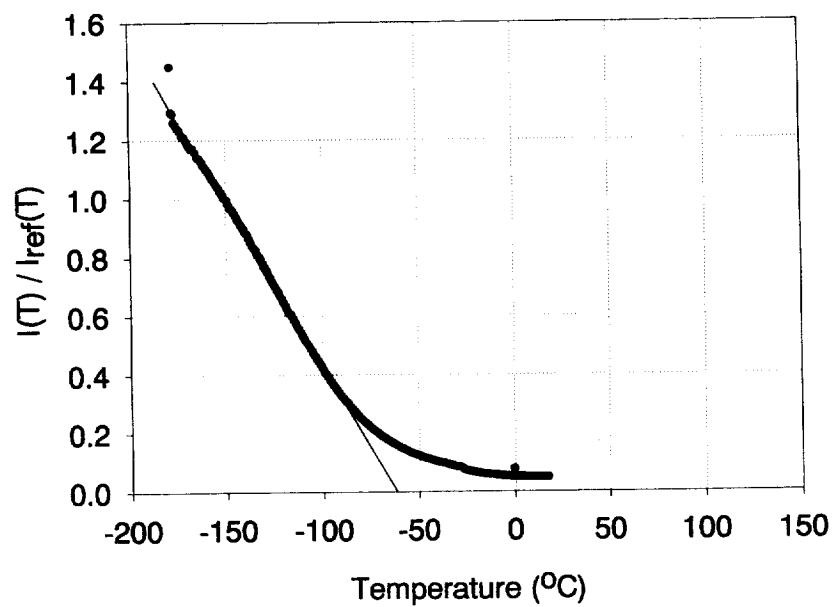


Figure A.9: [Ru(trpy)] in CC

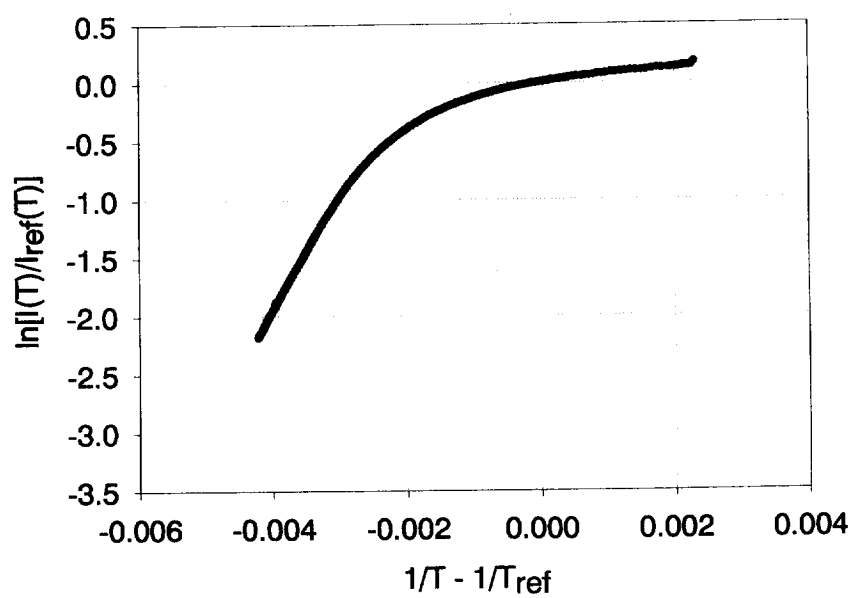
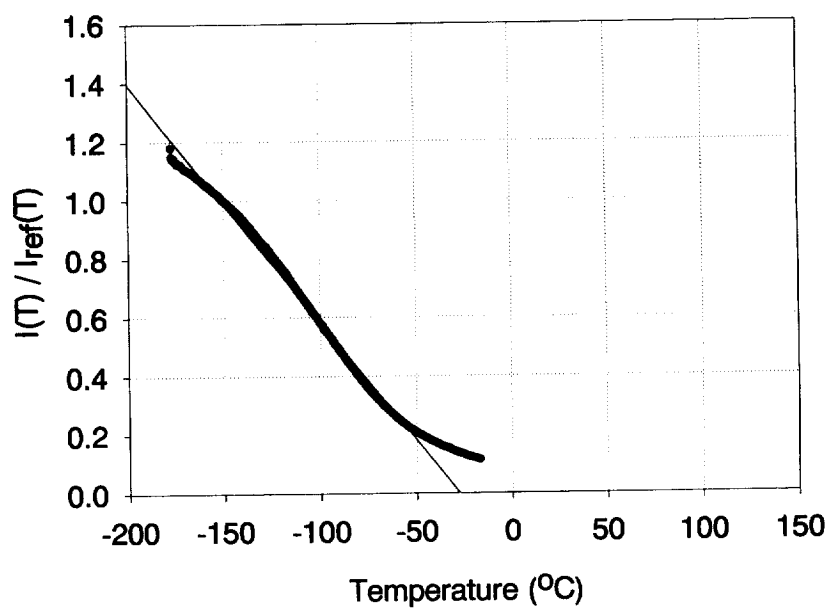


Figure A.10:  $[\text{Ru}(\text{trpy})(4'\text{-C}_6\text{F}_5\text{-trpy})](\text{NO}_3)_2$  in CC

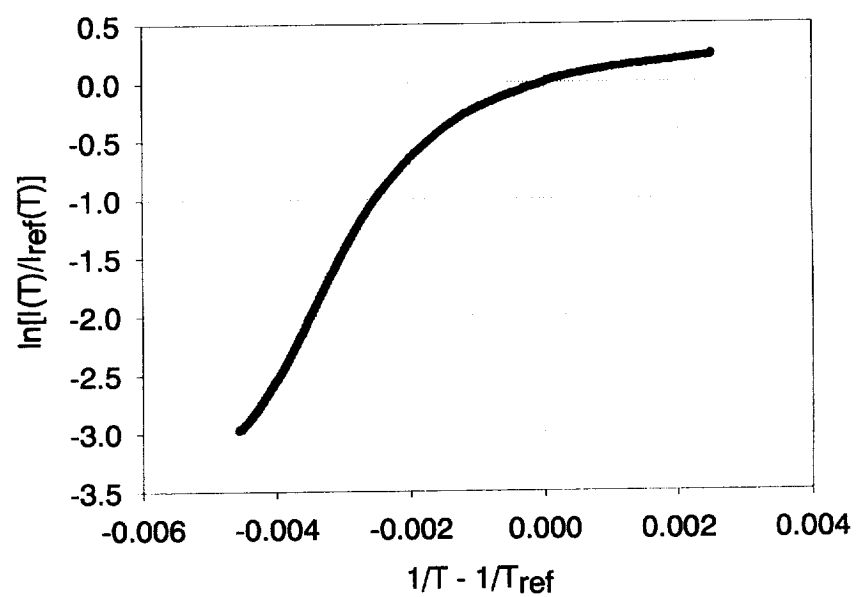
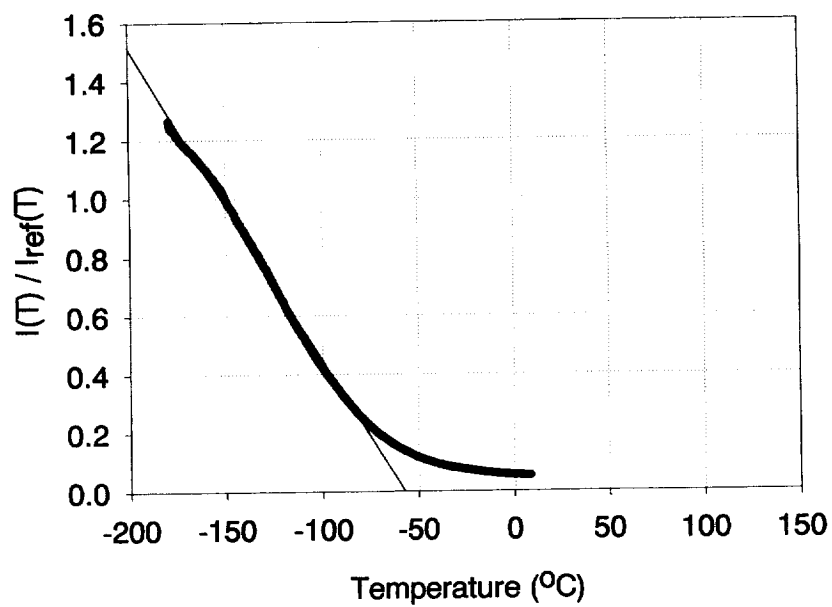


Figure A.11:  $[\text{Ru}(\text{trpy})(4'\text{-Cl-trpy})](\text{Cl}_2)$  in CC



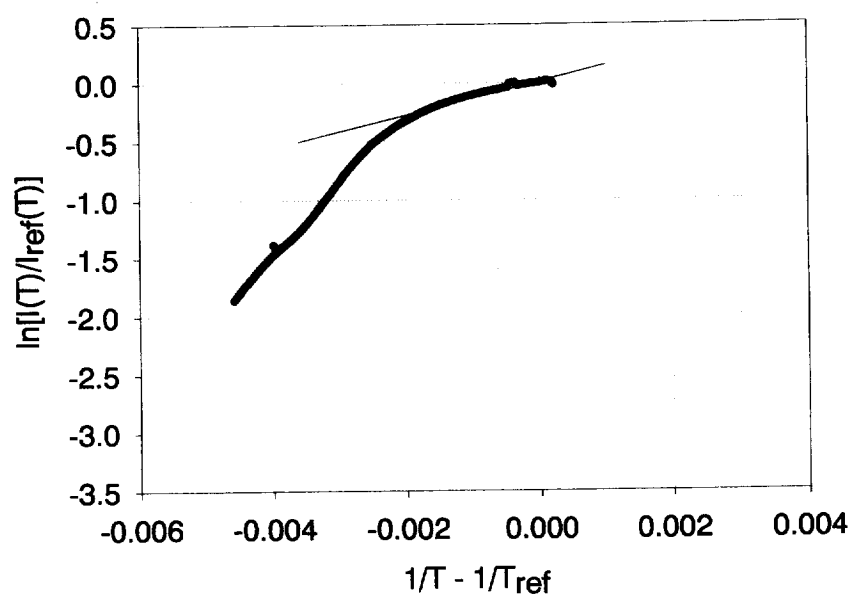
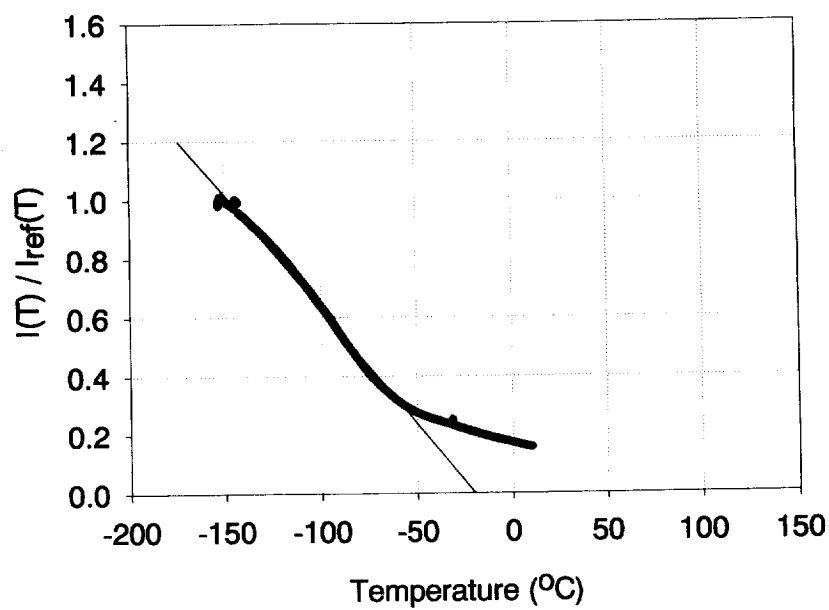


Figure A.12:  $[\text{Ru}(\text{trpy})(4'\text{-NC-trpy})](\text{NO}_3)_2$  in CC

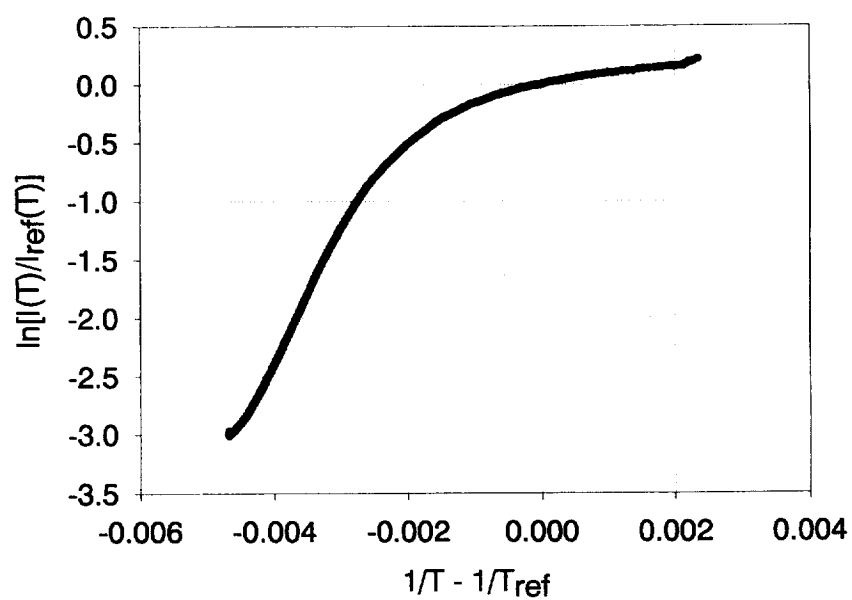
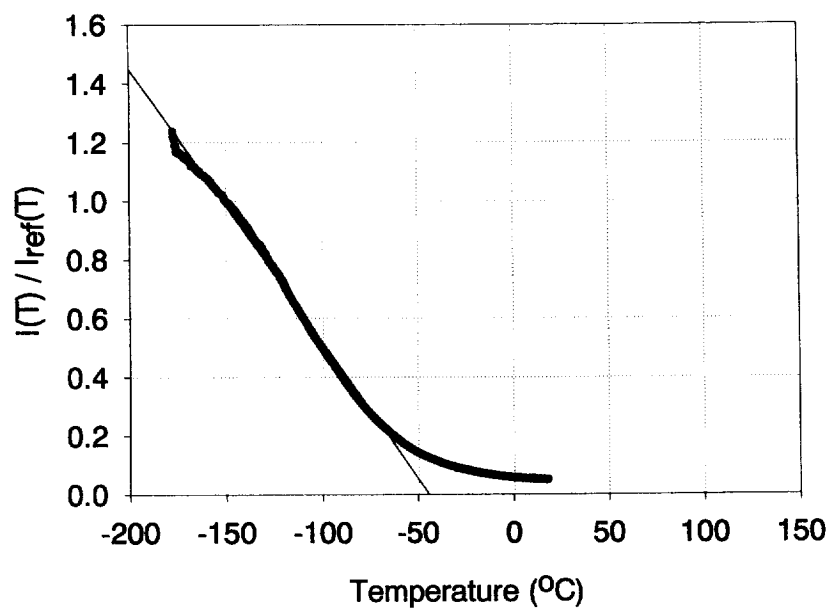


Figure A.13:  $[\text{Ru}(\text{phtrpy})(\text{Cltrpy})](\text{NO}_3)_2$  in CC

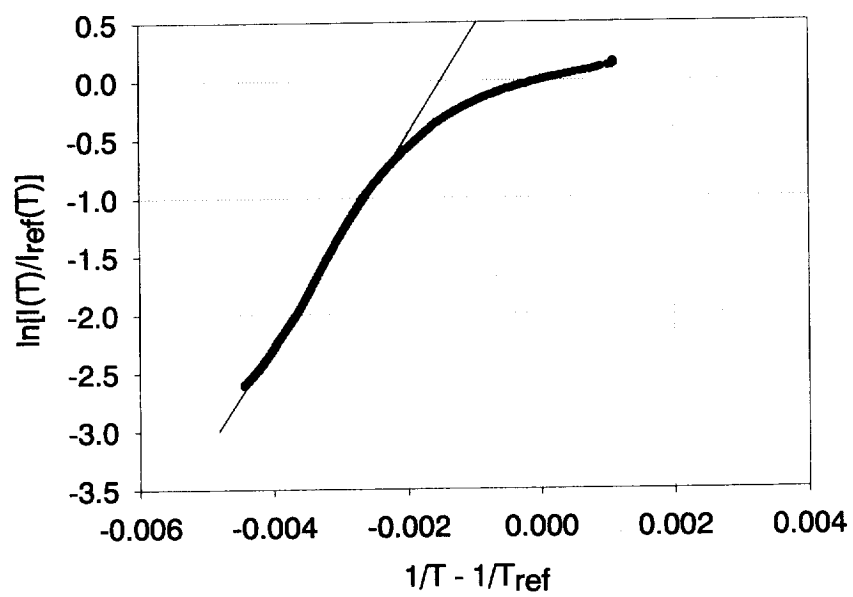
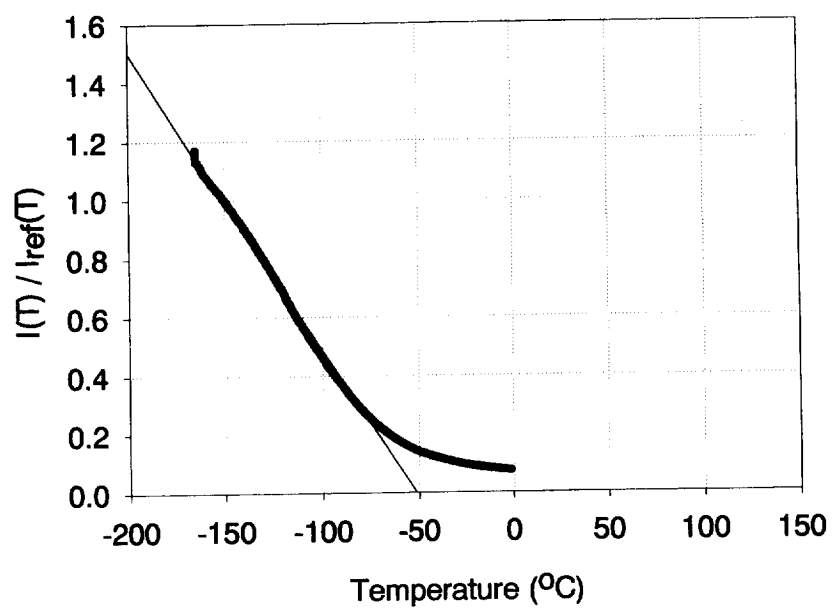


Figure A.14:  $[\text{Ru}(\text{trpy})(4'\text{-TfO-trpy})](\text{NO}_3)_2$  in CC

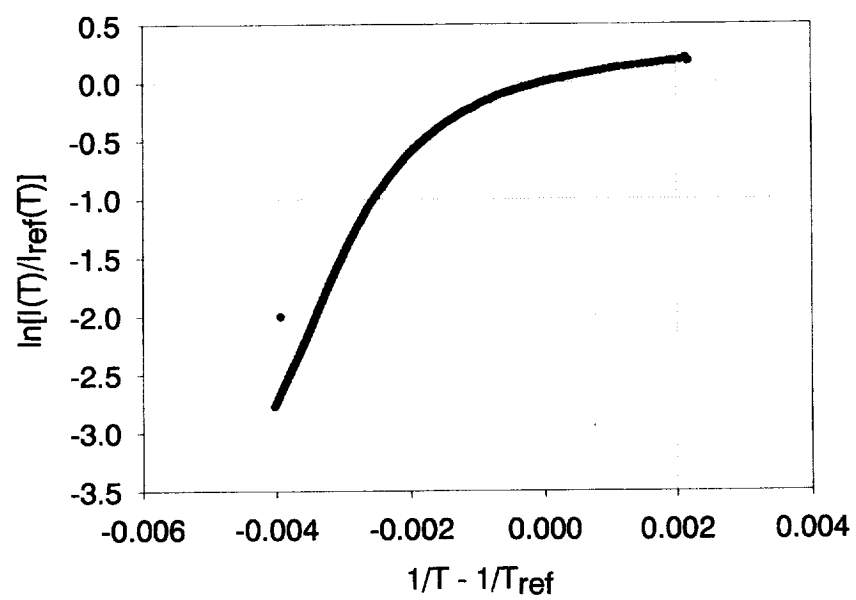
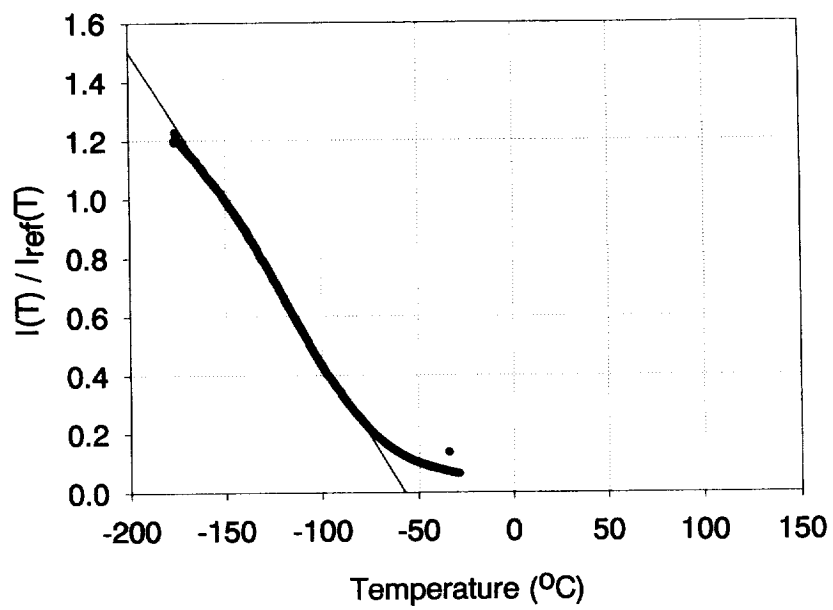


Figure A.15:  $[\text{Ru}(\text{trpy})(\text{MeStrpy})](\text{NO}_3)_2$  in CC

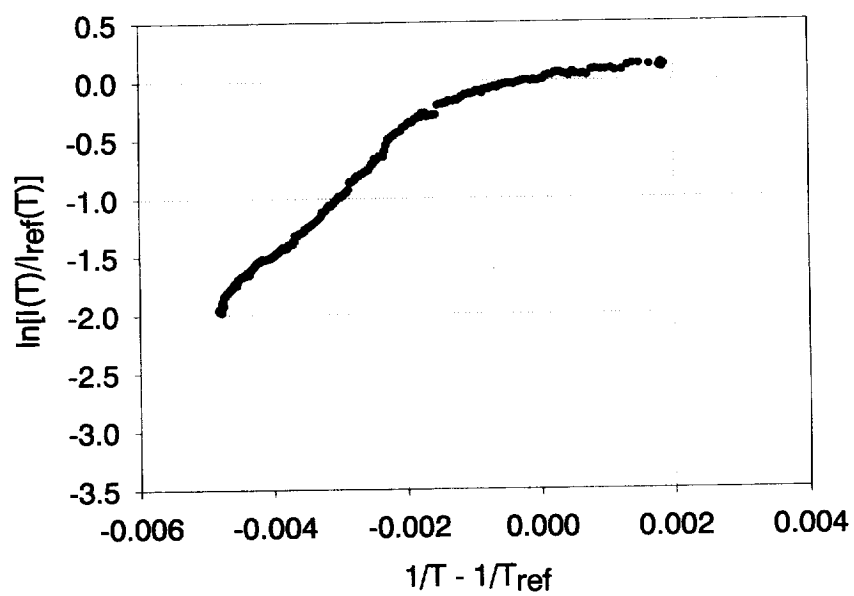
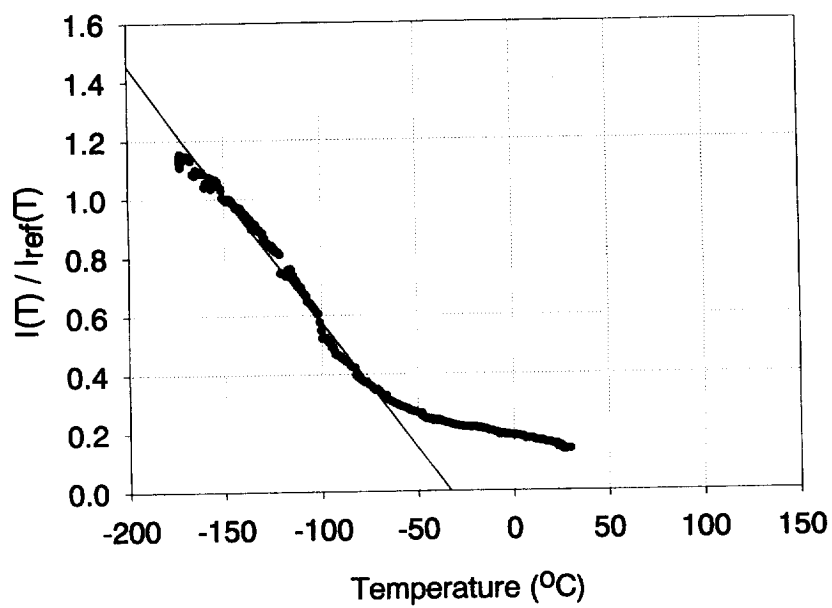


Figure A.16:  $[\text{Ru}(\text{trpy}_2)(\text{NO}_2(\text{Phtrpy}))](\text{PF}_6)$  in CC

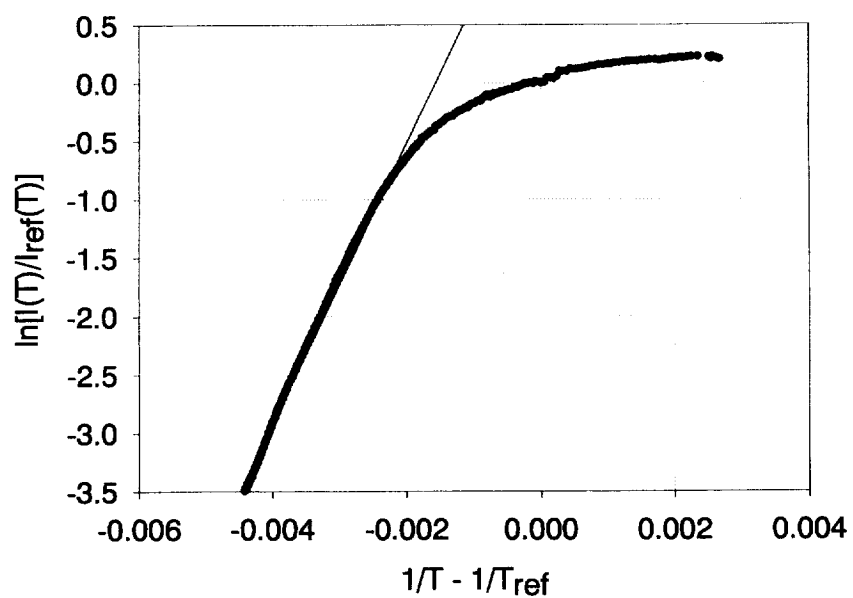
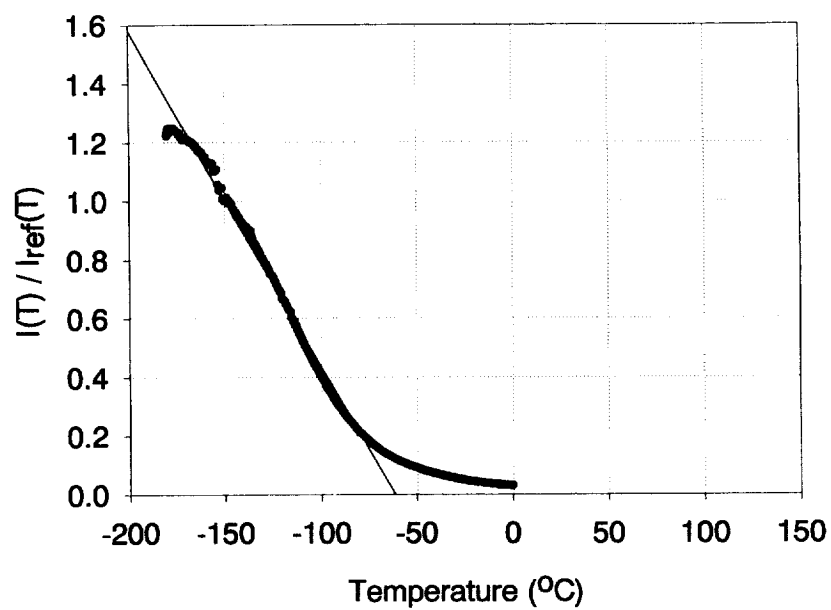
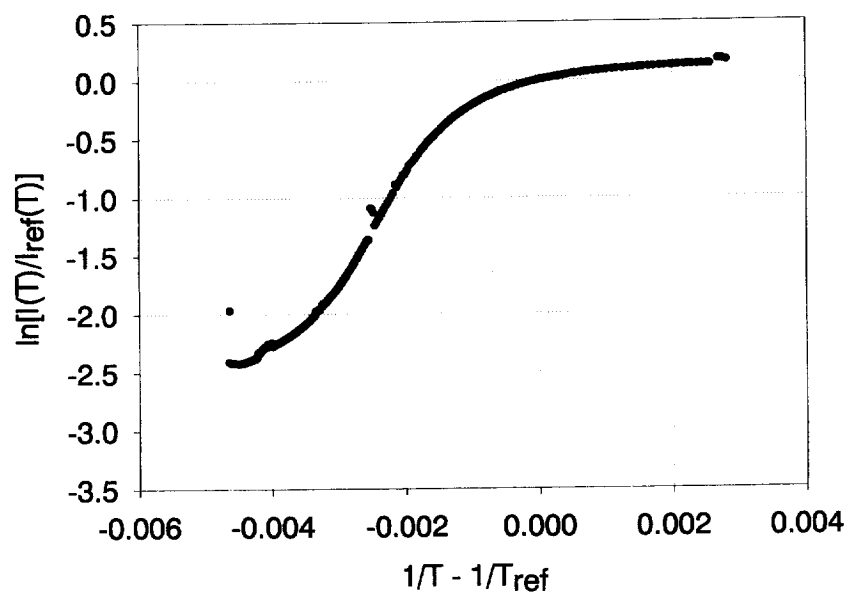
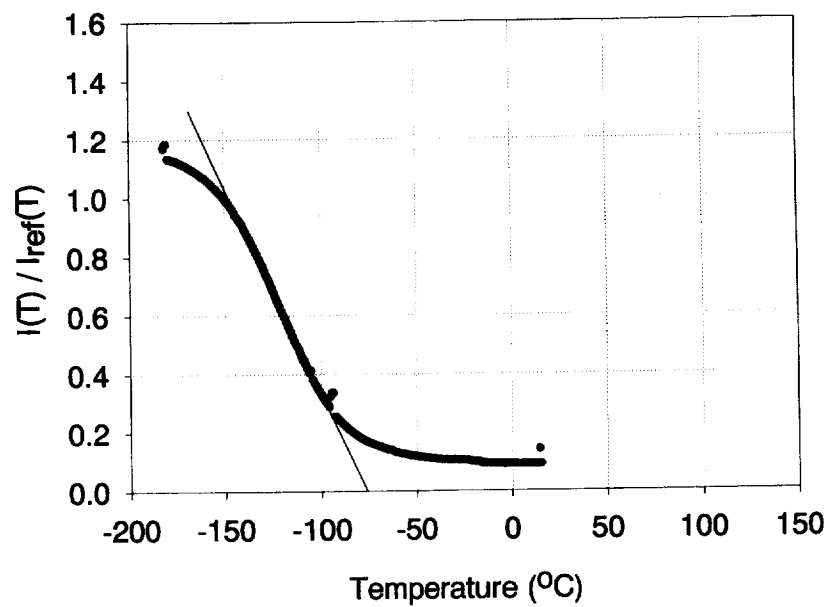


Figure A.17:  $[\text{Ru}(\text{trpy})(\text{phtrpy})](\text{PF}_6)_2$  in GP-197

Figure A.18:  $[\text{Ru}(\text{trpy})(\text{phtrpy})](\text{PF}_6)_2$  in CC

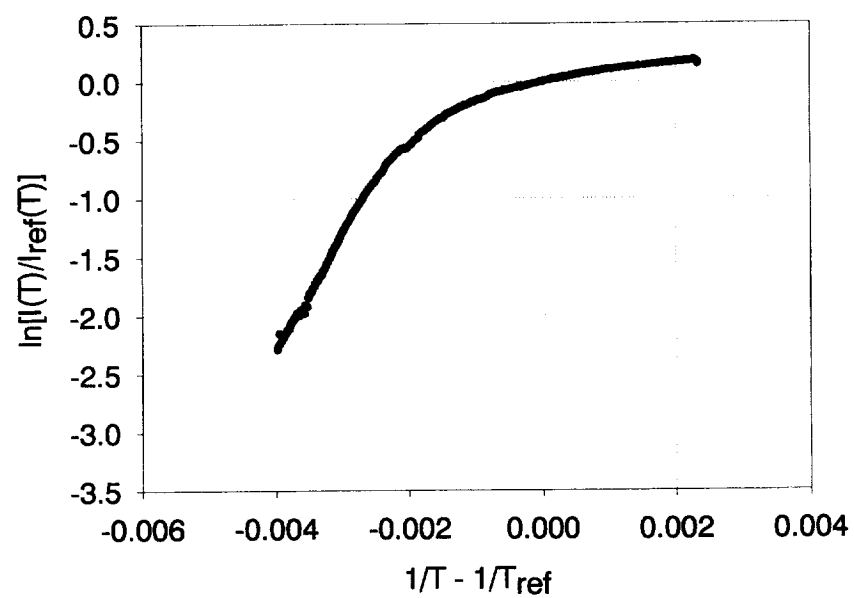
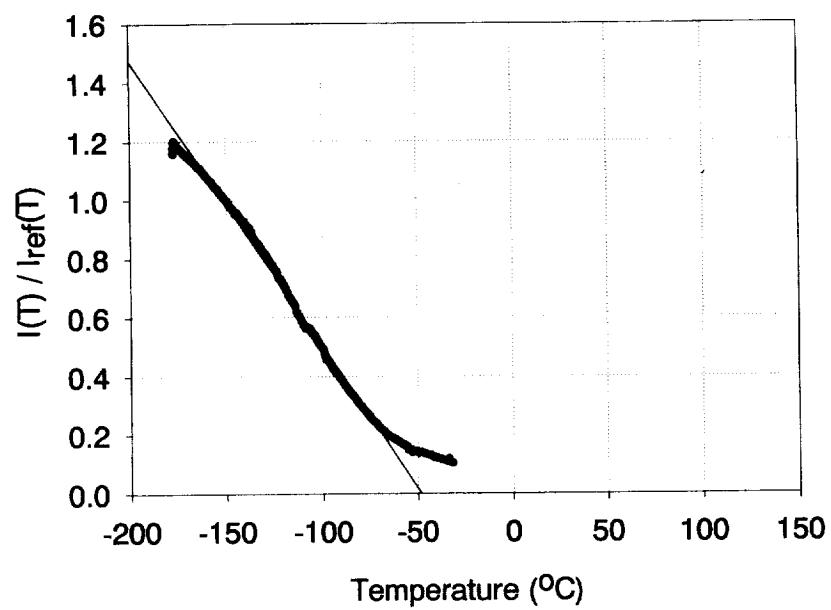


Figure A.19:  $[\text{Ru}(\text{trpy})(\text{ppd-trpy})](\text{TFPB})_2$  in CC



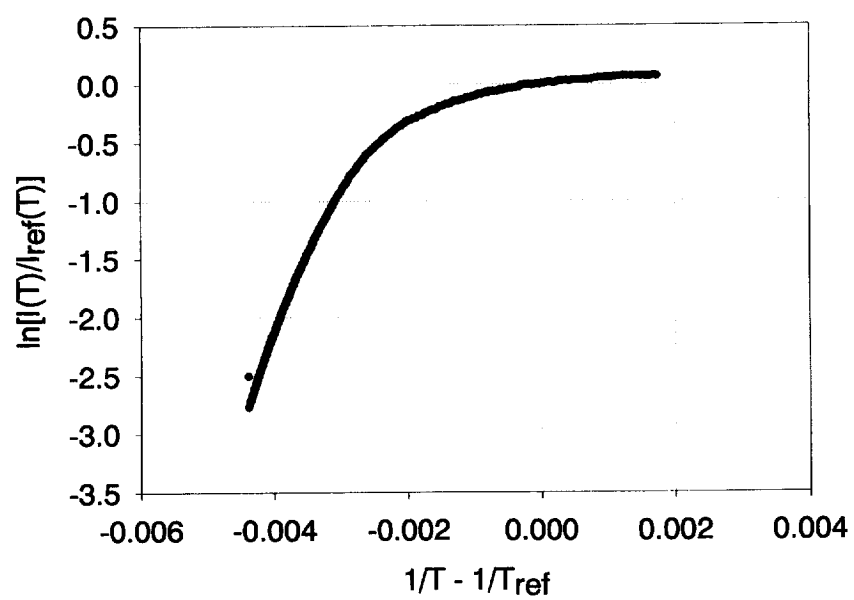
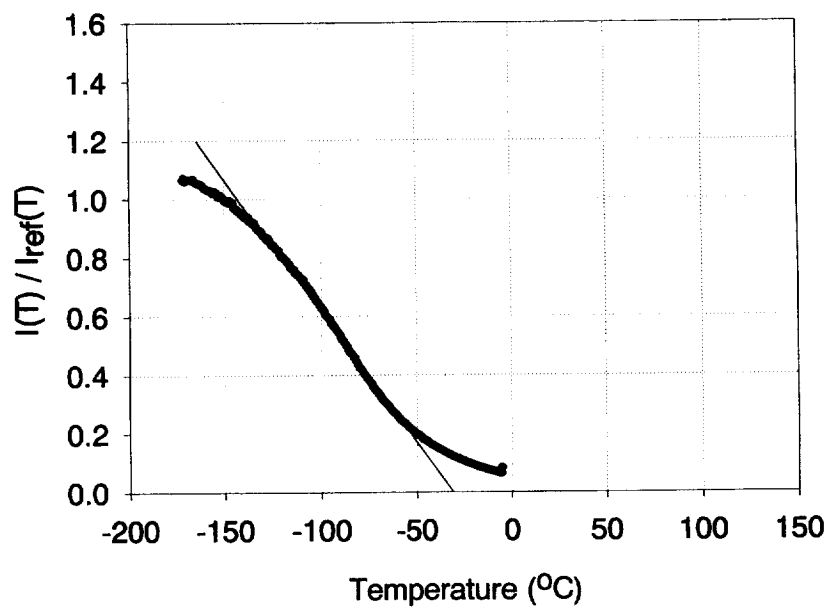


Figure A.20:  $[\text{Ru}(\text{trpy})(\text{phyphen})](\text{TFPB})_2$  in CC

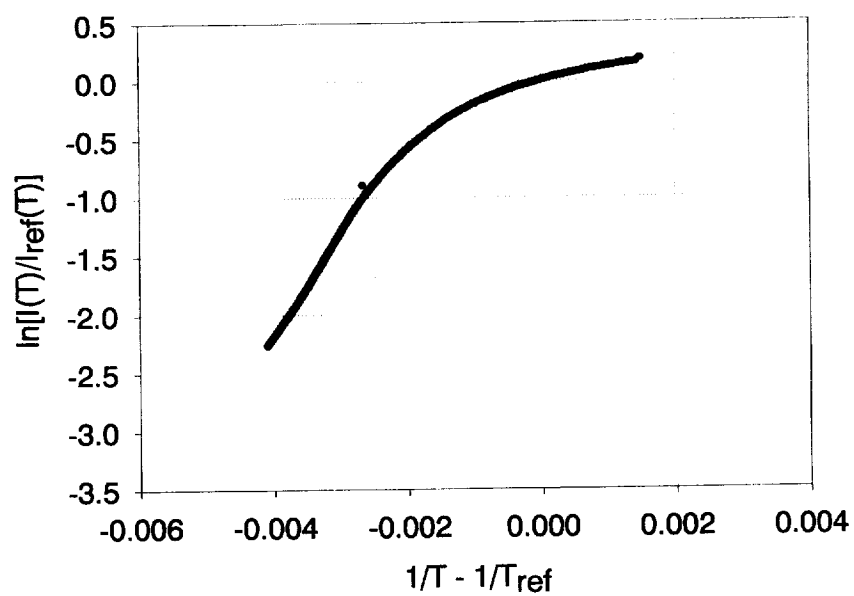
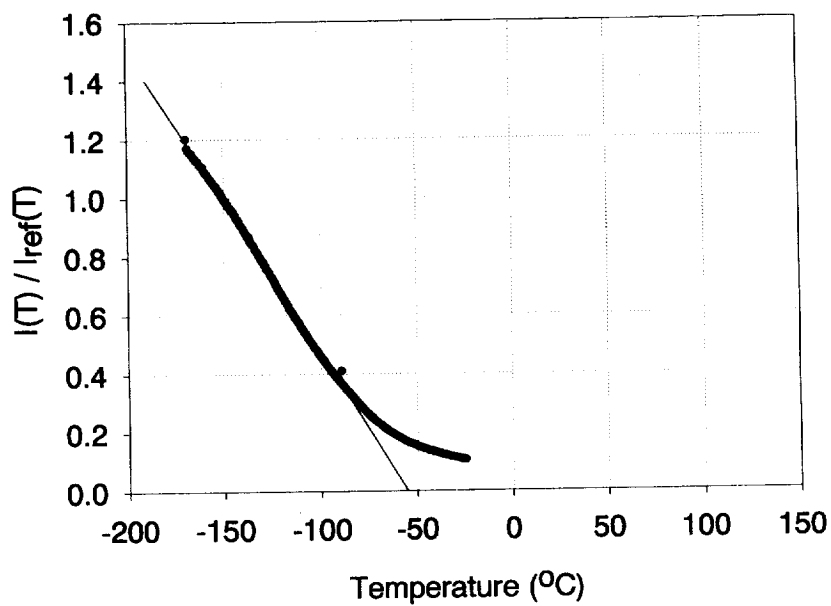
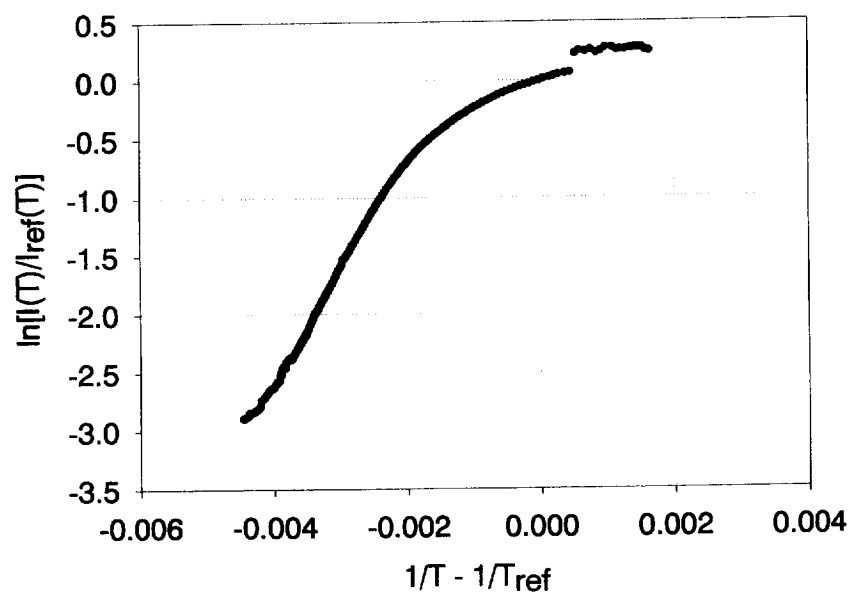
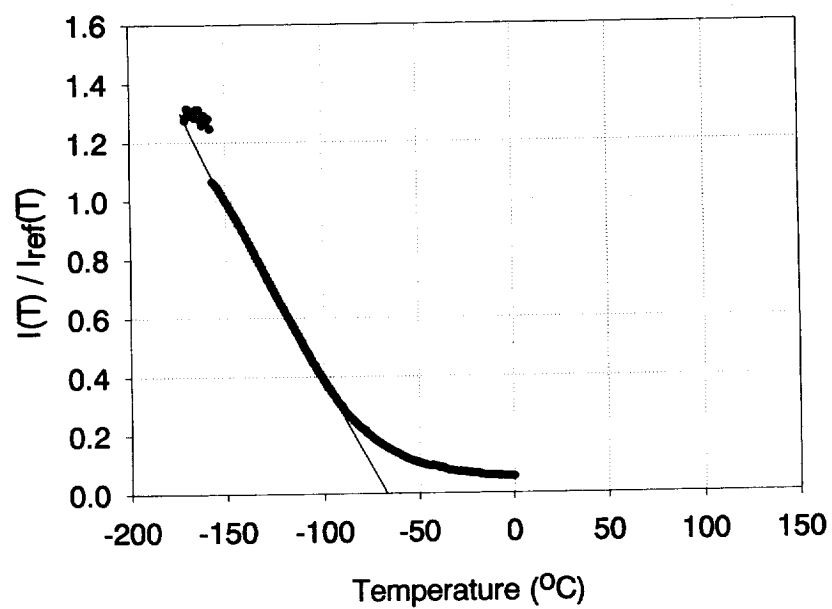
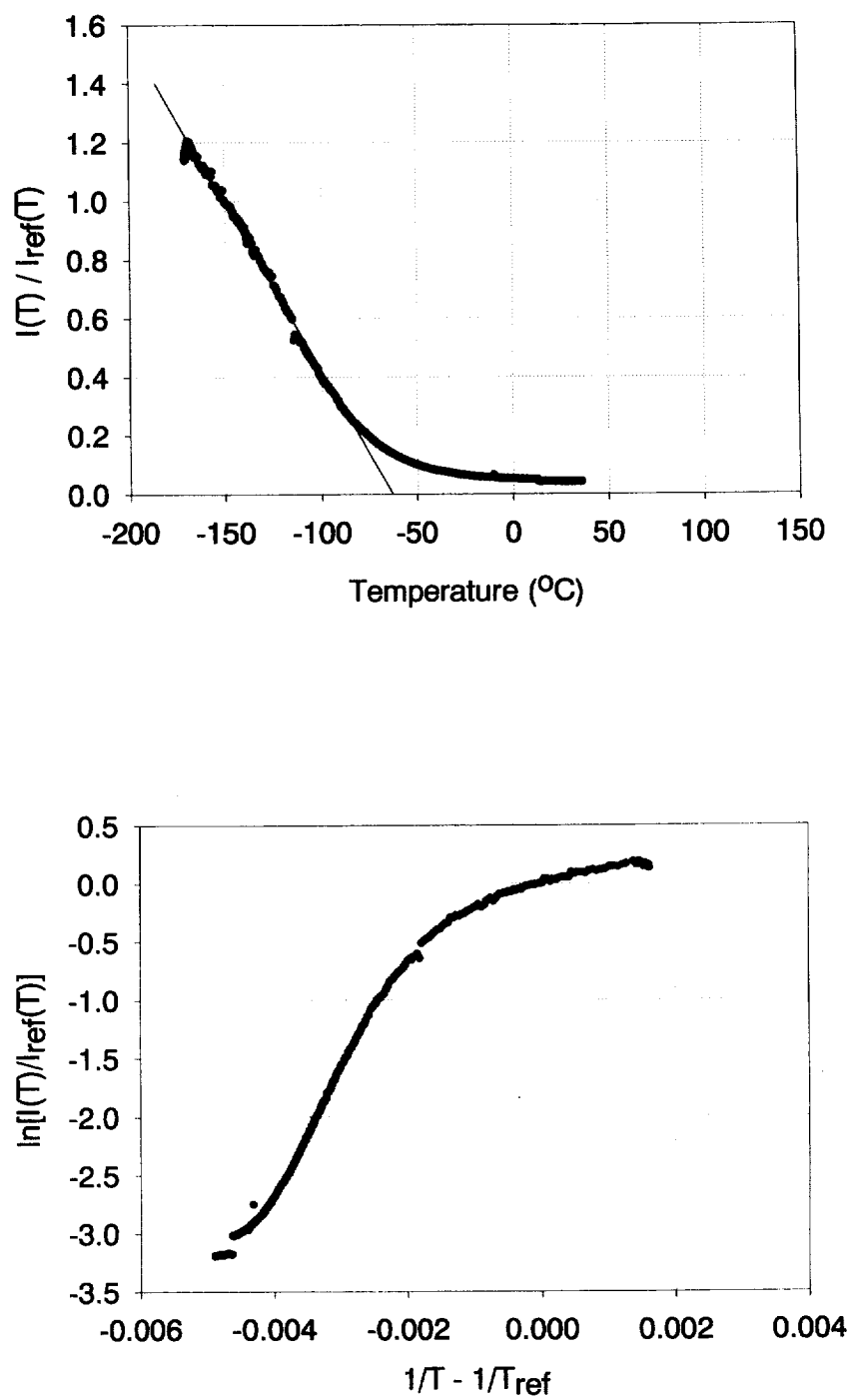


Figure A.21:  $[\text{Ru}(\text{trpy})(\text{SO}_2\text{Me-trpy})](\text{PF}_6)_2$  in CC

Figure A.22:  $[\text{Ru}(\text{trpy})_2](\text{DS})_2$  in CC

Figure A.23:  $[\text{Ru}(\text{trpy}_2)](\text{TFPB})_2$  in CC

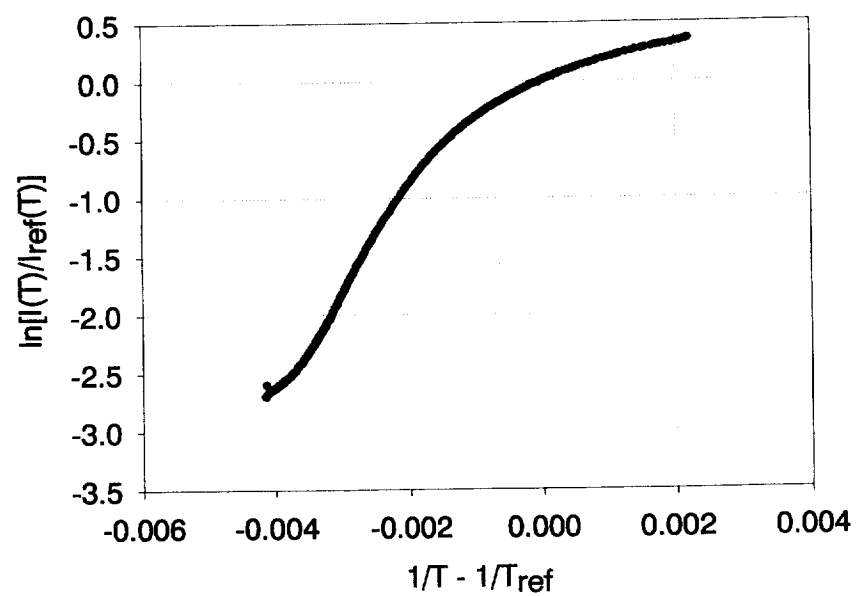
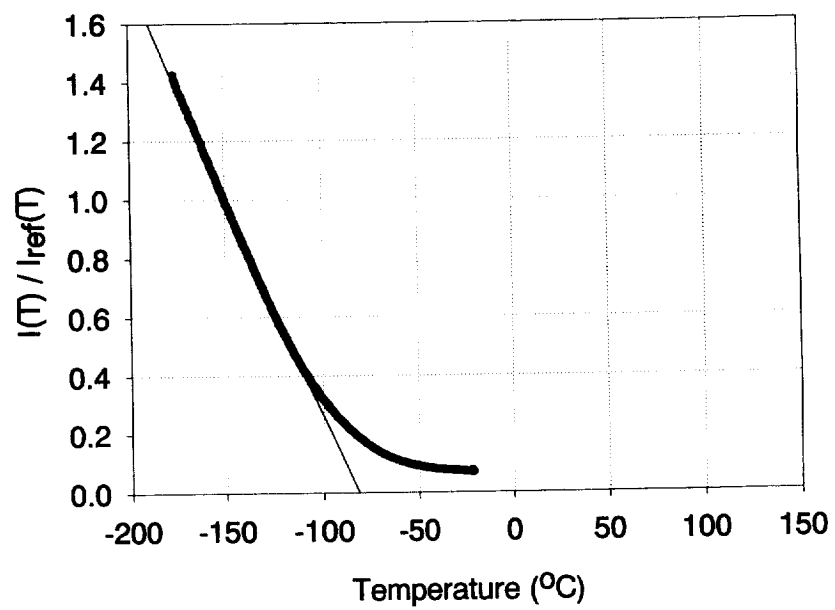
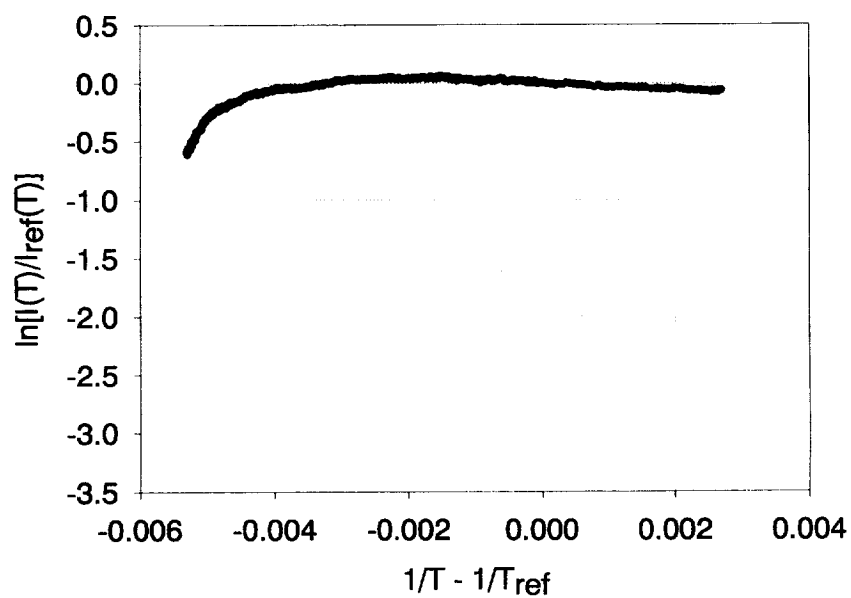
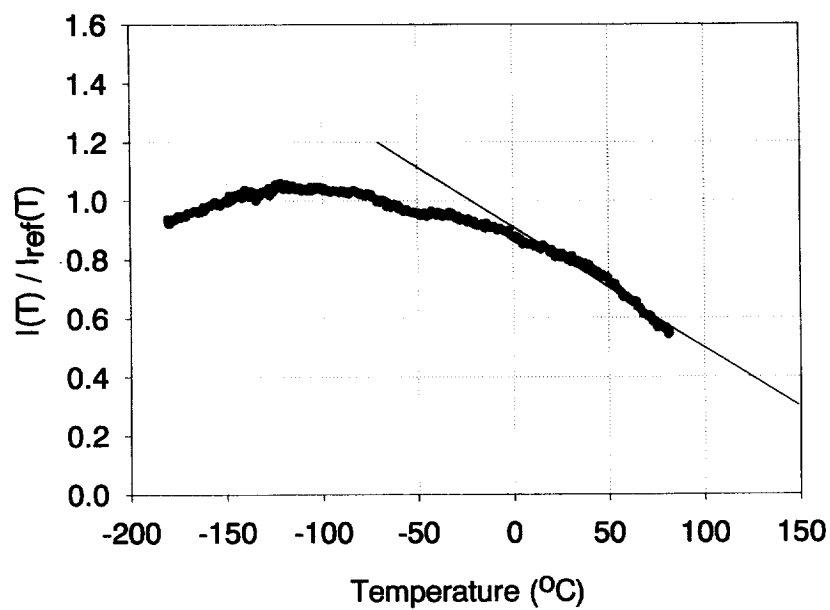


Figure A.24:  $[\text{Ru}(\text{ppd-trpy})_2](\text{TFPB})_2$  in CC

Figure A.25:  $[\text{Os}(\text{trpy})_2](\text{PF}_6)_2$  in CC

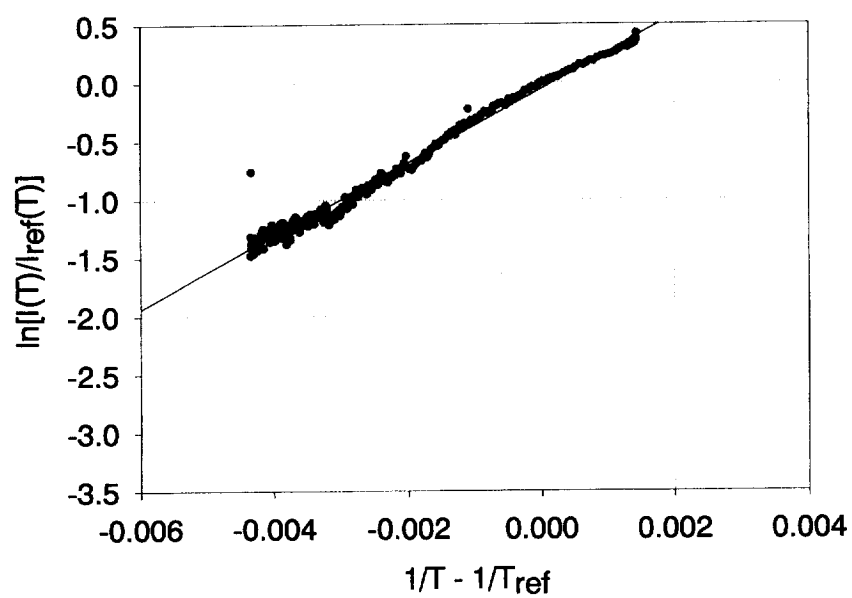
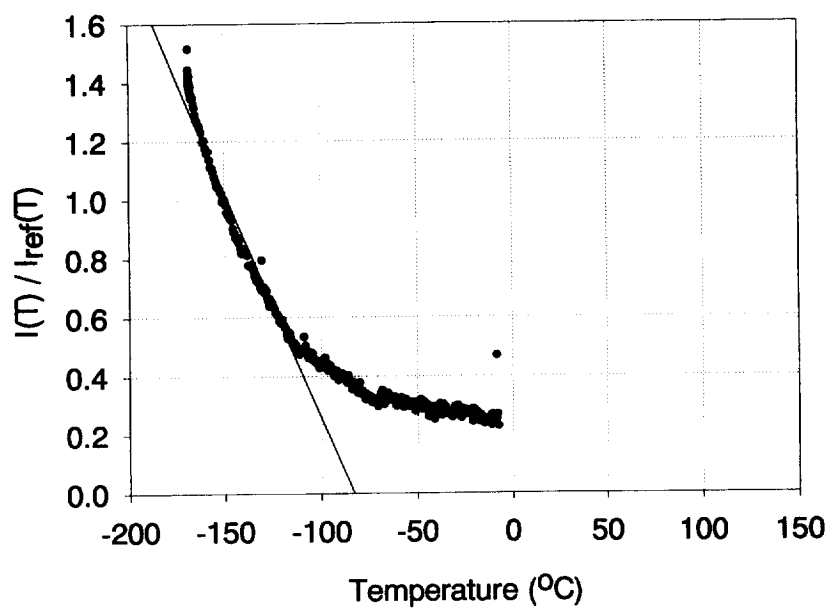


Figure A.26:  $[\text{Ru}(\text{trpy})(\text{Vh127})](\text{PF}_6)_2$  in GP-197

## APPENDIX B: ADDITIONAL PRESSURE CALIBRATION DATA

This appendix is a compilation of cryogenic pressure-sensitive paint calibration data. Data is presented in Stern-Volmer form. In all room temperature cases, reference conditions are taken at a static pressure of 14.7 psi with air as the test gas. All cryogenic data is normalized to reference conditions at O<sub>2</sub> partial pressure of 14.0 Pa.

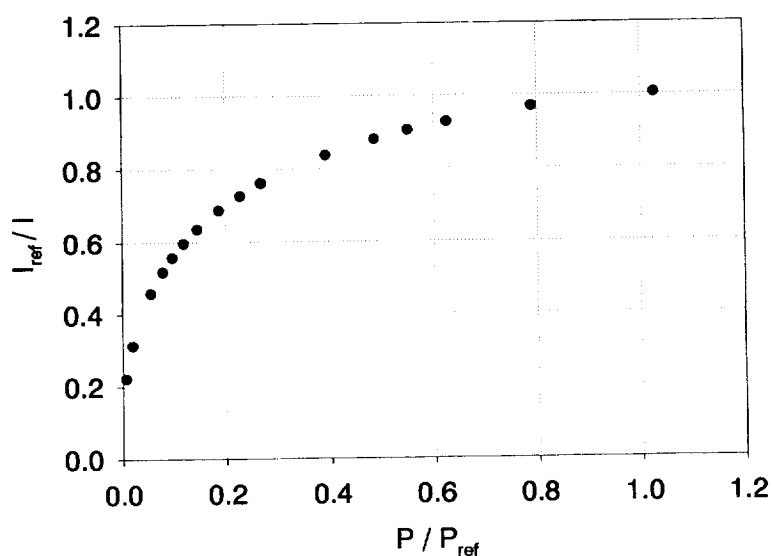


Figure B.1: Stern-Volmer for [Ru(ph<sub>2</sub>-phen)<sub>3</sub>] on Anodized Aluminum – 25 °C



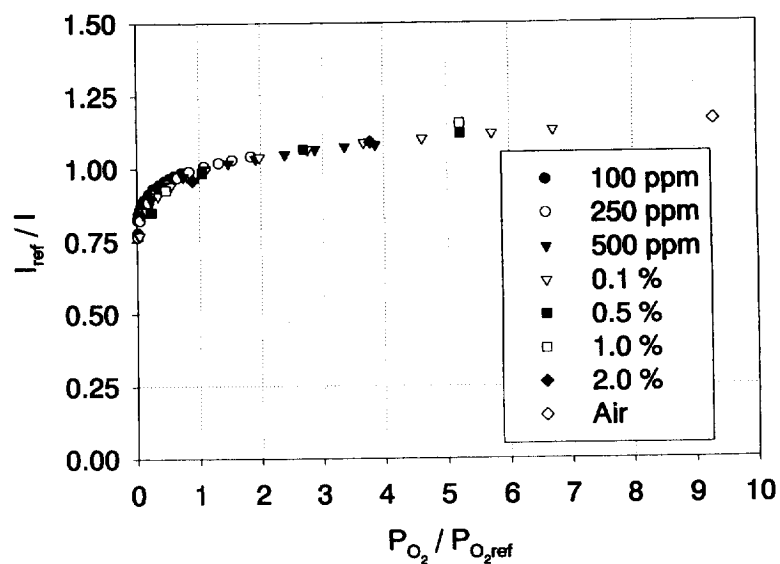


Figure B.2:  $[Ru(ph_2-phen)_3]$  on Anodized Aluminum – 150 K

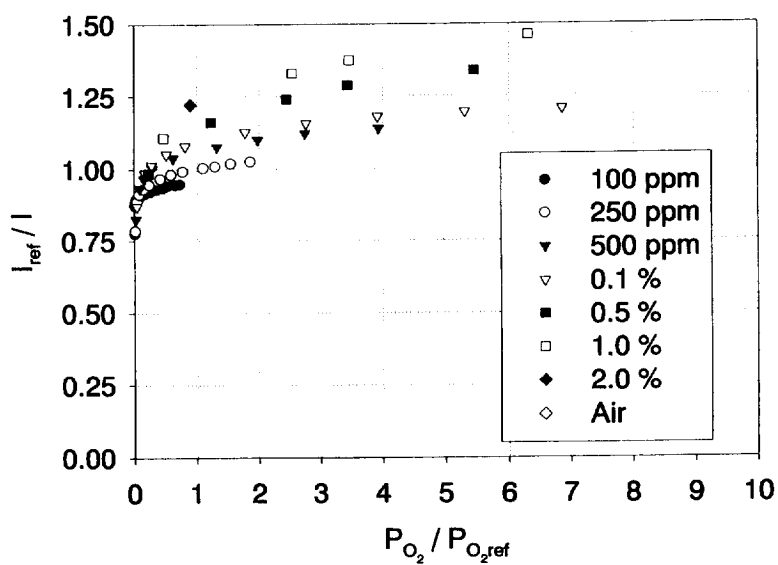


Figure B.3:  $[Ru(ph_2-phen)_3]$  on Anodized Aluminum – 100 K

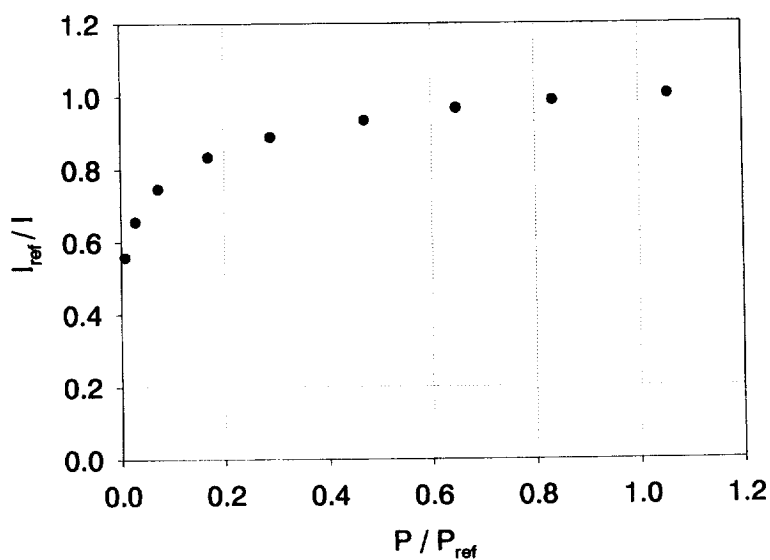


Figure B.4: Stern-Volmer for  $[Ru(ph_2-phen)_3]$  on Anodized 2024 Al Alloy – 25 °C

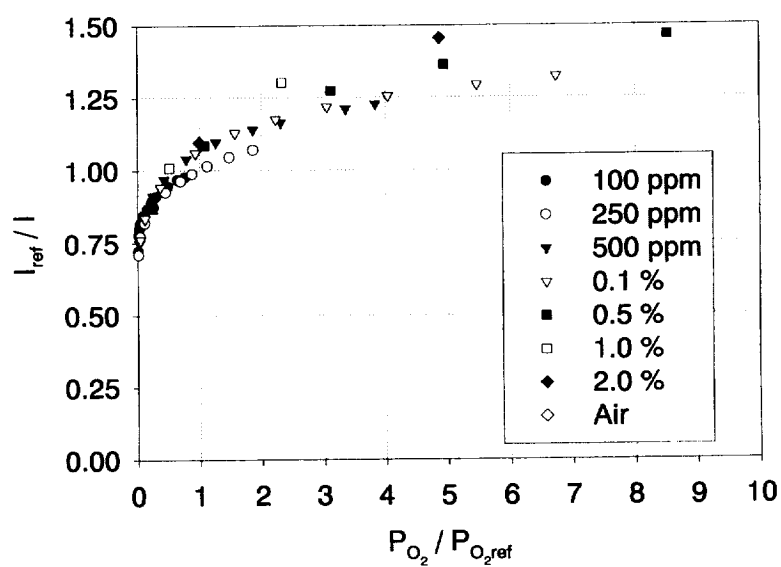


Figure B.5:  $[Ru(ph_2-phen)_3]$  on Anodized 2024 Al Alloy – 150 K

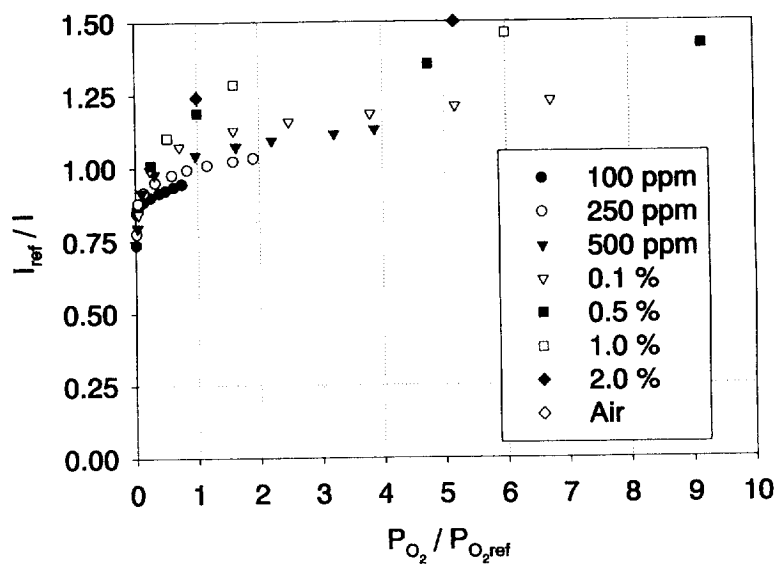


Figure B.6:  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  on Anodized 2024 Al Alloy – 100 K

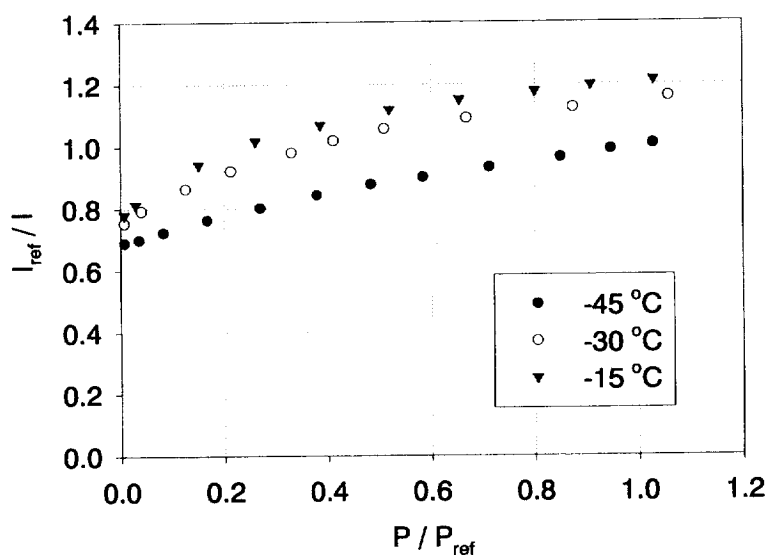


Figure B.7: Matrix Calibration for  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  in RTV

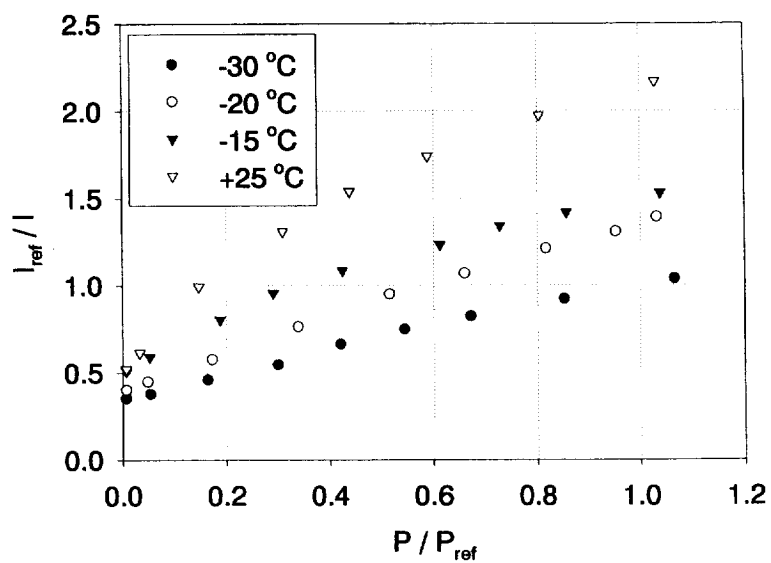


Figure B.8: Matrix Calibration for  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  in RTV + 0.5 g Silica Gel

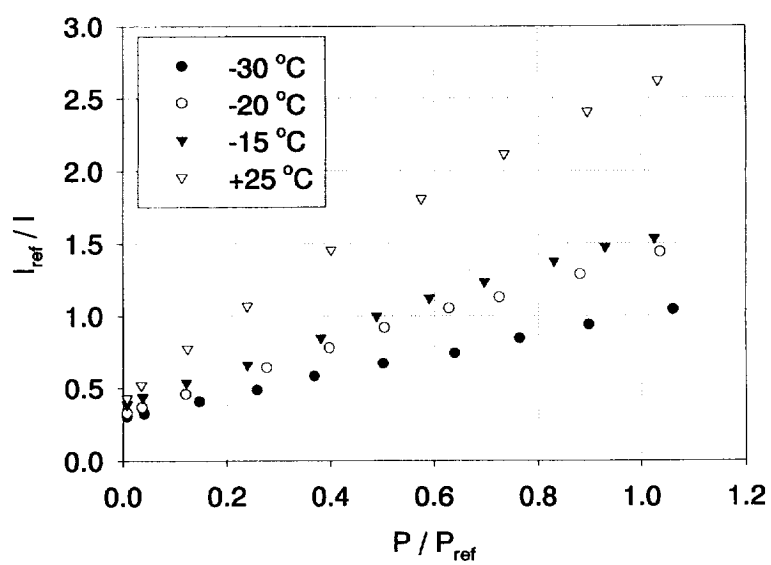


Figure B.9: Matrix Calibration for  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  in RTV + 1.0 g Silica Gel

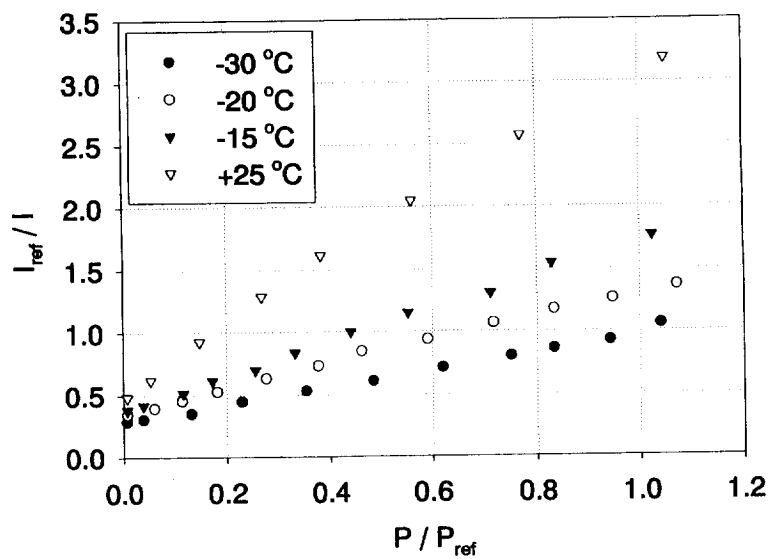


Figure B.10: Matrix Calibration for  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  in RTV + 2.5 g Silica Gel

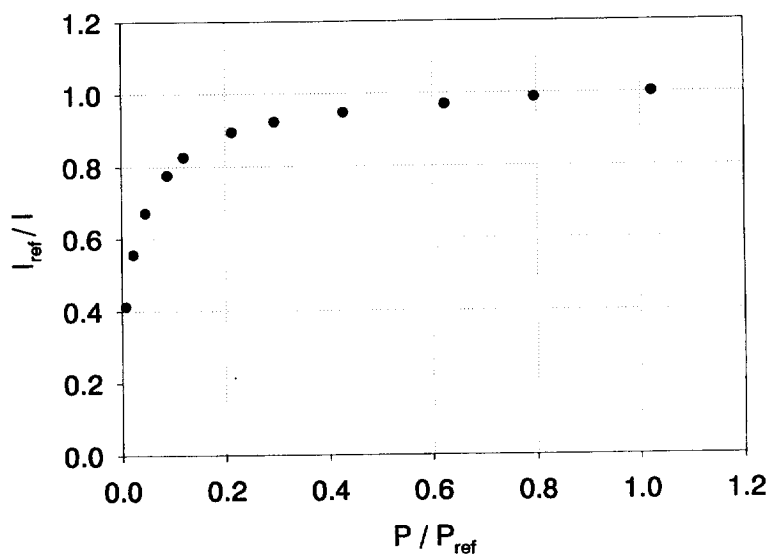


Figure B.11: Stern-Volmer for PtTFPP in RTV + 2.0 g RTV - 25 °C

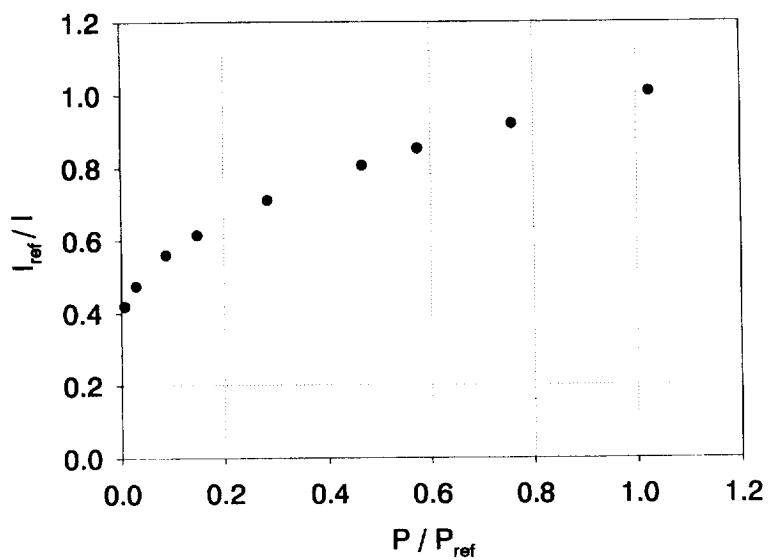


Figure B.12: Stern-Volmer for  $[Ru(ph_2-phen)_3]$  in GP-197 + 1.0g Silica Gel – 25 °C

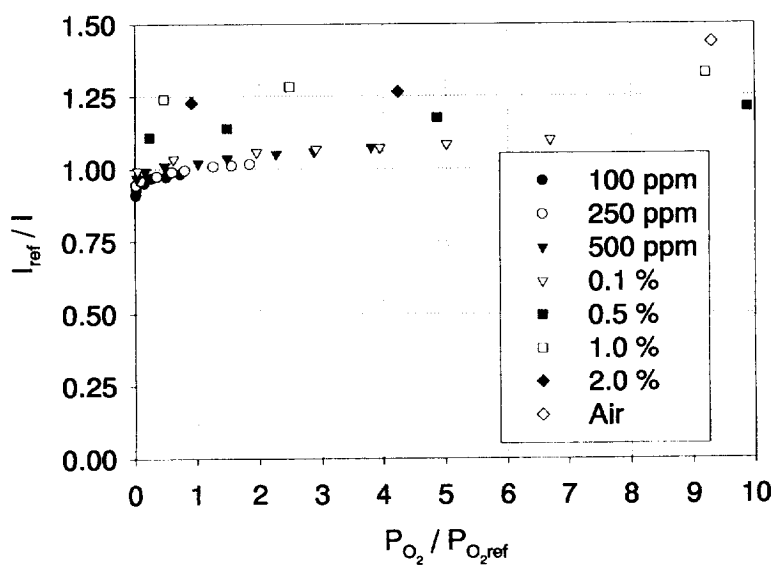


Figure B.13:  $[Ru(ph_2-phen)_3]$  in GP-197 + 1.0g Silica Gel – 150 K

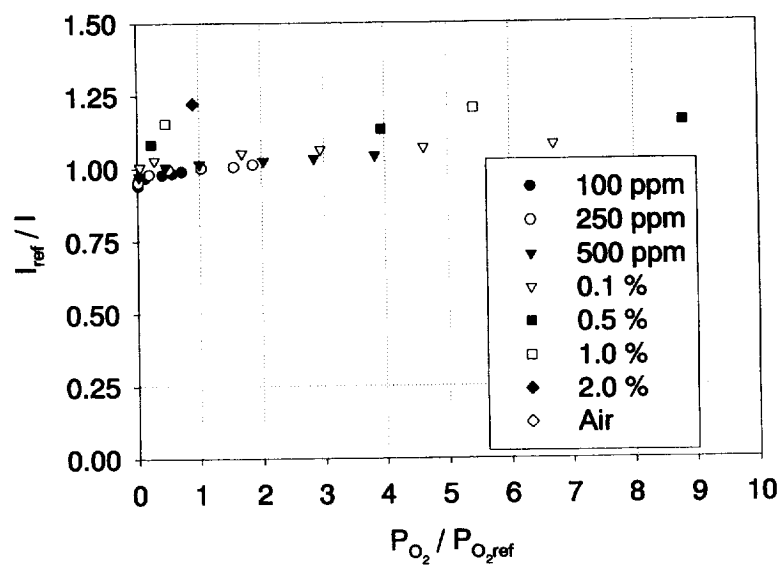


Figure B.14:  $[Ru(ph_2-phen)_3]$  in GP-197 + 1.0g Silica Gel – 100 K

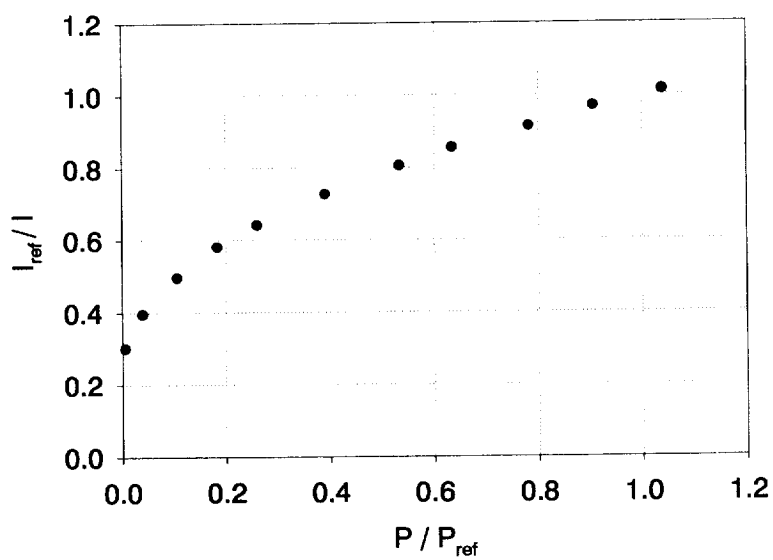


Figure B.15: Stern-Volmer for  $[Ru(ph_2-phen)_3]$  in GP-197 + 2.0g Silica Gel – 25 °C

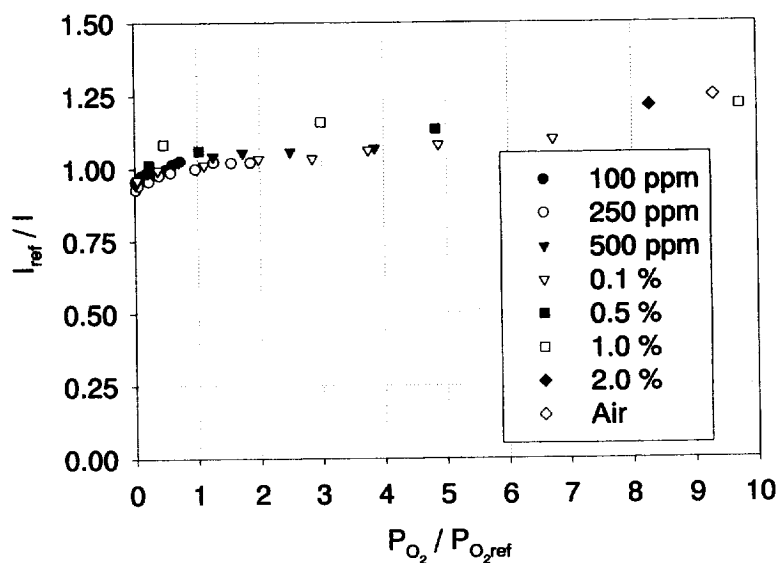


Figure B.16:  $[Ru(ph_2-phen)_3]$  in GP-197 + 2.0g Silica Gel – 150 K

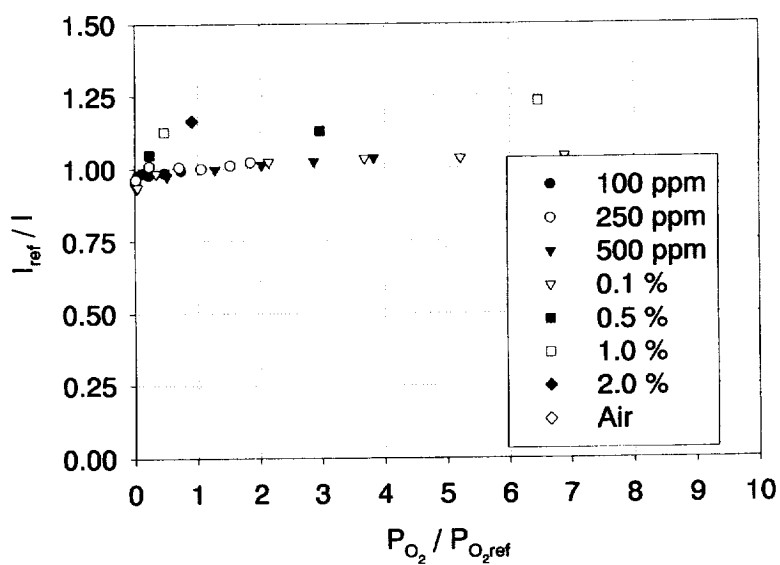


Figure B.17:  $[Ru(ph_2-phen)_3]$  in GP-197 + 2.0g Silica Gel – 100 K



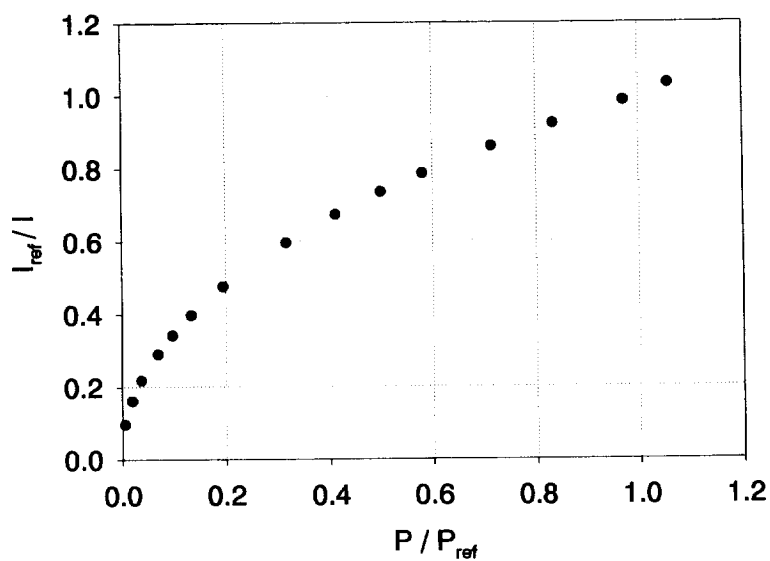


Figure B.18: Stern-Volmer for PtTFPP in GP-197 + 2.0 g Silica Gel – 25 °C

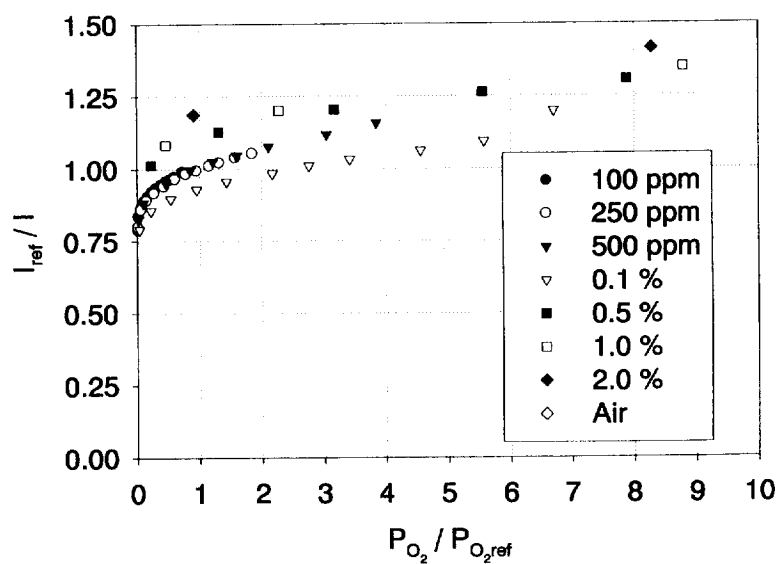


Figure B.19: PtTFPP in GP-197 + 2.0 g Silica Gel – 150 K

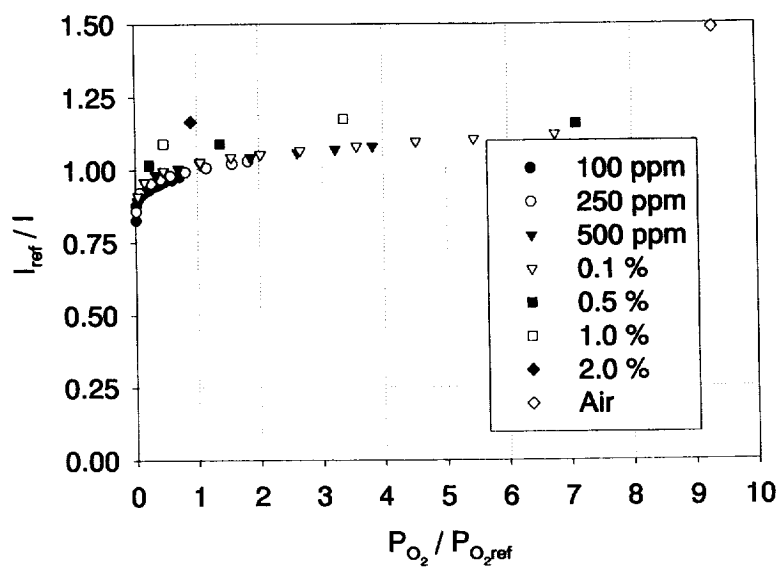


Figure B.20: PtTFPP in GP-197 + 2.0 g Silica Gel – 100 K

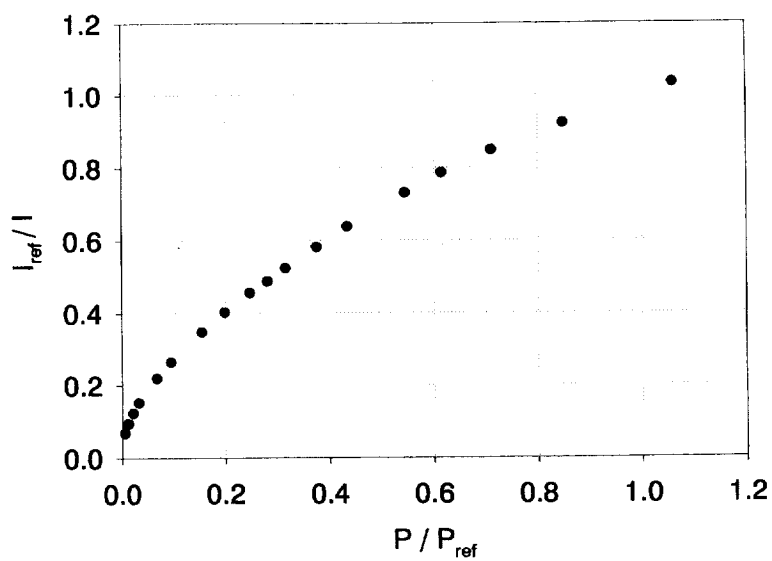


Figure B.21: Stern-Volmer for PtOEP in GP-197 + 2.0 g Silica Gel – 25 °C

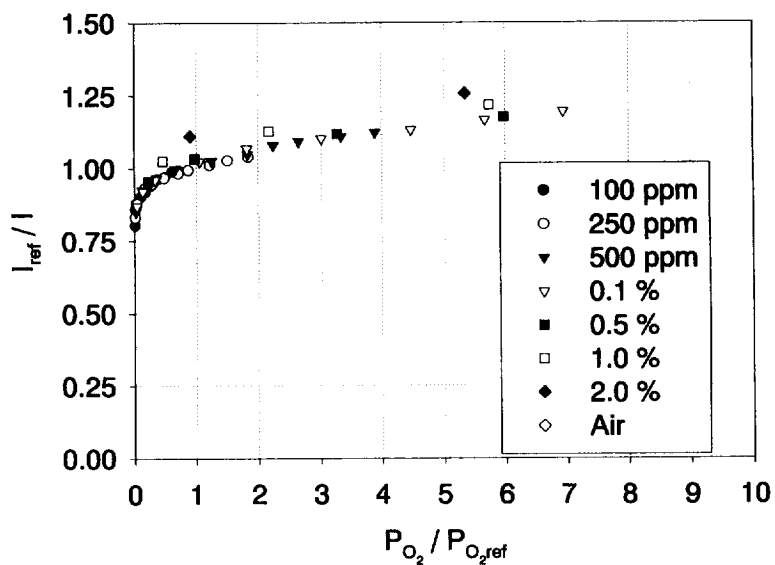


Figure B.22: PtOEP in GP-197 + 2.0 g Silica Gel – 150 K

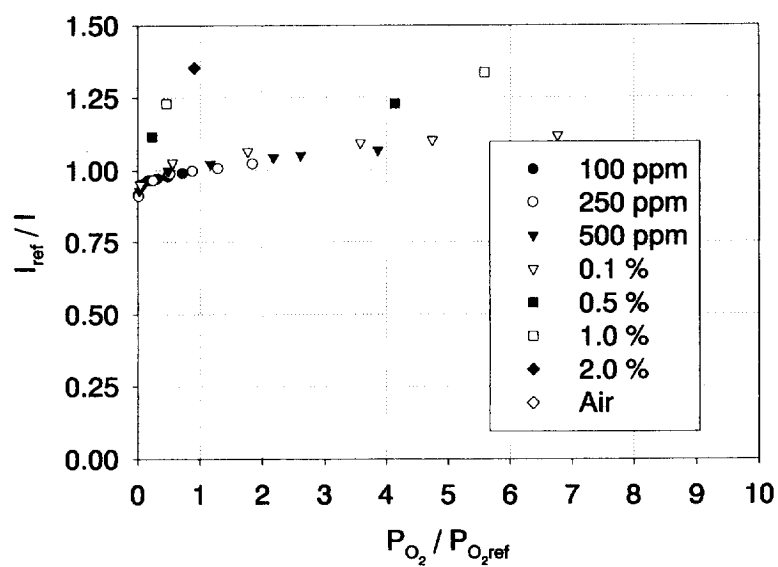


Figure B.23: PtOEP in GP-197 + 2.0 g Silica Gel – 100 K

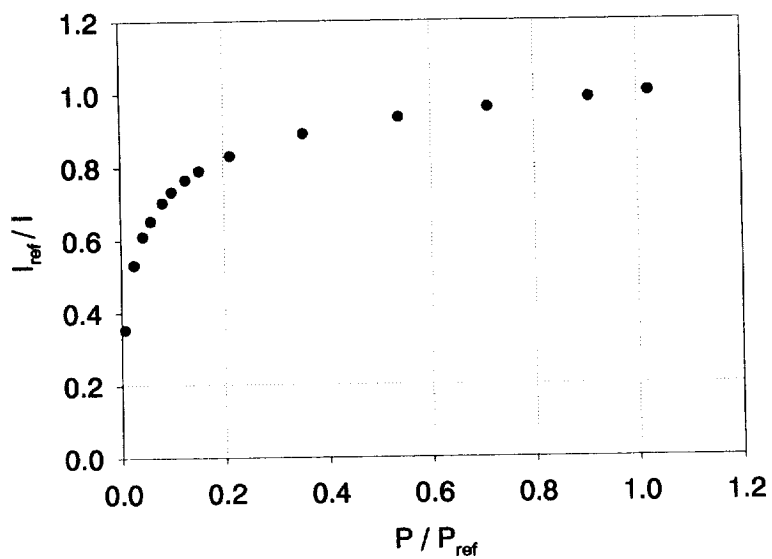


Figure B.24: Stern-Volmer for  $[Ru(ph_2-phen)_3]$  on TLC – 25 °C

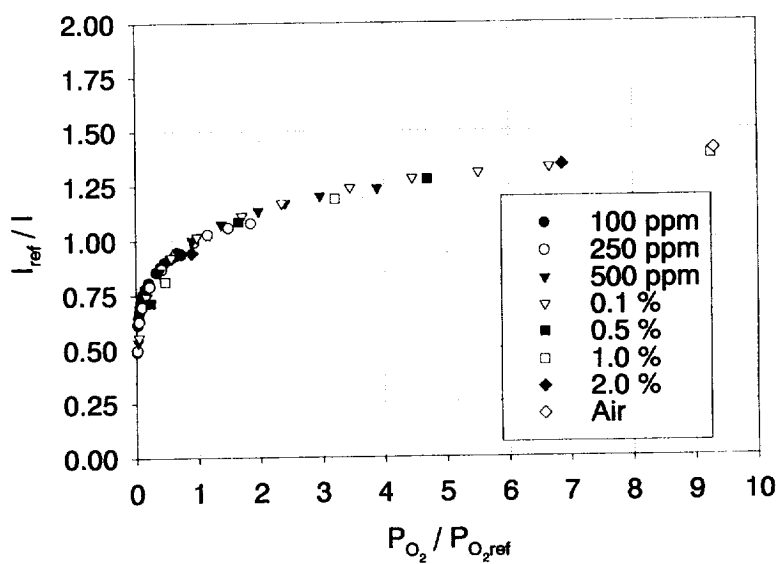


Figure B.25:  $[Ru(ph_2-phen)_3]$  on TLC – 150 K

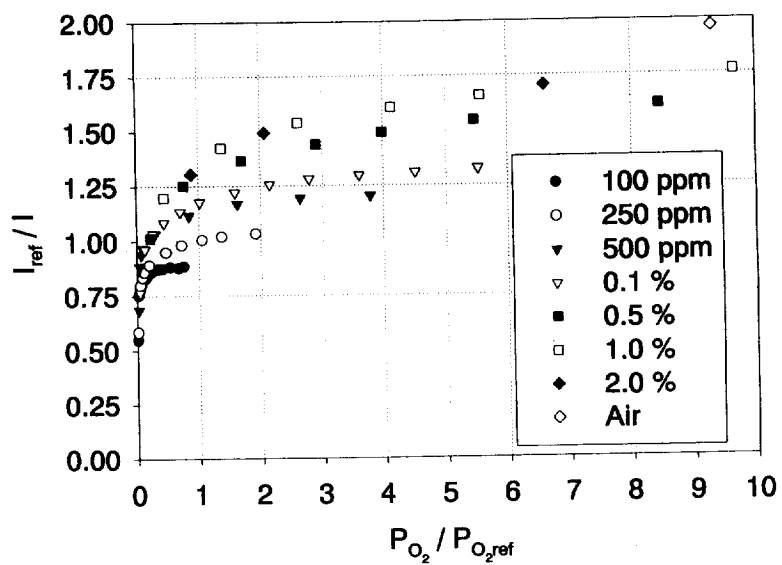


Figure B.26:  $[Ru(ph_2-phen)_3]$  on TLC – 100 K

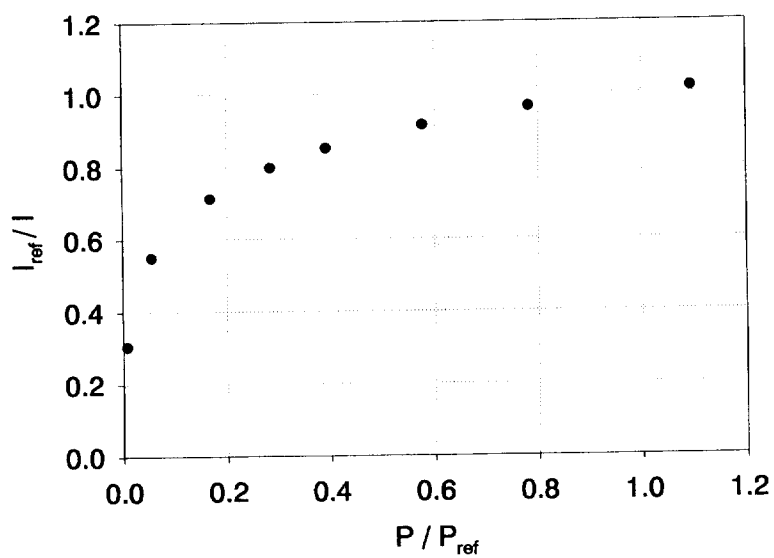


Figure B.27: Stern-Volmer for PtTFPP on TLC – 25 °C

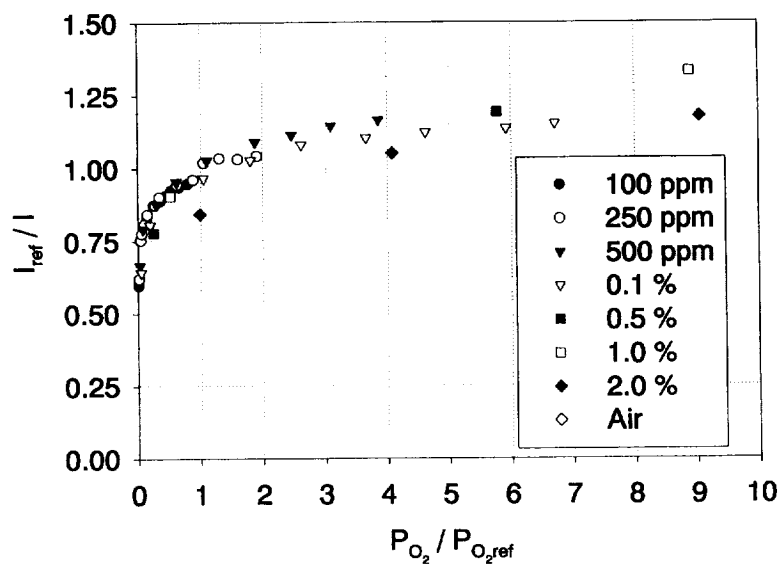


Figure B.28: PtTFPP on TLC – 150 K

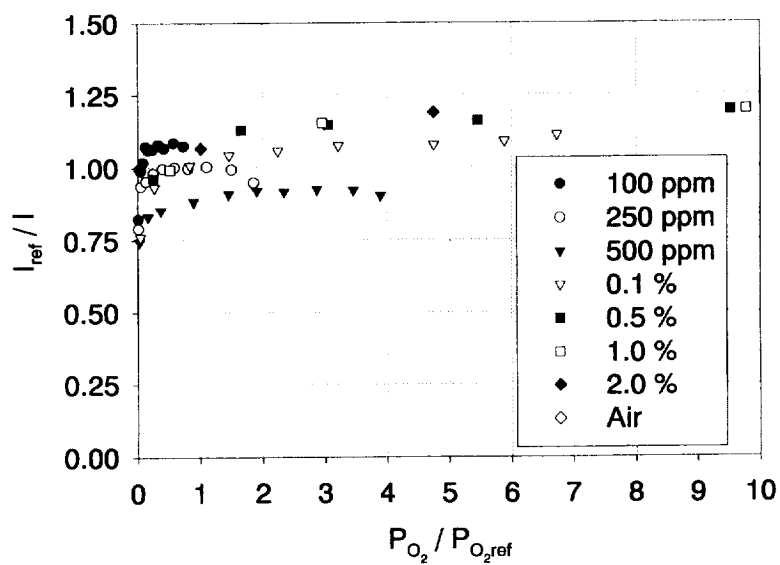


Figure B.29: PtTFPP on TLC – 100 K

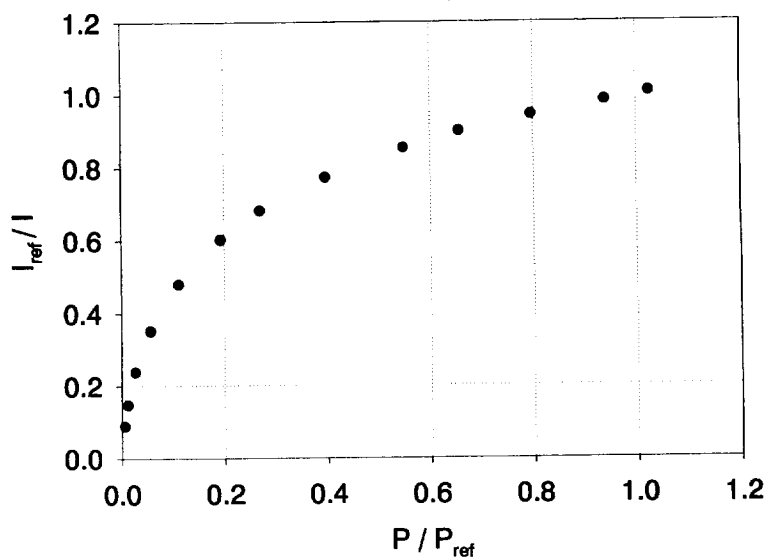


Figure B.30: Stern-Volmer for PtOEP on TLC – 25 °C

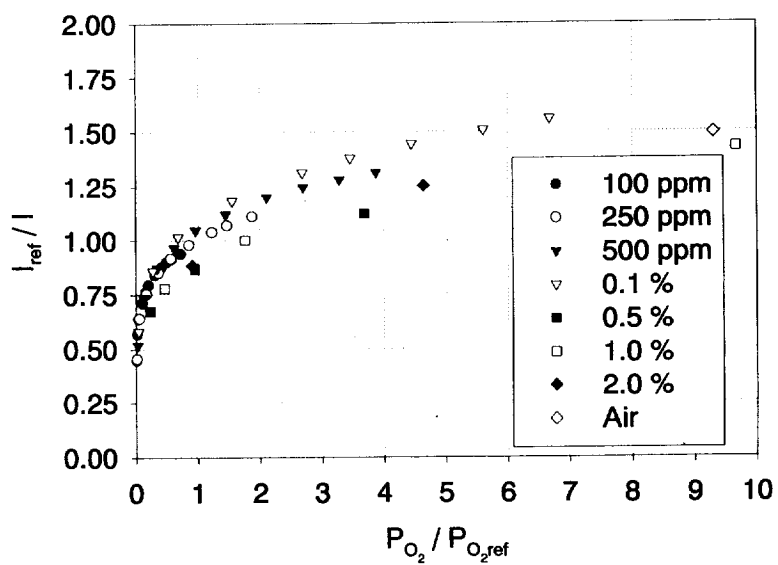


Figure B.31: PtOEP on TLC – 150 K

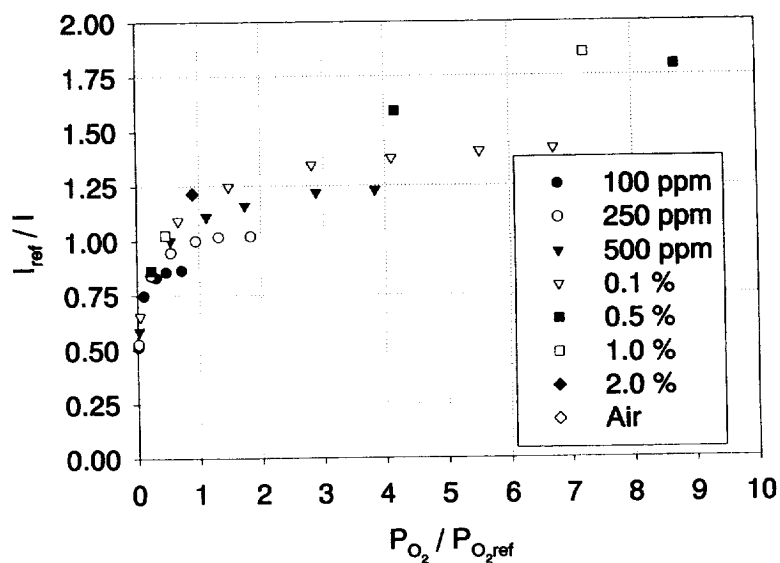
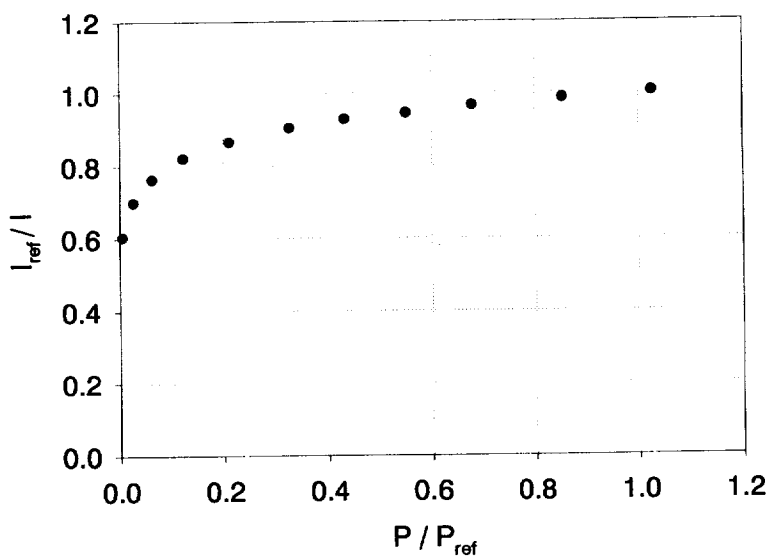


Figure B.32: PtOEP on TLC – 100 K

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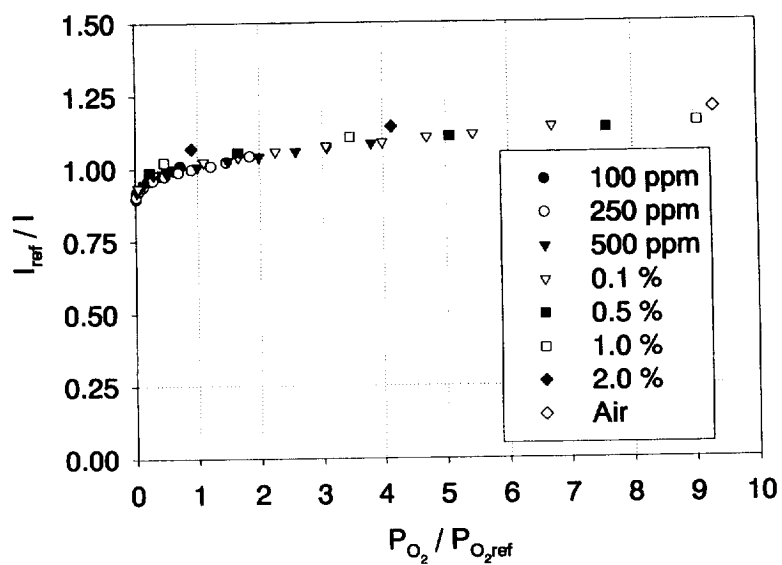


Figure B. 34:  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  in Filter Paper – 150 K

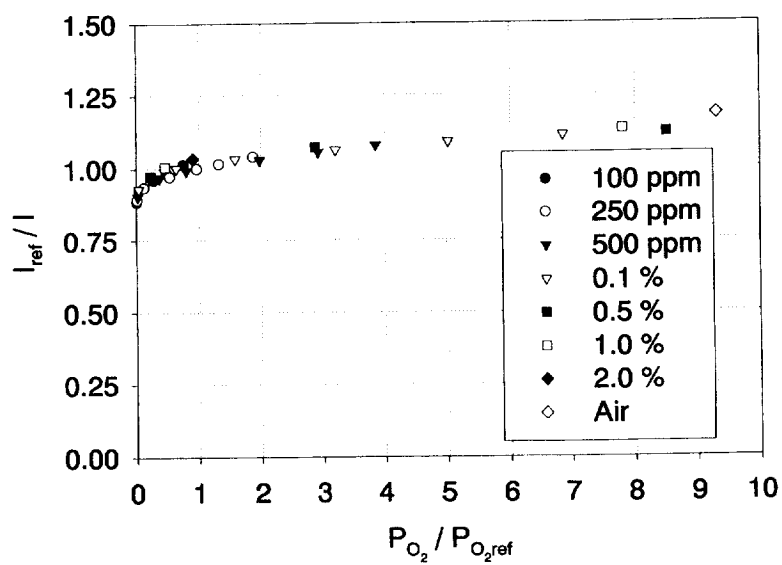


Figure B.35:  $[\text{Ru}(\text{ph}_2\text{-phen})_3]$  in Filter Paper – 100 K

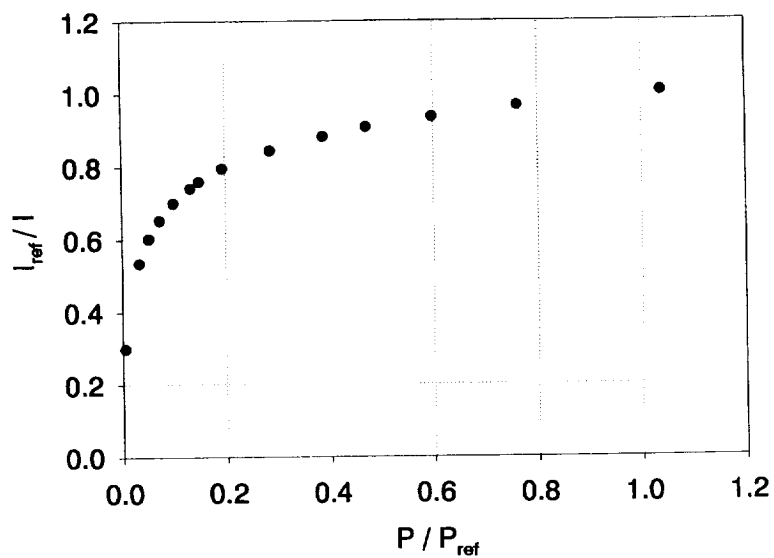


Figure B.36: Stern-Volmer for PtTFPP in Filter Paper – 25 °C

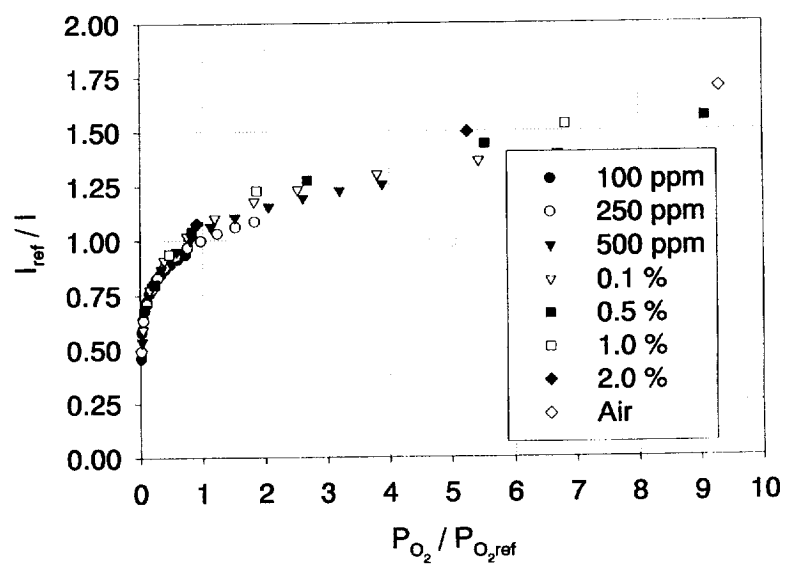


Figure B.37: PtTFPP in Filter Paper – 150 K

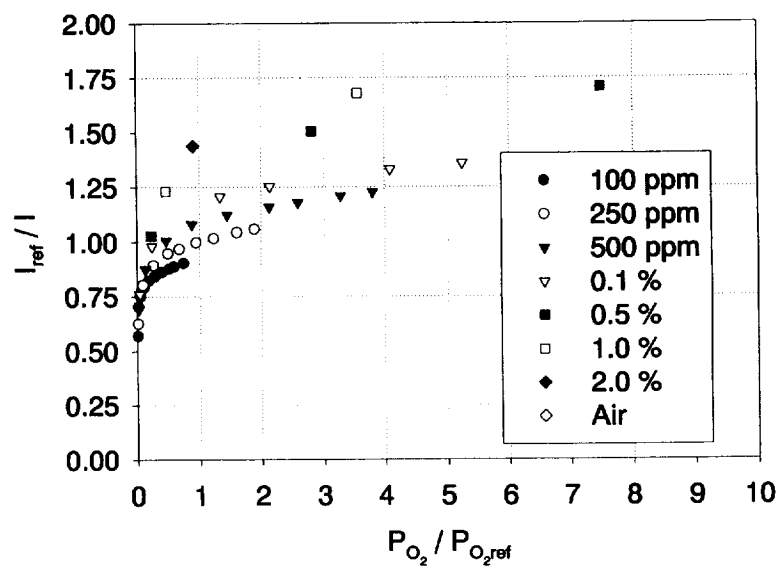


Figure B.38: PtTFPP in Filter Paper – 100 K

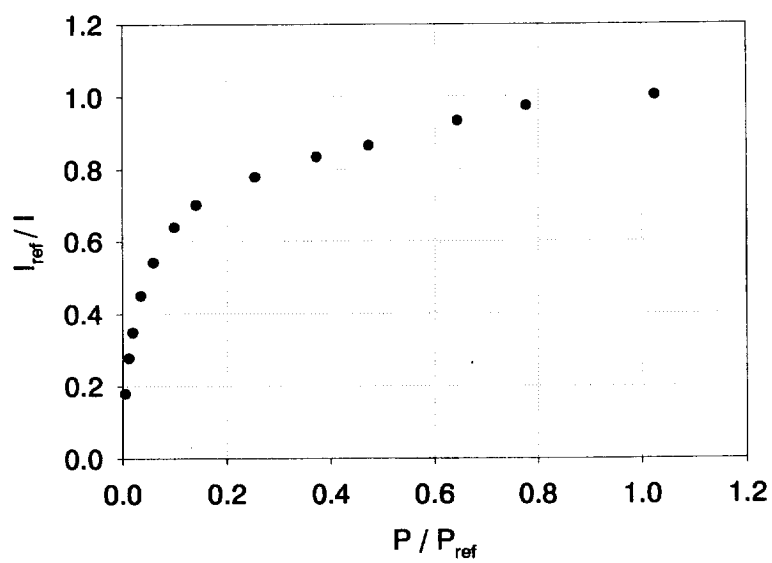


Figure B.39: Stern-Volmer for PtOEP in Filter Paper – 25 °C

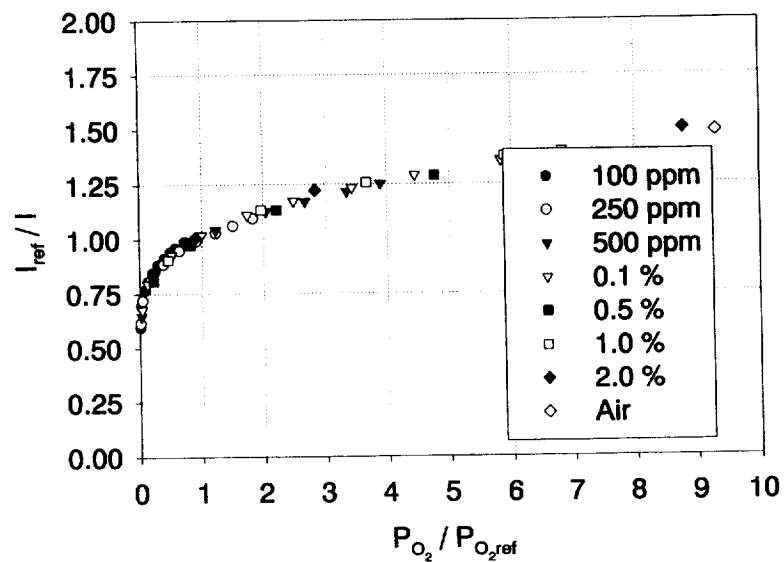


Figure B.40: PtOEP in Filter Paper – 150 K

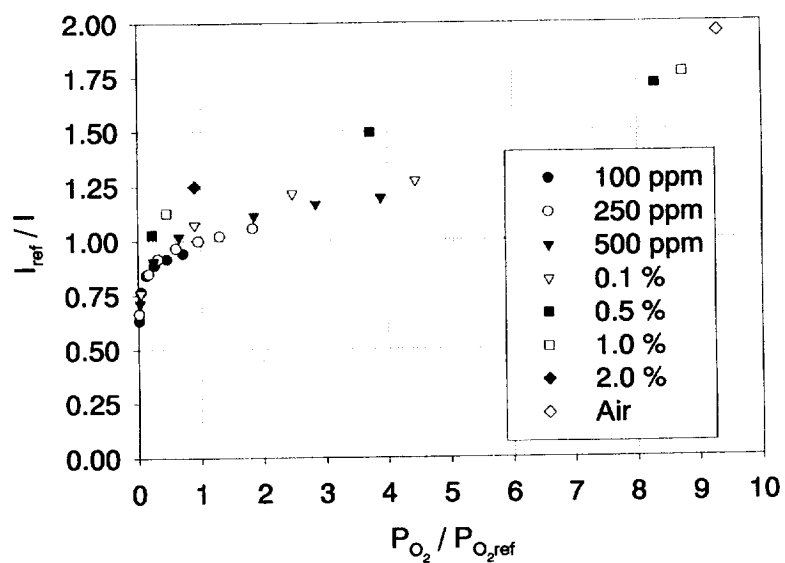


Figure B.41: PtOEP in Filter Paper – 100 K

**SYNTHETIC AND GEOMETRIC PERTURBATIONS  
OF THE EXCITED STATES OF  
METAL-POLYPYRIDINE SYSTEMS**

**A Thesis**

**Submitted to the Faculty**

**of**

**Purdue University**

**by**

**Corey Thomas Cunningham**

**In Partial Fulfillment of the**

**Requirements for the Degree**

**of**

**Doctor of Philosophy**

**December 1998**

To ALL of my family; my loving wife Kari;  
Miss Money Penny and the one and only Satan Dog

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## ABBREVIATIONS

|                                     |                                                                 |
|-------------------------------------|-----------------------------------------------------------------|
| Å                                   | Angstrom                                                        |
| bcp                                 | 2,9-dimethyl-4,7-diphenyl-1,10-phenanthroline                   |
| bipy                                | 2,2-bipyridine                                                  |
| BPh <sub>4</sub>                    | tetraphenylborate anion                                         |
| <i>p</i> -Br-ph-trpy                | 4'- <i>p</i> -bromophenyl-2,2':6',2"-terpyridine                |
| C <sub>6</sub> F <sub>5</sub> -trpy | 4'-pentafluorophenyl-2,2':6',2"-terpyridine                     |
| <i>p</i> -Cl-ph-trpy                | 4'- <i>p</i> -chlorophenyl-2,2':6',2"-terpyridine               |
| CT                                  | charge-transfer                                                 |
| dap                                 | 2,9-di- <i>p</i> -anisoyl-1,10-phenanthroline                   |
| dbdmp                               | 2,9-di- <i>n</i> -butyl-4,7-dimethyl-1,10-phenanthroline        |
| dbp                                 | 2,9-di- <i>n</i> -butyl-1,10-phenanthroline                     |
| dbtmp                               | 2,9-di- <i>n</i> -butyl-3,4,7,8-tetramethyl-1,10-phenanthroline |
| dcyp                                | 2,9-dicyclohexyl-1,10-phenanthroline                            |
| dipp                                | 2,9-di- <i>iso</i> -propyl-1,10-phenanthroline                  |
| dmbp                                | 6,6'-dimethyl-2,2'-bipyridine                                   |
| DMF                                 | <i>N,N'</i> -dimethylformamide                                  |
| dmp                                 | 2,9-dimethyl-1,10-phenanthroline                                |
| dnpp                                | 2,9-di- <i>neo</i> -pentyl-1,10-phenanthroline                  |

|                 |                                                                       |
|-----------------|-----------------------------------------------------------------------|
| dnpentp         | 2,9-di- <i>n</i> -pentyl-1,10-phenanthroline                          |
| dsbp            | 2,9-di- <i>sec</i> -butyl-1,10-phenanthroline                         |
| dpdmp           | 2,9-diphenyl-4,7-dimethyl-1,10-phenanthroline                         |
| dpp             | 2,9-diphenyl-1,10-phenanthroline                                      |
| dptmp           | 2,9-diphenyl-3,4,7,8-tetramethyl-1,10-phenanthroline                  |
| $\epsilon$      | molar extinction coefficient, $M^{-1}cm^{-1}$                         |
| EH              | Extended Hückel                                                       |
| Em              | emission                                                              |
| EtO-trpy        | 4'-ethoxy-2,2':6',2''-terpyridine                                     |
| $\phi$          | emission quantum yield                                                |
| HMPA            | hexamethylphosphoramide                                               |
| HOMO            | highest occupied molecular orbital                                    |
| IR              | infrared                                                              |
| K               | Kelvin                                                                |
| $k_o$           | excited state decay, $s^{-1}$                                         |
| $k_1$           | formation of the exciplex, $M^{-1}s^{-1}$                             |
| $k_{-1}$        | decomposition of the exciplex into starting materials, $M^{-1}s^{-1}$ |
| $k_Q$           | quenching of the exciplex, $s^{-1}$                                   |
| $k_q$           | overall quenching constant, $M^{-1}s^{-1}$                            |
| $\lambda$       | wavelength                                                            |
| $\lambda_{abs}$ | absorbance maximum                                                    |
| $\lambda_{em}$  | emission maximum                                                      |

|                               |                                                      |
|-------------------------------|------------------------------------------------------|
| LUMO                          | lowest unoccupied molecular orbital                  |
| M                             | Molar, moles/liter                                   |
| MeS-trpy                      | 4'-methylthio-2,2':6',2''-terpyridine                |
| MeSO <sub>2</sub> -trpy       | 4'-methylsulfonyl-2,2':6',2''-terpyridine            |
| Me <sub>2</sub> N-trpy        | 4'-dimethylamino-2,2':6',2''-terpyridine             |
| mL                            | milliliter                                           |
| MLCT                          | metal-to-ligand charge transfer                      |
| mmp                           | 2-methyl-1,10-phenanthroline                         |
| NB                            | notebook                                             |
| NC-trpy                       | 4'-cyano-2,2':6',2''-terpyridine                     |
| nm                            | nanometers                                           |
| NN                            | generic phenanthroline ligand                        |
| <i>p</i> -NO <sub>2</sub> -ph | 4'- <i>para</i> -nitrophenyl-2,2':6',2''-terpyridine |
| ppd-trpy                      | 4'- <i>N</i> -piperidinyl-2,2':6',2''-terpyridine    |
| ns                            | nanoseconds                                          |
| ph-trpy                       | 4'-phenyl-2,2':6',2''-terpyridine                    |
| phen                          | 1,10-phenanthroline                                  |
| pK <sub>a</sub>               | proton acidity                                       |
| PM3                           | Perturbation Method 3                                |
| pmp                           | 2,3,4,7,8-pentamethyl-1,10-phenanthroline            |
| ppm                           | parts per million                                    |
| PSP                           | pressure sensitive paint                             |

|            |                                                       |
|------------|-------------------------------------------------------|
| 4-py-trpy  | 4'-(4-pyridyl)-2,2':6',2"-terpyridine                 |
| 3-py-trpy  | 4'-(3-pyridyl)-2,2':6',2"-terpyridine                 |
| 2-py-trpy  | 4'-(2-pyridyl)-2,2':6',2"-terpyridine                 |
| SHOMO      | second highest occupied molecular orbital             |
| SLUMO      | second lowest occupied molecular orbital              |
| $\tau$     | excited state lifetime                                |
| $\tau_0$   | excited state lifetime in the absence of quencher     |
| $\Theta_z$ | dihedral angle between two opposing phen ligands      |
| TfO-trpy   | 4'-trifluoromethylsulfonato-2,2':6',2"-terpyridine    |
| TFPB       | tetrakis[3,5-bis(trifluoromethyl)-phenyl]borate anion |
| THF        | tetrahydrofuran                                       |
| TLC        | thin layer chromatography                             |
| trpy       | 2,2':6',6"-terpyridine                                |
| tmbp       | 4,4',6,6'-tetramethyl-2,2'-bipyridine                 |
| tmp        | 3,4,7,8-tetramethyl-1,10-phenanthroline               |
| TSP        | temperature sensitive paint                           |
| UV         | ultraviolet                                           |
| Vis        | visible                                               |
| zyz        | 2,6-bis-pyrazinyl-pyridine                            |

## ABSTRACT

Cunningham, Corey T. Ph.D., Purdue University, December, 1998.  
Synthetic and Geometric Perturbations of the Excited States of Metal-Polypyridine Systems. Major Professor: David R. McMillin.

This work encompasses three chapters investigating modifications to the excited states of ruthenium(II) and copper(I) polypyridine systems. The main emphasis is on understanding what changes occur when the polypyridine ligands surrounding the metal center are modified. The synthetic modifications are those done in order to create new ligands with specialized steric and electronic characteristics. The geometric modifications refer to environmental changes placed on the coordination complex. The photophysical properties that are a result of the changes are studied, characterized, and discussed in order to better understand the governing factors of the excited states.

Chapter 1 focuses on electronic modifications of ruthenium(II) bis-terpyridine. The new compounds are then employed as luminescent molecular temperature sensors. The research was done in conjunction with Dr. John Sullivan of the Aerospace Engineering Department at Purdue University and the sensors were evaluated in a cryogenic wind tunnel at the National Aerospace Laboratory in Japan. This project has lead to the development of luminescent sensors that are effective at sensing shock waves at cryogenic temperatures. This is the first time a shock wave has been visualized at cryogenic temperatures. This method of detection is an improvement over existing methods as it is cheaper, easier, and gives a complete map of the wind tunnel model.

The second and third chapters deal with copper(I) bis-phenanthroline complexes. In chapter 2, synthetic modifications to some phenanthroline ligands lead to new complexes that resist quenching by Lewis bases. The third chapter studies the

photophysics of the copper complexes in the solid state. In this chapter, the solid state geometry, dictated by the crystal structure, is shown to have a dramatic effect on the photochemistry of the copper compounds. Also in this chapter is the first reported emission from a copper phenanthroline, with no substituent in the 2,9 positions.

## **PUBLICATIONS**

# Luminescence Properties of Salts of the $[\text{Pt}(\text{trpy})\text{Cl}]^-$ and $[\text{Pt}(\text{trpy})(\text{MeCN})]^{2-}$ Chromophores: Crystal Structure of $[\text{Pt}(\text{trpy})(\text{MeCN})](\text{SbF}_6)_2$

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The crystal structure of  $[\text{Pt}(\text{trpy})(\text{MeCN})](\text{SbF}_6)_2$ , where trpy denotes 2,2':6',2''-terpyridine, shows that the platinum complex packs as a monomer; however, the  $^3\pi-\pi^*$  emission of the solid occurs at surprisingly long wavelengths at room temperature. At lower temperatures new, shorter-wavelength maxima appear. Of the known salts with the composition  $[\text{Pt}(\text{trpy})\text{Cl}]\text{A}$ , the  $\text{A} = \text{SbF}_6^-$  system is the lone example that exhibits a temperature-independent emission maximum. In these platinum(II) terpyridines, energy migration to defects or trap sites is one of the phenomena responsible for the temperature dependence of the solid-state emission spectrum. If trap emission is evident, the low-temperature spectral data are most representative of the bulk material.

## Introduction

Luminescent, square-planar complexes of Pt(II) containing *c,c'*-diimine ligands have intriguing spectroscopic and photophysical properties.<sup>1</sup> In a monomeric environment, such as in a dilute glass solution, the complexes may exhibit emission from intraligand<sup>2</sup> (IL), metal-to-ligand-charge-transfer<sup>3</sup> (MLCT), or ligand-field<sup>4</sup> (LF) states. Because these states are of similar energy, the relative ordering is sensitive to factors such as ligand field strength, diimine substituents, and the nature of the co-ligands. In the solid state, Pt–Pt or  $\pi-\pi$  interactions between chromophores often have a strong influence on the emission. Three idealized solid-state structure types occur: monomeric structures in which the Pt–Pt distances are all greater than 4.5 Å; linear-chain structures in which the Pt(II) complexes are stacked equidistantly (Pt–Pt separations of 3.2–3.4 Å) along an axis that is usually, but not always, perpendicular to the plane of the complex; and dimer structures in which the Pt complexes segregate into pairs.<sup>1</sup> Compounds with monomeric structures display luminescence properties similar to those observed in dilute solutions. On the other hand, those with linear-chain structures typically exhibit  $\pi^*(\text{L}) \rightarrow d^8$  emissions from metal–metal-to-ligand-charge-transfer (MMLCT) excited states.<sup>1</sup> With these systems, the emission undergoes a characteristic red shift at lower temperatures due to a decrease in the mean Pt–Pt spacing.<sup>4</sup> Compounds with dimer structures also typically exhibit MMLCT emissions, but less information is available about the temperature-dependent properties. However, one

study reported that the emissions from a series of ligand-bridged dimers blue-shift when the temperature drops from ambient to 77 K.<sup>5</sup>

By and large, Pt(II) complexes of the tridentate 2,2':6',2''-terpyridine (trpy) ligand possess luminescence properties much like those of the corresponding *c,c'*-diimine complexes. For example, Yip et al. have reported the properties of the  $[\text{Pt}(\text{trpy})\text{Cl}]\text{CF}_3\text{SO}_3$  salt at room temperature as well as 77 K, and they found that the emission maximum red-shifted at the lower temperature.<sup>6</sup> More recently, Bailey et al. examined the photophysical properties of a series of salts containing the  $[\text{Pt}(\text{trpy})\text{Cl}]^-$  moiety.<sup>7</sup> They assigned the low-temperature solid-state luminescence of these salts to  $^3\text{MMLCT}$  states, and they concluded that the emission energy varied with the counterion ( $\text{ClO}_4^-$ ,  $\text{Cl}^-$ ,  $\text{CF}_3\text{SO}_3^-$ , or  $\text{PF}_6^-$ ) because of differences in the Pt–Pt and  $\pi-\pi$  interactions in the lattice.<sup>7</sup> Contrary to the results of Yip et al., however, for all except the red perchlorate salt, Bailey et al. reported that the emission narrowed and exhibited a blue shift with a decrease in temperature.

The present report deals with the temperature dependence of the emissions from  $[\text{Pt}(\text{trpy})\text{Cl}]\text{SbF}_6$  and  $[\text{Pt}(\text{trpy})\text{Cl}]\text{CF}_3\text{SO}_3$  in the solid state as well as the crystal structure and emission spectrum of  $[\text{Pt}(\text{trpy})(\text{MeCN})](\text{SbF}_6)_2$ . The acetonitrile adduct exhibits a triplet emission ( $^3\text{IL}$  parentage) from the solid, but the energy varies with temperature due to the participation of various trap centers.

## Experimental Section

**Materials and Syntheses.** The purity of all reagent grade materials was adequate as received. The  $\text{Pt}(\text{PhCN})_2\text{Cl}_2$  starting complex and 2,2':6',2''-terpyridine (trpy) were obtained from Strem Chemicals, while the salts  $\text{AgSbF}_6$  and  $\text{AgCF}_3\text{SO}_3$  were from Fluka AG. Successive fractional distillations over sodium octanoate and sulfuric acid served

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<sup>‡</sup> Abstract published in *Advance ACS Abstracts*, August 15, 1997.

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to purify acetonitrile, but analytical grade solvents sufficed in all other cases.

**[Pt(ppy)Cl]A** ( $A = \text{SbF}_6^-$  or  $\text{CF}_3\text{SO}_3^-$ ). The preparation began with the addition of an equimolar amount of  $\text{AgA}$  (0.1–6 g for  $A = \text{SbF}_6^-$ , 0.109 g for  $A = \text{CF}_3\text{SO}_3^-$ , 0.424 mmol) in MeCN (5–7 cm<sup>3</sup>) to a suspension of  $\text{Pt(PhCN)}_2\text{Cl}_2$  (0.200 g, 0.424 mmol) in MeCN (15 cm<sup>3</sup>). After a 15 h reflux and a filtration step, came the addition of a 5% excess of 2,2':5',5''-terpyridine (0.104 g, 0.445 mmol) and another 15 h reflux. A second filtration removed any additional  $\text{AgCl}$  precipitate prior to the removal of solvent. Finally, treatment with hot MeCN provided for the extraction of the  $[\text{Pt(ppy)Cl}]A$  salt. Slow cooling of the MeCN solution resulted in the precipitation of a crystalline solid of bright orange ( $A = \text{SbF}_6^-$ ) or orange ( $A = \text{CF}_3\text{SO}_3^-$ ) material. Washing the bright orange  $\text{SbF}_6^-$  salt with acetone effected a color change to bright yellow but did not alter the color of the other salt. Yield: 70–80%. Anal. Calcd (for  $A = \text{SbF}_6^-$ ): C, 25.75; H, 1.59; N, 6.00. Found: C, 25.88; H, 1.67; N, 6.05. Calcd (for  $A = \text{CF}_3\text{SO}_3^-$ ): C, 31.36; H, 1.31; N, 5.86. Found: C, 30.97; H, 1.67; N, 5.87. IR (KBr, cm<sup>-1</sup>):  $\nu(\text{ppy})$  1606s, 1480m, 1456s, 1442m, 1400m, 1317m, 1035m, 773s;  $\nu(\text{SbF}_6^-)$  656s; ( $\nu(\text{CF}_3\text{SO}_3^-)$ ): 1256s, 1158s, 1030s.

**[Pt(ppy)(MeCN)(SbF<sub>6</sub>)<sub>2</sub>]**. A vapor-extraction apparatus facilitated the continuous extraction of solid  $[\text{Pt(ppy)Cl}]\text{SbF}_6$  (0.300 g, 0.318 mmol) into refluxing acetonitrile containing an excess of  $\text{AgSbF}_6$  (0.291 g, 0.348 mmol). When all the  $[\text{Pt(ppy)Cl}]\text{SbF}_6$  had dissolved (after ca. 4 h) and the solution had cooled to room temperature, filtration removed the precipitated  $\text{AgCl}$ . The precipitation of unreacted  $[\text{Pt(ppy)Cl}]\text{SbF}_6$  occurred as the volume decreased. After filtration, further evaporation led to the deposition of the desired product. The final purification steps involved a wash with acetone and diethyl ether and then exposure to a vacuum. After dissolution in acetonitrile, the crystallization of  $[\text{Pt(ppy)(MeCN)}](\text{SbF}_6)_2$  as light-yellow block-shaped crystals occurred as the solvent evaporated. Yield: 45%. Anal. Calcd: C, 21.70; H, 1.50; N, 5.95. Found: C, 21.61; H, 1.39; N, 5.93. IR (KBr, cm<sup>-1</sup>):  $\nu(\text{C}\equiv\text{N})$  2332m, 2304w;  $\nu(\text{ppy})$  1611s, 1574m, 1510m, 1510w, 1458m, 1455s, 1408m, 1322m, 1250m, 1036m, 783s;  $\nu(\text{SbF}_6^-)$  656s.

**Methods.** For luminescence measurements of solutions, a series of freeze–pump–thaw cycles served to remove dissolved dioxygen. During the steady-state emission studies and the lifetime experiments, a 420 nm long-wave-pass filter protected the detector from scattered light. For the lifetime studies, there was a 337 nm notch filter between the sample and the laser. In the course of the variable-temperature studies, all samples equilibrated at least 1 h after the sensor reached the desired temperature. A standard method of analysis yielded the lifetimes from the emission-decay data as before.<sup>4</sup>

**Instrumentation.** A Shimadzu FTIR-300 spectrophotometer provided infrared spectra of samples in KBr disks, and a Perkin-Elmer Lamda-4C and a Hewlett Packard 8452A diode-array spectrophotometer provided the absorbance data. An SLM Aminco SPF-500 instrument yielded the emission results, and a previously described apparatus<sup>9</sup> provided the lifetime data, except that the excitation source was a Laser Science, Inc., Model 337ND-S nitrogen laser. For the variable-temperature emission measurements, the cryostat was an Oxford Instruments Model DN1704 liquid-nitrogen-cooled system complete with an Oxford Instruments temperature controller. For the 77 K data, the sample holder was a quartz finger dewar filled with liquid nitrogen. The diffractometer was an Enraf–Nonius CAD4.

**Crystal Structure Determination.** The crystal of  $[\text{Pt(ppy)(MeCN)}](\text{SbF}_6)_2$  used for the diffraction study was a nearly cube-shaped block with dimensions 0.12 × 0.15 × 0.12 mm. The  $\omega$ – $\theta$  scan method in conjunction with monochromated Mo K $\alpha$  radiation yielded cell dimensions and diffraction intensities. A total of 25 reflections with  $6 < \theta < 12^\circ$  sufficed for determining cell dimensions. The data out to  $2\theta = 46^\circ$  (a total of 3708 reflections) showed monoclinic symmetry and exhibited systematic absences characteristic of the space group  $P2_1/c$  (14). Of the 3708 unique reflections, there were 1988 with  $I > 3\sigma(I)$

Table 1. Crystal Parameters at 295 K for  $[\text{Pt(ppy)(MeCN)}](\text{SbF}_6)_2$

|                                           |                                                                  |
|-------------------------------------------|------------------------------------------------------------------|
| empirical formula                         | $\text{C}_{17}\text{H}_{12}\text{F}_{12}\text{N}_4\text{PtSb}_2$ |
| <i>f</i> <sub>w</sub>                     | 940.39                                                           |
| space group (No.)                         | $P2_1/c$ (14)                                                    |
| temp, °C                                  | 22                                                               |
| <i>a</i> , Å                              | 13.705(6)                                                        |
| <i>b</i> , Å                              | 12.524(4)                                                        |
| <i>c</i> , Å                              | 14.507(4)                                                        |
| $\beta$ , deg                             | 98.27(3)                                                         |
| <i>Z</i>                                  | 4                                                                |
| <i>V</i> , Å <sup>3</sup>                 | 2425.0(16)                                                       |
| $\rho_{\text{calc}}$ , g cm <sup>-3</sup> | 2.58                                                             |
| $\lambda$ , Å                             | 0.710 73                                                         |
| $\mu$ , cm <sup>-1</sup>                  | 34.18                                                            |
| transm coeff                              | 0.678–0.998                                                      |
| $R$ ( $I > 3\sigma(I)$ ) <sup>a</sup>     | 0.043 for 1988 reflns                                            |
| $R_w$ <sup>a</sup>                        | 0.050 for 1988 reflns                                            |

$$^a R = \sum |F_o| - |F_c| / \sum F_o, R_w = \sum w^2(|F_o| - |F_c|)^2 / \sum w^2 F_o$$

that were useful for the solution and refinement of the structure. The solution of the Patterson function gave the location of the Pt and Sb atoms, and the remaining non-H atoms appeared in a difference Fourier map phased on the heavy atoms. The H atoms appeared in calculated positions. For the purposes of refinement, all atoms, except the H atoms, were assigned anisotropic temperature parameters. The refinement utilized the full-matrix least-squares method and the weighting scheme  $w = 1/(\sigma^2(F) + 0.00580F^2)$ . Table 1 gives a summary of the crystal parameters and other details of the refinement.

## Results

The approach used for the synthesis of the chloro-containing derivatives  $[\text{Pt(ppy)Cl}]A$  ( $A = \text{SbF}_6^-$ ,  $\text{CF}_3\text{SO}_3^-$ ) was different from that employed by Yio et al.<sup>8</sup> or Bailey et al.<sup>7</sup> in that the neutral compound  $\text{Pt(PhCN)}_2\text{Cl}_2$ , rather than the ionic species  $[\text{Pt(ppy)Cl}]\text{Cl}$ , served as the starting material. Thus, treatment of the benzotrifluoride complex with 1 equiv of the appropriate silver salt in refluxing acetonitrile, followed by addition of a slight excess of terpyridine, afforded an analytically pure product after workup and crystallization from acetonitrile. Interestingly, the  $\text{SbF}_6^-$  salt separated from acetonitrile as bright orange crystals that converted to yellow crystals over a period of ca. 10 min after the removal of the mother liquor. An instantaneous conversion from the metastable orange modification to the yellow form occurred with an acetone wash. For the synthesis of the acetonitrile salt  $[\text{Pt(ppy)(MeCN)}](\text{SbF}_6)_2$ ,  $[\text{Pt(ppy)Cl}]\text{SbF}_6$  was the starting material. Treatment of a boiling solution of the latter with 2 equiv of  $\text{AgSbF}_6$  led to the formation of the desired product, along with  $\text{AgCl}$  and unreacted  $[\text{Pt(ppy)Cl}](\text{SbF}_6)$ ; the latter selectively precipitated from a cooled acetonitrile solution, allowing the isolation of  $[\text{Pt(ppy)(MeCN)}](\text{SbF}_6)_2$  as light yellow block-shaped crystals. The solid-state infrared spectrum, measured in a KBr disk, exhibited two peaks in the C–N stretching region at 2330 and 2302 cm<sup>-1</sup>, each attributable to the MeCN ligand. A similar C–N stretching peak pattern has been observed for  $\text{Pt(MeCN)}_2\text{Cl}_2$ .<sup>10</sup> Attempts to synthesize the  $\text{BF}_4^-$  and  $\text{CF}_3\text{SO}_3^-$  salts of  $[\text{Pt(ppy)(MeCN)}]^{2+}$  from  $[\text{Pt(ppy)Cl}]A$  ( $A = \text{CF}_3\text{SO}_3^-$ ,  $\text{BF}_4^-$ ) were unsuccessful, largely because of the difficulties incurred in the separation of the starting material from the desired product.

**Crystal Structure of  $[\text{Pt(ppy)(MeCN)}](\text{SbF}_6)_2$ .** The structure shows that the platinum adopts a planar coordination geometry; see Figure 1 for a perspective view of the cation. The positional and thermal parameters as well as the calculated interatomic distances and angles for  $[\text{Pt(ppy)(MeCN)}](\text{SbF}_6)_2$  appear in Tables 2 and 3. The maximum deviation from the

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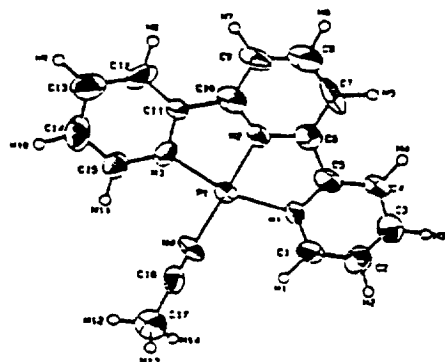


Figure 1. The molecular geometry and atom-numbering scheme employed for the  $[\text{Pt}(\text{terpy})(\text{MeCN})]^{2+}$  cation. Atom designators are 50% probability ellipsoids except for those of the H atoms, which appear as spheres of arbitrary radius.

Table 2. Positional ( $\times 10^4$ ) and Thermal Parameters ( $\text{\AA}^2 \times 10^3$ ) for  $[\text{Pt}(\text{terpy})(\text{MeCN})](\text{SbF}_6)_2$

| atom | x        | y        | z        | $U_{eq}$ |
|------|----------|----------|----------|----------|
| Pt   | 2394     | 2116(1)  | 4000     | 42       |
| N1   | 2983(9)  | 1172(12) | 3058(10) | 50(3)    |
| N2   | 2853(9)  | 3259(11) | 3262(9)  | 43(3)    |
| N3   | 1939(10) | 5403(10) | 4678(11) | 53(4)    |
| N4   | 1906(10) | 929(13)  | 4751(10) | 54(4)    |
| C1   | 3043(14) | 106(15)  | 3024(14) | 65(5)    |
| C2   | 3467(17) | -430(17) | 2330(16) | 85(7)    |
| C3   | 3857(13) | 147(19)  | 1709(15) | 69(6)    |
| C4   | 3842(14) | 1321(17) | 1736(14) | 66(5)    |
| C5   | 3384(12) | 1771(15) | 2439(13) | 52(4)    |
| C6   | 3322(12) | 2963(16) | 2546(12) | 53(4)    |
| C7   | 3693(13) | 3793(25) | 2044(14) | 84(7)    |
| C8   | 3539(17) | 4852(21) | 2295(18) | 81(7)    |
| C9   | 3062(15) | 5091(16) | 3004(12) | 65(5)    |
| C10  | 2710(12) | 4274(16) | 3507(11) | 55(5)    |
| C11  | 2163(11) | 4367(13) | 4305(12) | 44(4)    |
| C12  | 1889(14) | 5311(16) | 4648(17) | 73(6)    |
| C13  | 1376(15) | 5363(18) | 5390(17) | 76(6)    |
| C14  | 1154(14) | 4372(21) | 5754(17) | 86(7)    |
| C15  | 1446(12) | 3413(16) | 5419(13) | 56(5)    |
| C16  | 1654(12) | 231(13)  | 5164(13) | 57(5)    |
| C17  | 1314(14) | -673(15) | 5700(15) | 71(5)    |
| Sb1  | 4240(1)  | -2792(1) | 166(1)   | 58       |
| F1   | 3589(1)  | -4063(1) | 150(1)   | 133(5)   |
| F2   | 5288(1)  | -3468(1) | -188(1)  | 216(10)  |
| F3   | 3744(1)  | -2567(1) | -1032(1) | 198(9)   |
| F4   | 4897(1)  | -1521(1) | 195(1)   | 234(10)  |
| F5   | 3197(1)  | -2110(1) | 526(1)   | 188(9)   |
| F6   | 4740(1)  | -3013(1) | 1371(1)  | 159(7)   |
| Sb2  | 350(1)   | 6991(1)  | 7767(1)  | 65       |
| F7   | -13(1)   | 6484(1)  | 6607(1)  | 221(11)  |
| F8   | 1549(1)  | 7322(1)  | 7490(1)  | 148(6)   |
| F9   | -95(1)   | 8317(1)  | 7400(1)  | 232(11)  |
| F10  | 701(1)   | 7489(1)  | 8937(1)  | 144(6)   |
| F11  | -856(1)  | 6657(1)  | 8052(1)  | 149(6)   |
| F12  | 785(1)   | 5661(1)  | 8144(1)  | 186(8)   |

mean plane through the Pt and four bonded N atoms is 0.012 Å for the metal atom. As a consequence of the geometric constraints imposed by the terpy ligand, the angles subtended at the Pt atom deviate from the idealized values of 90 and 180°: the relevant angles are 81.8(6) (N1–Pt–N2), 162.5(6) (N1–Pt–N3), 98.3(6) (N1–Pt–N4), 80.8(6) (N2–Pt–N3), 179.3(5) (N2–Pt–N4), and 99.1(6)° (N3–Pt–N4). The Pt–N distances are also typical of metal–terpyridine complexes,<sup>67,11,12</sup> in that the distance to the inner N atom (Pt–N2, 1.938(13) Å)

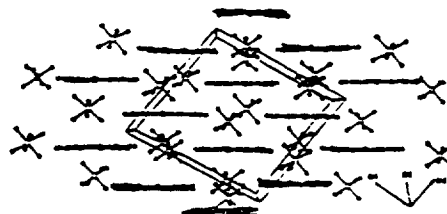


Figure 2. Packing diagram for  $[\text{Pt}(\text{terpy})(\text{MeCN})](\text{SbF}_6)_2$ .

Table 3. Selected Interatomic Distances (Å) and Angles (deg) for  $[\text{Pt}(\text{terpy})(\text{MeCN})](\text{SbF}_6)_2$

| Distances |           |         |           |
|-----------|-----------|---------|-----------|
| Pt–N1     | 2.047(14) | Pt–N2   | 1.938(13) |
| Pt–N3     | 2.013(13) | Pt–N4   | 1.996(14) |
| N1–C1     | 1.32(2)   | N1–C5   | 1.34(2)   |
| N2–C6     | 1.35(2)   | N3–C10  | 1.31(2)   |
| N3–C11    | 1.36(2)   | N3–C15  | 1.35(2)   |
| N4–C16    | 1.08(2)   | C1–C2   | 1.40(3)   |
| C2–C3     | 1.32(3)   | C3–C4   | 1.45(3)   |
| C4–C5     | 1.39(3)   | C5–C6   | 1.48(3)   |
| C5–C7     | 1.39(3)   | C7–C8   | 1.38(3)   |
| C8–C9     | 1.33(3)   | C9–C10  | 1.37(3)   |
| C10–C11   | 1.47(2)   | C11–C12 | 1.34(2)   |
| C12–C13   | 1.37(3)   | C13–C14 | 1.38(3)   |
| C14–C15   | 1.36(3)   | C16–C17 | 1.22(1)   |

| Angles    |           |            |           |
|-----------|-----------|------------|-----------|
| N1–Pt–N2  | 81.8(6)   | N1–Pt–N3   | 162.5(6)  |
| N1–Pt–N4  | 98.3(6)   | N2–Pt–N3   | 80.8(6)   |
| N2–Pt–N4  | 179.3(5)  | N3–Pt–N4   | 99.1(6)   |
| Pt–N1–C1  | 128.6(13) | Pt–N1–C5   | 112.0(12) |
| Pt–N2–C6  | 116.6(12) | Pt–N2–C10  | 118.1(12) |
| Pt–N3–C11 | 113.0(11) | Pt–N3–C15  | 128.5(13) |
| Pt–N4–C16 | 179(2)    | N4–C16–C17 | 177(2)    |

is significantly shorter than those to the two outer N atoms (Pt–N1, 2.047(14) Å; Pt–N3, 2.013(13) Å). The terpy ligand is only slightly ruffled, the mean planes of the outer pyridine rings defining angles of 2.1 (N1 ring) and 3.2° (N3 ring) with that of the central pyridine ring. The Pt–N4 distance is 1.996(14) Å. This value is similar to the Pt–N (N of MeCN) distances of 1.977 and 1.981 Å for  $\text{Pt}(\text{MeCN})_2\text{Cl}_2$ <sup>10</sup> and 1.94(2) Å for  $[\text{Pt}(\text{phbpy})(\text{MeCN})]\text{PF}_6$  (Hphbpy = 6-phenyl-2,2'-bipyridine).<sup>13</sup>

The crystal lattice consists of parallel sheets of cations and anions; Figure 2 gives a view of the packing parallel to these sheets. Within a sheet, the  $[\text{Pt}(\text{terpy})(\text{MeCN})]^{2+}$  and  $\text{SbF}_6^-$  moieties reside in alternating rows of cations and anions which extend along the *b* axis. Since the planar cations lie side-by-side, there are no  $\pi$ – $\pi$  or metal–metal interactions along a row of cations. A *c*-glide plane relates successive sheets such that a row of anions lies directly above a row of cations. Thus, there are no extended interactions involving cations in a direction perpendicular to the sheets either. Specifically, the Pt–Pt distances between neighboring cations from adjacent sheets are all greater than 4.90 Å. Similarly, the intermolecular C(terpy)–C(terpy) distances are all greater than 3.5 Å and close to the upper limit of 3.8 Å for  $\pi$  aromatic interactions.<sup>14</sup> We conclude that the  $[\text{Pt}(\text{terpy})(\text{MeCN})]^{2+}$  chromophore resides in a monomeric environment in the  $\text{SbF}_6^-$  salt and that this is a consequence of the cation:anion ratio of 1:2. Such a conclusion requires further verification, however, since this is the first

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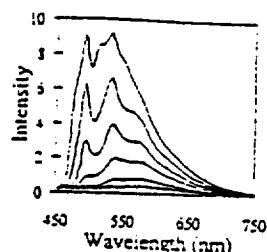


Figure 3. Solid-state emission spectra of  $[\text{Pt}(\text{trpy})(\text{MeCN})](\text{SbF}_6)_3$  recorded at 40 K intervals over the range 30–130 K. The emission intensity increases as the temperature decreases. The excitation wavelength was 350 nm.

reported crystal structure determination of a terpyridyl salt of  $\text{Pt(II)}$  of 1:2 cation:anion stoichiometry.

**Emission from  $[\text{Pt}(\text{trpy})(\text{MeCN})](\text{SbF}_6)_3$ .** In the solid state, the emission from  $[\text{Pt}(\text{trpy})(\text{MeCN})](\text{SbF}_6)_3$  clearly reflected different components at different temperatures (Figure 3). Thus, above ca. 140 K the principal emission maxima occurred at around 540 and 575 nm, respectively, and there were weaker emission maxima at ca. 495 and ca. 465 nm. From 120 K down to about 100 K, the overall intensity increased, but there was a change in the band shape. In this temperature regime, the band at 495 nm evolved into a dominant spectral feature along with the band at 530 nm, and both maxima shifted to somewhat shorter wavelengths. At the same time, the relative intensity of the band at 575 nm decreased, and it became a shoulder. Finally, at the lowest accessible temperature, ca. 30 K, the spectrum sharpened further and new shoulders appeared at about 480, 515, and 550 nm, respectively. At each temperature, the vibrational structure within the emission spectrum is consistent with a  $\pi^*-\pi^*$  orbital parentage. Parenthetically, we may note that the apparent emission maximum at 465 nm in the room-temperature spectrum of Figure 3 could represent  $\pi^*-\pi^*$  emission from coordinated trpy as well. However, it could also be an artifact, since the signal intensity changes very little at this wavelength over the entire temperature range investigated. A reviewer pointed out that reabsorption of the emission could be a factor influencing the observed band shape. However, experiments showed that, in the room-temperature, solid-state reference spectrum, the longest wavelength absorption band with any appreciable intensity had a maximum at about 390 nm and a tail that extended to only ca. 450 nm.

For comparison, we measured the emission from  $\text{Pt}(\text{trpy})(\text{MeCN})^{2+}$  in a butyronitrile glass at 77 K. The spectrum of the glass yielded well-resolved vibronic maxima, and the onset of the spectrum fell at a shorter wavelength. For a 150  $\mu\text{M}$  solution, the emission maxima occurred at 457, 491, 529, and 565 nm.

**Physical Data for the  $[\text{Pt}(\text{trpy})\text{Cl}]\text{A}$  Solids.** Like Bailey et al.,<sup>7</sup> we found that the emission spectrum of  $[\text{Pt}(\text{trpy})\text{Cl}]^+$  varied markedly with the counterion in the solid state as well as with the temperature. However, we often observed qualitatively different kinds of behavior. In our studies with  $\text{SbF}_6^-$  as the counterion, the compound was yellow and the maximum in the uncorrected emission spectrum occurred at 552 nm. Although the wavelength maximum of the emission was essentially independent of the temperature (Figure 4), the intensity increased as the temperature decreased. The room-temperature decay was not monoexponential, but the emission lifetime was about 750 ns in the tail of the decay curve. On the other hand, the decay was essentially monophasic at 77 K and had a lifetime of about 3  $\mu\text{s}$ . Although Bailey et al. studied

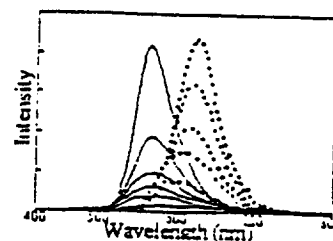


Figure 4. Emission spectra from solid-state samples of  $[\text{Pt}(\text{trpy})\text{Cl}](\text{SbF}_6)_3$  (left) and  $[\text{Pt}(\text{trpy})\text{Cl}](\text{CF}_3\text{SO}_3)_3$  (right). In each case, the intensity increases as the temperature decreases. The temperatures are 100, 150, 160, 190, 220, and 230 K; there is no 220 K spectrum for the triflate compound. The excitation wavelength was 350 nm.

ostensibly the same chromophore as part of a yellow solid with  $\text{PF}_6^-$  as the counterion,<sup>7</sup> they found that the room-temperature emission maximum occurred at a much longer wavelength, ca. 630 nm. Moreover, at lower temperatures, emission occurred at shorter wavelengths and there was a decrease in the bandwidth. By around 100 K, the emission maximum stopped shifting and stabilized at about 565 nm.<sup>7</sup> Our preparation of the triflate salt gave an uncorrected emission maximum at 585 nm at 130 K. At lower temperatures, the emission maximum shifted to longer wavelengths, out to 613 nm at 100 K (Figure 4), in line with the results of Yip et al.<sup>9</sup>

## Discussion

**The  $[\text{Pt}(\text{trpy})(\text{MeCN})](\text{SbF}_6)_3$  System.** The structured emission shown by the nitrile complex in the low-temperature glass or the solid state clearly represents ligand-centered  $\pi^*-\pi^*$  emission. However, for the solid state, the emission appears at longer wavelengths and the spectrum is quite temperature dependent. At low temperature, new shorter-wavelength emission maxima appear in the solid-state spectrum, but even at 30 K, the emission does not attain the energy found from the glass. In principle, a phase transition could account for the temperature dependence of the emission spectrum; however, this is unlikely. One reason is that the data would require a series of phase changes at different temperatures. The other problem with this model is that the lowest energy emission occurs at room temperature, where the structure shows there are no significant neighbor-neighbor interactions, at least in the bulk material.

The most likely explanation of the data is that the emission originates from different trap sites depending on the temperature. The trap centers could be either defect sites or sites where the excitation itself generates a locally modified structure.<sup>13</sup> When energy transfer is facile in the solid, the chromophores in the bulk simply act as antennae that efficiently take up the energy which then flows into lower energy trap sites. Of course, the energy-distribution processes are temperature dependent and, at a sufficiently low temperature, the population of particular traps may no longer be feasible. Under these conditions, new, higher energy emission spectra appear at lower and lower temperatures. This model nicely accounts for the data, but the crucial assumption is that energy transfer occurs readily in the solid state. There are, however, good precedents for this behavior, particularly when the excitation involves  $\pi$ , excited states of aromatic ligands.<sup>14-18</sup> With  $\pi$  excitation, the extent

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of structural reorganization and the barrier to energy transfer are frequently minimal. Regarding the structure of the trap center, some type of intermolecular interaction such as  $\pi\pi$ - $\pi\pi$  stacking is very likely to be responsible for the red shift in the solid-state emission spectrum. Miskowski and Houlding have proposed that interligand interactions of this type can give rise to very large red shifts as well as the loss of vibrational structure.<sup>17</sup> On the other hand, in their studies of platinum(II) isobiquinolines, Kato et al. reported finding much smaller red shifts and emission with residual vibrational structure.<sup>19</sup> Kato et al. also found that the <sup>3</sup>IL emission from a mixed-ligand, dicyanide derivative exhibited multiple origins, consistent with the possible participation of trap centers.

**The [Pt(trpy)Cl]A Systems in the Solid State.** Extended interactions often have a profound influence on the optical and electrical properties of platinum(II) complexes in the solid state.<sup>12b</sup> In the [Pt(trpy)Cl]A systems, this is evident from the influence the anion A has on the color of the material, as the energy of the MMLCT absorption varies with the metal-metal separation.<sup>13b-23</sup> In particular, the effective intermolecular separation is clearly larger in the case of the yellow SbF<sub>6</sub><sup>-</sup> derivative compared with the orange CF<sub>3</sub>SO<sub>3</sub><sup>-</sup> compound. Figure 4 shows that the same effect is evident in the emission spectra, where the emission appears at significantly longer wavelengths when triflate is the anion. Moreover, the shift increases at lower temperatures almost certainly because of a further decrease in the mean platinum-platinum separation.<sup>23</sup> In contrast, the emission from what is probably a monomeric

platinum center in the SbF<sub>6</sub><sup>-</sup> salt occurs at significantly higher energy, and the maximum is effectively temperature independent. In this context, it is worth noting that Bailey et al. found that the apparently very similar, yellow PF<sub>6</sub><sup>-</sup> salt exhibited a much longer wavelength emission maximum at room temperature.<sup>7</sup> However, they also reported that the emission underwent a blue shift at lower temperatures, down to about 160 K, and that at still lower temperatures a new emission signal emerged with a maximum at ca. 565 nm. The important point is that their low-temperature emission signal paralleled the signal we observed from the SbF<sub>6</sub><sup>-</sup> analogue. The simplest way to reconcile the data for the PF<sub>6</sub><sup>-</sup> system is to assume that the longer-wavelength emission, which was no longer evident at 100 K, originated at a trap site. This phenomenon provides another explanation for the fact that similar platinum(II) materials, or even different preparations of the same material, may exhibit distinct emissions. As a further illustration, consider the [Pt(trpy)Cl](CF<sub>3</sub>SO<sub>3</sub>) system. We observed a red shift in the emission maximum at lower temperatures whereas Bailey et al. reported a blue shift for the same compound. However, both groups observed similar emission spectra at the lowest temperatures.

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**Supporting Information Available:** Tables of complete atomic coordinates and isotropic thermal parameters, non-hydrogen anisotropic temperature factors, bond distances, and bond angles (7 pages). Ordering information is given on any current masthead page.

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## Remarkable substituent effects on the photophysics of $\text{Pt}(4'\text{-X-trpy})\text{Cl}^+$ systems (trpy = 2,2':6',2''-terpyridine)

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### Abstract

In view of the interest in probing the binding interactions that occur between platinum complexes and biological macromolecules, the aim of this work has been to develop systems that exhibit enhanced excited-state lifetimes and emission yields in fluid solution. The investigation focuses on a series of complexes of the type  $\text{Pt}(4'\text{-X-T})\text{Cl}^+$  where  $4'\text{-X-T}$  denotes a 4'-substituted derivative of 2,2':6',2''-terpyridine. In all cases the counterion is the non-coordinating ion tetrakis[3,5-bis(trifluoromethyl)phenyl]borate. The substituents employed include electron-withdrawing groups like CN and  $\text{SO}_2\text{Me}$  as well as electron-donating groups like SMe and NMe<sub>2</sub>. Within the series of complexes, the first reduction wave ranges over about 0.7 V in DMF. Although the process probably entails ligand reduction, the acceptor orbital appears to have some platinum 6p<sub>z</sub> character. Even though electron-donating substituents destabilize the reduced form of the ligand, all substituents induce a red-shift in the charge-transfer (CT) absorption band system that occurs around 400 nm. Furthermore, there is generally an increase in the CT absorption intensity, the emission lifetime and the emission quantum yield in methylene chloride. Thus, at room temperature, the complex with the terpyridine ligand itself is a very poor emitter with an emission lifetime of 10 ns or less, while the  $\text{Pt}(4'\text{-SMe-T})\text{Cl}^+$  and  $\text{Pt}(4'\text{-NMe}_2\text{-T})\text{Cl}^+$  systems exhibit lifetimes of 140 ns and 1.9  $\mu\text{s}$ , respectively. With the electron-donating substituents in particular, the lifetime enhancement reflects a configuration interaction between the original CT state and an intraligand charge-transfer excited state. Substituents also influence a thermally activated pathway to radiationless decay. © 1998 Elsevier Science S.A. All rights reserved.

**Keywords:** Luminescence; Photophysics; Platinum complexes; Terpyridine complexes

### 1. Introduction

The binding interactions that complexes of platinum(II) with polypyridine ligands undergo with DNA [1–5] and globular proteins [6] have helped fuel interest in these systems. In addition, the platinum(II) materials themselves show interesting electronic properties in the solid state including photoluminescence [7–10]. The observation of photoluminescence in fluid solution is a rarer phenomenon, but there are some recent reports of emission from monomeric platinum(II) polypyridine complexes [11–15]. In the present context, the most relevant systems are  $\text{Pt}(\text{trpy})\text{OH}^+$ , where trpy denotes the 2,2':6',2''-terpyridine ligand [13], and a  $\text{Pt}(4'\text{-R-trpy})\text{Cl}^+$  series, where  $\text{R} = \text{C}_6\text{H}_4\text{OMe-}p$ ,  $\text{C}_6\text{H}_4\text{Me-}p$ ,  $\text{C}_6\text{H}_4\text{Br-}p$  or  $\text{C}_6\text{H}_4\text{CN-}p$  [15]. When the emission

originates in a metal-to-ligand charge-transfer (CT) excited state, the intensity and the lifetime vary dramatically with the solvent probably in large part because of the availability of open coordination sites at the metal center [13]. Reductive quenching of the CT state is also common [5,15]. For  $\text{Pt}(\text{trpy})\text{L}^+$  systems, the luminescence properties are particularly sensitive to the nature of ligand L [13,15], due perhaps to a variation in the efficiency of radiationless decay via a thermally accessible d–d excited state [13,16]. In the case of the  $\text{Ru}(\text{trpy})_2^{2+}$  system, which shares some properties in common with platinum(II) terpyridines, the systematic exploration of substituent effects has provided useful insights into the photochemistry and photophysics [17–19]. Those reports provided the impetus for the following spectroscopic and electrochemical studies of a series of complexes of the type  $\text{Pt}(4'\text{-X-T})\text{Cl}^+$ , where  $4'\text{-X-T}$  denotes the trpy derivative with substituent X in the 4' position. The most intriguing finding is that the introduction of an electron-donating group

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can dramatically enhance the emission yield and the lifetime as a consequence of the admixture of intraligand excited state character that occurs in the emitting state.

## 2. Experimental

### 2.1. Materials

Aldrich supplied 2,2':6',2''-terpyridine, 4'-chloro-2,2':6',2''-terpyridine, potassium *tert*-butoxide, 2-acetylpyridine, carbon disulfide, methyl iodide, ammonium acetate, methyl magnesium bromide, selenium dioxide, potassium cyanide, *m*-chloroperoxybenzoic acid, 4-morpholineethanesulfonic acid (MES), 3,5-bis(trifluoromethyl)bromobenzene, hexamethylphosphoramide (HMPA) and tetrabutylammonium hexafluorophosphate (TBAH). The  $\text{ZnCl}_2$  came from Mallinckrodt. Janssen Chimica supplied boron trifluoroetherate. Baxter supplied B&J brand high purity solvents for spectroscopic measurements (acetonitrile, *N,N*-dimethylformamide and methylene chloride). Other solvents were reagent grade. The  $\text{K}_2\text{PtCl}_4$  was a gift from Johnson Matthey. The purity of most materials was satisfactory as received. In the case of TBAH, a series of three recrystallizations from ethanol gave a pure compound.

### 2.2. Methods

The methods reported by Potts et al. provided routes to the trpy derivatives 4'-thiomethyl-2,2':6',2''-terpyridine (4'-SMe-T), 4'-methylsulfonyl-2,2':6',2''-terpyridine (4'-SO<sub>2</sub>Me-T), 4'-methyl-2,2':6',2''-terpyridine (4'-Me-T) and 4'-cyano-2,2':6',2''-terpyridine (4'-CN-T) [20,21]. An adaptation of the procedure of Gupta et al. gave 4'-dimethylamino-2,2':6',2''-terpyridine (4'-NMe<sub>2</sub>-T) [22]. For the synthesis of each  $[\text{Pt}(4'\text{-X-T})\text{Cl}]\text{Cl}$  form, the reaction of  $\text{Pt}(\text{COD})\text{Cl}_2$  with the appropriate trpy derivative (4'-X-T ligand) gave the desired product in ~75% yield [23, 24]. The preparation of the counter ion tetrakis[3,5-bis(trifluoromethyl)phenyl]borate (TFPB) followed the procedure published by Nishida et al. [25]. Finally, the addition of an ethanolic solution of the sodium salt of TFPB to an aqueous solution of the chloride salt of  $\text{Pt}(4'\text{-X-T})\text{Cl}^-$  yielded the desired material  $[\text{Pt}(4'\text{-X-T})\text{Cl}]\text{TFPB}$ . Microanalysis and proton NMR data showed that recrystallization from toluene/methylene chloride typically yielded a hemisolvate containing toluene. Microanalysis of  $[\text{Pt}(4'\text{-X-trpy})\text{Cl}]\text{TFPB} \cdot \text{Y}$ , where Y = toluene; (X = NMe<sub>2</sub>·0.5 toluene): *Anal. Calc.*: C, 44.53; H, 2.23; N, 3.956. Found: C, 44.25; H, 2.32; N, 3.73%. (X = CN·0.75 toluene): *Anal. Calc.*: C, 45.0; H, 1.98; N, 3.9. Found: C, 44.85; H, 1.98; N, 3.84%. (X = SO<sub>2</sub>Me·0.5 toluene): *Anal. Calc.*: C, 42.62; H, 1.98; N, 2.89. Found: C, 42.92; H, 2.06; N, 2.88%. (X = SMe): *Anal. Calc.*: C, 41.98; H, 1.83; N, 3.06. Found: C, 41.59; H, 1.80; N, 2.90%. The procedure of Hill et al.

yielded the  $\text{Zn}(4'\text{-X-T})\text{Cl}_2$  derivatives without need for further purification [26].

A three electrode cell served to obtain the cyclic voltammetry data. In particular, the working electrode was a gold disc, the auxiliary electrode was a Pt wire and the reference electrode was a AgCl/Ag electrode in contact with 3 M NaCl(aq.). For reporting purposes ferrocene served as an internal reference and exhibited a potential of 0.57 V versus AgCl/Ag. The electrolyte solution was 0.1 M TBAH in DMF. This was the solvent of choice because the platinum complexes gave relatively clean waves in this medium, and the zinc complexes showed good solubility. A simple purge with dinitrogen gas sufficed to remove dissolved dioxygen from the sample. The scan rate was usually 50 mV s<sup>-1</sup>.

For the luminescence studies, a stream of Ar gas acted as the deoxygenating agent. During spectral measurements, the slit settings were 10 nm for both the excitation and emission beams. For emission spectra a 400 nm long-wave-pass filter removed the scattered light, usually at an excitation wavelength of 375 nm. In the case of the lifetime studies the excitation wavelength was either 440 or 420 nm, and the long-wave-pass filter had a cutoff of 475 nm. The laser dye was Coumarin 440 or Stilbene 420, and the solvent for NMR spectra was CDCl<sub>3</sub>. Dr H. Daniel Lee of Purdue University carried out the microanalyses.

### 2.3. Instrumentation

The spectrophotometer was a Perkin-Elmer Lambda 4C, and the spectrofluorometer was a SLM-Aminco SPF-500C. For variable temperature measurements the cryostat was an Oxford Instruments model DN1702 system with controller. Descriptions of the procedure and equipment for measuring lifetimes are in the literature [27]. The sweep unit for the electrochemical measurements was a model CV-27 cyclic voltammograph from Bioanalytical Systems.

## 3. Results

### 3.1. Electrochemistry

In accord with other platinum(II) complexes of heteroaromatic ligands, the  $\text{Pt}(4'\text{-X-T})\text{Cl}^-$  systems show two ligand reduction waves separated by about 0.6 V in DMF [26,28,29], whereas anodic scans out to the solvent limit gave no indication of platinum oxidation. The potential of the first reduction varies by as much as 0.7 V with the change in the 4' substituent, whereas the effect on the second reduction is somewhat smaller (Table 1). The second wave is chemically less reversible in that it shows a greater difference in the cathodic and anodic currents. The  $\text{Zn}(4'\text{-X-T})\text{Cl}_2$  analogues also give well-resolved reduction waves that are substituent dependent. In line with the results of Hill et al. who studied the two parent complexes [26], the potential of the

Table 2  
Reduction potentials in DMF vs. ferrocene<sup>a</sup>

| N                               | $E_1$ (V)         | $E_2$ (V)         |
|---------------------------------|-------------------|-------------------|
| <b>Zn(4'-X-T)Cl<sub>2</sub></b> |                   |                   |
| CN                              | -1.43 (60, 1.0) * |                   |
| SO <sub>2</sub> Me              | -1.45 (100, 1.4)  |                   |
| H                               | -1.86 (70, 1.7)   |                   |
| SMe                             | -1.89 (60, 1.4)   |                   |
| Me                              | -1.91 (60, 4.0)   |                   |
| NMe <sub>2</sub>                | -2.12 (70, 1.5)   |                   |
| <b>Pt(4'-X-T)Cl<sub>2</sub></b> |                   |                   |
| CN                              | -0.92 (60, 1.2) * | -1.56 (60, 1.4) * |
| SO <sub>2</sub> Me              | -0.98 (60, 1.3)   | -1.58 (60, 1.5)   |
| H                               | -1.24 (70, 1.2)   | -1.82 (70, 1.6)   |
| SMe                             | -1.28 (60, 1.2)   | -1.79 (60, 1.5)   |
| Me                              | -1.30 (70, 1.2)   | -1.87 (70, 1.9)   |
| NMe <sub>2</sub>                | -1.53 (70, 1.2)   | -1.97 (60, 2.5)   |

<sup>a</sup> From cyclic voltammetry scans at 50 mV s<sup>-1</sup> in DMF containing 0.1 M TBAH at 23°C.

\*  $E_2 = E_{1/2}$  (mV)  $\times 10^{-3}$ .

first ligand reduction is  $\sim 0.5$  V more negative for the zinc complex than it is for the corresponding platinum system.

### 3.2. Spectroscopy and photophysics

Solutions of the [Pt(4'-X-T)Cl]<sup>+</sup>TFPB compounds are stable in methylene chloride for short periods of time; however, decreases in the near-UV absorption intensity begin to be apparent after 5–6 h. All reported data refer to freshly prepared solutions, except for the low-temperature data where the course of the experiment required  $\sim 6$  h. As reported previously for the parent trpy complex [9,13], and for the 4'-phenyl-substituted complexes [15], the Pt(4'-X-T)Cl<sup>+</sup>

systems exhibit one series of intraligand  $\pi \rightarrow \pi^*$  absorptions centered around 280 nm and another around 320 nm (Fig. 1). Fig. 2 shows that Zn(4'-X-T)Cl<sub>2</sub> systems exhibit a similar series of UV absorption bands. Table 2 contains a compilation of absorbance data for the Pt(4'-X-T)Cl<sup>+</sup> complexes in two solvents. In addition to the  $\pi \rightarrow \pi^*$  absorptions, the platinum systems exhibit lesser intensity CT absorption bands in the vicinity of 400 nm. Due to a net reduction of the dipole moment in the CT excited state [13,30], the CT transitions occur at shorter wavelengths in polar solvents like acetonitrile. With the exception of the methyl group, which has almost no effect, the introduction of a substituent in the 4' position of the trpy ligand induces a bathochromic shift in the CT absorption network (Table 2). This is true whether the substituent group is electron withdrawing or electron donating. As the results in Table 2 show, the presence of the substituent can greatly enhance the intensity of the CT absorption as well. Similar effects are evident in the spectra of 4'-phenyl-substituted Pt(trpy)Cl<sup>+</sup> systems [15].

At room temperature, the emission intensity and the lifetime vary dramatically with the nature of the 4' substituent as well as the solvent. Apart from the 4'-NMe<sub>2</sub>-T derivative, none of the complexes listed in Table 2 gives a significant emission signal in the room temperature acetonitrile. For the most part, the complexes are emissive in methylene chloride, although the signal is extremely weak for Pt(trpy)Cl<sup>+</sup> itself and virtually non-detectable for the closely related 4'-Me-T system. In accordance with the CT absorption data, the introduction of a substituent at the 4' carbon of the trpy ligand generally causes the emission spectrum to shift to lower energy; however, the emission spectra all appear at rather similar wavelengths. For each system the emission shows well resolved vibrational structure, mono-exponential emis-

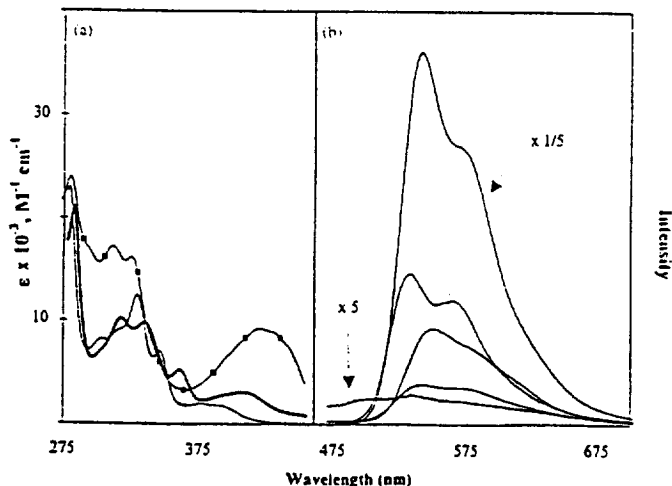


Fig. 1. (a) Near-UV absorption spectra of selected Pt(4'-X-T)Cl<sup>+</sup> complexes in MeCN at 23°C: X = NMe<sub>2</sub> (—■—), X = CN (—, thick trace), X = H (—, thin trace), (b) Uncorrected emission spectra of Pt(4'-X-T)Cl<sup>+</sup> systems in CH<sub>2</sub>Cl<sub>2</sub> at 23°C. The samples all had the same absorbance at the excitation wavelength of 375 nm. In order of increasing intensity at 550 nm the spectra correspond to X = H, SO<sub>2</sub>Me, CN, SMe and NMe<sub>2</sub>, respectively.

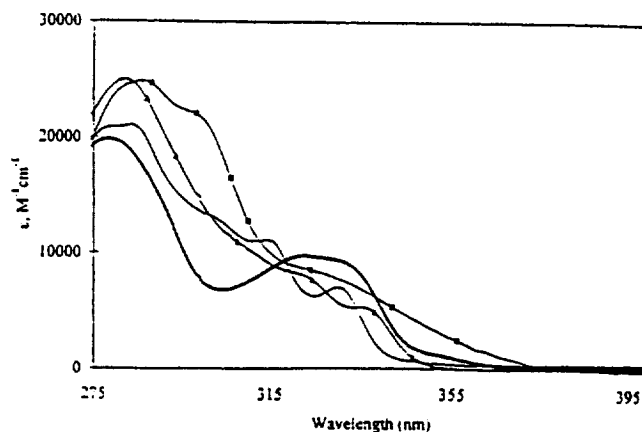


Fig. 2. Near-UV absorption spectra of  $\text{Zn}(4'\text{-X-T})\text{Cl}_2$  compounds in DMF at  $23^\circ\text{C}$ . The samples have  $\text{X} = \text{NMe}_2$  (—■—),  $\text{X} = \text{SMe}$  (—▲—),  $\text{X} = \text{Me}$  (—, thin trace) and  $\text{X} = \text{CN}$  (—, thick trace).

sion decay and an excitation spectrum that matches the absorption spectrum. See Fig. 1(b) for some representative spectra. Except for the  $4'\text{-Me-T}$  system, the introduction of an electron-withdrawing group or an electron-donating group at the  $4'$  position of the trpy ligand enhances the lifetime and the emission quantum yield (Table 2). The most dramatic instance is the  $4'\text{-NMe}_2\text{-T}$  derivative which has an emission lifetime in the microsecond regime. In view of the emission

Table 2  
Absorption and emission data from  $\text{Pt}(4'\text{-X-T})\text{Cl}_2$  systems at  $23^\circ\text{C}$

| X                      | $\lambda_{\text{abs}}$ (nm) |                          | Emission data <sup>a</sup> |                    |             |  |
|------------------------|-----------------------------|--------------------------|----------------------------|--------------------|-------------|--|
|                        | MeCN                        | $\text{CH}_2\text{Cl}_2$ | $\lambda_{\text{em}}$ (nm) | $\phi_{\text{em}}$ | $\tau$ (ns) |  |
| CN                     |                             | 311sh                    |                            |                    |             |  |
|                        | 316                         | 323                      | 550                        | 0.005              | 116         |  |
|                        | 335                         | 345                      | 590sh                      |                    |             |  |
|                        | (13 800) <sup>b</sup>       |                          |                            |                    |             |  |
|                        | 361                         | 366                      |                            |                    |             |  |
| $\text{SO}_2\text{Me}$ | 394                         | 405sh                    |                            |                    |             |  |
|                        | 409 (3920)                  | 428                      |                            |                    |             |  |
|                        | 316                         | 325                      | 542                        | 0.002              | 21          |  |
|                        | 336 (15 200)                | 377                      |                            |                    |             |  |
|                        | 358                         | 348                      |                            |                    |             |  |
| H                      | 385                         | 380                      |                            |                    |             |  |
|                        | 403 (3650)                  | 430                      |                            |                    |             |  |
|                        | 303                         | 305                      | 500                        | 0.0004             | < 10        |  |
|                        | 316                         | 320                      | 535                        |                    |             |  |
|                        | 330 (14 200)                | 340                      | 590                        |                    |             |  |
| SMe                    | 346                         |                          |                            |                    |             |  |
|                        | 377 (2200)                  | 390                      |                            |                    |             |  |
|                        | 390sh                       | 403                      |                            |                    |             |  |
|                        | 320                         | 305                      | 542                        | 0.006              | 142         |  |
|                        | 333 (17 900)                | 330                      | 575                        |                    |             |  |
|                        | 388                         | 400                      | 625sh                      |                    |             |  |
|                        | 409 (7750)                  | 425                      |                            |                    |             |  |

(continued)

Table 2 (continued)

| X              | $\lambda_{\text{abs}}$ (nm) |                          | Emission data              |                    |             |  |
|----------------|-----------------------------|--------------------------|----------------------------|--------------------|-------------|--|
|                | MeCN                        | $\text{CH}_2\text{Cl}_2$ | $\lambda_{\text{em}}$ (nm) | $\phi_{\text{em}}$ | $\tau$ (ns) |  |
| Me             | 282                         | 284                      |                            |                    |             |  |
|                | 302                         | 308                      |                            |                    |             |  |
|                | 316 (10 100)                | 322                      |                            |                    |             |  |
|                | 329                         | 336                      |                            |                    |             |  |
|                | 343 (6530)                  | 352                      |                            |                    |             |  |
|                | 374                         | 386                      |                            |                    |             |  |
| $\text{NMe}_2$ | 390 (2240)                  | 404                      |                            |                    |             |  |
|                | 280                         | 282                      | 535                        | 0.08               | 1920        |  |
|                | 311 (17 000)                | 316                      | 570                        |                    |             |  |
|                | 324 (16 000)                | 346sh                    | 635sh                      |                    |             |  |
|                | 340sh                       | 420                      |                            |                    |             |  |
|                | 419 (9290)                  | 433                      |                            |                    |             |  |

<sup>a</sup> Emission measurements in  $\text{CH}_2\text{Cl}_2$ .

<sup>b</sup> Molar absorptivity ( $\text{M}^{-1}\text{cm}^{-1}$ ).

lifetimes there is little doubt but that in all cases the emission originates from a state with triplet multiplicity. The presence of the well resolved vibronic structure is quite striking and contrasts with the broad emission attributed to metal-to-ligand  $^3\text{CT}$  excited states of related platinum(II) terpyridine complexes [13,15]. It is entirely possible that the vibronic structure reflects the fact that the emission emanates from states that have significant intraligand excited-state character, *vide infra*.

Temperature-dependent lifetime measurements were only possible over a limited temperature range since methylene chloride is a non-glassing medium. The lack of long-term sample stability was another complication. The complexes selected for detailed studies were  $\text{Pt}(4'\text{-SMe-T})\text{Cl}_2$  and  $\text{Pt}(4'\text{-CN-T})\text{Cl}_2$ . For each complex the data satisfies the following phenomenological equation for the temperature dependence of the lifetime:



$$I = I_0 - A \exp[-\Delta E/(RT)] \quad (1)$$

The best fit of the data for the 4'-SMe-T complex has a limiting lifetime ( $\lambda_{\infty}^{-1}$ ) of 2.5  $\mu$ s, a frequency factor ( $A$ ) of  $1.3 \times 10^{11} \text{ s}^{-1}$  and an apparent activation energy ( $\Delta E$ ) of 1640  $\text{cm}^{-1}$ . The corresponding parameters for the 4'-CN-T complex are 0.25  $\mu$ s,  $1.8 \times 10^{11} \text{ s}^{-1}$  and 730  $\text{cm}^{-1}$ .

#### 4. Discussion

The goals of this investigation have been to understand the electronic structure of the platinum(II) terpyridine complexes and to develop systems with longer excited state lifetimes. The parent complex  $\text{Pt}(\text{terpy})\text{Cl}^+$  shows no significant photoluminescence intensity in room temperature acetonitrile, although the mixed-ligand terpy complexes that have thiocyanate or hydroxide in place of the chloride ligand are emissive [13]. The systems selected for the present studies involve modified terpy ligands and are freely soluble with TFPB as the counterion in the non-coordinating medium methylene chloride. Although not the principal focus of this work, the electrochemistry of the complexes is germane to the interpretation of the CT spectra. The most important point to recognize is the strong influence substituents have on the first ligand reduction. Electron-donating substituents like SMe or NMe<sub>2</sub> shift the potential in the negative direction, while electron-accepting substituents like CN have the opposite effect.

##### 4.1. Intramolecular charge transfer

As noted above, the absorption bands with  $\lambda_{\text{max}} > 350 \text{ nm}$  and  $\epsilon > 1000 \text{ M}^{-1} \text{ cm}^{-1}$  normally correspond to platinum-to-terpy MLCT transitions and therefore involve a type of ligand reduction [13,30]. These band assignments are consistent with the shifts that occur with a change in solvent polarity or the spectator ligand. Comparisons with the low-temperature emission from systems like  $\text{Ru}(\text{terpy})_2^{2+}$  also reveal that the lifetime and the Stokes shift are compatible with photoluminescence from a corresponding <sup>3</sup>CT state [13,31]. Finally, the population of a metal-to-ligand CT state can account for the pronounced emission quenching that occurs in donor solvents like acetonitrile. Due to the increase in the metal's formal oxidation state and the availability of open coordination sites, solvent-induced exciplex quenching is likely to be a very efficient process for such CT states [32–34].

One problem with the concept of a low energy metal-to-ligand CT excited state is the absence of a well defined wave corresponding to the oxidation of the metal center. However, a compensating effect is the fact that the first terpy reduction occurs at an unusually positive potential. Previous investigators have attributed this to a mixing interaction involving the relatively low-lying 6p<sub>z</sub> orbital of platinum and an empty  $\pi^*$  orbital of the polypyridine ligand [26]. This requires that

the redox-active  $\pi^*$  orbital (assumed also to be one in the same as the spectroscopically active  $\pi^*$  orbital) be antisymmetric with respect to a rotation about the two-fold axis that passes through the ligand. In the notation of Orgel, the symbols  $\psi$  and  $\chi$  designate orbitals that are respectively antisymmetric and symmetric with respect to the two-fold rotation operation [35,36]. Extended Hückel calculations show that the LUMO of the terpy ligand has  $\psi$  symmetry [37], and mixing with the higher energy 6p<sub>z</sub> Pt orbital would tend to drive the energy of the corresponding molecular orbital of the complex to even lower energy. The fact that the first ligand reduction is so sensitive to substitution at the 4' position of terpy is certainly consistent with this interpretation. Thus, mesomeric interactions with donor groups like NMe<sub>2</sub> or acceptor groups like CN depend upon overlap with the p<sub>z</sub> orbital of the 4' carbon atom, and this requires an orbital with  $\psi$  symmetry. Table 1 reveals that the potential of the second ligand reduction is less sensitive to 4' substituents. This could mean that the electron enters a ligand orbital with a different symmetry or that this reduction involves a metal-centered orbital [26]. In terms of the spectroscopy, the fact that the introduction of a 4' CN or SO<sub>2</sub>Me group induces a bathochromic shift in the CT absorption and emission maxima is easy to appreciate because formation of the excited state at least formally entails a ligand reduction. It is no surprise that an electron-withdrawing group would facilitate the process. However, electron-donating groups like NMe<sub>2</sub> and SMe also shift the CT maxima to lower energy, so there are obviously other factors involved. Indeed, a number of recent studies have made the point that CT processes are not just one-electron, center-to-center charge transfers [38,39].

For the platinum(II)-terpy systems at hand, particularly those with electron-donating substituents, the following analysis suggests that a configuration interaction with another CT state has a major influence on the state energies. The literature dealing with substituent effects and the absorption spectrum of benzene illustrate the phenomenon and serve as a useful basis for comparison [40,41]. The important point is that the introduction of either an electron-withdrawing or an electron-releasing substituent induces a red shift in the low energy  $\pi \rightarrow \pi^*$  absorption of benzene. For example, the lowest energy  $\pi \rightarrow \pi^*$  transition, the so-called  $\alpha$  band, occurs around 250 nm in the spectrum of benzene whereas for aniline the corresponding band falls around 285 nm. The reason is clear if one views aniline as a composite molecule containing a benzene ring and a peripheral nitrogen center with an active lone pair [40]. In essence, a configuration interaction with a higher lying nitrogen-to-ring CT state drives down the energy of the  $\pi \rightarrow \pi^*$  state that is the terminus of the  $\alpha$  transition and, at the same time, enhances the oscillator strength. The same kind of effect is evident in the  $\text{Pt}(4'\text{-SMe-T})\text{Cl}^+$  and  $\text{Pt}(4'\text{-NMe}_2\text{-T})\text{Cl}^+$  systems which exhibit anomalously intense, but relatively low energy CT transitions. Note that the red shifts occur despite the fact that the 4' substituents are electron donating and destabilize the reduced forms of the respective ligands. The UV spectra of the  $\text{Zn}(4'\text{-X-T})\text{Cl}_2$  analogues

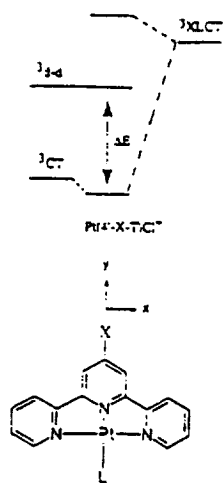


Fig. 3. Axis system and scheme for a configuration interaction between the emitting CT state and a  $\pi$ -CT intraligand excited state of  $\text{Pt}(4'\text{-X-T})\text{Cl}^-$ . The relative energy of the  $\pi$ -CT state is uncertain, but it may be the thermally accessible state that mediates decay.

are useful for the identification of the participating substituent-to- $\text{trpy}$  ( $\pi$ -CT) transitions since there are no interfering MLCT phenomena. Indeed, Fig. 2 shows that, by comparison with  $\text{Zn}(4'\text{-Me-T})\text{Cl}_2$ , both the  $4'\text{-SMe}$  and the  $4'\text{-NMe}_2$  complexes exhibit extra absorption intensity in the region of 290 nm that plausibly reflects  $\pi$ -CT excitation.

The structure given in Fig. 3 is useful for assessing the CT coupling phenomenon. Although the two-fold axis normally defines the  $z$ -direction in  $C_{2v}$  symmetry, the connections with archetypal  $D_{4h}$  complexes are more evident with the proposed choice of axes. However, apart from  $d(x^2 - y^2)$ , the relative order of the  $d$  orbitals is unclear in these polypyridine complexes [13,42]. Fortunately, intensity considerations are of some help in making band assignments. According to a simple model, the CT transitions that benefit from the charge-transfer term usually exhibit the bulk of the absorption intensity [43–45], and here these correspond to the  $y$ -polarized  $d(z^2) \rightarrow \psi$  and  $d(xz) \rightarrow \chi$  transitions to  $^1A_1$  excited states [13]. In view of the voltammetry data, the transition to the  $\psi$  orbital should occur at lower energy. Despite our earlier reservations [13], the CT absorption that occurs in the vicinity of 380 nm for  $\text{Pt}(\text{trpy})\text{Cl}^-$  appears to be intense enough to represent, or include, the  $d(z^2) \rightarrow \psi$  transition. For comparison, the reported values of the molar absorptivity of the corresponding visible band of  $\text{Ru}(\text{trpy})_2^{2+}$ , which contains twice as many acceptor ligands, range from 10 000 to 16 000  $\text{M}^{-1} \text{cm}^{-1}$  [19,31,46]. Thus, the CT absorption intensity is of the same order of magnitude for the platinum system. Since the  $y$ -polarized  $\pi$ -CT transition from the lone pair of the  $\text{NMe}_2$  group also gives rise to a  $^1A_1$  excited state, the interaction between the two zero-order  $^1A_1$  states produces the state with the absorption maximum at 420 nm in the spectrum

of  $\text{Pt}(4'\text{-NMe}_2\text{-T})\text{Cl}^-$ . A simple vector coupling argument based on the collinear transition moments accounts for the increase in the absorption intensity [40]. Exactly the same argument applies to the  $\text{SMe}$  analogue. By analogy with aniline, there is likely to be further mixing with a  $\pi-\pi^*$  state with  $^1A_1$  symmetry. In principle, the same kind of coupling is possible with a ligand-to-metal or a ligand-to-ligand CT state involving the ligand L opposite  $\text{trpy}$  [1,12]. And when X is electron-withdrawing, coupling to a  $\text{trpy-to-X}$  state can be important. However, a simple inductive argument is capable of explaining the absorption and the emission data pertaining to the  $4'\text{-CN-T}$  and  $4'\text{-SO}_2\text{-T}$  systems, and the absorption spectra of the corresponding  $\text{Zn}(4'\text{-X-T})\text{Cl}_2$  systems do not show any indication of that kind of a CT transition. Nevertheless, the emission from  $\text{Pt}(4'\text{-CN-T})\text{Cl}^-$  occurs at a lower energy than that of the  $\text{Pt}(4'\text{-NMe}_2\text{-T})\text{Cl}^-$  system. This is not a cause for concern because configuration interaction undoubtedly has a weaker influence on the energy of the triplet state of the  $4'\text{-NMe}_2\text{-T}$  complex. For sure, the dipole-dipole coupling between the two excitations is negligible in the triplet manifold due to the spin forbidden character of each of the CT processes.

#### 4.2. Emission intensities and lifetimes

Contrary to the energy-gap law [47], the unsubstituted  $\text{trpy}$  complex has the highest energy emission but practically the shortest excited-state lifetime in the whole series. The only system that appears to have a shorter lifetime is the  $4'\text{-Me-T}$  complex, and it, too, has a high energy CT absorption. These results are incompatible with direct relaxation from a homologous series of metal-to-ligand CT states [48], but they make sense if another state influences the decay. Suppose that an interaction with another state alters the orbital parentage to differing degrees within the series. Then, the intrinsic lifetimes vary in a way that does not simply depend on the excited state energy. Alternatively, there may be substituent-dependent deactivation through a thermally accessible excited state. The preliminary lifetime-versus-temperature results suggest that both effects are probably important. Although there is clear evidence of thermally activated decay, the nature of the state mediating decay is uncertain. In principle, the state involved could reside within the same potential energy surface. With certain copper(II) and zinc(II) porphyrins, for example, thermal population of vibrationally excited levels of the emitting state fosters decay [49–51]. The same effect can operate in the  $\text{Pt}(4'\text{-X-T})\text{Cl}^-$  systems if the resonance with the intra-ligand excited state alters the shape and/or the equilibrium geometry of the excited-state potential energy surface [52]. Although this mechanism is plausible, the presence of the vibrational structure in the emission spectra suggests that the excited-state surface nests within that of the ground state. If so, vibrationally induced relaxation is unlikely to be of great consequence.

In view of other reports dealing with emissive  $^3\text{CT}$  states of platinum(II) polypyridines and related systems [13,16,19], it seems more likely that the systems deactivate via a short-lived  $^3\text{d-d}$  state. The fact that electron-donating substituents could hinder such a pathway is interesting. In the course of their studies of the related  $\text{Ru}(\text{L})_2\text{-X-T}_2^{2+}$  systems, Maestri et al. have reported that an electron-donating substituent lowers the energy of the first  $^3\text{d-d}$  state and thereby reduces the barrier to quenching [19]. This makes sense in terms of the orbitals involved. While the lowest unoccupied orbital of the ruthenium system is a  $\text{d}\sigma^*$  orbital, the highest occupied orbital is a  $\text{d}\pi$  orbital. The inductive effect of an electron-donating group should destabilize the  $\text{d}\sigma^*$  orbital, but the substituent can destabilize the  $\text{d}\pi$  orbital even more because of direct conjugation via the  $\text{trpy } \pi$  orbital. With two  $\text{trpy}$  ligands involved, the upshot is that the deactivating  $^3\text{d-d}$  state drops to lower energy relative to the  $^3\text{CT}$  state so that quenching is more efficient. For platinum(II) polypyridines the relative energies of the d orbitals are less certain, but the filled  $\text{d}(z^2)$  orbital is probably the next highest energy level in these planar systems, in keeping with the importance metal-metal interactions have on packing and the electronic properties [7,8]. Thus, the HOMO and the LUMO of the metal center appear to have  $\text{d}\sigma^*$  character so that an electron-donating substituent destabilizes both. If so, the effect on  $\text{d}(x^2 - y^2)$  is likely to be greater due to better overlap with the nitrogen-donor orbitals of the ligand. The upshot would be an increase in the energy of the  $\text{d-d}$  state as well as  $\Delta E$ , the activation energy for radiationless decay. However, in view of the uncertain influence that other factors such as configuration interaction with the intraligand excited state have, the diagram in Fig. 3 assumes that the energy of the lowest energy  $^3\text{d-d}$  state remains essentially constant. Due to the drop in the energy of the emitting CT state, there is still a net increase in the energy required for deactivation via the metal-centered excited state. By the same kind of reasoning, the inductive effect associated with an electron-withdrawing substituent should stabilize the  $^3\text{d-d}$  state. The effect on the emitting  $^3\text{CT}$  state is also stabilizing, but even if there is a net increase in  $\Delta E$ , the effect will not be as dramatic as it is in the case of an electron-donating substituent. The results in Table 2 are obviously in accord with these qualitative predictions based on the assumption of a thermally accessible  $^3\text{d-d}$  state. On the other hand, the analyses of the temperature-dependent lifetime data yield modest frequency factors. The values obtained are indicative of nested surfaces or perhaps reversible population of the deactivating state [18,53]. Surer identification of the state that mediates the decay will require a great deal more experimental work.

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**Cooperative Substituent Effects Influence the Excited States of Copper Phenanthrolines**

**by**

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## ABSTRACT

Although copper systems are attractive as potential photosensitizers because of the ready availability of the metal, efficient nonradiative decay and solvent-induced quenching phenomena ordinarily limit their utility. Emission studies show that methyl substituents in the 3,8 positions constrain bulky groups in the 2,9 positions of 1,10-phenanthroline so as to enhance the lifetime of the reactive charge-transfer excited state of bis-ligand copper(I) complexes. Whereas, photoexcited  $\text{Cu}(\text{dbtmp})_2^+$  has a lifetime of 330 ns in dichloromethane, the parent complex without the 3,8 methyl substituents has a lifetime of only 150 ns under the same conditions. (dbtmp = 2,9-di(*n*-butyl)-3,4,7,8-tetramethyl-1,10-phenanthroline) Even in a strongly donating solvent like dimethylformamide, the dbtmp complex exhibits an excited-state lifetime of 140 ns. In dichloromethane the complex with the 2,9-diphenyl-3,4,7,8-tetramethyl-1,10-phenanthroline ligand exhibits a lifetime of 480 ns, the longest decay time yet reported for a bis-phenanthroline copper(I) complex in room temperature, fluid solution.

## INTRODUCTION

Substituent effects have come to the fore in the development of the chemistry of copper(I) with 1,10-phenanthroline derivatives. (In the following phen denotes the 1,10-phenanthroline ligand itself, and NN designates a generic derivative.) A seminal finding was that the presence of moderately bulky substituents in the 2,9 ring positions enhances the selectivity for copper(I) binding and stabilizes the copper(I) oxidation state.<sup>1,2</sup> Subsequent work has shown that incorporation of bulky substituents in the 2 and 9 positions also enhances the energy, the intensity and the lifetime of the emission from the lowest energy metal-to-ligand charge-transfer (CT) excited state.<sup>3,4,5</sup> One reason is that bulky substituents inhibit a flattening distortion that often occurs in the excited state and promotes nonradiative decay.<sup>3,4,6</sup> Bulky substituents also suppress ligand-addition reactions of the excited state, and formation of a fifth coordinate-covalent bond to the (formally) copper(II) center of the excited state initiates a novel type of exciplex quenching.<sup>7,8,9</sup> In 1983 Dietrich-Buchecker et al. showed that the reactive CT state of  $\text{Cu(dpp)}_2^+$  is much less susceptible to exciplex formation than that of the less hindered complex  $\text{Cu(dmp)}_2^+$ .<sup>10</sup> (dpp denotes 2,9-diphenyl-1,10-phenanthroline, and dmp denotes 2,9-dimethyl-1,10-phenanthroline.) Subsequent work involving alkyl substituents has shown that the importance of exciplex quenching decreases as follows with a change of substituent:<sup>4</sup>

methyl > *n*-butyl > neo-pentyl > sec-butyl.

However, if the substituents are too bulky, the ground-state complex itself becomes unstable as a result of interligand steric interactions. Thus, attempts to isolate the  $\text{Cu(NN)}_2^+$  complex carrying tert-butyl or mesityl substituents in the 2 and 9 positions have proved unsuccessful.<sup>11,12</sup> Recently, however, Karpishin and co-workers characterized the complex with the 2,9-bis(trifluoromethyl)-1,10-phenanthroline ligand.<sup>13</sup>

The present report shows that the coexistence of methyl substituents in the 3,8 positions and bulky substituents in the 2,9 positions of the phenanthroline produces a more crowded coordination sphere and dramatically extends the excited-state lifetime. The motivation for the investigation came from a recent study which showed that

reductive quenching of the  $\text{Cu}(\text{tptap})_2^+$  system is extremely facile.<sup>14</sup> (tptap is 2,3,6,7-tetraphenyl-1,4,6,7-tetraazaphenanthroline.) The implication was that juxtapositioning the phenyl substituents lent rigidity to the system and reduced the Franck-Condon barrier to electron-transfer quenching. The ligands employed below are 2,9-di(*n*-butyl)-3,4,7,8-tetramethyl-1,10-phenanthroline (dbtmp) and 2,9-diphenyl-3,4,7,8-tetramethyl-1,10-phenanthroline (dptmp). The emitting CT states of the resulting  $\text{Cu}(\text{NN})_2^+$  complexes exhibit remarkably long lifetimes even in donor media; indeed, the dptmp system has the longest excited-state lifetime ever measured for a  $\text{Cu}(\text{NN})_2^+$  system in fluid solution.

## EXPERIMENTAL

**Materials.** Scientific Products was the source of Burdick and Jackson high-purity, distilled-in-glass-grade acetonitrile, N,N-dimethylformamide (DMF), dichloromethane (DCM), and tetrahydrofuran (THF). The laser dye Coumarin 440 came from Laser Science. The phen, dmp, 3,4,7,8-tetramethyl-1,10-phenanthroline (tmp),  $\text{CuCl}_2 \cdot 2\text{H}_2\text{O}$ , KPF<sub>6</sub>, 2.0 M solutions of *n*-butyl lithium in hexanes and phenyl lithium in diethyl ether were from Aldrich Chemical Co. G. F. Smith provided the 4,7-dimethyl-1,10-phenanthroline (4,7-dmp). The complexes  $[\text{Cu}(\text{dbp})_2]\text{PF}_6$  and  $[\text{Cu}(\text{dpp})_2]\text{PF}_6$  were on hand from previous studies.<sup>15</sup> (dbp = 2,9-di(*n*-butyl)-1,10-phenanthroline).

**Methods.** The general method for the addition of the 2,9 substituents to the appropriate ligand precursor was that of Pallenburg and co-workers.<sup>11</sup> The desired product was typically the first fraction that eluted from an alumina column with DCM as the mobile phase. A published method sufficed for the preparation of all  $[\text{Cu}(\text{NN})_2]\text{PF}_6$  compounds.<sup>16</sup>

2,9-di(*n*-butyl)-4,7-dimethyl-1,10-phenanthroline (dbdmp). Recrystallization of a pale yellow fraction off the alumina column yielded a white solid. Here and in all subsequent tabulations the chemical shifts are relative to TMS. <sup>1</sup>H NMR ( $\text{CDCl}_3$ ,  $\delta$  in ppm): 7.92 (s, 2H), 7.34 (s, 2H), 3.19 (quartet, 4H), 2.74 (s, 6H), 1.88 (pentet, 4H), 1.51 (sextet, 4H), 1.00 (t, 6H).



*2,9-di(n-butyl)-3,4,7,8-tetramethyl-1,10-phenanthroline* (dbtmp). The final product was a white solid.  $^1\text{H}$  NMR ( $\text{CDCl}_3$ ,  $\delta$  in ppm): 7.92 (s, 2H), 3.18 (quartet, 4H), 2.67 (s, 6H), 2.50 (s, 6H), 1.90 (pentet, 4H), 1.55 (sextet, 4H), 1.07 (t, 6H).

*2,9-diphenyl-4,7-dimethyl-1,10-phenanthroline* (dpdmp). The final product was a pale yellow solid.  $^1\text{H}$  NMR ( $\text{CDCl}_3$ ,  $\delta$  in ppm): 8.49 (s, 4H), 8.00 (m, 4H), 7.55 (m, 6H), 2.85 (s, 6H).

*2,9-diphenyl-3,4,7,8-tetramethyl-1,10-phenanthroline* (dptmp). The final product was a cream-colored crystalline solid.  $^1\text{H}$  NMR ( $\text{CDCl}_3$ ,  $\delta$  in ppm): 8.09 (s, 2H), 7.70 (d, 4H), 7.45 (t, 2H), 7.15 (t, 4H), 2.78 (s, 6H), 2.50 (s, 6H)..

$[\text{Cu}(\text{dbdmp})_2]\text{PF}_6 \cdot \frac{1}{2}\text{H}_2\text{O}$ . This compound crystallized as an orange solid. Calculated: 61.56% C, 6.58% H, 6.53% N. Found: 61.52% C, 6.55% H, 6.46% N. The  $^1\text{H}$ -NMR spectrum confirmed the presence of the lattice water.

$[\text{Cu}(\text{dbtmp})_2]\text{PF}_6$ . After recrystallization from water and ethanol, the solid was orange brown. Calculated: 63.67% C, 7.12% H, 6.19% N. Found: 63.60% C, 6.81% H, 6.17% N.

$[\text{Cu}(\text{dpdmp})_2]\text{PF}_6 \cdot (\text{CH}_3\text{C}(\text{O})\text{CH}_3)$ . Recrystallization of a wine-red material from water and ethanol yielded dark red crystals. Calculated: 63.25% C, 4.08% H, 5.67% N. Found: 63.01% C, 4.15% H, 5.48% N. The  $^1\text{H}$ -NMR spectrum confirmed the presence of acetone.

$[\text{Cu}(\text{dptmp})_2]\text{PF}_6 \cdot \frac{1}{2}\text{H}_2\text{O}$ . Precipitation from water and ethanol yielded red needles. Calculated: 67.63% C, 4.97% H, 5.66% N. Found: 67.37% C, 4.74% H, 5.63% N. The  $^1\text{H}$ -NMR spectrum confirmed the presence of the lattice water.

Prior to luminescence, lifetime, or quenching studies, a series of freeze-pump-thaw cycles removed dioxygen from the samples. A 525 nm long-pass filter protected the photomultiplier tube from stray light, while a 450 nm notch filter helped isolate the excitation wavelength. A user-written program provided fits to the luminescence decay curves, and in all cases, the residual plots justified the use of a single exponential. The internal reference for the NMR spectra was the residual proton signal of the  $\text{CDCl}_3$  solvent.

**Instrumentation.** The absorption and emission spectra came from Perkin-Elmer Lambda 4C and SLM SPF 500C spectrophotometers, respectively. A description of the lifetime apparatus is in the literature.<sup>15</sup> The <sup>1</sup>H-NMR spectrometer was a 200 MHz Gemini unit. H. Daniel Lee performed the microanalyses at Purdue University.

## RESULTS

Table 1 contains absorbance data for the CT transitions of a number of Cu(phen)<sub>2</sub><sup>+</sup> derivatives. With or without other substituents present, the introduction of alkyl substituents in the 2,9 positions induces a distinct bathochromic shift in the CT maximum. The length of the carbon chain is not especially critical because Cu(dmp)<sub>2</sub><sup>+</sup> absorbs at almost the same wavelength as Cu(dbp)<sub>2</sub><sup>+</sup>.<sup>4</sup> Substituent effects are smaller at other ring positions. Upon introduction of methyl substituents at the 4,7 or the 3,8 positions, the principal CT absorption band shifts to slightly shorter wavelengths. Combinations of substituents at the 2,3,8,9 positions do, however, strongly impact the emission spectrum. Whereas the dbdmp and the dbp systems exhibit almost the same emission maximum and lifetime in DCM solution, the emission from Cu(dbtmp)<sub>2</sub><sup>+</sup> occurs at a shorter wavelength and has a significantly longer lifetime (Table 1).

The dptmp system shows a similar effect in the emission spectrum and is no less interesting from the point of view of absorption. Figure 1 reveals that the absorption spectrum exhibits a maximum at 467 nm in DCM as well as a rather weak shoulder at longer wavelengths. In contrast, the spectrum of the dpp or the dpdmp analogue has a maximum at ca. 440 nm and prominent shoulder at around 560 nm (Figure 1).

Independent of the ligand, the absorption maximum remains constant, but the emission maximum shifts to lower energy in polar solvents like DMF or acetonitrile (Table 2). The emission lifetime is also sensitive to the solvent, but it does not correlate with the polarity. Thus, the emission lifetime of Cu(dbtmp)<sub>2</sub><sup>+</sup> or Cu(dptmp)<sub>2</sub><sup>+</sup> is about the same in DCM or acetonitrile but much shorter in DMF. Most notably, the lifetime of the dptmp system in DCM is the longest yet reported for a Cu(NN)<sub>2</sub><sup>+</sup> system in room-temperature, fluid solution.

## DISCUSSION

**Absorption spectra.** The shape of the visible absorption spectrum provides important insights into the structure present in solution. Characteristically,  $\text{Cu}(\text{NN})_2^+$  systems with approximate  $D_{2d}$  symmetry exhibit an intense CT maximum in the neighborhood of 450 nm along with a weak shoulder at longer wavelengths. Both transitions relate to terms associated with the same HOMO  $\rightarrow$  LUMO excitation.<sup>17,18</sup> However, in order to account for the existence and the polarization of the low-energy shoulder, it is necessary to invoke a static or dynamic flattening distortion.<sup>17,18</sup> The data in Table 1 show that all complexes with *n*-butyl substituents in the 2,9 positions as well as  $\text{Cu}(\text{dptmp})_2^+$  exhibit spectra that conform to this classic pattern. In contrast, the anomalous intensity of the shoulder in the spectrum of the dpp or the dpdmp complex (Figure 1) reveals that some systems assume a highly flattened structure in solution. Crystallographic reports establish that a significant distortion is possible. Thus, in the solid state the dihedral angle between the two phenanthroline cores of the dpp system deviates 10 - 20° from the ideal value of 90° ( $D_{2d}$  symmetry), depending on the counterion.<sup>19,20</sup> Even larger distortions are possible because the dihedral angle of the copper(II) analogue is 118.9°.<sup>20</sup> The balance of forces includes steric effects and  $\pi$  conjugation between the phenyl substituents and the attached phenanthroline.<sup>19</sup> Such resonance is not possible in the  $D_{2d}$  structure which requires a 90° torsion angle for the two phenyl substituents. In the case of the dptmp complex the 3,8 methyl substituents should certainly promote the  $D_{2d}$  structure as they tend to enforce a 90° torsion angle for each phenyl substituent.

The wavelength of the CT absorption maximum varies markedly with the substituents present at the 2,9 positions of the phenanthroline. However, the basis for the variation is not clear.<sup>21</sup> The fact that the transition tends to shift to longer wavelength as the size of the substituent increases seems surprising. One might expect larger substituents to lead to longer Cu-N distances and higher-energy CT absorptions. The reason is that the excited state formally involves copper(II), an oxidation state that favors shorter Cu-N bond distances.<sup>20</sup> The CT absorption energy is not solvent

dependent because the  $\text{Cu}(\text{NN})_2^+$  system does not have a ground-state dipole moment that can specifically polarize the medium.

**Photophysical data.** The marked influence the 3,8 methyl substituents have on the luminescence is undoubtedly a steric effect. Whereas methyl substituents in the 4,7 positions have relatively little impact, methyl substituents in the 3,8 positions significantly restrict the conformational freedom of groups in the 2,9 positions. In the case of the dbtmp complex, for example, this is equivalent to increasing the effective size of the *n*-butyl groups. Consequently, the emission energy and the excited-state lifetime increase due to a reduction in structural relaxation. With phenyl groups in the 2,9 positions, the dptmp system exhibits an even longer excited-state lifetime. Till now, the dsbp complex had the longest reported lifetime (400 ns) for a photoexcited  $\text{Cu}(\text{NN})_2^+$  system in fluid solution.<sup>4</sup> (dsbp denotes 2,9-di(*sec*-butyl)-1,10-phenanthroline.) Aside from having a longer lived excited-state, the dptmp system is a better benchmark because the dsbp complex exists as a mixture of optical isomers.

Unlike the absorption, the emission is quite sensitive to the solvent medium. One obvious effect is the decrease in the emission energy as the dielectric constant increases. The probable explanation is that the CT state develops a dipole moment and  $\text{Cu}^{2+}-(\text{NN})^-$  character as the excitation localizes in the  $\pi^*$  orbital of one of the ligands.<sup>22</sup> Consequently, polar media more effectively solvate the relaxed CT state, and this produces a decrease in the emission energy. However, the same effect is not responsible for the trend in lifetimes because the emission from  $\text{Cu}(\text{dbtmp})_2^+$  occurs at the same wavelength in acetonitrile and DCM, yet the lifetime is much shorter in DMF. Solvent-induced exciplex quenching is evidently also a significant factor. As the Gutmann donor numbers reveal,<sup>23</sup> DMF is a much stronger Lewis base than acetonitrile and is therefore a more effective quencher. The results in Table 2 demonstrate that the addition of the 3,8 methyl groups also inhibits exciplex quenching. Inhibition occurs because the increase in interligand steric interactions destabilizes the five-coordinate form of copper.<sup>4,5,10</sup> Thus, the  $\text{Cu}(\text{dbtmp})_2^+$  system has a much longer excited-state lifetime than the analogous dbp complex in acetonitrile. For the same reason the emissive state of  $\text{Cu}(\text{dbtmp})_2^+$  has a

lifetime of 320 ns in acetonitrile, whereas the lifetime of dsbp complex is only 130 ns.<sup>4</sup> This is despite the fact that the 2,9 substituents, themselves, are larger in the case of the dsbp ligand.

## CONCLUSIONS

In combination with adjacent *n*-butyl or phenyl groups, methyl substituents in the 3,8 positions of bis-phenanthroline copper(I) complexes have a dramatic influence on the photochemical and photophysical properties. For the 2,9-diphenyl derivative, the presence of the 3,8 methyl groups destabilizes the flattened tetrahedral structure and forces the ground state to adopt a D<sub>2d</sub>-like geometry. Likewise, the same tetragonal distortion is less favorable in the CT excited state, and the emission therefore occurs at a higher energy. In dichloromethane the emission lifetime increases to 480 ns, the longest yet reported for a Cu(NN)<sub>2</sub><sup>+</sup> system. Finally, the back-to-back substituents combine to destabilize five-coordinate forms of the copper center and thereby suppress solvent-induced exciplex quenching. As a result, the dptmp complex exhibits a lifetime upwards of 100 ns even in donor media.

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Table 1. Room-Temperature Absorption and Emission Data for  $\text{Cu}(\text{NN})_2^+$  Systems in  $\text{CH}_2\text{Cl}_2$ .

| Ligand  | $\lambda_{\text{max}}(\text{abs})$ , nm | $\lambda_{\text{max}}(\text{em})^a$ , nm | $\tau$ , ns |
|---------|-----------------------------------------|------------------------------------------|-------------|
| phen    | 440                                     | -                                        | -           |
| 4,7-dmp | 434                                     | -                                        | -           |
| tmp     | 430                                     | -                                        | -           |
| dbp     | 457                                     | 670                                      | 150         |
| dbdmp   | 456                                     | 670                                      | 145         |
| dbtmp   | 453                                     | 635                                      | 330         |
| dpp     | 440                                     | 685                                      | 270         |
|         | 560sh                                   |                                          |             |
| dpdmp   | 440                                     | 685                                      | 310         |
|         | 550sh                                   |                                          |             |
| dptmp   | 467                                     | 670                                      | 480         |

<sup>a</sup>From uncorrected spectrum.



Table 2. Solvent Dependence of Room-Temperature Emission from  $\text{Cu}(\text{NN})_2^+$  Systems<sup>a</sup>

| NN    | MeCN                        |             | THF                         |             | DMF                         |             |
|-------|-----------------------------|-------------|-----------------------------|-------------|-----------------------------|-------------|
|       | $\lambda_{\text{max}}$ , nm | $\tau$ , ns | $\lambda_{\text{max}}$ , nm | $\tau$ , ns | $\lambda_{\text{max}}$ , nm | $\tau$ , ns |
| dbp   | 690                         | 35          | 680                         | 50          | 690                         | <10ns       |
| dbtmp | 650                         | 320         | 640                         | 330         | 650                         | 140         |
| dpp   | 715                         | 120         | 710                         | 190         | 700                         | 70          |
| dptmp | 690                         | 255         | 685                         | 365         | 685                         | 70          |

<sup>a</sup>All emission maxima from uncorrected spectra

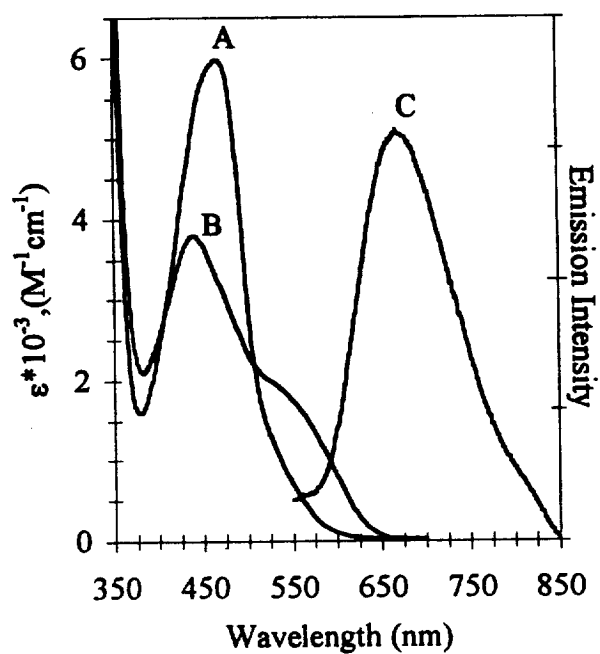


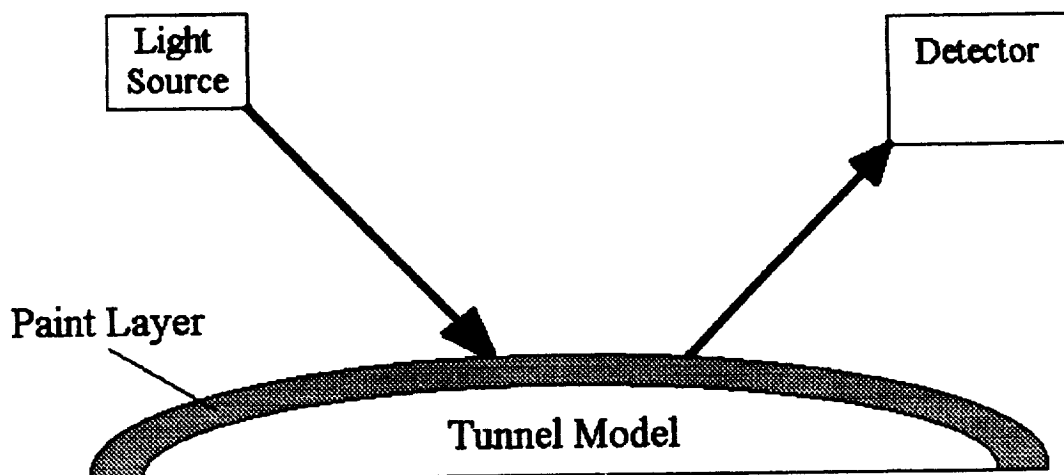
Figure 1. Absorption spectra of A:  $\text{Cu(dptmp)}_2^+$ , B:  $\text{Cu(dpdmp)}_2^+$  and emission spectrum of  $\text{Cu(dptmp)}_2^+$  (C) in DCM at room temperature.

## CHAPTER 1

### LUMINESCENT MOLECULAR TEMPERATURE SENSORS

#### Introduction

The synthesis of paint additives that have the ability to sense changes in temperature and or pressure is an area that is rapidly expanding.<sup>1, 2, 3</sup> The application of this kind of technology falls into two major categories, aerodynamics and biology. Applying this to aerodynamics involves mixing the desired compounds into a polymer and applying this paint on wind tunnel models, turbine blades, even airplane wings.<sup>2</sup> The information these sensors give back can be used to measure temperature, pressure, air flow, etc. Scheme 1.1 shows a schematic of the experimental setup for application of this type of sensor. This kind of sensor (thin surface film) is very desirable because it is a very non-destructive and non-invasive way to characterize a system. The pressure taps and thermocouples primarily used today do not allow for complete surface mapping, nor do they allow for testing without incorporating the sensors and the appropriate cables into the model.<sup>1</sup> In other words, a pressure tap or thermocouple requires the model to be structurally modified to hold the sensor, which can change the properties of the model. Mounting these sensors into a model could disrupt strength, increase stress, and can disrupt air flow, not to mention the cost involved in machining. By using a luminescent, thin film sensor that covers the surface, optical data can be sent to remote detectors located outside the wind tunnels with essentially no modification to the model. Also, since the entire model can be coated and measured, the data collected allows the entire model to be mapped, giving surfaces instead of data points.<sup>1-3</sup> There are two main types of luminescent chemical sensors in use today; pressure sensing paints (PSP)<sup>1, 2</sup> and temperature sensing paints (TSP).<sup>1, 3</sup>



Scheme 1.1. Schematic showing the experimental setup for a luminescent molecular sensor in a wind tunnel.

For the PSP's, an intense emission under anaerobic conditions that decreases dramatically as oxygen is introduced is desired. To date, several different types of compounds have been tested and it seems that tris(4,7-diphenyl-1,10-phenanthroline) ruthenium(II), as well as several porphyrins and laser dyes, work well here.<sup>1</sup> These compounds all have very intense room temperature emission that is adversely affected when oxygen is introduced. One difficulty in creating a very effective PSP is the juggling act that must be performed with the many factors that can affect the response of a PSP. For instance, if the sensor is a cationic coordination compound, the anion plays a major role in determining the solubility of the sensor in both the solvent and the paint.<sup>4</sup> Probably the most important factor is the polymer binder, since the oxygen molecule must travel through the binder to reach the sensor.<sup>5</sup> These and many other factors have been investigated and reported by others and will not be the focus of this project.<sup>1-5</sup>

For TSP's, there are several factors that figure in. The first is the temperature range of interest.<sup>3</sup> This is mostly determined by the facility since most wind tunnels are designed for use at specific temperatures. The lowest temperature range is approximately 100K to 150K, used in cryogenic wind tunnels. The paints that work in

this temperature region are called cryogenic TSP's, and are the focus of this research report. To date, the best sensors have been based on  $[\text{Ru}(\text{trpy})_2]^{2+}$  (where trpy = 2,2':6',2''-terpyridine).<sup>3</sup> An effective temperature sensor will be one which shows a dramatic change in luminescence intensity over a small temperature range and is consistent data in more than one binder.

Starting with the  $[\text{Ru}(\text{trpy})_2]^{2+}$  base, the easiest way to make changes is to add functional groups to one of the terpyridine ligands. Based on the response of the new sensors, it should be apparent which combination of ligands gives the best sensor. This report deals with the design and synthesis of terpyridine ligands and their use in creating new cryogenic sensors.

## Experimental

### Materials

All of the aldehydes and acetyl compounds, along with the NaH, ammonium acetate, paraformaldehyde, dimethylammonium chloride, iodine, triflic anhydride,  $\text{RuCl}_3$ ,  $\text{KPF}_6$ ,  $\text{NaBPh}_4$ , terpyridine, and 4'-chloro-terpyridine (Cl-trpy) were purchased from Aldrich and used as is. All solvents, except THF, were of reagent grade unless noted. The THF was distilled over Na metal and benzophenone under nitrogen to remove trace water. The deuterated solvents were purchased from Cambridge Isotope Laboratories. The ligands 4'-methylthio-2,2':6',2''-terpyridine (MeS-trpy) and 4'-methylsulfonyl-2,2':6',2''-terpyridine ( $\text{MeSO}_2$ -trpy) were available from a previous study.<sup>14</sup>

### Instrumentation

NMR spectra were recorded on a Gemini 200 MHz spectrometer and referenced to the residual proton of the solvent. Infrared spectra were recorded on a Perkin-Elmer IR spectrometer as nujol mulls. UV-Visible and emission spectra were measured on Perkin-Elmer Lambda 4C and SLM SPF 500C spectrophotometers, respectively. A

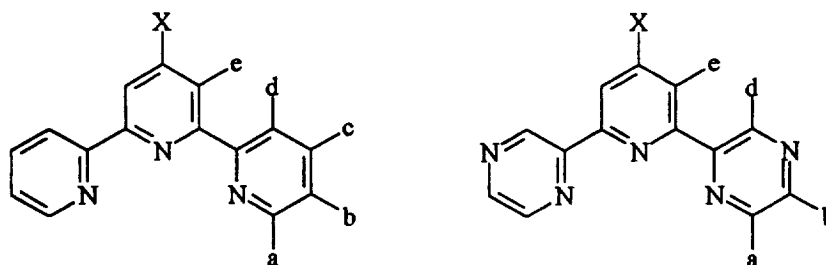
description of the lifetime apparatus is in the literature.<sup>14</sup> Luminophores were calibrated on the bench setup in the literature.<sup>3</sup> These calibrations were ran by Rick Erausquin. Wind tunnel measurements were performed by Dr. Keisuke Asai and his support staff at the National Aerospace Laboratory in Japan.

### Preparations

The ligands 4'-phenyl-2,2':6'-2"-terpyridine (ph-trpy),<sup>6</sup> 4'-(4-pyridyl)-2,2':6'-2"-terpyridine (4-py-trpy),<sup>7</sup> 4'-(3-pyridyl)-2,2':6'-2"-terpyridine (3-py-trpy),<sup>7</sup> 4'-(2-pyridyl)-2,2':6'-2"-terpyridine (2-py-trpy),<sup>7</sup> 4'-pentafluorophenyl-2,2':6'-2"-terpyridine (C<sub>6</sub>F<sub>5</sub>-trpy),<sup>6</sup> 4'-*p*-bromophenyl-2,2':6'-2"-terpyridine (*p*-Br-ph-trpy),<sup>6</sup> 4'-*p*-chlorophenyl-2,2':6'-2"-terpyridine (*p*-Cl-ph-trpy),<sup>6</sup> 4'-*p*-nitrophenyl-2,2':6'-2"-terpyridine (*p*-NO<sub>2</sub>-ph-trpy),<sup>7-10</sup> 2,6-bis(pyrazinyl)-pyridine (zyz),<sup>11</sup> 2,6-bis(2-pyridyl)-4-pyridone (HO-trpy),<sup>12, 13</sup> 2,6-bis(pyrazinyl)-4-pyridone (HO-zyz),<sup>12, 13</sup> 4'-triflato-2,2':6'-2"-terpyridine (TfO-trpy),<sup>12</sup> 2,6-bis(pyrazinyl)-4-triflato-pyridine (TfO-zyz),<sup>12</sup> 4'-dimethylamino-2,2':6'-2"-terpyridine (Me<sub>2</sub>N-trpy),<sup>14, 15</sup> 4'-ethoxy-2,2':6'-2"-terpyridine (EtO-trpy),<sup>13</sup> 2,4,6-triphenylpyridine,<sup>7-10</sup> 4,6-diphenyl-2,2'-bipyridine,<sup>7-10</sup> and 6,6"-diphenyl-2,2':6'-2"-terpyridine<sup>16-18</sup> were all prepared by literature methods using the appropriate starting materials. Tables 1.1 and 1.2 list the UV-Vis absorption and proton NMR data on all the prepared ligands, respectively.

Table 1.1. UV-Vis data for selected terpyridine ligands, in CH<sub>3</sub>CN, unless noted.

| Ligand                                     | $\lambda_{\text{max}}$ (nm) |
|--------------------------------------------|-----------------------------|
| trpy                                       | 310, 274, 251 <sup>a</sup>  |
| 4'-HO-trpy                                 | 278, 248                    |
| 4'-TfO-trpy                                | 277, 238                    |
| 4'-phenyl-trpy                             | 307, 275, 250               |
| 4'- <i>p</i> -NO <sub>2</sub> -phenyl-trpy | 284, 249, 241 <sup>a</sup>  |
| 4'-(4-pyridyl)-trpy                        | 312, 275, 240               |
| 4'-(3-pyridyl)-trpy                        | 307, 275, 245               |
| 4'-(2-pyridyl)-trpy                        | 316, 277, 243               |
| zyz                                        | 284, 241, 229               |

<sup>a</sup> in diethyl ether

Scheme 1.1. Labeling scheme for NMR data.

Table 1.2.  $^1\text{H}$  NMR data for terpyridine ligands, in  $\text{CDCl}_3$ .

| Ligand                                 | a    | b    | c    | d    | e    | other                  | NB-ref    |
|----------------------------------------|------|------|------|------|------|------------------------|-----------|
| trpy                                   | 8.73 | 7.36 | 7.86 | 8.64 | 8.47 | 8.0                    | III-73    |
| 4'-HO-trpy                             | 8.75 | 7.4  | 7.85 | 7.93 | 7.34 |                        | III-8, 28 |
| 4'-TfO-trpy                            | 8.73 | 7.4  | 7.9  | 8.63 | 8.43 |                        | III-18    |
| 4'-Cl-trpy                             | 8.7  | 7.35 | 7.85 | 8.6  | 8.48 |                        | III-63    |
| 4'-EtO-trpy                            | 8.7  | 7.34 | 7.87 | 8.63 | 8.2  | 4.3, 1.5               | III-134   |
| 4'-Me <sub>2</sub> N-trpy              | 8.67 | 7.3  | 7.83 | 8.62 | 7.78 | 3.2                    | III-53    |
| 4'-N-piperidinyl-trpy                  | 8.67 | 7.3  | 7.83 | 8.62 | 7.93 | 3.55, 1.69             | III-106   |
| 4'-N-piperazinyl-trpy                  | 8.66 | 7.29 | 7.82 | 8.62 | 7.94 | 4.13, 3.56, 2.68       | III-121   |
| 4'-ph-trpy                             | 8.74 | 7.37 | 7.9  | 8.69 | 8.77 | 7.9, 7.5               | III-74    |
| 4'-p-Cl-ph-trpy                        | 8.74 | 7.37 | 7.89 | 8.65 | 8.70 | 7.85, 7.48             | IV-1      |
| 4'-p-Br-ph-trpy                        | 8.73 | 7.37 | 7.89 | 8.67 | 8.7  | 7.79, 7.64             | III-83    |
| 4'-p-NO <sub>2</sub> -ph-trpy          | 8.72 | 7.37 | 7.88 | 8.66 | 8.73 | 8.35, 8.02             | II-124    |
| 4'-C <sub>6</sub> F <sub>5</sub> -trpy | 8.72 | 7.36 | 7.89 | 8.67 | 8.55 |                        | III-58    |
| 4-py-trpy                              | 8.74 | 7.39 | 7.9  | 8.69 | 8.77 | 8.77, 7.8              | III-59    |
| 3-py-trpy                              | 8.75 | 7.38 | 7.9  | 8.69 | 8.75 | 9.14, 8.75, 8.18, 7.45 | III-74    |
| 2-py-trpy                              | 8.74 | 7.35 | 7.87 | 8.66 | 9.1  | 8.8, 8.66, 7.83, 7.35  | III-70    |
| zyz                                    | 8.63 | 8.63 |      | 9.8  | 8.44 | 7.99                   | II-150    |
| 4-HO-zyz                               | 8.17 | 8.17 |      | 9.3  | 7.47 |                        | III-45    |
| 4-TfO-zyz                              | 8.73 | 8.73 |      | 9.83 | 8.43 |                        | IV-26     |
| 6,6"-diphenyl-trpy                     |      | 7.82 | 7.98 | 8.64 | 8.72 | 7.51, 7.98, 8.21       | V-11, 15  |
| 4,6-diphenyl-bipy                      | 8.23 | 7.35 | 7.96 | 8.7  | 8.0  | 7.52                   | III-143   |
| 2,4,6-triphenyl-pyridine               |      |      |      |      | 7.93 | 7.52, 7.78, 8.25       | III-133   |



All of the ruthenium compounds were synthesized and purified by following literature methods.<sup>19</sup> Metathesis reactions, when necessary, were performed by dissolving the ruthenium complex in acetone and adding the desired anion as a concentrated solution in water or in a mixture of acetone and water. Evaporation of the acetone resulted in precipitation of the ruthenium complex with the desired anion.

1,5-bis(2-pyridyl)-3-phenyl-1,5-pentanedione (II-72).<sup>6</sup> White solid, yield: 1.934 g (5.85 mmol) 66%. UV-Vis in Et<sub>2</sub>O: 266 nm, 227 nm. IR  $\nu_{\text{C=O}}$  in nujol oil: 1689 cm<sup>-1</sup>. <sup>1</sup>H NMR in CDCl<sub>3</sub>: 3.7 ppm (m, 4H), 4.15 ppm (p, 1H), 7.15 ppm (d, 1H), 7.24 ppm (t, 2H), 7.37 ppm (d, 2H), 7.43 ppm (ddd, 2H), 7.67 ppm (dt, 2H), 7.94 ppm (d, 2H), 8.63 ppm (d, 2H).

1-(2-pyridyl)-3-(*p*-nitrophenyl)-propenone (II-113).<sup>6</sup> Pale yellow solid, yield: 6.290 g (24.74 mmol) 92%. UV-Vis in Et<sub>2</sub>O: 314 nm. IR  $\nu_{\text{C=O}}$  in nujol oil: 1653 cm<sup>-1</sup>,  $\nu_{\text{N=O}}$ : 1636 cm<sup>-1</sup>. <sup>1</sup>H NMR in CDCl<sub>3</sub>: 7.51 ppm (ddd, 1H), 7.86 ppm (m, 4H), 8.18 ppm (d, 1H), 8.25 ppm (d, 2H), 8.41 ppm (d, 1H), 8.74 ppm (d, 1H).

*N*-{1-(2'-pyridyl)-1-oxo-2-ethyl}pyridinium iodide (II-111).<sup>20, 21</sup> Yellow product. IR  $\nu_{\text{C=O}}$  in nujol oil: 1627 cm<sup>-1</sup>. <sup>1</sup>H NMR in DMSO-*d*<sub>6</sub>: 6.50 ppm (s, 2H), 7.84 ppm (dt, 1H), 8.10 ppm (m, 2H), 8.27 ppm (t, 2H), 8.73 ppm (t, 1H), 8.87 ppm (d, 1H), 9.00 ppm (d, 2H).

1-pyrazinyl-3-dimethylaminopropanone (II-132).<sup>11</sup> White product, yield: 98 mg of white solid, only 64.3 % pure by NMR, 63 mg (0.352 mmol) 4.3%. <sup>1</sup>H NMR in CDCl<sub>3</sub>: 2.86 ppm (s, 6H), 3.51 ppm (brd. s, 2H), 3.92 ppm (brd s, 2H), 8.64 ppm (s, 1H), 8.78 ppm (s, 1H), 9.20 ppm (s, 1H).

*N*-{1-(2'-pyrazinyl)-1-oxo-2-ethyl}pyridinium iodide (II-146).<sup>20, 21</sup> Light beige product. IR  $\nu_{\text{C=O}}$  in nujol oil: 1699 cm<sup>-1</sup>. <sup>1</sup>H NMR in DMSO-*d*<sub>6</sub>: 6.49 ppm (s, 2H), 8.29 ppm (t, 2H), 8.75 ppm (t, 1H), 8.98 (m, 3H), 9.07 ppm (d, 1H), 9.25 (d, 1H).

1,5-bis(2-pyridyl)pentane-1,3,5-trione (III-4, III-26).<sup>12, 13</sup> Light mustard yellow solid. <sup>1</sup>H NMR in CDCl<sub>3</sub>: 8.65 ppm (d, 2H), 8.05 ppm (q, 2H), 7.8 ppm (t, 2H), 7.38 ppm (d, 2H), 6.78 ppm (s, 1.75H), 4.4 ppm (s, 0.75 H). IR in nujol:  $\nu_{\text{C=O}}$  1619 cm<sup>-1</sup>, 1558 cm<sup>-1</sup>. UV-Vis in CH<sub>3</sub>CN: 379 nm, 315 nm, 231 nm.

1,5-bis(pyrazinyl)pentane-1,3,5-trione (III-43).<sup>12, 13</sup> Orange solid, yield: 1.4 g (5.18 mmol) 60%. <sup>1</sup>H NMR in CDCl<sub>3</sub>: 8.90 ppm (s), 8.5 ppm (d), 8.45 ppm (d), 7.25 ppm (s), 6.58 ppm (s). UV-Vis in CH<sub>3</sub>CN: 382 nm, 321 nm, 268 nm, 220 nm.

4'-(*N*-piperidiny)-2,2':6'-2"-terpyridine (III-106). 541 mg (2.02 mmol) 4'-chloro-terpyridine was brought to reflux in a 25 mL rb flask containing 10 mL piperidine. This mixture was allowed to reflux overnight, whereupon a white ppt. had formed. After cooling to room temperature, this yellow-brown solution was poured onto 100 mL of ice and water. Lots of white solid formed immediately. This was filtered off and washed with ample amounts of water. Proton NMR of this material (in CDCl<sub>3</sub>) showed residual protons from the starting material so the product was treated a second time, in the same manner, with piperidine. Following the same work-up, this material gave a pure NMR spectrum, with the proper integration. Yield: 560 mg (1.8 mmol) 89%. <sup>1</sup>H NMR in CDCl<sub>3</sub>: 8.68 ppm (d, 2H), 8.66 ppm (d, 2H), 7.93 ppm (s, 2H), 7.83 ppm (t, 2H), 7.3 ppm (q, 2H + CHCl<sub>3</sub>), 3.55 ppm (broad s, 4H), 1.70 ppm (broad s, 6H).

4'-(*N*-piperaziny)-2,2':6'-2"-terpyridine (III-121). Same procedure as for 4'-(*N*-piperidiny)-terpyridine, utilizing 407 mg (1.52 mmol) 4'-chloro-terpyridine and 15 g (174 mmol) solid piperazine. Heating at ~140°C overnight followed by the same workup provided a pure (by NMR) sample. Yield: 473 mg (1.49 mmol) 98%. <sup>1</sup>H NMR in CDCl<sub>3</sub>: 8.65 ppm (m, 4H), 7.93 ppm (s, 2H), 7.84 ppm (t, 2H), 7.3 ppm (q, 2H + CHCl<sub>3</sub>), 4.1 ppm (broad, ~1H), 3.55 ppm (broad t, 4H), 3.08 ppm (broad t, 4H).

1-(2-pyridyl)-3-phenyl-propenone (II-177).<sup>6</sup> Yellow product. <sup>1</sup>H NMR in CDCl<sub>3</sub>: 7.42 ppm (m, 3H), 7.49 ppm (ddd, 1H), 7.74 ppm (m, 2H), 7.88 ppm (dt, 1H), 7.95 ppm (d, 1H), 8.20 ppm (d, 1H), 8.32 ppm (d, 1H), 8.75 ppm (d, 1H).

*N*-{1-(2'-phenyl)-1-oxo-2-ethyl}pyridinium iodide (III-130).<sup>20, 21</sup> Pale brown powder, yield: 36.7 g (113.2 mmol) 94%. <sup>1</sup>H NMR in DMSO-*d*<sub>6</sub>: 6.6 ppm (s, 2H), 7.67 ppm (t, 2H), 8.1 ppm (m, 4H), 8.63 ppm (t, 1H), 8.78 ppm (t, 1H), 9.07 ppm (d, 2H).

Bis-β-(dimethylamino)vinyl-2,6-pyridyl ketone (V-13).<sup>16-18</sup> Pale brown solid. <sup>1</sup>H NMR in CDCl<sub>3</sub>: 8.22 ppm (d, 2H), 7.9 ppm (m, 3H), 6.6 ppm (d, 2H), 3.2 ppm (s, 6H), 3.0 ppm (s, 6H).

## Results

### Synthesis

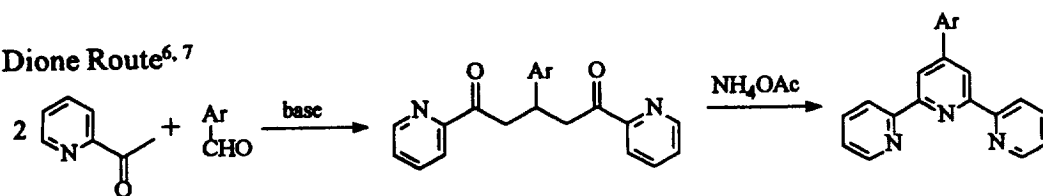
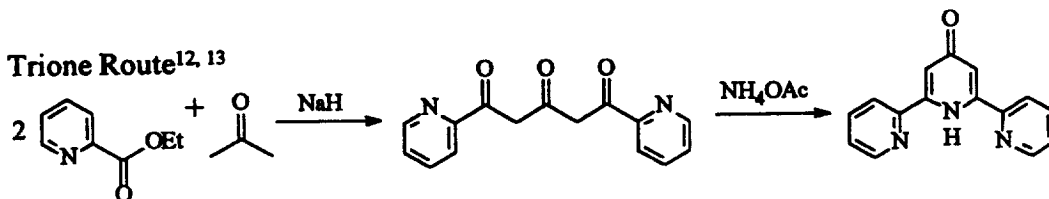
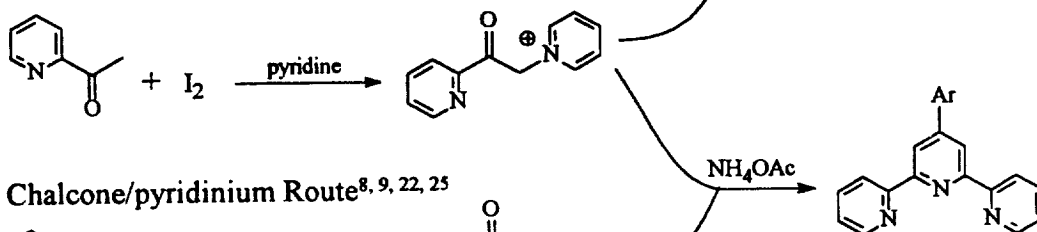
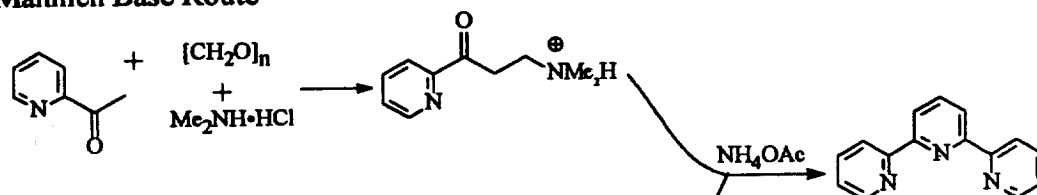
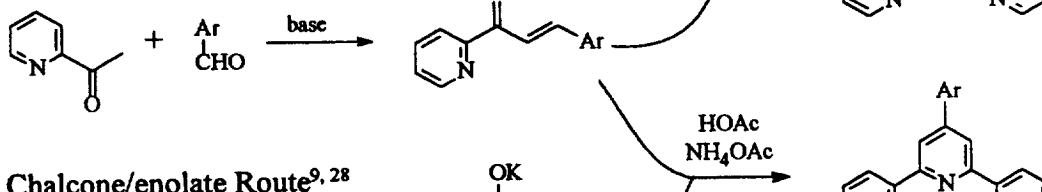
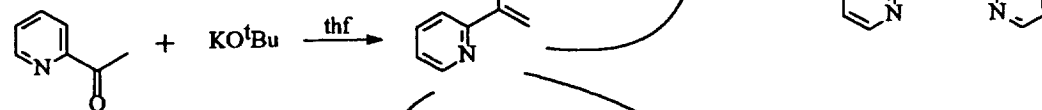
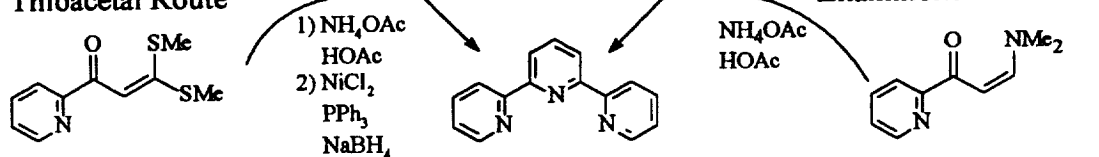
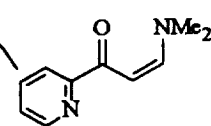
Ring-forming condensation (RFC) reactions make up the bulk of trpy synthesis.<sup>22</sup> These types of reaction schemes are usually based on the idea of taking the outer pieces, with the appropriate functional groups, and bringing them together while forming the central pyridine ring. The main RFC routes are shown in Scheme 1.2.

The dione route is the simplest of all the RFC reactions and works fairly well, when it is applicable. This pathway involves an Aldol condensation followed by a Michael addition, creating the 1,5-dione intermediate,<sup>6</sup> which then undergoes a RFC reaction, forming the central pyridine ring. This type of reaction was one of the first non-metal-mediated coupling pathways utilized to prepare 4'-aryl-terpyridines.

This route leads to 4'-aryl terpyridines in a relatively good yield under very simple reaction conditions. However, this route is not applicable to all aryl aldehydes. Unsubstituted to mildly substituted aldehydes work best. For example, benzaldehyde,<sup>6</sup> 2-, 3-, and 4-pyridine<sup>7</sup> carboxaldehyde all work very well and both the intermediate and final product are relatively pure, straight from the reaction mixture. The presence of a *para* Br, Cl, or CH<sub>3</sub> usually led to a gum-like dione product, which can be used directly in the next step, but does present some problems in characterizing the intermediate.

The exact reason for the gooey product is unclear. Different solvents (*iso*-propanol and butanols) and different ethanol concentrations have no effect on its formation. Regardless, the RFC reaction will still proceed on the gooey material and a pure terpyridine ligand is isolable without any extra work. E. C. Constable claims<sup>7</sup> that methanol titration of the gooey product will give a white precipitate, but it was unclear exactly how this is done and was therefore not investigated further since the goo produces a pure product.

In addition to the gooey product, if acetyl-pyrazine is used instead of acetyl-pyridine, a nice white powder is formed, which analyzes as some kind of oligomer that

**Dione Route<sup>6, 7</sup>****Trione Route<sup>12, 13</sup>****Mannich Base Route<sup>11</sup>****Chalcone/pyridinium Route<sup>8, 9, 22, 25</sup>****Chalcone/enolate Route<sup>9, 28</sup>****Thioacetal Route<sup>29</sup>****Enaminone Route<sup>30, 31</sup>**

Scheme 1.2. Summary of ring-forming condensation (RFC) reactions.

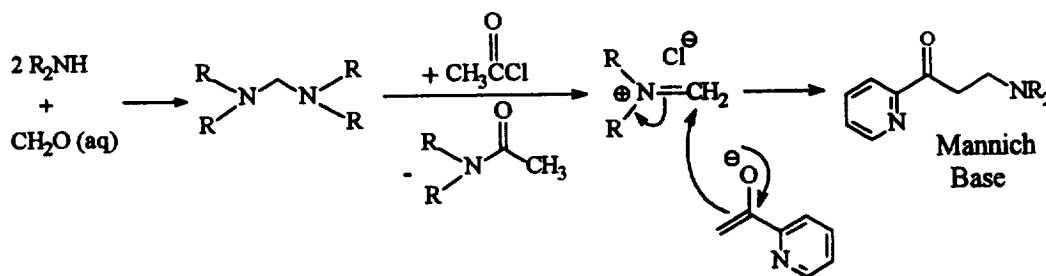
has well defined  $^1\text{H}$  NMR peaks from 1 ppm to 9 ppm almost continuously. This material is formed, regardless of the conditions, consistently in the reaction between acetyl-pyrazine and benzaldehyde.

The presence of strong functional groups (nitro, amino, methoxy) leads to the formation of highly colored precipitates. These precipitates analyze to be the corresponding chalcones ( $\alpha,\beta$ -ene-one product) and not the diones as was expected. These were not anticipated initially, but literature searches confirmed them as products and also how they could be converted to the corresponding terpyridine ligands.<sup>7-10</sup>

The trione route is based on the dione route, and leads, with decent yield, to 2,6-bis(2-pyridyl)-4-pyridone.<sup>12, 13</sup> Synthesis of the pyridone is based on a crossed Claisen condensation between the pyridyl ethyl ester and acetone, creating the trione product. Condensation of the two outer ketones with one equivalent of ammonium acetate creates the pyridone ring, which can tautomerize to give the 4'-hydroxyl-terpy derivative. This is facilitated by the presence of metal ions.<sup>13</sup> This reaction scheme also works on acetyl-pyrazine, creating 2,6-bis(pyrazinyl)-4-pyridone in excellent yield.

The Mannich base route offers a pathway to create unsubstituted central ring derivatives and has been used to synthesize several new ligands.<sup>11</sup> It utilizes the Mannich base generated in the reaction between an acetyl-pyridine derivative, dimethylammonium chloride, and paraformaldehyde. This then undergoes a Michael-type reaction, forming a non-isolable 1,5-dione-2-ene intermediate, which undergoes a RFC reaction to form the central ring. Formation of the Mannich base can be done in either acidic or basic conditions.<sup>23</sup> Alternatively, the Mannich base may be prepared by addition of the acetyl-derivative to an iminium reagent, as shown in Scheme 1.3.<sup>24</sup>

In our hands, for both pyrazine and pyridine, the corresponding Mannich bases were extremely difficult to synthesize, regardless of the conditions. Mostly a brown tar would be formed that had a strong amine stench to it. This material would not chromatograph well and TLC analysis showed a mixture of products. Synthesis via the Mannich base route was scrapped.

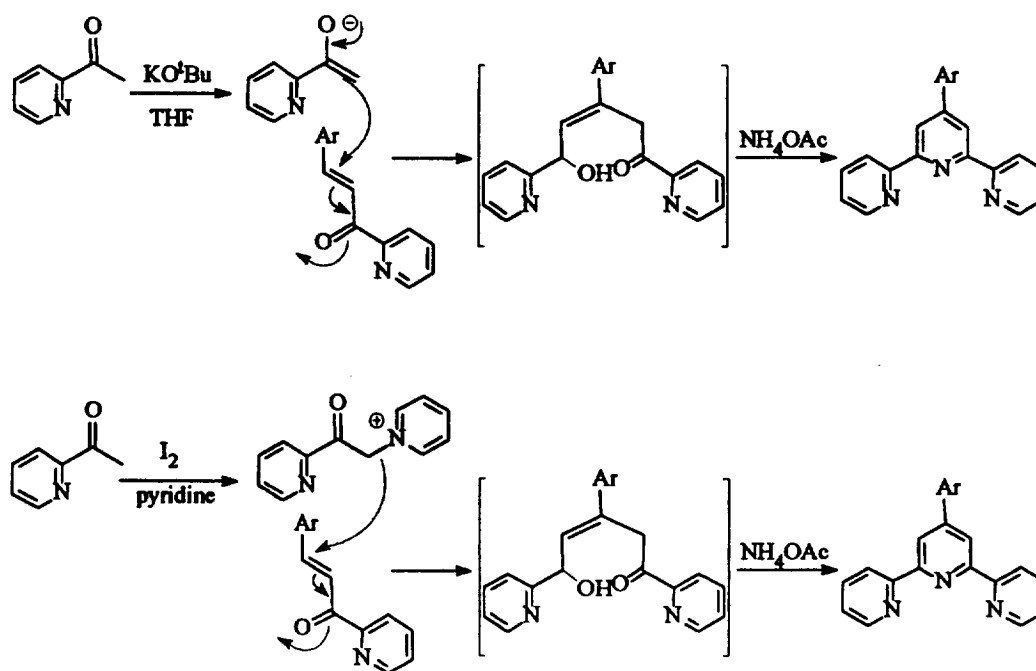


Scheme 1.3. Mannich base synthesis using an iminium reagent.

The chalcone/pyridinium and chalcone/enolate pathways are both used quite frequently to synthesize trpy derivatives.<sup>22, 25</sup> They work well for trpy derivatives that do not form the dione, due to solubility reasons, etc. In both cases the first step of the synthesis is the Aldol condensation of the acetyl-derivative with an aromatic aldehyde to form the chalcone. The second step is the Michael addition of an activated acetyl-derivative, either a preformed enolate or a stabilized enolate, to presumably create a 1,5-dion-2-ene intermediate.<sup>8</sup> This then condenses to form the central ring. Overall, this reaction scheme is more commonly referred to as the Kröhnke synthesis<sup>8</sup> and has been exploited very effectively by E.C. Constable et al.,<sup>9</sup> see Scheme 1.4.

The chalcone/pyridinium route was the first route examined in converting chalcones to terpyridines. The preparation of the pyridinium iodide salt was the first step. This reaction was in the literature,<sup>20</sup> but the purification and spectroscopic data (other than  $\nu_{C=O}$ ) was unavailable. Correspondence with Grant Summerton, of Dr. John Field's group in Natal, South Africa, lead to a simple purification involving a short reflux in ethanol with decolorizing charcoal.<sup>21</sup>

The pyridinium reagent is fairly interesting in itself. Based on the reaction and inductive arguments, it would seem that this reagent is a stabilized carbocation. This is very unlikely since the carbonyl carbon is already electrophilic in nature and the presence of two adjacent partial positive charges seems rather unlikely.<sup>26</sup> A better way of viewing this compound is by treating it as a stabilized enolate. In this case, even though the  $\alpha$ -methylene is bound to a quaternary nitrogen, the hydrogens are still acidic and the carbon is therefore nucleophilic in nature and will undergo Michael-type reactions.<sup>27</sup>

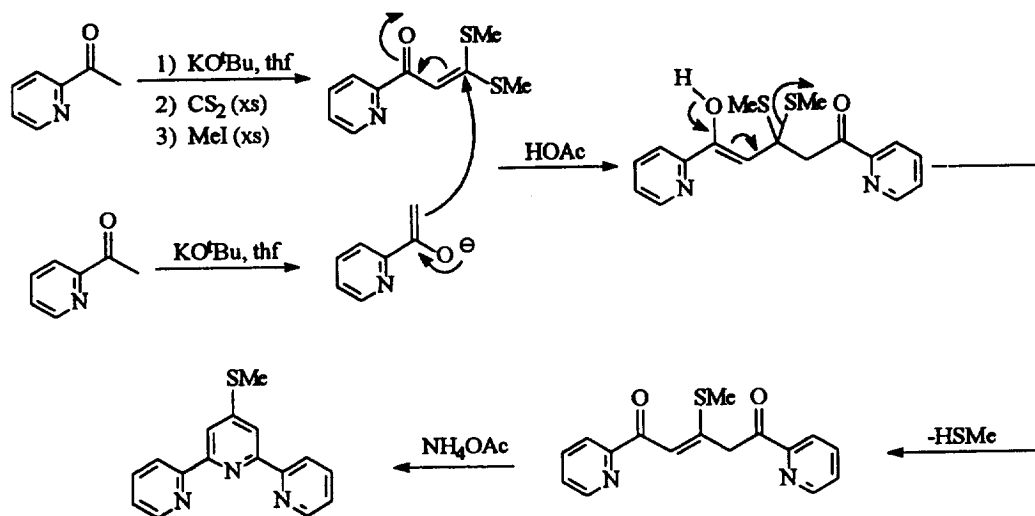


Scheme 1.4. Summary of the Kröhnke synthesis.

Once a pure pyridinium salt was obtained, examination of the literature revealed several different experimental conditions for the formation of terpyridines from chalcones and pyridinium salts.<sup>7-10</sup> With electron withdrawing groups, the reactions seemed to work best with just an ethanol reflux and ammonium acetate overnight. With electron donating groups present on the benzene ring, nothing seemed to work. It is not clear why, as there are literature reports of terpyridine ligand synthesis bearing electron donating substituents performed in this fashion. A solution to this problem was referred to in a review article<sup>22</sup> which turned out to be useful in synthesizing electron donating terpyridines as well as some sterically demanding terpyridines. This method has been utilized very effectively by Michalec et al<sup>28</sup> as well as E. C. Constable and co-workers.<sup>9</sup> This method is the chalcone/enolate route.

The chalcone/enolate route involves treating the chalcone with a preformed potassium enolate of acetyl-pyridine followed by treatment with acetic acid and ammonium acetate. The reaction itself works pretty well but the best method of purification is yet to be determined.

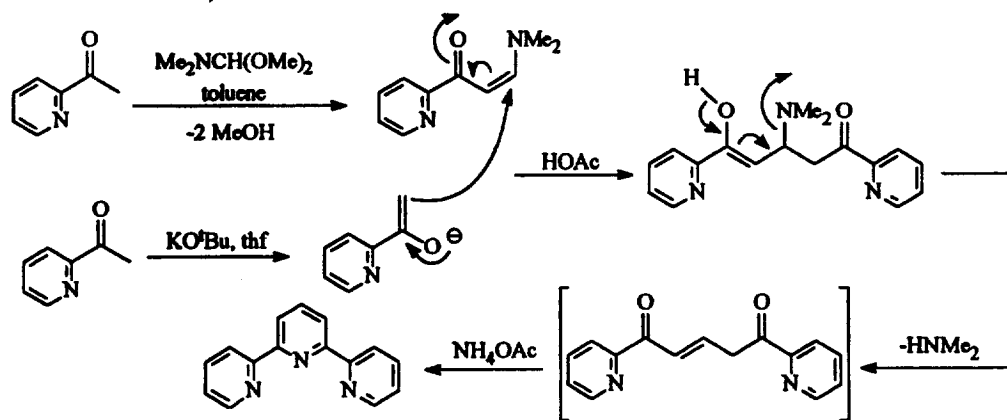
The thioacetal route has been pioneered by K.T. Potts et al.<sup>29</sup> This synthetic scheme produces 4'-methylthio-trpy, in which the MeS group can be converted to several different functional groups, including hydrogen.<sup>29</sup> This route is based on the chalcone/enolate pathway to some degree. In this case the bis(methylthioether)-eneone is synthesized, then treated with an enolate species, followed by condensation to give the corresponding trpy derivative in a Michael-type reaction, see Scheme 1.5. The bis(methylthioether) functionality activates the alkene for attack to create a 1,5-dione-2-ene intermediate that is usually not isolated. This method has relatively good yields, but the release of methylthiol, which never seems to leave the product,<sup>16</sup> makes this pathway somewhat unpleasant. Also, the remaining methylthioether functionality is somewhat difficult to remove.<sup>16</sup>



Scheme 1.5. Summary of the thioacetal method.

The last route has very recently crept into the forefront of trpy synthesis.<sup>6, 17</sup> This reaction is similar to the thioacetal route, except it uses an enaminone to react with the enolate. This reaction most likely, again, forms a 1,5-dione-2-ene intermediate that condenses to form the central ring, see Scheme 1.6. This method has been used to prepare unsubstituted terpyridine in 2 steps, with excellent yield.<sup>16</sup> It has also been used to prepare some trpy derivatives and is a very straightforward route to these ligands.<sup>17</sup>



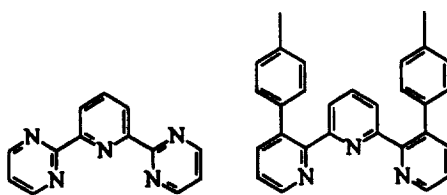


Scheme 1.6. Summary of the enaminone method.

One appealing feature of this preparation is the fact that it leaves the central ring unsubstituted. Until now, this was not an easy task, see the Mannich base discussion above. Other notable characteristics about this reaction are the rather high yield it offers and its applicability.

One of the main reasons for the high yield is the ability to obtain an almost quantitative yield of the starting enaminone. Reaction of acetyl-pyridine with dimethylformamide dimethyl acetal produces the enaminone and methanol. If the methanol is distilled off during the reaction,<sup>16</sup> the equilibrium is forced towards the product side. Purification is accomplished by precipitating the product and filtering. Analysis of the filtrate indicates it is mostly unreacted acetyl-pyridine with some product. By treating the mother liquor with another equivalent of dimethylformamide acetal, more enaminone is formed and the reaction nears 100% yield.

Another interesting point is that this route seems to be the only one so far that is completely applicable to all the nitrogen heterocycles. Terpyridine derivatives based on pyridine and pyrimidine have already been synthesized,<sup>17</sup> see Scheme 1.7, and there is no reason to suggest that pyrazine, quinolines, and other diazines would not work. This reaction also works with 2,6-diacetyl-pyridine, which makes it ideal for synthesizing 6,6''-disubstituted terpyridines.



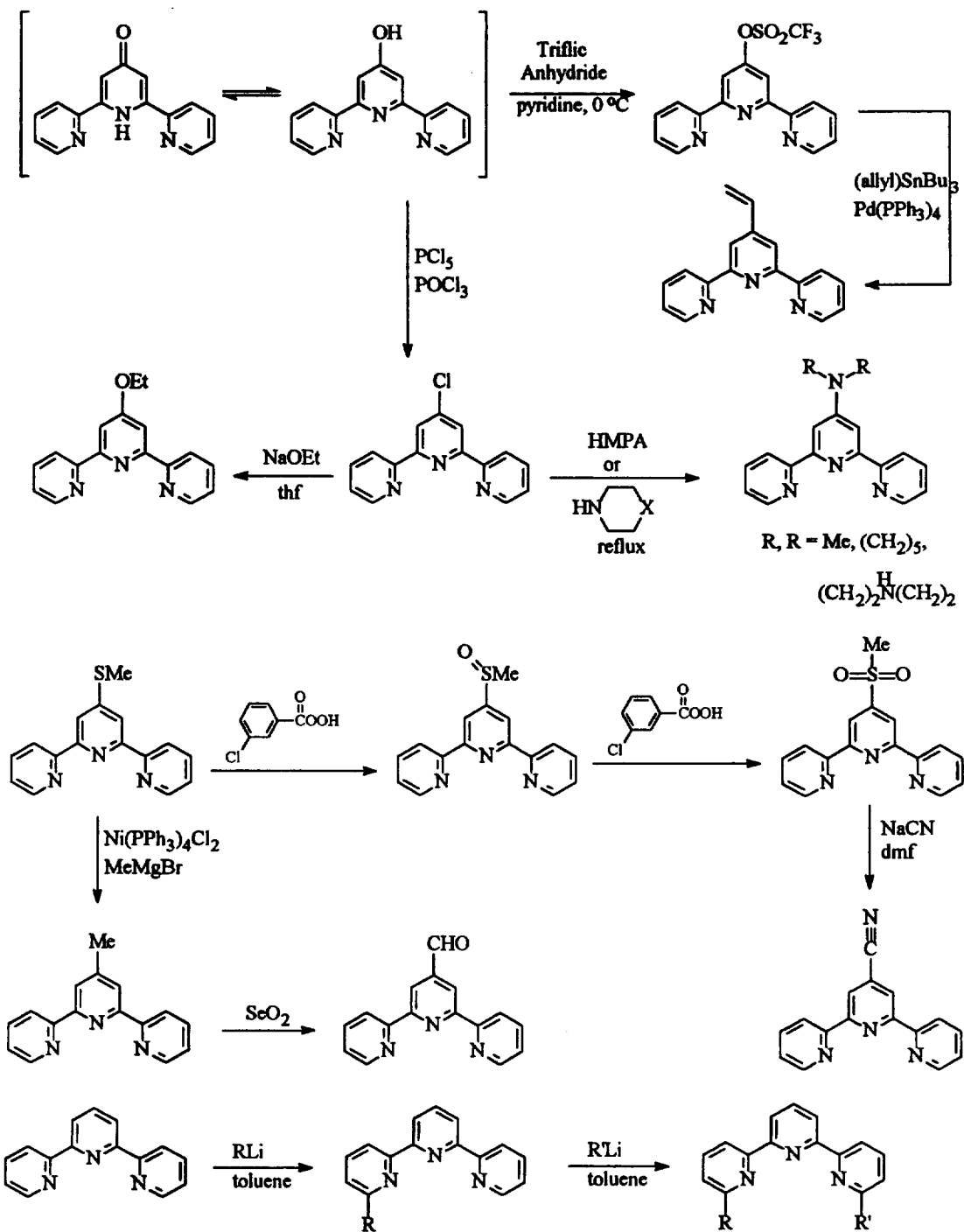
Scheme 1.7. Terpyridine ligands synthesized using acetyl-pyridine derivatives.

### Functional Group Transformation Reactions

There are many examples of synthetic functional group transformations in terpyridine chemistry, see Scheme 1.8. For the most part these reactions work as reported in the literature. The one exception is the conversion of 4'-chloro-terpyridine into 4'-dimethylamino-terpyridine.<sup>30</sup> Constable claims that chelation of 4'-Cl-trpy around Fe(II), refluxing in ethanol with dimethylammonium chloride and KOH, then oxidation of the iron produces the desired product in good yield.<sup>30</sup> In our work, no such reaction occurred with dimethylammonium chloride, diethyl amine, or piperidine. The chloride derivative could be converted, however; by simple reflux in the neat amine (to give the piperidine and piperazine derivatives) or HMPA<sup>15</sup> (to give the dimethylamine derivative). This type of reaction is much more straightforward and the work-up is simple. The yields of these reactions also were higher than the reported values. These types of reactions did not work on converting *p*-halogen-phenyl-terpyridine derivatives into their corresponding amino derivatives.

Potts and co-workers have done extensive work with the methylthioether functionality.<sup>29</sup> They have shown how to convert the alkyl thiol into a sulfonyl, alkyl, even an aldehyde. They have also shown how to synthesize a 4'-triflate-terpyridine derivative which allows for palladium catalyzed coupling reactions to be investigated.<sup>12</sup>

Electronically and sterically tuned terpyridines represent the next wave of these ligands and promise to hold some very interesting chemistry. The limiting reagent is the fact that terpyridine chemistry has only some similarities to pyridine chemistry and even fewer to benzene chemistry. This limited understanding is growing everyday and soon very elaborate ligands should be available with only limited synthetic effort.



**Scheme 1.8. Summary of substitution reactions.**

### NMR Data

All the terpyridine ligands synthesized in this project have similar chemical shifts for the outer ring protons, which is not surprising based on the limited interaction the three rings would have, in the metal-free case. The *e* proton (3' and 5' hydrogens) shows the most change in the chemical shift. This proton shifts to a higher field (lower chemical shift) as the  $\pi$ -donating ability of the 4' substituent increases. For example, the chemical shift decreases in the order H, TfO, EtO, *N*-piperidinyl, Me<sub>2</sub>N. This is consistent with the idea that the stronger  $\pi$ -donating amines can conjugate with the ring  $\pi$ -system more, thus decreasing the amount of shielding of the ring hydrogens by placing more electron density on the protons.<sup>31</sup> Conversely, with the electron withdrawing Cl group, the *e* proton is shielded more and the chemical shift moves to a slightly lower field (higher chemical shift) since it pulls electron density away from the proton.<sup>31</sup> These effects are also seen with substituted benzene complexes.<sup>31</sup> If the terpyridine is substituted in the 4' position with a phenyl ring, the *e* proton shift does not change as much when the phenyl ring is substituted. The main differences in these compounds are the locations of the phenyl protons, due to their proximity to the functional groups.

### Ruthenium Terpyridines

The photophysical properties of the ruthenium(II) terpyridines synthesized with the aforementioned ligands are tabulated below in Table 1.3, and some representative spectra are shown in Figure 1.1. Previously reported compounds agree with reported values, and the new compounds seem to follow the same trends.<sup>19</sup> One of the new compounds, [Ru(trpy)(NC-trpy)]<sup>2+</sup>, proved difficult to purify. The impurity seemed to be [Ru(trpy)<sub>2</sub>]<sup>2+</sup>, which only shows up during low temperature emission scans. The impurity seemed traceable back to the starting material Ru(trpy)Cl<sub>3</sub>. Boiling ethanol extractions and synthesis of Ru(trpy)Cl<sub>3</sub> in the presence of excess NaCl seemed to help considerably. The room temperature lifetime value for [Ru(trpy)(NC-trpy)]<sup>2+</sup> is one of the longest for simple bis-terpyridine ruthenium complexes.

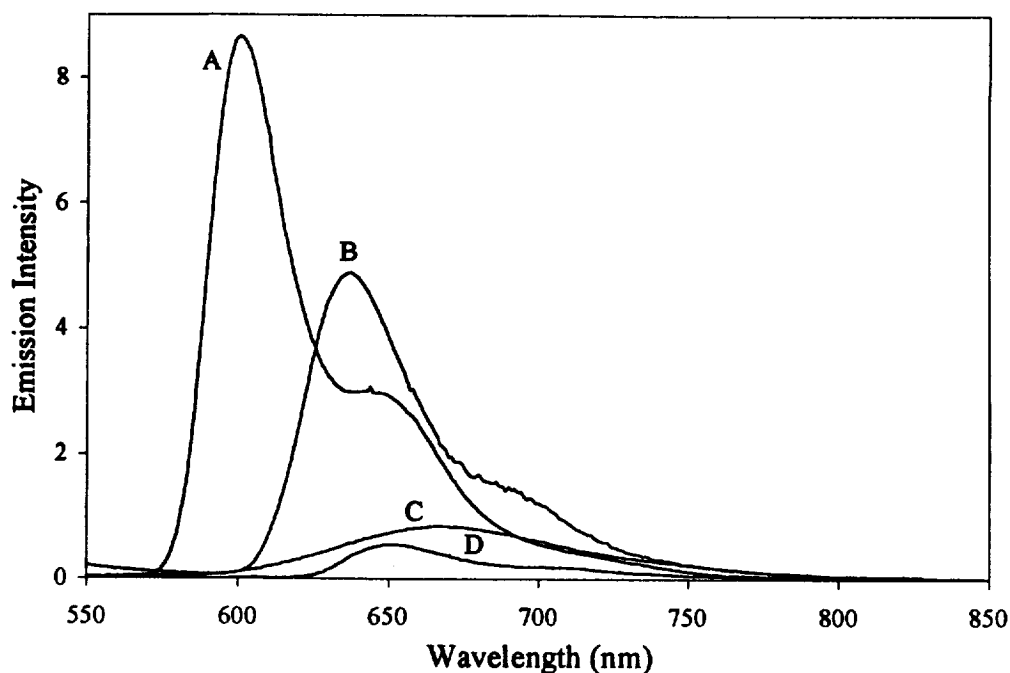


Figure 1.1. Representative emission spectra of  $[\text{Ru}(\text{X-trpy})(\text{Y-trpy})]^{2+}$  complexes at room temperature and 77K. A)  $[\text{Ru}(\text{trpy})_2]^{2+}$  in butyronitrile glass at 77K. B)  $[\text{Ru}(\text{NC-trpy})_2]^{2+}$  in butyronitrile glass at 77K. C)  $[\text{Ru}(\text{NC-trpy})_2]^{2+}$  in acetonitrile at room temperature. D)  $[\text{Ru}(\text{ppd-trpy})_2]^{2+}$  in butyronitrile glass at 77K.

### Sensor Calibrations

Calibration of the ruthenium complexes as temperature sensors was handled very effectively by the bench setup designed by Rick Erausquin of Dr. John Sullivan's laboratory. The emission intensity was monitored from 100K up to 300K. The faster the emission intensity drops as the temperature increases, the more sensitive the paint. Figure 1.2 shows the response of some of the new terpyridine complexes along with the benchmark sensor, VH-127, which was donated to the Sullivan laboratory by Prof. R. Thummel. The steep slope of the VH-127 compound makes it a very desirable compound, while its elaborate and involved synthesis makes it a very undesirable compound.

Table 1.3. Room temperature photophysical data for  $[\text{Ru}(\text{X-trpy})(\text{Y-trpy})]^{2+}$  complexes.

| X       | Y                             | Abs (nm) <sup>a</sup> | Em (nm) <sup>b</sup> | $\tau$ (ns) <sup>b</sup> |
|---------|-------------------------------|-----------------------|----------------------|--------------------------|
| H       | H                             | 475                   | ---                  | ---                      |
| H       | Cl                            | 478                   | ~635                 | <10                      |
| H       | MeS                           | 483                   | ---                  | ---                      |
| H       | TfO                           | 475                   |                      |                          |
| H       | MeSO <sub>2</sub>             | 479                   | 672                  | 44                       |
| H       | NC                            | 482                   | 665                  | 55                       |
| H       | ppd                           | 492                   | ~700                 | <10                      |
| H       | ph                            | 480                   | ---                  |                          |
| H       | <i>p</i> -NO <sub>2</sub> -ph | 475                   | ---                  |                          |
| H       | C <sub>6</sub> F <sub>5</sub> | 481                   | ---                  |                          |
| H       | 4-py                          |                       |                      |                          |
| NC      | NC                            | 489                   | 666                  |                          |
| ppd     | ppd                           | 502                   | ---                  | ---                      |
| TfO-zyz | TfO-zyz                       | 495                   | ---                  | ---                      |
| TfO     | TfO                           | 480                   | ---                  | ---                      |

a in CH<sub>3</sub>CNb in CH<sub>3</sub>CN, not deoxygenated

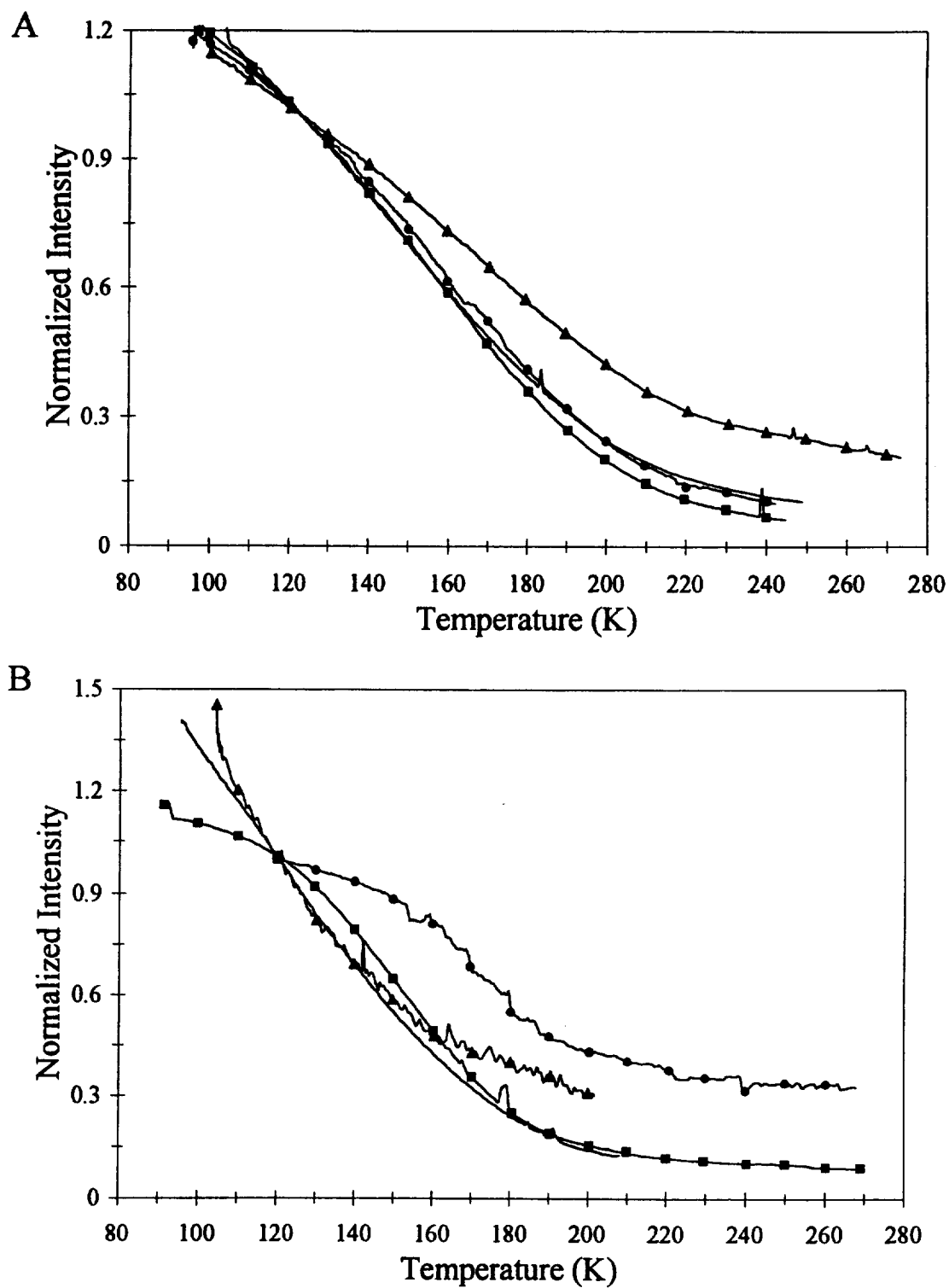


Figure 1.2. Intensity versus temperature calibration plots. In A, the triangle is HNC, the line is HMeSO<sub>2</sub>, the square is HMeS, and the circle is Hppd. In B, the triangle is HVH-127, the line is ppdppd, the square is Hph, and the circle is HH.

### Wind Tunnel Evaluation

Some of the new terpyridine compounds were tested in the cryogenic wind tunnel at the National Aerospace Laboratory (NAL) in Japan by Dr. Keisuke Asai. However, none of the new compounds were able to generate the emission signal that  $[\text{Ru}(\text{trpy})_2]^{2+}$  can at temperatures between 100 and 150K. Figure 1.3 shows the response of a  $[\text{Ru}(\text{trpy})_2]^{2+}$  based paint in the NAL cryogenic wind tunnel. This data was taken by Dr. John Sullivan, Dr. Keisuke Asai, and the cryogenic wind tunnel support staff at NAL. The model was a circular arc bump and the tunnel temperature was 150K. The picture is generated by taking a reference picture at Mach 0.25, then another picture at Mach 0.75. The ratio of the second photo to the first gives the image shown. The faint line about 3/4 of the way back is a shock wave. The temperature difference across the shock wave is  $\sim 5^\circ\text{C}$ . The dot followed by a triangular region is a small "bump" placed at the front of the model to induce turbulent flow as a test to see if the paint will in fact respond to such a small change in temperature. The gray scale is artificial.

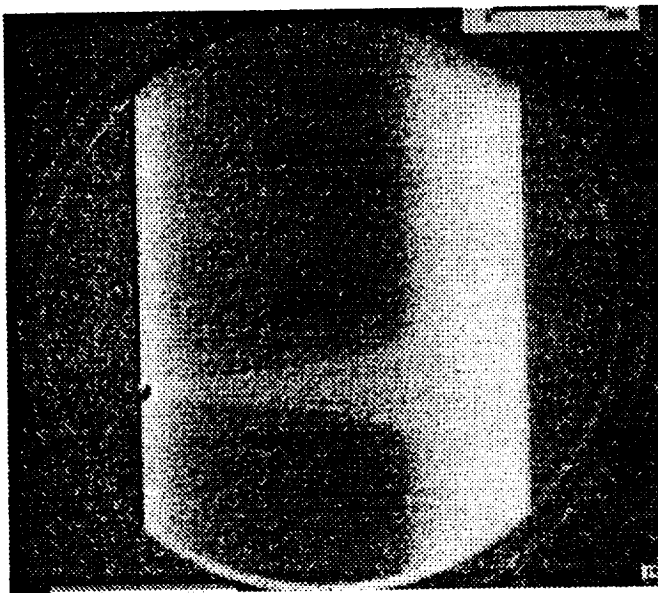


Figure 1.3.  $[\text{Ru}(\text{trpy})_2]^{2+}$  in GP-197 binder in NAL's cryogenic wind tunnel.

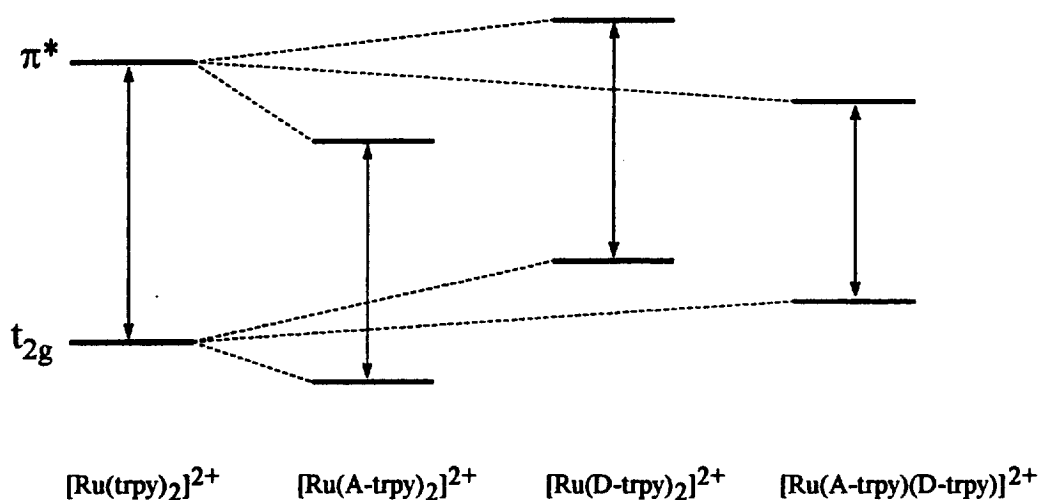


## Discussion

### Photophysics

The photophysical data reported here for this series of  $[\text{Ru}(\text{X-trpy})(\text{Y-trpy})]^{2+}$  complexes agrees with the literature data and these compounds follow the same trends.<sup>19</sup> The compounds all show a decrease in emission energy, relative to  $[\text{Ru}(\text{trpy})_2]^{2+}$ , regardless of the 4' substituent and an increase in room temperature excited state lifetime when the 4' substituent is strongly electron withdrawing.

The photophysical trends are explained by examining the effects the substituents have on the  $\pi^*$  orbital of the trpy ligand and on the lower energy  $t_{2g}$  orbitals of the metal center. The two types of functionalities placed on the trpy ligands are electron withdrawing (referred to as A) and electron donating (referred to as D). The  $\pi^*$  and  $t_{2g}$  orbitals are important because the absorption responsible for emission is metal-to-ligand charge transfer (MLCT) in origin. The MLCT takes a  $t_{2g}$  electron and places it in the ligand  $\pi^*$  orbital, thus, they are the two most important orbitals used in predicting changes in electronic structure. Scheme 1.9 shows an energy level diagram showing the  $\pi^*$  and  $t_{2g}$  orbitals for a generic bis-trpy ruthenium compound.



Scheme 1.9. Schematic of energy levels and the changes due to the presence of functional groups on the terpyridine ligands. This scheme is adapted from ref. 19.

As far as electron withdrawing groups are concerned, they will stabilize the ligand LUMO more than the metal orbitals simply because the metal is further away. Further, in the excited state, the electron withdrawing group can help to stabilize the anionic ligand, while the now Ru(III) metal center becomes more Lewis acidic. It receives no stabilization from the functional group in the excited state. The net result is a slight lowering of the energy gap between the LUMO and the metal orbitals.

Electron donating groups work in very much the opposite direction. In the ground state an electron donating group will place more electron density on the chelating nitrogen atoms, thus destabilizing the ligand LUMO. More importantly, the metal  $t_{2g}$  orbitals are destabilized more in the excited state by the donor group not directly involved in the MLCT. The donor group not involved in the transition places excess electron density on the metal center. Again, the net result is a slight lowering of the energy gap between the two orbitals.

When it comes to making a heteroleptic complex with both an electron withdrawing group and an electron donating group, both of the functional groups do what they do best. That is to say that the withdrawing group helps to stabilize the LUMO (and the anionic ligand in the excited state) and the donor group destabilizes the metal orbital, except in the excited state where it soothes the Ru(III) center. The net result for a heteroleptic complex is a lowering of the energy gap between the  $t_{2g}$  and  $\pi^*$  orbitals. Only this time the difference is more dramatic.

This discussion focuses on the energy levels involved in the MLCT only, since they are directly responsible for absorption and emission. There is a d-d transition that lies close in energy to the MLCT, which competes as a non-radiative pathway for relaxation. Even though the sharp temperature dependence has been attributed to this energy gap, it has been shown to be much less of a factor when not in the solution state.<sup>32</sup> Therefore, the effect on the d-d by donors and acceptors has been ignored.

### Sensor Effectiveness

From the data shown in Figure 1.3, it is fairly clear that the addition of donor groups increases the response to temperature much better than acceptor groups. The drawback is that with the addition of donor groups comes a decrease in intensity. Regardless, luminescent molecular sensors are very effective on wind tunnel models, and have been used, for the first time, to effectively visualize shockwaves at cryogenic temperatures. The application of these paints will make the testing of wind tunnel models much easier and will reduce the cost tremendously.

There are some bugs still to be worked out, however. First, these paints, especially the substituted terpyridine complexes, need to be brighter. It seems that for all the increase in slope that can be gained, the intensity falls off in some proportion. In order to make the detecting and analyzing easier and more precise, the intensity needs to be improved. It would be nice to use the much brighter tris-phen based sensors, but they have only a fraction of the temperature response as the trpy derivatives.

And secondly, there needs to be some more work done as to the best binder/complex/application method combination. These complex interactions can make or break a sensors effectiveness, and have proven quite the troublesome beast, especially in the PSP area.

### Conclusion

Through the use of rational design and understanding of the photophysics of a series of ruthenium(II) bis-terpyridine complexes, a set of luminescent molecular sensors have been developed and used to visualize a shock wave at cryogenic temperatures. Once this technology becomes more refined, it is hoped that it can be expanded to warmer temperatures and then used in other fields outside the world of aerodynamics.

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## CHAPTER 2

### PERIPHERAL METHYL GROUPS: A LOCK ON THE FLATTENING DISTORTION

#### Introduction

Since the discovery of luminescence from  $[\text{Cu}(\text{dmp})_2]^+$  in methylene chloride solution,<sup>1</sup> where dmp represents 2,9-dimethyl-1,10-phenanthroline, a lot of research has been focused on the photophysics of copper phenanthrolines. Specifically, studies have shown that both aryl and alkyl substituents in the 2 and 9 positions of the phenanthroline ligand have a dramatic effect upon the photophysics and photochemistry of the corresponding copper complexes.<sup>2, 4, 5</sup> One reason is that these substituents limit the extent of the  $D_2$  flattening distortion that occurs in the oxidized form of the complex.<sup>1, 2</sup> In addition, these substituents inhibit the addition of a fifth ligand that tends to occur when the excited state is created in donor media.<sup>3-5</sup>

Quenching of excited states has been studied for many years. The data obtained from quenching experiments help to understand both the energies of the excited state<sup>6</sup> and its reactivity.<sup>7</sup> McMillin and co-workers have investigated the quenching processes of copper phenanthrolines and they have proposed a model<sup>2</sup> in which the pseudo-tetrahedral bis-phenanthroline complex first absorbs light, then releases this excess energy by twisting (or flattening). They have also shown that deactivation is further facilitated by the presence of Lewis base quenchers such as  $\text{CH}_3\text{CN}$ , THF, and DMF.<sup>8</sup>

The Lewis bases facilitate the quenching by forming an excited state complex (exciplex) with the metal compound.<sup>8, 9</sup> Exciplex quenching has been known for years in organic chemistry,<sup>9, 10</sup> but is much more rare in inorganic chemistry.<sup>11</sup> The main reason is that much of inorganic photochemistry is dominated by systems like  $[\text{Ru}(\text{bipy})_3]^{2+}$ , which are coordinatively saturated and do not have enough physical space to add another

ligand to the metal center. The case is quite the opposite for Cu(I) bis-phenanthrolines, since their excited states involve the creation of a formal copper(II) center that is four coordinate. Since Cu(II) is Jahn-Teller active, if the flattening distortion is large enough, a fifth ligand can enter the coordination sphere around the copper center. This new five coordinate complex is the exciplex. Formation of the exciplex (or addition of a fifth ligand) is favored due to the stabilization of the more Lewis acidic Cu(II) metal center with more electron density from a fifth ligand. The exciplex then dissipates the excited state energy in returning to the ground state and thus has deactivated the excited state. Although the flattening occurs without a Lewis base present, the Cu(II)...Lewis base interaction is necessary for exciplex formation. Unfortunately, the exciplex only exists for the briefest amount of time and has yet to be observed directly.

Sakaki and coworkers have shown,<sup>12</sup> via ab initio calculations, that the preferred geometry for a copper(I) phenanthroline bis phosphine complex is pseudo-tetrahedral (by ca. 16.5 kcal/mol). Their computations predict a metal-to-ligand charge transfer absorbance low in energy that gives rise to a more Lewis acidic metal center. The computational data also predict that the excited state is not nearly as discerning in its structure. The difference between a pseudo-tetrahedral structure and a nearly planar one is only ca. 4.1 kcal/mol. When they factor in coordination by a water molecule, the nearly planar (now 5 coordinate) geometry is favored by ca. 19.2 kcal/mol over a trigonal bipyramidal structure. This data supports the previous hypothesis that it is not the excited state energy but rather the attack by a Lewis base that drives exciplex quenching. This data also agrees well with the models proposed by McMillin et al<sup>2, 8</sup> and also the fact that the sterics of the ligands and the strength of the base dictate the rate of quenching.

By increasing the steric bulk at the 2 and 9 positions on the phenanthroline backbone, the rate of attack by the Lewis base slows which allows the excited state to exist longer.<sup>1, 5, 8, 13, 14</sup> The increase in excited state lifetime suggests that the formation of the exciplex is less favored energetically. This type of response is intuitive if the structure of the exciplex is considered.<sup>1, 5, 8, 13, 14</sup> Since its structure will be trigonal



bipyramidal in nature, if the phenanthroline ligands cannot approach one another due to steric interactions, the approach and/or docking of the base will be blocked and the exciplex will not form.<sup>1, 5, 8, 13, 14</sup>

To date, many systems have been developed, using substituents such as methyl,<sup>1, 5, 8, 13, 14</sup> *n*-octyl,<sup>13</sup> *sec*-butyl,<sup>15</sup> *iso*-propyl,<sup>16</sup> *neo*-pentyl,<sup>13, 17</sup> and phenyl.<sup>3, 5, 14</sup> All of these systems have focused on steric bulk at the 2 and 9 positions and what effect it has on the photophysics. In this study, the addition of methyl groups at positions 3, 4, 7 and 8 has been investigated. These new ligands also have *n*-butyl or phenyl groups at the 2 and 9 positions. The effects of the methyl groups will be discussed with regard to absorption energies and excited state structure and reactivity.

## Experimental

### Materials

Acetonitrile, N,N'-dimethylformamide, methylene chloride, and tetrahydrofuran were obtained as Burdick and Jackson high-purity distilled in glass-grade chemicals from Scientific Products. The laser dye Coumarin 440 came from Laser Science, while Aldrich Chemical Co. supplied the 1,10-phenanthroline (phen), 2,9-dimethyl-1,10-phenanthroline (2,9-dmp), 3,4,7,8-tetramethyl-1,10-phenanthroline (tmp), 2,9-diphenyl-1,10-phenanthroline (dpp), CuCl<sub>2</sub>·2H<sub>2</sub>O, KPF<sub>6</sub>, 2.0 M *n*-butyl lithium in hexanes, and 2.0 M phenyl lithium in diethyl ether. G. F. Smith provided the 4,7-dimethyl-1,10-phenanthroline (4,7-dmp). The ligands 2,9-di(*n*-butyl)-1,10-phenanthroline (dbp), 2,9-di(*n*-butyl)-4,7-dimethyl-1,10-phenanthroline (dbdmp), 2,9-di(*n*-butyl)-3,4,7,8-tetramethyl-1,10-phenanthroline (dbtmp), 2,9-diphenyl-4,7-dimethyl-1,10-phenanthroline (dpdmp), 2,9-diphenyl-3,4,7,8-tetramethyl-1,10-phenanthroline (dptmp) were all prepared by modifications of the procedure of Pallenberg et al.<sup>15</sup> Copper complexes were prepared by literature methods.<sup>18</sup> 2,9-diphenyl-3,4,7,8-tetramethyl-phenanthroline (dptmp), [Cu(dbp)<sub>2</sub>]PF<sub>6</sub>, and [Cu(dpp)<sub>2</sub>]PF<sub>6</sub> were available from a previous study.<sup>16</sup>

### Methods

For luminescence, lifetime, and quenching studies, solutions were degassed using a series of freeze-pump-thaw cycles. A 525 nm long pass filter was used to keep stray light from the photomultiplier tube, while a 450 nm notch filter was used to filter stray light from the 440 nm excitation beam. The lifetime decays were analyzed with a user-written program. In all cases, the residual plots justified the use of a single exponential.

Quenching data was analyzed using a Stern-Volmer relationship<sup>19</sup> between the quencher concentration and the lifetime, as shown below:

$$1/\tau = 1/\tau_0 + k_q[Q]$$

where  $\tau_0$  is the lifetime of the complex in the absence of quencher, or in this case, pure  $\text{CH}_2\text{Cl}_2$  and  $[Q]$  is the concentration of the quencher, DMF in this case. Linear regression of the data yielded the second order quenching constant  $k_q$ . The data was also analyzed using the integrated emission intensity with the following relationship:

$$I_0/I = \tau_0 k_q [Q] + b$$

Here, again,  $\tau_0$  is the lifetime in the absence of quencher,  $[Q]$  is the concentration of quencher,  $I_0$  is the emission intensity in the absence of quencher, and  $b$  is taken to be 1. Linear regression of the data yielded the second order quenching constant  $k_q$ .

In both cases, the quencher concentration varied from 0 to 1 M, while the copper complex concentration remained constant. Linear regression was done on two sets of the same data. The first set spanned the range 0 to 1 M DMF, while the second only covered 0 to 0.1 M DMF.

$\text{p}K_a$  values were taken from references 20a, 20b, and 20c. Following the discussion in reference 20d, values for the new phenanthrolines were extrapolated. Butyl groups were considered to have the same effect as a methyl or ethyl group, based on data in references 20a, 20b, and 20d.

### Instrumentation

Absorption and emission spectra were recorded on Perkin-Elmer Lambda 4C and SLM SPF 500C spectrometers, respectively. A description of the lifetime apparatus is in the literature.<sup>7</sup> Microanalyses were performed by H. Daniel Lee at the Purdue University Microanalysis Laboratory.

### Computational Methodology

All computations were performed using HyperChem software, version 5.1 Pro, from HyperCube Inc., running on a Pentium II 166 MHz personal computer. The ligands were constructed using idealized bond distances and angles. This idealized geometry was used and no attempts were made to minimize the geometry of the ligand structure. Both molecular mechanics and semi-empirical computations were performed using the standard parameter sets included with the software.

For the molecular mechanics computations, ligand models were constructed using ethyl groups instead of butyl to isolate the rotation contribution to the  $\beta$  carbon. Also, only one "active" substituent was used, the remaining substituent was a methyl group. For example, to model the dbtmp ligand, computations were performed on 2-ethyl-3,4,7,8,9-pentamethyl-1,10-phenanthroline. Along a similar vein, to model the dptmp ligand, 2-phenyl-3,4,7,8,9-pentamethyl-1,10-phenanthroline was used. Only one "active" substituent was used to isolate the contribution of only one group and to minimize the number of conformations. The actual computations were single point calculations based on the idealized geometry, after adjusting the torsion angle between the nitrogen atom and the substituent of interest. Single point calculations were performed every 10 degrees.

For the semi-empirical computations, all butyl groups were replaced with methyl groups to minimize any conformational effects caused by the butyl chain. For example, the data reported for the dbp ligand was calculated using 2,9-dimethyl-1,10-phenanthroline as a model. Data for the phenyl derivatives was calculated with the

phenyl rings having the same torsion angle. Calculations were performed at torsion angles of 0, 30, 45, 52, 60, and 90 degrees. An average of the values is reported as the data. The crystal structure of dpp shows a torsion angle of 0 degrees, while crystal structures of copper(I) complexes with dpp show an average torsion angle of approximately 52 degrees.

### Preparations

2,9-di(*n*-butyl)-4,7-dimethyl-1,10-phenanthroline (dbdmp) [V-3]. This ligand was prepared by following the procedure of Pallenberg et al<sup>15</sup> using a 2.0 M *n*-butyl lithium solution in ether and 4,7-dimethyl-1,10-phenanthroline as starting materials. The product was purified on alumina and eluting with methylene chloride, collecting the first, faster moving fraction. The pale yellow material was recrystallized from ethanol to yield a white solid. <sup>1</sup>H NMR in CDCl<sub>3</sub> (in ppm): 7.92 (s, 2H), 7.34 (s, 2H), 3.19 (quartet, 4H), 2.74 (s, 6H), 1.88 (pentet, 4H), 1.51 (sextet, 4H), 1.00 (t, 6H).

2,9-di(*n*-butyl)-3,4,7,8-tetramethyl-1,10-phenanthroline (dbtmp) [IV-67]. This ligand was prepared as above<sup>15</sup> using a 2.0 M *n*-butyl lithium solution in ether and 3,4,7,8-tetramethyl-1,10-phenanthroline as starting materials and purified in the same fashion. The final product was a white solid. <sup>1</sup>H NMR in CDCl<sub>3</sub> (in ppm): 7.92 (s, 2H), 3.18 (quartet, 4H), 2.67 (s, 6H), 2.50 (s, 6H), 1.90 (pentet, 4H), 1.55 (sextet, 4H), 1.07 (t, 6H).

2,9-diphenyl-4,7-dimethyl-1,10-phenanthroline (dpdmp) [V-5]. This ligand was prepared as above<sup>15</sup> using a 1.6 M phenyl lithium solution in hexanes and 4,7-dimethyl-1,10-phenanthroline as starting materials and purified in the same manner. The final product was a pale yellow solid. <sup>1</sup>H NMR in CDCl<sub>3</sub> (in ppm): 8.49 (s, 4H), 8.00 (m, 4H), 7.55 (m, 6H), 2.85 (s, 6H).

$[\text{Cu}(\text{dbdmp})_2]\text{PF}_6$  [V-55]. This compound was prepared by previous methods.<sup>18</sup> The orange material was recrystallized from water and ethanol to yield orange crystals. Calculated:(based on the hemihydrate  $[\text{Cu}(\text{dbdmp})_2]\text{PF}_6 \cdot \frac{1}{2}\text{H}_2\text{O}$ ) 61.56% C, 6.58% H, 6.53% N. Found: 61.52% C, 6.55% H, 6.46% N. The presence of water was confirmed by proton NMR spectroscopy in  $\text{CDCl}_3$ .

$[\text{Cu}(\text{dbtmp})_2]\text{PF}_6$  [IV-111, IV-187]. This compound was prepared by previous methods.<sup>18</sup> The orange material was recrystallized from water and ethanol to yield orange brown crystals. Calculated: 63.67% C, 7.12% H, 6.19% N. Found: 63.60% C, 6.81% H, 6.17% N.

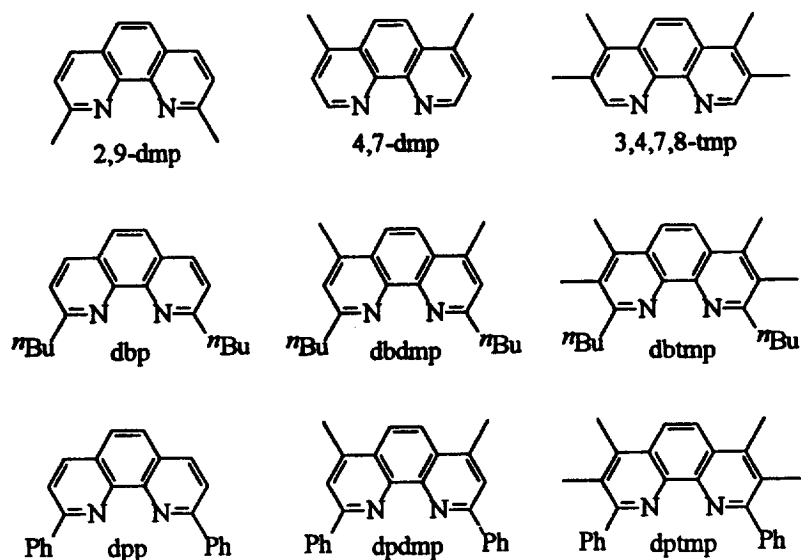
$[\text{Cu}(\text{dpdmp})_2]\text{PF}_6$  [V-57]. This compound was prepared by previous methods.<sup>18</sup> The wine red material was recrystallized from water and acetone to yield dark red crystals. Calculated:(based on the acetone monosolvate ) 63.25% C, 4.08% H, 5.67% N. Found: 63.01% C, 4.15% H, 5.48% N. The presence of acetone was confirmed by proton NMR spectroscopy in  $\text{CDCl}_3$ .

$[\text{Cu}(\text{dptmp})_2]\text{PF}_6$  [IV-188]. This compound was prepared by literature methods<sup>18</sup> and recrystallized from water and ethanol to yield red needles. Calculated:(based on the hemihydrate  $[\text{Cu}(\text{dptmp})_2]\text{PF}_6 \cdot \frac{1}{2}\text{H}_2\text{O}$ ) 67.63% C, 4.97% H, 5.63% N. Found: 67.37% C, 4.74% H, 5.63% N. The presence of water was confirmed by proton NMR spectroscopy in  $\text{CDCl}_3$ .

## Results

### Synthesis

A schematic diagram showing the ligands of interest is shown in Scheme 2.1. All of the ligands, except for 2,9-dmp, that have substituents in the 2 and 9 positions, were synthesized by addition of organolithium reagents to the parent phenanthroline backbone. The method of Pallenberg et al<sup>15</sup> was employed and worked very nicely for the synthesis of the substituted phenanthroline ligands.



Scheme 2.1. The ligands and abbreviations used in this study.

### Absorption Data

Table 2.1 shows all of the absorption data for both the butyl and phenyl derivatives as well as for the complexes with the parent phenanthroline backbones. None of the complexes show any appreciable solvatochromism in their absorption maxima.

Inspection of the absorption data suggests that the compounds can be divided into three groups. The first group is made of compounds with no substituents in the 2,9 positions. The second group has alkyl substituents in the 2,9 positions and the third group has aryl substituents in the 2,9 positions. These groups will be referred to as the parent group, the alkyl group, and the aryl group, respectively. The differentiation between the parent group and the alkyl group is necessary as substitution in the 2,9 positions of a phenanthroline drastically change its properties.<sup>22</sup>

Table 2.1. Absorption data for  $[\text{Cu}(\text{NN})_2]\text{PF}_6$  complexes.

| Ligand  | $\lambda_{\text{max}}$ (nm), $\text{CH}_2\text{Cl}_2$ | $\epsilon$ ( $\text{M}^{-1}\text{cm}^{-1}$ ) | $\lambda_{\text{max}}$ (nm), THF | $\lambda_{\text{max}}$ (nm), $\text{CH}_3\text{CN}$ |
|---------|-------------------------------------------------------|----------------------------------------------|----------------------------------|-----------------------------------------------------|
| phen    | 440                                                   | 7000 <sup>21</sup>                           | 441                              | 442                                                 |
| 4,7-dmp | 434                                                   |                                              | 435                              | 435                                                 |
| tmp     | 430                                                   |                                              | 430                              | 431                                                 |
| 2,9-dmp | 454                                                   | 7800 <sup>13</sup>                           | 456                              | 457                                                 |
| dbp     | 457                                                   | 7000 <sup>13</sup>                           | 457                              | 457                                                 |
| dbdmp   | 456                                                   | 9900                                         | 456                              | 457                                                 |
| dbtmp   | 453                                                   | 9300                                         | 452                              | 452                                                 |
| dpp     | 440, 560                                              | 3200 <sup>5</sup>                            | 440, 560                         | 440, 560                                            |
| dpdmp   | 440, 550                                              | 3800                                         | 440, 550                         | 441, 560                                            |
| dptmp   | 467                                                   | 6000                                         | 467                              | 467                                                 |

The absorption maxima, for the parent and alkyl groups, correlate well with the  $\text{pK}_\text{a}$  values for the ligands and also the calculated LUMO energies. This data is shown in Table 2.2 and Figure 2.1. This result is not surprising since the absorbance corresponds to placing an electron into a  $\pi^*$  orbital of the ligand, whose energy will be directly affected by the presence of electron donating functionalities. Therefore, the presence of additional electron donating methyl substituents on the ligand should make this process more difficult. The methyl groups also place more electron density on the nitrogen atoms in the free ligand, making them stronger bases.

The correlation of the parent and alkyl data indicates that within a group, the ground state structure, which is responsible for the absorbance energy, is not changing with addition of the peripheral methyl groups. This was not the case in the paper by Eggleston et al<sup>13</sup> in which the change in absorbance maxima was attributed to the changing steric bulk of the alkyl substituents in the 2,9 positions. The switching of substituents was causing a change in the ground state structure, as reflected in the absorption spectra. For the alkyl and parent groups, they should have a similar structure since they are substituted the same, within their respective series, at the 2,9 positions.

Table 2.2. Calculated orbital energies and pK<sub>a</sub> values.

| Ligand             | pK <sub>a</sub>    | EH LUMO <sup>d</sup> | PM3 LUMO <sup>d</sup> | EH SLUMO <sup>d</sup> | PM3 SLUMO <sup>d</sup> |
|--------------------|--------------------|----------------------|-----------------------|-----------------------|------------------------|
| phen               | 4.88 <sup>b</sup>  | -9.726260            | -1.043975             | -9.574359             | -0.728441              |
| 4,7-dmp            | 5.95 <sup>b</sup>  | -9.613302            | -0.998210             | -9.499872             | -0.656965              |
| tmp                | 6.48 <sup>b</sup>  | -9.576261            | -0.929885             | -9.479396             | -0.601576              |
| dbp <sup>a</sup>   | ~6.15 <sup>c</sup> | -9.680675            | -0.963496             | -9.456161             | -0.652240              |
| dbdmp <sup>a</sup> | ~6.81 <sup>c</sup> | -9.568657            | -0.920969             | -9.379386             | -0.583770              |
| dbtmp <sup>a</sup> | ~7.37 <sup>c</sup> | -9.525309            | -0.857133             | -9.380155             | -0.525717              |
| dpp <sup>e</sup>   | ~5.00 <sup>f</sup> | -12.0104             | -8.679496             |                       |                        |
| dpdmp <sup>e</sup> | ~6.1 <sup>g</sup>  | -11.8961             | -8.574135             |                       |                        |
| dptmp <sup>e</sup> | ~6.6 <sup>g</sup>  | -11.8409             | -8.523982             |                       |                        |

a calculations were performed on the methyl derivatives.

b pK<sub>a</sub> values were taken from ref. 20a, 20b, 20c.

c data from ref. 20a, 20b, & 20c and estimations from discussions in ref. 20d

d energies in eV

e single point calculations were performed with the torsion angle between the phenyl group and the phenanthroline at 0, 30, 45, 52, 60 and 90 degrees and the reported data reflects an average value

f the pK<sub>a</sub> is for 2,9-di(*p*-anisoyl)-1,10-phenanthroline, as reported in ref. 23

g data from ref. 23 and estimations from discussions in ref. 20d



Chart A

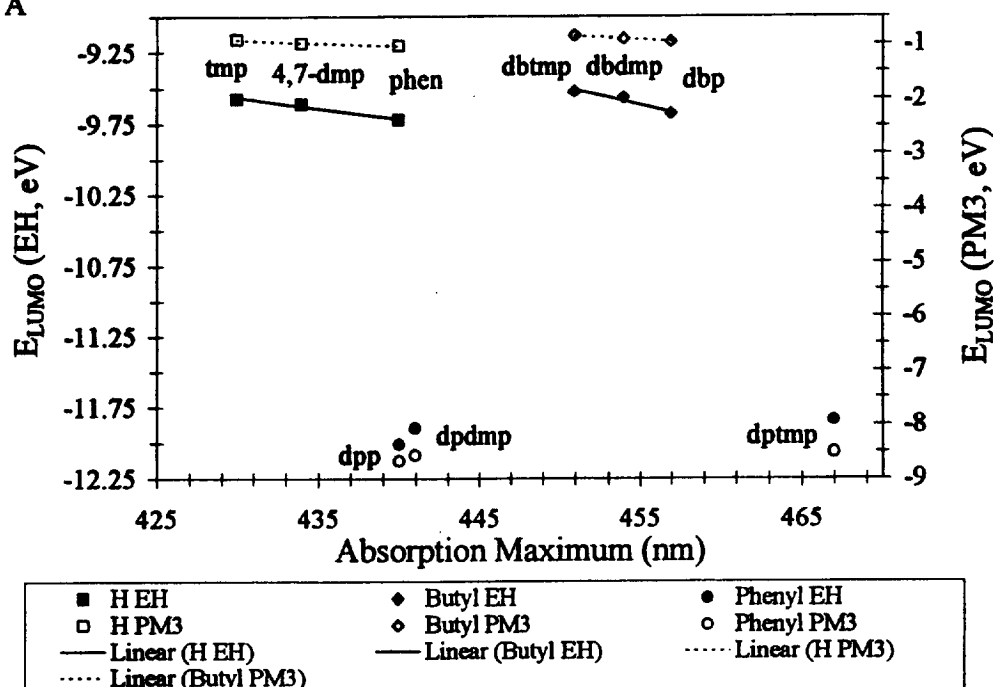


Chart B

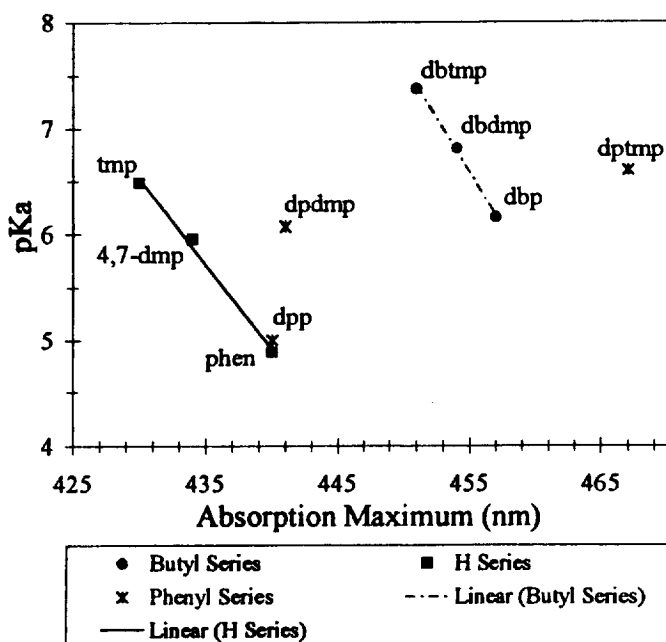


Figure 2.1. Correlation of the absorption of the copper complex with properties of the free ligand. Chart A is the correlation of the calculated orbital energies of the free ligand and the absorption maxima of the copper complexes. Chart B is the correlation of the free ligand  $pK_a$  and the absorption maxima of the copper complex.

Also shown in Table 2.2 and Figure 2.1 is the corresponding data for the aryl group. It is clear that this group does not correlate as well. The data for the dptmp complex does not seem to conform to the same trends when compared to the dpp and dpdmp complexes.

The dpp and dpdmp complexes show small changes in their  $pK_a$  and calculated LUMO energies compared to the changes with the corresponding butyl derivatives. Consequently, there is no apparent change in the absorption maximum to accompany the change in  $pK_a$  and LUMO energy. This is very different behavior compared to the parent and alkyl groups and most likely reflects a considerably different ground state structure.

As for the dptmp complex, it stands out from the other phenyl compounds as it has no low energy shoulder present in the absorption spectrum. In fact, the absorption spectrum of the dptmp complex resembles that of an alkyl-substituted phenanthroline more than it does and aryl-substituted phenanthroline, see Figure 2.2. Again this is indicative of a change in the ground state structure. In this case, the change is quite dramatic and seems to indicate a change back from an aryl-like to an alkyl-like structure.

A similar result was observed by McMillin et al using a derivative of phenanthroline containing 1-naphthyl groups in the 2 and 9 positions.<sup>14</sup> The steric bulk of the naphthyl groups keeps it from being in conjugation with the phenanthroline backbone. This lack of  $\pi$ -conjugation may also be occurring with the dptmp derivative since the 3,8 methyl groups should keep the phenyl ring approximately perpendicular to the phenanthroline backbone. A perpendicular phenyl ring will not conjugate in the  $\pi$  sense and thus is merely a  $\sigma$  donor.<sup>21</sup> However, a perpendicular phenyl ring will be able to stack, or interact, with the opposite phenanthroline backbone that it extends over.<sup>23</sup> This type of stacking may be responsible for the bathochromic shift observed in the absorption maxima relative to alkyl substituents.

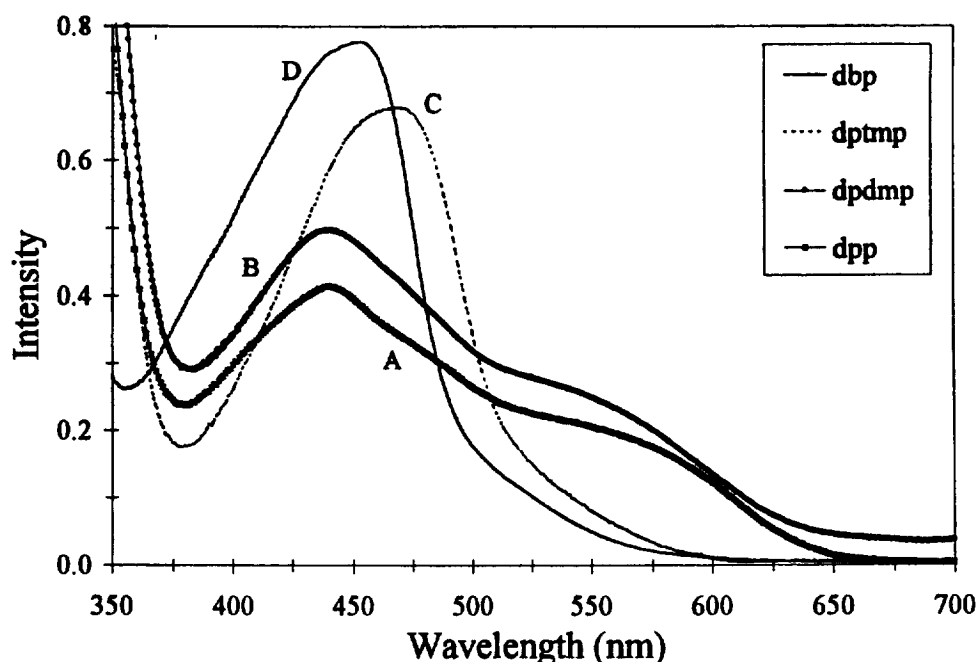


Figure 2.2. Absorption spectra for  $[\text{Cu}(\text{NN})_2]\text{PF}_6$  in  $\text{CH}_2\text{Cl}_2$ . Line A)  $\text{NN} = \text{dpp}$ , B)  $\text{NN} = \text{dpdmp}$ , C)  $\text{NN} = \text{dptmp}$ , D)  $\text{NN} = \text{dbp}$ .

#### Luminescence Data

Table 2.3 shows all of the luminescence data for both the butyl and phenyl derivatives. None of the complexes containing the parent phenanthroline backbones shows any emission in solution. All of the remaining complexes exhibit a bathochromic shift in their emission maxima with increasing polarity of the solvent.

For example, the dbp complex shifts from 670 nm to 685 nm to 690 nm as the solvent changes from  $\text{CH}_2\text{Cl}_2$  to THF to  $\text{CH}_3\text{CN}$ . The presence of aryl substituents also lowers the emission energy, relative to alkyl substituents. On the other hand, for both series of complexes, the addition of 3,8 methyl groups causes a hypsochromic shift in the emission energy, whereas 4,7 methyl groups have little effect.

The lifetimes for all of the compounds listed in Table 2.3 increase with addition of the 3,8 methyl groups. In the butyl series, the non-methylated complex has a lifetime in  $\text{CH}_2\text{Cl}_2$  of 136 ns, while the dbtmp complex has a lifetime of 330 ns. Addition of methyl groups in the 4 and 7 positions, again, has little effect. The lifetime data also

shows that the 3,8 methylated ligands add a resistance to exciplex quenching. For instance, the dbp complex has a lifetime of 136 ns in  $\text{CH}_2\text{Cl}_2$  while the lifetime is less than 10 ns in  $\text{CH}_3\text{CN}$ . The dbtmp complex has a lifetime of 330 ns in  $\text{CH}_2\text{Cl}_2$  and a lifetime of 320 ns in  $\text{CH}_3\text{CN}$ . This is the first copper phenanthroline that has shown a definite resistance to quenching by donor solvents. The dptmp complex has the longest-lived excited state in methylene chloride, but still shows considerable quenching by acetonitrile.

The quantum yield for emission follows a similar trend as the lifetimes and emission maxima; a small increase with addition of the 4,7 methyl groups and a significant increase with addition of the 3,8 methyl groups, for both series. A comparison of quantum yields in the different solvents also shows a dramatic loss of intensity for the non- and di-methylated ligand complexes, whereas the tetra-methylated ligand complexes show a resiliency to addition of a fifth ligand.

Table 2.3. Luminescence data for  $[\text{Cu}(\text{NN})_2]\text{PF}_6$  complexes.<sup>a</sup>

| Ligand  | $\text{CH}_2\text{Cl}_2$                                           | THF                                                                | $\text{CH}_3\text{CN}$                                             |
|---------|--------------------------------------------------------------------|--------------------------------------------------------------------|--------------------------------------------------------------------|
|         | Em $\lambda_{\text{max}}^b$ , [ $\tau^c$ ], ( $10^4 \times \phi$ ) | Em $\lambda_{\text{max}}^b$ , [ $\tau^c$ ], ( $10^4 \times \phi$ ) | Em $\lambda_{\text{max}}^b$ , [ $\tau^c$ ], ( $10^4 \times \phi$ ) |
| 2,9-dmp | 690, [90], (4)                                                     | ~700                                                               | ~700                                                               |
| dbp     | 670, [140], (9)                                                    | 685, [45], (3)                                                     | 690, [25], (1)                                                     |
| dbdmp   | 670, [145], (15)                                                   | 685, [105], (7)                                                    | 690, [45], (4)                                                     |
| dbtmp   | 635, [330], (125)                                                  | 640, [330], (124)                                                  | 650, [320], (44)                                                   |
| dpp     | 685, [270], (10)                                                   | 710, [190], (4)                                                    | 715, [120], (3)                                                    |
| dpdmp   | 685, [310], (26)                                                   | 700, [155], (13)                                                   | 710, [125], (9)                                                    |
| dptmp   | 670, [480], (57)                                                   | 685, [365], (29)                                                   | 690, [255], (24)                                                   |

a in deoxygenated methylene chloride from uncorrected spectra

b in nanometers

c in nanoseconds

### Lewis Base Quenching

Analysis of the data in Table 2.4 reveals two major trends. First of all, for the non-methylated and 4,7-dimethyl series of compounds, the aryl containing compounds have a smaller quenching rate. For example, the quenching rate of  $[\text{Cu}(\text{dbp})_2]^+$  is  $2.1 \times 10^7 \text{ M}^{-1}\text{s}^{-1}$  whereas  $[\text{Cu}(\text{dpp})_2]^+$  has a quenching constant of  $6.7 \times 10^6 \text{ M}^{-1}\text{s}^{-1}$ . This is no doubt due to the larger steric bulk of the phenyl ring relative to the butyl group.<sup>5</sup> The phenyl ring inhibits the approach of quencher molecules and limits the amount of flattening that can occur.

The second trend conveyed in the quenching data is that addition of the 3,8 methyls retards the quenching rate to a limiting value. For the phenyl series, the rate slows by about a factor of 3, whereas for the butyl series the rate is slowed by almost a full order of magnitude, which gives both  $[\text{Cu}(\text{dbtmp})_2]^+$  and  $[\text{Cu}(\text{dptmp})_2]^+$  a  $k_q$  of  $2 \times 10^6 \text{ M}^{-1}\text{s}^{-1}$ . This means that the 3,8 methyl groups are somehow hindering the attack of Lewis bases and causing the formation of the five coordinate to be much more difficult.

One other interesting observation was the fact that all four of the complexes measured showed some degree of downward curvature in their Stern-Volmer curves, see Figure 2.3 for an example. The data shown in Figure 2.3 is for the transient analysis of the dptmp complex. As the concentration of the DMF increases, the rate constant decreases. This is not a new phenomenon, and most likely stems from the fact that as the DMF concentration increases, the compound is being solvated differently, thus changing the  $\tau_0$  that is used as the Y-intercept. The changing Y-intercept gives the appearance of a non-linear quenching rate. This is a pre-equilibrium association and has been seen in other systems that are sensitive to the solvent.<sup>25</sup>

Table 2.4. Quenching constants,  $k_q$  in  $M^{-1}s^{-1}$ , for DMF in deoxygenated  $CH_2Cl_2$ . The data has been separated into low DMF concentration (up to .1M) and high DMF concentration (up to 1M) to show the variation due to solvent polarity change.

| Ligand | Transient, up to 1M | Transient, up to .1M | Intensity, up to 1 M | Intensity, up to .1 M |
|--------|---------------------|----------------------|----------------------|-----------------------|
| dbp    | $2.1 \cdot 10^7$    | $2.0 \cdot 10^7$     | $3.6 \cdot 10^7$     | $2.4 \cdot 10^7$      |
| dbtmp  | $1.7 \cdot 10^6$    | $2.9 \cdot 10^6$     | $7.0 \cdot 10^6$     | $1.2 \cdot 10^6$      |
| dpp    | $6.7 \cdot 10^6$    | $8.3 \cdot 10^6$     | $7.6 \cdot 10^7$     | $6.1 \cdot 10^6$      |
| dptmp  | $2.1 \cdot 10^6$    | $2.9 \cdot 10^6$     | $1.5 \cdot 10^7$     | $1.8 \cdot 10^6$      |

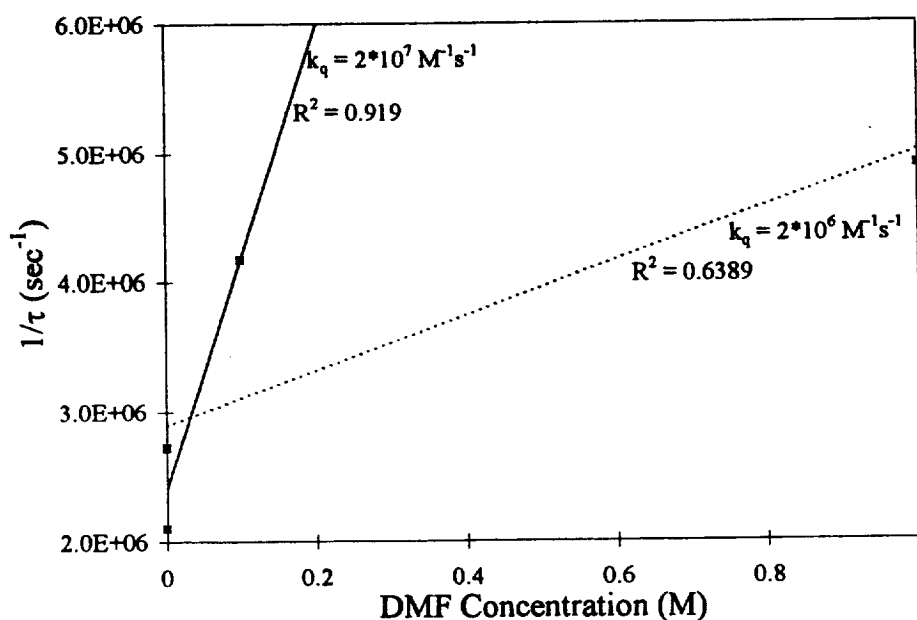


Figure 2.3. Stern-Volmer curve for  $[Cu(dptmp)_2]PF_6$ . The solid line represents the fit of the data up 0.1M DMF while the dotted line is the fit of the data up to 1M DMF.

### Discussion

The addition of the methyl groups in the 3 and 8 positions of the phenanthroline backbone adds some interesting characteristics to the copper compounds. These methyl groups affect the absorption spectra, the emission spectra, and the resistance to exciplex quenching by oxygen or Lewis base solvents. The ability to alter these three phenomena indicates that these methyl groups modify both the ground state and the excited state.

### Absorption Spectra

As mentioned previously, for the alkyl group, the addition of more methyl groups causes an increase in the energy of the charge-transfer absorbance for electronic reasons only. The ground state structure should be very similar within the series.

However, for the aryl series this is not the case. The spectrum of the dptmp complex does not look like other aryl-substituted phenanthroline complexes, indicative of a change in the ground state structure. Most aryl-substituted phenanthroline complexes show a maxima around 440 nm with a broad shoulder extending out past 600 nm. This is the case for dpp, dpdmp, and also agrees with the spectrum of  $[\text{Cu}(\text{tpp})_2]^+$ , where tpp is 2,4,7,9-tetraphenyl-1,10-phenanthroline.<sup>14</sup> With dptmp, the spectrum seems to look more like an alkyl-substituted derivative with one intense absorbance and a very weak shoulder (or tail).

The presence of shoulders on the CT spectra of aryl-substituted complexes has been ascribed to the  $D_2$  flattening distortion that is common to copper phenanthrolines.<sup>24</sup> For the usual aryl derivatives, the exceptionally broad shoulder is a result of the ease of rotation of the phenyl rings which allows for the flattening.<sup>5</sup> One of the main driving forces for flattening would be to increase conjugation between the aryl ring and the phenanthroline moiety it is bonded to.<sup>21</sup>

In the dptmp case this is assumed not to occur since the presence of the peripheral methyl groups should "lock" the geometry in a more rigid  $D_{2d}$  configuration thus limiting the contribution of the flattened geometry. Since the absorbance spectrum of the dptmp complex resembles that of an alkyl complex, where conjugation is not

possible, it should have a similar more  $D_{2d}$ -like structure. The bathochromic shift exhibited by the dptmp complex relative to the alkyl-substituted phenanthroline complexes may be attributed to  $\pi$ - $\pi$  interactions between a phenyl ring and the  $\pi$ -orbitals of the opposite phenanthroline backbone.<sup>23</sup>

Molecular modeling studies on the free phenanthroline ligands reveal that rotation of either the butyl or the phenyl group with a locking methyl group present is very difficult. Figures 2.4 and 2.5 show the total molecular mechanics energy as well as the Van der Waals component for both ligands. The computations were performed on model ligands that contained only one rotating group and used an ethyl group instead of a butyl group. These changes were done in order to isolate the rotational barrier for only one functional group and in the case of the butyl series, minimize conformational effects of the longer chain.

These figures indicate that it is approximately six times more difficult to rotate a butyl (ethyl) group with the 3,8 methyl groups present. Similarly, for the phenyl derivatives, the difference is roughly seven times as large. This data helps to support the idea that the phenyl groups remain perpendicular to the phenanthroline moiety and thus help to keep the geometry of the dptmp complex more  $D_{2d}$  and severely hamper the flattening distortion so common to copper phenanthrolines.



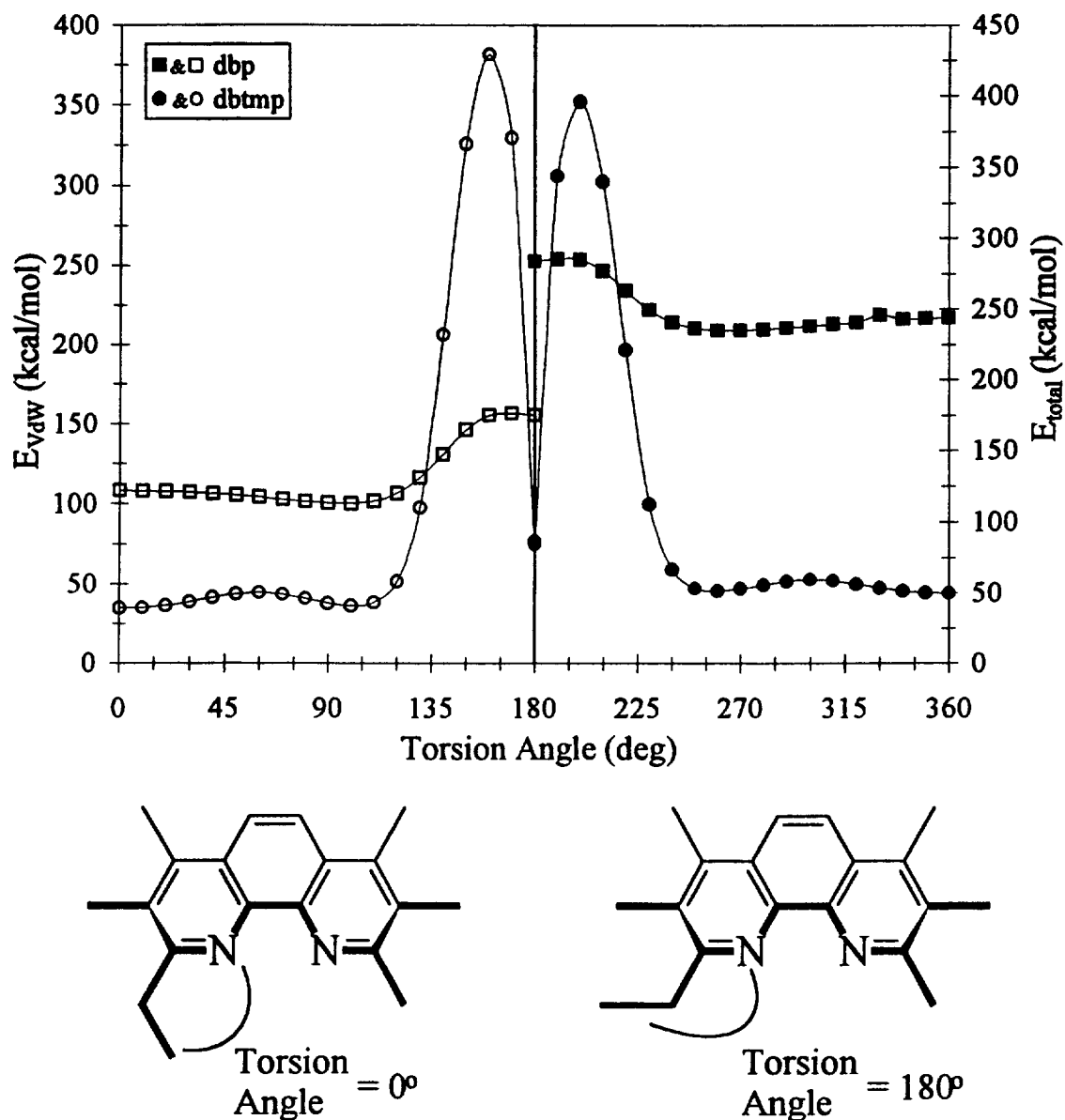


Figure 2.4. Molecular mechanics data for the free ligands dbp and dbtmp. The left side of the graph represents the Van der Waals component of the total energy, while the right side shows the total molecular mechanics energy of the free ligand. Circles are for data on the dbtmp ligand and squares are for data on the dbp ligand. The figures represent the torsion angles of interest at their extremes.

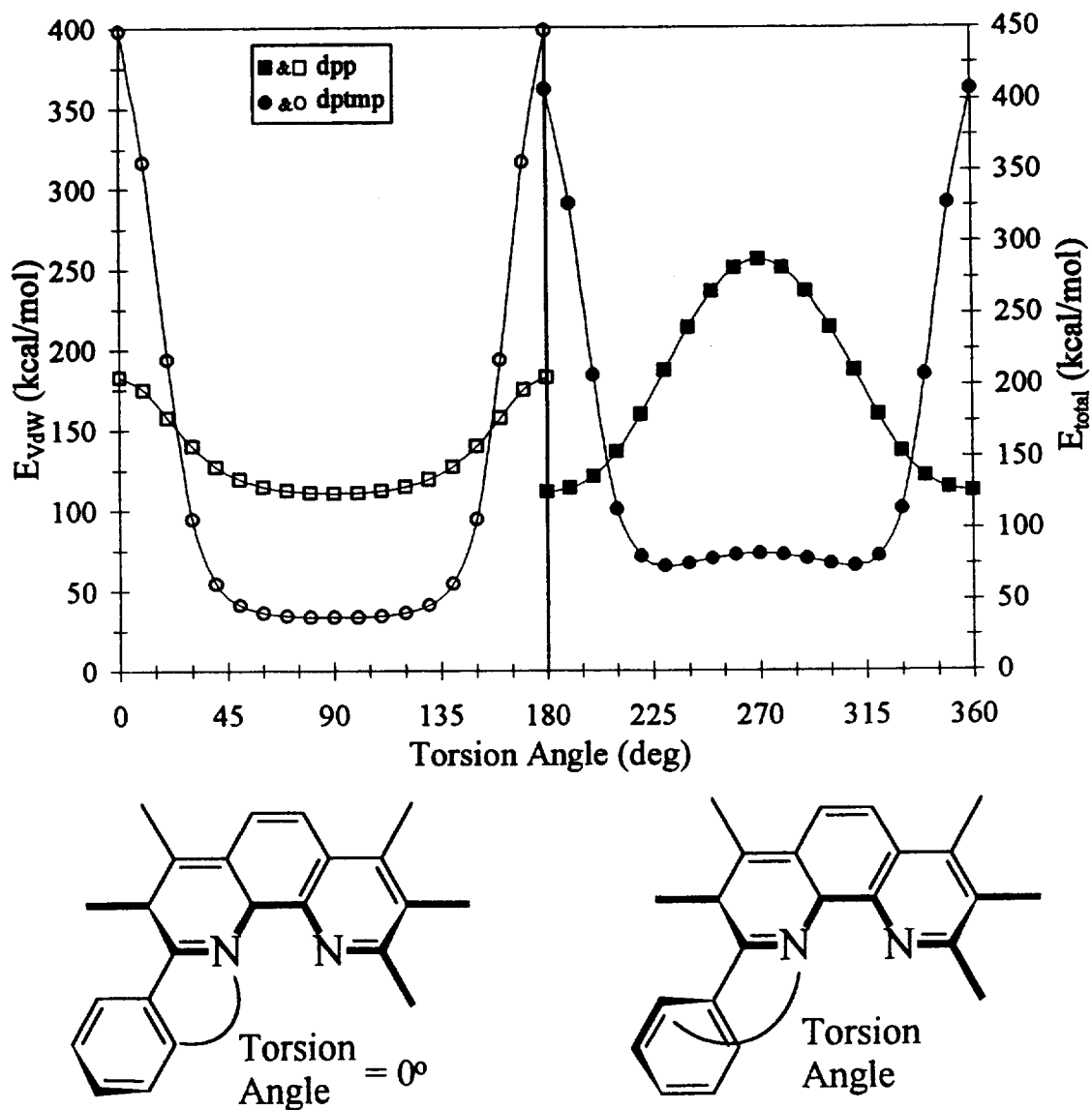


Figure 2.5. Molecular mechanics data for the free ligands dpp and dptmp. The left side of the graph represents the Van der Waals component of the total energy, while the right side shows the total molecular mechanics energy of the free ligand. Circles are for data on the dptmp ligand and squares are for data on the dpp ligand. The figures represent the torsion angles of interest, at their extremes.

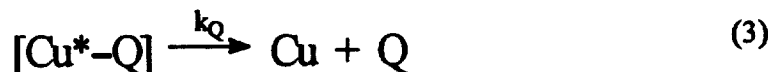
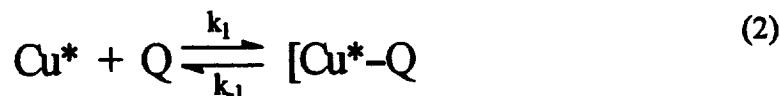
### Luminescence Data

As mentioned above, the addition of the methyl groups in the 3 and 8 positions is expected to rigidify the 2,9 substituents and therefore lock the copper complex into a more tetrahedral-like geometry. What is known about copper(I) phenanthrolines is that upon excitation of the metal electron into the ligand  $\pi^*$ , the now formal copper(II) complex undergoes a twisting or flattening distortion to form a complex that can accept a fifth ligand.<sup>2,8</sup> This distortion is due to the steric flexibility of most phenanthrolines and the Jahn-Teller distortion that Cu(II) is famous for.<sup>2,24</sup> With the tetra-methyl ligand series, the induced rigidity keeps the structure of the excited state close to that of tetrahedral. Since the major deactivation pathway is energy lost due to nuclear motion during the twisting processes, the lack of movement in this case results in a longer lived excited state and higher energy luminescence. The increase in emission energy is due to a larger energy difference between the more tetrahedral and more stable Cu(I) ground state and the more tetrahedral and destabilized Cu(II) excited state.<sup>2,8</sup>

### Quenching Phenomena

Exciplex quenching is a common type of quenching exhibited by copper(I) phenanthrolines and these new compounds are no different. The two tetra-methyl compounds do, however, exhibit a much slower rate of quenching when compared to other copper phenanthrolines.

A minimal kinetic scheme<sup>3,8</sup> is presented in equations 1 through 3, where Cu\* and Cu refer to the excited, emissive metal complex and the ground state metal complex, respectively. Q denotes the Lewis base quencher and [Cu\*-Q] denotes the complex formed between Cu\* and Q. These equations indicate that  $k_q$  is not a simple rate constant but a combination of several rates. In this scheme, all deexcitation processes are assumed to be irreversible.



The complex  $[\text{Cu}^*-\text{Q}]$  is not a simple encounter complex as can be the case,<sup>25</sup> but rather an exciplex that takes energy to dissociate. Since direct spectroscopic observance of the exciplex has yet to occur,<sup>26</sup> the concentration of the exciplex is assumed not to build up.<sup>3, 8</sup> This allows for the assumption of a steady-state concentration of  $[\text{Cu}^*-\text{Q}]$ . With this assumption,  $k_q$  is predicted to be second order, and takes the form of equation 4.

$$k_q = \frac{k_1}{1 + k_{-1}/k_Q} \quad (4)$$

This model predicts that when  $k_{-1}$ , dissociation of the exciplex, competes with  $k_Q$ , quenching of the excited state, the observed rate of quenching will slow. In the cases presented here involving the tetra-methyl derivatives,  $k_{-1}$  is not a factor. In this case it is actually  $k_1$ , the formation of the exciplex that is the rate limiting step. Due to the increased steric repulsions between the bulkier ligands and the quencher, formation of the exciplex is slow and therefore the overall quenching rate is reduced. The addition of the steric locks slows the quenching of the excited state by making it a much less stable species.

### Conclusion

The data presented in this paper show that the geometry of copper(I) phenanthrolines can not only be controlled by the size of the substituents in the 2,9 positions, but also by placing "locks" at the 3,8 positions of the ring. These locks help

to restrict the mobility of the 2,9 substituents which inhibit the flattening distortion usually associated with copper(I) phenanthrolines. This increased rigidity leads to complexes with longer lived excited states with more efficient quantum yields and with less susceptibility towards exciplex quenching. This series of compounds has provided the longest lived copper(I) phenanthroline in methylene chloride solution and also a copper(I) phenanthroline that is resistant to quenching by all except the strongest Lewis bases.

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### CHAPTER 3

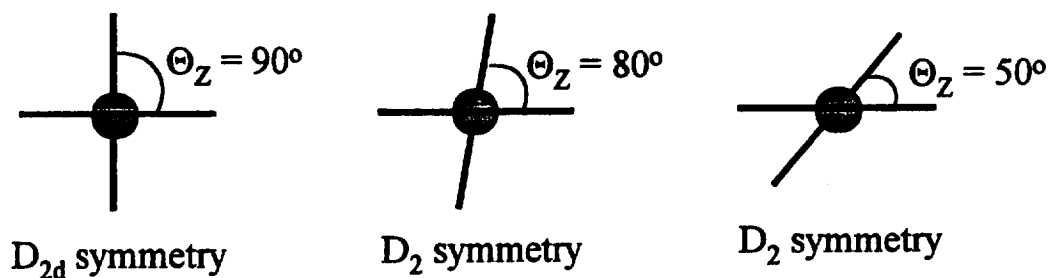
## SOLID STATE STRUCTURE CORRELATIONS IN COPPER(I) PHENANTHROLINES

### Introduction

Crystal structures have long been used to predict the structures of molecules in solution; however, with copper(I) phenanthroline compounds the crystal structure can differ greatly from the solution structure.<sup>1</sup> Copper(I) phenanthrolines are psuedo-tetrahedral molecules with  $D_{2d}$  symmetry in solution. This symmetry is apparent from the solution absorption data and even complexes with rather large substituents on the phenanthroline backbone still conform to this assignment.<sup>2</sup> When these molecules crystallize, however; they no longer keep their neat  $D_{2d}$  symmetry, as evident by the range of absorption maxima from the solid state absorbance data.<sup>1</sup>

In perfect  $D_{2d}$  symmetry, the angle defined by the planes of the two phenanthroline ligands, denoted  $\Theta_z$ , is  $90^\circ$ .<sup>3</sup> Scheme 3.1 shows a schematic representation of the dihedral angle and its effect on structure. In the solid state, most copper(I) phenanthrolines show major departure from the ideal value.  $\Theta_z$ 's have been reported anywhere from  $50^\circ$  to  $\sim 90^\circ$ . The flattening observed in the crystal structures has been attributed to the packing forces of the lattice.<sup>4, 25</sup> This is not unreasonable to assume since Cu(I) is stable with a coordination number of 3,<sup>10</sup> coupled with the fact that the same cation shows different dihedral values with different anions. For example,  $[\text{Cu}(\text{dmp})_2]^+$ , where dmp denotes 2,9-dimethyl-1,10-phenanthroline, has a dihedral angle of  $72.4^\circ$  with  $\text{NO}_3^-$  as the anion<sup>6</sup> and  $88.8^\circ$  when  $\text{TCNQ}^-$  is the anion.<sup>7</sup> In solution, the dihedral angle is assumed to be  $90^\circ$  since there are no outside forces distorting the geometry.<sup>1</sup>





Scheme 3.1. Schematic of  $\Theta_Z$  and its effect on structure and symmetry.

From the limited number of crystal structures published on copper(I) phenanthrolines, it seems that the dihedral angle can be controlled by either changing the anion or by altering the steric bulk of the substituents in the 2 and 9 positions of the phenanthroline ring. For instance, of the 5 crystal structures of  $[\text{Cu}(\text{dmp})_2]^+$ , none of them have the same dihedral angle, presumably due to the differing anions.<sup>3, 5-7</sup> Also, as the steric bulk, in the 2 and 9 positions, changes from H to  $\text{CH}_3$  to *n*-pentyl, the dihedral angle changes by  $40^\circ$ .<sup>3, 8, 9</sup> However, the comparison is somewhat artificial, as these compounds also have different anions.

Correlation of the photophysical properties of copper phenanthrolines with their dihedral angles is another area that has not been fully explored. Kaizu and Shinozaki<sup>1</sup> have previously shown, computationally, that for  $[\text{Cu}(\text{ethanediimine})_2]^+$ , the energy levels of the highest occupied and the lowest unoccupied molecular orbitals are dependant on the dihedral angle. Their DV- $X\alpha$  calculations predict that the lowest energy allowed metal-to-ligand charge transfer absorbance will decrease in energy as the dihedral angle between the diimine ligands becomes smaller. Experimentally, the solid state absorbance of some  $[\text{Cu}(\text{dmp})_2]\text{X}$  salts, where the dihedral angle was known, were shown to follow this prediction. However, only two of the solids measured had defined dihedral angles. Further absorption analysis of solids with known dihedral angles along with their luminescent properties in the solid state should lead to a more clear understanding of what impact the dihedral angle has on the spectrum.

Another interesting aspect of copper phenanthroline solution chemistry is emission. Copper phenanthrolines with substituents in the 2,9 positions show emission in  $\text{CH}_2\text{Cl}_2$  at room temperature.<sup>10</sup> If there are no substituents in positions 2 and 9, then the complexes are non-emissive in solution, as well as in a frozen glass.<sup>1, 10</sup> The main reason is due to a large geometry change that accompanies excitation.<sup>10</sup> Since the absorption is a metal-to-ligand charge transfer, a formal  $d^9$  Cu(II) metal center is created. Since  $d^9$  is Jahn-Teller active, tetrahedral geometry is not the preferred geometry for  $d^9$ . The excited compound undergoes a flattening distortion to alleviate the excess energy and return to the ground state.<sup>10</sup> McMillin and co-workers have shown many ways around this distortion,<sup>10, 11</sup> but perhaps one of the simplest is to examine the salts in the solid state. The solid state should severely retard the flattening distortion and lead to longer lived excited states. The examination and correlation of copper phenanthroline structure with absorption and emission properties will be the focus of this work.

## Experimental

### Materials

All solvents were of reagent grade unless otherwise stated. The 1,10-phenanthroline (phen), 3,4,7,8-tetramethyl-1,10-phenanthroline (tmp), 2,9-dimethyl-1,10-phenanthroline (dmp), 2,9-dimethyl-4,7-diphenyl-1,10-phenanthroline (bcp), 2,2'-bipyridine (bipy), 4,4'-dimethyl-2,2'-bipyridine (dmbp),  $\text{KPF}_6$ ,  $\text{NaBPh}_4$ , 2.0 M *n*-butyl lithium solution in ether, and 1.6 M phenyllithium in hexanes were purchased from Aldrich and used as is. The ligands 2,9-di-*n*-butyl-1,10-phenanthroline (dbp), 2,9-diphenyl-1,10-phenanthroline (dpp), 6,6'-dimethyl-2,2'-bipyridine (dmbp), and 4,4',6,6'-tetramethyl-2,2'-bipyridine (tmbp) were prepared by modifying the prep by Pallenberg et al<sup>9</sup> to include the necessary starting materials. The ligands 2,9-di-*n*-butyl-4,7-dimethyl-1,10-phenanthroline (dbdmp), 2,9-di-*n*-butyl-3,4,7,8-tetramethyl-1,10-phenanthroline (dbtmp), 2,9-diphenyl-4,7-dimethyl-1,10-phenanthroline (dpdmp), and 2,9-diphenyl-3,4,7,8-tetramethyl-1,10-phenanthroline (dptmp) were available from a previous study.<sup>11</sup>

## Methods

Solid state absorbance measurements were made using the opal-glass method.<sup>12</sup> Whatman filter paper grades 1 and 6 were used with paraffin oil. The spectrometer was backgrounded with a blank filter paper and oil sample. The data was corrected by dividing the intensity at each wavelength by the intensity at the starting wavelength of the scan, then subtracting 1. The new intensity value was then used in all the spectral plots.

Solid state emission measurements were made by packing a melting point capillary with ~1.75 cm (0.5 in.) of sample. The open end of the capillary was then sealed over a flame. During emission and lifetime measurements, a 452 nm notch filter was placed on the excitation beam to isolate the 440 nm excitation light. A 525 nm cutoff filter was used to protect the photomultiplier tube and both the excitation and emission bandpasses were set at 10 nm.

Excited state lifetimes were measured on the same capillary samples as for the emission measurements. The same filter setup was used except for an additional 575 nm filter that was placed in front of the photomultiplier tube. Data was taken from a digital oscilloscope and fit to an exponential decay with a user-written program.

Lorentz and polarization corrections were applied to the crystal structure data. The linear absorption coefficient is 5.2/cm for Mo K radiation. An empirical absorption correction using SCALEPACK<sup>14</sup> was applied. The structure was solved using the structure solution program PATTY in DIRDIF92,<sup>15a</sup> or by the direct methods using SIR97.<sup>15b</sup> The remaining atoms were located in succeeding difference Fourier syntheses. Hydrogen atoms were included in the refinement but restrained to ride on the atom to which they are bonded. The structure was refined in full-matrix least-squares where the function minimized was  $\sum w(|F_o|^2 - |F_c|^2)^2$  and the weight  $w$  is defined as

$$w = 1/[\sigma^2(F_o^2) + (0.0996P)^2 + 0.0000P]$$

where  $P = (F_o^2 + 2F_c^2)/3$ . Scattering factors were taken from the "International Tables for Crystallography".<sup>16</sup> The space group was determined by the program ABSEN.<sup>17</sup> Refinement of the crystal data was performed with SHELX-97.<sup>18</sup>

### Instrumentation

Absorbance measurements were made on a Perkin-Elmer Lambda 4C spectrophotometer, while emission measurements were recorded on a SLM SPF-500 spectrofluorometer. Excited state lifetime measurements were made on the laser setup described in the literature.<sup>13</sup> Preliminary examination of the crystals and subsequent data collection were performed with Mo K $\alpha$  radiation ( $\lambda = 0.71073\text{\AA}$ ) on a Nonius KappaCCD. Structure refinement was performed on a AlphaServer 2100 computer.

### Crystal Structure Determinations

[Cu(tmp)<sub>2</sub>]BPh<sub>4</sub>. An orange plate of C<sub>36</sub>H<sub>32</sub>CuBN<sub>4</sub> having approximate dimensions of 0.30 x 0.18 x 0.10 mm was grown from vapor diffusion of toluene into a methylene chloride solution of the complex. The crystal was mounted on a glass fiber in a random orientation. Cell constants and an orientation matrix for data collection were obtained from least-squares refinement, using the setting angles of 57010 reflections in the range  $2 < \theta < 32^\circ$ . Data were collected to a maximum  $2\theta$  of  $66.0^\circ$ . A total of 57010 reflections were collected, of which 12948 were unique. Transmission coefficients ranged from 0.770 to 0.949 with an average value of 0.905. Intensities of equivalent reflections were averaged. The agreement factor for the averaging was 8.8% based on intensity. 12948 reflections were used in the refinements. However, only reflections with  $F_o^2 > 2\sigma(F_o^2)$  were used in calculating R. The final cycle of refinement included 567 variable parameters and converged (largest parameter shift was 0.03 times its esd) with unweighted and weighted agreement factors of:

$$R1 = \Sigma |F_o - F_c| / \Sigma F_o = 0.065$$

$$R2 = \text{SQRT} ( \Sigma w ( F_o^2 - F_c^2 )^2 / \Sigma w (F_o^2)^2 ) = 0.157$$

The standard deviation of an observation of unit weight was 1.03. The highest peak in the final difference Fourier had a height of  $0.51 \text{ e/A}^3$ . The minimum negative peak had a height of  $-0.72 \text{ e/A}^3$ . Table 3.1 gives a summary of the crystal parameters and other details of refinement.

Table 3.1. Crystallographic data for  $[\text{Cu}(\text{C}_{32}\text{H}_{32}\text{N}_4)]\text{BC}_{24}\text{H}_{20}$ .

|                                           |                                               |
|-------------------------------------------|-----------------------------------------------|
| $\text{CuN}_4\text{C}_{36}\text{BH}_{32}$ | formula weight 855.42                         |
| $a = 17.4883(4)\text{\AA}$                | space group $\text{P2}_1/\text{n}$ (No. 14)   |
| $b = 9.86860(10)\text{\AA}$               | $T = 296. \text{ K}$                          |
| $c = 26.3747(6)\text{\AA}$                | $\lambda = 0.71073\text{\AA}$                 |
| $\beta = 97.7021(8)^\circ$                | $\rho_{\text{calc}} = 1.260\text{ g cm}^{-3}$ |
| $V = 4510.8(3)\text{\AA}^3$               | $\mu = 0.525\text{ mm}^{-1}$                  |
| $Z = 4$                                   | transmission coeff = 0.770-0.949              |
| $R(\text{F}_o)^a = 0.065$                 | $R_w(\text{F}_o^2)^b = 0.157$                 |

a  $R = \sum ||\text{F}_o| - |\text{F}_c|| / \sum |\text{F}_o|$  for  $\text{F}_o^2 > 2\sigma(\text{F}_o^2)$

b  $R_w = [\sum w (|\text{F}_o|^2 - |\text{F}_c|^2)|^2 / \sum w |\text{F}_o|^2]^{1/2}$

$[\text{Cu}(\text{dipp})_2]\text{TFPB}$ . A yellow-orange plate of  $\text{C}_{68}\text{H}_{52}\text{CuBF}_{24}\text{N}_4$  having approximate dimensions of  $0.25 \times 0.22 \times 0.10 \text{ mm}$  was grown by slow evaporation of an aqueous alcoholic solution of the compound. The crystal was mounted on a glass fiber in a random orientation. Cell constants and an orientation matrix for data collection were obtained from least-squares refinement, using the setting angles of 43343 reflections in the range  $4 < \theta < 30^\circ$ . Data were collected to a maximum  $2\theta$  of  $61.0^\circ$ . A total of 43343 reflections were collected, of which 8774 were unique. Transmission coefficients ranged from 0.706 to 0.958 with an average value of 0.894. Intensities of equivalent reflections were averaged. The agreement factor for the averaging was 6.2% based on intensity. 8774 reflections were used in the refinements. However, only reflections with  $\text{F}_o^2 > 2\sigma(\text{F}_o^2)$  were used in calculating R. The final cycle of refinement included 891 variable parameters and converged (largest parameter shift was 0.04 times its esd) with unweighted and weighted agreement factors of:

$$R1 = \sum |\text{F}_o - \text{F}_c| / \sum \text{F}_o = 0.093$$

$$R2 = \text{SQRT} ( \sum w ( \text{F}_o^2 - \text{F}_c^2 )^2 / \sum w (\text{F}_o^2)^2 ) = 0.253$$

The standard deviation of an observation of unit weight was 1.03. The highest peak in the final difference Fourier had a height of  $0.86 \text{ e/A}^3$ . The minimum negative peak had a height of  $-0.71 \text{ e/A}^3$ . Table 3.2 gives a summary of the crystal parameters and other details of refinement.

Table 3.2. Crystallographic data for  $[\text{Cu}(\text{C}_{44}\text{H}_{40}\text{N}_4)]\text{BC}_{24}\text{H}_{12}\text{F}_{24}$ .

|                                                        |                                                |
|--------------------------------------------------------|------------------------------------------------|
| $\text{CuF}_{24}\text{N}_4\text{C}_{68}\text{BH}_{32}$ | formula weight 1455.51                         |
| $a = 14.2523(3) \text{ \AA}$                           | space group $\text{P}\bar{1}$ (No. 2)          |
| $b = 16.0496(4) \text{ \AA}$                           | $T = 296. \text{ K}$                           |
| $c = 17.5801(3) \text{ \AA}$                           | $\lambda = 0.71073 \text{ \AA}$                |
| $\alpha = 112.4150(13)^\circ$                          | $\rho_{\text{calc}} = 1.418 \text{ g cm}^{-3}$ |
| $\beta = 105.7480(13)^\circ$                           | $\mu = 0.425 \text{ mm}^{-1}$                  |
| $\gamma = 99.6078(11)^\circ$                           | transmission coeff = 0.706-0.958               |
| $V = 3408.7(3) \text{ \AA}^3$                          | $R(\text{F}_o)^a = 0.093$                      |
| $Z = 2$                                                | $R_w(\text{F}_o^2)^b = 0.253$                  |

a  $R = \sum ||\text{F}_o| - |\text{F}_c|| / \sum |\text{F}_o|$  for  $\text{F}_o^2 > 2\sigma(\text{F}_o^2)$

b  $R_w = [\sum w (|\text{F}_o^2| - |\text{F}_c^2|)^2 / \sum w |\text{F}_o^2|]^2$

$[\text{Cu}(\text{dptmp})_2]\text{PF}_6 \cdot \text{THF}$ . An orange chunk of  $\text{C}_{60}\text{H}_{56}\text{CuF}_6\text{N}_4\text{OP}$  having approximate dimensions of  $0.25 \times 0.20 \times 0.18 \text{ mm}$  was grown by slow diffusion of toluene into a THF solution of the compound. The crystal was mounted on a glass fiber in a random orientation. Cell constants and an orientation matrix for data collection were obtained from least-squares refinement, using the setting angles of 33837 reflections in the range  $3 < \theta < 31^\circ$ . Data were collected to a maximum  $2\theta$  of  $63.9^\circ$ . A total of 33837 reflections were collected, of which 13753 were unique. Transmission coefficients ranged from 0.751 to 0.911 with an average value of 0.875. A secondary extinction correction was applied.<sup>18</sup> The final coefficient, refined in least-squares, was 0.0240000 (in absolute units). Intensities of equivalent reflections were averaged. The

agreement factor for the averaging was 5.5% based on intensity. 13753 reflections were used in the refinements. However, only reflections with  $F_o^2 > 2\sigma(F_o^2)$  were used in calculating R. The final cycle of refinement included 666 variable parameters and converged (largest parameter shift was 0.04 times its esd) with unweighted and weighted agreement factors of:

$$R1 = \Sigma |F_o - F_c| / \Sigma F_o = 0.074$$

$$R2 = \text{SQRT} ( \Sigma w (F_o^2 - F_c^2)^2 / \Sigma w (F_o^2)^2 ) = 0.190$$

The standard deviation of an observation of unit weight was 1.03. The highest peak in the final difference Fourier had a height of  $0.67 \text{ e}/\text{\AA}^3$ . The minimum negative peak had a height of  $-0.56 \text{ e}/\text{\AA}^3$ . Table 3.3 gives a summary of the crystal parameters and other details of refinement.

Table 3.3. Crystallographic data for  $[\text{Cu}(\text{C}_{56}\text{H}_{48}\text{N}_4)]\text{PF}_6 \cdot \text{C}_4\text{H}_8\text{O}$ .

|                                                      |                                                |
|------------------------------------------------------|------------------------------------------------|
| $\text{CuPF}_6\text{ON}_4\text{C}_{60}\text{H}_{56}$ | formula weight 1057.65                         |
| $a = 12.8486(4)\text{\AA}$                           | space group $P\bar{1}$ (No. 2)                 |
| $b = 13.7341(4)\text{\AA}$                           | $T = 296. \text{ K}$                           |
| $c = 15.1678(3)\text{\AA}$                           | $\lambda = 0.71073\text{\AA}$                  |
| $\alpha = 99.5819(14)^\circ$                         | $\rho_{\text{calc}} = 1.355 \text{ g cm}^{-3}$ |
| $\beta = 96.7263(13)^\circ$                          | $\mu = 0.516 \text{ mm}^{-1}$                  |
| $\gamma = 97.3311(12)^\circ$                         | transmission coeff = 0.751-0.911               |
| $V = 2591.3(2)\text{\AA}^3$                          | $R(F_o)^a = 0.074$                             |
| $Z = 2$                                              | $R_w(F_o^2)^b = 0.190$                         |

a  $R = \Sigma ||F_o| - |F_c|| / \Sigma |F_o|$  for  $F_o^2 > 2\sigma(F_o^2)$

b  $R_w = [\Sigma w (|F_o^2| - |F_c^2|)^2 / \Sigma w |F_o^2|^2]^{1/2}$

### Preparations

Copper complexes were prepared following literature methods<sup>19</sup> and were recrystallized from ethanol and water. Metathesis reactions were done in a mixture of ethanol and water and the compound was isolated sacrificially, meaning that the isolated yields were on the order of 75%. This was done to insure conversion without contamination.

### Results

#### Crystal Structure Analysis

##### [Cu(tmp)<sub>2</sub>]BPh<sub>4</sub>

Figure 3.1 gives a view of the copper complex along with the atom labels. The positional and thermal parameters, along with bond lengths and bond angles are given in Tables 3.4, 3.5, and 3.6, respectively. The geometry around the copper center is best described as pseudotetrahedral with molecular symmetry closer to  $D_{2d}$  than  $D_2$ . The average chelate-bite angle is  $81.25^\circ$ , which is a typical value for copper phenanthrolines.<sup>3, 20</sup> All of the Cu-N bond distances are similar in value, so there is no “rocking” distortion as is present in 2,9-diaryl substituted phenanthroline complexes.<sup>21, 22</sup> The average Cu-N bond distance is  $2.044 \text{ \AA}$ . This value is close to other non-2,9-substituted phenanthroline complexes. For example, the average Cu-N distance in [Cu(phen)<sub>2</sub>]ClO<sub>4</sub> is  $2.049 \text{ \AA}$ ,<sup>8</sup> while for [Cu(phen)<sub>2</sub>]CuBr<sub>2</sub> the average value is  $2.039 \text{ \AA}$ .<sup>8</sup> The one geometrical characteristic that sets [Cu(tmp)<sub>2</sub>]BPh<sub>4</sub> apart is its rather large dihedral angle. [Cu(tmp)<sub>2</sub>]BPh<sub>4</sub> has a dihedral angle of  $81.8^\circ$ , while the dihedral angles ( $\Theta_2$ ) for [Cu(phen)<sub>2</sub>]ClO<sub>4</sub>, [Cu(phen)<sub>2</sub>][Cu(OAc)<sub>2</sub>], and [Cu(phen)<sub>2</sub>]CuBr<sub>2</sub> are  $49.9^\circ$ ,<sup>8</sup>  $68.6^\circ$ ,<sup>8</sup> and  $76.8^\circ$ ,<sup>23</sup> respectively. In fact, this dihedral angle is larger than the  $\Theta_2$  of some [Cu(dmp)<sub>2</sub>]X complexes. [Cu(dmp)<sub>2</sub>]Br and [Cu(dmp)<sub>2</sub>]NO<sub>3</sub> have dihedral angles of



79.9° and 72.4°, respectively.<sup>3,6</sup> Figure 3.2 shows the  $[\text{Cu}(\text{tmp})_2]^+$  cation from behind one of the phenanthroline ligands. The almost perpendicular arrangement of the two tmp ligands is indicative of the large  $\Theta_z$ .

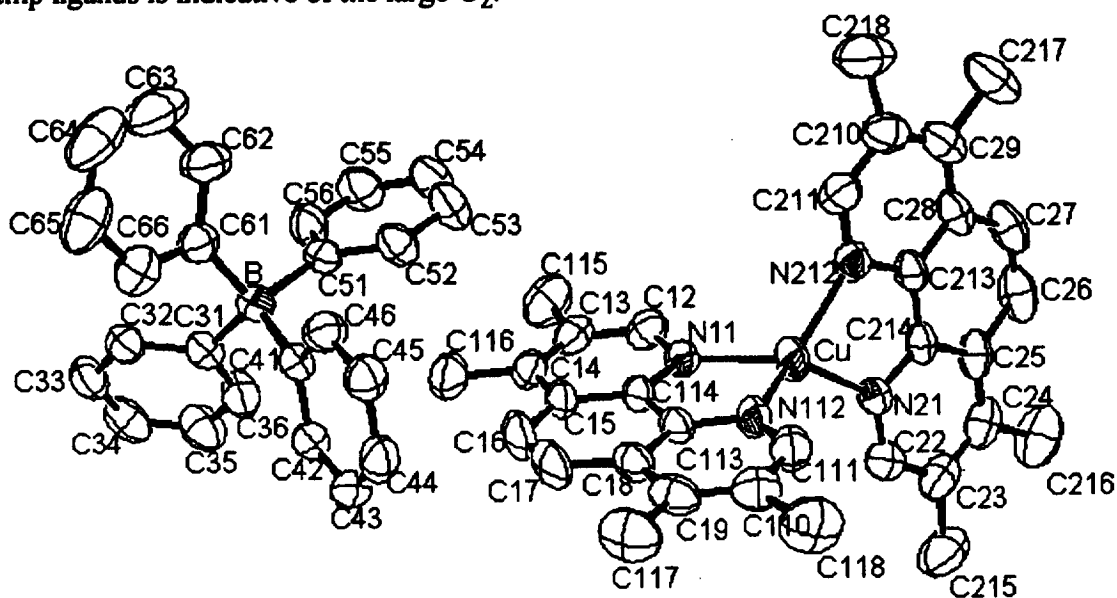


Figure 3.1. ORTEP drawing of  $[\text{Cu}(\text{tmp})_2]\text{BPh}_4$  with labeling scheme and 50% ellipsoids. Hydrogen atoms have been omitted for clarity.

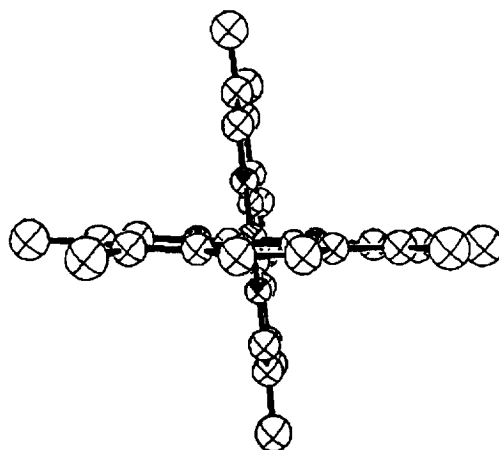


Figure 3.2. ORTEP drawing of the  $[\text{Cu}(\text{tmp})_2]^+$  cation from behind one phenanthroline ligand. The angle between the two phenanthroline ligands is  $\Theta_z$  (81.8°).

Table 3.4. Positional and temperature parameters ( $\text{\AA}^2$ ) for  $[\text{Cu}(\text{tmp})_2]\text{BPh}_4$ .

| Atom   | x             | y           | z             | U ( $\text{\AA}^2$ ) <sup>a</sup> |
|--------|---------------|-------------|---------------|-----------------------------------|
| Cu     | 0.253358 (19) | 0.06729 (4) | 0.274371 (15) | 0.06220 (14)                      |
| N(11)  | 0.18432 (12)  | 0.1880 (2)  | 0.31252 (8)   | 0.0479 (7)                        |
| N(21)  | 0.34472 (13)  | 0.1290 (2)  | 0.23961 (9)   | 0.0517 (7)                        |
| N(112) | 0.14921 (13)  | 0.0173 (2)  | 0.23484 (9)   | 0.0502 (7)                        |
| N(212) | 0.33801 (13)  | -0.0455 (2) | 0.31586 (9)   | 0.0507 (7)                        |
| C(12)  | 0.20183 (17)  | 0.2720 (3)  | 0.35194 (11)  | 0.0554 (9)                        |
| C(13)  | 0.14855 (19)  | 0.3512 (3)  | 0.37416 (11)  | 0.0592 (9)                        |
| C(14)  | 0.07192 (18)  | 0.3393 (3)  | 0.35543 (12)  | 0.0557 (9)                        |
| C(15)  | 0.05009 (15)  | 0.2467 (3)  | 0.31503 (11)  | 0.0495 (8)                        |
| C(16)  | -0.02781 (17) | 0.2174 (3)  | 0.29423 (14)  | 0.0674 (12)                       |
| C(17)  | -0.04626 (17) | 0.1275 (4)  | 0.25627 (14)  | 0.0676 (11)                       |
| C(18)  | 0.01154 (15)  | 0.0562 (3)  | 0.23309 (12)  | 0.0514 (8)                        |
| C(19)  | -0.00541 (18) | -0.0378 (3) | 0.19275 (13)  | 0.0585 (9)                        |
| C(22)  | 0.34804 (19)  | 0.2165 (3)  | 0.20183 (12)  | 0.0633 (10)                       |
| C(23)  | 0.4158 (2)    | 0.2577 (3)  | 0.18300 (13)  | 0.0668 (12)                       |
| C(24)  | 0.4848 (2)    | 0.2056 (3)  | 0.20613 (14)  | 0.0670 (10)                       |
| C(25)  | 0.48395 (16)  | 0.1112 (3)  | 0.24617 (13)  | 0.0580 (9)                        |
| C(26)  | 0.55179 (17)  | 0.0497 (4)  | 0.27391 (17)  | 0.0772 (12)                       |
| C(27)  | 0.54802 (18)  | -0.0411 (4) | 0.31152 (16)  | 0.0746 (12)                       |
| C(28)  | 0.47664 (16)  | -0.0813 (3) | 0.32707 (13)  | 0.0567 (9)                        |
| C(29)  | 0.4698 (2)    | -0.1775 (3) | 0.36633 (13)  | 0.0633 (10)                       |
| C(31)  | -0.23565 (15) | 0.3798 (3)  | 0.43421 (11)  | 0.0464 (8)                        |
| C(32)  | -0.29496 (17) | 0.4278 (3)  | 0.45997 (11)  | 0.0519 (8)                        |
| C(33)  | -0.31154 (19) | 0.5657 (3)  | 0.46317 (13)  | 0.0647 (10)                       |
| C(34)  | -0.2702 (2)   | 0.6609 (3)  | 0.44075 (14)  | 0.0701 (12)                       |
| C(35)  | -0.21201 (19) | 0.6182 (3)  | 0.41510 (15)  | 0.0701 (12)                       |
| C(36)  | -0.19498 (18) | 0.4810 (3)  | 0.41197 (13)  | 0.0621 (9)                        |
| C(41)  | -0.22485 (14) | 0.1543 (3)  | 0.37489 (10)  | 0.0446 (7)                        |
| C(42)  | -0.23328 (16) | 0.2281 (3)  | 0.32956 (11)  | 0.0518 (8)                        |
| C(43)  | -0.24297 (16) | 0.1646 (4)  | 0.28160 (11)  | 0.0609 (9)                        |
| C(44)  | -0.24423 (16) | 0.0265 (4)  | 0.27746 (12)  | 0.0606 (9)                        |
| C(45)  | -0.23670 (17) | -0.0502 (3) | 0.32147 (12)  | 0.0568 (9)                        |
| C(46)  | -0.22728 (17) | 0.0128 (3)  | 0.36839 (11)  | 0.0529 (9)                        |
| C(51)  | -0.11567 (15) | 0.2115 (2)  | 0.45375 (10)  | 0.0447 (7)                        |
| C(52)  | -0.06418 (17) | 0.1233 (3)  | 0.43470 (12)  | 0.0551 (9)                        |
| C(53)  | 0.01366 (18)  | 0.1190 (3)  | 0.45359 (14)  | 0.0672 (10)                       |
| C(54)  | 0.04453 (19)  | 0.2027 (3)  | 0.49220 (13)  | 0.0649 (10)                       |
| C(55)  | -0.0040 (2)   | 0.2922 (3)  | 0.51196 (13)  | 0.0689 (10)                       |
| C(56)  | -0.08184 (18) | 0.2955 (3)  | 0.49320 (11)  | 0.0588 (9)                        |
| C(61)  | -0.25896 (17) | 0.1261 (3)  | 0.46828 (11)  | 0.0500 (8)                        |
| C(62)  | -0.2267 (2)   | 0.0565 (3)  | 0.51226 (12)  | 0.0680 (12)                       |
| C(63)  | -0.2713 (4)   | -0.0246 (4) | 0.53970 (16)  | 0.0995 (18)                       |
| C(64)  | -0.3484 (4)   | -0.0403 (4) | 0.52524 (19)  | 0.1012 (18)                       |
| C(65)  | -0.3819 (3)   | 0.0252 (4)  | 0.48257 (18)  | 0.0872 (14)                       |
| C(66)  | -0.3379 (2)   | 0.1056 (3)  | 0.45446 (13)  | 0.0652 (10)                       |
| C(110) | 0.0558 (2)    | -0.0981 (3) | 0.17336 (13)  | 0.0631 (10)                       |
| C(111) | 0.13080 (19)  | -0.0676 (3) | 0.19632 (12)  | 0.0608 (10)                       |
| C(113) | 0.08919 (14)  | 0.0817 (3)  | 0.25270 (11)  | 0.0445 (7)                        |
| C(114) | 0.10867 (14)  | 0.1754 (3)  | 0.29405 (10)  | 0.0443 (7)                        |
| C(115) | 0.1788 (3)    | 0.4424 (4)  | 0.41808 (15)  | 0.0895 (14)                       |
| C(116) | 0.0121 (2)    | 0.4223 (3)  | 0.37779 (15)  | 0.0796 (14)                       |

Table 3.4, continued

| Atom                                                                   | x            | y          | z           | U (Å <sup>2</sup> ) <sup>a</sup> |
|------------------------------------------------------------------------|--------------|------------|-------------|----------------------------------|
| ----                                                                   | ---          | ---        | ---         | -----                            |
| C(117)                                                                 | -0.0877(2)   | -0.0736(4) | 0.17136(16) | 0.0845(14)                       |
| C(118)                                                                 | 0.0455(3)    | -0.1970(4) | 0.12931(14) | 0.0916(15)                       |
| C(210)                                                                 | 0.3983(2)    | -0.2019(3) | 0.37970(12) | 0.0652(10)                       |
| C(211)                                                                 | 0.33530(19)  | -0.1310(3) | 0.35433(12) | 0.0595(9)                        |
| C(213)                                                                 | 0.40965(14)  | -0.0200(3) | 0.30211(11) | 0.0449(8)                        |
| C(214)                                                                 | 0.41263(15)  | 0.0749(3)  | 0.26135(11) | 0.0469(8)                        |
| C(215)                                                                 | 0.4091(3)    | 0.3575(4)  | 0.13935(15) | 0.0992(17)                       |
| C(216)                                                                 | 0.5605(2)    | 0.2489(4)  | 0.18823(17) | 0.1001(17)                       |
| C(217)                                                                 | 0.5408(2)    | -0.2485(4) | 0.39281(16) | 0.0995(15)                       |
| C(218)                                                                 | 0.3835(3)    | -0.2995(4) | 0.42172(15) | 0.0973(16)                       |
| B                                                                      | -0.20917(18) | 0.2192(3)  | 0.43287(12) | 0.0452(9)                        |
| <sup>a</sup> $U_{eq} = (1/3) \sum_i \sum_j U_{ij} a_i^* a_j^* a_i a_j$ |              |            |             |                                  |

Table 3.5. Bond distances (Å) for [Cu(tmp)<sub>2</sub>]BPh<sub>4</sub>. Numbers in parentheses are estimated standard deviations in the least significant digits.

| Atom 1 | Atom 2 | Distance | Atom 1 | Atom 2 | Distance |
|--------|--------|----------|--------|--------|----------|
| =====  | =====  | =====    | =====  | =====  | =====    |
| Cu     | N(112) | 2.034(2) | C(29)  | C(210) | 1.365(5) |
| Cu     | N(21)  | 2.039(2) | C(29)  | C(217) | 1.512(4) |
| Cu     | N(212) | 2.048(2) | C(31)  | C(32)  | 1.397(4) |
| Cu     | N(11)  | 2.053(2) | C(31)  | C(36)  | 1.399(4) |
| N(11)  | C(12)  | 1.332(4) | C(31)  | B      | 1.653(4) |
| N(11)  | C(114) | 1.353(3) | C(32)  | C(33)  | 1.396(4) |
| N(21)  | C(22)  | 1.326(4) | C(33)  | C(34)  | 1.368(5) |
| N(21)  | C(214) | 1.357(3) | C(34)  | C(35)  | 1.362(5) |
| N(112) | C(111) | 1.323(4) | C(35)  | C(36)  | 1.391(4) |
| N(112) | C(113) | 1.364(3) | C(41)  | C(42)  | 1.391(4) |
| N(212) | C(211) | 1.326(4) | C(41)  | C(46)  | 1.408(4) |
| N(212) | C(213) | 1.373(3) | C(41)  | B      | 1.647(4) |
| C(12)  | C(13)  | 1.404(4) | C(42)  | C(43)  | 1.401(4) |
| C(13)  | C(14)  | 1.370(4) | C(43)  | C(44)  | 1.367(5) |
| C(13)  | C(115) | 1.506(5) | C(44)  | C(45)  | 1.377(4) |
| C(14)  | C(15)  | 1.417(4) | C(45)  | C(46)  | 1.375(4) |
| C(14)  | C(116) | 1.510(4) | C(51)  | C(52)  | 1.394(4) |
| C(15)  | C(114) | 1.415(3) | C(51)  | C(56)  | 1.398(4) |
| C(15)  | C(16)  | 1.428(4) | C(51)  | B      | 1.656(4) |
| C(16)  | C(17)  | 1.345(5) | C(52)  | C(53)  | 1.386(4) |
| C(17)  | C(18)  | 1.434(4) | C(53)  | C(54)  | 1.365(4) |
| C(18)  | C(113) | 1.409(4) | C(54)  | C(55)  | 1.375(4) |
| C(18)  | C(19)  | 1.412(4) | C(55)  | C(56)  | 1.385(4) |
| C(19)  | C(110) | 1.381(5) | C(61)  | C(66)  | 1.394(4) |
| C(19)  | C(117) | 1.515(4) | C(61)  | C(62)  | 1.400(4) |
| C(22)  | C(23)  | 1.405(4) | C(61)  | B      | 1.641(4) |
| C(23)  | C(24)  | 1.376(5) | C(62)  | C(63)  | 1.386(5) |
| C(23)  | C(215) | 1.508(5) | C(63)  | C(64)  | 1.360(7) |
| C(24)  | C(25)  | 1.410(5) | C(64)  | C(65)  | 1.360(6) |
| C(24)  | C(216) | 1.525(4) | C(65)  | C(66)  | 1.387(5) |
| C(25)  | C(214) | 1.407(4) | C(110) | C(111) | 1.401(5) |
| C(25)  | C(26)  | 1.442(5) | C(110) | C(118) | 1.509(5) |
| C(26)  | C(27)  | 1.345(5) | C(113) | C(114) | 1.436(4) |
| C(27)  | C(28)  | 1.421(5) | C(210) | C(211) | 1.398(4) |
| C(28)  | C(213) | 1.402(4) | C(210) | C(218) | 1.516(5) |
| C(28)  | C(29)  | 1.422(5) | C(213) | C(214) | 1.432(4) |

Table 3.6. Bond angles (deg.) for  $[\text{Cu}(\text{tmp})_2]\text{BPh}_4$ . Numbers in parentheses are estimated standard deviations in the least significant digits.

| Atom 1 | Atom 2 | Atom 3 | Angle      | Atom 1 | Atom 2 | Atom 3 | Angle    |
|--------|--------|--------|------------|--------|--------|--------|----------|
| =====  | =====  | =====  | =====      | =====  | =====  | =====  | =====    |
| N(112) | Cu     | N(21)  | 122.94(10) | C(25)  | C(24)  | C(216) | 120.9(4) |
| N(112) | Cu     | N(212) | 132.49(9)  | C(214) | C(25)  | C(24)  | 118.7(3) |
| N(21)  | Cu     | N(212) | 81.29(9)   | C(214) | C(25)  | C(26)  | 116.7(3) |
| N(112) | Cu     | N(11)  | 81.20(9)   | C(24)  | C(25)  | C(26)  | 124.6(3) |
| N(21)  | Cu     | N(11)  | 126.49(9)  | C(27)  | C(26)  | C(25)  | 122.4(3) |
| N(212) | Cu     | N(11)  | 118.95(9)  | C(26)  | C(27)  | C(28)  | 122.0(3) |
| C(12)  | N(11)  | C(114) | 116.7(2)   | C(213) | C(28)  | C(29)  | 118.9(3) |
| C(12)  | N(11)  | Cu     | 130.87(19) | C(213) | C(28)  | C(27)  | 117.1(3) |
| C(114) | N(11)  | Cu     | 112.40(18) | C(29)  | C(28)  | C(27)  | 124.0(3) |
| C(22)  | N(21)  | C(214) | 116.7(2)   | C(210) | C(29)  | C(28)  | 118.4(3) |
| C(22)  | N(21)  | Cu     | 130.43(19) | C(210) | C(29)  | C(217) | 121.5(3) |
| C(214) | N(21)  | Cu     | 112.74(18) | C(28)  | C(29)  | C(217) | 120.1(3) |
| C(111) | N(112) | C(113) | 116.2(3)   | C(32)  | C(31)  | C(36)  | 114.5(2) |
| C(111) | N(112) | Cu     | 131.0(2)   | C(32)  | C(31)  | B      | 124.3(2) |
| C(113) | N(112) | Cu     | 112.80(19) | C(36)  | C(31)  | B      | 121.0(2) |
| C(211) | N(212) | C(213) | 116.5(2)   | C(33)  | C(32)  | C(31)  | 122.3(3) |
| C(211) | N(212) | Cu     | 131.1(2)   | C(34)  | C(33)  | C(32)  | 121.2(3) |
| C(213) | N(212) | Cu     | 112.28(18) | C(35)  | C(34)  | C(33)  | 118.4(3) |
| N(11)  | C(12)  | C(13)  | 125.2(3)   | C(34)  | C(35)  | C(36)  | 120.7(3) |
| C(14)  | C(13)  | C(12)  | 118.3(3)   | C(35)  | C(36)  | C(31)  | 123.0(3) |
| C(14)  | C(13)  | C(115) | 123.7(3)   | C(42)  | C(41)  | C(46)  | 114.7(3) |
| C(12)  | C(13)  | C(115) | 118.0(3)   | C(42)  | C(41)  | B      | 125.5(2) |
| C(13)  | C(14)  | C(15)  | 118.6(2)   | C(46)  | C(41)  | B      | 119.8(2) |
| C(13)  | C(14)  | C(116) | 120.6(3)   | C(41)  | C(42)  | C(43)  | 121.9(3) |
| C(15)  | C(14)  | C(116) | 120.8(3)   | C(44)  | C(43)  | C(42)  | 121.1(3) |
| C(114) | C(15)  | C(14)  | 118.6(3)   | C(43)  | C(44)  | C(45)  | 118.8(3) |
| C(114) | C(15)  | C(16)  | 116.9(3)   | C(46)  | C(45)  | C(44)  | 119.8(3) |
| C(14)  | C(15)  | C(16)  | 124.5(3)   | C(45)  | C(46)  | C(41)  | 123.8(3) |
| C(17)  | C(16)  | C(15)  | 122.8(3)   | C(52)  | C(51)  | C(56)  | 114.2(3) |
| C(16)  | C(17)  | C(18)  | 121.9(3)   | C(52)  | C(51)  | B      | 124.4(2) |
| C(113) | C(18)  | C(19)  | 119.2(3)   | C(56)  | C(51)  | B      | 121.4(2) |
| C(113) | C(18)  | C(17)  | 117.1(3)   | C(53)  | C(52)  | C(51)  | 122.7(3) |
| C(19)  | C(18)  | C(17)  | 123.7(3)   | C(54)  | C(53)  | C(52)  | 121.4(3) |
| C(110) | C(19)  | C(18)  | 117.8(3)   | C(53)  | C(54)  | C(55)  | 118.0(3) |
| C(110) | C(19)  | C(117) | 120.4(3)   | C(54)  | C(55)  | C(56)  | 120.5(3) |
| C(18)  | C(19)  | C(117) | 121.8(3)   | C(55)  | C(56)  | C(51)  | 123.3(3) |
| N(21)  | C(22)  | C(23)  | 125.3(3)   | C(66)  | C(61)  | C(62)  | 114.8(3) |
| C(24)  | C(23)  | C(22)  | 117.8(3)   | C(66)  | C(61)  | B      | 121.0(3) |
| C(24)  | C(23)  | C(215) | 123.8(3)   | C(62)  | C(61)  | B      | 124.1(3) |
| C(22)  | C(23)  | C(215) | 118.4(4)   | C(63)  | C(62)  | C(61)  | 121.6(4) |
| C(23)  | C(24)  | C(25)  | 118.8(3)   | C(64)  | C(63)  | C(62)  | 121.6(4) |
| C(23)  | C(24)  | C(216) | 120.3(3)   | C(65)  | C(64)  | C(63)  | 118.6(4) |
| C(64)  | C(65)  | C(66)  | 120.4(4)   | C(211) | C(210) | C(218) | 117.9(3) |
| C(65)  | C(66)  | C(61)  | 123.0(4)   | N(212) | C(211) | C(210) | 125.3(3) |
| C(19)  | C(110) | C(111) | 118.3(3)   | N(212) | C(213) | C(28)  | 122.1(3) |
| C(19)  | C(110) | C(118) | 123.0(3)   | N(212) | C(213) | C(214) | 116.4(2) |
| C(111) | C(110) | C(118) | 118.6(3)   | C(28)  | C(213) | C(214) | 121.5(2) |
| N(112) | C(111) | C(110) | 125.8(3)   | N(21)  | C(214) | C(25)  | 122.6(3) |
| N(112) | C(113) | C(18)  | 122.6(3)   | N(21)  | C(214) | C(213) | 117.2(2) |

Table 3.6, continued

| Atom 1<br>===== | Atom 2<br>===== | Atom 3<br>===== | Angle<br>===== | Atom 1<br>===== | Atom 2<br>===== | Atom 3<br>===== | Angle<br>===== |
|-----------------|-----------------|-----------------|----------------|-----------------|-----------------|-----------------|----------------|
| N(112)          | C(113)          | C(114)          | 116.6(2)       | C(25)           | C(214)          | C(213)          | 120.2(3)       |
| C(18)           | C(113)          | C(114)          | 120.8(2)       | C(61)           | B               | C(41)           | 106.0(2)       |
| N(11)           | C(114)          | C(15)           | 122.5(3)       | C(61)           | B               | C(31)           | 110.7(2)       |
| N(11)           | C(114)          | C(113)          | 117.0(2)       | C(41)           | B               | C(31)           | 112.4(2)       |
| C(15)           | C(114)          | C(113)          | 120.5(2)       | C(61)           | B               | C(51)           | 111.1(2)       |
| C(29)           | C(210)          | C(211)          | 118.6(3)       | C(41)           | B               | C(51)           | 109.0(2)       |
| C(29)           | C(210)          | C(218)          | 123.5(3)       | C(31)           | B               | C(51)           | 107.7(2)       |

[Cu(dipp)<sub>2</sub>]TFPB

A view of the [Cu(dipp)<sub>2</sub>]<sup>+</sup> cation, along with the atomic labeling scheme, is shown in Figure 3.3. The positional and thermal parameters, bond distances, and bond angles are shown in Tables 3.7, 3.8, and 3.9, respectively. In this case, the dihedral angle between the two phenanthroline ligands around the metal complex is almost 90°. All 4 isopropyl groups are oriented so that each methine hydrogen is pointing towards the copper center, to relieve steric congestion. A least-squares fit of the two ligand planes gives an angle of 88.92°, while calculation of  $\Theta_z$  from the bond angles gives a value of 88.8°. This large angle is in line with that of other phenanthroline complexes with large 2,9 substituents and therefore not surprising considering the steric bulk of the isopropyl substituents. For example, with either *n*-pentyl<sup>9</sup> or CF<sub>3</sub><sup>24</sup> groups in the 2,9 positions,  $\Theta_z$  approximately is 87°. If however, a perchlorinated phenanthroline ligand is used,  $\Theta_z$  is 89.5°.<sup>25</sup> The average chelate-bite angle for the ligands in [Cu(dipp)<sub>2</sub>]<sup>+</sup> is 82.76°, in line with other phenanthroline complexes.<sup>3, 20</sup> What is surprising about this structure is the asymmetry of the Cu-N bond lengths. One of the ligands has average bond lengths (2.020 and 2.053 Å), while the other dipp ligand has one rather short (2.007 Å) and one rather long (2.068 Å) bond. This type of coordination is usually found in 2,9 aryl substituted phenanthrolines.<sup>21, 22</sup> In this case, however, the lack of conjugation with the 2,9 substituent has left the physical properties unaltered, unlike what occurs with aryl substitution, *vide infra*.

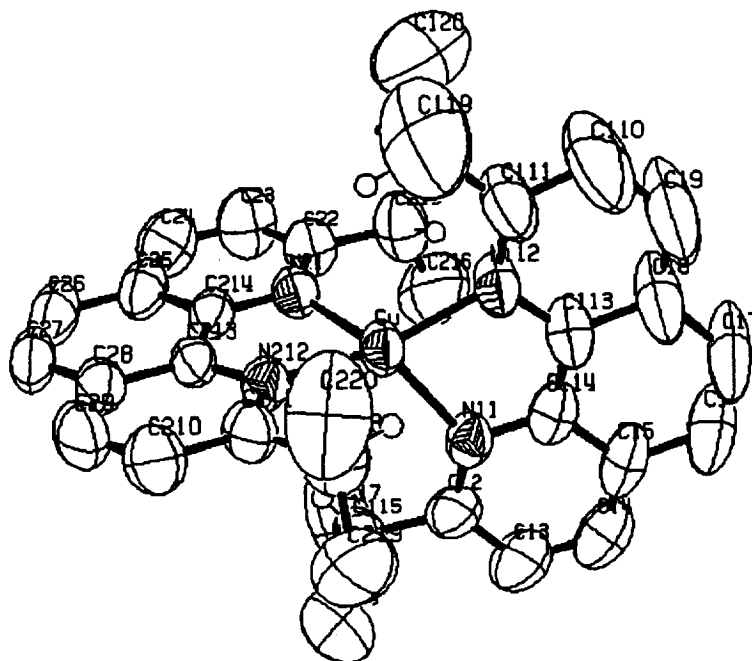


Figure 3.3. ORTEP drawing of the  $[\text{Cu}(\text{dipp})_2]^+$  cation with labeling scheme. All hydrogens, save the methine hydrogens, have been omitted for clarity. Ellipsoids are 50% except for the spheres representing hydrogen atoms.

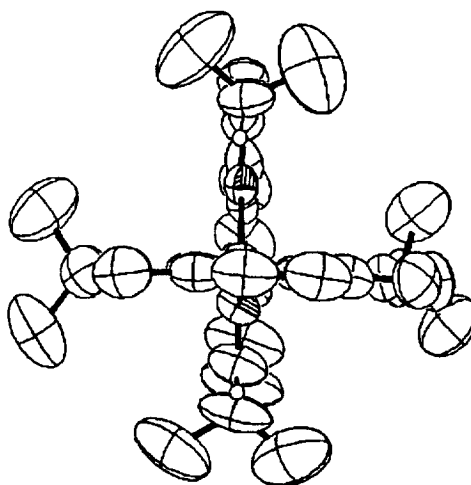


Figure 3.4. ORTEP drawing of the  $[\text{Cu}(\text{dipp})_2]^+$  cation from behind one phenanthroline ligand. The angle between the two phenanthroline ligands is  $\Theta_z$  ( $88.8^\circ$ ).

Table 3.7. Positional and temperature parameters ( $\text{\AA}^2$ ) for  $[\text{Cu}(\text{dipp})_2]\text{TFPB}$ .

| Atom   | x           | y           | z            | U ( $\text{\AA}^2$ ) <sup>a</sup> |
|--------|-------------|-------------|--------------|-----------------------------------|
| Cu     | 0.77055 (6) | 0.52667 (5) | -0.29681 (4) | 0.0632 (4)                        |
| N(11)  | 0.7266 (4)  | 0.3865 (4)  | -0.3888 (3)  | 0.063 (2)                         |
| N(21)  | 0.8736 (4)  | 0.5657 (3)  | -0.1728 (3)  | 0.063 (2)                         |
| N(112) | 0.8120 (4)  | 0.5486 (4)  | -0.3896 (3)  | 0.073 (2)                         |
| N(212) | 0.6846 (4)  | 0.5812 (3)  | -0.2281 (3)  | 0.061 (2)                         |
| C(12)  | 0.6842 (5)  | 0.3077 (5)  | -0.3859 (5)  | 0.079 (3)                         |
| C(13)  | 0.6612 (7)  | 0.2179 (6)  | -0.4572 (6)  | 0.107 (4)                         |
| C(14)  | 0.6863 (7)  | 0.2118 (6)  | -0.5280 (6)  | 0.104 (4)                         |
| C(15)  | 0.7325 (6)  | 0.2919 (6)  | -0.5321 (4)  | 0.091 (4)                         |
| C(16)  | 0.7607 (10) | 0.2893 (9)  | -0.6039 (6)  | 0.128 (6)                         |
| C(17)  | 0.8053 (12) | 0.3700 (10) | -0.6036 (6)  | 0.151 (7)                         |
| C(18)  | 0.8252 (10) | 0.4625 (8)  | -0.5319 (6)  | 0.128 (6)                         |
| C(19)  | 0.8743 (15) | 0.5485 (11) | -0.5252 (10) | 0.200 (10)                        |
| C(22)  | 0.9688 (5)  | 0.5614 (5)  | -0.1459 (4)  | 0.078 (3)                         |
| C(23)  | 1.0240 (7)  | 0.5865 (7)  | -0.0574 (6)  | 0.105 (4)                         |
| C(24)  | 0.9797 (7)  | 0.6154 (6)  | 0.0039 (5)   | 0.104 (4)                         |
| C(25)  | 0.8808 (7)  | 0.6223 (5)  | -0.0202 (4)  | 0.081 (3)                         |
| C(26)  | 0.8286 (9)  | 0.6538 (5)  | 0.0390 (5)   | 0.097 (4)                         |
| C(27)  | 0.7335 (8)  | 0.6596 (5)  | 0.0107 (5)   | 0.094 (4)                         |
| C(28)  | 0.6814 (6)  | 0.6366 (4)  | -0.0791 (4)  | 0.075 (3)                         |
| C(29)  | 0.5852 (7)  | 0.6454 (5)  | -0.1111 (6)  | 0.097 (4)                         |
| C(110) | 0.8900 (15) | 0.6329 (10) | -0.4553 (10) | 0.199 (11)                        |
| C(111) | 0.8552 (9)  | 0.6304 (6)  | -0.3876 (6)  | 0.113 (5)                         |
| C(113) | 0.7957 (6)  | 0.4644 (6)  | -0.4606 (4)  | 0.080 (3)                         |
| C(114) | 0.7508 (5)  | 0.3794 (5)  | -0.4599 (4)  | 0.069 (3)                         |
| C(115) | 0.6639 (7)  | 0.3174 (5)  | -0.3030 (6)  | 0.095 (4)                         |
| C(116) | 0.4438 (11) | 0.7328 (13) | 0.3212 (11)  | 0.221 (10)                        |
| C(117) | 0.2649 (15) | 0.7170 (16) | 0.2499 (11)  | 0.227 (15)                        |
| C(118) | 0.8725 (12) | 0.7229 (7)  | -0.3068 (8)  | 0.143 (7)                         |
| C(119) | 0.1959 (15) | 0.2211 (11) | 0.3400 (12)  | 0.210 (12)                        |
| C(120) | 0.0127 (15) | 0.2201 (12) | 0.2633 (13)  | 0.230 (12)                        |
| C(210) | 0.5405 (6)  | 0.6228 (6)  | -0.1974 (6)  | 0.096 (4)                         |
| C(211) | 0.5917 (5)  | 0.5906 (5)  | -0.2563 (5)  | 0.073 (3)                         |
| C(213) | 0.7288 (5)  | 0.6039 (4)  | -0.1413 (4)  | 0.061 (3)                         |
| C(214) | 0.8293 (5)  | 0.5964 (4)  | -0.1110 (4)  | 0.062 (2)                         |
| C(215) | 1.0144 (6)  | 0.5273 (7)  | -0.2167 (5)  | 0.100 (4)                         |
| C(216) | 1.0037 (10) | 0.4221 (9)  | -0.2473 (9)  | 0.170 (8)                         |
| C(217) | 0.1244 (8)  | 0.5834 (10) | 0.8108 (9)   | 0.161 (8)                         |
| C(218) | 0.5434 (6)  | 0.5676 (6)  | -0.3524 (5)  | 0.096 (4)                         |
| C(219) | 0.4479 (10) | 0.4796 (11) | 0.5979 (8)   | 0.175 (7)                         |
| C(220) | 0.4813 (12) | 0.3491 (11) | 0.3650 (9)   | 0.174 (9)                         |
| F(331) | 0.2798 (8)  | 0.3426 (5)  | -0.3282 (5)  | 0.195 (5)                         |
| F(332) | 0.2212 (6)  | 0.3860 (6)  | -0.2346 (8)  | 0.205 (7)                         |
| F(333) | 0.3562 (5)  | 0.4715 (4)  | 0.7854 (5)   | 0.171 (4)                         |
| F(351) | 0.6467 (8)  | 0.4497 (7)  | -0.0034 (9)  | 0.309 (8)                         |
| F(352) | 0.3272 (5)  | 0.6626 (14) | 0.0570 (6)   | 0.357 (12)                        |
| F(353) | 0.6248 (5)  | 0.3524 (7)  | 0.0346 (6)   | 0.211 (5)                         |
| F(431) | 0.0595 (4)  | 0.8343 (5)  | 0.2422 (4)   | 0.138 (4)                         |
| F(432) | 0.1086 (5)  | 0.8618 (10) | 0.1536 (6)   | 0.235 (8)                         |
| F(433) | 0.1211 (5)  | 0.9711 (5)  | 0.2706 (8)   | 0.268 (7)                         |
| F(451) | 0.1575 (8)  | 0.1673 (8)  | 0.0977 (4)   | 0.214 (7)                         |
| F(452) | 0.1591 (9)  | 0.0354 (6)  | 0.0496 (4)   | 0.255 (6)                         |



Table 3.7, continued

| Atom   | x          | y          | z          | U(Å <sup>2</sup> ) <sup>a</sup> |
|--------|------------|------------|------------|---------------------------------|
| F(453) | 0.2846(5)  | 0.1453(7)  | 0.0938(4)  | 0.192(5)                        |
| F(531) | 0.2882(4)  | -0.0351(5) | -0.6026(3) | 0.140(3)                        |
| F(532) | 0.4103(4)  | 0.0411(5)  | -0.4845(3) | 0.139(3)                        |
| F(533) | 0.3047(7)  | 0.1074(6)  | -0.5261(7) | 0.213(7)                        |
| F(551) | -0.0648(4) | -0.1574(4) | -0.4853(4) | 0.141(3)                        |
| F(552) | -0.0467(5) | -0.1715(5) | -0.6035(4) | 0.185(4)                        |
| F(553) | 0.0078(5)  | -0.2492(4) | -0.5396(5) | 0.157(3)                        |
| F(631) | 0.3285(10) | -0.1547(8) | -0.0764(9) | 0.295(11)                       |
| F(632) | 0.3553(8)  | -0.2572(5) | -0.1696(5) | 0.194(5)                        |
| F(633) | 0.4658(6)  | -0.1707(7) | -0.0615(7) | 0.208(6)                        |
| F(651) | 0.3477(6)  | 0.0857(7)  | 0.2378(6)  | 0.183(6)                        |
| F(652) | 0.4294(7)  | 0.0546(13) | 0.3279(8)  | 0.286(13)                       |
| F(653) | 0.3417(8)  | 0.9540(7)  | 0.2125(13) | 0.318(13)                       |
| C(31)  | 0.3539(4)  | 0.1844(4)  | -0.1894(3) | 0.048(2)                        |
| C(32)  | 0.3106(4)  | 0.2397(4)  | -0.2245(4) | 0.057(2)                        |
| C(33)  | 0.3604(5)  | 0.3329(4)  | -0.1994(4) | 0.063(3)                        |
| C(34)  | 0.4592(5)  | 0.3755(4)  | -0.1369(5) | 0.074(3)                        |
| C(35)  | 0.5043(5)  | 0.3226(4)  | -0.1002(4) | 0.069(2)                        |
| C(36)  | 0.4522(4)  | 0.2291(4)  | -0.1260(3) | 0.056(2)                        |
| C(41)  | 0.2048(4)  | 0.0820(4)  | -0.1741(3) | 0.049(2)                        |
| C(42)  | 0.1074(4)  | 0.0880(4)  | -0.2100(3) | 0.056(2)                        |
| C(43)  | 0.0404(4)  | 0.1003(5)  | -0.1653(4) | 0.068(3)                        |
| C(44)  | 0.0682(5)  | 0.1050(5)  | -0.0816(4) | 0.073(3)                        |
| C(45)  | 0.1630(4)  | 0.1011(4)  | -0.0435(4) | 0.062(3)                        |
| C(46)  | 0.2306(4)  | 0.0915(4)  | -0.0882(3) | 0.056(2)                        |
| C(51)  | 0.2335(4)  | 0.0251(3)  | -0.3331(3) | 0.049(2)                        |
| C(52)  | 0.2855(4)  | 0.0495(4)  | -0.3820(3) | 0.056(2)                        |
| C(53)  | 0.2484(5)  | 0.0043(5)  | -0.4739(4) | 0.065(3)                        |
| C(54)  | 0.1555(5)  | -0.0654(5) | -0.5213(4) | 0.072(3)                        |
| C(55)  | 0.1017(4)  | -0.0898(4) | -0.4754(4) | 0.064(2)                        |
| C(56)  | 0.1406(4)  | -0.0484(4) | -0.3836(4) | 0.057(2)                        |
| C(61)  | 0.3607(4)  | 0.0110(4)  | -0.2040(3) | 0.050(2)                        |
| C(62)  | 0.3416(4)  | -0.0525(4) | -0.1705(4) | 0.057(2)                        |
| C(63)  | 0.4070(5)  | -0.1063(4) | -0.1563(4) | 0.066(3)                        |
| C(64)  | 0.4911(5)  | -0.1008(5) | -0.1806(5) | 0.076(3)                        |
| C(65)  | 0.5097(5)  | -0.0405(5) | -0.2174(4) | 0.071(3)                        |
| C(66)  | 0.4477(4)  | 0.0142(4)  | -0.2273(4) | 0.061(3)                        |
| C(331) | 0.3099(6)  | 0.3850(5)  | 0.7576(7)  | 0.094(4)                        |
| C(351) | 0.6094(6)  | 0.3660(7)  | -0.0338(6) | 0.098(4)                        |
| C(431) | 0.0616(6)  | 0.8914(9)  | 0.2072(6)  | 0.109(5)                        |
| C(451) | 0.1918(6)  | 0.1057(7)  | 0.0447(5)  | 0.089(4)                        |
| C(531) | 0.3127(6)  | 0.0340(7)  | -0.5209(5) | 0.099(4)                        |
| C(551) | -0.0003(6) | -0.1655(6) | -0.5261(5) | 0.088(3)                        |
| C(631) | 0.3853(7)  | -0.1685(6) | -0.1166(6) | 0.091(4)                        |
| C(651) | 0.4020(8)  | 0.0364(9)  | 0.2460(8)  | 0.116(6)                        |
| B      | 0.2869(4)  | 0.0743(4)  | -0.2245(4) | 0.049(2)                        |

$$^a \quad U_{eq} = (1/3) \sum_i \sum_j U_{ij} a_i^* a_j^* a_i a_j$$

Table 3.8. Bond distances (Å) for [Cu(dipp)<sub>2</sub>]TFPB. Numbers in parentheses are estimated standard deviations in the least significant digits.

| Atom 1 | Atom 2 | Distance  | Atom 1 | Atom 2 | Distance  |
|--------|--------|-----------|--------|--------|-----------|
| =====  | =====  | =====     | =====  | =====  | =====     |
| Cu     | N(112) | 2.007(5)  | C(16)  | C(17)  | 1.341(15) |
| Cu     | N(212) | 2.020(5)  | C(17)  | C(18)  | 1.454(15) |
| Cu     | N(21)  | 2.053(5)  | C(18)  | C(19)  | 1.385(16) |
| Cu     | N(11)  | 2.068(5)  | C(18)  | C(113) | 1.418(10) |
| F(331) | C(331) | 1.301(11) | C(19)  | C(110) | 1.369(17) |
| F(332) | C(331) | 1.311(10) | C(22)  | C(23)  | 1.399(10) |
| F(333) | C(331) | 1.267(9)  | C(22)  | C(215) | 1.520(10) |
| F(351) | C(351) | 1.197(11) | C(23)  | C(24)  | 1.364(12) |
| F(352) | C(351) | 1.178(12) | C(24)  | C(25)  | 1.394(12) |
| F(353) | C(351) | 1.272(10) | C(25)  | C(26)  | 1.428(11) |
| F(431) | C(431) | 1.283(11) | C(25)  | C(214) | 1.421(9)  |
| F(432) | C(431) | 1.292(11) | C(26)  | C(27)  | 1.343(12) |
| F(433) | C(431) | 1.279(12) | C(27)  | C(28)  | 1.417(11) |
| F(451) | C(451) | 1.338(11) | C(28)  | C(29)  | 1.387(11) |
| F(452) | C(451) | 1.189(10) | C(28)  | C(213) | 1.417(8)  |
| F(453) | C(451) | 1.257(9)  | C(29)  | C(210) | 1.348(12) |
| F(531) | C(531) | 1.342(9)  | C(31)  | C(36)  | 1.388(7)  |
| F(532) | C(531) | 1.329(9)  | C(31)  | C(32)  | 1.394(8)  |
| F(533) | C(531) | 1.237(11) | C(31)  | B      | 1.644(8)  |
| F(551) | C(551) | 1.306(9)  | C(32)  | C(33)  | 1.381(8)  |
| F(552) | C(551) | 1.299(9)  | C(33)  | C(34)  | 1.387(9)  |
| F(553) | C(551) | 1.302(10) | C(33)  | C(331) | 1.475(10) |
| F(631) | C(631) | 1.205(9)  | C(34)  | C(35)  | 1.386(9)  |
| F(632) | C(631) | 1.283(10) | C(35)  | C(36)  | 1.392(8)  |
| F(633) | C(631) | 1.300(10) | C(35)  | C(351) | 1.475(10) |
| F(651) | C(651) | 1.215(10) | C(41)  | C(46)  | 1.394(7)  |
| F(652) | C(651) | 1.284(13) | C(41)  | C(42)  | 1.396(7)  |
| F(653) | C(651) | 1.260(13) | C(41)  | B      | 1.642(8)  |
| N(11)  | C(12)  | 1.333(8)  | C(42)  | C(43)  | 1.386(8)  |
| N(11)  | C(114) | 1.355(8)  | C(43)  | C(44)  | 1.384(9)  |
| N(21)  | C(22)  | 1.334(8)  | C(43)  | C(431) | 1.495(10) |
| N(21)  | C(214) | 1.375(7)  | C(44)  | C(45)  | 1.360(9)  |
| N(112) | C(111) | 1.336(9)  | C(45)  | C(46)  | 1.391(8)  |
| N(112) | C(113) | 1.374(9)  | C(45)  | C(451) | 1.461(9)  |
| N(212) | C(211) | 1.337(8)  | C(51)  | C(52)  | 1.397(7)  |
| N(212) | C(213) | 1.356(7)  | C(51)  | C(56)  | 1.405(7)  |
| C(12)  | C(13)  | 1.412(10) | C(51)  | B      | 1.645(7)  |
| C(12)  | C(115) | 1.517(10) | C(52)  | C(53)  | 1.389(8)  |
| C(13)  | C(14)  | 1.359(13) | C(53)  | C(54)  | 1.376(8)  |
| C(14)  | C(15)  | 1.381(12) | C(53)  | C(531) | 1.522(9)  |
| C(15)  | C(114) | 1.410(9)  | C(54)  | C(55)  | 1.368(8)  |
| C(15)  | C(16)  | 1.414(13) | C(55)  | C(56)  | 1.387(8)  |
| C(55)  | C(551) | 1.505(9)  | C(119) | C(118) | 1.576(18) |
| C(61)  | C(62)  | 1.384(7)  | C(120) | C(118) | 1.54(2)   |
| C(61)  | C(66)  | 1.405(8)  | C(210) | C(211) | 1.413(10) |
| C(61)  | B      | 1.643(8)  | C(211) | C(218) | 1.508(10) |
| C(62)  | C(63)  | 1.409(8)  | C(213) | C(214) | 1.428(9)  |
| C(63)  | C(64)  | 1.378(9)  | C(215) | C(217) | 1.513(13) |
| C(63)  | C(631) | 1.458(10) | C(215) | C(216) | 1.530(15) |

Table 3.8, continued

| Atom 1 | Atom 2 | Distance  | Atom 1 | Atom 2 | Distance  |
|--------|--------|-----------|--------|--------|-----------|
| =====  | =====  | =====     | =====  | =====  | =====     |
| C(64)  | C(65)  | 1.382(9)  | C(217) | C(215) | 1.513(13) |
| C(65)  | C(66)  | 1.368(8)  | C(218) | C(220) | 1.516(14) |
| C(65)  | C(651) | 1.478(10) | C(218) | C(219) | 1.544(14) |
| C(110) | C(111) | 1.421(13) | C(219) | C(218) | 1.544(14) |
| C(111) | C(118) | 1.536(13) | C(220) | C(218) | 1.516(14) |
| C(113) | C(114) | 1.413(10) | C(331) | F(331) | 1.301(11) |
| C(115) | C(116) | 1.494(14) | C(331) | F(332) | 1.311(10) |
| C(115) | C(117) | 1.508(16) | C(331) | C(33)  | 1.475(10) |
| C(116) | C(115) | 1.494(14) | C(351) | F(352) | 1.178(12) |
| C(117) | C(115) | 1.508(16) | C(431) | C(43)  | 1.495(10) |
| C(118) | C(120) | 1.54(2)   | C(651) | F(653) | 1.260(13) |
| C(118) | C(119) | 1.576(18) | C(651) | C(65)  | 1.478(10) |

Table 3.9. Bond angles (deg.) for [Cu(dipp)<sub>2</sub>]TFPB.

| Atom 1 | Atom 2 | Atom 3 | Angle      | Atom 1 | Atom 2 | Atom 3 | Angle     |
|--------|--------|--------|------------|--------|--------|--------|-----------|
| =====  | =====  | =====  | =====      | =====  | =====  | =====  | =====     |
| N(112) | Cu     | N(212) | 132.8(2)   | C(29)  | C(28)  | C(213) | 116.6(7)  |
| N(112) | Cu     | N(21)  | 122.6(2)   | C(29)  | C(28)  | C(27)  | 123.7(7)  |
| N(212) | Cu     | N(21)  | 82.76(19)  | C(213) | C(28)  | C(27)  | 119.7(7)  |
| N(112) | Cu     | N(11)  | 82.6(2)    | C(210) | C(29)  | C(28)  | 120.5(7)  |
| N(212) | Cu     | N(11)  | 123.09(19) | C(36)  | C(31)  | C(32)  | 115.6(5)  |
| N(21)  | Cu     | N(11)  | 117.60(19) | C(36)  | C(31)  | B      | 125.4(5)  |
| C(12)  | N(11)  | C(114) | 119.1(5)   | C(32)  | C(31)  | B      | 118.9(4)  |
| C(12)  | N(11)  | Cu     | 130.5(4)   | C(33)  | C(32)  | C(31)  | 123.4(5)  |
| C(114) | N(11)  | Cu     | 110.4(4)   | C(32)  | C(33)  | C(34)  | 119.8(6)  |
| C(22)  | N(21)  | C(214) | 118.5(5)   | C(32)  | C(33)  | C(331) | 119.7(6)  |
| C(22)  | N(21)  | Cu     | 131.4(4)   | C(34)  | C(33)  | C(331) | 120.4(6)  |
| C(214) | N(21)  | Cu     | 110.0(4)   | C(35)  | C(34)  | C(33)  | 118.2(5)  |
| C(111) | N(112) | C(113) | 120.0(6)   | C(34)  | C(35)  | C(36)  | 120.9(5)  |
| C(111) | N(112) | Cu     | 128.8(5)   | C(34)  | C(35)  | C(351) | 119.4(6)  |
| C(113) | N(112) | Cu     | 111.1(4)   | C(36)  | C(35)  | C(351) | 119.7(7)  |
| C(211) | N(212) | C(213) | 118.2(5)   | C(31)  | C(36)  | C(35)  | 122.0(6)  |
| C(211) | N(212) | Cu     | 130.3(4)   | C(46)  | C(41)  | C(42)  | 114.5(5)  |
| C(213) | N(212) | Cu     | 111.3(4)   | C(46)  | C(41)  | B      | 122.2(4)  |
| N(11)  | C(12)  | C(13)  | 120.8(7)   | C(42)  | C(41)  | B      | 123.1(4)  |
| N(11)  | C(12)  | C(115) | 117.9(6)   | C(43)  | C(42)  | C(41)  | 123.2(5)  |
| C(13)  | C(12)  | C(115) | 121.2(7)   | C(42)  | C(43)  | C(44)  | 119.9(5)  |
| C(14)  | C(13)  | C(12)  | 119.5(8)   | C(42)  | C(43)  | C(431) | 120.1(6)  |
| C(13)  | C(14)  | C(15)  | 121.1(7)   | C(44)  | C(43)  | C(431) | 119.9(6)  |
| C(14)  | C(15)  | C(114) | 116.6(7)   | C(45)  | C(44)  | C(43)  | 118.8(5)  |
| C(14)  | C(15)  | C(16)  | 123.3(8)   | C(44)  | C(45)  | C(46)  | 120.6(5)  |
| C(114) | C(15)  | C(16)  | 120.1(9)   | C(44)  | C(45)  | C(451) | 118.6(6)  |
| C(17)  | C(16)  | C(15)  | 120.2(9)   | C(46)  | C(45)  | C(451) | 120.8(6)  |
| C(16)  | C(17)  | C(18)  | 122.6(9)   | C(45)  | C(46)  | C(41)  | 122.9(5)  |
| C(19)  | C(18)  | C(113) | 117.2(9)   | C(52)  | C(51)  | C(56)  | 115.1(5)  |
| C(19)  | C(18)  | C(17)  | 125.9(9)   | C(52)  | C(51)  | B      | 120.0(4)  |
| C(113) | C(18)  | C(17)  | 116.8(10)  | C(56)  | C(51)  | B      | 124.7(4)  |
| C(110) | C(19)  | C(18)  | 122.3(9)   | C(53)  | C(52)  | C(51)  | 122.5(5)  |
| N(21)  | C(22)  | C(23)  | 122.0(7)   | C(54)  | C(53)  | C(52)  | 120.8(5)  |
| N(21)  | C(22)  | C(215) | 116.4(6)   | C(54)  | C(53)  | C(531) | 120.8(5)  |
| C(23)  | C(22)  | C(215) | 121.5(7)   | C(52)  | C(53)  | C(531) | 118.4(5)  |
| C(24)  | C(23)  | C(22)  | 119.7(8)   | C(55)  | C(54)  | C(53)  | 118.1(5)  |
| C(23)  | C(24)  | C(25)  | 120.8(7)   | C(54)  | C(55)  | C(56)  | 121.4(5)  |
| C(24)  | C(25)  | C(26)  | 125.2(7)   | C(54)  | C(55)  | C(551) | 118.9(5)  |
| C(24)  | C(25)  | C(214) | 116.6(7)   | C(56)  | C(55)  | C(551) | 119.7(5)  |
| C(26)  | C(25)  | C(214) | 118.2(8)   | C(55)  | C(56)  | C(51)  | 121.9(5)  |
| C(27)  | C(26)  | C(25)  | 121.6(7)   | C(62)  | C(61)  | C(66)  | 114.8(5)  |
| C(26)  | C(27)  | C(28)  | 121.3(7)   | C(62)  | C(61)  | B      | 125.5(5)  |
| C(66)  | C(61)  | B      | 119.5(4)   | F(333) | C(331) | F(331) | 109.1(9)  |
| C(61)  | C(62)  | C(63)  | 122.7(5)   | F(333) | C(331) | F(332) | 103.4(8)  |
| C(64)  | C(63)  | C(62)  | 120.0(5)   | F(331) | C(331) | F(332) | 99.3(9)   |
| C(64)  | C(63)  | C(631) | 120.0(6)   | F(333) | C(331) | C(33)  | 117.7(7)  |
| C(62)  | C(63)  | C(631) | 120.0(6)   | F(331) | C(331) | C(33)  | 113.4(7)  |
| C(63)  | C(64)  | C(65)  | 118.3(6)   | F(332) | C(331) | C(33)  | 112.0(7)  |
| C(66)  | C(65)  | C(64)  | 120.9(5)   | F(352) | C(351) | F(351) | 101.7(11) |
| C(66)  | C(65)  | C(651) | 120.7(6)   | F(352) | C(351) | F(353) | 99.1(12)  |
| C(64)  | C(65)  | C(651) | 118.4(6)   | F(351) | C(351) | F(353) | 103.0(10) |

Table 3.9, continued

| Atom 1 | Atom 2 | Atom 3 | Angle     | Atom 1 | Atom 2 | Atom 3 | Angle     |
|--------|--------|--------|-----------|--------|--------|--------|-----------|
| =====  | =====  | =====  | =====     | =====  | =====  | =====  | =====     |
| C(65)  | C(66)  | C(61)  | 123.2(5)  | F(352) | C(351) | C(35)  | 115.9(8)  |
| C(19)  | C(110) | C(111) | 117.8(11) | F(351) | C(351) | C(35)  | 118.1(10) |
| N(112) | C(111) | C(110) | 121.5(9)  | F(353) | C(351) | C(35)  | 116.3(7)  |
| N(112) | C(111) | C(118) | 118.4(6)  | F(433) | C(431) | F(431) | 104.8(9)  |
| C(110) | C(111) | C(118) | 120.0(9)  | F(433) | C(431) | F(432) | 107.3(9)  |
| N(112) | C(113) | C(114) | 118.3(5)  | F(431) | C(431) | F(432) | 104.0(10) |
| N(112) | C(113) | C(18)  | 121.0(8)  | F(433) | C(431) | C(43)  | 110.8(9)  |
| C(114) | C(113) | C(18)  | 120.6(7)  | F(431) | C(431) | C(43)  | 114.8(7)  |
| N(11)  | C(114) | C(15)  | 122.9(7)  | F(432) | C(431) | C(43)  | 114.4(8)  |
| N(11)  | C(114) | C(113) | 117.4(5)  | F(452) | C(451) | F(453) | 110.9(9)  |
| C(15)  | C(114) | C(113) | 119.7(7)  | F(452) | C(451) | F(451) | 101.8(8)  |
| C(116) | C(115) | C(117) | 108.6(13) | F(453) | C(451) | F(451) | 95.1(9)   |
| C(116) | C(115) | C(12)  | 113.5(9)  | F(452) | C(451) | C(45)  | 117.1(8)  |
| C(117) | C(115) | C(12)  | 111.9(8)  | F(453) | C(451) | C(45)  | 116.4(6)  |
| C(111) | C(118) | C(120) | 109.6(11) | F(451) | C(451) | C(45)  | 112.4(7)  |
| C(111) | C(118) | C(119) | 107.5(11) | F(533) | C(531) | F(532) | 110.8(8)  |
| C(120) | C(118) | C(119) | 112.0(12) | F(533) | C(531) | F(531) | 108.8(8)  |
| C(29)  | C(210) | C(211) | 120.3(8)  | F(532) | C(531) | F(531) | 100.7(7)  |
| N(212) | C(211) | C(210) | 121.1(7)  | F(533) | C(531) | C(53)  | 113.4(8)  |
| N(212) | C(211) | C(218) | 118.3(5)  | F(532) | C(531) | C(53)  | 111.6(6)  |
| C(210) | C(211) | C(218) | 120.6(7)  | F(531) | C(531) | C(53)  | 110.9(7)  |
| N(212) | C(213) | C(28)  | 123.3(6)  | F(552) | C(551) | F(553) | 106.4(7)  |
| N(212) | C(213) | C(214) | 118.0(5)  | F(552) | C(551) | F(551) | 107.0(8)  |
| C(28)  | C(213) | C(214) | 118.7(6)  | F(553) | C(551) | F(551) | 102.3(7)  |
| N(21)  | C(214) | C(25)  | 122.3(6)  | F(552) | C(551) | C(55)  | 113.3(6)  |
| N(21)  | C(214) | C(213) | 117.2(5)  | F(553) | C(551) | C(55)  | 112.2(7)  |
| C(25)  | C(214) | C(213) | 120.5(6)  | F(551) | C(551) | C(55)  | 114.7(6)  |
| C(217) | C(215) | C(22)  | 114.2(8)  | F(631) | C(631) | F(632) | 107.6(10) |
| C(217) | C(215) | C(216) | 110.4(9)  | F(631) | C(631) | F(633) | 104.0(10) |
| C(22)  | C(215) | C(216) | 110.0(8)  | F(632) | C(631) | F(633) | 95.4(7)   |
| C(211) | C(218) | C(220) | 112.7(8)  | F(631) | C(631) | C(63)  | 117.9(6)  |
| C(211) | C(218) | C(219) | 111.9(8)  | F(632) | C(631) | C(63)  | 114.8(7)  |
| C(220) | C(218) | C(219) | 110.9(10) | F(633) | C(631) | C(63)  | 114.5(8)  |
| F(651) | C(651) | F(653) | 105.4(11) | C(41)  | B      | C(61)  | 113.4(4)  |
| F(651) | C(651) | F(652) | 104.6(11) | C(41)  | B      | C(31)  | 104.8(4)  |
| F(653) | C(651) | F(652) | 99.0(11)  | C(61)  | B      | C(31)  | 111.5(4)  |
| F(651) | C(651) | C(65)  | 120.4(8)  | C(41)  | B      | C(51)  | 114.1(4)  |
| F(653) | C(651) | C(65)  | 113.4(10) | C(61)  | B      | C(51)  | 104.7(4)  |
| F(652) | C(651) | C(65)  | 111.5(9)  | C(31)  | B      | C(51)  | 108.4(4)  |

### [Cu(dptmp)<sub>2</sub>]<sup>+</sup>PF<sub>6</sub><sup>-</sup>·THF

A view of the [Cu(dptmp)<sub>2</sub>]<sup>+</sup>PF<sub>6</sub><sup>-</sup>·THF cation, along with the atomic labeling scheme, is shown in Figure 3.5. The positional and thermal parameters, bond distances, and bond angles are shown in Tables 3.10, 3.11, and 3.12, respectively. The crystal structure of this 2,9 aryl substituted phenanthroline complex looks on the surface like other aryl substituted phenanthrolines.<sup>21, 22, 26</sup> This compound shows a very distorted geometry around the copper center with one long, one short, and two average Cu-N bond distances. This type of arrangement has been seen in both of the crystal structures of [Cu(dpp)<sub>2</sub>]<sup>+</sup>,<sup>21, 22</sup> however, the dptmp complex shows the greatest difference between the long and the short bonds (0.157 Å for dptmp, 0.093 Å for [Cu(dpp)<sub>2</sub>]<sup>+</sup>PF<sub>6</sub><sup>-</sup>,<sup>22</sup> and 0.137 Å for [Cu(dpp)<sub>2</sub>]<sup>+</sup>CuCl<sub>2</sub>.<sup>21</sup>). This uneven bonding leads to chelate-bite angles that are uneven, as if one of the dptmp ligands was trying to back away. This type of distortion was not seen in the dpp structures.<sup>21, 22</sup> Another interesting feature of this crystal structure is its rather large dihedral angle, see Figure 3.6. This is most likely a steric consequence caused by the lock placed on the phenyl rings by the peripheral methyl groups.<sup>11</sup> Indeed, the torsion angles between the phenyl groups and the phenanthroline backbone are much larger for dptmp than any other aryl substituted phenanthroline. For dptmp, the phenyl-phenanthroline torsion angles are 73.38°, 99.53°, -52.30°, and 81.49°, whereas in the dpp structures, the phenyl torsion angles all lie in the range of 40-70°.<sup>21, 22</sup> The rather large angles indicate an almost perpendicular arrangement with the ligand backbone and a lack of  $\pi$ -conjugation. The smaller angles indicate some twisting and probably cause the larger distortions seen in the coordination geometry around the copper center.<sup>21, 22</sup> Figures 3.6, 3.7, and 3.8 show different views of the [Cu(dptmp)<sub>2</sub>]<sup>+</sup> cation that show the phenyl torsion angles and the displacements present in the coordination geometry. For [Cu(dpp)<sub>2</sub>]<sup>+</sup>, the phenyl-phenanthroline torsion angles fall in the range of 50-60°, depending on the amount of interligand  $\pi$ -overlap and intraligand  $\pi$ -conjugation.<sup>21, 22, 26</sup>

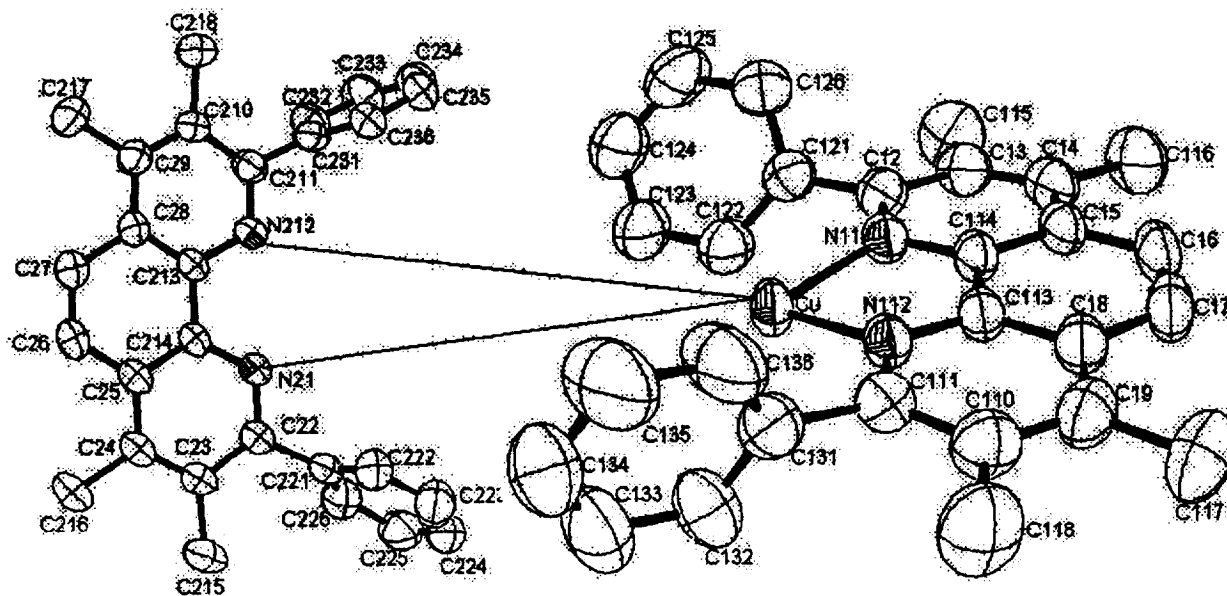


Figure 3.5. ORTEP drawing of the  $[\text{Cu}(\text{dptmp})_2]^+$  cation with atomic labeling scheme and 50% ellipsoids. One of the dptmp ligands has been pulled out from the metal center for ease of viewing. Additionally, the hydrogen atoms have been omitted for clarity.

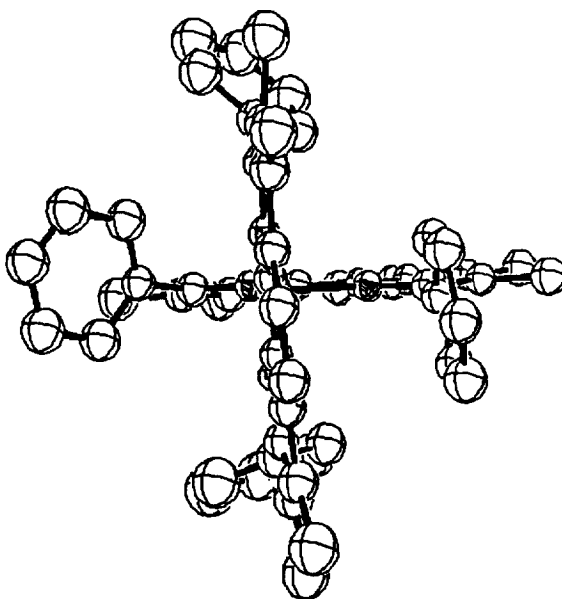


Figure 3.6. ORTEP drawing of the  $[\text{Cu}(\text{dptmp})_2]^+$  cation from behind one of the phenanthroline ligands.

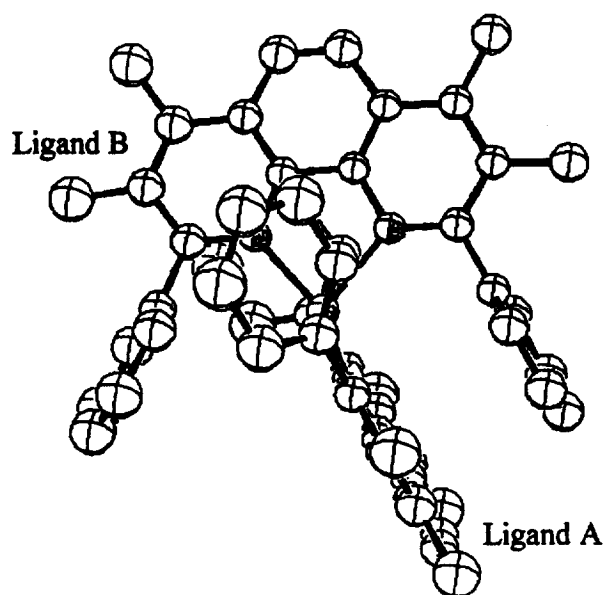


Figure 3.7. ORTEP drawing of the  $[\text{Cu}(\text{dptmp})_2]^+$  cation looking down onto one phenanthroline ligand.

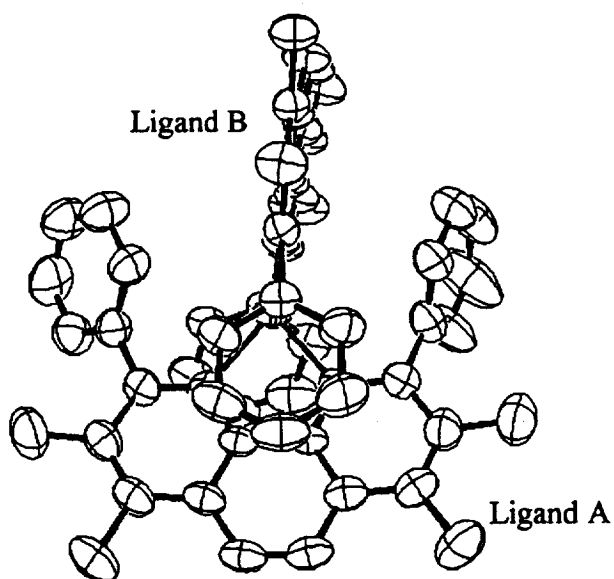


Figure 3.8. ORTEP drawing of the  $[\text{Cu}(\text{dptmp})_2]^+$  cation looking down onto one phenanthroline ligand.



Table 3.10. Positional and temperature parameters ( $\text{\AA}^2$ ) for  $[\text{Cu}(\text{dptmp})_2]\text{PF}_6 \cdot \text{THF}$ .

| Atom    | x            | y             | z            | U ( $\text{\AA}^2$ ) <sup>a</sup> |
|---------|--------------|---------------|--------------|-----------------------------------|
| ----    | ---          | ---           | ---          | -----                             |
| Cu      | 0.14447 (3)  | 0.19769 (3)   | 0.27160 (3)  | 0.05238 (16)                      |
| P (1)   | 0.51069 (14) | -0.20560 (13) | 0.21604 (13) | 0.1007 (6)                        |
| F (1)   | 0.4909 (6)   | -0.3152 (4)   | 0.1802 (7)   | 0.272 (5)                         |
| F (2)   | 0.4216 (7)   | -0.1896 (8)   | 0.1541 (7)   | 0.332 (6)                         |
| F (3)   | 0.5854 (6)   | -0.1864 (9)   | 0.1531 (5)   | 0.312 (6)                         |
| F (4)   | 0.6104 (6)   | -0.2178 (6)   | 0.2782 (4)   | 0.233 (4)                         |
| F (5)   | 0.4421 (11)  | -0.2245 (6)   | 0.2845 (8)   | 0.351 (7)                         |
| F (6)   | 0.5258 (5)   | -0.0954 (4)   | 0.2697 (4)   | 0.194 (3)                         |
| O (301) | 0.2337 (6)   | 0.4909 (8)    | 0.8560 (6)   | 0.208 (4)                         |
| N (11)  | 0.0589 (2)   | 0.1986 (2)    | 0.14837 (19) | 0.0480 (8)                        |
| N (21)  | 0.2832 (2)   | 0.2580 (2)    | 0.34572 (19) | 0.0497 (8)                        |
| N (112) | 0.0740 (2)   | 0.0522 (2)    | 0.24421 (18) | 0.0475 (8)                        |
| N (212) | 0.0868 (2)   | 0.2723 (2)    | 0.38816 (18) | 0.0463 (8)                        |
| C (12)  | 0.0522 (3)   | 0.2733 (3)    | 0.1018 (3)   | 0.0546 (11)                       |
| C (13)  | -0.0257 (3)  | 0.2653 (3)    | 0.0250 (3)   | 0.0626 (13)                       |
| C (14)  | -0.0921 (3)  | 0.1767 (3)    | -0.0065 (3)  | 0.0624 (13)                       |
| C (15)  | -0.0837 (3)  | 0.0962 (3)    | 0.0401 (2)   | 0.0546 (10)                       |
| C (16)  | -0.1509 (3)  | 0.0016 (3)    | 0.0154 (3)   | 0.0651 (13)                       |
| C (17)  | -0.1468 (3)  | -0.0691 (3)   | 0.0656 (3)   | 0.0672 (13)                       |
| C (18)  | -0.0725 (3)  | -0.0571 (3)   | 0.1462 (3)   | 0.0583 (11)                       |
| C (19)  | -0.0672 (3)  | -0.1283 (3)   | 0.2032 (3)   | 0.0679 (13)                       |
| C (22)  | 0.3800 (3)   | 0.2464 (3)    | 0.3256 (2)   | 0.0581 (12)                       |
| C (23)  | 0.4737 (3)   | 0.2832 (4)    | 0.3875 (3)   | 0.0707 (13)                       |
| C (24)  | 0.4655 (3)   | 0.3342 (3)    | 0.4727 (3)   | 0.0654 (13)                       |
| C (25)  | 0.3640 (3)   | 0.3492 (3)    | 0.4942 (3)   | 0.0575 (10)                       |
| C (26)  | 0.3469 (3)   | 0.4033 (4)    | 0.5785 (3)   | 0.0707 (13)                       |
| C (27)  | 0.2503 (3)   | 0.4180 (3)    | 0.5971 (3)   | 0.0667 (13)                       |
| C (28)  | 0.1559 (3)   | 0.3756 (3)    | 0.5334 (2)   | 0.0505 (10)                       |
| C (29)  | 0.0528 (3)   | 0.3868 (3)    | 0.5512 (2)   | 0.0511 (10)                       |
| C (110) | 0.0105 (4)   | -0.1083 (3)   | 0.2783 (3)   | 0.0713 (16)                       |
| C (111) | 0.0813 (3)   | -0.0174 (3)   | 0.2954 (3)   | 0.0583 (11)                       |
| C (113) | -0.0014 (3)  | 0.0331 (3)    | 0.1707 (2)   | 0.0489 (10)                       |
| C (114) | -0.0084 (3)  | 0.1120 (3)    | 0.1178 (2)   | 0.0484 (10)                       |
| C (115) | -0.0364 (5)  | 0.3577 (4)    | -0.0171 (4)  | 0.096 (2)                         |
| C (116) | -0.1762 (4)  | 0.1641 (5)    | -0.0881 (3)  | 0.091 (2)                         |
| C (117) | -0.1443 (5)  | -0.2238 (4)   | 0.1824 (5)   | 0.100 (2)                         |
| C (118) | 0.0202 (5)   | -0.1805 (4)   | 0.3425 (4)   | 0.103 (2)                         |
| C (121) | 0.1291 (3)   | 0.3653 (3)    | 0.1376 (3)   | 0.0590 (11)                       |
| C (122) | 0.1395 (4)   | 0.4111 (3)    | 0.2269 (3)   | 0.0695 (14)                       |
| C (123) | 0.2143 (4)   | 0.4955 (4)    | 0.2617 (4)   | 0.088 (2)                         |
| C (124) | 0.2785 (5)   | 0.5359 (4)    | 0.2084 (4)   | 0.098 (2)                         |
| C (125) | 0.2699 (5)   | 0.4917 (4)    | 0.1198 (4)   | 0.098 (2)                         |
| C (126) | 0.1967 (4)   | 0.4079 (4)    | 0.0828 (3)   | 0.0796 (16)                       |
| C (131) | 0.1711 (3)   | 0.0065 (3)    | 0.3723 (3)   | 0.0669 (13)                       |
| C (132) | 0.1626 (4)   | 0.0669 (4)    | 0.4522 (3)   | 0.0794 (18)                       |
| C (133) | 0.2465 (5)   | 0.0907 (5)    | 0.5211 (4)   | 0.099 (2)                         |
| C (134) | 0.3370 (5)   | 0.0539 (7)    | 0.5113 (5)   | 0.128 (3)                         |
| C (135) | 0.3458 (6)   | -0.0122 (8)   | 0.4318 (5)   | 0.157 (4)                         |
| C (136) | 0.2632 (5)   | -0.0327 (6)   | 0.3634 (4)   | 0.116 (3)                         |
| C (210) | -0.0318 (3)  | 0.3359 (3)    | 0.4878 (2)   | 0.0502 (10)                       |
| C (211) | -0.0114 (3)  | 0.2774 (3)    | 0.4079 (2)   | 0.0476 (10)                       |

Table 3.10, continued

| Atom   | x           | y           | z           | U (Å <sup>2</sup> ) <sup>a</sup> |
|--------|-------------|-------------|-------------|----------------------------------|
| C(213) | 0.1701 (3)  | 0.3206 (2)  | 0.4506 (2)  | 0.0456 (9)                       |
| C(214) | 0.2753 (3)  | 0.3093 (3)  | 0.4290 (2)  | 0.0498 (10)                      |
| C(215) | 0.5803 (4)  | 0.2650 (5)  | 0.3597 (4)  | 0.109 (2)                        |
| C(216) | 0.5634 (3)  | 0.3727 (5)  | 0.5420 (3)  | 0.0895 (19)                      |
| C(217) | 0.0352 (4)  | 0.4517 (3)  | 0.6366 (3)  | 0.0684 (14)                      |
| C(218) | -0.1453 (3) | 0.3429 (4)  | 0.5031 (3)  | 0.0693 (14)                      |
| C(221) | 0.3865 (3)  | 0.1978 (3)  | 0.2310 (3)  | 0.0596 (12)                      |
| C(222) | 0.3709 (4)  | 0.2519 (4)  | 0.1626 (3)  | 0.0749 (14)                      |
| C(223) | 0.3852 (4)  | 0.2139 (5)  | 0.0753 (3)  | 0.090 (2)                        |
| C(224) | 0.4135 (4)  | 0.1202 (5)  | 0.0560 (4)  | 0.091 (2)                        |
| C(225) | 0.4264 (4)  | 0.0642 (5)  | 0.1217 (4)  | 0.095 (2)                        |
| C(226) | 0.4131 (4)  | 0.1033 (4)  | 0.2099 (3)  | 0.0816 (18)                      |
| C(231) | -0.0993 (3) | 0.2150 (3)  | 0.3415 (2)  | 0.0512 (10)                      |
| C(232) | -0.1448 (3) | 0.1237 (3)  | 0.3582 (3)  | 0.0693 (14)                      |
| C(233) | -0.2278 (4) | 0.0652 (4)  | 0.2974 (4)  | 0.0795 (16)                      |
| C(234) | -0.2660 (3) | 0.0972 (4)  | 0.2219 (3)  | 0.0783 (15)                      |
| C(235) | -0.2226 (3) | 0.1876 (4)  | 0.2052 (3)  | 0.0775 (15)                      |
| C(236) | -0.1391 (3) | 0.2465 (3)  | 0.2642 (3)  | 0.0621 (13)                      |
| C(302) | 0.2586 (10) | 0.5817 (9)  | 0.8681 (14) | 0.298 (13)                       |
| C(303) | 0.3620 (11) | 0.6198 (10) | 0.8954 (17) | 0.348 (13)                       |
| C(304) | 0.4180 (8)  | 0.5414 (9)  | 0.8782 (12) | 0.240 (10)                       |
| C(305) | 0.3401 (10) | 0.4548 (9)  | 0.8637 (9)  | 0.184 (6)                        |

a  $U_{eq} = (1/3) \sum_i \sum_j U_{ij} a_i^* a_j^* a_i a_j$

Table 3.11. Bond distances (Å) for [Cu(dptmp)<sub>2</sub>]PF<sub>6</sub>·THF. Numbers in parentheses are estimated standard deviations in the least significant digits.

| Atom 1 | Atom 2 | Distance | Atom 1 | Atom 2 | Distance  |
|--------|--------|----------|--------|--------|-----------|
| =====  | =====  | =====    | =====  | =====  | =====     |
| Cu     | N(21)  | 1.993(3) | C(28)  | C(213) | 1.396(5)  |
| Cu     | N(112) | 2.039(3) | C(28)  | C(29)  | 1.405(5)  |
| Cu     | N(11)  | 2.058(3) | C(29)  | C(210) | 1.390(5)  |
| Cu     | N(212) | 2.150(3) | C(29)  | C(217) | 1.503(5)  |
| P(1)   | F(2)   | 1.457(6) | C(110) | C(111) | 1.415(6)  |
| P(1)   | F(3)   | 1.461(6) | C(110) | C(118) | 1.508(6)  |
| P(1)   | F(5)   | 1.472(7) | C(111) | C(131) | 1.503(5)  |
| P(1)   | F(1)   | 1.491(6) | C(113) | C(114) | 1.458(5)  |
| P(1)   | F(4)   | 1.543(6) | C(121) | C(122) | 1.378(6)  |
| P(1)   | F(6)   | 1.570(5) | C(121) | C(126) | 1.411(6)  |
| N(11)  | C(12)  | 1.345(5) | C(123) | C(124) | 1.353(7)  |
| N(11)  | C(114) | 1.355(4) | C(123) | C(122) | 1.393(6)  |
| N(21)  | C(22)  | 1.337(5) | C(124) | C(125) | 1.365(8)  |
| N(21)  | C(214) | 1.362(4) | C(125) | C(126) | 1.381(7)  |
| N(112) | C(111) | 1.334(5) | C(131) | C(136) | 1.374(7)  |
| N(112) | C(113) | 1.355(4) | C(131) | C(132) | 1.375(7)  |
| N(212) | C(211) | 1.339(4) | C(132) | C(133) | 1.376(7)  |
| N(212) | C(213) | 1.362(4) | C(133) | C(134) | 1.339(9)  |
| C(12)  | C(13)  | 1.423(5) | C(134) | C(135) | 1.409(11) |
| C(12)  | C(121) | 1.481(5) | C(135) | C(136) | 1.360(8)  |
| C(13)  | C(14)  | 1.371(6) | C(232) | C(231) | 1.390(6)  |
| C(13)  | C(115) | 1.528(6) | C(232) | C(233) | 1.392(6)  |
| C(14)  | C(15)  | 1.416(6) | C(210) | C(211) | 1.410(5)  |
| C(14)  | C(116) | 1.517(5) | C(210) | C(218) | 1.516(5)  |
| C(15)  | C(114) | 1.402(5) | C(211) | C(231) | 1.490(5)  |
| C(15)  | C(16)  | 1.432(6) | C(213) | C(214) | 1.449(5)  |
| C(16)  | C(17)  | 1.332(6) | C(221) | C(226) | 1.381(6)  |
| C(17)  | C(18)  | 1.433(6) | C(221) | C(222) | 1.383(6)  |
| C(18)  | C(113) | 1.408(5) | C(222) | C(223) | 1.383(7)  |
| C(18)  | C(19)  | 1.412(6) | C(223) | C(224) | 1.375(8)  |
| C(19)  | C(110) | 1.388(6) | C(224) | C(225) | 1.364(8)  |
| C(19)  | C(117) | 1.503(6) | C(225) | C(226) | 1.395(7)  |
| C(22)  | C(23)  | 1.417(5) | C(231) | C(236) | 1.382(5)  |
| C(22)  | C(221) | 1.495(5) | C(233) | C(234) | 1.356(7)  |
| C(23)  | C(24)  | 1.387(6) | C(234) | C(235) | 1.370(7)  |
| C(23)  | C(215) | 1.517(6) | C(235) | C(236) | 1.386(6)  |
| C(24)  | C(25)  | 1.412(6) | O(301) | C(302) | 1.225(12) |
| C(24)  | C(216) | 1.518(5) | O(301) | C(305) | 1.511(12) |
| C(25)  | C(214) | 1.405(5) | C(304) | C(303) | 1.375(18) |
| C(25)  | C(26)  | 1.424(6) | C(304) | C(305) | 1.423(13) |
| C(26)  | C(27)  | 1.336(6) | C(302) | C(303) | 1.354(14) |
| C(27)  | C(28)  | 1.450(5) |        |        |           |

Table 3.12. Bond angles (deg.) for  $[\text{Cu}(\text{dptmp})_2]\text{PF}_6 \cdot \text{THF}$ . Numbers in parentheses are estimated standard deviations in the least significant digits.

| Atom 1 | Atom 2 | Atom 3 | Angle      | Atom 1 | Atom 2 | Atom 3 | Angle    |
|--------|--------|--------|------------|--------|--------|--------|----------|
| =====  | =====  | =====  | =====      | =====  | =====  | =====  | =====    |
| N(21)  | Cu     | N(112) | 128.85(12) | C(114) | C(15)  | C(14)  | 117.8(4) |
| N(21)  | Cu     | N(11)  | 140.15(12) | C(114) | C(15)  | C(16)  | 118.1(4) |
| N(112) | Cu     | N(11)  | 81.82(11)  | C(14)  | C(15)  | C(16)  | 124.1(3) |
| N(21)  | Cu     | N(212) | 81.23(11)  | C(17)  | C(16)  | C(15)  | 122.2(4) |
| N(112) | Cu     | N(212) | 108.22(11) | C(16)  | C(17)  | C(18)  | 122.3(4) |
| N(11)  | Cu     | N(212) | 116.18(11) | C(113) | C(18)  | C(19)  | 118.1(3) |
| F(2)   | P(1)   | F(3)   | 92.1(6)    | C(113) | C(18)  | C(17)  | 117.3(4) |
| F(2)   | P(1)   | F(5)   | 91.9(7)    | C(19)  | C(18)  | C(17)  | 124.5(4) |
| F(3)   | P(1)   | F(5)   | 175.9(7)   | C(110) | C(19)  | C(18)  | 118.7(4) |
| F(2)   | P(1)   | F(1)   | 91.5(5)    | C(110) | C(19)  | C(117) | 121.0(4) |
| F(3)   | P(1)   | F(1)   | 93.0(6)    | C(18)  | C(19)  | C(117) | 120.3(4) |
| F(5)   | P(1)   | F(1)   | 87.8(5)    | N(21)  | C(22)  | C(23)  | 123.0(3) |
| F(2)   | P(1)   | F(4)   | 175.9(6)   | N(21)  | C(22)  | C(221) | 116.6(3) |
| F(3)   | P(1)   | F(4)   | 84.1(5)    | C(23)  | C(22)  | C(221) | 120.3(3) |
| F(5)   | P(1)   | F(4)   | 91.8(7)    | C(24)  | C(23)  | C(22)  | 118.9(4) |
| F(1)   | P(1)   | F(4)   | 90.4(5)    | C(24)  | C(23)  | C(215) | 121.5(4) |
| F(2)   | P(1)   | F(6)   | 92.5(4)    | C(22)  | C(23)  | C(215) | 119.6(4) |
| F(3)   | P(1)   | F(6)   | 96.2(5)    | C(23)  | C(24)  | C(25)  | 118.8(3) |
| F(5)   | P(1)   | F(6)   | 82.8(4)    | C(23)  | C(24)  | C(216) | 120.8(4) |
| F(1)   | P(1)   | F(6)   | 169.8(5)   | C(25)  | C(24)  | C(216) | 120.4(4) |
| F(4)   | P(1)   | F(6)   | 86.2(4)    | C(214) | C(25)  | C(24)  | 118.5(3) |
| C(12)  | N(11)  | C(114) | 118.0(3)   | C(214) | C(25)  | C(26)  | 118.2(3) |
| C(12)  | N(11)  | Cu     | 130.1(2)   | C(24)  | C(25)  | C(26)  | 123.4(3) |
| C(114) | N(11)  | Cu     | 111.5(2)   | C(27)  | C(26)  | C(25)  | 122.5(3) |
| C(22)  | N(21)  | C(214) | 118.0(3)   | C(26)  | C(27)  | C(28)  | 121.6(4) |
| C(22)  | N(21)  | Cu     | 127.4(2)   | C(213) | C(28)  | C(29)  | 119.4(3) |
| C(214) | N(21)  | Cu     | 114.3(2)   | C(213) | C(28)  | C(27)  | 117.3(3) |
| C(111) | N(112) | C(113) | 118.6(3)   | C(29)  | C(28)  | C(27)  | 123.4(3) |
| C(111) | N(112) | Cu     | 128.5(2)   | C(210) | C(29)  | C(28)  | 118.0(3) |
| C(113) | N(112) | Cu     | 112.0(2)   | C(210) | C(29)  | C(217) | 121.3(3) |
| C(211) | N(212) | C(213) | 118.3(3)   | C(28)  | C(29)  | C(217) | 120.7(3) |
| C(211) | N(212) | Cu     | 131.9(2)   | C(19)  | C(110) | C(111) | 119.1(4) |
| C(213) | N(212) | Cu     | 109.7(2)   | C(19)  | C(110) | C(118) | 121.6(4) |
| N(11)  | C(12)  | C(13)  | 122.0(4)   | C(111) | C(110) | C(118) | 119.3(4) |
| N(11)  | C(12)  | C(121) | 115.4(3)   | N(112) | C(111) | C(110) | 122.6(4) |
| C(13)  | C(12)  | C(121) | 122.5(4)   | N(112) | C(111) | C(131) | 115.5(3) |
| C(14)  | C(13)  | C(12)  | 119.5(4)   | C(110) | C(111) | C(131) | 121.9(4) |
| C(14)  | C(13)  | C(115) | 121.8(4)   | N(112) | C(113) | C(18)  | 122.8(3) |
| C(12)  | C(13)  | C(115) | 118.6(4)   | N(112) | C(113) | C(114) | 116.8(3) |
| C(13)  | C(14)  | C(15)  | 119.1(3)   | C(18)  | C(113) | C(114) | 120.4(3) |
| C(13)  | C(14)  | C(116) | 121.6(4)   | N(11)  | C(114) | C(15)  | 123.5(3) |
| C(15)  | C(14)  | C(116) | 119.3(4)   | N(11)  | C(114) | C(113) | 116.9(3) |
| C(15)  | C(114) | C(113) | 119.6(3)   | C(28)  | C(213) | C(214) | 121.0(3) |
| C(122) | C(121) | C(126) | 117.3(4)   | N(21)  | C(214) | C(25)  | 122.8(3) |
| C(122) | C(121) | C(12)  | 121.1(4)   | N(21)  | C(214) | C(213) | 117.7(3) |
| C(126) | C(121) | C(12)  | 121.6(4)   | C(25)  | C(214) | C(213) | 119.5(3) |
| C(124) | C(123) | C(122) | 120.8(5)   | C(226) | C(221) | C(222) | 118.7(4) |
| C(123) | C(124) | C(125) | 118.9(5)   | C(226) | C(221) | C(22)  | 122.6(4) |
| C(124) | C(125) | C(126) | 122.0(5)   | C(222) | C(221) | C(22)  | 118.6(4) |

Table 3.12, continued

| Atom 1 | Atom 2 | Atom 3 | Angle    | Atom 1 | Atom 2 | Atom 3 | Angle     |
|--------|--------|--------|----------|--------|--------|--------|-----------|
| =====  | =====  | =====  | =====    | =====  | =====  | =====  | =====     |
| C(125) | C(126) | C(121) | 119.7(5) | C(223) | C(222) | C(221) | 120.9(5)  |
| C(136) | C(131) | C(132) | 119.0(4) | C(224) | C(223) | C(222) | 119.4(5)  |
| C(136) | C(131) | C(111) | 120.0(4) | C(225) | C(224) | C(223) | 120.8(5)  |
| C(132) | C(131) | C(111) | 121.1(4) | C(224) | C(225) | C(226) | 119.6(5)  |
| C(131) | C(132) | C(133) | 120.5(5) | C(221) | C(226) | C(225) | 120.5(5)  |
| C(134) | C(133) | C(132) | 120.2(6) | C(236) | C(231) | C(232) | 118.6(4)  |
| C(133) | C(134) | C(135) | 120.4(6) | C(236) | C(231) | C(211) | 121.7(3)  |
| C(136) | C(135) | C(134) | 118.6(7) | C(232) | C(231) | C(211) | 119.7(3)  |
| C(135) | C(136) | C(131) | 121.2(6) | C(121) | C(122) | C(123) | 121.3(4)  |
| C(231) | C(232) | C(233) | 120.3(4) | C(234) | C(233) | C(232) | 120.4(4)  |
| C(29)  | C(210) | C(211) | 119.3(3) | C(233) | C(234) | C(235) | 119.8(4)  |
| C(29)  | C(210) | C(218) | 121.0(3) | C(234) | C(235) | C(236) | 120.8(4)  |
| C(211) | C(210) | C(218) | 119.6(3) | C(231) | C(236) | C(235) | 120.1(4)  |
| N(212) | C(211) | C(210) | 122.5(3) | C(302) | O(301) | C(305) | 102.5(9)  |
| N(212) | C(211) | C(231) | 116.2(3) | C(303) | C(304) | C(305) | 104.4(10) |
| C(210) | C(211) | C(231) | 121.3(3) | O(301) | C(302) | C(303) | 117.8(11) |
| N(212) | C(213) | C(28)  | 122.2(3) | C(304) | C(305) | O(301) | 106.4(9)  |
| N(212) | C(213) | C(214) | 116.8(3) | C(302) | C(303) | C(304) | 106.3(13) |

## Absorbance

Tables 3.13-3.15 contain all of the solid state absorbance data as well as dihedral angle values for all of the compounds used in this study. The data has been roughly divided into three categories. The first is the parent group. This group contains compounds with ligands that contain only hydrogen atoms in the 2 and 9 positions of the phenanthroline (or 6 and 6' of bipyridine) ligand. There may be substitution at other places on the ligand, but only the 2,9 positions are being considered. The second group is referred to as the alkyl group. This group contains ligands with alkyl groups in the 2 and 9 positions of the phenanthroline (or 6 and 6' of bipyridine) ligand. Again, this group may have other substituents on the ligands, but only the positions directly adjacent to the chelating nitrogens are being considered. The third and final group is the aryl group. This group contains molecules with aryl functionalities in the positions adjacent to the nitrogen atoms.

Table 3.13. Absorbance and dihedral angle data for the parent group.

| Compound                                 | CH <sub>2</sub> Cl <sub>2</sub> Abs (nm) | Solid Abs (nm) | $\Theta_z$ (deg) | $\Theta_z$ Ref. |
|------------------------------------------|------------------------------------------|----------------|------------------|-----------------|
| [Cu(phen) <sub>2</sub> ]ClO <sub>4</sub> | 435                                      | 620            | 49.9             | 8               |
| [Cu(phen) <sub>2</sub> ]BPh <sub>4</sub> | 435                                      | 480, 550       |                  |                 |
| [Cu(tmp) <sub>2</sub> ]PF <sub>6</sub>   | 430                                      | 575            |                  |                 |
| [Cu(tmp) <sub>2</sub> ]BPh <sub>4</sub>  | 430                                      | 450, 485       | 81.9             | this work       |
| [Cu(bipy) <sub>2</sub> ]ClO <sub>4</sub> |                                          | 460, 530       | 75.2             | 27              |
| [Cu(bipy) <sub>2</sub> ]BPh <sub>4</sub> |                                          | 475, 550       |                  |                 |

Table 3.14. Absorbance and dihedral angle data for the aryl group.

| Compound                                 | CH <sub>2</sub> Cl <sub>2</sub> Abs (nm) | Solid Abs (nm) | $\Theta_z$ (deg)    | $\Theta_z$ Ref. |
|------------------------------------------|------------------------------------------|----------------|---------------------|-----------------|
| [Cu(dpp) <sub>2</sub> ]BF <sub>4</sub>   | 441, 560                                 | 475, 540       | (71.8) <sup>a</sup> | 20              |
| [Cu(dpp) <sub>2</sub> ]PF <sub>6</sub>   | 441, 560                                 | 475, 540       | 79.8                | 21              |
| [Cu(dpp) <sub>2</sub> ]TFPB              | 441, 560                                 | 450, 550       |                     |                 |
| [Cu(dpdp) <sub>2</sub> ]PF <sub>6</sub>  | 440, 550                                 | 425, 530       |                     |                 |
| [Cu(dptmp) <sub>2</sub> ]PF <sub>6</sub> | 467                                      | 490            | 87.8                | this work       |
| [Cu(dptmp) <sub>2</sub> ]TFPB            | 467                                      | 480            |                     |                 |

<sup>a</sup> Data extrapolated from the value for [Cu(dpp)<sub>2</sub>]CuCl<sub>2</sub>

Table 3.15. Absorbance and dihedral angle data for the alkyl group.

| Compound                                 | CH <sub>2</sub> Cl <sub>2</sub> Abs (nm) | Solid Abs (nm) | $\Theta_z$ (deg)        | $\Theta_z$ Ref. |
|------------------------------------------|------------------------------------------|----------------|-------------------------|-----------------|
| [Cu(dmp) <sub>2</sub> ]Br                | 455                                      | 475, 550       | 79.9                    | 3               |
| [Cu(dmp) <sub>2</sub> ]NO <sub>3</sub>   | 455                                      | 475, 550       | 72.4, 85.4 <sup>a</sup> | 6               |
| [Cu(dmp) <sub>2</sub> ]ClO <sub>4</sub>  | 455                                      | 460, 545       | 81.8                    | 5               |
| [Cu(dmp) <sub>2</sub> ]TFPB              | 455                                      | 460            |                         |                 |
| [Cu(bcp) <sub>2</sub> ]BF <sub>4</sub>   | 479                                      | 480            | 88.1                    | 20              |
| [Cu(bcp) <sub>2</sub> ]BPh <sub>4</sub>  | 479                                      | 480, 560       |                         |                 |
| [Cu(dbp) <sub>2</sub> ]PF <sub>6</sub>   | 457                                      | 470            | (87.4) <sup>b</sup>     | 9               |
| [Cu(dbdmp) <sub>2</sub> ]PF <sub>6</sub> | 456                                      | 470            |                         |                 |
| [Cu(dbtmp) <sub>2</sub> ]PF <sub>6</sub> | 453                                      | 460            |                         |                 |
| [Cu(dnpp) <sub>2</sub> ]PF <sub>6</sub>  | 449                                      | 425, 550       | 66.3                    | 4               |
| [Cu(dipp) <sub>2</sub> ]Cl               | 445                                      | 460            |                         |                 |
| [Cu(dipp) <sub>2</sub> ]PF <sub>6</sub>  | 445                                      | 460            |                         |                 |
| [Cu(dipp) <sub>2</sub> ]TFPB             | 445                                      | 465            | 88.9                    | this work       |
| [Cu(dryp) <sub>2</sub> ]PF <sub>6</sub>  | 457                                      | 470            |                         |                 |
| [Cu(dsbp) <sub>2</sub> ]Cl               | 455                                      | 460            |                         |                 |
| [Cu(dsbp) <sub>2</sub> ]PF <sub>6</sub>  | 455                                      | 470, 515       |                         |                 |
| [Cu(dmbp) <sub>2</sub> ]BF <sub>4</sub>  |                                          | 450, 550       | 80.8                    | 28              |
| [Cu(dmbp) <sub>2</sub> ]BPh <sub>4</sub> |                                          | 485            |                         |                 |
| [Cu(tmbp) <sub>2</sub> ]BF <sub>4</sub>  |                                          | 440, 540       |                         |                 |
| [Cu(tmbp) <sub>2</sub> ]ClO <sub>4</sub> |                                          | 440, 540       | 75.0                    | 29              |

a This nitrate salt was a dihydrate

b Data extrapolated from [Cu(di-*n*-pentyl-phen)<sub>2</sub>]CuCl<sub>2</sub>

An overlay of the solid state absorbance spectra for  $[\text{Cu}(\text{phen})_2]\text{ClO}_4$ ,  $[\text{Cu}(\text{phen})_2]\text{BPh}_4$ ,  $[\text{Cu}(\text{tmp})_2]\text{PF}_6$ , and  $[\text{Cu}(\text{tmp})_2]\text{BPh}_4$  is shown in Figure 3.9. Based on the aforementioned spectra and the two known  $\Theta_z$  values for  $\text{phen}]\text{ClO}_4$  and  $\text{tmp}]\text{BPh}_4$ , it seems reasonable to estimate a  $\Theta_z$  of  $\sim 80^\circ$  for  $\text{phen}]\text{BPh}_4$  and a  $\Theta_z$  of  $\sim 60^\circ$  for  $\text{tmp}]\text{PF}_6$ . This suggests that large anions tend to open up the crystal lattice and allow the copper complex to “open up” and approach a  $\Theta_z$  of  $90^\circ$ . The dihedral angle can also be estimated by examining the color of the salt. For instance,  $\text{phen}]\text{ClO}_4$  and  $\text{tmp}]\text{PF}_6$  are both purple, while  $\text{phen}]\text{BPh}_4$  and  $\text{tmp}]\text{BPh}_4$  are red-orange in color.

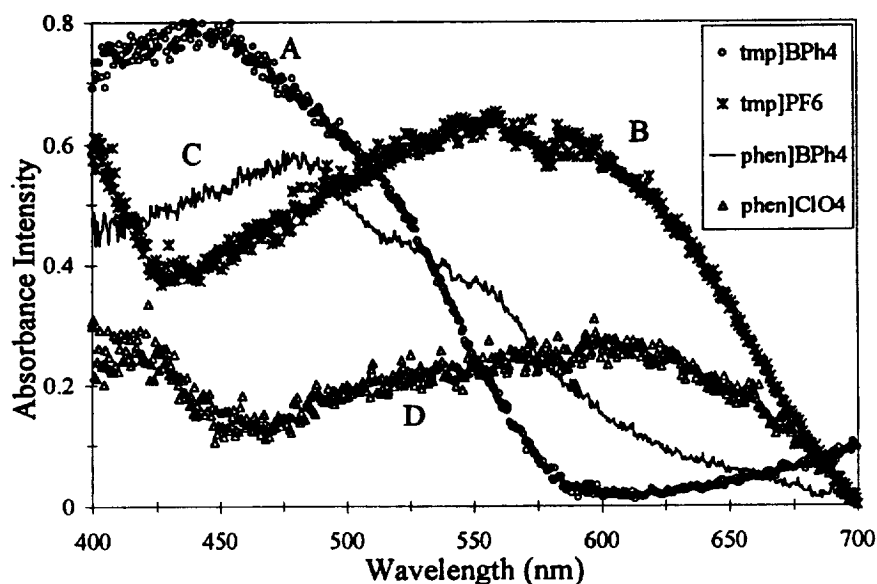


Figure 3.9. Solid state absorbance spectra for selected compounds of the parent group. A =  $[\text{Cu}(\text{tmp})_2]\text{BPh}_4$ , B =  $[\text{Cu}(\text{tmp})_2]\text{PF}_6$ , C =  $[\text{Cu}(\text{phen})_2]\text{BPh}_4$ , D =  $[\text{Cu}(\text{phen})_2]\text{ClO}_4$ . NB V-51.

For the aryl group, simple examination of the color of the salt is not sufficient. All of the aryl group compounds are a wine-red colored solid. The difference in these compounds can only be observed in their spectra. All of the dpp and dpdmp salts have similar absorption spectra, indicating similar structures in the solid state, see Figure 3.10. The stand outs are the salts of dptmp. These compounds exhibit only one peak, like the



compounds in the parent and alkyl groups. This phenomena has been discussed previously.<sup>11</sup> Interestingly, for the aryl group, the anion seems to have only a limited effect on the absorption spectrum. This could be indicating that the structure of the molecule is determined by the ligands and not the lattice forces.

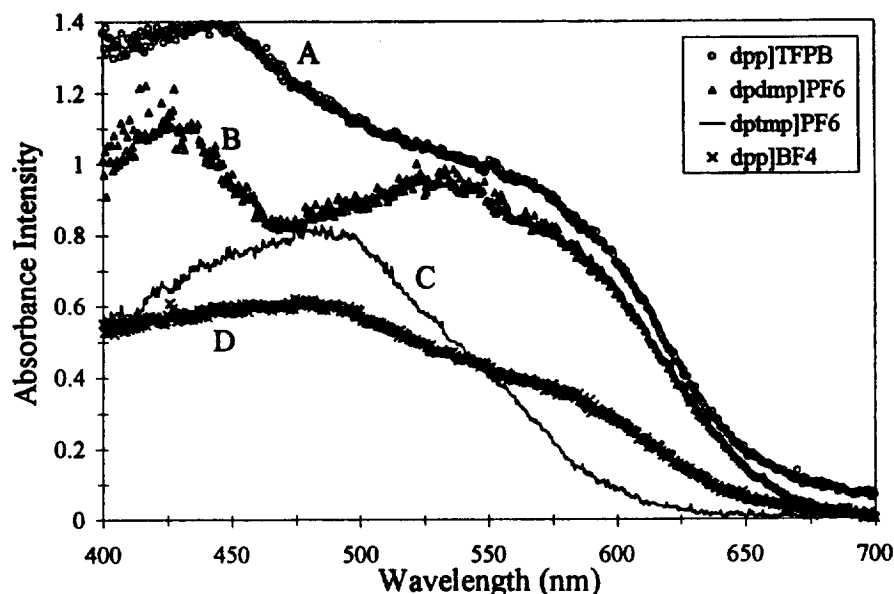


Figure 3.10. Solid state absorbance spectra for selected compounds of the aryl group. A =  $[\text{Cu}(\text{dpp})_2]\text{TFPB}$ , B =  $[\text{Cu}(\text{dpdmp})_2]\text{PF}_6$ , C =  $[\text{Cu}(\text{dptmp})_2]\text{PF}_6$ , D =  $[\text{Cu}(\text{dpp})_2]\text{BF}_4$ . NB V-52

For the alkyl group, there are three apparent trends. The first is that ligands with small substituents in positions 2 and 9 are anion dependent, especially dmp. The absorption maxima for dmp complexes vary, as does  $\Theta_z$ , with dmp]TFPB having the highest energy absorbance maximum.

The second trend is that bulky substituents in the 2,9 positions override any influence the anion has. For example, for dipp, the absorbance maxima does not change as the anion goes from  $\text{Cl}^-$  to  $\text{PF}_6^-$  to TFPB. Considering the vast size difference between  $\text{Cl}^-$  and TFPB, that is quite a feat to be that consistent. Based on earlier evidence, the *iso*-propyl groups must be keeping the phenanthroline ligands from flattening and therefore keeping a similar  $\Theta_z$  throughout the series of dipp compounds.

The third trend is based on the fact that as  $\Theta_z$  maximizes, so does the absorbance energy. For instance, the compounds dmp]TFPB, bcp]BF<sub>4</sub>, dbp]PF<sub>6</sub>, and dipp]TFPB all have absorbance maxima around 460 nm, except bcp]BF<sub>4</sub> which is red-shifted due to the 4,7-diphenyl substitution it has. Most of these compounds have a reported  $\Theta_z$ , or at least one that can be estimated easily, that is 85° or greater. These compounds do not exhibit the pronounced shoulders in their absorbance spectra that are indicative of a flattening distortion, consistent with the idea of a large  $\Theta_z$ . On the other hand, for compounds like dmp]Br and dnpp]PF<sub>6</sub>, their spectra show low energy shoulders and their measured  $\Theta_z$ 's are quite low compared to the first group. Figure 3.11 contains a sampling of the absorption spectra discussed above.

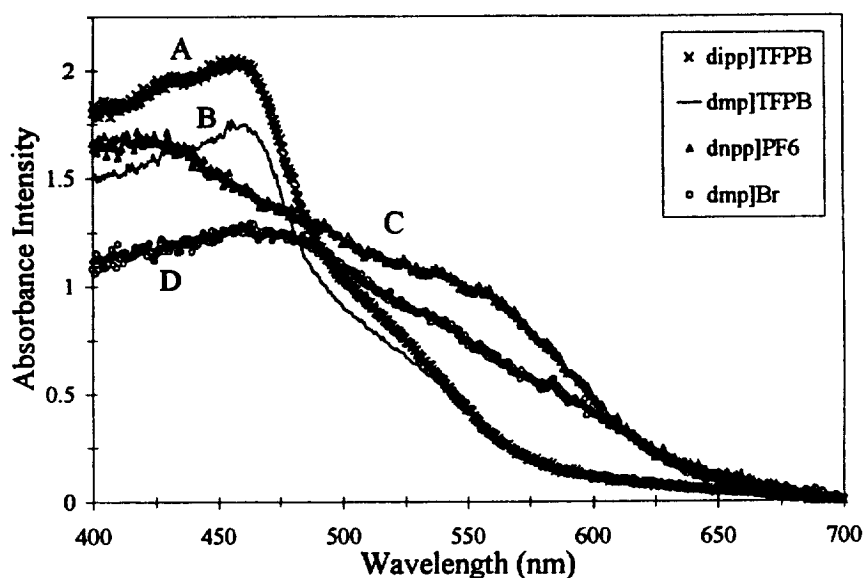


Figure 3.11. Solid state absorbance spectra for select compounds of the alkyl group. A = [Cu(dipp)<sub>2</sub>]TFPB, B = [Cu(dmp)<sub>2</sub>]TFPB, C = [Cu(dnpp)<sub>2</sub>]PF<sub>6</sub>, D = [Cu(dmp)<sub>2</sub>]Br. NB V-52, 53, 54

### Luminescence

One of the most interesting aspects of this project is the solid state luminescence measurements that were made. The data taken on the parent group, shown in Table 3.16, shows that for the first time, a non-2,9-substituted phenanthroline complex emits!

There have been many reports over the years that  $[\text{Cu}(\text{phen})_2]^+$  does not emit in any state,<sup>1</sup> but by using a large anion to increase lattice spacing, and consequently the dihedral angle,  $[\text{Cu}(\text{phen})_2]\text{BPh}_4$  and  $[\text{Cu}(\text{tmp})_2]\text{BPh}_4$  can be made to emit. Further, even  $[\text{Cu}(\text{bipy})_2]^+$  salts give a measurable emission signal at room temperature. The signal is weaker than the phen and tmp complexes, but it is nonetheless measurable. Figure 3.12 contains the uncorrected emission spectra for the parent group complexes that show room temperature emission. These signals were checked against, and found to be different than free ligand, free anion, and the empty sample holder.

Table 3.16. Luminescence and dihedral angle data for the parent group.

| Compound                                 | $\text{CH}_2\text{Cl}_2$<br>Em (nm) | $\text{CH}_2\text{Cl}_2$ $\tau$<br>(ns) | Solid<br>Em (nm) | Solid $\tau$<br>(ns) | $\Theta_z$<br>(deg) | $\Theta_z$<br>Ref. |
|------------------------------------------|-------------------------------------|-----------------------------------------|------------------|----------------------|---------------------|--------------------|
| $[\text{Cu}(\text{phen})_2]\text{ClO}_4$ | ---                                 | ---                                     | ---              | ---                  | 49.9                | 8                  |
| $[\text{Cu}(\text{phen})_2]\text{BPh}_4$ | ---                                 | ---                                     | 695              | 20                   |                     |                    |
| $[\text{Cu}(\text{tmp})_2]\text{PF}_6$   | ---                                 | ---                                     | ---              | ---                  |                     |                    |
| $[\text{Cu}(\text{tmp})_2]\text{BPh}_4$  | ---                                 | ---                                     | 700              | 15                   | 81.9                | this work          |
| $[\text{Cu}(\text{bipy})_2]\text{ClO}_4$ | ---                                 | ---                                     | 660              | <10                  | 75.2                | 27                 |
| $[\text{Cu}(\text{bipy})_2]\text{BPh}_4$ | ---                                 | ---                                     | 660              | ~10                  |                     |                    |

Luminescence data for the aryl group is shown in Table 3.17. Analysis of this data shows that the emission energy of the dptmp complexes is sharply shifted to higher energy relative to the dpp and dpdmp complexes. This shift to higher energy is also followed by dramatic increases in the excited state lifetimes of the dptmp complexes. With lifetimes of 1.5  $\mu\text{s}$  and 4.7  $\mu\text{s}$  in the solid at room temperature, the  $[\text{Cu}(\text{dptmp})_2]^+$  cation has become the longest lived copper phenanthroline in both the solid and solution states. This increase in emission energy and lifetime are most likely consequences of the increased dihedral angle, based on the data reported for  $\text{dpp}]\text{PF}_6$  and that extrapolated

for  $\text{dpp}]\text{BF}_4$ . A comparison of the uncorrected emission spectra for  $\text{dpp}]\text{PF}_6$ ,  $\text{dpdmp}]\text{PF}_6$ , and  $\text{dptmp}]\text{PF}_6$  is shown in Figure 3.13.

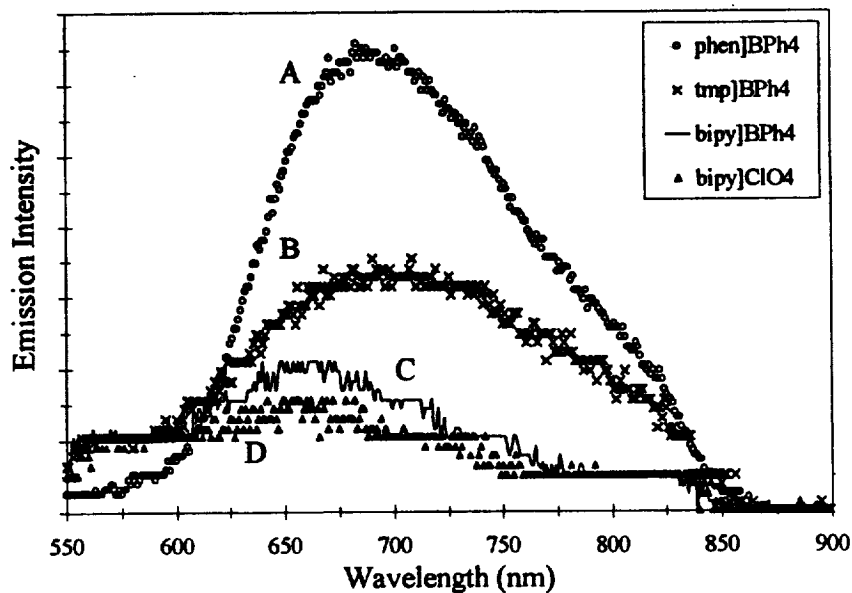


Figure 3.12. Room temperature solid state emission spectra from the parent group. A =  $[\text{Cu}(\text{phen})_2]\text{BPh}_4$ , B =  $[\text{Cu}(\text{tmp})_2]\text{BPh}_4$ , C =  $[\text{Cu}(\text{bipy})_2]\text{BPh}_4$ , D =  $[\text{Cu}(\text{bipy})_2]\text{ClO}_4$ . NB V-70, 71

Table 3.17. Luminescence and dihedral angle data for the aryl group.

| Compound                                 | $\text{CH}_2\text{Cl}_2$<br>Em (nm) | $\text{CH}_2\text{Cl}_2$<br>$\tau$ (ns) | Solid Em<br>(nm) | Solid $\tau$<br>(ns) | $\Theta_z$<br>(deg) | $\Theta_z$<br>Ref. |
|------------------------------------------|-------------------------------------|-----------------------------------------|------------------|----------------------|---------------------|--------------------|
| $[\text{Cu}(\text{dpp})_2]\text{BF}_4$   | 675 <sup>b</sup>                    | 310 <sup>b</sup>                        | 695              | 280                  | (71.8) <sup>a</sup> | 21                 |
| $[\text{Cu}(\text{dpp})_2]\text{PF}_6$   | 685 <sup>c</sup>                    | 270 <sup>c</sup>                        | 670              | 780                  | 79.8                | 22                 |
| $[\text{Cu}(\text{dpp})_2]\text{TFPB}$   | 680 <sup>d</sup>                    | 280 <sup>d</sup>                        | 700              | 310                  |                     |                    |
| $[\text{Cu}(\text{dpdmp})_2]\text{PF}_6$ | 685 <sup>c</sup>                    | 310 <sup>c</sup>                        | 690              | 325                  |                     |                    |
| $[\text{Cu}(\text{dptmp})_2]\text{PF}_6$ | 670 <sup>c</sup>                    | 480 <sup>c</sup>                        | 655              | 1570                 | 87.8                | this work          |
| $[\text{Cu}(\text{dptmp})_2]\text{TFPB}$ | 671 <sup>d</sup>                    | 495 <sup>d</sup>                        | 625              | 4710                 |                     |                    |

a Data extrapolated from the value for  $[\text{Cu}(\text{dpp})_2]\text{CuCl}_2$

b Data taken from ref. r19

c Data taken from ref. r11

d Data taken from ref. r23

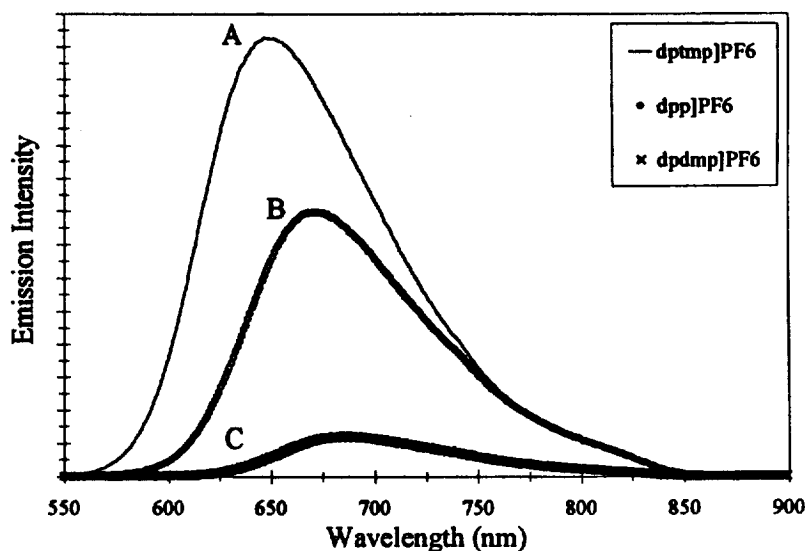


Figure 3.13. Room temperature solid state emission spectra for selected compounds of the aryl group. A =  $[\text{Cu}(\text{dptmp})_2]\text{PF}_6$ , B =  $[\text{Cu}(\text{dpp})_2]\text{PF}_6$ , C =  $[\text{Cu}(\text{dpdmp})_2]\text{PF}_6$ . NB V-68, 69

For the alkyl group, the data is much more difficult to categorize, see Table 3.18. The main reason is the lack of dihedral angle data for a majority of the compounds presented in the table; however, two general trends can be theorized. The first is that with an increasing  $\Theta_z$ , the emission maxima shifts to higher energy. The dnpp complex is an exception to the rule. Figure 3.14 shows an overlay of some emission spectra that illustrate this idea. The second is that with an increasing  $\Theta_z$ , the excited state lifetime also increases.

These two trends are not surprising, if  $\Theta_z$  is examined more closely.  $\Theta_z$  refers to the angle between the two phenanthroline ligands, which also refers to the symmetry of the cation. The closer the symmetry of the cation is to  $D_{2d}$  (or tetrahedral coordination geometry), the larger  $\Theta_z$ . A more tetrahedral structure tends to offer a more stable ground state and a more destabilized excited state. This in turn causes a larger energy difference between the ground and excited states and therefore a higher energy emission. A consequence of the large energy difference between the ground and excited states is an excited state that takes longer to decay, or span the gap to return to the ground state.

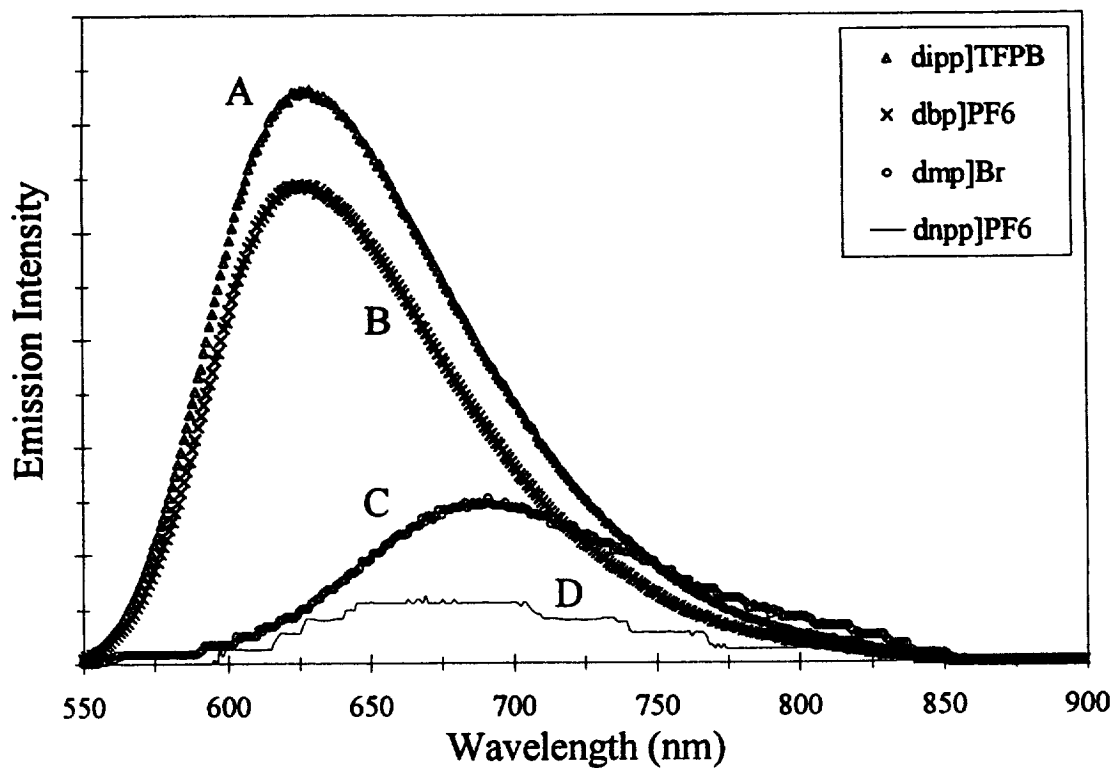


Figure 3.14. Room temperature solid state emission spectra for selected compounds of the alkyl group. A = [Cu(dipp)<sub>2</sub>]TFPB, B = [Cu(dbp)<sub>2</sub>]PF<sub>6</sub>, C = [Cu(dmp)<sub>2</sub>]Br, D = [Cu(dnpp)<sub>2</sub>]PF<sub>6</sub>. NB V-66, 67

Table 3.18. Luminescence and dihedral angle data for the alkyl group.

| Compound                                 | CH <sub>2</sub> Cl <sub>2</sub><br>Em (nm) | CH <sub>2</sub> Cl <sub>2</sub><br>$\tau$ (ns) | Solid Em<br>(nm) | Solid<br>$\tau$ (ns) | $\Theta_2$<br>(deg)     | $\Theta_2$<br>Ref. |
|------------------------------------------|--------------------------------------------|------------------------------------------------|------------------|----------------------|-------------------------|--------------------|
| [Cu(dmp) <sub>2</sub> ]Br                |                                            |                                                | 690              | 250                  | 79.9                    | 3                  |
| [Cu(dmp) <sub>2</sub> ]NO <sub>3</sub>   |                                            |                                                | 680              | 300                  | 72.4, 85.4 <sup>a</sup> | 6                  |
| [Cu(dmp) <sub>2</sub> ]ClO <sub>4</sub>  |                                            |                                                | 670              | 235                  | 81.8                    | 5                  |
| [Cu(dmp) <sub>2</sub> ]TFPB              |                                            |                                                | 650              | 690                  |                         |                    |
| [Cu(bcp) <sub>2</sub> ]BF <sub>4</sub>   | 685                                        | 80                                             | 690              | 135                  | 88.1                    | 20                 |
| [Cu(dbp) <sub>2</sub> ]PF <sub>6</sub>   | 670 <sup>c</sup>                           | 150 <sup>c</sup>                               | 625              | 1240                 | (87.4) <sup>b</sup>     | 9                  |
| [Cu(dbdmp) <sub>2</sub> ]PF <sub>6</sub> | 670 <sup>c</sup>                           | 145 <sup>c</sup>                               | 630              | 740                  |                         |                    |
| [Cu(dbtmp) <sub>2</sub> ]PF <sub>6</sub> | 635 <sup>c</sup>                           | 330 <sup>c</sup>                               | 635              | 1710                 |                         |                    |
| [Cu(dnpp) <sub>2</sub> ]PF <sub>6</sub>  | 665 <sup>c</sup>                           | 260 <sup>c</sup>                               | 670              | 595                  | 66.3                    | 4                  |
| [Cu(dipp) <sub>2</sub> ]Cl               |                                            |                                                | 625              | 1420                 |                         |                    |
| [Cu(dipp) <sub>2</sub> ]PF <sub>6</sub>  |                                            |                                                | 630              | 1290                 |                         |                    |
| [Cu(dipp) <sub>2</sub> ]TFPB             | 650 <sup>f</sup>                           | 365 <sup>f</sup>                               | 625              | 1330                 | 88.9                    | this work          |
| [Cu(dcp) <sub>2</sub> ]PF <sub>6</sub>   | 649 <sup>f</sup>                           | 360 <sup>f</sup>                               | 630              | 765                  |                         |                    |
| [Cu(dsbp) <sub>2</sub> ]Cl               |                                            |                                                | 625              | 1020                 |                         |                    |
| [Cu(dsbp) <sub>2</sub> ]PF <sub>6</sub>  | 650 <sup>c</sup>                           | 400 <sup>c</sup>                               | 625              | 1240                 |                         |                    |
| [Cu(dmbp) <sub>2</sub> ]BF <sub>4</sub>  |                                            |                                                | 685              |                      | 80.8                    | 28                 |
| [Cu(dmbp) <sub>2</sub> ]BPh <sub>4</sub> |                                            |                                                | 670              |                      |                         |                    |
| [Cu(tmbp) <sub>2</sub> ]BF <sub>4</sub>  | 725 <sup>d</sup>                           | 18 <sup>d</sup>                                | 695              | 65                   |                         |                    |
| [Cu(tmbp) <sub>2</sub> ]ClO <sub>4</sub> |                                            |                                                | 695              | 230                  | 75.0                    | 29                 |

a This nitrate salt was a dihydrate

b Data extrapolated from [Cu(di-*n*-pentyl-phen)<sub>2</sub>]CuCl<sub>2</sub>

c Data taken from ref. 31

d Data taken from ref. 14

e Data taken from ref. 11

f Data taken from ref. 30

## Discussion

### Controlling the Dihedral Angle

Table 3.19 lists dihedral angles based on reported crystal structures in the literature. This table contains both spectrally characterized and spectrally uncharacterized compounds (those not examined in this report). Examination of this data reveals two controlling factors as to the dihedral angle: ligand-ligand repulsions and anions. Thus, for the same cation, a different anion can induce a drastic change in the dihedral angle. The most obvious reason is packing forces overcome ligand-ligand repulsions and force the copper complex into a flattened geometry.<sup>4</sup> Or, the anion can be large and bulky and reduce the packing forces and allow the geometry to open up. By the same token, a complex with little to no steric bulk in the 2 and 9 positions of the ligand is one that can flatten.<sup>8</sup> On the other hand, a complex with bulky groups in the 2 and 9 positions is one that is rigid and keeps a tetrahedral-like coordination geometry around the copper center.

What the data above signifies is that the dihedral angle can be systematically varied to give a copper complex with a specific angle. For example,  $[\text{Cu}(\text{phen})_2]^+$  cations all show smallish dihedral angles.<sup>8, 23</sup> It is presumed that this is due to the lack of steric blocks in positions 2 and 9 to keep a more rigid structure.<sup>8</sup> However, by switching to a larger anion such as  $\text{BPh}_4^-$ , crystals of  $[\text{Cu}(\text{tmp})_2]^+$  were able to be grown which show a much larger dihedral angle. The result of this finding is the room temperature solid state emission from  $[\text{Cu}(\text{tmp})_2]\text{BPh}_4$  and  $[\text{Cu}(\text{phen})_2]\text{BPh}_4$ , which is assumed to have a much similar dihedral angle even though no crystal data exists.



Table 3.19. Dihedral angle data for copper bis-phenanthroline complexes.

| Compound                                                                                 | $\Theta_z^a$ | Ref.         | Compound                                                                             | $\Theta_z^a$ | Ref.           |
|------------------------------------------------------------------------------------------|--------------|--------------|--------------------------------------------------------------------------------------|--------------|----------------|
| [Cu(phen) <sub>2</sub> ]CuBr <sub>2</sub>                                                | 77.8         | 8            | [Cu(phen) <sub>2</sub> ]ClO <sub>4</sub>                                             | 49.9         | 8              |
| [Cu(phen) <sub>2</sub> ] <sub>2</sub> [Cu(OAc) <sub>2</sub> ]<br>[OAc]•HOAc <sup>b</sup> | 68.5         | 23           | [Cu(bipy) <sub>2</sub> ]ClO <sub>4</sub>                                             | 75.2         | 27             |
| [Cu(tmp) <sub>2</sub> ]BPh <sub>4</sub>                                                  | 81.9         | <sup>c</sup> | [Cu(dmp) <sub>2</sub> ]Br•H <sub>2</sub> O                                           | 79.9         | 3              |
| [Cu(dmp) <sub>2</sub> ]NO <sub>3</sub>                                                   | 72.4         | 6            | [Cu(dmp) <sub>2</sub> ]NO <sub>3</sub> •3H <sub>2</sub> O                            | 85.4         | 3              |
| [Cu(dmp) <sub>2</sub> ]ClO <sub>4</sub>                                                  | 81.8         | 5            | [Cu(dmp) <sub>2</sub> ] <sub>2</sub> [TCNQ] <sub>2</sub>                             | 88.8         | 7              |
| [Cu(dmbp) <sub>2</sub> ]BF <sub>4</sub>                                                  | 80.8         | 28           | [Cu(tmbp) <sub>2</sub> ]ClO <sub>4</sub>                                             | 75.0         | 29             |
| [Cu(bcp) <sub>2</sub> ]BF <sub>4</sub> •CH <sub>3</sub> OH                               | 88.1         | 20           | [Cu(tmbp) <sub>2</sub> ]Cl•2H <sub>2</sub> O                                         | 79.0         | 3              |
| [Cu( <i>n</i> -pentylphen) <sub>2</sub> ]CuCl <sub>2</sub>                               | 87.4         | 9            | [Cu(dnpp) <sub>2</sub> ]PF <sub>6</sub>                                              | 66.3         | 4 <sup>d</sup> |
| [Cu(dipp) <sub>2</sub> ]TFPB                                                             | 88.9         | <sup>e</sup> | [Cu(dptmp) <sub>2</sub> ]PF <sub>6</sub> •THF                                        | 87.8         | <sup>e</sup>   |
| [Cu(bfp) <sub>2</sub> ]PF <sub>6</sub> <sup>e</sup>                                      | 87           | 24           | [Cu(ocp) <sub>2</sub> ]BF <sub>4</sub> •CH <sub>2</sub> Cl <sub>2</sub> <sup>d</sup> | 89.4         | 25             |
| [Cu(dap) <sub>2</sub> ]BF <sub>4</sub> <sup>e</sup>                                      | ~71          | 26           | [Cu(dpp) <sub>2</sub> ]CuCl <sub>2</sub> • $\frac{2}{3}$ CH <sub>3</sub> CN          | 71.8         | 21             |
| [Cu(dpp) <sub>2</sub> ]PF <sub>6</sub>                                                   | 79.8         | 22           |                                                                                      |              |                |

a in degrees

b OAc = acetate

c this work

d the previously reported value of 75° is erroneous

e bfp = 2,9-bis(trifluoromethyl)-1,10-phenanthroline

f ocp = 2,3,4,5,6,7,8,9-octachloro-1,10-phenanthroline

g dap = 2,9-bis(*p*-anisoyl)-1,10-phenanthroline

The other facet of the crystal data from above is that the dihedral angle can be controlled by modifying the steric size of the 2,9 substituents. For instance, *iso*-propyl, Cl,<sup>25</sup> CF<sub>3</sub>,<sup>19</sup> and *n*-pentyl<sup>9</sup> groups are all rather large and all of their structures show very nearly 90° dihedral angles, even though their anions range from BF<sub>4</sub><sup>-</sup> to PF<sub>6</sub><sup>-</sup> to CuCl<sub>2</sub><sup>-</sup> to TFPB<sup>-</sup>. What this steric control offers is the ability to create a very nearly D<sub>2d</sub> copper phenanthroline cation, which has a very long lifetime in the solid state. One exception is the substituent *neo*-pentyl.<sup>4</sup> When this molecule crystallized, it distorted the *neo*-pentyl groups in a way as to flatten its structure. The fact that the *tert*-butyl part was out away from the phenanthroline core one methylene unit was probably the reason for the unusual packing which lead to the small dihedral angle.<sup>4</sup> This molecule also showed very long Cu-N bonds which indicate excessive strain in the cation. This molecule does not lessen ones ability to induce a change in the dihedral angle by altering the sterics.

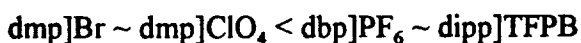
The dihedral angle can also be forced to increase by placing steric locks on remote positions of the phenanthroline as well.<sup>20</sup> In the case of [Cu(dptmp)<sub>2</sub>]<sup>+</sup>, the 3 and 8 methyls act as locks on the 2,9 phenyls, keeping them in a very twisted orientation, with respect to the phenanthroline core. This lack of mobility of the phenyl groups does not allow for the flattening distortion seen in other 2,9-bis(aryl)-phenanthroline complexes.<sup>21, 22, 26</sup> The dptmp crystal structure does, however, still show the rocking distortion so common to 2,9-bis(aryl)-phenanthroline complexes.<sup>21, 22, 26</sup> This rocking distortion is no doubt caused by the intramolecular  $\pi$ -stacking that occurs after the distortion.<sup>21, 22</sup>

### Electronic Structure

The dihedral angle obviously effects the electronic structure of the copper complex, see Tables 3.13 through 3.18. Based on the changes seen in the absorption spectra, the energy of the orbitals involved in the MLCT absorbance are obviously being altered. Kaizu et al<sup>1</sup> have performed DV-X $\alpha$  computations on the model complex [Cu(ethane-diimine)<sub>2</sub>]<sup>+</sup> in order to better understand the changes.

Figure 3.15 shows the highest occupied and lowest unoccupied molecular orbitals, as calculated in ref. 1, and how they change with the dihedral angle. Analysis of the calculated orbitals for percent composition revealed that all of the highest occupied orbitals shown were predominately Cu 3d in character and all of the lowest unoccupied orbitals shown were predominately N 2p and C 2p in character. From these calculations, it is obvious that the lowest allowed transition is MLCT in nature and that the energy decreases in the order:  $90^\circ > 60^\circ > 40^\circ$ . The solid state absorption-dihedral angle correlation presented above is supported by the orbital energy data.<sup>1</sup> As the dihedral angle is maximizing, so is  $\Delta E_{\text{MLCT}}$ .

The emission data correlate with the calculated energy level data. For example, in the aryl group, the dptmp complex has a larger  $\Theta_z$ , higher energy emission, longer lifetime, and based on the  $\Theta_z$  a larger  $\Delta E_{\text{MLCT}}$  than dpp]PF<sub>6</sub>, see Table 3.17. Similarly, Table 3.18 shows that in the alkyl group,  $\Theta_z$ , emission energy, and lifetime all increase in the order:



Based on the reported dihedral angles for these molecules, the calculated  $\Delta E_{\text{MLCT}}$  also increases the that order. And most importantly, in the parent group, the large dihedral angles of tmp]BPh<sub>4</sub> and, presumably, phen]BPh<sub>4</sub>, lead to emissive compounds with measurable lifetimes. These molecules would be calculated to have larger  $\Delta E_{\text{MLCT}}$  values than their non-emissive counterparts tmp]PF<sub>6</sub> and phen]ClO<sub>4</sub>.

The one limit to this data is that it does not predict boundaries. For example, the one exception to many of the trends is dnpp]PF<sub>6</sub>. This molecule has an extremely small  $\Theta_z$  ( $66.3^\circ$ )<sup>4</sup> yet it has a moderate energy emission maximum and a considerable lifetime, while tmp]BPh<sub>4</sub> has a large  $\Theta_z$  ( $81.9^\circ$ ) a low energy emission and a very short lifetime. The electronic differences in the ligands may be responsible for the photophysical differences,<sup>11</sup> however it does not explain why the dnpp]PF<sub>6</sub> complex does not fit the trends of other alkyl group molecules. Regardless, the data presented here along with that of Kaizu et al<sup>1</sup> gives a pretty clear picture of the flattening distortion and its effects on the photochemistry of copper phenanthrolines.<sup>6</sup>

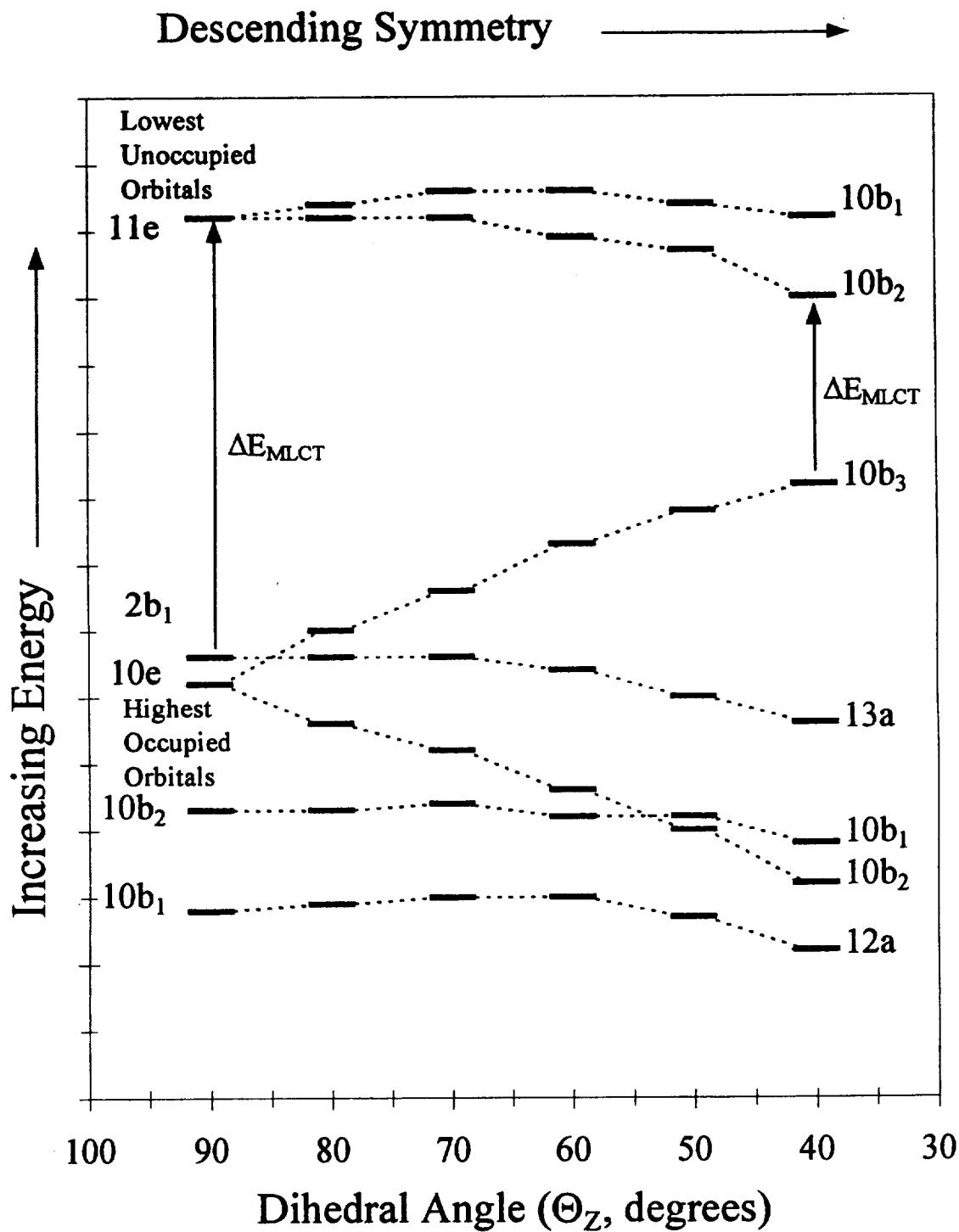


Figure 3.19. Energies of the highest occupied and lowest unoccupied molecular orbitals of  $[\text{Cu}(\text{ethane-diimine})_2]^+$ , as predicted by DV- $X\alpha$  calculations in ref 1.

### Conclusion

The correlation between the computational, structural and photophysical data presented above indicates that the solid state is a good media in which to study the flattening distortion that copper phenanthrolines undergo in solution.<sup>10</sup> In the solid state, the molecules are predisposed to a specific amount of flattening, which can be changed by altering the anion or the steric bulk of the 2,9 positions. The amount of flattening will then dictate the photochemistry the copper complex is able to perform. It is a very good example of the impact the flattening distortion, proposed by McMillin et al, has on the photochemistry of copper phenanthrolines.<sup>10</sup>

## APPENDICES

# Appendix A: Crystal Data for [Cu(dptmp)<sub>2</sub>]PF<sub>6</sub>•THF

**Table A.1. Anisotropic temperature factor coefficients - U's<sup>a</sup> for [Cu(dptmp)<sub>2</sub>]PF<sub>6</sub>•THF.**

| Name   | U(1,1)     | U(2,2)     | U(3,3)     | U(1,2)      | U(1,3)       | U(2,3)       |
|--------|------------|------------|------------|-------------|--------------|--------------|
| Cu     | 0.0415(3)  | 0.0599(3)  | 0.0473(3)  | 0.00107(19) | -0.00415(17) | -0.00195(19) |
| P(1)   | 0.0894(11) | 0.0920(10) | 0.1125(12) | -0.0125(8)  | 0.0008(9)    | 0.0246(9)    |
| F(1)   | 0.191(6)   | 0.125(4)   | 0.466(13)  | 0.000(4)    | 0.087(7)     | -0.053(6)    |
| F(2)   | 0.193(7)   | 0.399(12)  | 0.340(11)  | 0.107(8)    | -0.160(8)    | -0.028(10)   |
| F(3)   | 0.187(6)   | 0.595(17)  | 0.166(5)   | -0.036(8)   | 0.057(5)     | 0.154(8)     |
| F(4)   | 0.258(8)   | 0.291(8)   | 0.147(5)   | 0.119(6)    | -0.046(5)    | 0.022(5)     |
| F(5)   | 0.468(16)  | 0.213(7)   | 0.397(14)  | -0.043(9)   | 0.323(14)    | 0.016(8)     |
| F(6)   | 0.218(6)   | 0.115(3)   | 0.224(6)   | 0.008(4)    | -0.016(5)    | 0.002(4)     |
| O(301) | 0.144(6)   | 0.243(9)   | 0.224(8)   | -0.024(6)   | -0.016(5)    | 0.074(7)     |
| N(11)  | 0.0424(15) | 0.0528(16) | 0.0449(15) | 0.0079(12)  | 0.0012(12)   | 0.0010(12)   |
| N(21)  | 0.0376(15) | 0.0618(17) | 0.0447(15) | 0.0036(12)  | 0.0001(11)   | 0.0024(13)   |
| N(112) | 0.0419(15) | 0.0535(16) | 0.0428(14) | 0.0054(12)  | -0.0011(11)  | 0.0033(12)   |
| N(212) | 0.0353(14) | 0.0544(16) | 0.0460(15) | 0.0037(12)  | 0.0014(11)   | 0.0054(12)   |
| C(12)  | 0.047(2)   | 0.063(2)   | 0.054(2)   | 0.0122(16)  | 0.0056(16)   | 0.0097(17)   |
| C(13)  | 0.055(2)   | 0.077(3)   | 0.059(2)   | 0.018(2)    | 0.0045(18)   | 0.018(2)     |
| C(14)  | 0.050(2)   | 0.086(3)   | 0.051(2)   | 0.021(2)    | -0.0011(16)  | 0.0095(19)   |
| C(15)  | 0.0403(18) | 0.071(2)   | 0.0470(18) | 0.0101(16)  | -0.0014(14)  | -0.0012(17)  |
| C(16)  | 0.047(2)   | 0.079(3)   | 0.055(2)   | 0.0030(19)  | -0.0103(17)  | -0.011(2)    |
| C(17)  | 0.051(2)   | 0.063(2)   | 0.072(3)   | -0.0045(18) | -0.0031(19)  | -0.014(2)    |
| C(18)  | 0.048(2)   | 0.060(2)   | 0.060(2)   | 0.0042(16)  | 0.0054(16)   | -0.0042(17)  |
| C(19)  | 0.061(2)   | 0.056(2)   | 0.081(3)   | -0.0009(19) | 0.011(2)     | 0.003(2)     |
| C(22)  | 0.0384(18) | 0.079(3)   | 0.051(2)   | 0.0046(17)  | 0.0011(15)   | 0.0017(18)   |
| C(23)  | 0.038(2)   | 0.106(3)   | 0.060(2)   | 0.007(2)    | 0.0012(17)   | -0.001(2)    |
| C(24)  | 0.0378(19) | 0.090(3)   | 0.059(2)   | 0.0028(19)  | -0.0047(16)  | 0.000(2)     |
| C(25)  | 0.0385(18) | 0.072(2)   | 0.054(2)   | -0.0017(16) | -0.0020(15)  | 0.0027(17)   |
| C(26)  | 0.050(2)   | 0.094(3)   | 0.052(2)   | -0.003(2)   | -0.0075(17)  | -0.012(2)    |
| C(27)  | 0.051(2)   | 0.083(3)   | 0.053(2)   | 0.001(2)    | 0.0007(17)   | -0.0133(19)  |
| C(28)  | 0.0455(19) | 0.056(2)   | 0.0446(17) | 0.0028(15)  | 0.0031(14)   | 0.0002(15)   |
| C(29)  | 0.052(2)   | 0.0508(19) | 0.0491(18) | 0.0069(15)  | 0.0083(15)   | 0.0051(15)   |
| C(110) | 0.075(3)   | 0.067(3)   | 0.074(3)   | 0.006(2)    | 0.011(2)     | 0.022(2)     |
| C(111) | 0.057(2)   | 0.063(2)   | 0.054(2)   | 0.0077(18)  | 0.0069(17)   | 0.0096(18)   |
| C(113) | 0.0405(17) | 0.0537(19) | 0.0460(18) | 0.0039(14)  | 0.0015(14)   | -0.0038(15)  |
| C(114) | 0.0363(17) | 0.059(2)   | 0.0441(17) | 0.0054(14)  | -0.0022(13)  | 0.0000(15)   |
| C(115) | 0.096(4)   | 0.103(4)   | 0.098(4)   | 0.026(3)    | -0.006(3)    | 0.046(3)     |
| C(116) | 0.070(3)   | 0.131(5)   | 0.068(3)   | 0.021(3)    | -0.020(2)    | 0.021(3)     |
| C(117) | 0.088(4)   | 0.068(3)   | 0.133(5)   | -0.014(3)   | 0.008(3)     | 0.011(3)     |
| C(118) | 0.112(5)   | 0.084(4)   | 0.114(5)   | -0.004(3)   | 0.000(4)     | 0.043(3)     |
| C(121) | 0.057(2)   | 0.061(2)   | 0.061(2)   | 0.0080(18)  | 0.0111(18)   | 0.0158(18)   |
| C(122) | 0.069(3)   | 0.062(2)   | 0.075(3)   | 0.003(2)    | 0.017(2)     | 0.006(2)     |
| C(123) | 0.084(4)   | 0.076(3)   | 0.093(4)   | -0.011(3)   | 0.021(3)     | -0.006(3)    |
| C(124) | 0.093(4)   | 0.081(3)   | 0.108(4)   | -0.022(3)   | 0.017(3)     | 0.005(3)     |
| C(125) | 0.090(4)   | 0.091(4)   | 0.115(5)   | -0.013(3)   | 0.031(3)     | 0.033(3)     |
| C(126) | 0.081(3)   | 0.087(3)   | 0.071(3)   | 0.001(3)    | 0.016(2)     | 0.020(2)     |
| C(131) | 0.059(2)   | 0.083(3)   | 0.061(2)   | 0.009(2)    | 0.0018(19)   | 0.026(2)     |
| C(132) | 0.096(4)   | 0.076(3)   | 0.064(3)   | 0.019(3)    | -0.007(2)    | 0.015(2)     |
| C(133) | 0.108(5)   | 0.110(4)   | 0.070(3)   | 0.009(4)    | -0.016(3)    | 0.019(3)     |
| C(134) | 0.084(4)   | 0.209(8)   | 0.085(4)   | 0.008(5)    | -0.025(3)    | 0.045(5)     |
| C(135) | 0.088(5)   | 0.305(12)  | 0.086(5)   | 0.068(6)    | 0.000(4)     | 0.037(6)     |
| C(136) | 0.078(4)   | 0.210(8)   | 0.065(3)   | 0.053(4)    | 0.001(3)     | 0.018(4)     |
| C(210) | 0.0387(17) | 0.058(2)   | 0.0534(19) | 0.0082(15)  | 0.0079(14)   | 0.0072(16)   |
| C(211) | 0.0402(17) | 0.0531(19) | 0.0490(18) | 0.0054(14)  | 0.0039(14)   | 0.0108(15)   |
| C(213) | 0.0349(16) | 0.0511(18) | 0.0465(17) | 0.0025(13)  | -0.0012(13)  | 0.0045(14)   |
| C(214) | 0.0376(17) | 0.060(2)   | 0.0458(18) | 0.0008(15)  | -0.0010(14)  | 0.0022(15)   |
| C(215) | 0.039(2)   | 0.171(6)   | 0.097(4)   | 0.012(3)    | 0.004(2)     | -0.027(4)    |
| C(216) | 0.043(2)   | 0.138(5)   | 0.072(3)   | 0.005(3)    | -0.013(2)    | -0.004(3)    |
| C(217) | 0.067(3)   | 0.073(3)   | 0.059(2)   | 0.010(2)    | 0.014(2)     | -0.009(2)    |
| C(218) | 0.048(2)   | 0.087(3)   | 0.070(3)   | 0.016(2)    | 0.0110(19)   | 0.000(2)     |
| C(221) | 0.0321(17) | 0.081(3)   | 0.059(2)   | 0.0072(17)  | 0.0025(15)   | -0.0025(19)  |
| C(222) | 0.064(3)   | 0.095(3)   | 0.059(2)   | 0.004(2)    | 0.007(2)     | 0.002(2)     |
| C(223) | 0.083(4)   | 0.114(4)   | 0.065(3)   | -0.009(3)   | 0.009(2)     | 0.011(3)     |

Table A.1, continued

| Name   | U(1,1)     | U(2,2)    | U(3,3)    | U(1,2)     | U(1,3)      | U(2,3)     |
|--------|------------|-----------|-----------|------------|-------------|------------|
| C(224) | 0.061(3)   | 0.133(5)  | 0.064(3)  | 0.001(3)   | 0.009(2)    | -0.017(3)  |
| C(225) | 0.067(3)   | 0.109(4)  | 0.098(4)  | 0.026(3)   | 0.012(3)    | -0.021(3)  |
| C(226) | 0.070(3)   | 0.098(4)  | 0.073(3)  | 0.022(3)   | 0.005(2)    | 0.001(3)   |
| C(231) | 0.0382(18) | 0.058(2)  | 0.055(2)  | 0.0063(15) | 0.0078(15)  | 0.0035(16) |
| C(232) | 0.058(2)   | 0.070(3)  | 0.072(3)  | -0.003(2)  | 0.001(2)    | 0.006(2)   |
| C(233) | 0.059(3)   | 0.074(3)  | 0.093(3)  | -0.015(2)  | 0.006(2)    | 0.002(2)   |
| C(234) | 0.046(2)   | 0.092(3)  | 0.080(3)  | -0.004(2)  | 0.002(2)    | -0.017(3)  |
| C(235) | 0.051(2)   | 0.113(4)  | 0.060(2)  | 0.016(2)   | -0.0049(19) | -0.002(2)  |
| C(236) | 0.048(2)   | 0.077(3)  | 0.059(2)  | 0.0094(18) | 0.0018(17)  | 0.0100(19) |
| C(302) | 0.131(10)  | 0.141(9)  | 0.63(4)   | 0.003(7)   | -0.036(14)  | 0.167(15)  |
| C(303) | 0.131(10)  | 0.164(11) | 0.74(4)   | -0.021(9)  | -0.068(17)  | 0.179(18)  |
| C(304) | 0.103(7)   | 0.143(9)  | 0.49(3)   | 0.017(7)   | 0.031(11)   | 0.111(12)  |
| C(305) | 0.157(10)  | 0.191(11) | 0.216(11) | 0.053(9)   | 0.033(8)    | 0.050(9)   |

a The form of the anisotropic temperature factor is:  
 $\exp[-2\pi \{h^2a'^2U(1,1) + k^2b'^2U(2,2) + l^2c'^2U(3,3) + 2hka'b'U(1,2) + 2hla'c'U(1,3) + 2klb'c'U(2,3)\}]$  where  $a'$ ,  $b'$ , and  $c'$  are reciprocal lattice constants.



Table A.2. Torsion angles in degrees for [Cu(dptmp)<sub>2</sub>]PF<sub>6</sub>·THF.

| Atom 1 | Atom 2 | Atom 3 | Atom 4 | Angle           |
|--------|--------|--------|--------|-----------------|
| =====  | =====  | =====  | =====  | =====           |
| N(21)  | Cu     | N(11)  | C(12)  | -35.62 ( 0.39)  |
| N(21)  | Cu     | N(11)  | C(114) | 152.63 ( 0.23)  |
| N(112) | Cu     | N(11)  | C(12)  | 179.61 ( 0.33)  |
| N(112) | Cu     | N(11)  | C(114) | 7.86 ( 0.23)    |
| N(212) | Cu     | N(11)  | C(12)  | 73.26 ( 0.33)   |
| N(212) | Cu     | N(11)  | C(114) | -98.49 ( 0.24)  |
| N(11)  | Cu     | N(21)  | C(22)  | -62.66 ( 0.36)  |
| N(11)  | Cu     | N(21)  | C(214) | 123.35 ( 0.26)  |
| N(112) | Cu     | N(21)  | C(22)  | 70.18 ( 0.34)   |
| N(112) | Cu     | N(21)  | C(214) | -103.81 ( 0.26) |
| N(212) | Cu     | N(21)  | C(22)  | 176.56 ( 0.32)  |
| N(212) | Cu     | N(21)  | C(214) | 2.57 ( 0.25)    |
| N(11)  | Cu     | N(112) | C(111) | -177.66 ( 0.32) |
| N(11)  | Cu     | N(112) | C(113) | -8.93 ( 0.23)   |
| N(21)  | Cu     | N(112) | C(111) | 30.68 ( 0.36)   |
| N(21)  | Cu     | N(112) | C(113) | -160.59 ( 0.22) |
| N(212) | Cu     | N(112) | C(111) | -62.70 ( 0.32)  |
| N(212) | Cu     | N(112) | C(113) | 106.03 ( 0.23)  |
| N(11)  | Cu     | N(212) | C(211) | 38.61 ( 0.35)   |
| N(11)  | Cu     | N(212) | C(213) | -142.17 ( 0.20) |
| N(21)  | Cu     | N(212) | C(211) | -179.24 ( 0.33) |
| N(21)  | Cu     | N(212) | C(213) | -0.02 ( 0.28)   |
| N(112) | Cu     | N(212) | C(211) | -51.13 ( 0.34)  |
| N(112) | Cu     | N(212) | C(213) | 128.09 ( 0.20)  |
| C(305) | O(301) | C(302) | C(303) | -8.90 ( 2.21)   |
| C(302) | O(301) | C(305) | C(304) | -1.82 ( 1.60)   |
| Cu     | N(11)  | C(12)  | C(13)  | -168.40 ( 0.29) |
| Cu     | N(11)  | C(12)  | C(121) | 9.77 ( 0.50)    |
| C(114) | N(11)  | C(12)  | C(13)  | 2.90 ( 0.55)    |
| C(114) | N(11)  | C(12)  | C(121) | -178.93 ( 0.33) |
| Cu     | N(11)  | C(114) | C(15)  | 173.36 ( 0.29)  |
| Cu     | N(11)  | C(114) | C(113) | -5.63 ( 0.39)   |
| C(12)  | N(11)  | C(114) | C(15)  | 0.50 ( 0.53)    |
| C(12)  | N(11)  | C(114) | C(113) | -178.49 ( 0.33) |
| Cu     | N(21)  | C(22)  | C(23)  | -172.47 ( 0.34) |
| Cu     | N(21)  | C(22)  | C(221) | 11.51 ( 0.50)   |
| C(214) | N(21)  | C(22)  | C(23)  | 1.33 ( 0.58)    |
| C(214) | N(21)  | C(22)  | C(221) | -174.70 ( 0.34) |
| Cu     | N(21)  | C(214) | C(25)  | 173.94 ( 0.31)  |
| Cu     | N(21)  | C(214) | C(213) | -4.76 ( 0.42)   |
| C(22)  | N(21)  | C(214) | C(25)  | -0.65 ( 0.55)   |
| C(22)  | N(21)  | C(214) | C(213) | -179.35 ( 0.32) |
| Cu     | N(112) | C(111) | C(110) | 165.16 ( 0.32)  |
| Cu     | N(112) | C(111) | C(131) | -15.61 ( 0.49)  |
| C(113) | N(112) | C(111) | C(110) | -2.93 ( 0.57)   |
| C(113) | N(112) | C(111) | C(131) | 176.31 ( 0.33)  |
| Cu     | N(112) | C(113) | C(18)  | -169.85 ( 0.30) |
| Cu     | N(112) | C(113) | C(114) | 8.59 ( 0.39)    |
| C(111) | N(112) | C(113) | C(18)  | 0.12 ( 0.52)    |
| C(111) | N(112) | C(113) | C(114) | 178.57 ( 0.33)  |
| Cu     | N(212) | C(211) | C(210) | -176.55 ( 0.27) |
| Cu     | N(212) | C(211) | C(231) | 5.14 ( 0.51)    |
| C(213) | N(212) | C(211) | C(210) | 4.28 ( 0.52)    |
| C(213) | N(212) | C(211) | C(231) | -174.02 ( 0.30) |
| Cu     | N(212) | C(213) | C(28)  | 179.97 ( 0.32)  |
| Cu     | N(212) | C(213) | C(214) | -2.43 ( 0.34)   |
| C(211) | N(212) | C(213) | C(28)  | -0.69 ( 0.47)   |
| C(211) | N(212) | C(213) | C(214) | 176.92 ( 0.32)  |
| N(11)  | C(12)  | C(13)  | C(14)  | -4.23 ( 0.62)   |
| N(11)  | C(12)  | C(13)  | C(115) | 172.75 ( 0.41)  |
| C(121) | C(12)  | C(13)  | C(14)  | 177.74 ( 0.39)  |
| C(121) | C(12)  | C(13)  | C(115) | -5.28 ( 0.63)   |
| N(11)  | C(12)  | C(121) | C(122) | -52.30 ( 0.54)  |
| N(11)  | C(12)  | C(121) | C(126) | 125.78 ( 0.45)  |

Table A.2, continued

| Atom 1 | Atom 2 | Atom 3 | Atom 4 | Angle           |
|--------|--------|--------|--------|-----------------|
| =====  | =====  | =====  | =====  | =====           |
| C(13)  | C(12)  | C(121) | C(122) | 125.86 ( 0.48)  |
| C(13)  | C(12)  | C(121) | C(126) | -56.07 ( 0.59)  |
| C(12)  | C(13)  | C(14)  | C(15)  | 2.03 ( 0.60)    |
| C(12)  | C(13)  | C(14)  | C(116) | -179.86 ( 0.40) |
| C(115) | C(13)  | C(14)  | C(15)  | -174.85 ( 0.42) |
| C(115) | C(13)  | C(14)  | C(116) | 3.26 ( 0.66)    |
| C(13)  | C(14)  | C(15)  | C(16)  | 177.81 ( 0.38)  |
| C(13)  | C(14)  | C(15)  | C(114) | 1.13 ( 0.56)    |
| C(116) | C(14)  | C(15)  | C(16)  | -0.34 ( 0.60)   |
| C(116) | C(14)  | C(15)  | C(114) | -177.02 ( 0.37) |
| C(14)  | C(15)  | C(16)  | C(17)  | -173.84 ( 0.40) |
| C(114) | C(15)  | C(16)  | C(17)  | 2.83 ( 0.59)    |
| C(14)  | C(15)  | C(114) | N(11)  | -2.53 ( 0.55)   |
| C(14)  | C(15)  | C(114) | C(113) | 176.44 ( 0.34)  |
| C(16)  | C(15)  | C(114) | N(11)  | -179.41 ( 0.34) |
| C(16)  | C(15)  | C(114) | C(113) | -0.44 ( 0.53)   |
| C(15)  | C(16)  | C(17)  | C(18)  | -2.21 ( 0.64)   |
| C(16)  | C(17)  | C(18)  | C(19)  | 177.88 ( 0.41)  |
| C(16)  | C(17)  | C(18)  | C(113) | -0.84 ( 0.61)   |
| C(17)  | C(18)  | C(19)  | C(110) | 178.48 ( 0.41)  |
| C(17)  | C(18)  | C(19)  | C(117) | -1.39 ( 0.67)   |
| C(113) | C(18)  | C(19)  | C(110) | -2.81 ( 0.60)   |
| C(113) | C(18)  | C(19)  | C(117) | 177.32 ( 0.43)  |
| C(17)  | C(18)  | C(113) | N(112) | -178.45 ( 0.35) |
| C(17)  | C(18)  | C(113) | C(114) | 3.16 ( 0.55)    |
| C(19)  | C(18)  | C(113) | N(112) | 2.75 ( 0.58)    |
| C(19)  | C(18)  | C(113) | C(114) | -175.65 ( 0.35) |
| C(18)  | C(19)  | C(110) | C(111) | 0.25 ( 0.64)    |
| C(18)  | C(19)  | C(110) | C(118) | 179.46 ( 0.45)  |
| C(117) | C(19)  | C(110) | C(111) | -179.89 ( 0.47) |
| C(117) | C(19)  | C(110) | C(118) | -0.68 ( 0.73)   |
| N(21)  | C(22)  | C(23)  | C(24)  | -0.45 ( 0.70)   |
| N(21)  | C(22)  | C(23)  | C(215) | 178.83 ( 0.45)  |
| C(221) | C(22)  | C(23)  | C(24)  | 175.44 ( 0.41)  |
| C(221) | C(22)  | C(23)  | C(215) | -5.28 ( 0.70)   |
| N(21)  | C(22)  | C(221) | C(222) | 73.38 ( 0.52)   |
| N(21)  | C(22)  | C(221) | C(226) | -110.26 ( 0.47) |
| C(23)  | C(22)  | C(221) | C(222) | -102.76 ( 0.52) |
| C(23)  | C(22)  | C(221) | C(226) | 73.61 ( 0.59)   |
| C(22)  | C(23)  | C(24)  | C(25)  | -1.11 ( 0.68)   |
| C(22)  | C(23)  | C(24)  | C(216) | 178.47 ( 0.46)  |
| C(215) | C(23)  | C(24)  | C(25)  | 179.62 ( 0.47)  |
| C(215) | C(23)  | C(24)  | C(216) | -0.79 ( 0.77)   |
| C(23)  | C(24)  | C(25)  | C(26)  | -177.88 ( 0.46) |
| C(23)  | C(24)  | C(25)  | C(214) | 1.72 ( 0.63)    |
| C(216) | C(24)  | C(25)  | C(26)  | 2.54 ( 0.69)    |
| C(216) | C(24)  | C(25)  | C(214) | -177.86 ( 0.44) |
| C(24)  | C(25)  | C(26)  | C(27)  | 178.96 ( 0.45)  |
| C(214) | C(25)  | C(26)  | C(27)  | -0.64 ( 0.72)   |
| C(24)  | C(25)  | C(214) | N(21)  | -0.87 ( 0.61)   |
| C(24)  | C(25)  | C(214) | C(213) | 177.80 ( 0.35)  |
| C(26)  | C(25)  | C(214) | N(21)  | 178.75 ( 0.40)  |
| C(26)  | C(25)  | C(214) | C(213) | -2.57 ( 0.59)   |
| C(25)  | C(26)  | C(27)  | C(28)  | 2.76 ( 0.74)    |
| C(26)  | C(27)  | C(28)  | C(29)  | 178.14 ( 0.44)  |
| C(26)  | C(27)  | C(28)  | C(213) | -1.53 ( 0.61)   |
| C(27)  | C(28)  | C(29)  | C(210) | -174.86 ( 0.38) |
| C(27)  | C(28)  | C(29)  | C(217) | 4.90 ( 0.61)    |
| C(213) | C(28)  | C(29)  | C(210) | 4.80 ( 0.56)    |
| C(213) | C(28)  | C(29)  | C(217) | -175.44 ( 0.34) |
| C(27)  | C(28)  | C(213) | N(212) | 175.79 ( 0.32)  |
| C(27)  | C(28)  | C(213) | C(214) | -1.71 ( 0.51)   |
| C(29)  | C(28)  | C(213) | N(212) | -3.89 ( 0.52)   |
| C(29)  | C(28)  | C(213) | C(214) | 178.60 ( 0.35)  |

Table A.2, continued

| Atom 1 | Atom 2 | Atom 3 | Atom 4 | Angle           |
|--------|--------|--------|--------|-----------------|
| =====  | =====  | =====  | =====  | =====           |
| C(28)  | C(29)  | C(210) | C(211) | -1.44 ( 0.57)   |
| C(28)  | C(29)  | C(210) | C(218) | 178.92 ( 0.39)  |
| C(217) | C(29)  | C(210) | C(211) | 178.81 ( 0.36)  |
| C(217) | C(29)  | C(210) | C(218) | -0.83 ( 0.60)   |
| C(19)  | C(110) | C(111) | N(112) | 2.76 ( 0.66)    |
| C(19)  | C(110) | C(111) | C(131) | -176.42 ( 0.40) |
| C(118) | C(110) | C(111) | N(112) | -176.47 ( 0.43) |
| C(118) | C(110) | C(111) | C(131) | 4.35 ( 0.67)    |
| N(112) | C(111) | C(131) | C(132) | 81.48 ( 0.53)   |
| N(112) | C(111) | C(131) | O(136) | -98.87 ( 0.56)  |
| C(110) | C(111) | C(131) | C(132) | -99.28 ( 0.55)  |
| C(110) | C(111) | C(131) | C(136) | 80.37 ( 0.64)   |
| N(112) | C(113) | C(114) | N(11)  | -1.99 ( 0.49)   |
| N(112) | C(113) | C(114) | C(15)  | 178.98 ( 0.32)  |
| C(18)  | C(113) | C(114) | N(11)  | 176.50 ( 0.34)  |
| C(18)  | C(113) | C(114) | C(15)  | -2.53 ( 0.54)   |
| C(12)  | C(121) | C(122) | C(123) | 177.65 ( 0.43)  |
| C(126) | C(121) | C(122) | C(123) | -0.51 ( 0.69)   |
| C(12)  | C(121) | C(126) | C(125) | -177.66 ( 0.46) |
| C(122) | C(121) | C(126) | C(125) | 0.48 ( 0.72)    |
| C(121) | C(122) | C(123) | C(124) | 0.74 ( 0.80)    |
| C(122) | C(123) | C(124) | C(125) | -0.91 ( 0.87)   |
| C(123) | C(124) | C(125) | C(126) | 0.90 ( 0.92)    |
| C(124) | C(125) | C(126) | C(121) | -0.69 ( 0.87)   |
| C(111) | C(131) | C(132) | C(133) | -178.01 ( 0.49) |
| C(136) | C(131) | C(132) | C(133) | 2.33 ( 0.82)    |
| C(111) | C(131) | C(136) | C(135) | 179.88 ( 0.71)  |
| C(132) | C(131) | C(136) | C(135) | -0.46 ( 1.04)   |
| C(131) | C(132) | C(133) | C(134) | -0.95 ( 0.97)   |
| C(132) | C(133) | C(134) | C(135) | -2.27 ( 1.23)   |
| C(133) | C(134) | C(135) | C(136) | 4.06 ( 1.39)    |
| C(134) | C(135) | C(136) | C(131) | -2.67 ( 1.32)   |
| C(29)  | C(210) | C(211) | N(212) | -3.24 ( 0.59)   |
| C(29)  | C(210) | C(211) | C(231) | 174.99 ( 0.36)  |
| C(218) | C(210) | C(211) | N(212) | 176.41 ( 0.38)  |
| C(218) | C(210) | C(211) | C(231) | -5.37 ( 0.58)   |
| N(212) | C(211) | C(231) | C(232) | 99.53 ( 0.42)   |
| N(212) | C(211) | C(231) | C(236) | -82.10 ( 0.48)  |
| C(210) | C(211) | C(231) | C(232) | -78.80 ( 0.51)  |
| C(210) | C(211) | C(231) | C(236) | 99.57 ( 0.46)   |
| N(212) | C(213) | C(214) | N(21)  | 4.88 ( 0.47)    |
| N(212) | C(213) | C(214) | C(25)  | -173.87 ( 0.33) |
| C(28)  | C(213) | C(214) | N(21)  | -177.49 ( 0.32) |
| C(28)  | C(213) | C(214) | C(25)  | 3.77 ( 0.53)    |
| C(22)  | C(221) | C(222) | C(223) | 174.25 ( 0.44)  |
| C(226) | C(221) | C(222) | C(223) | -2.26 ( 0.73)   |
| C(22)  | C(221) | C(226) | C(225) | -174.87 ( 0.44) |
| C(222) | C(221) | C(226) | C(225) | 1.49 ( 0.72)    |
| C(221) | C(222) | C(223) | C(224) | 1.17 ( 0.80)    |
| C(222) | C(223) | C(224) | C(225) | 0.72 ( 0.84)    |
| C(223) | C(224) | C(225) | C(226) | -1.47 ( 0.84)   |
| C(224) | C(225) | C(226) | C(221) | 0.34 ( 0.80)    |
| C(211) | C(231) | C(232) | C(233) | 179.19 ( 0.40)  |
| C(236) | C(231) | C(232) | C(233) | 0.78 ( 0.61)    |
| C(211) | C(231) | C(236) | C(235) | -178.37 ( 0.37) |
| C(232) | C(231) | C(236) | C(235) | 0.02 ( 0.84)    |
| C(231) | C(232) | C(233) | C(234) | -0.84 ( 0.71)   |
| C(232) | C(233) | C(234) | C(235) | 0.10 ( 0.71)    |
| C(233) | C(234) | C(235) | C(236) | 0.70 ( 0.68)    |
| C(234) | C(235) | C(236) | C(231) | -0.75 ( 0.64)   |
| O(301) | C(302) | C(303) | C(304) | 16.60 ( 2.70)   |
| C(302) | C(303) | C(304) | C(305) | -15.48 ( 2.20)  |
| C(303) | C(304) | C(305) | O(301) | 10.85 ( 1.80)   |

Table A.3. Structure factors ( $F^2_{\text{obs}}$  &  $F^2_{\text{calc}}$ )<sup>a</sup> for  $[\text{Cu}(\text{dptmp})_2]\text{PF}_6 \cdot \text{THF}$ .

| M   | K | L | Obs   | Calc  | M   | K  | L | Obs  | Calc | M   | K  | L | Obs  | Calc | M    | K   | L   | Obs | Calc | M    | K   | L   | Obs | Calc |      |
|-----|---|---|-------|-------|-----|----|---|------|------|-----|----|---|------|------|------|-----|-----|-----|------|------|-----|-----|-----|------|------|
| 3   | 0 | 0 | 3079  | 3799  | 11  | 2  | 0 | 337  | 356  | 11  | 4  | 0 | -1   |      | 1    | 9   | 6   | 0   | 904  | 708  | 9   | 8   | 0   | 227  | 237  |
| 4   | 0 | 0 | 2968  | 2626  | 12  | 2  | 0 | 836  | 723  | 12  | 4  | 0 | 288  |      | 265  | 10  | 6   | 0   | 12   | 27   | 10  | 8   | 0   | 77   | 74   |
| 5   | 0 | 0 | 996   | 817   | 13  | 2  | 0 | 0    | 3    | 13  | 4  | 0 | 12   |      | 3    | 11  | 6   | 0   | 9    | 15   | 11  | 8   | 0   | 87   | 71   |
| 6   | 0 | 0 | 22    | 65    | 14  | 2  | 0 | 11   | 4    | 14  | 4  | 0 | 10   |      | 3    | 12  | 6   | 0   | 149  | 125  | 12  | 8   | 0   | 53   | 58   |
| 7   | 0 | 0 | 1045  | 1014  | 15  | 2  | 0 | 14   | 3    | 15  | 4  | 0 | 17   |      | 8    | 13  | 6   | 0   | 67   | 69   | 13  | 8   | 0   | 34   | 30   |
| 8   | 0 | 0 | 1722  | 1465  | 16  | 2  | 0 | -9   | 0    | -10 | 5  | 0 | 22   |      | 2    | 14  | 6   | 0   | -7   | 3    | 14  | 8   | 0   | -11  | 3    |
| 9   | 0 | 0 | 1365  | 1173  | -16 | 3  | 0 | 18   | 26   | -17 | 5  | 0 | 61   |      | 28   | 15  | 6   | 0   | 76   | 36   | -17 | 9   | 0   | 31   | 7    |
| 10  | 0 | 0 | 955   | 977   | -15 | 3  | 0 | 11   | 15   | -16 | 5  | 0 | 11   |      | 5    | -18 | 7   | 0   | -19  | 3    | -16 | 9   | 0   | 32   | 31   |
| 11  | 0 | 0 | 57    | 68    | -14 | 3  | 0 | 68   | 72   | -15 | 5  | 0 | -2   |      | 1    | -17 | 7   | 0   | 81   | 54   | -15 | 9   | 0   | 15   | 16   |
| 12  | 0 | 0 | 120   | 129   | -13 | 3  | 0 | 1    | 0    | -14 | 5  | 0 | 102  |      | 89   | -16 | 7   | 0   | 24   | 27   | -14 | 9   | 0   | -8   | 0    |
| 13  | 0 | 0 | 282   | 261   | -12 | 3  | 0 | 68   | 60   | -13 | 5  | 0 | 37   |      | 36   | -15 | 7   | 0   | 15   | 10   | -13 | 9   | 0   | 15   | 10   |
| 14  | 0 | 0 | 544   | 429   | -11 | 3  | 0 | 137  | 134  | -12 | 5  | 0 | 22   |      | 26   | -14 | 7   | 0   | 36   | 24   | -12 | 9   | 0   | 82   | 74   |
| 15  | 0 | 0 | 60    | 38    | -10 | 3  | 0 | 272  | 237  | -11 | 5  | 0 | 397  |      | 354  | -13 | 7   | 0   | 69   | 63   | -11 | 9   | 0   | 17   | 41   |
| 16  | 0 | 0 | 18    | 40    | -9  | 3  | 0 | 154  | 153  | -10 | 5  | 0 | 809  |      | 759  | -12 | 7   | 0   | 7    | 0    | -10 | 9   | 0   | 45   | 52   |
| -16 | 1 | 0 | 27    | 12    | -8  | 3  | 0 | 889  | 749  | -9  | 5  | 0 | 153  |      | 152  | -11 | 7   | 0   | 71   | 84   | -9  | 9   | 0   | 466  | 417  |
| -15 | 1 | 0 | 68    | 48    | -7  | 3  | 0 | 7    | 3    | -8  | 5  | 0 | 265  |      | 293  | -10 | 7   | 0   | 168  | 199  | -8  | 9   | 0   | 79   | 88   |
| -14 | 1 | 0 | 2     | 14    | -6  | 3  | 0 | 1635 | 1373 | -7  | 5  | 0 | 199  |      | 227  | -9  | 7   | 0   | 471  | 424  | -7  | 9   | 0   | -3   | 5    |
| -13 | 1 | 0 | 17    | 1     | -5  | 3  | 0 | 20   | 6    | -6  | 5  | 0 | 1786 |      | 2025 | -8  | 7   | 0   | 7    | 3    | -6  | 9   | 0   | 897  | 819  |
| -12 | 1 | 0 | 127   | 98    | -4  | 3  | 0 | 25   | 32   | -5  | 5  | 0 | 2    |      | 0    | -7  | 7   | 0   | 23   | 16   | -5  | 9   | 0   | 396  | 324  |
| -11 | 1 | 0 | 65    | 76    | -3  | 3  | 0 | 2362 | 2630 | -4  | 5  | 0 | 4398 |      | 4103 | -6  | 7   | 0   | 341  | 360  | -4  | 9   | 0   | 152  | 173  |
| -10 | 1 | 0 | 758   | 659   | -2  | 3  | 0 | 1372 | 1354 | -3  | 5  | 0 | 168  |      | 178  | -5  | 7   | 0   | 169  | 194  | -3  | 9   | 0   | 537  | 627  |
| -9  | 1 | 0 | 477   | 428   | -1  | 3  | 0 | 19   | 9    | -2  | 5  | 0 | 1    |      | 4    | -4  | 7   | 0   | 790  | 730  | -2  | 9   | 0   | 264  | 198  |
| -8  | 1 | 0 | 285   | 273   | 1   | 3  | 0 | 671  | 588  | -1  | 5  | 0 | 2651 |      | 2871 | -3  | 7   | 0   | 1482 | 1715 | -1  | 9   | 0   | 1151 | 1282 |
| -7  | 1 | 0 | 94    | 96    | 2   | 3  | 0 | 2    | 11   | 0   | 5  | 0 | 2304 |      | 2576 | -2  | 7   | 0   | 482  | 409  | 0   | 9   | 0   | 86   | 111  |
| -6  | 1 | 0 | 492   | 464   | 3   | 3  | 0 | 48   | 57   | 1   | 5  | 0 | 55   |      | 77   | -1  | 7   | 0   | 7    | 4    | 1   | 9   | 0   | 100  | 84   |
| -5  | 1 | 0 | 3044  | 3267  | 4   | 3  | 0 | 502  | 427  | 2   | 5  | 0 | 592  |      | 428  | 0   | 7   | 0   | 3686 | 4249 | 2   | 9   | 0   | 878  | 838  |
| -4  | 1 | 0 | 2902  | 3009  | 5   | 3  | 0 | 465  | 490  | 3   | 5  | 0 | 4498 |      | 4128 | 1   | 7   | 0   | 7    | 25   | 3   | 9   | 0   | -1   | 0    |
| -3  | 1 | 0 | 959   | 967   | 6   | 3  | 0 | 10   | 5    | 4   | 5  | 0 | 8554 |      | 7165 | 2   | 7   | 0   | 280  | 473  | 4   | 9   | 0   | 378  | 424  |
| -2  | 1 | 0 | 9400  | 9017  | 7   | 3  | 0 | 525  | 582  | 5   | 5  | 0 | 32   |      | 17   | 3   | 7   | 0   | 816  | 853  | 5   | 9   | 0   | 360  | 297  |
| -1  | 1 | 0 | 537   | 565   | 8   | 3  | 0 | 95   | 76   | 6   | 5  | 0 | 456  |      | 413  | 4   | 7   | 0   | 958  | 885  | 6   | 9   | 0   | 42   | 33   |
| 0   | 1 | 0 | 2592  | 2466  | 9   | 3  | 0 | 452  | 361  | 7   | 5  | 0 | 2    |      | 3    | 5   | 7   | 0   | 525  | 489  | 7   | 9   | 0   | 271  | 268  |
| 1   | 1 | 0 | 193   | 215   | 10  | 3  | 0 | 435  | 402  | 8   | 5  | 0 | 283  |      | 218  | 6   | 7   | 0   | 11   | 24   | 8   | 9   | 0   | 616  | 569  |
| 2   | 1 | 0 | 106   | 112   | 11  | 3  | 0 | 711  | 707  | 9   | 5  | 0 | 173  |      | 129  | 7   | 7   | 0   | 73   | 102  | 9   | 9   | 0   | 102  | 65   |
| 3   | 1 | 0 | 248   | 298   | 12  | 3  | 0 | 35   | 27   | 10  | 5  | 0 | 138  |      | 133  | 8   | 7   | 0   | 629  | 557  | 10  | 9   | 0   | 4    | 7    |
| 4   | 1 | 0 | 951   | 872   | 13  | 3  | 0 | 102  | 80   | 11  | 5  | 0 | 277  |      | 287  | 9   | 7   | 0   | 11   | 31   | 11  | 9   | 0   | 33   | 38   |
| 5   | 1 | 0 | 1293  | 1152  | 14  | 3  | 0 | 8    | 3    | 12  | 5  | 0 | 2    |      | 2    | 10  | 7   | 0   | 95   | 86   | 12  | 9   | 0   | 51   | 65   |
| 6   | 1 | 0 | 97    | 73    | 15  | 3  | 0 | 9    | 2    | 13  | 5  | 0 | 62   |      | 50   | 11  | 7   | 0   | 297  | 261  | 13  | 9   | 0   | 17   | 8    |
| 7   | 1 | 0 | 2063  | 1949  | -18 | 4  | 0 | 8    | 7    | 14  | 5  | 0 | 5    |      | 15   | 12  | 7   | 0   | 61   | 67   | -17 | 10  | 0   | 85   | 2    |
| 8   | 1 | 0 | 852   | 761   | -17 | 4  | 0 | 22   | 24   | 15  | 5  | 0 | -10  |      | 0    | 13  | 7   | 0   | 38   | 19   | -16 | 10  | 0   | -15  | 6    |
| 9   | 1 | 0 | 143   | 232   | -16 | 4  | 0 | 103  | 102  | -18 | 6  | 0 | 12   |      | 1    | 14  | 7   | 0   | 51   | 35   | -15 | 10  | 0   | -12  | 3    |
| 10  | 1 | 0 | 8     | 17    | -15 | 4  | 0 | 17   | 5    | -17 | 6  | 0 | -13  |      | 15   | -17 | 8   | 0   | -10  | 1    | -14 | 10  | 0   | 0    | 16   |
| 11  | 1 | 0 | 14    | 5     | -14 | 4  | 0 | 14   | 9    | -16 | 6  | 0 | -1   |      | 19   | -16 | 8   | 0   | 7    | 1    | -13 | 10  | 0   | 32   | 51   |
| 12  | 1 | 0 | 62    | 58    | -13 | 4  | 0 | 130  | 129  | -15 | 6  | 0 | 4    |      | 12   | -15 | 8   | 0   | -1   | 4    | -12 | 10  | 0   | 76   | 65   |
| 13  | 1 | 0 | 22    | 10    | -12 | 4  | 0 | 178  | 156  | -14 | 6  | 0 | -1   |      | 0    | -14 | 8   | 0   | 14   | 6    | -11 | 10  | 0   | 19   | 6    |
| 14  | 1 | 0 | 31    | 24    | -11 | 4  | 0 | 13   | 2    | -13 | 6  | 0 | 44   |      | 33   | -13 | 8   | 0   | -5   | 12   | -10 | 10  | 0   | 14   | 12   |
| 15  | 1 | 0 | 228   | 203   | -10 | 4  | 0 | 90   | 87   | -12 | 6  | 0 | 334  |      | 364  | -12 | 8   | 0   | -3   | 4    | -9  | 10  | 0   | 51   | 49   |
| 16  | 1 | 0 | -5    | 3     | -9  | 4  | 0 | 2706 | 2565 | -11 | 6  | 0 | 128  |      | 88   | -11 | 8   | 0   | 81   | 62   | -8  | 10  | 0   | 49   | 39   |
| -11 | 2 | 0 | 19    | 9     | -8  | 4  | 0 | 460  | 400  | -10 | 6  | 0 | 22   |      | 27   | -10 | 8   | 0   | 23   | 34   | -7  | 10  | 0   | 80   | 73   |
| -10 | 2 | 0 | 95    | 144   | -7  | 4  | 0 | 37   | 70   | -9  | 6  | 0 | 426  |      | 394  | -9  | 8   | 0   | 25   | 27   | -6  | 10  | 0   | 297  | 278  |
| -9  | 2 | 0 | 716   | 617   | -6  | 4  | 0 | 249  | 152  | -8  | 6  | 0 | 754  |      | 657  | -8  | 8   | 0   | 176  | 135  | -5  | 10  | 0   | -2   | 2    |
| -8  | 2 | 0 | -2    | 2     | -5  | 4  | 0 | 802  | 895  | -7  | 6  | 0 | 158  |      | 128  | -7  | 8   | 0   | 11   | 10   | -4  | 10  | 0   | 128  | 113  |
| -7  | 2 | 0 | 293   | 358   | -4  | 4  | 0 | 119  | 82   | -6  | 6  | 0 | 132  |      | 112  | -6  | 8   | 0   | 3    | 5    | -3  | 10  | 0   | 1517 | 1366 |
| -6  | 2 | 0 | 1047  | 1312  | -3  | 4  | 0 | 25   | 12   | -5  | 6  | 0 | 2897 |      | 2839 | -5  | 8   | 0   | 904  | 870  | -2  | 10  | 0   | 355  | 323  |
| -5  | 2 | 0 | 3     | 12    | -2  | 4  | 0 | 2205 | 2135 | -4  | 6  | 0 | 486  |      | 528  | -4  | 8   | 0   | 801  | 745  | -1  | 10  | 0   | 6    | 7    |
| -4  | 2 | 0 | 714   | 788   | -1  | 4  | 0 | 862  | 1090 | -3  | 6  | 0 | 7    |      | 13   | -3  | 8   | 0   | 648  | 618  | 0   | 10  | 0   | 1101 | 1037 |
| -3  | 2 | 0 | 19034 | 14924 | 0   | 4  | 0 | 1435 | 1368 | -2  | 6  | 0 | 1153 |      | 1258 | -2  | 8   | 0   | 69   | 51   | 1   | 10  | 0   | 60   | 63   |
| -2  | 2 | 0 | 37913 | 29271 | 1   | 4  | 0 | 8    | 18   | -1  | 6  | 0 | 1935 |      | 2298 | -1  | 8   | 0   | 55   | 55   | 2   | 10  | 0   | 136  | 115  |
| -1  | 2 | 0 | 5110  | 5120  | 2   | 4  | 0 | 207  | 251  | 0   | 6  | 0 | 413  |      | 454  | 0   | 8   | 0   | 339  | 433  | 3   | 10  | 0   | 278  | 286  |
| 0   | 2 | 0 | 493   | 564   | 3   | 4  | 0 | 47   | 36   | 1   | 6  | 0 | 573  |      | 406  | 1   | 8   | 0   | 10   | 18   | 4   | 10  | 0   | 0    | 10   |
| 1   | 2 | 0 | 8224  | 8178  | 4   | 4  | 0 | 2    | 26   | 2   | 6  | 0 | 2405 |      | 2375 | 2   | 8   | 0   | 23   | 22   | 5   | 10  | 0   | 70   | 80   |
| 2   | 2 | 0 | 80    | 117   | 5   | 4  | 0 | 2061 | 1955 | 3   | 6  | 0 | 3158 |      | 3065 | 3   | 8   | 0   | 980  | 1093 | 6   | 10  | 0   | 37   | 36   |
| 3   | 2 | 0 | 352   | 327   | 6   | 4  | 0 | 5    | 8    | 4   | 6  | 0 | 210  |      | 258  | 4   | 8   | 0   | 382  | 387  | 7   | 10  | 0   | 69   | 58   |
| 4   | 2 | 0 | 353   | 390   | 7   | 4  | 0 | -1   | 3    | 5   | 6  | 0 | 1919 |      | 1803 | 5   | 8   | 0   | 11   | 17   | 8   | 10  | 0   | 86   | 99   |
| 5   | 2 | 0 | 3033  | 2660  | 8   | 4  | 0 | 1110 | 1041 | 6   | 6  | 0 | 1108 |      | 1247 | 6   | 8   | 0   | 196  | 169  | 9   | 10  | 0   | 3    | 11   |
| 6   | 2 | 0 | 433   | 458   | 9   | 4  | 0 | 599  | 542  | 7   | 6  | 0 | 23   |      | 21   | 7   | 8   | 0   | -3   | 1    | 10  | 10  | 0   | 40   | 14   |
| 7   | 2 | 0 | 38    | 55    | 10  | 4  | 0 | 542  | 571  | 8   | 6  | 0 | 616  |      | 638  | 8   | 8   | 0   | 2    | 3    | 11  | 10  | 0   | 62   | 46   |
| 8   | 2 | 0 | 14    | 1     | -6  | 13 | 0 | -2   | 3    | -7  | 16 | 0 | 75   |      | 25   | 0   | -17 | 1   | 24   | 23   | 3   | -14 | 1   | 3    | 8    |
| 9   | 2 | 0 | 15    | 0     | -5  | 13 | 0 | 20   | 2    | -6  | 16 | 0 | 34   |      | 0    | 1   | -17 | 1   | 22   | 14   | 4   | -14 | 1   | 53   | 44   |
| 10  | 2 | 0 | 12    | 1     | -4  | 13 | 0 | 8    | 21   | -5  | 16 | 0 | 14   |      | 8    | 2   | -17 | 1   |      |      |     |     |     |      |      |

Table A.3, continued

| M   | K   | L | Obe | Calc | M   | K  | L | Obe  | Calc | M   | K   | L | Obe  | Calc | M   | K   | L | Obe  | Calc | M   | K   | L | Obe  | Calc |
|-----|-----|---|-----|------|-----|----|---|------|------|-----|-----|---|------|------|-----|-----|---|------|------|-----|-----|---|------|------|
| -9  | 12  | 0 | 31  | 24   | 6   | 14 | 0 | 20   | 12   | 1   | 18  | 0 | 11   | 10   | -2  | -15 | 1 | 3    | 12   | 14  | -13 | 1 | 3    | 0    |
| -9  | 12  | 0 | 3   | 2    | 7   | 14 | 0 | 22   | 14   | 2   | 18  | 0 | 4    | 18   | -1  | -15 | 1 | 13   | 5    | 15  | -13 | 1 | 11   | 1    |
| -7  | 12  | 0 | 28  | 41   | 8   | 14 | 0 | 14   | 0    | 3   | 18  | 0 | 11   | 4    | 0   | -15 | 1 | 19   | 20   | -12 | -12 | 1 | -4   | 5    |
| -6  | 12  | 0 | 97  | 92   | 9   | 14 | 0 | -7   | 1    | -1  | 19  | 0 | 8    | 1    | 1   | -15 | 1 | 21   | 10   | -11 | -12 | 1 | -6   | 0    |
| -5  | 12  | 0 | 17  | 17   | -12 | 15 | 0 | -11  | 1    | -2  | -19 | 1 | -2   | 7    | 2   | -15 | 1 | 5    | 3    | -10 | -12 | 1 | 53   | 49   |
| -4  | 12  | 0 | 4   | 2    | -11 | 15 | 0 | 5    | 7    | -1  | -19 | 1 | -9   | 1    | 3   | -15 | 1 | -4   | 0    | -9  | -12 | 1 | 24   | 31   |
| -3  | 12  | 0 | 20  | 18   | -10 | 15 | 0 | 15   | 10   | 0   | -19 | 1 | 6    | 4    | 4   | -15 | 1 | 19   | 26   | -8  | -12 | 1 | 17   | 22   |
| -2  | 12  | 0 | 175 | 157  | -9  | 15 | 0 | 31   | 10   | 1   | -19 | 1 | 39   | 3    | 5   | -15 | 1 | 42   | 36   | -7  | -12 | 1 | 74   | 76   |
| -1  | 12  | 0 | 67  | 49   | -8  | 15 | 0 | 16   | 12   | 2   | -19 | 1 | -1   | 0    | 6   | -15 | 1 | 0    | 4    | -6  | -12 | 1 | 79   | 64   |
| 0   | 12  | 0 | 116 | 100  | -7  | 15 | 0 | -5   | 1    | 3   | -19 | 1 | -13  | 2    | 7   | -15 | 1 | 1    | 1    | -5  | -12 | 1 | 6    | 1    |
| 1   | 12  | 0 | 73  | 81   | -6  | 15 | 0 | 5    | 5    | 4   | -19 | 1 | -1   | 7    | 8   | -15 | 1 | 39   | 11   | -4  | -12 | 1 | 72   | 86   |
| 2   | 12  | 0 | 110 | 142  | -5  | 15 | 0 | 22   | 10   | -4  | -19 | 1 | -4   | 2    | 9   | -15 | 1 | 36   | 4    | -3  | -12 | 1 | 87   | 63   |
| 3   | 12  | 0 | -3  | 5    | -4  | 15 | 0 | 82   | 84   | -3  | -19 | 1 | 6    | 7    | 10  | -15 | 1 | -1   | 0    | -2  | -12 | 1 | 35   | 30   |
| 4   | 12  | 0 | 79  | 80   | -3  | 15 | 0 | 68   | 86   | -2  | -19 | 1 | 14   | 34   | 11  | -15 | 1 | -10  | 2    | -1  | -12 | 1 | 81   | 91   |
| 5   | 12  | 0 | 126 | 130  | -2  | 15 | 0 | -3   | 3    | -1  | -19 | 1 | 26   | 57   | 12  | -15 | 1 | 41   | 4    | 0   | -12 | 1 | 103  | 101  |
| 6   | 12  | 0 | 6   | 1    | -1  | 15 | 0 | 27   | 13   | 0   | -19 | 1 | 1    | 13   | 13  | -15 | 1 | 8    | 0    | 1   | -12 | 1 | 110  | 133  |
| 7   | 12  | 0 | 2   | 0    | 0   | 15 | 0 | 119  | 144  | 1   | -19 | 1 | 10   | 0    | -10 | -14 | 1 | -11  | 4    | 2   | -12 | 1 | 4    | 2    |
| 8   | 12  | 0 | 4   | 4    | 1   | 15 | 0 | 46   | 46   | 2   | -19 | 1 | 21   | 4    | -9  | -14 | 1 | 34   | 4    | 3   | -12 | 1 | 121  | 97   |
| 9   | 12  | 0 | -5  | 1    | 2   | 15 | 0 | 13   | 13   | 3   | -19 | 1 | -5   | 0    | -8  | -14 | 1 | 17   | 0    | 4   | -12 | 1 | 206  | 193  |
| 10  | 12  | 0 | 9   | 1    | 3   | 15 | 0 | 8    | 9    | 4   | -19 | 1 | -8   | 0    | -7  | -14 | 1 | 11   | 3    | 5   | -12 | 1 | 77   | 76   |
| 11  | 12  | 0 | -8  | 11   | 4   | 15 | 0 | -4   | 3    | 5   | -19 | 1 | 0    | 4    | -6  | -14 | 1 | 1    | 1    | 6   | -12 | 1 | 12   | 1    |
| -14 | 13  | 0 | 15  | 17   | 5   | 15 | 0 | 9    | 2    | 6   | -19 | 1 | -4   | 2    | -5  | -14 | 1 | -1   | 0    | 7   | -12 | 1 | 114  | 92   |
| -13 | 13  | 0 | -10 | 6    | 6   | 15 | 0 | 12   | 11   | 7   | -19 | 1 | 0    | 1    | -4  | -14 | 1 | 59   | 44   | 8   | -12 | 1 | 91   | 110  |
| -12 | 13  | 0 | 10  | 19   | 7   | 15 | 0 | 10   | 2    | -6  | -17 | 1 | 16   | 6    | -3  | -14 | 1 | 27   | 37   | 9   | -12 | 1 | 11   | 13   |
| -11 | 13  | 0 | 22  | 35   | 8   | 15 | 0 | -12  | 2    | -5  | -17 | 1 | 0    | 1    | -2  | -14 | 1 | 16   | 26   | 10  | -12 | 1 | 29   | 3    |
| -10 | 13  | 0 | 0   | 3    | -11 | 16 | 0 | -9   | 12   | -4  | -17 | 1 | 8    | 9    | -1  | -14 | 1 | 46   | 46   | 11  | -12 | 1 | 83   | 74   |
| -9  | 13  | 0 | 0   | 8    | -10 | 16 | 0 | 12   | 15   | -3  | -17 | 1 | 16   | 29   | 0   | -14 | 1 | 147  | 126  | 12  | -12 | 1 | 31   | 29   |
| -8  | 13  | 0 | 93  | 72   | -9  | 16 | 0 | -8   | 2    | -2  | -17 | 1 | 2    | 23   | 1   | -14 | 1 | 89   | 100  | 13  | -12 | 1 | 5    | 1    |
| -7  | 13  | 0 | 33  | 32   | -8  | 16 | 0 | -9   | 6    | -1  | -17 | 1 | -5   | 0    | 2   | -14 | 1 | 29   | 30   | 14  | -12 | 1 | 6    | 0    |
| -15 | -12 | 1 | -9  | 0    | -10 | -9 | 1 | 196  | 239  | -9  | -7  | 1 | 15   | 39   | -11 | -5  | 1 | -4   | 1    | -14 | -3  | 1 | 3    | 7    |
| -16 | -12 | 1 | 14  | 0    | -9  | -9 | 1 | 13   | 29   | -8  | -7  | 1 | 485  | 381  | -10 | -5  | 1 | 618  | 541  | -13 | -3  | 1 | 33   | 29   |
| -12 | -11 | 1 | -6  | 20   | -8  | -9 | 1 | 42   | 32   | -7  | -7  | 1 | 215  | 150  | -9  | -5  | 1 | 140  | 158  | -12 | -3  | 1 | 169  | 178  |
| -11 | -11 | 1 | 38  | 43   | -7  | -9 | 1 | 128  | 54   | -6  | -7  | 1 | 87   | 87   | -8  | -5  | 1 | 1001 | 985  | -11 | -3  | 1 | 62   | 87   |
| -10 | -11 | 1 | 29  | 24   | -6  | -9 | 1 | 247  | 203  | -5  | -7  | 1 | 391  | 378  | -7  | -5  | 1 | 26   | 40   | -10 | -3  | 1 | 23   | 15   |
| -9  | -11 | 1 | 2   | 17   | -5  | -9 | 1 | 46   | 37   | -4  | -7  | 1 | 1219 | 1206 | -6  | -5  | 1 | 404  | 410  | -9  | -3  | 1 | 136  | 110  |
| -8  | -11 | 1 | 63  | 63   | -4  | -9 | 1 | 363  | 312  | -3  | -7  | 1 | 945  | 987  | -5  | -5  | 1 | 241  | 302  | -8  | -3  | 1 | 669  | 680  |
| -7  | -11 | 1 | 168 | 171  | -3  | -9 | 1 | 373  | 292  | -2  | -7  | 1 | 121  | 185  | -4  | -5  | 1 | -1   | 5    | -7  | -3  | 1 | 8    | 2    |
| -6  | -11 | 1 | -2  | 6    | -2  | -9 | 1 | 98   | 125  | -1  | -7  | 1 | 23   | 44   | -3  | -5  | 1 | 419  | 397  | -6  | -3  | 1 | 1029 | 934  |
| -5  | -11 | 1 | 65  | 38   | -1  | -9 | 1 | 1791 | 1756 | 0   | -7  | 1 | 53   | 57   | -2  | -5  | 1 | 3840 | 3870 | -5  | -3  | 1 | 2171 | 2042 |
| -4  | -11 | 1 | 166 | 169  | 0   | -9 | 1 | 416  | 333  | -1  | -7  | 1 | 799  | 841  | -1  | -5  | 1 | 810  | 886  | -4  | -3  | 1 | 3692 | 3955 |
| -3  | -11 | 1 | 3   | 4    | 1   | -9 | 1 | 239  | 295  | 2   | -7  | 1 | 37   | 51   | 0   | -5  | 1 | 1626 | 1656 | -3  | -3  | 1 | 259  | 295  |
| -2  | -11 | 1 | 101 | 88   | 2   | -9 | 1 | 1160 | 1095 | 3   | -7  | 1 | 242  | 282  | 1   | -5  | 1 | 257  | 144  | -2  | -3  | 1 | 13   | 25   |
| -1  | -11 | 1 | 591 | 548  | 3   | -9 | 1 | 341  | 318  | 4   | -7  | 1 | 35   | 22   | 2   | -5  | 1 | 2197 | 2438 | -1  | -3  | 1 | 27   | 34   |
| 0   | -11 | 1 | 94  | 69   | 4   | -9 | 1 | 677  | 618  | 5   | -7  | 1 | 195  | 160  | 3   | -5  | 1 | 1575 | 1647 | 1   | -3  | 1 | 793  | 501  |
| 1   | -11 | 1 | 97  | 100  | 5   | -9 | 1 | 82   | 78   | 6   | -7  | 1 | 893  | 759  | 4   | -5  | 1 | 349  | 315  | 2   | -3  | 1 | 2200 | 2013 |
| 2   | -11 | 1 | 519 | 473  | 6   | -9 | 1 | 91   | 129  | 7   | -7  | 1 | 37   | 44   | 5   | -5  | 1 | 1980 | 2010 | 3   | -3  | 1 | 809  | 906  |
| 3   | -11 | 1 | 355 | 283  | 7   | -9 | 1 | 316  | 259  | 8   | -7  | 1 | 258  | 321  | 6   | -5  | 1 | 467  | 455  | 4   | -3  | 1 | 324  | 307  |
| 4   | -11 | 1 | 378 | 316  | 8   | -9 | 1 | 10   | 15   | 9   | -7  | 1 | 339  | 326  | 7   | -5  | 1 | 5    | 0    | 5   | -3  | 1 | 687  | 760  |
| 5   | -11 | 1 | 90  | 91   | 9   | -9 | 1 | 39   | 47   | 10  | -7  | 1 | 51   | 28   | 8   | -5  | 1 | 1191 | 1242 | 6   | -3  | 1 | 799  | 798  |
| 6   | -11 | 1 | 122 | 112  | 10  | -9 | 1 | 141  | 122  | 11  | -7  | 1 | 254  | 257  | 9   | -5  | 1 | 645  | 526  | 7   | -3  | 1 | 1    | 1    |
| 7   | -11 | 1 | 130 | 99   | 11  | -9 | 1 | 11   | 15   | 12  | -7  | 1 | 140  | 105  | 10  | -5  | 1 | 5    | 1    | 8   | -3  | 1 | 1507 | 1468 |
| 8   | -11 | 1 | 23  | 18   | 12  | -9 | 1 | 46   | 34   | 13  | -7  | 1 | 10   | 1    | 11  | -5  | 1 | 246  | 241  | 9   | -3  | 1 | 520  | 544  |
| 9   | -11 | 1 | 46  | 51   | 13  | -9 | 1 | 0    | 1    | 14  | -7  | 1 | 4    | 12   | 12  | -5  | 1 | 112  | 100  | 10  | -3  | 1 | 998  | 834  |
| 10  | -11 | 1 | 94  | 90   | 14  | -9 | 1 | 0    | 2    | 15  | -7  | 1 | -6   | 2    | 13  | -5  | 1 | 177  | 165  | 11  | -3  | 1 | 106  | 103  |
| 11  | -11 | 1 | -4  | 2    | 15  | -9 | 1 | -1   | 2    | 16  | -7  | 1 | 31   | 32   | 14  | -5  | 1 | -4   | 3    | 12  | -3  | 1 | 90   | 92   |
| 12  | -11 | 1 | 39  | 31   | 16  | -9 | 1 | 0    | 18   | 17  | -7  | 1 | 24   | 3    | 15  | -5  | 1 | -3   | 14   | 13  | -3  | 1 | 283  | 283  |
| 13  | -11 | 1 | 56  | 21   | 17  | -9 | 1 | 33   | 16   | 18  | -7  | 1 | -5   | 0    | 16  | -5  | 1 | 110  | 121  | 14  | -3  | 1 | 12   | 0    |
| 14  | -11 | 1 | 13  | 0    | -14 | -8 | 1 | -7   | 4    | -15 | -6  | 1 | 3    | 24   | 17  | -5  | 1 | -12  | 4    | 15  | -3  | 1 | 19   | 35   |
| 15  | -11 | 1 | -4  | 0    | -13 | -8 | 1 | 15   | 7    | -14 | -6  | 1 | 24   | 11   | 18  | -5  | 1 | 1    | 5    | 16  | -3  | 1 | 166  | 142  |
| 16  | -11 | 1 | 10  | 9    | -12 | -8 | 1 | 41   | 45   | -13 | -6  | 1 | 48   | 30   | -15 | -4  | 1 | 50   | 26   | -16 | -2  | 1 | 16   | 35   |
| -13 | -10 | 1 | 37  | 17   | -11 | -8 | 1 | 131  | 109  | -12 | -6  | 1 | 42   | 56   | -14 | -4  | 1 | 13   | 12   | -15 | -2  | 1 | 6    | 10   |
| -12 | -10 | 1 | 47  | 53   | -10 | -8 | 1 | 21   | 21   | -11 | -6  | 1 | 351  | 351  | -13 | -4  | 1 | 99   | 120  | -14 | -2  | 1 | 113  | 109  |
| -11 | -10 | 1 | -5  | 4    | -9  | -8 | 1 | 52   | 51   | -10 | -6  | 1 | -3   | 4    | -12 | -4  | 1 | 0    | 7    | -13 | -2  | 1 | 375  | 384  |
| -10 | -10 | 1 | 85  | 90   | -8  | -8 | 1 | 141  | 107  | -9  | -6  | 1 | 394  | 348  | -11 | -4  | 1 | 69   | 71   | -12 | -2  | 1 | 428  | 335  |
| -9  | -10 | 1 | 64  | 66   | -7  | -8 | 1 | 58   | 41   | -8  | -6  | 1 | 373  | 418  | -10 | -4  | 1 | 1059 | 1020 | -11 | -2  | 1 | 16   | 27   |
| -8  | -10 | 1 | 146 | 171  | -6  | -8 | 1 | 532  | 527  | -7  | -6  | 1 | 456  | 329  | -9  | -4  | 1 | 0    | 3    | -10 | -2  | 1 | 16   | 24   |
| -7  | -10 | 1 | 32  | 41   | -5  | -8 | 1 | 532  | 503  | -6  | -6  | 1 | 77   | 50   | -8  | -4  | 1 | 100  | 166  | -9  | -2  | 1 | 812  | 898  |
| -6  | -10 | 1 | 10  | 3    | -4  | -8 | 1 | 1707 | 1558 | -5  | -6  | 1 | 708  | 745  | -7  | -4  | 1 | 191  | 190  | -8  | -2  | 1 | 202  | 173  |
| -5  | -10 | 1 | 52  | 51   | -3  | -8 | 1 | 90   | 111  | -4  | -6  | 1 | 679  | 675  | -6  | -4  | 1 | 14   | 6    | -7  | -2  | 1 | 1987 | 1954 |
| -4  | -10 | 1 | 200 | 191  | -2  | -8 | 1 | 248  | 220  | -3  | -6  | 1 | 225  | 210  | -5  | -4  | 1 | 584  | 427  | -6  | -2  | 1 | 134  | 176  |
| -3  | -10 | 1 | 21  | 31   | -1  | -8 | 1 | 85   | 115  | -2  | -6  | 1 | 13   | 25   | -4  | -4  | 1 | 6362 | 6396 | -5  | -2  | 1 | 30   | 13   |
| -2  | -10 | 1 | 174 | 159  | 0   | -8 | 1 | 83   |      |     |     |   |      |      |     |     |   |      |      |     |     |   |      |      |

Table A.3, continued

| M  | K  | L | Obs   | Calc  | M   | K  | L | Obs   | Calc | M   | K  | L | Obs  | Calc | M   | K   | L | Obs  | Calc | M   | K   | L | Obs  | Calc |
|----|----|---|-------|-------|-----|----|---|-------|------|-----|----|---|------|------|-----|-----|---|------|------|-----|-----|---|------|------|
| 3  | -1 | 1 | 974   | 1116  | 12  | 1  | 1 | 212   | 261  | 14  | 3  | 1 | 21   | 26   | 14  | 5   | 1 | 31   | 49   | 13  | 7   | 1 | 140  | 133  |
| 4  | -1 | 1 | 15827 | 14418 | 13  | 1  | 1 | 1     | 28   | 15  | 3  | 1 | 2    | 6    | 15  | 5   | 1 | -11  | 3    | 14  | 7   | 1 | -12  | 13   |
| 5  | -1 | 1 | 276   | 314   | 14  | 1  | 1 | 19    | 13   | -10 | 4  | 1 | -16  | 7    | -10 | 6   | 1 | 40   | 3    | -17 | 0   | 1 | -19  | 7    |
| 6  | -1 | 1 | 389   | 360   | 15  | 1  | 1 | -1    | 10   | -16 | 4  | 1 | 40   | 12   | -17 | 6   | 1 | 40   | 29   | -16 | 0   | 1 | 22   | 36   |
| 7  | -1 | 1 | 1991  | 1951  | 16  | 1  | 1 | -6    | 5    | -15 | 4  | 1 | 3    | 9    | -16 | 6   | 1 | 32   | 24   | -15 | 0   | 1 | -9   | 4    |
| 8  | -1 | 1 | 40    | 71    | -16 | 2  | 1 | 85    | 94   | -14 | 4  | 1 | 83   | 70   | -15 | 6   | 1 | 17   | 0    | -14 | 0   | 1 | 7    | 3    |
| 9  | -1 | 1 | 239   | 355   | -15 | 2  | 1 | 5     | 1    | -13 | 4  | 1 | 24   | 20   | -14 | 6   | 1 | 25   | 31   | -13 | 0   | 1 | -1   | 9    |
| 10 | -1 | 1 | 25    | 11    | -14 | 2  | 1 | 61    | 31   | -12 | 4  | 1 | 344  | 395  | -13 | 6   | 1 | 34   | 40   | -12 | 0   | 1 | 70   | 63   |
| 11 | -1 | 1 | 20    | 6     | -13 | 2  | 1 | 43    | 55   | -11 | 4  | 1 | 1250 | 1140 | -12 | 6   | 1 | 84   | 100  | -11 | 0   | 1 | 14   | 22   |
| 12 | -1 | 1 | 41    | 72    | -12 | 2  | 1 | 542   | 99   | -10 | 4  | 1 | 2008 | 1771 | -11 | 6   | 1 | 61   | 41   | -10 | 0   | 1 | 184  | 181  |
| 13 | -1 | 1 | 120   | 103   | -11 | 2  | 1 | 340   | 254  | -9  | 4  | 1 | 13   | 25   | -10 | 6   | 1 | 311  | 241  | -9  | 0   | 1 | 240  | 225  |
| 14 | -1 | 1 | 104   | 89    | -10 | 2  | 1 | 200   | 191  | -8  | 4  | 1 | 815  | 878  | -9  | 6   | 1 | 74   | 105  | -8  | 0   | 1 | 180  | 135  |
| 15 | -1 | 1 | -1    | 2     | -9  | 2  | 1 | 223   | 200  | -7  | 4  | 1 | 89   | 107  | -8  | 6   | 1 | 17   | 7    | -7  | 0   | 1 | 131  | 106  |
| 16 | -1 | 1 | 46    | 27    | -8  | 2  | 1 | 289   | 391  | -6  | 4  | 1 | 1331 | 1263 | -7  | 6   | 1 | 318  | 327  | -6  | 0   | 1 | 445  | 401  |
| 17 | -1 | 1 | 159   | 126   | -7  | 2  | 1 | 92    | 93   | -5  | 4  | 1 | 61   | 69   | -6  | 6   | 1 | 2357 | 2026 | -5  | 0   | 1 | 1022 | 1051 |
| 18 | -1 | 1 | 44    | 36    | -6  | 2  | 1 | 110   | 87   | -4  | 4  | 1 | 306  | 434  | -5  | 6   | 1 | 20   | 25   | -4  | 0   | 1 | 121  | 120  |
| 19 | -1 | 1 | 0     | 16    | -5  | 2  | 1 | 108   | 277  | -3  | 4  | 1 | 3402 | 3715 | -4  | 6   | 1 | 802  | 844  | -3  | 0   | 1 | 590  | 536  |
| 20 | -1 | 1 | 132   | 130   | -4  | 2  | 1 | 809   | 863  | -2  | 4  | 1 | 603  | 532  | -3  | 6   | 1 | 211  | 230  | -2  | 0   | 1 | 3035 | 3119 |
| 21 | -1 | 1 | 100   | 92    | -3  | 2  | 1 | 246   | 411  | -1  | 4  | 1 | 5470 | 5305 | -2  | 6   | 1 | 1386 | 1237 | -1  | 0   | 1 | 13   | 19   |
| 22 | -1 | 1 | 183   | 128   | -2  | 2  | 1 | 19    | 31   | 0   | 4  | 1 | 65   | 66   | -1  | 6   | 1 | 243  | 292  | 0   | 0   | 1 | 5    | 5    |
| 23 | -1 | 1 | 34    | 30    | -1  | 2  | 1 | 404   | 971  | 1   | 4  | 1 | 136  | 144  | 0   | 6   | 1 | 993  | 973  | 1   | 0   | 1 | 938  | 1091 |
| 24 | -1 | 1 | 28    | 42    | 2   | 2  | 1 | 3941  | 4161 | 2   | 4  | 1 | 1472 | 1565 | 1   | 6   | 1 | 623  | 6605 | 2   | 1   | 1 | 68   | 26   |
| 25 | -1 | 1 | 945   | 869   | 3   | 2  | 1 | 510   | 690  | 3   | 4  | 1 | 2697 | 2655 | 2   | 6   | 1 | 861  | 475  | 3   | 0   | 1 | 487  | 566  |
| 26 | -1 | 1 | 32    | 41    | 4   | 2  | 1 | 346   | 400  | 4   | 4  | 1 | 4817 | 5293 | 3   | 6   | 1 | 176  | 122  | 4   | 0   | 1 | 419  | 397  |
| 27 | -1 | 1 | 2806  | 2477  | 5   | 2  | 1 | 1744  | 2006 | 5   | 4  | 1 | 164  | 117  | 4   | 6   | 1 | 1553 | 1769 | 5   | 0   | 1 | 182  | 171  |
| 28 | -1 | 1 | 348   | 439   | 6   | 2  | 1 | 73    | 81   | 6   | 4  | 1 | 240  | 267  | 5   | 6   | 1 | 623  | 636  | 6   | 0   | 1 | 431  | 377  |
| 29 | -1 | 1 | 257   | 260   | 7   | 2  | 1 | 41    | 36   | 7   | 4  | 1 | 1024 | 836  | 6   | 6   | 1 | 16   | 8    | 7   | 0   | 1 | 180  | 179  |
| 30 | -1 | 1 | 2784  | 3005  | 8   | 2  | 1 | 149   | 125  | 8   | 4  | 1 | -1   | 3    | 7   | 6   | 1 | 345  | 238  | 8   | 0   | 1 | 502  | 468  |
| 31 | -1 | 1 | 2075  | 2134  | 9   | 2  | 1 | 245   | 268  | 9   | 4  | 1 | 189  | 245  | 8   | 6   | 1 | 21   | 53   | 9   | 0   | 1 | 123  | 127  |
| 32 | -1 | 1 | 101   | 96    | 10  | 2  | 1 | 579   | 529  | 10  | 4  | 1 | 1102 | 923  | 9   | 6   | 1 | 30   | 7    | 10  | 0   | 1 | 22   | 23   |
| 33 | -1 | 1 | 3318  | 3674  | 11  | 2  | 1 | 194   | 213  | 11  | 4  | 1 | 96   | 54   | 10  | 6   | 1 | 243  | 230  | 11  | 0   | 1 | 106  | 105  |
| 34 | -1 | 1 | 34    | 11    | 12  | 2  | 1 | 46    | 41   | 12  | 4  | 1 | 13   | 36   | 11  | 6   | 1 | 96   | 78   | 12  | 0   | 1 | 119  | 76   |
| 35 | -1 | 1 | 145   | 180   | 13  | 2  | 1 | 70    | 80   | 13  | 4  | 1 | 343  | 272  | 12  | 6   | 1 | 59   | 42   | 13  | 0   | 1 | 5    | 6    |
| 36 | -1 | 1 | 1897  | 1854  | 14  | 2  | 1 | 55    | 32   | 14  | 4  | 1 | 17   | 14   | 13  | 6   | 1 | 96   | 107  | -17 | 9   | 1 | 13   | 4    |
| 37 | -1 | 1 | 48    | 36    | 15  | 2  | 1 | 2     | 0    | 15  | 4  | 1 | -8   | 1    | 14  | 6   | 1 | 2    | 18   | -16 | 9   | 1 | -13  | 0    |
| 38 | -1 | 1 | 884   | 889   | 16  | 2  | 1 | 30    | 35   | -17 | 5  | 1 | -14  | 8    | -18 | 7   | 1 | 0    | 0    | -15 | 9   | 1 | 8    | 30   |
| 39 | -1 | 1 | 5     | 7     | -16 | 3  | 1 | 15    | 4    | -16 | 5  | 1 | 22   | 18   | -17 | 7   | 1 | -6   | 6    | -14 | 9   | 1 | 20   | 40   |
| 40 | -1 | 1 | 185   | 152   | -15 | 3  | 1 | 22    | 9    | -15 | 5  | 1 | 27   | 11   | -16 | 7   | 1 | 41   | 9    | -13 | 9   | 1 | 40   | 50   |
| 41 | -1 | 1 | 173   | 163   | -14 | 3  | 1 | 5     | 9    | -14 | 5  | 1 | -1   | 7    | -15 | 7   | 1 | 30   | 21   | -12 | 9   | 1 | 5    | 1    |
| 42 | -1 | 1 | -8    | 1     | -13 | 3  | 1 | 146   | 142  | -13 | 5  | 1 | 102  | 105  | -14 | 7   | 1 | 5    | 11   | -11 | 9   | 1 | 192  | 174  |
| 43 | -1 | 1 | 5     | 1     | -12 | 3  | 1 | 6     | 7    | -12 | 5  | 1 | 358  | 298  | -13 | 7   | 1 | 8    | 0    | -10 | 9   | 1 | 48   | 34   |
| 44 | -1 | 1 | 44    | 3     | -11 | 3  | 1 | 39    | 27   | -11 | 5  | 1 | 295  | 292  | -12 | 7   | 1 | 23   | 8    | -9  | 9   | 1 | 5    | 2    |
| 45 | -1 | 1 | -12   | 5     | -10 | 3  | 1 | 472   | 452  | -10 | 5  | 1 | 19   | 15   | -11 | 7   | 1 | 82   | 83   | -9  | 9   | 1 | 5    | 3    |
| 46 | -1 | 1 | 110   | 76    | -9  | 3  | 1 | 542   | 612  | -9  | 5  | 1 | 238  | 272  | -10 | 7   | 1 | 31   | 26   | -7  | 9   | 1 | 54   | 21   |
| 47 | -1 | 1 | 47    | 92    | -8  | 3  | 1 | 241   | 219  | -8  | 5  | 1 | 722  | 663  | -9  | 7   | 1 | 83   | 73   | -6  | 9   | 1 | 68   | 62   |
| 48 | -1 | 1 | 70    | 109   | -7  | 3  | 1 | 23    | 27   | -7  | 5  | 1 | 24   | 12   | -8  | 7   | 1 | 484  | 453  | -5  | 9   | 1 | 88   | 104  |
| 49 | -1 | 1 | 59    | 46    | -6  | 3  | 1 | 171   | 98   | -6  | 5  | 1 | 44   | 34   | -7  | 7   | 1 | 9    | 12   | -4  | 9   | 1 | 806  | 815  |
| 50 | -1 | 1 | -1    | 2     | -5  | 3  | 1 | 160   | 121  | -5  | 5  | 1 | 2466 | 2376 | -6  | 7   | 1 | 124  | 136  | -3  | 9   | 1 | 373  | 310  |
| 51 | -1 | 1 | 1234  | 1085  | -4  | 3  | 1 | 480   | 630  | -4  | 5  | 1 | 78   | 106  | -5  | 7   | 1 | 872  | 771  | -2  | 9   | 1 | 227  | 233  |
| 52 | -1 | 1 | 67    | 30    | -3  | 3  | 1 | 850   | 1048 | -3  | 5  | 1 | 150  | 142  | -4  | 7   | 1 | 1283 | 1215 | -1  | 9   | 1 | 568  | 549  |
| 53 | -1 | 1 | -3    | 10    | -2  | 3  | 1 | 126   | 121  | -2  | 5  | 1 | 489  | 636  | -3  | 7   | 1 | 61   | 40   | 0   | 9   | 1 | 186  | 176  |
| 54 | -1 | 1 | 1438  | 1191  | -1  | 3  | 1 | 4516  | 4031 | -1  | 5  | 1 | 1261 | 1175 | -2  | 7   | 1 | 54   | 73   | 1   | 9   | 1 | 257  | 291  |
| 55 | -1 | 1 | 920   | 835   | 0   | 3  | 1 | 5021  | 4135 | 0   | 5  | 1 | 412  | 229  | -1  | 7   | 1 | 1126 | 1101 | 2   | 9   | 1 | 118  | 87   |
| 56 | -1 | 1 | 22    | 42    | 1   | 3  | 1 | 10183 | 8939 | 1   | 5  | 1 | 1446 | 1752 | 0   | 7   | 1 | 4    | 2    | 3   | 9   | 1 | 27   | 8    |
| 57 | -1 | 1 | 2073  | 2354  | 2   | 3  | 1 | 80    | 119  | 2   | 5  | 1 | 6497 | 5755 | 1   | 7   | 1 | 3    | 10   | 4   | 9   | 1 | 92   | 137  |
| 58 | -1 | 1 | 5788  | 5470  | 3   | 3  | 1 | 720   | 770  | 3   | 5  | 1 | 4518 | 3973 | 2   | 7   | 1 | 29   | 44   | 5   | 9   | 1 | 35   | 35   |
| 59 | -1 | 1 | 3650  | 32136 | 4   | 3  | 1 | 42    | 84   | 4   | 5  | 1 | 411  | 458  | 3   | 7   | 1 | 395  | 398  | 6   | 9   | 1 | 10   | 1    |
| 60 | -1 | 1 | 264   | 249   | -13 | 12 | 1 | 5     | 1    | 3   | 14 | 1 | 69   | 42   | 1   | 18  | 1 | -1   | 6    | -4  | -15 | 2 | 4    | 6    |
| 61 | -1 | 1 | 10    | 14    | -12 | 12 | 1 | 29    | 24   | 4   | 14 | 1 | 20   | 31   | 2   | 18  | 1 | -6   | 1    | -3  | -15 | 2 | -1   | 2    |
| 62 | -1 | 1 | 6     | 15    | -11 | 12 | 1 | 27    | 38   | 5   | 14 | 1 | 18   | 6    | -1  | -19 | 2 | 21   | 9    | -2  | -15 | 2 | 12   | 17   |
| 63 | -1 | 1 | 100   | 104   | -10 | 12 | 1 | 0     | 3    | 6   | 14 | 1 | 25   | 24   | 0   | -19 | 2 | -8   | 2    | -1  | -15 | 2 | 25   | 21   |
| 64 | -1 | 1 | 16    | 2     | -9  | 12 | 1 | 4     | 0    | 7   | 14 | 1 | 76   | 49   | 1   | -19 | 2 | -2   | 2    | 0   | -15 | 2 | 16   | 25   |
| 65 | -1 | 1 | 32    | 6     | -8  | 12 | 1 | 25    | 18   | 8   | 14 | 1 | 14   | 7    | 2   | -19 | 2 | -6   | 1    | 1   | -15 | 2 | 6    | 1    |
| 66 | -1 | 1 | 34    | 24    | -7  | 12 | 1 | -3    | 1    | 9   | 14 | 1 | 84   | 20   | 3   | -19 | 2 | 2    | 1    | 2   | -15 | 2 | -4   | 1    |
| 67 | -1 | 1 | -18   | 7     | -6  | 12 | 1 | 12    | 7    | -12 | 15 | 1 | 34   | 8    | 4   | -19 | 2 | 0    | 0    | 3   | -15 | 2 | 45   | 41   |
| 68 | -1 | 1 | 66    | 23    | -5  | 12 | 1 | 6     | 9    | -11 | 15 | 1 | 38   | 10   | 5   | -19 | 2 | 137  | 1    | 6   | -15 | 2 | 23   | 15   |
| 69 | -1 | 1 | 1     | 10    | -4  | 12 | 1 | 32    | 26   | -10 | 15 | 1 | -19  | 5    | 6   | -19 | 2 | 0    | 0    | 5   | -15 | 2 | -3   | 0    |
| 70 | -1 | 1 | 1     | 0     | -3  | 12 | 1 | 16    | 11   | -9  | 15 | 1 | 2    | 0    | -4  | -10 | 2 | 23   | 1    | 6   | -15 | 2 | 39   | 22   |
| 71 | -1 | 1 | 88    | 112   | -2  | 12 | 1 | 85    | 81   | -8  | 15 | 1 | 10   | 46   | -3  | -10 | 2 | 8    | 6    | 7   | -15 | 2 | 32   | 22   |
| 72 | -1 | 1 | 34    | 33    | -1  | 12 | 1 | 81    | 75   | -7  | 15 | 1 | 0    | 5    | -2  | -10 | 2 | -2   | 0    | 8   | -15 | 2 | 15   | 20   |
| 73 | -1 | 1 | 17    | 26    | 0   | 12 | 1 | 215   | 195  | -6  | 15 | 1 | 49   | 25   | -1  | -10 | 2 | 11   | 1    |     |     |   |      |      |

Table A.3, continued

| M   | K   | L | Obs | Calc | M   | K   | L | Obs | Calc | M   | K  | L | Obs  | Calc | M   | K   | L | Obs  | Calc | M   | K   | L | Obs   | Calc  |
|-----|-----|---|-----|------|-----|-----|---|-----|------|-----|----|---|------|------|-----|-----|---|------|------|-----|-----|---|-------|-------|
| -5  | 11  | 1 | 78  | 107  | 8   | 13  | 1 | 26  | 28   | -8  | 17 | 1 | 26   | 34   | -1  | -16 | 2 | -2   | 7    | -7  | -13 | 2 | 10    | 4     |
| -4  | 11  | 1 | 162 | 145  | 9   | 13  | 1 | 7   | 44   | -7  | 17 | 1 | -8   | 8    | 0   | -16 | 2 | 17   | 33   | -6  | -13 | 2 | 26    | 51    |
| -3  | 11  | 1 | 253 | 248  | 10  | 13  | 1 | 33  | 3    | -6  | 17 | 1 | 9    | 3    | 1   | -16 | 2 | 10   | 4    | -5  | -13 | 2 | -1    | 3     |
| -2  | 11  | 1 | 60  | 66   | -13 | 14  | 1 | 7   | 1    | -5  | 17 | 1 | -7   | 1    | 2   | -16 | 2 | 2    | 0    | -4  | -13 | 2 | 25    | 12    |
| -1  | 11  | 1 | 30  | 27   | -12 | 14  | 1 | 17  | 9    | -4  | 17 | 1 | 19   | 7    | 3   | -16 | 2 | 0    | 2    | -3  | -13 | 2 | 138   | 145   |
| 0   | 11  | 1 | 50  | 46   | -11 | 14  | 1 | 30  | 33   | -3  | 17 | 1 | 4    | 4    | 4   | -16 | 2 | 17   | 13   | -2  | -13 | 2 | -3    | 5     |
| 1   | 11  | 1 | 387 | 341  | -10 | 14  | 1 | 32  | 28   | -2  | 17 | 1 | -6   | 0    | 5   | -16 | 2 | 5    | 10   | -1  | -13 | 2 | 47    | 49    |
| 2   | 11  | 1 | 8   | 3    | -9  | 14  | 1 | 40  | 23   | -1  | 17 | 1 | 11   | 3    | 6   | -16 | 2 | 8    | 1    | 0   | -13 | 2 | 420   | 376   |
| 3   | 11  | 1 | -3  | 1    | -8  | 14  | 1 | 19  | 15   | 0   | 17 | 1 | 2    | 1    | 7   | -16 | 2 | -8   | 4    | 1   | -13 | 2 | 211   | 212   |
| 4   | 11  | 1 | 105 | 73   | -7  | 14  | 1 | 41  | 25   | 1   | 17 | 1 | 39   | 19   | 8   | -16 | 2 | 20   | 28   | 2   | -13 | 2 | 15    | 11    |
| 5   | 11  | 1 | 0   | 5    | -6  | 14  | 1 | 22  | 0    | 2   | 17 | 1 | 11   | 25   | 15  | -16 | 2 | 22   | 31   | 3   | -13 | 2 | 103   | 86    |
| 6   | 11  | 1 | 8   | 2    | -5  | 14  | 1 | 3   | 24   | 3   | 17 | 1 | 20   | 0    | 10  | -16 | 2 | -5   | 8    | 4   | -13 | 2 | 43    | 43    |
| 7   | 11  | 1 | 88  | 98   | -4  | 14  | 1 | 129 | 105  | 4   | 17 | 1 | 15   | 0    | 11  | -16 | 2 | -4   | 0    | 5   | -13 | 2 | -1    | 7     |
| 8   | 11  | 1 | 22  | 14   | -3  | 14  | 1 | 67  | 74   | -5  | 19 | 1 | 21   | 0    | 12  | -16 | 2 | 69   | 2    | 6   | -13 | 2 | 28    | 31    |
| 9   | 11  | 1 | -7  | 5    | -2  | 14  | 1 | 4   | 7    | -4  | 19 | 1 | -9   | 2    | -9  | -15 | 2 | 30   | 2    | 7   | -13 | 2 | 70    | 56    |
| 10  | 11  | 1 | 23  | 29   | -1  | 14  | 1 | 46  | 35   | -3  | 19 | 1 | -4   | 1    | -8  | -15 | 2 | 9    | 0    | 8   | -13 | 2 | 53    | 51    |
| 11  | 11  | 1 | 14  | 6    | 0   | 14  | 1 | 220 | 198  | -2  | 19 | 1 | -5   | 5    | -7  | -15 | 2 | -6   | 2    | 9   | -13 | 2 | -3    | 0     |
| -15 | 12  | 1 | 37  | 35   | 1   | 14  | 1 | 128 | 130  | -1  | 19 | 1 | 2    | 0    | -6  | -15 | 2 | 34   | 0    | 10  | -13 | 2 | 15    | 22    |
| -14 | 12  | 1 | 39  | 16   | 2   | 14  | 1 | 15  | 1    | 0   | 19 | 1 | 14   | 3    | -5  | -15 | 2 | 38   | 19   | 11  | -13 | 2 | 31    | 29    |
| -12 | -13 | 2 | 6   | 1    | -10 | -10 | 2 | 57  | 62   | -8  | -8 | 2 | 272  | 226  | -10 | -6  | 2 | 99   | 83   | -13 | -4  | 2 | 8     | 2     |
| -13 | -13 | 2 | -9  | 9    | -9  | -10 | 2 | 8   | 16   | -7  | -8 | 2 | 12   | 1    | -9  | -6  | 2 | 105  | 66   | -12 | -4  | 2 | 638   | 500   |
| -14 | -13 | 2 | 7   | 9    | -8  | -10 | 2 | 68  | 60   | -6  | -8 | 2 | 128  | 87   | -8  | -6  | 2 | 212  | 263  | -11 | -4  | 2 | 27    | 42    |
| -15 | -13 | 2 | 6   | 1    | -7  | -10 | 2 | 78  | 76   | -5  | -8 | 2 | 180  | 145  | -7  | -6  | 2 | 0    | 7    | -10 | -4  | 2 | 217   | 174   |
| -12 | -12 | 2 | 42  | 2    | -6  | -10 | 2 | 157 | 148  | -4  | -8 | 2 | 141  | 167  | -6  | -6  | 2 | 1744 | 1621 | -9  | -4  | 2 | 317   | 281   |
| -11 | -12 | 2 | -1  | 11   | -5  | -10 | 2 | 88  | 74   | -3  | -8 | 2 | 1327 | 1165 | -5  | -6  | 2 | 279  | 315  | -8  | -4  | 2 | 142   | 181   |
| -10 | -12 | 2 | 13  | 0    | -4  | -10 | 2 | 418 | 387  | -2  | -8 | 2 | 34   | 18   | -4  | -6  | 2 | 10   | 23   | -7  | -4  | 2 | 177   | 148   |
| -9  | -12 | 2 | 6   | 3    | -3  | -10 | 2 | 614 | 562  | -1  | -8 | 2 | 265  | 187  | -3  | -6  | 2 | 702  | 801  | -6  | -4  | 2 | 2873  | 2707  |
| -8  | -12 | 2 | 50  | 45   | -2  | -10 | 2 | 139 | 163  | 0   | -8 | 2 | 261  | 1084 | -2  | -6  | 2 | 994  | 893  | -5  | -4  | 2 | 3201  | 2675  |
| -7  | -12 | 2 | 6   | 15   | -1  | -10 | 2 | 2   | 2    | 1   | -8 | 2 | 251  | 185  | -1  | -6  | 2 | 29   | 11   | -4  | -4  | 2 | 2812  | 2626  |
| -6  | -12 | 2 | 8   | 2    | 0   | -10 | 2 | 649 | 693  | 2   | -8 | 2 | 2    | 2    | 0   | -6  | 2 | 1736 | 1535 | -3  | -4  | 2 | 175   | 141   |
| -5  | -12 | 2 | 101 | 98   | 1   | -10 | 2 | 3   | 2    | 3   | -8 | 2 | 46   | 41   | 1   | -6  | 2 | 1230 | 1342 | -2  | -4  | 2 | 3813  | 3962  |
| -4  | -12 | 2 | 60  | 61   | 2   | -10 | 2 | 16  | 24   | 4   | -8 | 2 | 43   | 72   | 2   | -6  | 2 | 636  | 654  | -1  | -4  | 2 | 18744 | 15984 |
| -3  | -12 | 2 | 27  | 25   | 3   | -10 | 2 | 771 | 672  | 5   | -8 | 2 | 10   | 5    | 3   | -6  | 2 | -1   | 4    | 0   | -4  | 2 | 23390 | 18306 |
| -2  | -12 | 2 | 118 | 143  | 4   | -10 | 2 | 54  | 65   | 6   | -8 | 2 | 827  | 837  | 4   | -6  | 2 | 67   | 81   | 1   | -4  | 2 | 7280  | 6821  |
| -1  | -12 | 2 | 131 | 146  | 5   | -10 | 2 | 2   | 7    | 7   | -8 | 2 | 53   | 76   | 5   | -6  | 2 | 48   | 74   | 2   | -4  | 2 | 5177  | 5184  |
| 0   | -12 | 2 | 365 | 529  | 6   | -10 | 2 | 741 | 584  | 8   | -8 | 2 | 149  | 136  | 6   | -6  | 2 | 1334 | 1220 | 3   | -4  | 2 | 292   | 318   |
| 1   | -12 | 2 | 38  | 35   | 7   | -10 | 2 | 67  | 86   | 9   | -8 | 2 | 67   | 56   | 7   | -6  | 2 | 62   | 40   | 4   | -4  | 2 | 3064  | 3210  |
| 2   | -12 | 2 | -2  | 6    | 8   | -10 | 2 | 35  | 38   | 10  | -8 | 2 | 237  | 255  | 8   | -6  | 2 | 465  | 410  | 5   | -4  | 2 | 5803  | 5785  |
| 3   | -12 | 2 | 66  | 65   | 9   | -10 | 2 | 147 | 92   | 11  | -8 | 2 | 285  | 229  | 9   | -6  | 2 | 212  | 225  | 6   | -4  | 2 | 1346  | 1280  |
| 4   | -12 | 2 | 69  | 52   | 10  | -10 | 2 | 191 | 187  | 12  | -8 | 2 | 28   | 26   | 10  | -6  | 2 | 36   | 49   | 7   | -4  | 2 | 374   | 441   |
| 5   | -12 | 2 | 27  | 26   | 11  | -10 | 2 | 346 | 266  | 13  | -8 | 2 | -3   | 11   | 11  | -6  | 2 | 170  | 133  | 8   | -4  | 2 | 364   | 334   |
| 6   | -12 | 2 | 109 | 107  | 12  | -10 | 2 | 98  | 133  | 14  | -8 | 2 | 24   | 40   | 12  | -6  | 2 | 32   | 47   | 9   | -4  | 2 | 2241  | 2028  |
| 7   | -12 | 2 | 6   | 2    | 13  | -10 | 2 | 18  | 24   | 15  | -8 | 2 | 2    | 2    | 13  | -6  | 2 | 2    | 10   | 10  | -4  | 2 | 14    | 2     |
| 8   | -12 | 2 | 0   | 14   | 14  | -10 | 2 | 0   | 9    | 16  | -8 | 2 | -3   | 1    | 14  | -6  | 2 | 7    | 4    | 11  | -4  | 2 | 118   | 95    |
| 9   | -12 | 2 | 139 | 117  | 15  | -10 | 2 | 20  | 10   | 17  | -8 | 2 | -8   | 19   | 15  | -6  | 2 | 20   | 7    | 12  | -4  | 2 | 139   | 146   |
| 10  | -12 | 2 | 60  | 47   | 16  | -10 | 2 | 7   | 11   | 18  | -8 | 2 | -6   | 2    | 16  | -6  | 2 | 21   | 59   | 13  | -4  | 2 | 95    | 87    |
| 11  | -12 | 2 | 2   | 0    | 17  | -10 | 2 | 56  | 15   | -15 | -7 | 2 | 5    | 25   | 17  | -6  | 2 | 128  | 0    | 14  | -4  | 2 | 7     | 6     |
| 12  | -12 | 2 | 6   | 17   | -14 | -9  | 2 | -9  | 0    | -14 | -7 | 2 | 12   | 5    | 18  | -6  | 2 | 18   | 6    | 15  | -4  | 2 | 34    | 44    |
| 13  | -12 | 2 | 10  | 11   | -13 | -9  | 2 | 10  | 27   | -13 | -7 | 2 | -5   | 0    | -15 | -5  | 2 | -7   | 16   | 16  | -4  | 2 | 40    | 37    |
| 14  | -12 | 2 | 11  | 1    | -12 | -9  | 2 | 41  | 45   | -12 | -7 | 2 | 88   | 114  | -14 | -5  | 2 | 92   | 63   | 17  | -4  | 2 | 22    | 2     |
| 15  | -12 | 2 | 45  | 2    | -11 | -9  | 2 | 19  | 16   | -11 | -7 | 2 | 251  | 271  | -13 | -5  | 2 | 71   | 63   | 18  | -4  | 2 | 17    | 5     |
| 16  | -12 | 2 | -4  | 6    | -10 | -9  | 2 | 0   | 3    | -10 | -7 | 2 | 223  | 221  | -12 | -5  | 2 | 18   | 15   | -16 | -3  | 2 | 46    | 46    |
| -13 | -11 | 2 | 72  | 1    | -9  | -9  | 2 | 43  | 53   | -9  | -7 | 2 | 282  | 289  | -11 | -5  | 2 | 219  | 231  | -15 | -3  | 2 | -6    | 0     |
| -12 | -11 | 2 | 33  | 33   | -8  | -9  | 2 | 85  | 81   | -8  | -7 | 2 | 661  | 533  | -10 | -5  | 2 | 196  | 176  | -14 | -3  | 2 | 105   | 71    |
| -11 | -11 | 2 | -9  | 0    | -7  | -9  | 2 | 30  | 21   | -7  | -7 | 2 | 140  | 223  | -9  | -5  | 2 | 1    | 1    | -13 | -3  | 2 | -4    | 1     |
| -10 | -11 | 2 | 26  | 21   | -6  | -9  | 2 | 305 | 304  | -6  | -7 | 2 | 8    | 12   | -8  | -5  | 2 | 1593 | 1315 | -12 | -3  | 2 | -2    | 1     |
| -9  | -11 | 2 | 92  | 113  | -5  | -9  | 2 | 652 | 621  | -5  | -7 | 2 | 864  | 747  | -7  | -5  | 2 | 443  | 533  | -11 | -3  | 2 | 13    | 33    |
| -8  | -11 | 2 | 1   | 0    | -4  | -9  | 2 | 127 | 120  | -4  | -7 | 2 | 207  | 224  | -6  | -5  | 2 | 12   | 10   | -10 | -3  | 2 | 15    | 3     |
| -7  | -11 | 2 | 8   | 19   | -3  | -9  | 2 | 394 | 406  | -3  | -7 | 2 | 81   | 99   | -5  | -5  | 2 | 1287 | 1310 | -9  | -3  | 2 | 756   | 664   |
| -6  | -11 | 2 | 114 | 139  | -2  | -9  | 2 | 483 | 498  | -2  | -7 | 2 | 1542 | 1613 | -4  | -5  | 2 | 3986 | 3861 | -8  | -3  | 2 | 116   | 109   |
| -5  | -11 | 2 | 24  | 30   | -1  | -9  | 2 | 161 | 178  | -1  | -7 | 2 | 418  | 451  | -3  | -5  | 2 | 2141 | 2488 | -7  | -3  | 2 | 2473  | 2474  |
| -4  | -11 | 2 | 117 | 94   | 0   | -9  | 2 | 186 | 130  | 0   | -7 | 2 | 225  | 334  | -2  | -5  | 2 | 19   | 23   | -6  | -3  | 2 | 1544  | 1737  |
| -3  | -11 | 2 | 260 | 239  | 1   | -9  | 2 | 248 | 260  | 1   | -7 | 2 | 22   | 41   | -1  | -5  | 2 | 1968 | 2248 | -5  | -3  | 2 | 2409  | 1910  |
| -2  | -11 | 2 | 335 | 344  | 2   | -9  | 2 | 286 | 303  | 2   | -7 | 2 | 1314 | 1163 | 0   | -5  | 2 | 3391 | 3642 | -4  | -3  | 2 | 125   | 93    |
| -1  | -11 | 2 | 311 | 320  | 3   | -9  | 2 | 60  | 58   | 3   | -7 | 2 | 272  | 371  | 1   | -5  | 2 | 720  | 654  | -3  | -3  | 2 | 59    | 68    |
| 0   | -11 | 2 | 67  | 67   | 4   | -9  | 2 | 395 | 435  | 4   | -7 | 2 | 217  | 285  | 2   | -5  | 2 | 146  | 143  | -2  | -3  | 2 | 178   | 156   |
| 1   | -11 | 2 | 42  | 59   | 5   | -9  | 2 | 734 | 635  | 5   | -7 | 2 | 547  | 535  | 3   | -5  | 2 | 986  | 1121 | -1  | -3  | 2 | 11181 | 10155 |
| 2   | -11 | 2 | -2  | 5    | 6   | -9  | 2 | 98  | 110  | 6   | -7 | 2 | 5    | 4    | 4   | -5  | 2 | 1263 | 1235 | 1   | -3  | 2 | 6429  | 6437  |
| 3   | -11 | 2 | 118 | 95   | 7   | -9  | 2 | 102 | 93   | 7   | -7 | 2 | 2    | 7    | 5   | -5  | 2 | 57   | 94   | 2   | -3  | 2 | 136   | 147   |
| 4   | -11 | 2 | 161 | 192  | 8   | -9  | 2 | 247 | 221  | 8   | -7 | 2 | 75   | 47   | 6   | -5  | 2 | 1244 | 1646 | 3   | -3  | 2 | 6887  | 5310  |
| 5   | -11 | 2 | 235 | 195  | 9   | -9  | 2 | 214 | 193  | 9   | -7 | 2 | 437  | 465  | 7   | -5  | 2 | 535  | 475  | 4   | -3  | 2 | 111   |       |

Table A.3, continued

| M  | K  | L | Obs   | Calc  | M   | K  | L | Obs   | Calc  | M   | K  | L | Obs  | Calc | M   | K  | L | Obs  | Calc | M   | K   | L | Obs  | Calc |
|----|----|---|-------|-------|-----|----|---|-------|-------|-----|----|---|------|------|-----|----|---|------|------|-----|-----|---|------|------|
| 6  | -2 | 2 | 5325  | 5407  | 14  | 0  | 2 | 69    | 55    | -16 | 3  | 2 | -9   | 2    | -16 | 5  | 2 | 11   | 4    | -15 | 7   | 2 | -4   | 2    |
| 7  | -2 | 2 | 215   | 102   | 15  | 0  | 2 | -1    | 3     | -15 | 3  | 2 | -7   | 12   | -15 | 5  | 2 | -1   | 14   | -14 | 7   | 2 | 41   | 24   |
| 8  | -2 | 2 | 988   | 827   | 16  | 0  | 2 | -13   | 5     | -14 | 3  | 2 | 21   | 26   | -14 | 5  | 2 | 1    | 12   | -13 | 7   | 2 | 28   | 20   |
| 9  | -2 | 2 | 302   | 292   | -16 | 1  | 2 | 297   | 326   | -13 | 3  | 2 | 23   | 12   | -13 | 5  | 2 | 7    | 11   | -12 | 7   | 2 | 63   | 59   |
| 10 | -2 | 2 | 594   | 565   | -15 | 1  | 2 | 80    | 99    | -12 | 3  | 2 | 661  | 712  | -12 | 5  | 2 | 28   | 14   | -11 | 7   | 2 | 26   | 17   |
| 11 | -2 | 2 | 132   | 130   | -14 | 1  | 2 | 44    | 31    | -11 | 3  | 2 | 446  | 428  | -11 | 5  | 2 | 167  | 138  | -10 | 7   | 2 | 52   | 30   |
| 12 | -2 | 2 | 215   | 197   | -13 | 1  | 2 | 13    | 24    | -10 | 3  | 2 | 347  | 286  | -10 | 5  | 2 | 200  | 221  | -9  | 7   | 2 | 108  | 70   |
| 13 | -2 | 2 | 81    | 132   | -12 | 1  | 2 | 203   | 260   | -9  | 3  | 2 | 116  | 129  | -9  | 5  | 2 | 64   | 76   | -8  | 7   | 2 | 70   | 42   |
| 14 | -2 | 2 | 41    | 38    | -11 | 1  | 2 | 68    | 90    | -8  | 3  | 2 | 610  | 568  | -8  | 5  | 2 | 523  | 559  | -7  | 7   | 2 | 95   | 105  |
| 15 | -2 | 2 | -1    | 9     | -10 | 1  | 2 | 260   | 250   | -7  | 3  | 2 | 30   | 39   | -7  | 5  | 2 | 695  | 664  | -6  | 7   | 2 | 640  | 690  |
| 16 | -2 | 2 | 46    | 23    | -9  | 1  | 2 | 891   | 878   | -6  | 3  | 2 | 4979 | 4395 | -6  | 5  | 2 | 364  | 394  | -5  | 7   | 2 | 69   | 46   |
| 17 | -2 | 2 | 65    | 81    | -8  | 1  | 2 | 1065  | 1102  | -5  | 3  | 2 | 233  | 252  | -5  | 5  | 2 | 15   | 24   | -4  | 7   | 2 | 294  | 241  |
| 18 | -2 | 2 | -6    | 8     | -7  | 1  | 2 | 16    | 4     | -4  | 3  | 2 | 4157 | 4135 | -4  | 5  | 2 | 1678 | 1695 | -3  | 7   | 2 | 3409 | 3466 |
| 19 | -2 | 2 | 10    | 7     | -6  | 1  | 2 | 543   | 750   | -3  | 3  | 2 | 5711 | 5825 | -3  | 5  | 2 | 1208 | 1223 | -2  | 7   | 2 | 1165 | 980  |
| 20 | -2 | 2 | 203   | 201   | -5  | 1  | 2 | 83    | 86    | -2  | 3  | 2 | 255  | 237  | -2  | 5  | 2 | 246  | 287  | -1  | 7   | 2 | 467  | 540  |
| 21 | -2 | 2 | 335   | 348   | -4  | 1  | 2 | 8411  | 7267  | -1  | 3  | 2 | 4169 | 3801 | -1  | 5  | 2 | 32   | 30   | 0   | 7   | 2 | 2726 | 2761 |
| 22 | -2 | 2 | 9     | 6     | -3  | 1  | 2 | 32801 | 24412 | 0   | 3  | 2 | 1983 | 2305 | 0   | 5  | 2 | 2465 | 2388 | 1   | 7   | 2 | 54   | 31   |
| 23 | -2 | 2 | 119   | 160   | -2  | 1  | 2 | 21340 | 36919 | 1   | 3  | 2 | 6    | 1    | 1   | 5  | 2 | 1197 | 1152 | 2   | 7   | 2 | 209  | 231  |
| 24 | -2 | 2 | 666   | 518   | 1   | 1  | 2 | 107   | 217   | 2   | 3  | 2 | 437  | 689  | 2   | 5  | 2 | 1411 | 1552 | 3   | 7   | 2 | 493  | 645  |
| 25 | -2 | 2 | 56    | 65    | 2   | 1  | 2 | 2319  | 2091  | 3   | 3  | 2 | 2    | 9    | 3   | 5  | 2 | 560  | 857  | 4   | 7   | 2 | 34   | 42   |
| 26 | -2 | 2 | 834   | 667   | 3   | 1  | 2 | 130   | 88    | 4   | 3  | 2 | 345  | 347  | 4   | 5  | 2 | 0    | 2    | 5   | 7   | 2 | 87   | 123  |
| 27 | -2 | 2 | 583   | 740   | 4   | 1  | 2 | 88    | 57    | 5   | 3  | 2 | 1861 | 1736 | 5   | 5  | 2 | 99   | 70   | 6   | 7   | 2 | 123  | 108  |
| 28 | -2 | 2 | 13    | 24    | 5   | 1  | 2 | 5786  | 5455  | 6   | 3  | 2 | 1530 | 1743 | 6   | 5  | 2 | 667  | 687  | 7   | 7   | 2 | -2   | 2    |
| 29 | -2 | 2 | 1518  | 1586  | 6   | 1  | 2 | 3     | 9     | 7   | 3  | 2 | 12   | 3    | 7   | 5  | 2 | 103  | 147  | 8   | 7   | 2 | 334  | 275  |
| 30 | -2 | 2 | 27198 | 21213 | 7   | 1  | 2 | 1053  | 998   | 8   | 3  | 2 | 74   | 90   | 8   | 5  | 2 | 124  | 96   | 9   | 7   | 2 | 15   | 11   |
| 31 | -2 | 2 | 1968  | 2142  | 8   | 1  | 2 | 1086  | 1075  | 9   | 3  | 2 | 3291 | 2837 | 9   | 5  | 2 | 347  | 288  | 10  | 7   | 2 | 35   | 36   |
| 32 | -2 | 2 | 85    | 62    | 9   | 1  | 2 | 841   | 821   | 10  | 3  | 2 | 2486 | 2303 | 10  | 5  | 2 | 136  | 150  | 11  | 7   | 2 | 115  | 109  |
| 33 | -2 | 2 | 1923  | 1938  | 10  | 1  | 2 | 160   | 184   | 11  | 3  | 2 | 536  | 509  | 11  | 5  | 2 | 150  | 153  | 12  | 7   | 2 | 5    | 3    |
| 34 | -2 | 2 | 2121  | 2280  | 11  | 1  | 2 | 3     | 1     | 12  | 3  | 2 | 4    | 15   | 12  | 5  | 2 | 17   | 5    | 13  | 7   | 2 | 35   | 2    |
| 35 | -2 | 2 | 53    | 38    | 12  | 1  | 2 | 96    | 86    | 13  | 3  | 2 | 154  | 160  | 13  | 5  | 2 | 81   | 62   | -17 | 8   | 2 | 9    | 4    |
| 36 | -2 | 2 | 346   | 357   | 13  | 1  | 2 | 26    | 19    | 14  | 3  | 2 | 17   | 17   | 14  | 5  | 2 | 3    | 1    | -15 | 8   | 2 | 28   | 32   |
| 37 | -2 | 2 | 497   | 463   | 14  | 1  | 2 | 4     | 5     | 15  | 3  | 2 | 26   | 18   | 15  | 5  | 2 | 25   | 2    | -14 | 8   | 2 | 0    | 10   |
| 38 | -2 | 2 | 70    | 70    | 15  | 1  | 2 | 25    | 24    | -16 | 4  | 2 | 33   | 6    | -18 | 6  | 2 | -16  | 0    | -13 | 8   | 2 | 23   | 2    |
| 39 | -2 | 2 | 123   | 104   | 16  | 1  | 2 | 9     | 16    | -15 | 4  | 2 | 13   | 11   | -17 | 6  | 2 | 3    | 7    | -12 | 8   | 2 | 125  | 140  |
| 40 | -2 | 2 | 13    | 42    | -16 | 2  | 2 | 14    | 0     | -14 | 4  | 2 | 51   | 19   | -16 | 6  | 2 | -5   | 25   | -11 | 8   | 2 | 263  | 235  |
| 41 | -2 | 2 | 102   | 99    | -15 | 2  | 2 | -9    | 2     | -13 | 4  | 2 | 70   | 58   | -15 | 6  | 2 | 62   | 51   | -10 | 8   | 2 | 5    | 2    |
| 42 | -2 | 2 | -4    | 2     | -14 | 2  | 2 | 77    | 77    | -12 | 4  | 2 | 93   | 99   | -14 | 6  | 2 | 4    | 1    | -9  | 8   | 2 | 56   | 47   |
| 43 | -2 | 2 | 134   | 109   | -13 | 2  | 2 | 50    | 44    | -11 | 4  | 2 | 4    | 3    | -13 | 6  | 2 | 2    | 7    | -8  | 8   | 2 | 224  | 211  |
| 44 | -2 | 2 | -1    | 23    | -12 | 2  | 2 | 5     | 6     | -10 | 2  | 2 | -4   | 9    | -12 | 6  | 2 | 51   | 49   | -7  | 8   | 2 | 243  | 181  |
| 45 | -2 | 2 | 16    | 0     | -11 | 2  | 2 | 266   | 228   | -9  | 4  | 2 | 492  | 405  | -11 | 6  | 2 | 80   | 91   | -6  | 8   | 2 | 69   | 88   |
| 46 | -2 | 2 | 76    | 80    | -10 | 2  | 2 | 195   | 159   | -8  | 4  | 2 | 44   | 87   | -10 | 6  | 2 | 60   | 68   | -5  | 8   | 2 | 390  | 413  |
| 47 | -2 | 2 | 231   | 274   | -9  | 2  | 2 | 149   | 72    | -7  | 4  | 2 | 285  | 327  | -9  | 6  | 2 | 594  | 534  | -4  | 8   | 2 | 475  | 387  |
| 48 | -2 | 2 | 448   | 426   | -8  | 2  | 2 | 1171  | 991   | -6  | 4  | 2 | 450  | 504  | -8  | 6  | 2 | 264  | 249  | -3  | 8   | 2 | 11   | 19   |
| 49 | -2 | 2 | 194   | 180   | -7  | 2  | 2 | 316   | 457   | -5  | 4  | 2 | 870  | 853  | -7  | 6  | 2 | 98   | 116  | -2  | 8   | 2 | 1890 | 1640 |
| 50 | -2 | 2 | 25    | 31    | -6  | 2  | 2 | 399   | 557   | -4  | 4  | 2 | 1381 | 1354 | -6  | 6  | 2 | 373  | 348  | -1  | 8   | 2 | 253  | 277  |
| 51 | -2 | 2 | 489   | 444   | -5  | 2  | 2 | 372   | 343   | -3  | 4  | 2 | 2062 | 2078 | -5  | 6  | 2 | 493  | 486  | 0   | 8   | 2 | 480  | 482  |
| 52 | -2 | 2 | 232   | 222   | -4  | 2  | 2 | 19309 | 16403 | -2  | 4  | 2 | 340  | 426  | -4  | 6  | 2 | 355  | 381  | 1   | 8   | 2 | 97   | 6    |
| 53 | -2 | 2 | 32    | 37    | 10  | 10 | 2 | 21    | 26    | -4  | 13 | 2 | 25   | 38   | 0   | 16 | 2 | 4    | 0    | -2  | 16  | 3 | -5   | 8    |
| 54 | -2 | 2 | 587   | 649   | 11  | 10 | 2 | 5     | 12    | -3  | 13 | 2 | 59   | 45   | -1  | 16 | 2 | 4    | 0    | -1  | 16  | 3 | -2   | 17   |
| 55 | -2 | 2 | 9     | 29    | 12  | 10 | 2 | 21    | 16    | -2  | 13 | 2 | -3   | 0    | 2   | 16 | 2 | 2    | 0    | 0   | -16 | 3 | -4   | 1    |
| 56 | -2 | 2 | 361   | 315   | -15 | 11 | 2 | 65    | 31    | -1  | 13 | 2 | 13   | 25   | 3   | 16 | 2 | 19   | 5    | -1  | 16  | 3 | 4    | 0    |
| 57 | -2 | 2 | 242   | 241   | -14 | 11 | 2 | 0     | 4     | 0   | 13 | 2 | 36   | 39   | 4   | 16 | 2 | -6   | 0    | 2   | -16 | 3 | 27   | 18   |
| 58 | -2 | 2 | 11    | 3     | -13 | 11 | 2 | 7     | 2     | 1   | 13 | 2 | 0    | 0    | 5   | 16 | 2 | 30   | 10   | 3   | -16 | 3 | 7    | 12   |
| 59 | -2 | 2 | 22    | 39    | -12 | 11 | 2 | 63    | 48    | 2   | 13 | 2 | 132  | 88   | 6   | 16 | 2 | 11   | 1    | 4   | -16 | 3 | 0    | 3    |
| 60 | -2 | 2 | 258   | 189   | -11 | 11 | 2 | 18    | 16    | 3   | 13 | 2 | 126  | 129  | -8  | 17 | 2 | -18  | 2    | 5   | -16 | 3 | 12   | 8    |
| 61 | -2 | 2 | 58    | 70    | -10 | 11 | 2 | 5     | 0     | 4   | 13 | 2 | 54   | 65   | -7  | 17 | 2 | -3   | 5    | 6   | -16 | 3 | 6    | 6    |
| 62 | -2 | 2 | 7     | 6     | -9  | 11 | 2 | 6     | 2     | 5   | 13 | 2 | 1    | 0    | -6  | 17 | 2 | 0    | 2    | 7   | -16 | 3 | 26   | 2    |
| 63 | -2 | 2 | 109   | 107   | -8  | 11 | 2 | 34    | 6     | 6   | 13 | 2 | 45   | 53   | -5  | 17 | 2 | 4    | 1    | 8   | -16 | 3 | 19   | 1    |
| 64 | -2 | 2 | 82    | 64    | -7  | 11 | 2 | 7     | 3     | 7   | 13 | 2 | 43   | 27   | -4  | 17 | 2 | 1    | 4    | 9   | -16 | 3 | -7   | 2    |
| 65 | -2 | 2 | 24    | 19    | -6  | 11 | 2 | 145   | 143   | 8   | 13 | 2 | 8    | 1    | -3  | 17 | 2 | 10   | 15   | 10  | -16 | 3 | 0    | 2    |
| 66 | -2 | 2 | 6     | 14    | -5  | 11 | 2 | 163   | 112   | 9   | 13 | 2 | -8   | 37   | -2  | 17 | 2 | 13   | 5    | -1  | -16 | 3 | -10  | 0    |
| 67 | -2 | 2 | 5     | 0     | -4  | 11 | 2 | 166   | 162   | -13 | 14 | 2 | 4    | 7    | -1  | 17 | 2 | -6   | 1    | 12  | -16 | 3 | 31   | 2    |
| 68 | -2 | 2 | 9     | 6     | -3  | 11 | 2 | 56    | 70    | -12 | 14 | 2 | 48   | 9    | 0   | 17 | 2 | 40   | 5    | -9  | -15 | 3 | 3    | 8    |
| 69 | -2 | 2 | 189   | 183   | -2  | 11 | 2 | 9     | 6     | -11 | 14 | 2 | 26   | 1    | 1   | 17 | 2 | -1   | 1    | -8  | -15 | 3 | 7    | 10   |
| 70 | -2 | 2 | 10    | 0     | -1  | 11 | 2 | 160   | 122   | -10 | 14 | 2 | -10  | 1    | 2   | 17 | 2 | 0    | 1    | -7  | -15 | 3 | 5    | 6    |
| 71 | -2 | 2 | -3    | 0     | 0   | 11 | 2 | 20    | 12    | -9  | 14 | 2 | 42   | 25   | 3   | 17 | 2 | -6   | 0    | -6  | -15 | 3 | 18   | 25   |
| 72 | -2 | 2 | 61    | 48    | 1   | 11 | 2 | 106   | 177   | -8  | 14 | 2 | 57   | 94   | 4   | 17 | 2 | 38   | 0    | -5  | -15 | 3 | 42   | 18   |
| 73 | -2 | 2 | 59    | 51    | 2   | 11 | 2 | 167   | 153   | -7  | 14 | 2 | 33   | 2    | -4  | 18 | 2 | 35   | 5    | -4  | -15 | 3 | -3   | 4    |
| 74 | -2 | 2 | 461   | 419   | 3   | 11 | 2 | 20    | 13    | -6  | 14 | 2 | 0    | 4    | -3  | 18 | 2 | 0    | 2    | -3  | -15 | 3 | 28   | 24   |
| 75 | -2 | 2 | 1322  | 1186  | 4   | 11 | 2 | 179   | 261   | -5  | 14 | 2 | -2   | 14   | -2  | 18 | 2 | 10   | 0    | -2  | -15 | 3 | 29   | 32   |
| 76 | -2 | 2 | 141   | 136   | 5   | 11 | 2 | 340   | 371   | -4  | 14 | 2 | 52   | 24   | -1  | 18 | 2 | 33   | 13   | -1  | -15 | 3 | -    |      |



Table A.3, continued

| M   | K   | L | Obs | Calc | M   | K   | L | Obs | Calc | M   | K  | L | Obs  | Calc | M   | K   | L | Obs  | Calc | M   | K   | L | Obs   | Calc  |
|-----|-----|---|-----|------|-----|-----|---|-----|------|-----|----|---|------|------|-----|-----|---|------|------|-----|-----|---|-------|-------|
| 1   | 10  | 2 | 2   | 3    | -13 | 13  | 2 | -13 | 0    | -9  | 16 | 2 | -3   | 7    | 8   | -17 | 3 | 5    | 21   | 8   | -14 | 3 | 11    | 4     |
| 2   | 10  | 2 | 26  | 25   | -12 | 13  | 2 | 4   | 14   | -8  | 16 | 2 | 23   | 7    | 9   | -17 | 3 | 4    | 10   | 9   | -14 | 3 | 0     | 0     |
| 3   | 10  | 2 | 66  | 63   | -11 | 13  | 2 | 23  | 34   | -7  | 16 | 2 | 13   | 14   | 10  | -17 | 3 | -13  | 2    | 10  | -14 | 3 | 7     | 14    |
| 4   | 10  | 2 | 15  | 12   | -10 | 13  | 2 | 21  | 28   | -6  | 16 | 2 | 5    | 15   | -8  | -16 | 3 | -9   | 2    | 11  | -14 | 3 | 13    | 2     |
| 5   | 10  | 2 | 45  | 43   | -9  | 13  | 2 | 28  | 22   | -5  | 16 | 2 | 2    | 10   | -7  | -16 | 3 | 18   | 2    | 12  | -14 | 3 | 1     | 3     |
| 6   | 10  | 2 | 177 | 233  | -8  | 13  | 2 | -2  | 2    | -4  | 16 | 2 | 8    | 5    | -6  | -16 | 3 | 25   | 5    | 13  | -14 | 3 | 18    | 7     |
| 7   | 10  | 2 | 27  | 41   | -7  | 13  | 2 | 94  | 105  | -3  | 16 | 2 | 0    | 3    | -5  | -16 | 3 | 21   | 18   | 14  | -14 | 3 | -10   | 2     |
| 8   | 10  | 2 | 63  | 53   | -6  | 13  | 2 | -2  | 2    | -2  | 16 | 2 | 3    | 12   | -4  | -16 | 3 | 36   | 19   | -12 | -13 | 3 | -5    | 0     |
| 9   | 10  | 2 | 94  | 24   | -5  | 13  | 2 | -4  | 4    | -1  | 16 | 2 | 18   | 17   | -3  | -16 | 3 | 20   | 2    | -11 | -13 | 3 | -10   | 0     |
| -10 | -13 | 3 | 2   | 10   | -2  | -11 | 3 | 281 | 243  | 0   | -9 | 3 | 265  | 202  | 0   | -7  | 3 | 19   | 28   | -2  | -5  | 3 | 431   | 758   |
| -9  | -13 | 3 | 20  | 19   | -1  | -11 | 3 | 14  | 13   | 1   | -9 | 3 | 440  | 379  | 1   | -7  | 3 | 1769 | 1969 | -1  | -5  | 3 | 758   | 613   |
| -8  | -13 | 3 | 10  | 8    | 0   | -11 | 3 | 261 | 264  | 2   | -9 | 3 | 480  | 488  | 2   | -7  | 3 | 454  | 365  | 0   | -5  | 3 | 1112  | 959   |
| -7  | -13 | 3 | 28  | 7    | 1   | -11 | 3 | 133 | 143  | 3   | -9 | 3 | 194  | 208  | 3   | -7  | 3 | 130  | 103  | 1   | -5  | 3 | 2089  | 2274  |
| -6  | -13 | 3 | 32  | 23   | 2   | -11 | 3 | 258 | 234  | 4   | -9 | 3 | 1209 | 999  | 4   | -7  | 3 | 2    | 6    | 2   | -5  | 3 | 294   | 269   |
| -5  | -13 | 3 | 32  | 38   | 3   | -11 | 3 | 34  | 30   | 5   | -9 | 3 | 194  | 161  | 5   | -7  | 3 | -1   | 1    | 3   | -5  | 3 | 22    | 35    |
| -4  | -13 | 3 | 51  | 49   | 4   | -11 | 3 | 2   | 4    | 6   | -9 | 3 | 0    | 1    | 6   | -7  | 3 | 6    | 0    | 4   | -5  | 3 | 86    | 78    |
| -3  | -13 | 3 | -3  | 1    | 5   | -11 | 3 | 414 | 336  | 7   | -9 | 3 | 146  | 131  | 7   | -7  | 3 | -2   | 4    | 5   | -5  | 3 | 333   | 245   |
| -2  | -13 | 3 | 57  | 36   | 6   | -11 | 3 | 14  | 9    | 8   | -9 | 3 | 2    | 9    | 8   | -7  | 3 | 7    | 1    | 6   | -5  | 3 | 1266  | 1372  |
| -1  | -13 | 3 | 52  | 66   | 7   | -11 | 3 | 17  | 15   | 9   | -9 | 3 | 190  | 185  | 9   | -7  | 3 | -1   | 2    | 7   | -5  | 3 | 134   | 124   |
| 0   | -13 | 3 | 0   | 1    | 8   | -11 | 3 | 21  | 26   | 10  | -9 | 3 | 28   | 200  | 10  | -7  | 3 | 314  | 266  | 8   | -5  | 3 | 371   | 385   |
| 1   | -13 | 3 | 2   | 2    | 9   | -11 | 3 | 29  | 34   | 11  | -9 | 3 | 27   | 40   | 11  | -7  | 3 | 50   | 48   | 9   | -5  | 3 | 319   | 248   |
| 2   | -13 | 3 | 11  | 20   | 10  | -11 | 3 | 162 | 142  | 12  | -9 | 3 | 5    | 14   | 12  | -7  | 3 | 21   | 14   | 10  | -5  | 3 | 307   | 288   |
| 3   | -13 | 3 | 18  | 10   | 11  | -11 | 3 | 39  | 67   | 13  | -9 | 3 | 111  | 100  | 13  | -7  | 3 | 25   | 35   | 11  | -5  | 3 | 9     | 1     |
| 4   | -13 | 3 | 118 | 97   | 12  | -11 | 3 | 34  | 28   | 14  | -9 | 3 | 29   | 48   | 14  | -7  | 3 | 14   | 20   | 12  | -5  | 3 | 100   | 81    |
| 5   | -13 | 3 | 149 | 145  | 13  | -11 | 3 | 3   | 4    | 15  | -9 | 3 | 12   | 1    | 15  | -7  | 3 | 24   | 11   | 13  | -5  | 3 | 69    | 76    |
| 6   | -13 | 3 | 38  | 28   | 14  | -11 | 3 | 24  | 5    | 16  | -9 | 3 | 7    | 1    | 16  | -7  | 3 | -7   | 6    | 14  | -5  | 3 | 21    | 14    |
| 7   | -13 | 3 | 20  | 8    | 15  | -11 | 3 | 39  | 10   | 17  | -9 | 3 | -10  | 18   | 17  | -7  | 3 | 56   | 21   | 15  | -5  | 3 | 29    | 8     |
| 8   | -13 | 3 | 50  | 56   | 16  | -11 | 3 | -4  | 2    | -15 | -8 | 3 | 31   | 8    | -15 | -6  | 3 | 38   | 16   | 16  | -5  | 3 | 18    | 0     |
| 9   | -13 | 3 | 47  | 33   | 17  | -11 | 3 | -2  | 5    | -14 | -8 | 3 | 28   | 0    | -14 | -6  | 3 | 52   | 63   | 17  | -5  | 3 | 38    | 32    |
| 10  | -13 | 3 | 17  | 6    | -14 | -10 | 3 | 34  | 0    | -13 | -8 | 3 | 25   | 24   | -13 | -6  | 3 | -6   | 2    | 18  | -5  | 3 | 2     | 14    |
| 11  | -13 | 3 | 0   | 8    | -13 | -10 | 3 | 39  | 50   | -12 | -8 | 3 | 34   | 54   | -12 | -6  | 3 | 99   | 91   | -16 | -4  | 3 | 37    | 35    |
| 12  | -13 | 3 | -6  | 1    | -12 | -10 | 3 | 27  | 35   | -11 | -8 | 3 | 32   | 50   | -11 | -6  | 3 | 13   | 8    | -15 | -4  | 3 | 16    | 5     |
| 13  | -13 | 3 | -9  | 1    | -11 | -10 | 3 | 26  | 2    | -10 | -8 | 3 | 79   | 83   | -10 | -6  | 3 | 2    | 0    | -14 | -4  | 3 | 29    | 23    |
| 14  | -13 | 3 | -8  | 3    | -10 | -10 | 3 | 291 | 267  | -9  | -8 | 3 | -5   | 10   | -9  | -6  | 3 | 5    | 3    | -13 | -4  | 3 | 12    | 40    |
| 15  | -13 | 3 | 0   | 7    | -9  | -10 | 3 | 97  | 105  | -8  | -8 | 3 | 225  | 216  | -8  | -6  | 3 | 170  | 176  | -12 | -4  | 3 | 29    | 57    |
| -12 | -12 | 3 | -4  | 10   | -8  | -10 | 3 | 85  | 81   | -7  | -8 | 3 | -2   | 0    | -7  | -6  | 3 | 453  | 391  | -11 | -4  | 3 | 97    | 117   |
| -11 | -12 | 3 | 7   | 4    | -7  | -10 | 3 | 48  | 34   | -6  | -8 | 3 | 163  | 142  | -6  | -6  | 3 | 13   | 8    | -10 | -4  | 3 | 636   | 585   |
| -10 | -12 | 3 | 47  | 27   | -6  | -10 | 3 | 37  | 30   | -5  | -8 | 3 | 247  | 224  | -5  | -6  | 3 | 759  | 780  | -9  | -4  | 3 | 24    | 24    |
| -9  | -12 | 3 | 6   | 11   | -5  | -10 | 3 | 316 | 302  | -4  | -8 | 3 | 20   | 21   | -4  | -6  | 3 | 611  | 631  | -8  | -4  | 3 | 179   | 170   |
| -8  | -12 | 3 | 4   | 1    | -4  | -10 | 3 | 154 | 182  | -3  | -8 | 3 | 224  | 186  | -3  | -6  | 3 | 211  | 205  | -7  | -4  | 3 | 1527  | 1462  |
| -7  | -12 | 3 | 63  | 79   | -3  | -10 | 3 | 556 | 463  | -2  | -8 | 3 | 288  | 317  | -2  | -6  | 3 | 600  | 585  | -6  | -4  | 3 | 809   | 626   |
| -6  | -12 | 3 | 14  | 5    | -2  | -10 | 3 | 326 | 329  | -1  | -8 | 3 | 258  | 309  | -1  | -6  | 3 | 211  | 262  | -5  | -4  | 3 | 109   | 71    |
| -5  | -12 | 3 | 57  | 51   | -1  | -10 | 3 | 1   | 1    | 0   | -8 | 3 | 116  | 135  | 0   | -6  | 3 | 744  | 6831 | -4  | -4  | 3 | 981   | 1176  |
| -4  | -12 | 3 | 114 | 104  | 0   | -10 | 3 | 243 | 228  | 1   | -8 | 3 | -1   | 2    | 1   | -6  | 3 | 2571 | 2251 | -3  | -4  | 3 | 2749  | 2707  |
| -3  | -12 | 3 | 271 | 237  | 1   | -10 | 3 | 678 | 636  | 2   | -8 | 3 | 829  | 785  | 2   | -6  | 3 | 347  | 246  | -2  | -4  | 3 | 62    | 68    |
| -2  | -12 | 3 | 340 | 343  | 2   | -10 | 3 | 251 | 269  | 3   | -8 | 3 | 438  | 429  | 3   | -6  | 3 | 148  | 77   | -1  | -4  | 3 | 11676 | 10799 |
| -1  | -12 | 3 | 83  | 61   | 3   | -10 | 3 | 31  | 46   | 4   | -8 | 3 | -1   | 0    | 4   | -6  | 3 | 1388 | 1148 | 0   | -4  | 3 | 19227 | 16248 |
| 0   | -12 | 3 | 39  | 39   | 4   | -10 | 3 | 738 | 623  | 5   | -8 | 3 | 568  | 558  | 5   | -6  | 3 | 763  | 935  | 1   | -4  | 3 | 5     | 8     |
| 1   | -12 | 3 | 12  | 15   | 5   | -10 | 3 | 195 | 204  | 6   | -8 | 3 | 142  | 140  | 6   | -6  | 3 | 295  | 210  | 2   | -4  | 3 | 150   | 131   |
| 2   | -12 | 3 | 254 | 200  | 6   | -10 | 3 | 123 | 139  | 7   | -8 | 3 | 60   | 70   | 7   | -6  | 3 | 788  | 928  | 3   | -4  | 3 | 1585  | 1726  |
| 3   | -12 | 3 | 39  | 40   | 7   | -10 | 3 | 23  | 29   | 8   | -8 | 3 | 826  | 838  | 8   | -6  | 3 | 16   | 8    | 4   | -4  | 3 | 1959  | 2604  |
| 4   | -12 | 3 | 122 | 82   | 8   | -10 | 3 | 205 | 234  | 9   | -8 | 3 | 458  | 400  | 9   | -6  | 3 | 73   | 51   | 5   | -4  | 3 | 167   | 234   |
| 5   | -12 | 3 | 8   | 2    | 9   | -10 | 3 | 212 | 186  | 10  | -8 | 3 | 64   | 76   | 10  | -6  | 3 | 488  | 470  | 6   | -4  | 3 | 487   | 388   |
| 6   | -12 | 3 | 52  | 62   | 10  | -10 | 3 | 69  | 48   | 11  | -8 | 3 | 26   | 31   | 11  | -6  | 3 | 17   | 2    | 7   | -4  | 3 | 3037  | 3310  |
| 7   | -12 | 3 | 265 | 217  | 11  | -10 | 3 | -4  | 3    | 12  | -8 | 3 | 81   | 63   | 12  | -6  | 3 | 74   | 43   | 8   | -4  | 3 | 18    | 15    |
| 8   | -12 | 3 | 72  | 112  | 12  | -10 | 3 | 4   | 4    | 13  | -8 | 3 | 73   | 92   | 13  | -6  | 3 | 389  | 386  | 9   | -4  | 3 | 465   | 454   |
| 9   | -12 | 3 | -4  | 1    | 13  | -10 | 3 | 27  | 12   | 14  | -8 | 3 | -4   | 2    | 14  | -6  | 3 | 47   | 55   | 10  | -4  | 3 | 423   | 454   |
| 10  | -12 | 3 | 66  | 38   | 14  | -10 | 3 | 61  | 31   | 15  | -8 | 3 | -10  | 4    | 15  | -6  | 3 | -4   | 2    | 11  | -4  | 3 | 56    | 61    |
| 11  | -12 | 3 | 16  | 21   | 15  | -10 | 3 | 14  | 4    | 16  | -8 | 3 | 72   | 85   | 16  | -6  | 3 | 62   | 58   | 12  | -4  | 3 | 11    | 2     |
| 12  | -12 | 3 | 15  | 16   | 16  | -10 | 3 | -12 | 3    | 17  | -8 | 3 | 30   | 14   | 17  | -6  | 3 | 45   | 12   | 13  | -4  | 3 | 124   | 109   |
| 13  | -12 | 3 | 10  | 6    | 17  | -10 | 3 | 22  | 0    | -15 | -7 | 3 | 14   | 1    | 18  | -6  | 3 | 4    | 2    | 14  | -4  | 3 | 61    | 40    |
| 14  | -12 | 3 | -6  | 1    | -14 | -9  | 3 | 18  | 9    | -14 | -7 | 3 | 14   | 7    | -16 | -5  | 3 | 46   | 29   | 15  | -4  | 3 | 33    | 11    |
| 15  | -12 | 3 | 26  | 1    | -13 | -9  | 3 | -10 | 5    | -13 | -7 | 3 | 79   | 101  | -15 | -5  | 3 | 30   | 12   | 16  | -4  | 3 | 4     | 38    |
| 16  | -12 | 3 | -1  | 2    | -12 | -9  | 3 | -6  | 12   | -12 | -7 | 3 | 3    | 5    | -14 | -5  | 3 | 5    | 0    | 17  | -4  | 3 | 43    | 24    |
| -13 | -11 | 3 | 30  | 2    | -11 | -9  | 3 | 123 | 122  | -11 | -7 | 3 | -3   | 4    | -13 | -5  | 3 | 17   | 36   | 18  | -3  | 3 | 43    | 15    |
| -12 | -11 | 3 | 17  | 22   | -10 | -9  | 3 | 121 | 122  | -10 | -7 | 3 | 215  | 257  | -12 | -5  | 3 | 105  | 106  | -16 | -3  | 3 | 21    | 61    |
| -11 | -11 | 3 | 23  | 25   | -9  | -9  | 3 | 50  | 46   | -9  | -7 | 3 | 602  | 487  | -11 | -5  | 3 | 308  | 252  | -15 | -3  | 3 | 55    | 67    |
| -10 | -11 | 3 | 10  | 12   | -8  | -9  | 3 | 22  | 28   | -8  | -7 | 3 | 24   | 70   | -10 | -5  | 3 | 161  | 189  | -14 | -3  | 3 | 28    | 32    |
| -9  | -11 | 3 | 23  | 34   | -7  | -9  | 3 | 430 | 364  | -7  | -7 | 3 | 112  | 58   | -9  | -5  | 3 | 493  | 525  | -13 | -3  | 3 | 60    | 58    |
| -8  | -11 | 3 | 52  | 48   | -6  | -9  | 3 | 8   | 4    | -6  | -7 | 3 | 7    | 15   | -8  | -5  | 3 | 731  | 655  | -12 | -3  | 3 | 226   | 192   |
| -7  | -11 | 3 | 38  | 37   | -5  | -9  | 3 | 117 | 184  | -5  | -7 | 3 | 208  | 195  | -7  | -5  | 3 | 594  | 561  | -11 | -3  | 3 | 208   | 148   |
| -6  | -11 | 3 | 13  |      |     |     |   |     |      |     |    |   |      |      |     |     |   |      |      |     |     |   |       |       |

Table A.3, continued

| M   | K  | L | Obs  | Calc | M   | K  | L | Obs   | Calc  | M   | K  | L | Obs   | Calc  | M   | K  | L   | Obs  | Calc | M   | K   | L  | Obs  | Calc |
|-----|----|---|------|------|-----|----|---|-------|-------|-----|----|---|-------|-------|-----|----|-----|------|------|-----|-----|----|------|------|
| -11 | -2 | 3 | 61   | 68   | -8  | 0  | 3 | 513   | 472   | -6  | 2  | 3 | 14    | 16    | -5  | 4  | 3   | 90   | 126  | -5  | 6   | 3  | 364  | 339  |
| -10 | -2 | 3 | 189  | 187  | -7  | 0  | 3 | 831   | 804   | -5  | 2  | 3 | 5216  | 5171  | -4  | 4  | 3   | 1996 | 2220 | -4  | 6   | 3  | 1369 | 1651 |
| -9  | -2 | 3 | 2    | 2    | -6  | 0  | 3 | 160   | 125   | -4  | 2  | 3 | 2783  | 2963  | -3  | 4  | 3   | 868  | 840  | -3  | 6   | 3  | 983  | 864  |
| -8  | -2 | 3 | 66   | 73   | -5  | 0  | 3 | 841   | 1099  | -3  | 2  | 3 | 15861 | 12996 | -2  | 4  | 3   | 48   | 27   | -2  | 6   | 3  | 334  | 433  |
| -7  | -2 | 3 | 2011 | 1820 | -4  | 0  | 3 | 1107  | 1201  | -2  | 2  | 3 | 8863  | 8364  | -1  | 4  | 3   | 2989 | 3337 | -1  | 6   | 3  | 3911 | 3773 |
| -6  | -2 | 3 | 6    | 7    | -3  | 0  | 3 | 1516  | 1457  | -1  | 2  | 3 | 1158  | 849   | 0   | 3  | 3   | 16   | 36   | 0   | 3   | 3  | 1863 | 1865 |
| -5  | -2 | 3 | 84   | 35   | -2  | 0  | 3 | 1740  | 1580  | 0   | 2  | 3 | 36    | 79    | 1   | 4  | 3   | 0    | 1    | 1   | 6   | 3  | 4480 | 4234 |
| -4  | -2 | 3 | 12   | 20   | -1  | 0  | 3 | 5784  | 5105  | 1   | 2  | 3 | 2400  | 2577  | 2   | 4  | 3   | 4    | 11   | 2   | 6   | 3  | 27   | 5    |
| -3  | -2 | 3 | 34   | 35   | 1   | 0  | 3 | 9338  | 8246  | 2   | 2  | 3 | 1160  | 1237  | 3   | 4  | 3   | 65   | 78   | 3   | 6   | 3  | 34   | 23   |
| -2  | -2 | 3 | 5739 | 5887 | 2   | 0  | 3 | 2123  | 2656  | 3   | 2  | 3 | 1402  | 1468  | 4   | 4  | 3   | 760  | 575  | 4   | 6   | 3  | 675  | 765  |
| -1  | -2 | 3 | 603  | 691  | 3   | 0  | 3 | 239   | 249   | 4   | 2  | 3 | 1844  | 1711  | 5   | 4  | 3   | 14   | 25   | 5   | 6   | 3  | 55   | 66   |
| 0   | -2 | 3 | 2312 | 2318 | 4   | 0  | 3 | 180   | 130   | 5   | 2  | 3 | 6001  | 5468  | 6   | 4  | 3   | 530  | 592  | 6   | 6   | 3  | 45   | 51   |
| 1   | -2 | 3 | 304  | 270  | 5   | 0  | 3 | 3429  | 3282  | 6   | 2  | 3 | 740   | 813   | 7   | 4  | 3   | 691  | 513  | 7   | 6   | 3  | 614  | 542  |
| 2   | -2 | 3 | 5641 | 5159 | 6   | 0  | 3 | 19    | 11    | 7   | 2  | 3 | 163   | 163   | 8   | 4  | 3   | 12   | 2    | 8   | 6   | 3  | 27   | 31   |
| 3   | -2 | 3 | 116  | 141  | 7   | 0  | 3 | 28    | 23    | 8   | 2  | 3 | 1015  | 932   | 9   | 4  | 3   | 24   | 17   | 9   | 6   | 3  | 16   | 37   |
| 4   | -2 | 3 | 724  | 821  | 8   | 0  | 3 | 910   | 842   | 9   | 2  | 3 | 1755  | 1580  | 10  | 4  | 3   | 312  | 281  | 10  | 6   | 3  | 436  | 355  |
| 5   | -2 | 3 | 194  | 102  | 9   | 0  | 3 | 546   | 544   | 10  | 2  | 3 | 742   | 770   | 11  | 4  | 3   | 1    | 1    | 11  | 3   | 3  | 2    |      |
| 6   | -2 | 3 | 90   | 153  | 10  | 0  | 3 | 754   | 728   | 11  | 2  | 3 | 49    | 40    | 12  | 4  | 3   | 11   | 12   | 12  | 6   | 3  | 4    | 6    |
| 7   | -2 | 3 | 783  | 915  | 11  | 0  | 3 | 118   | 112   | 12  | 2  | 3 | -4    | 23    | 13  | 4  | 102 | 108  | 13   | 6   | 3   | 57 | 61   |      |
| 8   | -2 | 3 | 760  | 737  | 12  | 0  | 3 | 175   | 183   | 13  | 2  | 3 | 113   | 114   | 14  | 4  | 3   | -1   | 1    | 14  | 6   | 3  | 90   | 67   |
| 9   | -2 | 3 | 2    | 10   | 13  | 0  | 3 | 3     | 5     | 14  | 2  | 3 | -7    | 11    | 15  | 4  | 3   | 0    | 3    | -17 | 7   | 3  | 56   | 5    |
| 10  | -2 | 3 | 118  | 138  | 14  | 0  | 3 | 55    | 38    | 15  | 2  | 3 | 6     | 0     | -17 | 5  | 3   | -16  | 5    | -15 | 7   | 3  | 69   | 49   |
| 11  | -2 | 3 | 14   | 11   | 15  | 0  | 3 | 16    | 31    | 16  | 2  | 3 | 25    | 24    | -16 | 5  | 3   | 29   | 29   | -14 | 7   | 3  | 60   | 34   |
| 12  | -2 | 3 | 0    | 1    | 16  | 0  | 3 | 11    | 10    | -16 | 3  | 3 | 35    | 6     | -15 | 5  | 3   | -7   | 2    | -13 | 7   | 3  | 14   | 1    |
| 13  | -2 | 3 | 21   | 45   | -16 | 1  | 3 | 32    | 26    | -15 | 3  | 3 | 4     | 0     | -14 | 5  | 3   | -8   | 2    | -12 | 7   | 3  | 142  | 142  |
| 14  | -2 | 3 | 90   | 83   | -15 | 1  | 3 | -5    | 3     | -14 | 3  | 3 | 24    | 39    | -13 | 5  | 3   | 85   | 59   | -11 | 7   | 3  | 77   | 94   |
| 15  | -2 | 3 | 76   | 45   | -14 | 1  | 3 | 38    | 22    | -13 | 3  | 3 | 98    | 70    | -12 | 5  | 3   | 216  | 205  | -10 | 7   | 3  | 18   | 22   |
| 16  | -1 | 3 | 168  | 162  | -13 | 1  | 3 | 85    | 89    | -12 | 3  | 3 | 72    | 115   | -11 | 5  | 3   | 385  | 397  | -9  | 7   | 3  | 66   | 65   |
| 17  | -1 | 3 | 89   | 112  | -12 | 1  | 3 | 32    | 24    | -11 | 3  | 3 | 40    | 70    | -10 | 5  | 3   | 200  | 238  | -8  | 7   | 3  | 501  | 392  |
| 18  | -1 | 3 | 96   | 100  | -11 | 1  | 3 | 381   | 306   | -10 | 3  | 3 | 430   | 328   | -9  | 5  | 3   | 392  | 383  | -7  | 7   | 3  | 181  | 197  |
| 19  | -1 | 3 | 11   | 2    | -10 | 1  | 3 | 1146  | 963   | -9  | 3  | 3 | 18    | 29    | -8  | 5  | 3   | 53   | 39   | -6  | 7   | 3  | 21   | 10   |
| 20  | -1 | 3 | 91   | 89   | -9  | 1  | 3 | 27    | 4     | -8  | 3  | 3 | 58    | 31    | -7  | 5  | 3   | 215  | 167  | -5  | 7   | 3  | 412  | 340  |
| 21  | -1 | 3 | 189  | 205  | -8  | 1  | 3 | 599   | 680   | -7  | 3  | 3 | 974   | 897   | -6  | 5  | 3   | 916  | 1098 | -4  | 7   | 3  | 302  | 355  |
| 22  | -1 | 3 | 354  | 314  | -7  | 1  | 3 | 2229  | 1947  | -6  | 3  | 3 | 5403  | 4972  | -5  | 5  | 3   | 28   | 31   | -3  | 7   | 3  | 224  | 163  |
| 23  | -1 | 3 | 70   | 71   | -6  | 1  | 3 | 392   | 403   | -5  | 3  | 3 | 412   | 419   | -4  | 5  | 3   | 45   | 20   | -2  | 7   | 3  | 4611 | 4391 |
| 24  | -1 | 3 | 230  | 341  | -5  | 1  | 3 | 300   | 317   | -4  | 3  | 3 | 276   | 334   | -3  | 5  | 3   | 559  | 682  | -1  | 7   | 3  | 2117 | 1897 |
| 25  | -1 | 3 | 165  | 180  | -4  | 1  | 3 | 16532 | 14636 | -3  | 3  | 3 | 2524  | 2676  | -2  | 5  | 3   | 3807 | 3575 | 0   | 7   | 3  | 3143 | 2908 |
| 26  | -1 | 3 | 31   | 11   | 5   | 9  | 3 | 68    | 96    | -9  | 12 | 3 | -1    | 1     | -8  | 15 | 3   | 13   | 1    | 0   | -17 | 4  | 18   | 1    |
| 27  | -1 | 3 | 778  | 844  | 6   | 9  | 3 | 99    | 98    | -8  | 12 | 3 | 130   | 102   | -7  | 15 | 3   | 108  | 99   | 1   | -17 | 4  | 14   | 5    |
| 28  | -1 | 3 | 708  | 657  | 7   | 9  | 3 | 212   | 207   | -7  | 12 | 3 | 102   | 114   | -6  | 15 | 3   | 56   | 88   | 2   | -17 | 4  | 27   | 17   |
| 29  | -1 | 3 | 7    | 1    | 8   | 9  | 3 | 38    | 66    | -6  | 12 | 3 | 50    | 50    | -5  | 15 | 3   | 76   | 70   | 3   | -17 | 4  | 26   | 8    |
| 30  | -1 | 3 | 857  | 927  | 9   | 9  | 3 | 50    | 41    | -5  | 12 | 3 | 76    | 88    | -4  | 15 | 3   | -1   | 1    | 4   | -17 | 4  | 25   | 1    |
| 31  | -1 | 3 | 229  | 187  | 10  | 9  | 3 | 172   | 184   | -4  | 12 | 3 | 117   | 95    | -3  | 15 | 3   | 35   | 8    | 5   | -17 | 4  | 7    | 8    |
| 32  | -1 | 3 | 0    | 0    | 11  | 9  | 3 | 30    | 11    | -3  | 12 | 3 | 15    | 26    | -2  | 15 | 3   | 99   | 76   | 6   | -17 | 4  | 41   | 7    |
| 33  | -1 | 3 | 232  | 175  | 12  | 9  | 3 | 3     | 0     | -2  | 12 | 3 | 43    | 37    | -1  | 15 | 3   | 22   | 27   | 7   | -17 | 4  | 43   | 1    |
| 34  | -1 | 3 | 102  | 95   | -16 | 10 | 3 | 16    | 12    | -1  | 12 | 3 | 70    | 66    | 0   | 15 | 3   | 13   | 2    | 8   | -17 | 4  | 15   | 10   |
| 35  | -1 | 3 | 51   | 63   | -15 | 10 | 3 | 10    | 7     | 0   | 12 | 3 | 14    | 11    | 1   | 15 | 3   | 16   | 13   | 9   | -17 | 4  | -4   | 14   |
| 36  | -1 | 3 | 26   | 12   | -14 | 10 | 3 | -8    | 0     | 1   | 12 | 3 | 269   | 218   | 2   | 15 | 3   | 15   | 18   | 10  | -17 | 4  | -3   | 3    |
| 37  | -1 | 3 | 147  | 151  | -13 | 10 | 3 | 41    | 37    | 2   | 12 | 3 | 544   | 465   | 3   | 15 | 3   | -8   | 1    | 11  | -17 | 4  | 24   | 0    |
| 38  | -1 | 3 | 144  | 149  | -12 | 10 | 3 | 93    | 90    | 3   | 12 | 3 | 35    | 30    | 4   | 15 | 3   | -4   | 2    | -7  | -16 | 4  | 19   | 1    |
| 39  | -1 | 3 | -18  | 18   | -11 | 10 | 3 | 31    | 31    | 4   | 12 | 3 | 6     | 12    | 5   | 15 | 3   | 9    | 13   | -6  | -16 | 4  | 8    | 16   |
| 40  | -1 | 3 | 10   | 17   | -10 | 10 | 3 | 18    | 18    | 5   | 12 | 3 | 55    | 62    | 6   | 15 | 3   | 37   | 5    | -5  | -16 | 4  | 18   | 10   |
| 41  | -1 | 3 | 58   | 12   | -9  | 10 | 3 | -4    | 1     | 6   | 12 | 3 | 68    | 66    | -10 | 16 | 3   | -10  | 1    | -4  | -16 | 4  | 7    | 13   |
| 42  | -1 | 3 | -8   | 2    | -8  | 10 | 3 | 1     | 1     | 7   | 12 | 3 | -8    | 14    | -9  | 16 | 3   | -11  | 0    | -3  | -16 | 4  | 13   | 1    |
| 43  | -1 | 3 | 20   | 6    | -7  | 10 | 3 | 87    | 81    | 8   | 12 | 3 | 14    | 43    | -8  | 16 | 3   | 24   | 38   | -2  | -16 | 4  | -4   | 0    |
| 44  | -1 | 3 | 24   | 37   | -6  | 10 | 3 | 410   | 342   | 9   | 12 | 3 | 46    | 73    | -7  | 16 | 3   | 60   | 35   | -1  | -16 | 4  | -5   | 1    |
| 45  | -1 | 3 | 11   | 16   | -5  | 10 | 3 | 309   | 297   | -14 | 13 | 3 | 6     | 0     | -6  | 16 | 3   | 37   | 18   | 0   | -16 | 4  | 24   | 18   |
| 46  | -1 | 3 | 0    | 8    | -4  | 10 | 3 | 41    | 8     | -13 | 13 | 3 | 27    | 9     | -5  | 16 | 3   | -2   | 5    | 1   | -16 | 4  | 14   | 26   |
| 47  | -1 | 3 | 32   | 5    | -3  | 10 | 3 | 98    | 103   | -12 | 13 | 3 | -18   | 4     | -4  | 16 | 3   | 26   | 2    | 2   | -16 | 4  | 19   | 3    |
| 48  | -1 | 3 | 73   | 1    | -2  | 10 | 3 | 280   | 261   | -11 | 13 | 3 | 0     | 0     | -3  | 16 | 3   | -9   | 9    | 3   | -16 | 4  | 21   | 20   |
| 49  | -1 | 3 | 75   | 102  | -1  | 10 | 3 | 70    | 73    | -10 | 13 | 3 | 24    | 17    | -2  | 16 | 3   | 6    | 11   | 4   | -16 | 4  | 41   | 36   |
| 50  | -1 | 3 | 607  | 533  | 0   | 10 | 3 | 15    | 12    | -9  | 13 | 3 | 71    | 163   | -1  | 16 | 3   | 19   | 4    | 5   | -16 | 4  | 30   | 26   |
| 51  | -1 | 3 | 367  | 344  | 1   | 10 | 3 | 521   | 458   | -8  | 13 | 3 | 61    | 86    | 0   | 16 | 3   | 10   | 6    | 6   | -16 | 4  | 6    | 1    |
| 52  | -1 | 3 | 445  | 481  | 2   | 10 | 3 | 353   | 309   | -7  | 13 | 3 | 49    | 31    | 1   | 16 | 3   | -7   | 0    | 7   | -16 | 4  | 8    | 6    |
| 53  | -1 | 3 | 149  | 236  | 3   | 10 | 3 | 114   | 78    | -6  | 13 | 3 | 45    | 27    | 2   | 16 | 3   | 11   | 2    | 8   | -16 | 4  | 62   | 12   |
| 54  | -1 | 3 | 410  | 384  | 4   | 10 | 3 | 400   | 403   | -5  | 13 | 3 | 40    | 13    | 3   | 16 | 3   | 3    | 0    | 9   | -16 | 4  | 35   | 9    |
| 55  | -1 | 3 | 636  | 674  | 5   | 10 | 3 | 618   | 533   | -4  | 13 | 3 | -1    | 0     | 4   | 16 | 3   | 33   | 11   | 10  | -16 | 4  | -4   | 0    |
| 56  | -1 | 3 | 130  | 131  | 6   | 10 | 3 | 105   | 137   | -3  | 13 | 3 | 49    | 50    | 5   | 16 | 3   | -19  | 5    | 11  | -16 | 4  | 2    | 4    |
| 57  | -1 | 3 | 190  | 178  | 7   | 10 | 3 | 1     | 2     | -2  | 13 | 3 | 130   | 117   | 6   | 16 | 3   | 55   | 32   | 12  | -16 | 4  | -2   | 0    |
| 58  | -1 | 3 | 1604 | 1619 | 8   | 10 | 3 | 30    | 33    | -1  | 13 | 3 | 23    | 17    | -7  | 17 | 3   | 18   | 2    | -9  | -15 | 4  | 15   | 0    |
| 59  | -1 | 3 | 4    | 1    | 9   | 10 | 3 | 178   | 151   | 0   | 13 | 3 | 13    | 11    | -6  | 17 | 3   | 14   | 4    | -8  |     |    |      |      |

Table A.3, continued

| H      | K | L   | Obs | Calc   | H | K   | L   | Obs | Calc | H | K    | L    | Obs | Calc | H | K    | L    | Obs | Calc | H | K     | L     | Obs | Calc |
|--------|---|-----|-----|--------|---|-----|-----|-----|------|---|------|------|-----|------|---|------|------|-----|------|---|-------|-------|-----|------|
| 2-14   | 4 | 16  | 12  | 12-12  | 4 | 68  | 38  | -14 | -9   | 4 | -8   | 0    | -14 | -7   | 4 | 1    | 3    | -15 | -5   | 4 | 66    | 48    |     |      |
| 3-14   | 4 | 13  | 2   | 13-12  | 4 | 10  | 14  | -13 | -9   | 4 | 20   | 23   | -13 | -7   | 4 | -2   | 1    | -14 | -5   | 4 | 57    | 66    |     |      |
| 4-14   | 4 | 30  | 50  | 14-12  | 4 | 14  | 0   | -12 | -9   | 4 | 83   | 99   | -12 | -7   | 4 | 48   | 40   | -13 | -5   | 4 | 10    | 7     |     |      |
| 5-14   | 4 | 191 | 167 | 15-12  | 4 | -6  | 4   | -11 | -9   | 4 | 30   | 24   | -11 | -7   | 4 | -4   | 9    | -12 | -5   | 4 | 228   | 163   |     |      |
| 6-14   | 4 | 78  | 76  | 16-12  | 4 | 2   | 0   | -10 | -9   | 4 | 13   | 0    | -10 | -7   | 4 | 96   | 81   | -11 | -5   | 4 | 196   | 183   |     |      |
| 7-14   | 4 | 0   | 1   | -13-11 | 4 | 22  | 5   | -9  | -9   | 4 | 11   | 23   | -9  | -7   | 4 | 65   | 71   | -10 | -5   | 4 | 453   | 419   |     |      |
| 8-14   | 4 | 9   | 6   | -12-11 | 4 | 7   | 24  | -8  | -9   | 4 | 107  | 78   | -8  | -7   | 4 | 77   | 93   | -9  | -5   | 4 | 32    | 27    |     |      |
| 9-14   | 4 | 8   | 10  | -11-11 | 4 | 0   | 12  | -7  | -9   | 4 | 22   | 15   | -7  | -7   | 4 | 7    | 1    | -8  | -5   | 4 | 688   | 661   |     |      |
| 10-14  | 4 | 22  | 0   | -10-11 | 4 | 83  | 105 | -6  | -9   | 4 | 679  | 553  | -6  | -7   | 4 | 32   | 32   | -7  | -5   | 4 | 981   | 842   |     |      |
| 11-14  | 4 | -3  | 3   | -9-11  | 4 | 87  | 99  | -5  | -9   | 4 | 317  | 341  | -5  | -7   | 4 | 193  | 153  | -6  | -5   | 4 | 56    | 49    |     |      |
| 12-14  | 4 | 25  | 2   | -8-11  | 4 | 8   | 11  | -4  | -9   | 4 | 22   | 23   | -4  | -7   | 4 | 194  | 179  | -5  | -5   | 4 | 1030  | 1062  |     |      |
| 13-14  | 4 | -15 | 2   | -7-11  | 4 | 74  | 64  | -3  | -9   | 4 | 374  | 374  | -3  | -7   | 4 | 9    | 1    | -4  | -5   | 4 | 1829  | 1711  |     |      |
| 14-14  | 4 | 10  | 1   | -6-11  | 4 | 121 | 112 | -2  | -9   | 4 | 350  | 305  | -2  | -7   | 4 | 166  | 96   | -3  | -5   | 4 | 186   | 212   |     |      |
| -12-13 | 4 | -9  | 0   | -5-11  | 4 | -4  | 0   | -1  | -9   | 4 | 80   | 112  | -1  | -7   | 4 | 1434 | 1463 | -2  | -5   | 4 | 105   | 146   |     |      |
| -11-13 | 4 | 24  | 11  | -4-11  | 4 | 29  | 50  | 0   | -9   | 4 | 337  | 281  | 0   | -7   | 4 | 8263 | 7243 | -1  | -5   | 4 | 4862  | 4832  |     |      |
| -10-13 | 4 | 11  | 1   | -3-11  | 4 | 954 | 783 | 1   | -9   | 4 | 575  | 577  | 1   | -7   | 4 | 29   | 14   | 0   | -5   | 4 | 1625  | 2143  |     |      |
| -9-13  | 4 | 7   | 1   | -2-11  | 4 | 139 | 136 | 2   | -9   | 4 | 297  | 281  | 2   | -7   | 4 | 20   | 37   | 1   | -5   | 4 | 2384  | 2484  |     |      |
| -8-13  | 4 | 23  | 20  | -1-11  | 4 | 103 | 107 | 3   | -9   | 4 | -1   | 1    | 3   | -7   | 4 | 29   | 26   | 2   | -5   | 4 | 1828  | 1770  |     |      |
| -7-13  | 4 | 14  | 6   | 0-11   | 4 | 211 | 213 | 4   | -9   | 4 | 354  | 384  | 4   | -7   | 4 | 284  | 278  | 3   | -5   | 4 | 1383  | 1484  |     |      |
| -6-13  | 4 | 36  | 28  | 1-11   | 4 | 72  | 79  | 5   | -9   | 4 | 479  | 452  | 5   | -7   | 4 | 1326 | 1298 | 4   | -5   | 4 | 6     | 8     |     |      |
| -5-13  | 4 | 9   | 3   | 2-11   | 4 | 2   | 2   | 6   | -9   | 4 | 192  | 179  | 6   | -7   | 4 | 1070 | 992  | 5   | -5   | 4 | 31    | 10    |     |      |
| -4-13  | 4 | 112 | 100 | 3-11   | 4 | 79  | 50  | 7   | -9   | 4 | 68   | 53   | 7   | -7   | 4 | 2    | 22   | 6   | -5   | 4 | 815   | 1017  |     |      |
| -3-13  | 4 | 248 | 237 | 4-11   | 4 | 148 | 204 | 8   | -9   | 4 | 326  | 338  | 8   | -7   | 4 | 157  | 137  | 7   | -5   | 4 | -2    | 3     |     |      |
| -2-13  | 4 | -1  | 8   | 5-11   | 4 | 137 | 109 | 9   | -9   | 4 | 917  | 761  | 9   | -7   | 4 | 1157 | 1124 | 8   | -5   | 4 | 71    | 101   |     |      |
| -1-13  | 4 | 2   | 4   | 6-11   | 4 | 49  | 46  | 10  | -9   | 4 | 100  | 104  | 10  | -7   | 4 | 58   | 53   | 9   | -5   | 4 | 597   | 580   |     |      |
| 0-13   | 4 | 171 | 162 | 7-11   | 4 | 26  | 24  | 11  | -9   | 4 | -1   | 1    | 11  | -7   | 4 | 30   | 26   | 10  | -5   | 4 | 46    | 65    |     |      |
| 1-13   | 4 | -2  | 0   | 8-11   | 4 | 184 | 153 | 12  | -9   | 4 | 34   | 13   | 12  | -7   | 4 | 48   | 79   | 11  | -5   | 4 | 57    | 64    |     |      |
| 2-13   | 4 | 1   | 13  | 9-11   | 4 | 8   | 6   | 13  | -9   | 4 | 9    | 7    | 13  | -7   | 4 | 116  | 131  | 12  | -5   | 4 | 2     | 10    |     |      |
| 3-13   | 4 | 46  | 46  | 10-11  | 4 | 38  | 7   | 14  | -9   | 4 | 25   | 5    | 14  | -7   | 4 | 0    | 6    | 13  | -5   | 4 | 115   | 111   |     |      |
| 4-13   | 4 | 41  | 38  | 11-11  | 4 | 30  | 14  | 15  | -9   | 4 | 37   | 7    | 15  | -7   | 4 | -6   | 15   | 14  | -5   | 4 | 15    | 9     |     |      |
| 5-13   | 4 | 11  | 7   | 12-11  | 4 | 21  | 4   | 16  | -9   | 4 | 60   | 34   | 16  | -7   | 4 | 83   | 53   | 15  | -5   | 4 | 45    | 25    |     |      |
| 6-13   | 4 | 79  | 64  | 13-11  | 4 | -5  | 0   | 17  | -9   | 4 | 41   | 1    | 17  | -7   | 4 | -11  | 3    | 16  | -5   | 4 | 24    | 28    |     |      |
| 7-13   | 4 | 14  | 5   | 14-11  | 4 | -9  | 6   | -15 | -8   | 4 | 10   | 1    | -15 | -6   | 4 | 22   | 9    | 17  | -5   | 4 | 38    | 17    |     |      |
| 8-13   | 4 | -3  | 1   | 15-11  | 4 | 26  | 1   | -14 | -8   | 4 | 46   | 25   | -14 | -6   | 4 | 65   | 31   | -16 | -4   | 4 | 90    | 87    |     |      |
| 9-13   | 4 | 31  | 13  | 16-11  | 4 | 6   | 1   | -13 | -8   | 4 | 28   | 44   | -13 | -6   | 4 | 11   | 22   | -15 | -4   | 4 | 26    | 42    |     |      |
| 10-13  | 4 | 24  | 36  | -14-10 | 4 | 4   | 9   | -12 | -8   | 4 | 33   | 20   | -12 | -6   | 4 | -3   | 0    | -14 | -4   | 4 | 0     | 7     |     |      |
| 11-13  | 4 | 32  | 13  | -13-10 | 4 | 23  | 3   | -11 | -8   | 4 | 0    | 1    | -11 | -6   | 4 | 14   | 21   | -13 | -4   | 4 | 40    | 26    |     |      |
| 12-13  | 4 | -6  | 0   | -12-10 | 4 | 14  | 7   | -10 | -8   | 4 | 207  | 170  | -10 | -6   | 4 | 36   | 65   | -12 | -4   | 4 | 399   | 351   |     |      |
| 13-13  | 4 | -1  | 4   | -11-10 | 4 | 43  | 86  | -9  | -8   | 4 | 0    | 0    | -9  | -6   | 4 | 457  | 384  | -11 | -4   | 4 | 73    | 89    |     |      |
| 14-13  | 4 | 12  | 6   | -10-10 | 4 | 19  | 32  | -8  | -8   | 4 | 888  | 685  | -8  | -6   | 4 | 30   | 18   | -10 | -4   | 4 | 46    | 56    |     |      |
| 15-13  | 4 | -2  | 0   | -9-10  | 4 | 43  | 54  | -7  | -8   | 4 | 173  | 199  | -7  | -6   | 4 | 3    | 4    | -9  | -4   | 4 | 1372  | 1259  |     |      |
| -13-12 | 4 | 10  | 1   | -8-10  | 4 | 281 | 218 | -6  | -8   | 4 | 247  | 193  | -6  | -6   | 4 | 1050 | 1049 | -8  | -4   | 4 | 127   | 134   |     |      |
| -12-12 | 4 | 15  | 15  | -7-10  | 4 | 125 | 128 | -5  | -8   | 4 | 626  | 518  | -5  | -6   | 4 | 24   | 47   | -7  | -4   | 4 | 488   | 381   |     |      |
| -11-12 | 4 | 11  | 3   | -6-10  | 4 | 130 | 109 | -4  | -8   | 4 | 251  | 271  | -4  | -6   | 4 | 1372 | 1479 | -6  | -4   | 4 | 1654  | 1694  |     |      |
| -10-12 | 4 | 16  | 11  | -5-10  | 4 | 263 | 233 | -3  | -8   | 4 | 1393 | 1301 | -3  | -6   | 4 | 194  | 256  | -5  | -4   | 4 | 451   | 425   |     |      |
| -9-12  | 4 | 45  | 47  | -4-10  | 4 | 689 | 728 | -2  | -8   | 4 | 90   | 94   | -2  | -6   | 4 | 68   | 58   | -4  | -4   | 4 | 1210  | 1250  |     |      |
| -8-12  | 4 | 56  | 45  | -3-10  | 4 | 718 | 694 | -1  | -8   | 4 | 23   | 19   | -1  | -6   | 4 | 734  | 962  | -3  | -4   | 4 | 659   | 774   |     |      |
| -7-12  | 4 | 6   | 2   | -2-10  | 4 | 55  | 39  | 0   | -8   | 4 | 1065 | 1165 | 0   | -6   | 4 | 1882 | 2144 | -2  | -4   | 4 | 1331  | 1435  |     |      |
| -6-12  | 4 | 62  | 57  | -1-10  | 4 | 16  | 11  | 1   | -8   | 4 | 714  | 706  | 1   | -6   | 4 | 925  | 893  | -1  | -4   | 4 | 265   | 294   |     |      |
| -5-12  | 4 | 131 | 142 | 0-10   | 4 | 294 | 275 | 2   | -8   | 4 | 80   | 85   | 2   | -6   | 4 | 236  | 181  | 0   | -4   | 4 | 15051 | 14009 |     |      |
| -4-12  | 4 | 77  | 65  | 1-10   | 4 | 79  | 60  | 3   | -8   | 4 | 643  | 564  | 3   | -6   | 4 | 1193 | 1242 | 1   | -4   | 4 | 358   | 293   |     |      |
| -3-12  | 4 | 34  | 44  | 2-10   | 4 | 42  | 44  | 4   | -8   | 4 | 655  | 744  | 4   | -6   | 4 | 111  | 99   | 2   | -4   | 4 | 3694  | 3718  |     |      |
| -2-12  | 4 | 15  | 16  | 3-10   | 4 | 303 | 273 | 5   | -8   | 4 | 212  | 188  | 5   | -6   | 4 | 460  | 475  | 3   | -4   | 4 | 696   | 645   |     |      |
| -1-12  | 4 | 9   | 4   | 4-10   | 4 | -1  | 0   | 6   | -8   | 4 | 259  | 269  | 6   | -6   | 4 | 23   | 37   | 4   | -4   | 4 | 1054  | 1102  |     |      |
| 0-12   | 4 | 9   | 18  | 5-10   | 4 | 101 | 116 | 7   | -8   | 4 | 169  | 165  | 7   | -6   | 4 | 70   | 58   | 5   | -4   | 4 | 1691  | 1804  |     |      |
| 1-12   | 4 | 34  | 46  | 6-10   | 4 | 47  | 29  | 8   | -8   | 4 | 313  | 304  | 8   | -6   | 4 | 371  | 321  | 6   | -4   | 4 | 1523  | 1426  |     |      |
| 2-12   | 4 | 1   | 5   | 7-10   | 4 | -3  | 5   | 9   | -8   | 4 | 45   | 41   | 9   | -6   | 4 | 168  | 167  | 7   | -4   | 4 | 302   | 297   |     |      |
| 3-12   | 4 | 1   | 2   | 8-10   | 4 | 13  | 14  | 10  | -8   | 4 | 125  | 110  | 10  | -6   | 4 | 511  | 512  | 8   | -4   | 4 | 926   | 856   |     |      |
| 4-12   | 4 | 278 | 282 | 9-10   | 4 | 136 | 140 | 11  | -8   | 4 | 26   | 11   | 11  | -6   | 4 | 18   | 22   | 9   | -4   | 4 | -2    | 1     |     |      |
| 5-12   | 4 | 311 | 265 | 10-10  | 4 | 42  | 51  | 12  | -8   | 4 | 5    | 6    | 12  | -6   | 4 | 23   | 22   | 10  | -4   | 4 | 152   | 175   |     |      |
| 6-12   | 4 | 6   | 23  | 11-10  | 4 | 19  | 9   | 13  | -8   | 4 | 164  | 166  | 13  | -6   | 4 | -4   | 2    | 11  | -4   | 4 | 71    | 74    |     |      |
| 7-12   | 4 | 19  | 45  | 12-10  | 4 | 30  | 28  | 14  | -8   | 4 | 62   | 58   | 14  | -6   | 4 | -4   | 6    | 12  | -4   | 4 | 91    | 82    |     |      |
| 8-12   | 4 | 45  | 52  | 13-10  | 4 | 37  | 34  | 15  | -8   | 4 | 10   | 2    | 15  | -6   | 4 | 1    | 4    | 13  | -4   | 4 | 26    | 23    |     |      |
| 9-12   | 4 | 97  | 93  | 14-10  | 4 | 24  | 8   | 16  | -8   | 4 | 12   | 13   | 16  | -6   | 4 | -11  | 8    | 14  | -4   | 4 | 4     | 28    |     |      |
| 10-12  | 4 | 10  | 2   | 15-10  | 4 | 25  | 0   | 17  | -8   | 4 | 75   | 41   | 17  | -6   | 4 | 54   | 43   | 15  | -4   | 4 | 14    | 3     |     |      |
| 16-4   | 4 | 32  | 8   | 14-2   | 4 | 14  | 0   | -16 | 1    | 4 | -10  | 8    | -14 | 3    | 4 | 14   | 21   | -12 | 5    | 4 | 293   | 272   |     |      |
| 17-4   | 4 | 7   | 1   | 15-2   | 4 | 34  | 48  | -15 | 1    | 4 | 63   | 47   | -13 | 3    | 4 | 5    | 7    | -11 | 5    | 4 | 22    | 35    |     |      |
| -16-3  | 4 | 7   | 1   | -16-1  | 4 | -10 | 8   | -14 | 1    | 4 | 37   | 16   | -12 | 3    | 4 | 10   | 3    | -10 | 5    | 4 | -3    | 0     |     |      |
| -15-3  | 4 | 62  | 56  | -15-1  | 4 | 10  | 1   | -13 | 1    | 4 | 6    | 4    | -11 | 3    | 4 | 19   | 46   | -9  | 5    | 4 | 359   | 332   |     |      |
| -14-3  | 4 | 44  | 49  | -14-1  | 4 | 5   | 16  | -12 | 1    | 4 | 37   | 39   | -10 | 3    | 4 | 209  | 213  | -8  | 5    | 4 | 991   | 890   |     |      |
| -13-3  | 4 | 9   | 3   | -13-1  | 4 | 24  | 7   | -11 | 1    | 4 | 34   | 20   | -9  | 3    | 4 | 719  | 680  | -7  | 5    | 4 | 54    | 112   |     |      |
| -12-3  | 4 | 82  | 63  | -12-1  | 4 | 180 | 217 | -10 | 1    | 4 | 0    | 21   | -8  | 3    | 4 | 70   | 83   | -6  | 5    | 4 | 622   | 762   |     |      |
| -11-3  | 4 | 161 | 180 | -11-1  | 4 | 113 | 111 | -9  | 1    | 4 | 400  | 412  | -7  | 3    | 4 | 298  | 269  | -5  | 5    | 4 | 4190  | 3753  |     |      |
| -10-3  | 4 | 5   | 10  | -10-1  | 4 | 299 | 273 | -8  | 1    | 4 | 449  | 509  | -6  | 3    | 4 | 1982 | 1932 | -4  | 5    | 4 | 910   | 1183  |     |      |
| -9-3   | 4 | -3  | 6   | -9-1   | 4 | 866 | 722 | -7  | 1    | 4 |      |      |     |      |   |      |      |     |      |   |       |       |     |      |

Table A.3. continued

| M   | R  | L | Obe  | Calc | M   | K  | L | Obe  | Calc | M   | K  | L | Obe  | Calc | M   | K  | L    | Obe  | Calc |
|-----|----|---|------|------|-----|----|---|------|------|-----|----|---|------|------|-----|----|------|------|------|
| -13 | -2 | 4 | 95   | 75   | -11 | 0  | 4 | 361  | 413  | -9  | 2  | 4 | 148  | 115  | -7  | 4  | 4    | 759  | 938  |
| -12 | -2 | 4 | 290  | 280  | -10 | 0  | 4 | 229  | 283  | -8  | 2  | 4 | 699  | 699  | -6  | 4  | 4    | 3207 | 2829 |
| -11 | -2 | 4 | 36   | 3    | 0   | 0  | 4 | 3    | 3    | -7  | 2  | 4 | 784  | 855  | -5  | 4  | 4    | 331  | 400  |
| -10 | -2 | 4 | 6    | 0    | -8  | 0  | 4 | 943  | 892  | -6  | 2  | 4 | 775  | 698  | -4  | 4  | 4    | 683  | 683  |
| -9  | -2 | 4 | 1144 | 1082 | -7  | 0  | 4 | 179  | 187  | -5  | 2  | 4 | 99   | 126  | -3  | 4  | 4    | 5370 | 5139 |
| -8  | -2 | 4 | 2644 | 2320 | -6  | 0  | 4 | 3706 | 3171 | -4  | 2  | 4 | 1817 | 1906 | -2  | 4  | 4    | 4725 | 4004 |
| -7  | -2 | 4 | 1199 | 1278 | -5  | 0  | 4 | 43   | 57   | -3  | 2  | 4 | 2614 | 2529 | -1  | 4  | 4    | 50   | 60   |
| -6  | -2 | 4 | 110  | 77   | -4  | 0  | 4 | 1838 | 1709 | -2  | 2  | 4 | 257  | 291  | 0   | 4  | 4    | 47   | 114  |
| -5  | -2 | 4 | 123  | 159  | -3  | 0  | 4 | 7703 | 7674 | -1  | 2  | 4 | 313  | 386  | 1   | 4  | 4    | 939  | 959  |
| -4  | -2 | 4 | 136  | 160  | -2  | 0  | 4 | 573  | 794  | 0   | 2  | 4 | 402  | 426  | 2   | 4  | 4    | 378  | 419  |
| -3  | -2 | 4 | 12   | 14   | -1  | 0  | 4 | 3017 | 2900 | 1   | 2  | 4 | 1358 | 1536 | 3   | 4  | 4    | 670  | 640  |
| -2  | -2 | 4 | 190  | 683  | 0   | 0  | 4 | 807  | 1082 | 2   | 2  | 4 | 9    | 1    | 4   | 4  | 1107 | 1084 |      |
| -1  | -2 | 4 | 4137 | 4276 | 0   | 0  | 4 | 122  | 171  | 3   | 2  | 4 | 580  | 616  | 5   | 4  | 4    | 776  | 828  |
| 0   | -2 | 4 | 1116 | 1558 | 2   | 0  | 4 | 645  | 664  | 4   | 2  | 4 | 319  | 372  | 6   | 4  | 4    | 1135 | 978  |
| 1   | -2 | 4 | 4956 | 5388 | 3   | 0  | 4 | 1685 | 2166 | 5   | 2  | 4 | 11   | 13   | 7   | 4  | 910  | 905  |      |
| 2   | -2 | 4 | 7292 | 6920 | 4   | 0  | 4 | 3377 | 3088 | 6   | 2  | 4 | 581  | 576  | 8   | 4  | 4    | 1859 | 1604 |
| 3   | -2 | 4 | 1154 | 1334 | 5   | 0  | 4 | 551  | 451  | 7   | 2  | 4 | 622  | 703  | 9   | 4  | 4    | 83   | 69   |
| 4   | -2 | 4 | 1110 | 1040 | 6   | 0  | 4 | 633  | 645  | 8   | 2  | 4 | 1014 | 916  | 10  | 4  | 4    | 23   | 16   |
| 5   | -2 | 4 | 4480 | 4137 | 7   | 0  | 4 | 16   | 34   | 9   | 2  | 4 | 47   | 25   | 11  | 4  | 4    | 181  | 150  |
| 6   | -2 | 4 | 3533 | 3252 | 8   | 0  | 4 | 116  | 111  | 10  | 2  | 4 | 59   | 53   | 12  | 4  | 4    | 22   | 29   |
| 7   | -2 | 4 | 13   | 0    | 9   | 0  | 4 | 410  | 430  | 11  | 2  | 4 | 338  | 287  | 13  | 4  | 4    | 7    | 4    |
| 8   | -2 | 4 | 353  | 340  | 10  | 0  | 4 | 460  | 460  | 12  | 2  | 4 | 3    | 1    | 14  | 4  | 7    | 4    | -17  |
| 9   | -2 | 4 | 1256 | 1296 | 11  | 0  | 4 | 273  | 293  | 13  | 2  | 4 | 128  | 122  | -17 | 5  | 4    | 41   | 21   |
| 10  | -2 | 4 | 1027 | 919  | 12  | 0  | 4 | 15   | 14   | 14  | 2  | 4 | -6   | 1    | -16 | 5  | 4    | -7   | 3    |
| 11  | -2 | 4 | 41   | 41   | 13  | 0  | 4 | 220  | 191  | 15  | 2  | 4 | 5    | 2    | -15 | 5  | 4    | 128  | 98   |
| 12  | -2 | 4 | 176  | 192  | 14  | 0  | 4 | 84   | 93   | -16 | 3  | 4 | 2    | 9    | -14 | 5  | 4    | 217  | 182  |
| 13  | -2 | 4 | 45   | 31   | 15  | 0  | 4 | -5   | 1    | -15 | 3  | 4 | 79   | 78   | -13 | 5  | 4    | 187  | 225  |
| -10 | 7  | 4 | -1   | 2    | -3  | 9  | 4 | 453  | 477  | 8   | 11 | 4 | 40   | 55   | 5   | 14 | 4    | 3    | 37   |
| -9  | 7  | 4 | 6    | 3    | -2  | 9  | 4 | 16   | 28   | 9   | 11 | 4 | 42   | 45   | 6   | 14 | 4    | -2   | 0    |
| -8  | 7  | 4 | 591  | 549  | -1  | 9  | 4 | 476  | 431  | 10  | 11 | 4 | 13   | 4    | -11 | 15 | 4    | -13  | 4    |
| -7  | 7  | 4 | 294  | 289  | 0   | 9  | 4 | 410  | 412  | -14 | 12 | 4 | -6   | 5    | -10 | 15 | 4    | -4   | 8    |
| -6  | 7  | 4 | 600  | 611  | 1   | 9  | 4 | 214  | 212  | -13 | 12 | 4 | -7   | 3    | 9   | 15 | 4    | -14  | 1    |
| -5  | 7  | 4 | 1    | 2    | 9   | 9  | 4 | 918  | 759  | -12 | 12 | 4 | -4   | 4    | -8  | 15 | 4    | 3    | 16   |
| -4  | 7  | 4 | 38   | 46   | 3   | 9  | 4 | 9    | 2    | -11 | 12 | 4 | 26   | 18   | -7  | 15 | 4    | 12   | 20   |
| -3  | 7  | 4 | 1383 | 1354 | 4   | 9  | 4 | 38   | 24   | -10 | 12 | 4 | 50   | 56   | -6  | 15 | 4    | 34   | 24   |
| -2  | 7  | 4 | 0    | 3    | 5   | 9  | 4 | 360  | 386  | -9  | 12 | 4 | 82   | 71   | -5  | 15 | 4    | -6   | 0    |
| -1  | 7  | 4 | 765  | 694  | 6   | 9  | 4 | 9    | 3    | -8  | 12 | 4 | 0    | 1    | -4  | 15 | 4    | 10   | 4    |
| 0   | 7  | 4 | 907  | 948  | 7   | 9  | 4 | 16   | 21   | -7  | 12 | 4 | 210  | 188  | -3  | 15 | 4    | 1    | 10   |
| 1   | 7  | 4 | 5    | 2    | 8   | 9  | 4 | 292  | 350  | -6  | 12 | 4 | 20   | 46   | -2  | 15 | 4    | -2   | 1    |
| 2   | 7  | 4 | 6    | 10   | 9   | 9  | 4 | 85   | 81   | -5  | 12 | 4 | -2   | 0    | -1  | 15 | 4    | 14   | 7    |
| 3   | 7  | 4 | 321  | 632  | 10  | 9  | 4 | 19   | 3    | -4  | 12 | 4 | 12   | 19   | 10  | 16 | 4    | 13   | 22   |
| 4   | 7  | 4 | 164  | 164  | 11  | 9  | 4 | 12   | 2    | -3  | 12 | 4 | 23   | 16   | 1   | 15 | 4    | 8    | 12   |
| 5   | 7  | 4 | 104  | 116  | 12  | 9  | 4 | -1   | 1    | -2  | 12 | 4 | 8    | 2    | 2   | 15 | 4    | 14   | 9    |
| 6   | 7  | 4 | 301  | 317  | -15 | 10 | 4 | 13   | 9    | -1  | 12 | 4 | 29   | 18   | 3   | 15 | 4    | 15   | 18   |
| 7   | 7  | 4 | 34   | 36   | -14 | 10 | 4 | 14   | 13   | 0   | 12 | 4 | 6    | 5    | 4   | 15 | 4    | 31   | 26   |
| 8   | 7  | 4 | 127  | 114  | -13 | 10 | 4 | 12   | 1    | 1   | 12 | 4 | 15   | 19   | 5   | 15 | 4    | -7   | 0    |
| 9   | 7  | 4 | 16   | 11   | -12 | 10 | 4 | 31   | 6    | 2   | 12 | 4 | 398  | 372  | 6   | 15 | 4    | 24   | 19   |
| 10  | 7  | 4 | 143  | 117  | -11 | 10 | 4 | 3    | 34   | 3   | 12 | 4 | 327  | 299  | -9  | 16 | 4    | 126  | 3    |
| 11  | 7  | 4 | 111  | 96   | -10 | 10 | 4 | 3    | 5    | 4   | 12 | 4 | 104  | 97   | -8  | 16 | 4    | -3   | 0    |
| 12  | 7  | 4 | -4   | 0    | -9  | 10 | 4 | 2    | 0    | 5   | 12 | 4 | 21   | 36   | -7  | 16 | 4    | 13   | 10   |
| 13  | 7  | 4 | -4   | 5    | -8  | 10 | 4 | 2    | 6    | 6   | 12 | 4 | -5   | 19   | -6  | 16 | 4    | 11   | 16   |
| -14 | 8  | 4 | -16  | 0    | -7  | 10 | 4 | 196  | 214  | 7   | 12 | 4 | 11   | 19   | -5  | 16 | 4    | 27   | 10   |
| -15 | 8  | 4 | 28   | 23   | -6  | 10 | 4 | 3    | 10   | 8   | 12 | 4 | 9    | 5    | -4  | 16 | 4    | 19   | 16   |
| -14 | 8  | 4 | -8   | 4    | -5  | 10 | 4 | 5    | 1    | 9   | 12 | 4 | 43   | 23   | -3  | 16 | 4    | 15   | 0    |
| -13 | 8  | 4 | 1    | 0    | -4  | 10 | 4 | 63   | 78   | -13 | 13 | 4 | -15  | 0    | -2  | 16 | 4    | 9    | 6    |
| -12 | 8  | 4 | 64   | 75   | -3  | 10 | 4 | 47   | 24   | -12 | 13 | 4 | 57   | 15   | -1  | 16 | 4    | 20   | 13   |
| -11 | 8  | 4 | 22   | 16   | -2  | 10 | 4 | 34   | 26   | -11 | 13 | 4 | 10   | 17   | 0   | 16 | 4    | 2    | 0    |
| -10 | 8  | 4 | -4   | 5    | -1  | 10 | 4 | 235  | 232  | -10 | 13 | 4 | 20   | 9    | 1   | 16 | 4    | 0    | 0    |
| -9  | 8  | 4 | 9    | 1    | 0   | 10 | 4 | 375  | 284  | -9  | 13 | 4 | 59   | 1    | 2   | 16 | 4    | 0    | 0    |
| -8  | 8  | 4 | 43   | 47   | 1   | 10 | 4 | 40   | 40   | -8  | 13 | 4 | 29   | 62   | 4   | 16 | 4    | 13   | 12   |
| -7  | 8  | 4 | 1    | 2    | 1   | 10 | 4 | 281  | 177  | -7  | 13 | 4 | 0    | 0    | 4   | 16 | 4    | 83   | 0    |
| -6  | 8  | 4 | 31   | 41   | 3   | 10 | 4 | 218  | 271  | -6  | 13 | 4 | -1   | 3    | 5   | 16 | 4    | 20   | 19   |
| -5  | 8  | 4 | 318  | 317  | 4   | 10 | 4 | 16   | 7    | -5  | 13 | 4 | 17   | 23   | -6  | 17 | 4    | -2   | 5    |
| -4  | 8  | 4 | 919  | 788  | 5   | 10 | 4 | -1   | 0    | -4  | 13 | 4 | 54   | 42   | -5  | 17 | 4    | 27   | 7    |
| -3  | 8  | 4 | 1    | 1    | 6   | 10 | 4 | 82   | 100  | -3  | 13 | 4 | 11   | 16   | -4  | 17 | 4    | 5    | 0    |
| -2  | 8  | 4 | 101  | 89   | 7   | 10 | 4 | 113  | 102  | -2  | 13 | 4 | 43   | 24   | -3  | 17 | 4    | 12   | 13   |
| -1  | 8  | 4 | 8    | 10   | 8   | 10 | 4 | 19   | 30   | -1  | 13 | 4 | 104  | 87   | -2  | 17 | 4    | 13   | 2    |
| 0   | 8  | 4 | 126  | 125  | 9   | 10 | 4 | 90   | 94   | 0   | 13 | 4 | -4   | 0    | -1  | 17 | 4    | 11   | 0    |
| 1   | 8  | 4 | 46   | 37   | 10  | 10 | 4 | 0    | 28   | 1   | 13 | 4 | 130  | 155  | 0   | 17 | 4    | 7    | 4    |
| 2   | 8  | 4 | 225  | 236  | 11  | 10 | 4 | 19   | 10   | 2   | 13 | 4 | 114  | 103  | 3   | 17 | 4    | 35   | 0    |
| 3   | 8  | 4 | 230  | 247  | -15 | 11 | 4 | 48   | 38   | 3   | 13 | 4 | 1    | 1    | 2   | 17 | 4    | 11   | 1    |
| 4   | 8  | 4 | 15   | 26   | -14 | 11 | 4 | 10   | 11   | 4   | 13 | 4 | 23   | 21   | -2  | 18 | 4    | -16  | 3    |
| 5   | 8  | 4 | 214  | 189  | -13 | 11 | 4 | -6   | 1    | 5   | 13 | 4 | 29   | 31   | -1  | 18 | 4    | -8   | 0    |
| 6   | 8  | 4 | 374  | 328  | -12 | 11 | 4 | 2    | 3    | 6   | 13 | 4 | 78   | 66   | 0   | 18 | 4    | 23   | 1    |
| 7   | 8  | 4 | 31   | 38   | -11 | 11 | 4 | 24   | 12   | 7   | 13 | 4 | 3    | 5    | 1   | 18 | 4    | 9    | 4    |
| 8   | 8  | 4 | 101  | 84   | -10 | 11 | 4 | 103  | 88   | 8   | 13 | 4 | 15   | 11   | 2   | 18 | 4    | 5    | 5    |
| 9   | 8  | 4 | 204  | 162  | -9  | 11 | 4 | 240  | 200  | -12 | 14 | 4 | 11   | 3    | 3   | 18 | 4    | 14   | 2    |
| 10  | 8  | 4 | 91   | 88   | -8  | 11 | 4 | 448  | 418  | -11 | 14 | 4 | -5   | 1    | 4   | 18 | 4    | -3   | 6    |
| 11  | 8  | 4 | 27   | 5    | -7  | 11 | 4 | 27   | 9    | -10 | 14 | 4 | -6   | 5    | -5  | 18 | 4    | 5    | 6    |
| 12  | 8  | 4 | -1   | 2    | -6  | 11 | 4 | 336  | 312  | -9  | 14 | 4 | 49   | 306  | 6   | 18 | 4    | 2    | 7    |
| 13  | 8  | 4 | -1   | 1    | 15  | 11 | 4 | 86   | 85   | -8  | 14 | 4 | 2    | 1    | 7   | 18 | 4    | 1    | 4    |
| -16 | 9  | 4 | -1   | 8    | -4  | 11 | 4 | 0    | 7    | -7  | 14 | 4 | 30   | 24   | 8   | 18 | 4    | 4    | 11   |
| -14 | 9  | 4 | -3   | 5    | -3  | 11 | 4 | 146  | 128  | -6  | 14 | 4 | 70   | 66   | 9   | 18 | 4    | 15   | 6    |
| -13 | 9  | 4 | 23   | 31   | -2  | 11 | 4 | 80   | 95   | -5  | 14 | 4 | 75   | 75   | -4  | 17 | 4    | 2    | 0    |
| -12 | 9  | 4 | 39   | 56   | -1  | 11 | 4 | 98   | 79   | -4  | 14 | 4 | 7    | 12   | -3  | 17 | 4    | 20   | 1    |
| -11 | 9  | 4 | 2    | 9    | 0   | 11 | 4 | 52   | 30   | -3  | 14 | 4 | 21   | 16   | -2  | 17 | 4    | -5   | 0    |
| -10 | 9  | 4 | 20   | 27   | 1   | 11 | 4 | 381  | 351  | -2  | 14 | 4 | 78   | 78   | -1  | 17 | 4    | 10   | 7    |
| -9  | 9  | 4 | 87   | 68   | 2   | 11 | 4 | 598  | 580  | -1  | 14 | 4 | 22   | 30   | 0   | 17 | 4    | 5    | 4    |
| -8  | 9  | 4 | 18   | 3    | 11  | 11 | 4 | 319  | 31   | -10 | 15 | 4 | -4   | 1    | 3   | 17 | 4    | 6    | 1    |
| -7  | 9  | 4 | 37   | 8    | 12  | 11 | 4 | 125  | 136  | 1   | 14 | 4 | 14   | 17   | 2   | 17 | 4    | 37   | 17   |
| -6  | 9  | 4 | 363  | 325  |     |    |   |      |      |     |    |   |      |      |     |    |      |      |      |

Table A.3, continued

| M      | K | L    | Obs  | Calc  | M | K    | L    | Obs  | Calc | M    | K    | L    | Obs | Calc | M    | K    | L | Obs  | Calc | M | K | L | Obs | Calc |
|--------|---|------|------|-------|---|------|------|------|------|------|------|------|-----|------|------|------|---|------|------|---|---|---|-----|------|
| -5-13  | 5 | 125  | 118  | 5-11  | 5 | 257  | 242  | 9-9  | 5    | 160  | 147  | 11-7 | 5   | 12   | 5    | 11-5 | 5 | 41   | 31   |   |   |   |     |      |
| -4-13  | 5 | 21   | 10   | 6-11  | 5 | 4    | 1    | 10-9 | 5    | -1   | 12   | 12-7 | 5   | 10   | 2    | 12-5 | 5 | 9    | 8    |   |   |   |     |      |
| -3-13  | 5 | 184  | 163  | 7-11  | 5 | 21   | 30   | 11-9 | 5    | 148  | 167  | 13-7 | 5   | 136  | 98   | 13-5 | 5 | -4   | 1    |   |   |   |     |      |
| -2-13  | 5 | 171  | 146  | 8-11  | 5 | 11   | 21   | 12-9 | 5    | 47   | 41   | 14-7 | 5   | 101  | 110  | 14-5 | 5 | 34   | 28   |   |   |   |     |      |
| -1-13  | 5 | 0    | 4    | 9-11  | 5 | 74   | 63   | 13-9 | 5    | 122  | 142  | 15-7 | 5   | 8    | 0    | 15-5 | 5 | 12   | 13   |   |   |   |     |      |
| 0-13   | 5 | 11   | 14   | 10-11 | 5 | 43   | 22   | 14-9 | 5    | 6    | 11   | 16-7 | 5   | 0    | 9    | 16-5 | 5 | 14   | 8    |   |   |   |     |      |
| 1-13   | 5 | 127  | 121  | 11-11 | 5 | 20   | 12   | 15-9 | 5    | 13   | 1    | 16-6 | 5   | 21   | 18   | 16-4 | 5 | 23   | 10   |   |   |   |     |      |
| 2-13   | 5 | 47   | 68   | 12-11 | 5 | 18   | 11   | 16-9 | 5    | 22   | 31   | 17-6 | 5   | 69   | 50   | 17-4 | 5 | 101  | 85   |   |   |   |     |      |
| 3-13   | 5 | 9    | 0    | 13-11 | 5 | 17   | 22   | 17-9 | 5    | 10   | 8    | 17-5 | 5   | 35   | 50   | 17-4 | 5 | 97   | 76   |   |   |   |     |      |
| 4-13   | 5 | 67   | 80   | 14-11 | 5 | 58   | 0    | 18-9 | 5    | -9   | 0    | 17-4 | 5   | 22   | 7    | 17-3 | 5 | -5   | 0    |   |   |   |     |      |
| 5-13   | 5 | 187  | 204  | 15-11 | 5 | 25   | 2    | 19-9 | 5    | 28   | 34   | 17-2 | 5   | 56   | 58   | 17-1 | 5 | 86   | 91   |   |   |   |     |      |
| 6-13   | 5 | 7    | 5    | 16-10 | 5 | 15   | 0    | 20-9 | 5    | 18   | 28   | 17-1 | 5   | 65   | 68   | 17-1 | 5 | 295  | 236  |   |   |   |     |      |
| 7-13   | 5 | 49   | 53   | 17-10 | 5 | 26   | 30   | 21-9 | 5    | 26   | 13   | 17-0 | 5   | 10   | 1    | 17-0 | 5 | 231  | 242  |   |   |   |     |      |
| 8-13   | 5 | 74   | 92   | 18-10 | 5 | 15   | 16   | 22-9 | 5    | 118  | 134  | 17-0 | 5   | 47   | 50   | 17-0 | 5 | 6    | 9    |   |   |   |     |      |
| 9-13   | 5 | 26   | 41   | 19-10 | 5 | -7   | 10   | 23-9 | 5    | 42   | 31   | 17-0 | 5   | 100  | 110  | 17-0 | 5 | 650  | 632  |   |   |   |     |      |
| 10-13  | 5 | -5   | 0    | 20-10 | 5 | 2    | 4    | 24-9 | 5    | 241  | 205  | 17-0 | 5   | 7    | 8    | 17-0 | 5 | 592  | 655  |   |   |   |     |      |
| 11-13  | 5 | 44   | 44   | 21-10 | 5 | 28   | 14   | 25-9 | 5    | 183  | 184  | 17-0 | 5   | 1    | 6    | 17-0 | 5 | 205  | 238  |   |   |   |     |      |
| 12-13  | 5 | 39   | 52   | 22-10 | 5 | -4   | 0    | 26-9 | 5    | 435  | 391  | 17-0 | 5   | 206  | 229  | 17-0 | 5 | 17   | 4    |   |   |   |     |      |
| 13-13  | 5 | 17   | 19   | 23-10 | 5 | 156  | 168  | 27-9 | 5    | 676  | 619  | 17-0 | 5   | 370  | 343  | 17-0 | 5 | 2432 | 2576 |   |   |   |     |      |
| 14-13  | 5 | -3   | 0    | 24-10 | 5 | 70   | 71   | 28-9 | 5    | 90   | 78   | 17-0 | 5   | 19   | 35   | 17-0 | 5 | 67   | 57   |   |   |   |     |      |
| -12-12 | 5 | -7   | 4    | 25-10 | 5 | 817  | 723  | 29-9 | 5    | 206  | 219  | 17-0 | 5   | 90   | 34   | 17-0 | 5 | 4    | 1    |   |   |   |     |      |
| -11-12 | 5 | 22   | 25   | 26-10 | 5 | 377  | 368  | 30-9 | 5    | 270  | 409  | 17-0 | 5   | 1759 | 1673 | 17-0 | 5 | 35   | 59   |   |   |   |     |      |
| -10-12 | 5 | 3    | 14   | 27-10 | 5 | 200  | 180  | 31-9 | 5    | 1252 | 1026 | 17-0 | 5   | 14   | 22   | 17-0 | 5 | 9    | 3    |   |   |   |     |      |
| -9-12  | 5 | 7    | 19   | 28-10 | 5 | 40   | 59   | 32-9 | 5    | 0    | 8    | 17-0 | 5   | 1738 | 1756 | 17-0 | 5 | 409  | 346  |   |   |   |     |      |
| -8-12  | 5 | 9    | 0    | 29-10 | 5 | 469  | 427  | 33-9 | 5    | 3637 | 3670 | 17-0 | 5   | 636  | 664  | 17-0 | 5 | 827  | 1024 |   |   |   |     |      |
| -7-12  | 5 | 119  | 135  | 30-10 | 5 | 11   | 9    | 34-9 | 5    | 1139 | 1031 | 17-0 | 5   | 1279 | 1290 | 17-0 | 5 | 84   | 78   |   |   |   |     |      |
| -6-12  | 5 | 29   | 19   | 31-10 | 5 | 684  | 672  | 35-9 | 5    | -1   | 0    | 17-0 | 5   | 2    | 0    | 17-0 | 5 | 841  | 971  |   |   |   |     |      |
| -5-12  | 5 | 2    | 10   | 32-10 | 5 | 3    | 4    | 36-9 | 5    | 56   | 35   | 17-0 | 5   | 712  | 724  | 17-0 | 5 | 516  | 604  |   |   |   |     |      |
| -4-12  | 5 | 331  | 298  | 33-10 | 5 | 5    | 0    | 37-9 | 5    | 645  | 637  | 17-0 | 5   | 157  | 164  | 17-0 | 5 | 37   | 23   |   |   |   |     |      |
| -3-12  | 5 | 69   | 59   | 34-10 | 5 | 319  | 254  | 38-9 | 5    | 257  | 248  | 17-0 | 5   | 149  | 192  | 17-0 | 5 | 1051 | 1064 |   |   |   |     |      |
| -2-12  | 5 | 7    | 9    | 35-10 | 5 | 374  | 408  | 39-9 | 5    | 0    | 2    | 17-0 | 5   | 429  | 344  | 17-0 | 5 | 71   | 79   |   |   |   |     |      |
| -1-12  | 5 | 17   | 3    | 36-10 | 5 | 66   | 46   | 40-9 | 5    | 53   | 54   | 17-0 | 5   | 10   | 4    | 17-0 | 5 | 9    | 5    |   |   |   |     |      |
| 0-12   | 5 | 34   | 23   | 37-10 | 5 | 66   | 14   | 41-9 | 5    | 196  | 161  | 17-0 | 5   | 32   | 4    | 17-0 | 5 | 142  | 150  |   |   |   |     |      |
| 1-12   | 5 | 49   | 33   | 38-10 | 5 | 102  | 85   | 42-9 | 5    | 568  | 519  | 17-0 | 5   | -1   | 4    | 17-0 | 5 | 854  | 837  |   |   |   |     |      |
| 2-12   | 5 | 77   | 61   | 39-10 | 5 | 159  | 139  | 43-9 | 5    | 216  | 214  | 17-0 | 5   | 32   | 22   | 17-0 | 5 | 22   | 16   |   |   |   |     |      |
| 3-12   | 5 | 13   | 2    | 40-10 | 5 | 18   | 17   | 44-9 | 5    | 92   | 78   | 17-0 | 5   | 238  | 187  | 17-0 | 5 | 82   | 59   |   |   |   |     |      |
| 4-12   | 5 | 245  | 221  | 41-10 | 5 | 7    | 20   | 45-9 | 5    | 59   | 44   | 17-0 | 5   | -5   | 7    | 17-0 | 5 | -5   | 1    |   |   |   |     |      |
| 5-12   | 5 | 1    | 0    | 42-10 | 5 | 3    | 0    | 46-9 | 5    | 12   | 12   | 17-0 | 5   | 4    | 10   | 17-0 | 5 | 11   | 5    |   |   |   |     |      |
| 6-12   | 5 | 0    | 0    | 43-10 | 5 | -6   | 1    | 47-9 | 5    | 30   | 9    | 17-0 | 5   | 28   | 15   | 17-0 | 5 | -7   | 10   |   |   |   |     |      |
| 7-12   | 5 | 6    | 14   | 44-10 | 5 | 31   | 9    | 48-9 | 5    | -10  | 16   | 17-0 | 5   | 98   | 95   | 17-0 | 5 | 42   | 22   |   |   |   |     |      |
| 8-12   | 5 | 43   | 37   | 45-10 | 5 | 9    | 6    | 49-9 | 5    | -9   | 1    | 17-0 | 5   | 9    | 0    | 17-0 | 5 | 24   | 6    |   |   |   |     |      |
| 9-12   | 5 | -4   | 1    | 46-10 | 5 | 16   | 6    | 50-9 | 5    | 24   | 6    | 17-0 | 5   | 2    | 0    | 17-0 | 5 | 22   | 24   |   |   |   |     |      |
| 10-12  | 5 | 53   | 38   | 47-10 | 5 | 27   | 6    | 51-9 | 5    | 63   | 49   | 17-0 | 5   | 36   | 19   | 17-0 | 5 | 24   | 15   |   |   |   |     |      |
| 11-12  | 5 | 9    | 22   | 48-10 | 5 | 13   | 13   | 52-9 | 5    | 17   | 8    | 17-0 | 5   | 10   | 4    | 17-0 | 5 | 347  | 283  |   |   |   |     |      |
| 12-12  | 5 | -6   | 0    | 49-10 | 5 | 3    | 12   | 53-9 | 5    | 4    | 18   | 17-0 | 5   | 5    | 34   | 17-0 | 5 | 189  | 196  |   |   |   |     |      |
| 13-12  | 5 | 2    | 6    | 50-10 | 5 | 36   | 24   | 54-9 | 5    | 282  | 228  | 17-0 | 5   | 8    | 6    | 17-0 | 5 | 221  | 197  |   |   |   |     |      |
| 14-12  | 5 | 8    | 13   | 51-10 | 5 | 6    | 3    | 55-9 | 5    | 0    | 3    | 17-0 | 5   | 121  | 119  | 17-0 | 5 | 768  | 662  |   |   |   |     |      |
| 15-12  | 5 | -9   | 2    | 52-10 | 5 | 11   | 1    | 56-9 | 5    | 115  | 118  | 17-0 | 5   | 470  | 466  | 17-0 | 5 | 1851 | 1743 |   |   |   |     |      |
| -13-11 | 5 | 9    | 5    | 53-9  | 5 | 28   | 40   | 57-9 | 5    | 510  | 404  | 17-0 | 5   | 643  | 640  | 17-0 | 5 | 5    | 24   |   |   |   |     |      |
| -12-11 | 5 | 36   | 18   | 54-9  | 5 | 8    | 14   | 58-9 | 5    | 2    | 1    | 17-0 | 5   | 20   | 13   | 17-0 | 5 | 716  | 719  |   |   |   |     |      |
| -11-11 | 5 | 6    | 0    | 55-9  | 5 | 428  | 357  | 59-9 | 5    | 19   | 20   | 17-0 | 5   | 175  | 238  | 17-0 | 5 | 774  | 1010 |   |   |   |     |      |
| -10-11 | 5 | 130  | 114  | 56-9  | 5 | 52   | 86   | 60-9 | 5    | 422  | 359  | 17-0 | 5   | 757  | 827  | 17-0 | 5 | 806  | 770  |   |   |   |     |      |
| -9-11  | 5 | 53   | 38   | 57-9  | 5 | -3   | 1    | 61-9 | 5    | 167  | 163  | 17-0 | 5   | 32   | 22   | 17-0 | 5 | 134  | 110  |   |   |   |     |      |
| -8-11  | 5 | 100  | 90   | 58-9  | 5 | 683  | 599  | 62-9 | 5    | 557  | 598  | 17-0 | 5   | 5    | 5    | 17-0 | 5 | 1976 | 2365 |   |   |   |     |      |
| -7-11  | 5 | 11   | 9    | 59-9  | 5 | 38   | 22   | 63-9 | 5    | 512  | 509  | 17-0 | 5   | 2308 | 2181 | 17-0 | 5 | 2007 | 2091 |   |   |   |     |      |
| 0-11   | 5 | 8    | 2    | 60-9  | 5 | 314  | 472  | 64-9 | 5    | 5    | 7    | 17-0 | 5   | 486  | 562  | 17-0 | 5 | 48   | 29   |   |   |   |     |      |
| 1-11   | 5 | 2009 | 2249 | 61-9  | 5 | 1091 | 1312 | 65-9 | 5    | 69   | 33   | 17-0 | 5   | 2679 | 2324 | 17-0 | 5 | 63   | 68   |   |   |   |     |      |
| 2-11   | 5 | 397  | 372  | 62-9  | 5 | 6620 | 6169 | 66-9 | 5    | 24   | 26   | 17-0 | 5   | 623  | 580  | 17-0 | 5 | 36   | 32   |   |   |   |     |      |
| 3-11   | 5 | 644  | 784  | 63-9  | 5 | 2362 | 2097 | 67-9 | 5    | 202  | 193  | 17-0 | 5   | 201  | 197  | 17-0 | 5 | 61   | 53   |   |   |   |     |      |
| 4-11   | 5 | 347  | 452  | 64-9  | 5 | 3383 | 3437 | 68-9 | 5    | 1278 | 1124 | 17-0 | 5   | 341  | 333  | 17-0 | 5 | 7    | 0    |   |   |   |     |      |
| 5-11   | 5 | 1814 | 1726 | 65-9  | 5 | 49   | 59   | 69-9 | 5    | 21   | 4    | 17-0 | 5   | 41   | 61   | 17-0 | 5 | 76   | 6    |   |   |   |     |      |
| 6-11   | 5 | 21   | 49   | 7-11  | 5 | 816  | 797  | 70-9 | 5    | 87   | 59   | 17-0 | 5   | 15   | 15   | 17-0 | 5 | 6    | 6    |   |   |   |     |      |
| 7-11   | 5 | 254  | 245  | 8-11  | 5 | 186  | 172  | 71-9 | 5    | 445  | 453  | 17-0 | 5   | 39   | 46   | 17-0 | 5 | 49   | 51   |   |   |   |     |      |
| 8-11   | 5 | 699  | 675  | 9-11  | 5 | 565  | 470  | 72-9 | 5    | 97   | 73   | 17-0 | 5   | 21   | 43   | 17-0 | 5 | 23   | 16   |   |   |   |     |      |
| 9-11   | 5 | 222  | 176  | 10-11 | 5 | 222  | 267  | 73-9 | 5    | -4   | 0    | 17-0 | 5   | -5   | 2    | 17-0 | 5 | 94   | 83   |   |   |   |     |      |
| 10-11  | 5 | 995  | 860  | 11-11 | 5 | 11   | 1    | 74-9 | 5    | 196  | 179  | 17-0 | 5   | 9    | 45   | 17-0 | 5 | 31   | 14   |   |   |   |     |      |
| 11-11  | 5 | 89   | 99   | 12-11 | 5 | 48   | 74   | 75-9 | 5    | 0    | 1    | 17-0 | 5   | 38   | 51   | 17-0 | 5 | 73   | 70   |   |   |   |     |      |
| 12-11  | 5 | 47   | 44   | 13-11 | 5 | 268  | 253  | 76-9 | 5    | 72   | 33   | 17-0 | 5   | 13   | 9    | 17-0 | 5 | 34   | 28   |   |   |   |     |      |
| 13-11  | 5 | 41   | 23   | 14-11 | 5 | 11   | 0    | 77-9 | 5    | 14   | 6    | 17-0 | 5   | 188  | 195  | 17-0 | 5 | 61   | 70   |   |   |   |     |      |
| 14-11  | 5 | 43   | 21   | 15-11 | 5 | -6   | 1    | 78-9 | 5    | 47   | 26   | 17-0 | 5   | 232  | 238  | 17-0 | 5 | 307  | 355  |   |   |   |     |      |
| 15-11  | 5 | 17   | 38   | 16-11 | 5 | 36   | 10   | 79-9 | 5    | 19   | 18   | 17-0 | 5   | 20   | 22   | 17-0 | 5 | 395  | 375  |   |   |   |     |      |
| 16-11  | 5 | 25   | 22   | 17-11 | 5 | 16   | 22   | 80-9 | 5    | -1   | 3    | 17-0 | 5   | 133  | 123  | 17-0 | 5 | 99   | 79   |   |   |   |     |      |
| -16-10 | 5 | -5   | 6    | 18-10 | 5 | 0    | 3    | 81-9 | 5    | -4   | 2    | 17-0 | 5   | 716  | 586  | 17-0 | 5 | 284  | 221  |   |   |   |     |      |
| -15-10 | 5 | 13   | 28   | 19-10 | 5 | 23   | 32   | 82-9 | 5    | 292  | 357  | 17-0 | 5   | 1161 | 1118 | 17-0 | 5 | 1111 | 1083 |   |   |   |     |      |
| -14-10 | 5 | 14   | 25   | 20-10 | 5 | 1    | 9    | 83-9 | 5    | 459  | 395  | 17-0 | 5   | 3138 | 2822 | 17-0 | 5 | -1   | 3    |   |   |   |     |      |
| -13-10 | 5 | 12   | 3    | 21-10 | 5 | 21   | 9    | 84-9 | 5    | 520  | 481  | 17-0 | 5   | 379  | 395  | 17-0 | 5 | 0    | 2    |   |   |   |     |      |
| -12-10 | 5 | 0    | 22   | 22-10 | 5 | 925  | 783  | 85-9 | 5    | 488  | 402  | 17-0 | 5   | 19   | 46   | 17-0 | 5 | 74   | 102  |   |   |   |     |      |
| -11-10 | 5 | 214  | 177  | 23-10 | 5 | 54   | 38   | 86-9 | 5    | 1817 | 1594 | 17-0 | 5   | 314  | 306  | 17-0 | 5 | 121  | 141  |   |   |   |     |      |
| -10-10 | 5 | 755  | 661  | 24-10 | 5 | 185  | 177  | 87-9 | 5    | 8384 | 8033 | 17-0 | 5   | 3405 | 3139 | 17-0 | 5 | 344  | 583  |   |   |   |     |      |
| -9-10  | 5 | 163  | 173  | 25-10 | 5 |      |      |      |      |      |      |      |     |      |      |      |   |      |      |   |   |   |     |      |

Table A.3, continued

| H   | K  | L | Obs | Calc | H   | K  | L | Obs | Calc | H   | K  | L | Obs  | Calc | H  | K   | L  | Obs  | Calc | H   | K   | L   | Obs | Calc | H   | K  | L | Obs | Calc |     |    |    |      |      |     |     |    |       |      |     |     |    |      |      |    |     |     |     |     |    |     |     |     |     |     |    |   |
|-----|----|---|-----|------|-----|----|---|-----|------|-----|----|---|------|------|----|-----|----|------|------|-----|-----|-----|-----|------|-----|----|---|-----|------|-----|----|----|------|------|-----|-----|----|-------|------|-----|-----|----|------|------|----|-----|-----|-----|-----|----|-----|-----|-----|-----|-----|----|---|
| -16 | -1 | 5 | 27  | 1    | -14 | 1  | 5 | 12  | 18   | -11 | 3  | 5 | 152  | 179  | -8 | 5   | 5  | 59   | 63   | -3  | 7   | 5   | 251 | 339  | -15 | -1 | 5 | 31  | 49   | -13 | 1  | 5  | 7    | 4    | -10 | 3   | 5  | 442   | 367  | -7  | 5   | 5  | 894  | 818  | -2 | 7   | 5   | 587 | 590 |    |     |     |     |     |     |    |   |
| -14 | -1 | 5 | 7   | 6    | -12 | 1  | 5 | 8   | 10   | -9  | 3  | 5 | 8    | 2    | -6 | 5   | 5  | 646  | 690  | -1  | 7   | 5   | 219 | 240  | -13 | -1 | 5 | 13  | 14   | -11 | 1  | 5  | 124  | 139  | -8  | 3   | 5  | 338   | 357  | -5  | 5   | 5  | 99   | 70   | 0  | 7   | 5   | -2  | 1   |    |     |     |     |     |     |    |   |
| -12 | -1 | 5 | 130 | 134  | -10 | 1  | 5 | 50  | 43   | -7  | 3  | 5 | 4683 | 4249 | -4 | 5   | 5  | 302  | 377  | 1   | 7   | 5   | 849 | 800  | -11 | -1 | 5 | 140 | 151  | -9  | 1  | 5  | 110  | 74   | -6  | 3   | 5  | 10518 | 9088 | -3  | 5   | 5  | 1005 | 1180 | 2  | 7   | 5   | 175 | 134 |    |     |     |     |     |     |    |   |
| -10 | -1 | 5 | 4   | 3    | -8  | 1  | 5 | 512 | 545  | -5  | 3  | 5 | 3232 | 3057 | -2 | 5   | 5  | 518  | 514  | 3   | 7   | 5   | 144 | 111  | -9  | -1 | 5 | 0   | 10   | -7  | 1  | 5  | 1037 | 1005 | -4  | 3   | 5  | 421   | 199  | -1  | 5   | 5  | 1365 | 1139 | 4  | 7   | 5   | 202 | 162 |    |     |     |     |     |     |    |   |
| -8  | -1 | 5 | 513 | 532  | -6  | 1  | 5 | 472 | 480  | -3  | 3  | 5 | 1010 | 936  | 0  | 3   | 5  | 19   | 35   | 5   | 7   | 5   | 316 | 321  | -7  | -1 | 5 | 241 | 181  | -5  | 1  | 5  | 96   | 132  | -2  | 3   | 5  | 1261  | 1405 | 1   | 5   | 5  | 3627 | 3643 | 6  | 7   | 5   | 214 | 179 |    |     |     |     |     |     |    |   |
| -6  | -1 | 5 | 344 | 358  | -4  | 1  | 5 | 697 | 757  | -1  | 3  | 5 | 21   | 12   | 2  | 5   | 5  | 717  | 679  | 7   | 7   | 5   | 11  | 5    | -5  | -1 | 5 | 506 | 568  | -3  | 1  | 5  | 2481 | 2501 | 0   | 3   | 5  | 157   | 237  | 3   | 5   | 5  | 9    | 6    | 8  | 7   | 5   | 22  | 13  |    |     |     |     |     |     |    |   |
| -4  | -1 | 5 | 267 | 364  | -2  | 1  | 5 | 173 | 230  | 1   | 3  | 5 | 3308 | 3187 | 4  | 5   | 5  | 1433 | 1432 | 9   | 7   | 5   | 182 | 212  | -3  | -1 | 5 | 17  | 11   | -1  | 1  | 5  | 3987 | 4822 | 2   | 3   | 5  | 197   | 173  | 5   | 5   | 5  | 858  | 884  | 10 | 7   | 5   | -3  | 0   |    |     |     |     |     |     |    |   |
| -2  | -1 | 5 | 3   | 5    | 0   | 1  | 5 | 431 | 400  | 3   | 3  | 5 | 875  | 948  | 6  | 5   | 5  | 709  | 708  | 11  | 7   | 5   | 28  | 28   | -1  | -1 | 5 | 397 | 592  | 1   | 1  | 5  | 39   | 42   | 4   | 3   | 5  | 1072  | 1140 | 7   | 5   | 5  | 37   | 35   | 12 | 7   | 5   | 3   | 10  |    |     |     |     |     |     |    |   |
| 0   | -1 | 5 | 155 | 134  | 2   | 1  | 5 | 2   | 2    | 5   | 3  | 5 | 34   | 56   | 8  | 5   | 5  | 210  | 237  | 13  | 7   | 5   | 2   | 4    | -16 | 0  | 5 | 59  | 39   | -7  | 10 | 5  | 240  | 187  | 8   | 12  | 5  | 10    | 21   | 0   | 16  | 5  | 0    | 10   | -1 | -15 | 6   | 1   | 1   |    |     |     |     |     |     |    |   |
| -15 | 0  | 5 | 59  | 39   | -7  | 10 | 5 | 240 | 187  | 8   | 12 | 5 | 10   | 21   | 0  | 16  | 5  | 0    | 10   | -1  | -15 | 6   | 1   | 1    | -15 | 0  | 5 | 5   | 59   | 39  | -7 | 10 | 5    | 240  | 187 | 8   | 12 | 5     | 10   | 21  | 0   | 16 | 5    | 0    | 10 | -1  | -15 | 6   | 1   | 1  |     |     |     |     |     |    |   |
| -14 | 0  | 5 | 5   | 5    | -7  | 1  | 5 | 151 | 118  | -13 | 13 | 5 | 25   | 4    | 1  | 16  | 5  | -11  | 1    | 0   | -15 | 6   | 4   | 6    | -14 | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 185  | 193 | -12 | 13 | 5     | 0    | 2   | 2   | 16 | 5    | 9    | 3  | 1   | -15 | 6   | 1   | 0  |     |     |     |     |     |    |   |
| -13 | 0  | 5 | 5   | 5    | -5  | 1  | 5 | 185 | 193  | -12 | 13 | 5 | 0    | 2    | 2  | 16  | 5  | 9    | 3    | 1   | -15 | 6   | 1   | 0    | -12 | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 12   | 7   | -11 | 13 | 5     | -8   | 2   | 3   | 16 | 5    | 5    | 8  | 2   | -15 | 6   | 5   | 12 |     |     |     |     |     |    |   |
| -12 | 0  | 5 | 5   | 5    | -4  | 1  | 5 | 12  | 7    | -11 | 13 | 5 | -8   | 2    | 3  | 16  | 5  | 5    | 8    | 2   | -15 | 6   | 5   | 12   | -11 | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 86   | 88  | -10 | 13 | 5     | 22   | 12  | 4   | 16 | 5    | -9   | 0  | 3   | -15 | 6   | 18  | 18 |     |     |     |     |     |    |   |
| -11 | 0  | 5 | 5   | 5    | -3  | 1  | 5 | 273 | 283  | -9  | 13 | 5 | 23   | 29   | 5  | 16  | 5  | 50   | 14   | 4   | -15 | 6   | 11  | 1    | -10 | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 217  | 150 | -1  | 10 | 5     | 155  | 151 | -8  | 13 | 5    | 7    | 10 | -5  | 17  | 5   | 21  | 14 | 5   | -15 | 6   | 13  | 10  |    |   |
| -10 | 0  | 5 | 5   | 5    | -2  | 1  | 5 | 155 | 151  | -8  | 13 | 5 | 7    | 10   | -5 | 17  | 5  | 21   | 14   | 4   | -15 | 6   | 11  | 1    | -9  | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 105  | 143 | 0   | 10 | 5     | 2    | 9   | -7  | 13 | 5    | 58   | 31 | -4  | 17  | 5   | -7  | 11 | 6   | -15 | 6   | 25  | 9   |    |   |
| -9  | 0  | 5 | 5   | 5    | -1  | 1  | 5 | 2   | 9    | -7  | 13 | 5 | 58   | 31   | -4 | 17  | 5  | -7   | 11   | 6   | -15 | 6   | 25  | 9    | -8  | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 602  | 498 | 1   | 10 | 5     | 885  | 723 | -6  | 13 | 5    | 34   | 59 | -3  | 17  | 5   | -17 | 1  | 7   | -15 | 6   | -4  | 5   |    |   |
| -8  | 0  | 5 | 5   | 5    | 0   | 1  | 5 | 124 | 109  | -5  | 13 | 5 | 1    | 16   | -2 | 17  | 5  | 57   | 7    | 8   | -15 | 6   | 0   | 3    | -7  | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 65   | 57  | 2   | 10 | 5     | 124  | 109 | -5  | 13 | 5    | 1    | 16 | -2  | 17  | 5   | 57  | 7  | 8   | -15 | 6   | 0   | 3   |    |   |
| -7  | 0  | 5 | 5   | 5    | 0   | 1  | 5 | 26  | 19   | -4  | 13 | 5 | -3   | 3    | -1 | 17  | 5  | -9   | 1    | 9   | -15 | 6   | 8   | 10   | -5  | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 108  | 119 | 3   | 10 | 5     | 26   | 19  | -4  | 13 | 5    | -3   | 3  | -1  | 17  | 5   | -9  | 1  | 9   | -15 | 6   | 8   | 10  |    |   |
| -6  | 0  | 5 | 5   | 5    | 0   | 1  | 5 | 184 | 144  | -3  | 13 | 5 | 6    | 6    | 1  | 0   | 17 | 5    | 8    | 0   | 10  | -15 | 6   | 6    | 6   | -4 | 0 | 5   | 5    | 5   | 5  | -9 | 1    | 5    | 266 | 301 | 4  | 10    | 5    | 184 | 144 | -3 | 13   | 5    | 6  | 6   | 1   | 0   | 17  | 5  | 8   | 0   | 10  | -15 | 6   | 6  | 6 |
| -5  | 0  | 5 | 5   | 5    | 0   | 1  | 5 | 239 | 217  | -2  | 13 | 5 | 36   | 37   | 1  | 17  | 5  | 35   | 4    | 11  | -15 | 6   | 1   | 0    | -3  | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 729  | 807 | 5   | 10 | 5     | 239  | 217 | -2  | 13 | 5    | 36   | 37 | 1   | 17  | 5   | 35  | 4  | 11  | -15 | 6   | 1   | 0   |    |   |
| -4  | 0  | 5 | 5   | 5    | 0   | 1  | 5 | 60  | 78   | -1  | 13 | 5 | 0    | 1    | 2  | 17  | 5  | 2    | 2    | 12  | -15 | 6   | -1  | 2    | -2  | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 617  | 519 | 6   | 10 | 5     | 60   | 78  | -1  | 13 | 5    | 0    | 1  | 2   | 17  | 5   | 2   | 2  | 12  | -15 | 6   | -1  | 2   |    |   |
| -3  | 0  | 5 | 5   | 5    | 0   | 1  | 5 | 44  | 38   | 0   | 13 | 5 | 16   | 18   | -2 | -17 | 5  | 23   | 0    | 13  | -15 | 6   | -10 | 2    | -2  | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 1112 | 927 | 7   | 10 | 5     | 44   | 38  | 0   | 13 | 5    | 16   | 18 | -2  | -17 | 5   | 23  | 0  | 13  | -15 | 6   | -10 | 2   |    |   |
| -2  | 0  | 5 | 5   | 5    | 0   | 1  | 5 | 109 | 111  | 1   | 13 | 5 | 36   | 42   | 0  | -18 | 5  | 37   | 0    | -18 | 5   | 37  | 0   | 67   | 43  | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 0    | 9   | 8   | 10 | 5     | 109  | 111 | 1   | 13 | 5    | 36   | 42 | 0   | -18 | 5   | 37  | 0  | -18 | 5   | 37  | 0   | 67  | 43 |   |
| -1  | 0  | 5 | 5   | 5    | 0   | 1  | 5 | 56  | 58   | 2   | 13 | 5 | 1    | 3    | 0  | -18 | 5  | 18   | 0    | -8  | -14 | 6   | 35  | 24   | -1  | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 220  | 232 | 9   | 10 | 5     | 56   | 58  | 2   | 13 | 5    | 1    | 3  | 0   | -18 | 5   | 18  | 0  | -8  | -14 | 6   | 35  | 24  |    |   |
| 0   | 0  | 5 | 5   | 5    | 0   | 1  | 5 | -4  | 3    | 3   | 13 | 5 | 7    | 14   | 1  | -18 | 5  | -7   | 5    | -7  | -14 | 6   | -6  | 0    | -2  | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 701  | 612 | 10  | 10 | 5     | -4   | 3   | 3   | 13 | 5    | 7    | 14 | 1   | -18 | 5   | -7  | 5  | -7  | -14 | 6   | -6  | 0   |    |   |
| 1   | 0  | 5 | 5   | 5    | 0   | 1  | 5 | 1   | 3    | 4   | 13 | 5 | 76   | 73   | 2  | -18 | 5  | 19   | 21   | -6  | -14 | 6   | 27  | 22   | 2   | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 86   | 109 | 11  | 10 | 5     | 1    | 3   | 4   | 13 | 5    | 76   | 73 | 2   | -18 | 5   | 19  | 21 | -6  | -14 | 6   | 27  | 22  |    |   |
| 2   | 0  | 5 | 5   | 5    | 0   | 1  | 5 | 44  | 26   | 5   | 13 | 5 | 8    | 3    | 3  | -18 | 5  | 24   | 33   | -5  | -14 | 6   | 5   | 1    | -15 | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 34   | 18  | -14 | 11 | 5     | 44   | 26  | 5   | 13 | 5    | 8    | 3  | 3   | -18 | 5   | 24  | 33 | -5  | -14 | 6   | 5   | 1   |    |   |
| 3   | 0  | 5 | 5   | 5    | 0   | 1  | 5 | -16 | 0    | 6   | 13 | 5 | -8   | 3    | 4  | -18 | 5  | 20   | 8    | -4  | -14 | 6   | 3   | 0    | -14 | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 483  | 455 | -13 | 11 | 5     | -16  | 0   | 6   | 13 | 5    | -8   | 3  | 4   | -18 | 5   | 20  | 8  | -4  | -14 | 6   | 3   | 0   |    |   |
| 4   | 0  | 5 | 5   | 5    | 0   | 1  | 5 | 25  | 33   | 7   | 13 | 5 | 35   | 13   | 5  | -18 | 5  | -7   | 1    | -3  | -14 | 6   | 113 | 132  | -6  | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 52   | 32  | -12 | 11 | 5     | 25   | 33  | 7   | 13 | 5    | 35   | 13 | 5   | -18 | 5   | -7  | 1  | -3  | -14 | 6   | 113 | 132 |    |   |
| 5   | 0  | 5 | 5   | 5    | 0   | 1  | 5 | 69  | 76   | -12 | 14 | 5 | 47   | 1    | 6  | -18 | 5  | 27   | 5    | -2  | -14 | 6   | 77  | 80   | -7  | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 58   | 66  | -11 | 11 | 5     | 69   | 76  | -12 | 14 | 5    | 47   | 1  | 6   | -18 | 5   | 27  | 5  | -2  | -14 | 6   | 77  | 80  |    |   |
| 6   | 0  | 5 | 5   | 5    | 0   | 1  | 5 | 92  | 69   | -11 | 14 | 5 | 25   | 3    | 7  | -18 | 5  | -2   | 2    | -1  | -14 | 6   | 37  | 28   | -8  | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 380  | 378 | -10 | 11 | 5     | 92   | 69  | -11 | 14 | 5    | 25   | 3  | 7   | -18 | 5   | -2  | 2  | -1  | -14 | 6   | 37  | 28  |    |   |
| 7   | 0  | 5 | 5   | 5    | 0   | 1  | 5 | -4  | 4    | -10 | 14 | 5 | 38   | 3    | 8  | -18 | 5  | 15   | 0    | 0   | -14 | 6   | 34  | 37   | -10 | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 166  | 166 | -9  | 11 | 5     | -4   | 4   | -10 | 14 | 5    | 38   | 3  | 8   | -18 | 5   | 15  | 0  | 0   | -14 | 6   | 34  | 37  |    |   |
| 8   | 0  | 5 | 5   | 5    | 0   | 1  | 5 | 168 | 136  | -9  | 14 | 5 | -6   | 0    | 0  | -18 | 5  | -4   | 0    | -14 | 6   | 122 | 121 | -11  | 0   | 5  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 166  | 166 | -9  | 11 | 5     | 168  | 136 | -9  | 14 | 5    | -6   | 0  | 0   | -18 | 5   | -4  | 0  | -14 | 6   | 122 | 121 |     |    |   |
| 9   | 0  | 5 | 5   | 5    | 0   | 1  | 5 | 95  | 122  | -8  | 14 | 5 | 4    | 16   | -4 | -17 | 5  | -13  | 8    | 2   | -14 | 6   | 71  | 53   | -12 | 0  | 5 | 5   | 5    | 5   | -9 | 1  | 5    | 166  | 174 | -7  | 11 | 5     | 95   | 122 | -8  | 14 | 5    | 4    | 16 | -4  | -17 | 5   | -13 | 8  | 2   | -14 | 6   | 71  | 53  |    |   |
| 10  | 0  | 5 | 5   | 5    | 0   | 1  | 5 | -5  | 1    | -7  | 14 | 5 |      |      |    |     |    |      |      |     |     |     |     |      |     |    |   |     |      |     |    |    |      |      |     |     |    |       |      |     |     |    |      |      |    |     |     |     |     |    |     |     |     |     |     |    |   |

Table A.3, continued

| M      | K | L   | Obe | Calc | M  | K | L    | Obe  | Calc | M  | K | L    | Obe  | Calc | M  | K | L    | Obe  | Calc | M  | K | L    | Obe  | Calc | M | K | L | Obe | Calc |
|--------|---|-----|-----|------|----|---|------|------|------|----|---|------|------|------|----|---|------|------|------|----|---|------|------|------|---|---|---|-----|------|
| 12-12  | 6 | 43  | 43  | -11  | -9 | 6 | 17   | 4    | -8   | -7 | 6 | 238  | 209  | -6   | -5 | 6 | 30   | 27   | -5   | -3 | 6 | 52   | 104  |      |   |   |   |     |      |
| 13-12  | 6 | 34  | 25  | -10  | -9 | 6 | 5    | 0    | -7   | -7 | 6 | 97   | 91   | -5   | -5 | 6 | 22   | 5    | -4   | -3 | 6 | 1429 | 1276 |      |   |   |   |     |      |
| 14-12  | 6 | 3   | 0   | -9   | -9 | 6 | 262  | 220  | -6   | -7 | 6 | 1056 | 951  | -4   | -5 | 6 | 687  | 740  | -3   | -3 | 6 | 3104 | 3410 |      |   |   |   |     |      |
| -13-11 | 6 | -11 | 3   | -8   | -9 | 6 | -1   | 1    | -5   | -7 | 6 | 331  | 293  | -3   | -3 | 6 | 361  | 338  | -2   | -3 | 6 | 1502 | 1449 |      |   |   |   |     |      |
| -12-11 | 6 | -7  | 1   | -7   | -9 | 6 | 11   | 7    | -4   | -7 | 6 | 819  | 869  | -2   | -5 | 6 | 1639 | 1490 | -1   | -3 | 6 | 1581 | 1458 |      |   |   |   |     |      |
| -11-11 | 6 | -3  | 9   | -6   | -9 | 6 | 580  | 553  | -3   | -7 | 6 | 59   | 59   | -1   | -8 | 6 | 553  | 534  | 0    | -3 | 6 | 1805 | 2452 |      |   |   |   |     |      |
| -10-11 | 6 | 16  | 54  | -5   | -9 | 6 | 98   | 109  | -2   | -7 | 6 | 234  | 228  | 0    | -5 | 6 | 48   | 9    | 0    | -3 | 6 | 284  | 326  |      |   |   |   |     |      |
| -9-11  | 6 | -4  | 2   | -4   | -9 | 6 | 1    | 16   | -1   | -7 | 6 | 393  | 344  | 1    | -5 | 6 | 1857 | 1751 | 2    | -3 | 6 | 944  | 1311 |      |   |   |   |     |      |
| -8-11  | 6 | 30  | 21  | -3   | -9 | 6 | 1262 | 1249 | 0    | -7 | 6 | 2341 | 2501 | 2    | -5 | 6 | 2373 | 2211 | 3    | -3 | 6 | 1100 | 1012 |      |   |   |   |     |      |
| -7-11  | 6 | 75  | 73  | -2   | -9 | 6 | 293  | 299  | 1    | -7 | 6 | 2358 | 2310 | 3    | -5 | 6 | 1560 | 1717 | 4    | -3 | 6 | 0    | 3    |      |   |   |   |     |      |
| -6-11  | 6 | 207 | 186 | -1   | -9 | 6 | 184  | 201  | 2    | -7 | 6 | 1336 | 1420 | 4    | -5 | 6 | 316  | 280  | 5    | -3 | 6 | 1811 | 2050 |      |   |   |   |     |      |
| -5-11  | 6 | 8   | 7   | 0    | -9 | 6 | 855  | 759  | 3    | -7 | 6 | 106  | 115  | 5    | -5 | 6 | 538  | 405  | 6    | -3 | 6 | 167  | 140  |      |   |   |   |     |      |
| -4-11  | 6 | 18  | 32  | 1    | -9 | 6 | 2257 | 2229 | 4    | -7 | 6 | 6    | 14   | 6    | -5 | 6 | 1131 | 1048 | 7    | -3 | 6 | 77   | 87   |      |   |   |   |     |      |
| -3-11  | 6 | 46  | 35  | 2    | -9 | 6 | 582  | 454  | 5    | -7 | 6 | 719  | 710  | 7    | -5 | 6 | 182  | 152  | 8    | -3 | 6 | 851  | 704  |      |   |   |   |     |      |
| -2-11  | 6 | 137 | 114 | 3    | -9 | 6 | 73   | 65   | 6    | -7 | 6 | 1530 | 1430 | 8    | -5 | 6 | 26   | 41   | 9    | -3 | 6 | 378  | 336  |      |   |   |   |     |      |
| -1-11  | 6 | 121 | 104 | 4    | -9 | 6 | 128  | 126  | 7    | -7 | 6 | 14   | 5    | 9    | -5 | 6 | 468  | 457  | 10   | -3 | 6 | 95   | 124  |      |   |   |   |     |      |
| 0-11   | 6 | -1  | 3   | 5    | -9 | 6 | 565  | 521  | 8    | -7 | 6 | 151  | 132  | 10   | -5 | 6 | 1179 | 1100 | 11   | -3 | 6 | 38   | 46   |      |   |   |   |     |      |
| 1-11   | 6 | 128 | 136 | 6    | -9 | 6 | 2    | 4    | 9    | -7 | 6 | 89   | 102  | 11   | -5 | 6 | 317  | 322  | 12   | -3 | 6 | 223  | 221  |      |   |   |   |     |      |
| 2-11   | 6 | 6   | 0   | 7    | -9 | 6 | 2    | 1    | 10   | -7 | 6 | 37   | 61   | 12   | -5 | 6 | 25   | 15   | 13   | -3 | 6 | 80   | 89   |      |   |   |   |     |      |
| 3-11   | 6 | 106 | 86  | 8    | -9 | 6 | 38   | 21   | 11   | -7 | 6 | -3   | 12   | 13   | -5 | 6 | 37   | 42   | 14   | -3 | 6 | -7   | 2    |      |   |   |   |     |      |
| 4-11   | 6 | 72  | 88  | 9    | -9 | 6 | 5    | 6    | 12   | -7 | 6 | 0    | 15   | 14   | -5 | 6 | 0    | 6    | 15   | -3 | 6 | 19   | 0    |      |   |   |   |     |      |
| 5-11   | 6 | 307 | 242 | 10   | -9 | 6 | 381  | 389  | 13   | -7 | 6 | 84   | 97   | 15   | -5 | 6 | 64   | 48   | -16  | -2 | 6 | 57   | 68   |      |   |   |   |     |      |
| 6-11   | 6 | 1   | 5   | 11   | -9 | 6 | 31   | 31   | 14   | -7 | 6 | 10   | 1    | -16  | -4 | 6 | 15   | 3    | -15  | -2 | 6 | -4   | 0    |      |   |   |   |     |      |
| 7-11   | 6 | 32  | 14  | 12   | -9 | 6 | 23   | 19   | 15   | -7 | 6 | 47   | 24   | -15  | -4 | 6 | -6   | 0    | -14  | -2 | 6 | 12   | 18   |      |   |   |   |     |      |
| 8-11   | 6 | 53  | 44  | 13   | -9 | 6 | 10   | 0    | -16  | -6 | 6 | -4   | 16   | -14  | -4 | 6 | 4    | 14   | -13  | -2 | 6 | 115  | 102  |      |   |   |   |     |      |
| 9-11   | 6 | -3  | 0   | 14   | -9 | 6 | 37   | 28   | -15  | -6 | 6 | 13   | 1    | -13  | -4 | 6 | 9    | 1    | -12  | -2 | 6 | 22   | 4    |      |   |   |   |     |      |
| 10-11  | 6 | 60  | 82  | 15   | -9 | 6 | 44   | 14   | -14  | -6 | 6 | 9    | 1    | -12  | -4 | 6 | 106  | 137  | -11  | -2 | 6 | 67   | 75   |      |   |   |   |     |      |
| 11-11  | 6 | 11  | 6   | -15  | -9 | 6 | -1   | 5    | -13  | -6 | 6 | 1    | 19   | -10  | -4 | 6 | -8   | 0    | -10  | -2 | 6 | 337  | 313  |      |   |   |   |     |      |
| 12-11  | 6 | -5  | 0   | -14  | -9 | 6 | 26   | 17   | -12  | -6 | 6 | 1    | 163  | -9   | -4 | 6 | 715  | 693  | -9   | -2 | 6 | 405  | 338  |      |   |   |   |     |      |
| 13-11  | 6 | 10  | 7   | -13  | -9 | 6 | 16   | 17   | -11  | -6 | 6 | 131  | 31   | -8   | -4 | 6 | -2   | 1    | -7   | -2 | 6 | 175  | 282  |      |   |   |   |     |      |
| 14-11  | 6 | 6   | 16  | -12  | -9 | 6 | 5    | 16   | -10  | -6 | 6 | 26   | 31   | -7   | -4 | 6 | 52   | 42   | -6   | -2 | 6 | 637  | 671  |      |   |   |   |     |      |
| 15-11  | 6 | 27  | 8   | -11  | -9 | 6 | 101  | 89   | -9   | -6 | 6 | 31   | 79   | -7   | -4 | 6 | 8    | 21   | -5   | -2 | 6 | 548  | 443  |      |   |   |   |     |      |
| -14-10 | 6 | 0   | 2   | -10  | -9 | 6 | 121  | 140  | -8   | -6 | 6 | 59   | 64   | -6   | -4 | 6 | 0    | 1    | -4   | -2 | 6 | 423  | 499  |      |   |   |   |     |      |
| -13-10 | 6 | 10  | 1   | -9   | -9 | 6 | 108  | 86   | -7   | -6 | 6 | 139  | 108  | -5   | -4 | 6 | 13   | 290  | -3   | -2 | 6 | 392  | 419  |      |   |   |   |     |      |
| -12-10 | 6 | 26  | 37  | -8   | -9 | 6 | 296  | 249  | -6   | -6 | 6 | 78   | 81   | -4   | -4 | 6 | 223  | 188  | -2   | -2 | 6 | 209  | 231  |      |   |   |   |     |      |
| -11-10 | 6 | 2   | 4   | -7   | -9 | 6 | 601  | 579  | -5   | -6 | 6 | 66   | 75   | -3   | -4 | 6 | 94   | 10   | -1   | -2 | 6 | 676  | 615  |      |   |   |   |     |      |
| -10-10 | 6 | 9   | 14  | -6   | -9 | 6 | 377  | 301  | -4   | -6 | 6 | 200  | 149  | -2   | -4 | 6 | 20   | 55   | 0    | -2 | 6 | 56   | 80   |      |   |   |   |     |      |
| -9-10  | 6 | 16  | 5   | -5   | -9 | 6 | 298  | 265  | -3   | -6 | 6 | 1601 | 1584 | -1   | -4 | 6 | 1422 | 1341 | 1    | -2 | 6 | 1698 | 1731 |      |   |   |   |     |      |
| -8-10  | 6 | 54  | -50 | -4   | -9 | 6 | 674  | 682  | -2   | -6 | 6 | 678  | 712  | 0    | -4 | 6 | 713  | 813  | 2    | -2 | 6 | 324  | 307  |      |   |   |   |     |      |
| -7-10  | 6 | 1   | 3   | -3   | -9 | 6 | 965  | 793  | -1   | -6 | 6 | 252  | 302  | 1    | -4 | 6 | 88   | 117  | 3    | -2 | 6 | 1904 | 1544 |      |   |   |   |     |      |
| -6-10  | 6 | 10  | 4   | -2   | -9 | 6 | 112  | 94   | 0    | -6 | 6 | 32   | 275  | 3    | -4 | 6 | 313  | 290  | 4    | -2 | 6 | 1067 | 1023 |      |   |   |   |     |      |
| -5-10  | 6 | 0   | 6   | -1   | -9 | 6 | 597  | 684  | 1    | -5 | 6 | 398  | 275  | 3    | -4 | 6 | 22   | 10   | 5    | -2 | 6 | 578  | 505  |      |   |   |   |     |      |
| -4-10  | 6 | 66  | 40  | 0    | -9 | 6 | 2236 | 2075 | 2    | -6 | 6 | 26   | 40   | 4    | -4 | 6 | 1993 | 2222 | 6    | -2 | 6 | 56   | 76   |      |   |   |   |     |      |
| -3-10  | 6 | 22  | 33  | 1    | -8 | 6 | 50   | 15   | 3    | -6 | 6 | 471  | 502  | 5    | -4 | 6 | 13   | 18   | 7    | -2 | 6 | -3   | 2    |      |   |   |   |     |      |
| -2-10  | 6 | 355 | 295 | 2    | -8 | 6 | 175  | 217  | 4    | -6 | 6 | 61   | 78   | 6    | -4 | 6 | 20   | 112  | -5   | 7  | 6 | 30   | 40   |      |   |   |   |     |      |
| -1-10  | 6 | 17  | 18  | 9    | 0  | 6 | 570  | 537  | 13   | 2  | 6 | 109  | 99   | -13  | 5  | 6 | 100  | 72   | -4   | 7  | 6 | 591  | 578  |      |   |   |   |     |      |
| 0-10   | 6 | 360 | 325 | 10   | 0  | 6 | 153  | 146  | 14   | 2  | 6 | 254  | 260  | -12  | 5  | 6 | 77   | 0    | -3   | 7  | 6 | 3    | 0    |      |   |   |   |     |      |
| 1-10   | 6 | 22  | 25  | 11   | 0  | 6 | 5    | 7    | -16  | 3  | 6 | 12   | 0    | -11  | 5  | 6 | 4    | 0    | -2   | 7  | 6 | 1    | 1    |      |   |   |   |     |      |
| 2-10   | 6 | 15  | 22  | 12   | 0  | 6 | 71   | 101  | -15  | 3  | 6 | 33   | 8    | -10  | 5  | 6 | 4    | 0    | -3   | 7  | 6 | 1525 | 1548 |      |   |   |   |     |      |
| 3-10   | 6 | 316 | 271 | 13   | 0  | 6 | 113  | 107  | -14  | 3  | 6 | 3    | 1    | -9   | 5  | 6 | -3   | 61   | -1   | 7  | 6 | 23   | 17   |      |   |   |   |     |      |
| 4-10   | 6 | 95  | 99  | 14   | 0  | 6 | 21   | 12   | -13  | 3  | 6 | 20   | 5    | -8   | 5  | 6 | 45   | 46   | 0    | 7  | 6 | 9    | 9    |      |   |   |   |     |      |
| 5-10   | 6 | 56  | 43  | -16  | 1  | 6 | 5    | 2    | -12  | 3  | 6 | 250  | 248  | -7   | 5  | 6 | 26   | 0    | 1    | 7  | 6 | 1091 | 1103 |      |   |   |   |     |      |
| 6-10   | 6 | 15  | 4   | -15  | 1  | 6 | 49   | 29   | -11  | 3  | 6 | 27   | 35   | -6   | 5  | 6 | 3    | 5    | 6    | 7  | 6 | 423  | 381  |      |   |   |   |     |      |
| 7-10   | 6 | -15 | 0   | -14  | 1  | 6 | 0    | 7    | -10  | 3  | 6 | 13   | 21   | -5   | 5  | 6 | 77   | 93   | 2    | 7  | 6 | 266  | 257  |      |   |   |   |     |      |
| 8-10   | 6 | -8  | 0   | -13  | 1  | 6 | 3    | 9    | -9   | 3  | 6 | 508  | 377  | -4   | 5  | 6 | 2104 | 1836 | 3    | 7  | 6 | 170  | 164  |      |   |   |   |     |      |
| 9-10   | 6 | 2   | 0   | -12  | 1  | 6 | 138  | 143  | -8   | 3  | 6 | 407  | 463  | -3   | 5  | 6 | 30   | 14   | 4    | 7  | 6 | 127  | 117  |      |   |   |   |     |      |
| -14-1  | 6 | 30  | 22  | -11  | 1  | 6 | 12   | 21   | -7   | 3  | 6 | 915  | 799  | -2   | 5  | 6 | 126  | 173  | 5    | 7  | 6 | 100  | 113  |      |   |   |   |     |      |
| -13-1  | 6 | 15  | 13  | -10  | 1  | 6 | 247  | 216  | -6   | 3  | 6 | 34   | 23   | -1   | 5  | 6 | 6    | 5    | 6    | 7  | 6 | 266  | 257  |      |   |   |   |     |      |
| -12-1  | 6 | 55  | 46  | -9   | 1  | 6 | 359  | 274  | -5   | 3  | 6 | 1015 | 849  | 0    | 5  | 6 | 222  | 210  | 7    | 7  | 6 | 170  | 164  |      |   |   |   |     |      |
| -11-1  | 6 | 345 | 268 | -8   | 1  | 6 | 8    | 4    | -4   | 3  | 6 | 155  | 116  | 1    | 5  | 6 | 59   | 49   | 8    | 7  | 6 | 127  | 117  |      |   |   |   |     |      |
| -10-1  | 6 | 777 | 781 | -7   | 1  | 6 | 50   | 50   | -3   | 3  | 6 | 9    | 11   | 2    | 5  | 6 | 215  | 230  | 9    | 7  | 6 | 100  | 113  |      |   |   |   |     |      |
| -9-1   | 6 | 554 | 494 | -6   | 1  | 6 | 2788 | 2463 | -2   | 3  | 6 | 2097 | 1818 | 3    | 5  | 6 | 327  | 368  | 10   | 7  | 6 | 25   | 41   |      |   |   |   |     |      |
| -8-1   | 6 | 141 | 155 | -5   | 1  | 6 | 32   | 25   | -1   | 3  | 6 | 4    | 3    | 4    | 5  | 6 | 12   | 13   | 11   | 7  | 6 | -11  | 0    |      |   |   |   |     |      |
| -7-1   | 6 | 338 | 328 | -4   | 1  | 6 | 55   | 67   | 0    | 3  | 6 | 229  |      |      |    |   |      |      |      |    |   |      |      |      |   |   |   |     |      |

Table A.3, continued

| H    | K  | L | Obs  | Calc | H   | K  | L | Obs  | Calc | H   | K  | L | Obs | Calc | H      | K | L | Obs  | Calc | H      | K | L | Obs  | Calc |
|------|----|---|------|------|-----|----|---|------|------|-----|----|---|-----|------|--------|---|---|------|------|--------|---|---|------|------|
| 2    | 0  | 6 | 5469 | 5651 | 6   | 2  | 6 | 1092 | 1006 | 11  | 4  | 6 | 133 | 123  | -13    | 7 | 6 | 4    | 3    | -3     | 9 | 6 | 130  | 139  |
| 3    | 0  | 6 | 4596 | 4536 | 7   | 2  | 6 | 103  | 114  | 12  | 4  | 6 | 17  | 3    | -12    | 7 | 6 | 5    | 1    | -2     | 9 | 6 | 23   | 30   |
| 4    | 0  | 6 | 5    | 18   | 8   | 2  | 6 | 32   | 24   | 13  | 4  | 6 | -5  | 10   | -11    | 7 | 6 | 237  | 181  | -1     | 9 | 6 | 309  | 253  |
| 5    | 0  | 6 | 182  | 177  | 9   | 2  | 6 | 117  | 130  | -17 | 5  | 6 | 41  | 1    | -10    | 7 | 6 | 34   | 55   | 0      | 9 | 6 | 24   | 25   |
| 6    | 0  | 6 | 1954 | 1873 | 10  | 2  | 6 | 362  | 319  | -16 | 5  | 6 | 8   | 2    | -9     | 7 | 6 | 340  | 291  | 1      | 9 | 6 | 188  | 138  |
| 7    | 0  | 6 | 4    | 5    | 11  | 2  | 6 | 44   | 66   | -15 | 5  | 6 | 37  | 50   | -8     | 7 | 6 | 48   | 54   | 2      | 9 | 6 | 107  | 91   |
| 8    | 0  | 6 | 52   | 49   | 12  | 2  | 6 | 26   | 12   | -14 | 5  | 6 | -1  | 1    | -7     | 7 | 6 | 1215 | 1236 | 3      | 9 | 6 | 206  | 223  |
| 9    | 0  | 6 | 228  | 222  | -5  | 12 | 6 | 14   | 3    | 6   | 15 | 6 | 2   | 25   | -1-15  | 7 | 6 | 15   | 12   | -5-12  | 7 | 6 | -3   | 4    |
| 5    | 9  | 6 | 239  | 237  | -4  | 12 | 6 | 13   | 14   | -7  | 16 | 8 | 23  | 1    | 0-15   | 7 | 6 | 1    | 1    | -4-12  | 7 | 6 | 170  | 160  |
| 6    | 9  | 6 | 11   | 13   | -3  | 12 | 6 | 14   | 4    | -6  | 16 | 6 | 24  | 9    | 1-15   | 7 | 6 | 8    | 1    | -3-12  | 7 | 6 | 56   | 78   |
| 7    | 9  | 6 | 71   | 68   | -2  | 12 | 6 | 27   | 25   | -5  | 16 | 6 | 34  | 22   | 2-15   | 7 | 6 | 14   | 2    | -2-12  | 7 | 6 | 5    | 0    |
| 8    | 9  | 6 | 179  | 163  | -1  | 12 | 6 | 18   | 24   | -4  | 16 | 6 | -3  | 5    | 3-15   | 7 | 6 | -3   | 0    | -1-12  | 7 | 6 | 90   | 77   |
| 9    | 9  | 6 | 8    | 10   | 0   | 12 | 6 | 19   | 9    | -3  | 16 | 6 | 44  | 17   | 4-15   | 7 | 6 | 2    | 9    | 0-12   | 7 | 6 | 94   | 85   |
| 10   | 9  | 6 | -7   | 2    | 1   | 12 | 6 | 0    | 1    | -2  | 16 | 6 | -10 | 12   | 5-15   | 7 | 6 | -4   | 0    | 1-12   | 7 | 6 | 338  | 321  |
| 11   | 9  | 6 | 47   | 6    | 2   | 12 | 6 | 9    | 13   | -1  | 16 | 6 | 47  | 14   | 6-15   | 7 | 6 | 16   | 0    | 2-12   | 7 | 6 | 27   | 17   |
| -15  | 10 | 6 | -18  | 22   | 3   | 12 | 6 | -4   | 1    | 0   | 16 | 6 | 39  | 2    | 7-15   | 7 | 6 | 13   | 0    | 3-12   | 7 | 6 | 4    | 3    |
| -14  | 10 | 6 | 16   | 22   | 4   | 12 | 6 | 55   | 80   | 1   | 16 | 6 | 53  | 8    | 8-15   | 7 | 6 | 4    | 0    | 4-12   | 7 | 6 | 6    | 1    |
| -13  | 10 | 6 | 6    | 3    | 5   | 12 | 6 | -6   | 2    | 2   | 16 | 6 | -1  | 14   | 9-15   | 7 | 6 | -1   | 0    | 5-12   | 7 | 6 | 41   | 49   |
| -12  | 10 | 6 | 27   | 35   | 6   | 12 | 6 | 81   | 32   | 3   | 16 | 6 | -17 | 1    | 10-15  | 7 | 6 | -2   | 1    | 6-12   | 7 | 6 | 89   | 85   |
| -11  | 10 | 6 | 62   | 67   | 7   | 12 | 6 | 13   | 8    | 4   | 16 | 6 | -21 | 9    | 11-15  | 7 | 6 | -3   | 2    | 7-12   | 7 | 6 | 97   | 90   |
| -10  | 10 | 6 | 50   | 37   | 8   | 12 | 6 | 20   | 8    | -3  | 17 | 6 | -19 | 3    | 12-15  | 7 | 6 | -4   | 1    | 8-12   | 7 | 6 | 13   | 4    |
| -9   | 10 | 6 | 9    | 7    | -12 | 13 | 6 | 28   | 15   | -2  | 17 | 6 | -18 | 0    | 13-15  | 7 | 6 | 3    | 3    | 9-12   | 7 | 6 | 9    | 14   |
| -8   | 10 | 6 | 231  | 212  | -11 | 13 | 6 | -3   | 2    | -1  | 17 | 6 | -10 | 4    | -7-14  | 7 | 6 | 15   | 14   | 10-12  | 7 | 6 | 147  | 122  |
| -7   | 10 | 6 | 88   | 74   | -10 | 13 | 6 | 7    | 0    | 0   | 17 | 6 | -6  | 13   | -6-14  | 7 | 6 | 4    | 6    | 11-12  | 7 | 6 | 0    | 2    |
| -6   | 10 | 6 | 4    | 1    | -9  | 13 | 6 | 49   | 30   | -2  | 18 | 7 | 18  | 2    | -5-14  | 7 | 6 | -3   | 6    | 12-12  | 7 | 6 | 6    | 0    |
| -5   | 10 | 6 | -3   | 1    | -8  | 13 | 6 | 1    | 22   | -1  | 18 | 7 | -15 | 0    | -4-14  | 7 | 6 | 4    | 1    | 13-12  | 7 | 6 | 8    | 14   |
| -4   | 10 | 6 | 90   | 95   | -7  | 13 | 6 | -1   | 0    | 0   | 18 | 7 | -5  | 3    | -3-14  | 7 | 6 | 2    | 4    | 14-12  | 7 | 6 | 5    | 8    |
| -3   | 10 | 6 | 63   | 67   | -6  | 13 | 6 | -3   | 2    | 1   | 18 | 7 | -11 | 6    | -2-14  | 7 | 6 | 1    | 7    | -12-11 | 7 | 6 | 11   | 23   |
| -2   | 10 | 6 | 25   | 22   | -5  | 13 | 6 | -6   | 10   | 2   | 18 | 7 | 3   | 3    | -1-14  | 7 | 6 | 12   | 14   | -11-11 | 7 | 6 | 2    | 4    |
| -1   | 10 | 6 | 228  | 197  | -4  | 13 | 6 | 30   | 27   | 3   | 18 | 7 | 9   | 1    | 0-14   | 7 | 6 | 9    | 10   | -10-11 | 7 | 6 | -5   | 8    |
| 0    | 10 | 6 | 337  | 329  | -3  | 13 | 6 | -4   | 7    | 4   | 18 | 7 | 31  | 9    | 1-14   | 7 | 6 | 29   | 34   | -9-11  | 7 | 6 | 0    | 0    |
| 1    | 10 | 6 | 191  | 165  | -2  | 13 | 6 | 17   | 15   | 5   | 18 | 7 | -6  | 11   | 2-14   | 7 | 6 | 52   | 47   | -8-11  | 7 | 6 | 43   | 36   |
| 2    | 10 | 6 | 406  | 392  | -1  | 13 | 6 | 35   | 38   | 6   | 18 | 7 | -14 | 1    | 3-14   | 7 | 6 | 13   | 8    | -7-11  | 7 | 6 | 0    | 0    |
| 3    | 10 | 6 | 4    | 10   | 0   | 13 | 6 | 10   | 3    | 7   | 18 | 7 | 34  | 1    | 4-14   | 7 | 6 | 3    | 5    | -6-11  | 7 | 6 | 71   | 71   |
| 4    | 10 | 6 | 135  | 115  | 1   | 13 | 6 | 39   | 43   | 8   | 18 | 7 | 9   | 0    | 5-14   | 7 | 6 | -4   | 1    | -5-11  | 7 | 6 | 53   | 47   |
| 5    | 10 | 6 | 43   | 41   | 2   | 13 | 6 | 33   | 46   | 9   | 18 | 7 | 0   | 0    | 6-14   | 7 | 6 | 2    | 6    | -4-11  | 7 | 6 | 5    | 8    |
| 6    | 10 | 6 | 190  | 197  | 3   | 13 | 6 | 30   | 27   | -3  | 17 | 7 | 14  | 9    | 7-14   | 7 | 6 | 9    | 0    | -3-11  | 7 | 6 | 5    | 8    |
| 7    | 10 | 6 | 141  | 122  | 4   | 13 | 6 | 6    | 0    | -2  | 17 | 7 | -8  | 2    | 8-14   | 7 | 6 | 8    | 7    | -2-11  | 7 | 6 | 22   | 17   |
| 8    | 10 | 6 | 26   | 29   | 5   | 13 | 6 | 51   | 27   | -1  | 17 | 7 | 33  | 8    | 9-14   | 7 | 6 | 13   | 8    | -1-11  | 7 | 6 | 93   | 71   |
| 9    | 10 | 6 | 29   | 18   | 6   | 13 | 6 | 26   | 26   | 0   | 17 | 7 | -2  | 4    | 10-14  | 7 | 6 | 6    | 13   | 0-11   | 7 | 6 | 118  | 90   |
| 10   | 10 | 6 | -10  | 5    | -11 | 14 | 6 | 8    | 0    | 1   | 17 | 7 | 3   | 4    | 11-14  | 7 | 6 | 2    | 1    | 1-11   | 7 | 6 | 337  | 347  |
| -14  | 11 | 6 | 5    | 12   | -10 | 14 | 6 | 21   | 9    | 2   | 17 | 7 | 3   | 2    | 12-14  | 7 | 6 | -6   | 7    | 2-11   | 7 | 6 | 616  | 565  |
| -13  | 11 | 6 | 1    | 18   | -9  | 14 | 6 | 12   | 22   | 3   | 17 | 7 | 1   | 5    | 13-14  | 7 | 6 | -5   | 8    | 3-11   | 7 | 6 | 1    | 2    |
| -12  | 11 | 6 | 2    | 6    | -8  | 14 | 6 | -10  | 0    | 4   | 17 | 7 | 5   | 2    | -10-13 | 7 | 6 | -7   | 0    | 4-11   | 7 | 6 | 51   | 50   |
| -11  | 11 | 6 | 18   | 4    | -7  | 14 | 6 | 4    | 4    | 4   | 17 | 7 | -7  | 4    | 9-13   | 7 | 6 | 23   | 13   | 5-11   | 7 | 6 | 336  | 288  |
| -10  | 11 | 6 | -5   | 18   | -6  | 14 | 6 | -6   | 8    | 6   | 17 | 7 | 30  | 14   | -8-13  | 7 | 6 | 7    | 0    | 6-11   | 7 | 6 | 136  | 139  |
| -9   | 11 | 6 | 96   | 91   | -5  | 14 | 6 | 38   | 32   | 7   | 17 | 7 | 23  | 5    | -7-13  | 7 | 6 | 9    | 42   | 7-11   | 7 | 6 | 3    | 11   |
| -8   | 11 | 6 | 2    | 9    | -4  | 14 | 6 | 6    | 15   | 8   | 17 | 7 | 1   | 0    | -6-13  | 7 | 6 | 62   | 42   | 8-11   | 7 | 6 | 11   | 27   |
| -7   | 11 | 6 | 34   | 13   | -3  | 14 | 6 | 36   | 16   | 9   | 17 | 7 | 16  | 1    | -5-13  | 7 | 6 | 55   | 43   | 9-11   | 7 | 6 | 227  | 234  |
| -6   | 11 | 6 | 23   | 26   | -2  | 14 | 6 | 10   | 15   | 10  | 17 | 7 | 0   | 5    | -4-13  | 7 | 6 | 0    | 2    | 10-11  | 7 | 6 | 13   | 3    |
| -5   | 11 | 6 | 18   | 12   | -1  | 14 | 6 | 13   | 2    | 11  | 17 | 7 | -3  | 1    | -3-13  | 7 | 6 | 46   | 43   | 11-11  | 7 | 6 | 18   | 46   |
| -4   | 11 | 6 | -2   | 1    | 0   | 14 | 6 | 60   | 64   | -4  | 16 | 7 | -5  | 2    | -2-13  | 7 | 6 | 224  | 190  | 12-11  | 7 | 6 | 38   | 23   |
| -3   | 11 | 6 | 105  | 90   | 1   | 14 | 6 | 77   | 43   | -3  | 16 | 7 | -1  | 4    | -1-13  | 7 | 6 | 0    | 3    | 13-11  | 7 | 6 | 21   | 23   |
| -2   | 11 | 6 | 178  | 149  | 2   | 14 | 6 | 56   | 35   | -2  | 16 | 7 | 19  | 13   | 0-13   | 7 | 6 | 25   | 21   | 14-11  | 7 | 6 | 7    | 1    |
| -1   | 11 | 6 | 61   | 46   | 3   | 14 | 6 | 19   | 3    | -1  | 16 | 7 | -3  | 1    | 1-13   | 7 | 6 | 159  | 132  | -13-10 | 7 | 6 | -8   | 9    |
| 0    | 11 | 6 | 0    | 3    | 4   | 14 | 6 | 15   | 8    | 0   | 16 | 7 | 9   | 13   | 2-13   | 7 | 6 | 49   | 60   | -12-10 | 7 | 6 | 1    | 1    |
| 1    | 11 | 6 | 86   | 99   | 6   | 14 | 6 | 32   | 4    | 1   | 16 | 7 | 12  | 6    | 3-13   | 7 | 6 | 30   | 15   | -11-10 | 7 | 6 | 20   | 0    |
| 2    | 11 | 6 | 3    | 4    | -10 | 15 | 6 | 2    | 3    | 2   | 16 | 7 | 12  | 3    | 4-13   | 7 | 6 | 0    | 1    | -10-10 | 7 | 6 | 82   | 75   |
| 3    | 11 | 6 | 51   | 40   | -9  | 15 | 6 | 36   | 18   | 3   | 16 | 7 | -3  | 0    | 5-13   | 7 | 6 | 40   | 30   | -9-10  | 7 | 6 | 75   | 84   |
| 4    | 11 | 6 | 6    | 1    | -8  | 15 | 6 | 17   | 40   | 4   | 16 | 7 | 17  | 2    | 6-13   | 7 | 6 | 24   | 12   | -8-10  | 7 | 6 | 25   | 22   |
| 5    | 11 | 6 | 152  | 173  | -7  | 15 | 6 | 0    | 28   | 5   | 16 | 7 | -4  | 11   | 7-13   | 7 | 6 | 3    | 0    | -7-10  | 7 | 6 | 173  | 174  |
| 6    | 11 | 6 | 19   | 3    | -6  | 15 | 6 | -3   | 4    | 6   | 16 | 7 | -4  | 0    | 8-13   | 7 | 6 | 15   | 13   | -6-10  | 7 | 6 | 62   | 52   |
| 7    | 11 | 6 | 15   | 5    | -5  | 15 | 6 | 18   | 8    | 7   | 16 | 7 | 4   | 3    | 9-13   | 7 | 6 | 5    | 9    | -5-10  | 7 | 6 | 98   | 81   |
| 8    | 11 | 6 | 43   | 13   | -4  | 15 | 6 | 80   | 59   | 8   | 16 | 7 | -4  | 6    | 10-13  | 7 | 6 | -5   | 0    | -4-10  | 7 | 6 | -1   | 2    |
| 9    | 11 | 6 | 1    | 8    | -3  | 15 | 6 | -7   | 0    | 9   | 16 | 7 | -4  | 3    | 11-13  | 7 | 6 | 8    | 12   | -3-10  | 7 | 6 | 42   | 46   |
| -13  | 12 | 6 | -4   | 0    | -2  | 15 | 6 | 9    | 21   | 10  | 16 | 7 | -2  | 1    | 12-13  | 7 | 6 | 20   | 5    | -2-10  | 7 | 6 | 34   | 32   |
| -12  | 12 | 6 | -9   | 8    | -1  | 15 | 6 | 36   | 41   | 11  | 16 | 7 | -1  | 3    | 13-13  | 7 | 6 | -9   | 4    | -1-10  | 7 | 6 | 83   | 53   |
| -11  | 12 | 6 | 37   | 14   | 0   | 15 | 6 | 7    | 22   | 12  | 16 | 7 | 22  | 5    | -11-12 | 7 | 6 | 19   | 2    | 0-10   | 7 | 6 | 628  | 648  |
| -10  | 12 | 6 | 15   | 15   | 1   | 15 | 6 | 13   | 1    | -6  | 15 | 7 | 6   | 0    | -10-12 | 7 | 6 | 1    | 6    | 1-10   | 7 | 6 | 1013 | 859  |
| -9   | 12 | 6 | -3   | 9    | 2   | 15 | 6 | 31   | 9    | -5  | 15 | 7 | 6   | 0    | -9-12  | 7 | 6 | 2    | 5    | 2-10   | 7 | 6 | 43   | 61   |
| -8   | 12 | 6 | 35   | 21   | 3   | 15 | 6 | 16   | 30   | -4  | 15 | 7 | 25  | 31   | -8-12  | 7 | 6 | 4    | 3    | 3-10   | 7 | 6 | 21   | 9    |
| -7</ |    |   |      |      |     |    |   |      |      |     |    |   |     |      |        |   |   |      |      |        |   |   |      |      |



Table A.3, continued

| M   | K  | L | Obs  | Calc | M   | K  | L | Obs  | Calc | M   | K  | L | Obs  | Calc | M   | K  | L | Obs  | Calc | M   | K  | L | Obs  | Calc | M | K | L | Obs | Calc |
|-----|----|---|------|------|-----|----|---|------|------|-----|----|---|------|------|-----|----|---|------|------|-----|----|---|------|------|---|---|---|-----|------|
| 8   | -9 | 7 | 10   | 6    | 12  | -7 | 7 | 3    | 9    | 14  | -5 | 7 | 82   | 96   | -17 | -2 | 7 | 21   | 1    | -15 | 0  | 7 | -8   | 0    |   |   |   |     |      |
| 9   | -9 | 7 | 22   | 21   | 13  | -7 | 7 | 8    | 24   | 15  | -5 | 7 | 8    | 5    | -16 | -2 | 7 | -8   | 2    | -14 | 0  | 7 | 38   | 54   |   |   |   |     |      |
| 10  | -9 | 7 | 7    | 6    | 14  | -7 | 7 | 18   | 37   | -16 | -4 | 7 | 11   | 1    | -15 | -2 | 7 | 16   | 20   | -13 | 0  | 7 | 143  | 107  |   |   |   |     |      |
| 11  | -9 | 7 | 1    | 19   | 15  | -7 | 7 | 1    | 2    | -15 | -4 | 7 | 30   | 25   | -14 | -2 | 7 | 17   | 19   | -12 | 0  | 7 | 212  | 220  |   |   |   |     |      |
| 12  | -9 | 7 | 2    | 4    | -16 | -6 | 7 | 30   | 12   | -14 | -4 | 7 | 110  | 68   | -13 | -2 | 7 | 1    | 14   | -11 | 0  | 7 | 30   | 20   |   |   |   |     |      |
| 13  | -9 | 7 | 35   | 51   | -15 | -6 | 7 | 15   | 1    | -13 | -4 | 7 | 7    | 0    | -12 | -2 | 7 | -8   | 2    | -10 | 0  | 7 | 325  | 259  |   |   |   |     |      |
| 14  | -9 | 7 | 15   | 14   | -14 | -6 | 7 | -3   | 1    | -12 | -4 | 7 | 104  | 120  | -11 | -2 | 7 | 47   | 55   | -9  | 0  | 7 | 156  | 113  |   |   |   |     |      |
| -15 | -9 | 7 | -10  | 11   | -13 | -6 | 7 | 14   | 11   | -11 | -4 | 7 | 239  | 199  | -10 | -2 | 7 | 724  | 657  | -8  | 0  | 7 | 8    | 11   |   |   |   |     |      |
| -14 | -9 | 7 | -8   | 0    | -12 | -6 | 7 | 43   | 39   | -10 | -4 | 7 | 45   | 57   | -9  | -2 | 7 | 35   | 35   | -7  | 0  | 7 | 139  | 203  |   |   |   |     |      |
| -13 | -9 | 7 | 64   | 52   | -11 | -6 | 7 | 115  | 95   | -9  | -4 | 7 | 10   | 11   | -8  | -2 | 7 | 119  | 104  | -6  | 0  | 7 | 18   | 43   |   |   |   |     |      |
| -12 | -9 | 7 | 38   | 26   | -10 | -6 | 7 | 4    | 2    | -8  | -4 | 7 | 218  | 186  | -7  | -2 | 7 | 1726 | 1660 | -5  | 0  | 7 | 461  | 692  |   |   |   |     |      |
| -11 | -9 | 7 | 2    | 6    | -9  | -6 | 7 | 113  | 83   | -7  | -4 | 7 | 521  | 512  | -6  | -2 | 7 | 275  | 267  | -4  | 0  | 7 | 681  | 511  |   |   |   |     |      |
| -10 | -9 | 7 | 92   | 58   | -8  | -6 | 7 | 434  | 412  | -6  | -4 | 7 | 478  | 460  | -5  | -2 | 7 | 12   | 1    | -3  | 0  | 7 | 2969 | 3208 |   |   |   |     |      |
| -9  | -9 | 7 | 88   | 84   | -7  | -6 | 7 | 4    | 0    | -5  | -4 | 7 | 49   | 47   | -4  | -2 | 7 | 1537 | 1652 | -2  | 0  | 7 | -2   | 1    |   |   |   |     |      |
| -8  | -9 | 7 | 421  | 387  | -6  | -6 | 7 | 141  | 111  | -4  | -4 | 7 | 741  | 615  | -3  | -2 | 7 | 365  | 305  | -1  | 0  | 7 | 407  | 390  |   |   |   |     |      |
| -7  | -9 | 7 | 13   | 11   | -5  | -6 | 7 | 34   | 27   | -3  | -4 | 7 | 679  | 617  | -2  | -2 | 7 | 372  | 431  | 0   | 0  | 7 | 4779 | 4600 |   |   |   |     |      |
| -6  | -9 | 7 | 17   | 6    | -4  | -6 | 7 | 393  | 369  | -2  | -4 | 7 | 32   | 37   | -1  | -2 | 7 | 937  | 1266 | 1   | 0  | 7 | 5431 | 4754 |   |   |   |     |      |
| -5  | -9 | 7 | 19   | 16   | -3  | -6 | 7 | 28   | 24   | -1  | -4 | 7 | 1132 | 1297 | 0   | -2 | 7 | 93   | 67   | 2   | 0  | 7 | 62   | 96   |   |   |   |     |      |
| -4  | -9 | 7 | 276  | 295  | -2  | -6 | 7 | 1124 | 1280 | 0   | -8 | 7 | 1341 | 1186 | 1   | -2 | 7 | 86   | 181  | 3   | 0  | 7 | 313  | 454  |   |   |   |     |      |
| -3  | -9 | 7 | 320  | 356  | -1  | -6 | 7 | 423  | 380  | 1   | -4 | 7 | 17   | 11   | 2   | -2 | 7 | 278  | 343  | 4   | 0  | 7 | 44   | 41   |   |   |   |     |      |
| -2  | -9 | 7 | 341  | 306  | 0   | -6 | 7 | 64   | 61   | 2   | -4 | 7 | 731  | 934  | 3   | -2 | 7 | 19   | 19   | 5   | 0  | 7 | 10   | 1    |   |   |   |     |      |
| -1  | -9 | 7 | 31   | 38   | 1   | -6 | 7 | 451  | 422  | 3   | -4 | 7 | 896  | 836  | 4   | -2 | 7 | 87   | 238  | 6   | 0  | 7 | 349  | 410  |   |   |   |     |      |
| 0   | -9 | 7 | 140  | 172  | 2   | -6 | 7 | 104  | 123  | 4   | -4 | 7 | 1484 | 1585 | 5   | -2 | 7 | 57   | 69   | 7   | 0  | 7 | 57   | 34   |   |   |   |     |      |
| 1   | -9 | 7 | 747  | 670  | 3   | -6 | 7 | 133  | 118  | 5   | -4 | 7 | 2529 | 2560 | 6   | -2 | 7 | 106  | 81   | 8   | 0  | 7 | 99   | 117  |   |   |   |     |      |
| 2   | -9 | 7 | 275  | 318  | 4   | -6 | 7 | -1   | 0    | 6   | -4 | 7 | 248  | 215  | 7   | -2 | 7 | 1036 | 992  | 9   | 0  | 7 | 239  | 215  |   |   |   |     |      |
| 3   | -9 | 7 | 8    | 0    | 5   | -6 | 7 | 1075 | 1156 | 7   | -4 | 7 | 670  | 631  | 8   | -2 | 7 | 90   | 60   | 10  | 0  | 7 | 160  | 144  |   |   |   |     |      |
| 4   | -9 | 7 | 307  | 298  | 6   | -6 | 7 | 400  | 410  | 8   | -4 | 7 | 44   | 54   | 9   | -2 | 7 | 109  | 61   | 11  | 0  | 7 | 89   | 102  |   |   |   |     |      |
| 5   | -9 | 7 | 877  | 813  | 7   | -6 | 7 | 24   | 29   | 9   | -4 | 7 | 263  | 269  | 10  | -2 | 7 | 169  | 182  | 12  | 0  | 7 | 26   | 23   |   |   |   |     |      |
| 6   | -9 | 7 | 556  | 560  | 8   | -6 | 7 | 653  | 641  | 10  | -4 | 7 | 424  | 369  | 11  | -2 | 7 | 34   | 30   | 13  | 0  | 7 | 62   | 81   |   |   |   |     |      |
| 7   | -9 | 7 | 99   | 91   | 9   | -6 | 7 | 450  | 409  | 11  | -4 | 7 | 19   | 12   | 12  | -2 | 7 | 2    | 1    | 14  | 0  | 7 | 3    | 0    |   |   |   |     |      |
| 8   | -9 | 7 | 57   | 63   | 10  | -6 | 7 | 397  | 352  | 12  | -4 | 7 | 57   | 62   | 13  | -2 | 7 | 114  | 111  | -16 | 1  | 7 | 5    | 45   |   |   |   |     |      |
| 9   | -9 | 7 | 15   | 18   | 11  | -6 | 7 | 0    | 11   | 13  | -4 | 7 | 329  | 287  | 14  | -2 | 7 | 6    | 47   | -14 | 1  | 7 | 63   | 45   |   |   |   |     |      |
| 10  | -9 | 7 | 14   | 6    | 12  | -6 | 7 | 30   | 26   | 14  | -4 | 7 | 18   | 23   | 15  | -2 | 7 | 60   | 47   | -14 | 1  | 7 | 33   | 19   |   |   |   |     |      |
| 11  | -9 | 7 | 6    | 10   | 13  | -6 | 7 | 96   | 67   | 15  | -4 | 7 | 41   | 0    | -17 | -1 | 7 | -11  | 1    | -13 | 1  | 7 | 6    | 21   |   |   |   |     |      |
| 12  | -9 | 7 | 17   | 5    | 14  | -6 | 7 | 0    | 0    | -16 | -3 | 7 | 34   | 3    | -16 | -1 | 7 | 9    | 10   | -12 | 1  | 7 | 46   | 46   |   |   |   |     |      |
| -13 | -9 | 7 | 286  | 324  | -6  | 3  | 7 | 1275 | 1134 | 1   | 5  | 7 | 481  | 518  | 8   | 7  | 7 | 80   | 83   | -5  | 10 | 7 | 19   | 6    |   |   |   |     |      |
| -10 | -9 | 7 | 30   | 5    | -5  | 3  | 7 | 41   | 25   | 1   | 5  | 7 | 2309 | 2022 | 9   | 7  | 7 | 51   | 81   | -4  | 10 | 7 | 91   | 76   |   |   |   |     |      |
| -9  | -9 | 7 | 99   | 127  | -4  | 3  | 7 | 325  | 360  | 2   | 5  | 7 | 1210 | 1345 | 10  | 7  | 7 | 2    | 1    | -3  | 10 | 7 | 183  | 163  |   |   |   |     |      |
| -8  | -9 | 7 | 475  | 494  | -3  | 3  | 7 | 201  | 190  | 3   | 5  | 7 | 187  | 218  | 11  | 7  | 7 | 63   | 53   | -2  | 10 | 7 | 14   | 4    |   |   |   |     |      |
| -7  | -9 | 7 | 589  | 541  | -2  | 3  | 7 | 67   | 25   | 4   | 5  | 7 | 2818 | 2612 | -15 | 0  | 7 | 10   | 9    | -1  | 10 | 7 | 5    | 5    |   |   |   |     |      |
| -6  | -9 | 7 | 63   | 72   | -1  | 3  | 7 | 65   | 111  | 5   | 5  | 7 | 2487 | 2349 | -14 | 0  | 7 | 89   | 56   | 0   | 10 | 7 | 392  | 352  |   |   |   |     |      |
| -5  | -9 | 7 | 1234 | 1281 | 0   | 3  | 7 | 29   | 72   | 6   | 5  | 7 | 395  | 327  | -13 | 0  | 7 | 28   | 13   | 1   | 10 | 7 | 2    | 2    |   |   |   |     |      |
| -4  | -9 | 7 | 750  | 911  | 1   | 3  | 7 | 782  | 654  | 7   | 5  | 7 | 467  | 482  | -12 | 0  | 7 | 24   | 13   | 2   | 10 | 7 | 18   | 32   |   |   |   |     |      |
| -3  | -9 | 7 | 1082 | 1144 | 2   | 3  | 7 | 171  | 117  | 8   | 5  | 7 | 379  | 313  | -11 | 0  | 7 | 16   | 37   | 3   | 10 | 7 | 184  | 187  |   |   |   |     |      |
| -2  | -9 | 7 | 6189 | 5472 | 3   | 3  | 7 | 1442 | 1601 | 9   | 5  | 7 | 115  | 142  | -10 | 0  | 7 | 147  | 110  | 4   | 10 | 7 | 89   | 99   |   |   |   |     |      |
| -1  | -9 | 7 | 3988 | 3962 | 4   | 3  | 7 | 716  | 645  | 10  | 5  | 7 | 194  | 172  | -9  | 0  | 7 | 26   | 42   | 5   | 10 | 7 | 8    | 11   |   |   |   |     |      |
| 0   | -9 | 7 | 1525 | 1503 | 5   | 3  | 7 | 64   | 60   | 11  | 5  | 7 | 32   | 75   | -8  | 0  | 7 | 22   | 31   | 6   | 10 | 7 | 42   | 36   |   |   |   |     |      |
| 1   | -9 | 7 | 1389 | 1442 | 6   | 3  | 7 | 6    | 8    | 12  | 5  | 7 | 12   | 43   | -7  | 0  | 7 | 923  | 887  | 7   | 10 | 7 | 18   | 20   |   |   |   |     |      |
| 2   | -9 | 7 | 3    | 3    | 7   | 3  | 7 | 334  | 276  | -16 | 6  | 7 | -10  | 8    | -6  | 0  | 7 | -4   | 4    | 8   | 10 | 7 | 9    | 1    |   |   |   |     |      |
| 3   | -9 | 7 | 225  | 360  | 8   | 3  | 7 | 29   | 28   | -15 | 6  | 7 | 20   | 23   | -5  | 0  | 7 | 4    | 7    | 9   | 10 | 7 | -10  | 1    |   |   |   |     |      |
| 4   | -9 | 7 | 407  | 397  | 9   | 3  | 7 | 49   | 56   | -14 | 6  | 7 | 18   | 21   | -4  | 0  | 7 | 6    | 22   | -13 | 11 | 7 | 0    | 8    |   |   |   |     |      |
| 5   | -9 | 7 | 274  | 273  | 10  | 3  | 7 | 481  | 481  | -13 | 6  | 7 | 11   | 0    | -3  | 0  | 7 | 248  | 230  | -12 | 11 | 7 | 19   | 12   |   |   |   |     |      |
| 6   | -9 | 7 | 458  | 476  | 11  | 3  | 7 | 48   | 35   | -12 | 6  | 7 | 33   | 20   | -2  | 0  | 7 | 15   | 8    | -11 | 11 | 7 | 35   | 11   |   |   |   |     |      |
| 7   | -9 | 7 | 470  | 430  | 12  | 3  | 7 | 7    | 5    | -11 | 6  | 7 | 271  | 253  | -1  | 0  | 7 | 43   | 47   | -10 | 11 | 7 | 0    | 0    |   |   |   |     |      |
| 8   | -9 | 7 | 131  | 156  | 13  | 3  | 7 | 33   | 34   | -10 | 6  | 7 | 21   | 14   | 0   | 8  | 7 | 78   | 69   | -9  | 11 | 7 | 79   | 52   |   |   |   |     |      |
| 9   | -9 | 7 | 82   | 54   | -16 | 4  | 7 | 19   | 0    | -9  | 6  | 7 | 222  | 240  | 1   | 8  | 7 | 6    | 5    | -8  | 11 | 7 | 7    | 21   |   |   |   |     |      |
| 10  | -9 | 7 | 286  | 307  | -15 | 4  | 7 | 37   | 13   | -8  | 6  | 7 | 26   | 21   | 2   | 8  | 7 | 1972 | 1808 | -7  | 11 | 7 | 16   | 20   |   |   |   |     |      |
| 11  | -9 | 7 | 32   | 33   | -14 | 4  | 7 | -6   | 3    | -7  | 6  | 7 | 976  | 947  | 3   | 8  | 7 | 19   | 22   | -6  | 11 | 7 | 5    | 8    |   |   |   |     |      |
| 12  | -9 | 7 | 21   | 15   | -13 | 4  | 7 | 24   | 4    | -6  | 6  | 7 | 29   | 33   | 4   | 8  | 7 | 227  | 212  | -5  | 11 | 7 | 35   | 40   |   |   |   |     |      |
| 13  | -9 | 7 | 270  | 244  | -12 | 4  | 7 | 142  | 129  | -5  | 6  | 7 | 20   | 7    | 5   | 8  | 7 | 4    | 2    | -4  | 11 | 7 | 164  | 167  |   |   |   |     |      |
| 14  | -9 | 7 | 193  | 221  | -11 | 4  | 7 | 46   | 62   | -4  | 6  | 7 | 536  | 493  | 6   | 8  | 7 | 69   | 63   | -3  | 11 | 7 | 48   | 54   |   |   |   |     |      |
| -16 | -9 | 7 | -1   | 4    | -10 | 4  | 7 | 188  | 185  | -3  | 6  | 7 | 1    | 3    | 7   | 8  | 7 | 183  | 188  | -2  | 11 | 7 | 217  | 203  |   |   |   |     |      |
| -15 | -9 | 7 | 16   | 0    | -9  | 4  | 7 | 92   | 101  | -2  | 6  | 7 | 294  | 256  | 8   | 8  | 7 | 14   | 10   | -1  | 11 | 7 | 173  | 170  |   |   |   |     |      |
| -14 | -9 | 7 | 1    | 3    | -8  | 4  | 7 | 42   | 34   | -1  | 6  | 7 | 208  | 214  | 9   | 8  |   |      |      |     |    |   |      |      |   |   |   |     |      |

Table A.3, continued

| M   | K   | L | Obs  | Calc | M     | K | L   | Obs | Calc   | M | K   | L   | Obs    | Calc | M   | K   | L     | Obs | Calc | M    | K | L | Obs | Calc | M | K | L | Obs | Calc |
|-----|-----|---|------|------|-------|---|-----|-----|--------|---|-----|-----|--------|------|-----|-----|-------|-----|------|------|---|---|-----|------|---|---|---|-----|------|
| -3  | 13  | 7 | 1    | 6    | 1-17  | 0 | 34  | 24  | -6-13  | 0 | 1   | 0   | 11-11  | 0    | 9   | 0   | -6-8  | 0   | 288  | 256  |   |   |     |      |   |   |   |     |      |
| -2  | 13  | 7 | 15   | 16   | 2-17  | 0 | 39  | 19  | -5-13  | 0 | 57  | 51  | 12-11  | 0    | 3   | 0   | -5-8  | 0   | 450  | 434  |   |   |     |      |   |   |   |     |      |
| -1  | 13  | 7 | 60   | 43   | 3-17  | 0 | -3  | 0   | -4-13  | 0 | 10  | 21  | 13-11  | 0    | -1  | 7   | -4-8  | 0   | 313  | 355  |   |   |     |      |   |   |   |     |      |
| 0   | 13  | 7 | 94   | 80   | 4-17  | 0 | 26  | 10  | -3-13  | 0 | 52  | 42  | -12-10 | 0    | 15  | 22  | -3-8  | 0   | 59   | 30   |   |   |     |      |   |   |   |     |      |
| 1   | 13  | 7 | 61   | 62   | 5-17  | 0 | -1  | 7   | -2-13  | 0 | 15  | 15  | -11-10 | 0    | 26  | 9   | -2-8  | 0   | 148  | 97   |   |   |     |      |   |   |   |     |      |
| 2   | 13  | 7 | 0    | 1    | 6-17  | 0 | 3   | 0   | -1-13  | 0 | 57  | 35  | -10-10 | 0    | -4  | 2   | -1-8  | 0   | 5    | 0    |   |   |     |      |   |   |   |     |      |
| 3   | 13  | 7 | 4    | 12   | 7-17  | 0 | 29  | 1   | 0-13   | 0 | 320 | 340 | -9-10  | 0    | 18  | 18  | 0-8   | 0   | 50   | 20   |   |   |     |      |   |   |   |     |      |
| 4   | 13  | 7 | 17   | 16   | 8-17  | 0 | 16  | 1   | 1-13   | 0 | 8   | 16  | -8-10  | 0    | 72  | 47  | 1-8   | 0   | 35   | 22   |   |   |     |      |   |   |   |     |      |
| 5   | 13  | 7 | 24   | 1    | 9-17  | 0 | -1  | 1   | 2-13   | 0 | 13  | 19  | -7-10  | 0    | -1  | 7   | 2-8   | 0   | 47   | 66   |   |   |     |      |   |   |   |     |      |
| 6   | 13  | 7 | 45   | 48   | 10-17 | 0 | -2  | 0   | 3-13   | 0 | 14  | 20  | -6-10  | 0    | 68  | 55  | 3-8   | 0   | 268  | 242  |   |   |     |      |   |   |   |     |      |
| -10 | 14  | 7 | 37   | 4    | 11-17 | 0 | 17  | 4   | 4-13   | 0 | 14  | 11  | -5-10  | 0    | -2  | 1   | 4-8   | 0   | 170  | 184  |   |   |     |      |   |   |   |     |      |
| -9  | 14  | 7 | 45   | 7    | -2-16 | 0 | -3  | 0   | 5-13   | 0 | 5   | 7   | -4-10  | 0    | -1  | 1   | 5-8   | 0   | 223  | 214  |   |   |     |      |   |   |   |     |      |
| -8  | 14  | 7 | 25   | 15   | -1-16 | 0 | 27  | 19  | 6-13   | 0 | 52  | 56  | -3-10  | 0    | 3   | 1   | 6-8   | 0   | 0    | 2    |   |   |     |      |   |   |   |     |      |
| -7  | 14  | 7 | 1    | 0    | 0-16  | 0 | 17  | 23  | 7-13   | 0 | 12  | 12  | -2-10  | 0    | 59  | 41  | 7-8   | 0   | 183  | 193  |   |   |     |      |   |   |   |     |      |
| -6  | 14  | 7 | -3   | 1    | 1-16  | 0 | 5   | 7   | 8-13   | 0 | 1   | 3   | -1-10  | 0    | 101 | 108 | 8-8   | 0   | 188  | 170  |   |   |     |      |   |   |   |     |      |
| -5  | 14  | 7 | 14   | 38   | 2-16  | 0 | -3  | 1   | 9-13   | 0 | 21  | 20  | 0-10   | 0    | 178 | 209 | 9-8   | 0   | 105  | 103  |   |   |     |      |   |   |   |     |      |
| -4  | 14  | 7 | 59   | 62   | 3-16  | 0 | 0   | 7   | 10-13  | 0 | 16  | 18  | 1-10   | 0    | 881 | 811 | 10-8  | 0   | 211  | 194  |   |   |     |      |   |   |   |     |      |
| -3  | 14  | 7 | 11   | 11   | 4-16  | 0 | 5   | 1   | 11-13  | 0 | -6  | 1   | 2-10   | 0    | 504 | 503 | 11-8  | 0   | 97   | 97   |   |   |     |      |   |   |   |     |      |
| -2  | 14  | 7 | 109  | 101  | 5-16  | 0 | 0   | 1   | 12-13  | 0 | 6   | 4   | 3-10   | 0    | 74  | 70  | 12-8  | 0   | 15   | 7    |   |   |     |      |   |   |   |     |      |
| -1  | 14  | 7 | 88   | 101  | 6-16  | 0 | 5   | 2   | 13-13  | 0 | -22 | 6   | 4-10   | 0    | 8   | 10  | 13-8  | 0   | 17   | 19   |   |   |     |      |   |   |   |     |      |
| 0   | 14  | 7 | 16   | 21   | 7-16  | 0 | 6   | 1   | -10-12 | 0 | 6   | 2   | 5-10   | 0    | 4   | 3   | 14-8  | 0   | 32   | 33   |   |   |     |      |   |   |   |     |      |
| 1   | 14  | 7 | -2   | 3    | 8-16  | 0 | -2  | 1   | -9-12  | 0 | 34  | 41  | 6-10   | 0    | 185 | 152 | -15-7 | 0   | 33   | 4    |   |   |     |      |   |   |   |     |      |
| 2   | 14  | 7 | 8    | 10   | 9-16  | 0 | 10  | 0   | -8-12  | 0 | 15  | 10  | 7-10   | 0    | 4   | 2   | -14-7 | 0   | 1    | 0    |   |   |     |      |   |   |   |     |      |
| 3   | 14  | 7 | 18   | 26   | 10-16 | 0 | 20  | 2   | -7-12  | 0 | -1  | 0   | 8-10   | 0    | 28  | 26  | -13-7 | 0   | 10   | 18   |   |   |     |      |   |   |   |     |      |
| 4   | 14  | 7 | 41   | 3    | 11-16 | 0 | -4  | 1   | -6-12  | 0 | 94  | 108 | 9-10   | 0    | 106 | 119 | -12-7 | 0   | 48   | 46   |   |   |     |      |   |   |   |     |      |
| 5   | 14  | 7 | 7    | 17   | -5-15 | 0 | -4  | 3   | -5-12  | 0 | 67  | 71  | 10-10  | 0    | 7   | 2   | -11-7 | 0   | 6    | 1    |   |   |     |      |   |   |   |     |      |
| 6   | 14  | 7 | -10  | 18   | -4-15 | 0 | 0   | 0   | -4-12  | 0 | 14  | 11  | 11-10  | 0    | -3  | 0   | -10-7 | 0   | 31   | 36   |   |   |     |      |   |   |   |     |      |
| -9  | 15  | 7 | 33   | 8    | -3-15 | 0 | 15  | 7   | -3-12  | 0 | 195 | 174 | 12-10  | 0    | 15  | 14  | -9-7  | 0   | 296  | 281  |   |   |     |      |   |   |   |     |      |
| -8  | 15  | 7 | -4   | 6    | -2-15 | 0 | 20  | 21  | -2-12  | 0 | 254 | 220 | 13-10  | 0    | 25  | 31  | -8-7  | 0   | 32   | 31   |   |   |     |      |   |   |   |     |      |
| -7  | 15  | 7 | 5    | 0    | -1-15 | 0 | -2  | 2   | -1-12  | 0 | 148 | 131 | 14-10  | 0    | 32  | 3   | -7-7  | 0   | 19   | 26   |   |   |     |      |   |   |   |     |      |
| -6  | 15  | 7 | 32   | 3    | 0-15  | 0 | 4   | 1   | 0-12   | 0 | 56  | 59  | -13-9  | 0    | 24  | 8   | -6-7  | 0   | 307  | 294  |   |   |     |      |   |   |   |     |      |
| -5  | 15  | 7 | -4   | 11   | 1-15  | 0 | 9   | 1   | 1-12   | 0 | 574 | 537 | -12-9  | 0    | 24  | 23  | -5-7  | 0   | 205  | 173  |   |   |     |      |   |   |   |     |      |
| -4  | 15  | 7 | -5   | 4    | 2-15  | 0 | -2  | 1   | 2-12   | 0 | 364 | 315 | -11-9  | 0    | 6   | 3   | -4-7  | 0   | 135  | 157  |   |   |     |      |   |   |   |     |      |
| -3  | 15  | 7 | 11   | 27   | 3-15  | 0 | 5   | 4   | 3-12   | 0 | 7   | 9   | -10-9  | 0    | 52  | 43  | -3-7  | 0   | 391  | 371  |   |   |     |      |   |   |   |     |      |
| -2  | 15  | 7 | 28   | 28   | 4-15  | 0 | 0   | 2   | 4-12   | 0 | 28  | 46  | -9-8   | 0    | 181 | 173 | -2-7  | 0   | 712  | 708  |   |   |     |      |   |   |   |     |      |
| -1  | 15  | 7 | 2    | 10   | 5-15  | 0 | 18  | 6   | 5-12   | 0 | 146 | 132 | -8-9   | 0    | 69  | 51  | -1-7  | 0   | 863  | 790  |   |   |     |      |   |   |   |     |      |
| 0   | 15  | 7 | 5    | 0    | 6-15  | 0 | 11  | 9   | 6-12   | 0 | 21  | 17  | -7-9   | 0    | 34  | 39  | 0-7   | 0   | 65   | 38   |   |   |     |      |   |   |   |     |      |
| 1   | 15  | 7 | 32   | 12   | 7-15  | 0 | 7   | 4   | 7-12   | 0 | 60  | 59  | -6-9   | 0    | 78  | 71  | 1-7   | 0   | 629  | 773  |   |   |     |      |   |   |   |     |      |
| 2   | 15  | 7 | -4   | 3    | 8-15  | 0 | -5  | 0   | 8-12   | 0 | 94  | 74  | -5-9   | 0    | 519 | 467 | 2-7   | 0   | 450  | 414  |   |   |     |      |   |   |   |     |      |
| 3   | 15  | 7 | 13   | 1    | 9-15  | 0 | 15  | 1   | 9-12   | 0 | 51  | 62  | -4-9   | 0    | 28  | 28  | 3-7   | 0   | 2    | 0    |   |   |     |      |   |   |   |     |      |
| 4   | 15  | 7 | 14   | 10   | 10-15 | 0 | 4   | 0   | 10-12  | 0 | 12  | 21  | -3-9   | 0    | 325 | 271 | 4-7   | 0   | 25   | 19   |   |   |     |      |   |   |   |     |      |
| 5   | 15  | 7 | 17   | 2    | 11-15 | 0 | -1  | 10  | 11-12  | 0 | 28  | 11  | -2-9   | 0    | 57  | 63  | 5-7   | 0   | 185  | 165  |   |   |     |      |   |   |   |     |      |
| 6   | 15  | 7 | -19  | 0    | 12-15 | 0 | 18  | 16  | 12-12  | 0 | 18  | 9   | -1-9   | 0    | 30  | 33  | 6-7   | 0   | 227  | 201  |   |   |     |      |   |   |   |     |      |
| -6  | 16  | 7 | 23   | 0    | -7-14 | 0 | 7   | 5   | 13-12  | 0 | -4  | 2   | 0-9    | 0    | 130 | 107 | 7-7   | 0   | 754  | 714  |   |   |     |      |   |   |   |     |      |
| -5  | 16  | 7 | -22  | 8    | -6-14 | 0 | 39  | 36  | -11-11 | 0 | 4   | 26  | 1-9    | 0    | 34  | 49  | 8-7   | 0   | 481  | 453  |   |   |     |      |   |   |   |     |      |
| -4  | 16  | 7 | 45   | 1    | -5-14 | 0 | 1   | 0   | -10-11 | 0 | 59  | 32  | 2-9    | 0    | 363 | 310 | 9-7   | 0   | 206  | 186  |   |   |     |      |   |   |   |     |      |
| -3  | 16  | 7 | -7   | 1    | -4-14 | 0 | 4   | 2   | -9-11  | 0 | 45  | 56  | 3-9    | 0    | -1  | 1   | 10-7  | 0   | 112  | 109  |   |   |     |      |   |   |   |     |      |
| -2  | 16  | 7 | -14  | 0    | -3-14 | 0 | 26  | 28  | -8-11  | 0 | -1  | 2   | 4-9    | 0    | 9   | 3   | 11-7  | 0   | 46   | 26   |   |   |     |      |   |   |   |     |      |
| -1  | 16  | 7 | -4   | 7    | -2-14 | 0 | 7   | 1   | -7-11  | 0 | 13  | 13  | 5-9    | 0    | 233 | 236 | 12-7  | 0   | 27   | 50   |   |   |     |      |   |   |   |     |      |
| 0   | 16  | 7 | 13   | 22   | -1-14 | 0 | 13  | 9   | -6-11  | 0 | 121 | 104 | 6-9    | 0    | 48  | 31  | 13-7  | 0   | 34   | 34   |   |   |     |      |   |   |   |     |      |
| 1   | 16  | 7 | 19   | 2    | 0-14  | 0 | -1  | 1   | -5-11  | 0 | 44  | 30  | 7-9    | 0    | 1   | 1   | 14-7  | 0   | 29   | 0    |   |   |     |      |   |   |   |     |      |
| 2   | 16  | 7 | -6   | 7    | 1-14  | 0 | 22  | 35  | -4-11  | 0 | 53  | 37  | 8-9    | 0    | 62  | 64  | -16-6 | 0   | -10  | 0    |   |   |     |      |   |   |   |     |      |
| 3   | 16  | 7 | 0    | 21   | 2-14  | 0 | 41  | 38  | -3-11  | 0 | 175 | 172 | 9-9    | 0    | 8   | 16  | -15-6 | 0   | 1    | 1    |   |   |     |      |   |   |   |     |      |
| 4   | 16  | 7 | 18   | 8    | 3-14  | 0 | 5   | 0   | -2-11  | 0 | 17  | 13  | 10-9   | 0    | 18  | 30  | -14-6 | 0   | 19   | 19   |   |   |     |      |   |   |   |     |      |
| -2  | -10 | 8 | 19   | 0    | 4-14  | 0 | -5  | 1   | -1-11  | 0 | 75  | 85  | 11-9   | 0    | 0   | 2   | -13-6 | 0   | -3   | 1    |   |   |     |      |   |   |   |     |      |
| -1  | -10 | 8 | -2   | 1    | 5-14  | 0 | 18  | 9   | 0-11   | 0 | 757 | 629 | 12-9   | 0    | 19  | 6   | -12-6 | 0   | 9    | 22   |   |   |     |      |   |   |   |     |      |
| 0   | -10 | 8 | -31  | 1    | 6-14  | 0 | 12  | 2   | -1-11  | 0 | 25  | 34  | 13-9   | 0    | -4  | 0   | -11-6 | 0   | 112  | 105  |   |   |     |      |   |   |   |     |      |
| 1   | -10 | 8 | 16   | 0    | 7-14  | 0 | 6   | 0   | 2-11   | 0 | 13  | 14  | 14-9   | 0    | 12  | 16  | -10-6 | 0   | 177  | 181  |   |   |     |      |   |   |   |     |      |
| 2   | -10 | 8 | -12  | 1    | 8-14  | 0 | 9   | 6   | 3-11   | 0 | 115 | 94  | -14-8  | 0    | 13  | 13  | -9-6  | 0   | 27   | 42   |   |   |     |      |   |   |   |     |      |
| 3   | -10 | 8 | 27   | 9    | 9-14  | 0 | 7   | 3   | 4-11   | 0 | 20  | 15  | -13-8  | 0    | 11  | 1   | -8-6  | 0   | 152  | 187  |   |   |     |      |   |   |   |     |      |
| 4   | -10 | 8 | -6   | 2    | 10-14 | 0 | 12  | 4   | 5-11   | 0 | 36  | 44  | -12-8  | 0    | 7   | 18  | -7-6  | 0   | 416  | 345  |   |   |     |      |   |   |   |     |      |
| 5   | -10 | 8 | -11  | 0    | 11-14 | 0 | 2   | 6   | 6-11   | 0 | 66  | 77  | -11-8  | 0    | 111 | 81  | -6-6  | 0   | 989  | 1034 |   |   |     |      |   |   |   |     |      |
| 6   | -10 | 8 | 1    | 2    | 12-14 | 0 | 12  | 1   | 7-11   | 0 | 116 | 91  | -10-8  | 0    | 13  | 33  | -5-6  | 0   | 27   | 42   |   |   |     |      |   |   |   |     |      |
| -4  | -6  | 8 | 2    | 3    | 0-4   | 0 | 206 | 210 | 3-2    | 0 | 24  | 33  | 6-0    | 0    | 481 | 439 | 12-2  | 0   | 16   | 23   |   |   |     |      |   |   |   |     |      |
| -3  | -6  | 8 | 1384 | 1145 | 1-4   | 0 | 446 | 613 | 4-2    | 0 | 98  | 85  | 7-0    | 0</  |     |     |       |     |      |      |   |   |     |      |   |   |   |     |      |

Table A.3, continued

| H   | K  | L | Obs  | Calc | H   | K  | L   | Obs  | Calc | H   | K  | L  | Obs  | Calc | H   | K  | L   | Obs  | Calc | H     | K   | L  | Obs  | Calc |
|-----|----|---|------|------|-----|----|-----|------|------|-----|----|----|------|------|-----|----|-----|------|------|-------|-----|----|------|------|
| -   | -  | - | -    | -    | -   | -  | -   | -    | -    | -   | -  | -  | -    | -    | -   | -  | -   | -    | -    | -     | -   | -  | -    | -    |
| -   | 5  | 8 | 974  | 926  | 10  | -3 | 0   | 169  | 136  | 12  | -1 | 0  | 27   | 19   | -13 | 2  | 0   | 39   | 19   | -6    | 4   | 0  | 142  | 132  |
| -   | 7  | 5 | 186  | 165  | 11  | -3 | 0   | 110  | 11   | 13  | -1 | 0  | 27   | 19   | -13 | 2  | 0   | 26   | 26   | -5    | 4   | 0  | 3    | 3    |
| -   | 9  | 5 | 1    | 3    | 12  | -3 | 0   | 83   | 72   | 14  | -1 | 0  | 107  | 131  | -11 | 2  | 0   | 255  | 257  | -4    | 4   | 0  | 110  | 117  |
| -   | 9  | 5 | 204  | 183  | 17  | -3 | 0   | 95   | 102  | -16 | 0  | 0  | 0    | 0    | -10 | 2  | 0   | 122  | 154  | -3    | 4   | 0  | 256  | 229  |
| 10  | -5 | 0 | 68   | 58   | 14  | -2 | 0   | 20   | 21   | -15 | 0  | 0  | 29   | 49   | -9  | 2  | 0   | 29   | 31   | -2    | 4   | 0  | 55   | 72   |
| 11  | -5 | 0 | 5    | 1    | -17 | -2 | 0   | 49   | 2    | -14 | 0  | 0  | 3    | 3    | -8  | 2  | 0   | 14   | 2    | -1    | 4   | 0  | 9    | 24   |
| 12  | -5 | 0 | 124  | 95   | -16 | -2 | 0   | 7    | 0    | -13 | 0  | 0  | -2   | 0    | -7  | 2  | 0   | 68   | 73   | 0     | 4   | 0  | 1431 | 1384 |
| 13  | -5 | 0 | 122  | 121  | -15 | -2 | 0   | 62   | 29   | -12 | 0  | 0  | 95   | 109  | -6  | 2  | 0   | 58   | 51   | 1     | 4   | 0  | 1003 | 984  |
| 14  | -5 | 0 | -4   | 2    | -14 | -2 | 0   | 0    | 0    | -11 | 0  | 0  | 136  | 114  | -5  | 2  | 0   | 736  | 662  | 2     | 4   | 0  | 811  | 693  |
| -16 | -4 | 0 | -3   | 1    | -13 | -2 | 0   | 15   | 4    | -10 | 0  | 0  | 12   | 17   | -4  | 2  | 0   | 1167 | 1150 | 3     | 4   | 0  | 2650 | 2611 |
| -15 | -4 | 0 | -5   | 0    | -12 | -2 | 0   | 133  | 91   | -9  | 0  | 0  | 149  | 139  | -3  | 2  | 0   | 35   | 66   | 4     | 4   | 0  | 136  | 142  |
| -14 | -4 | 0 | -46  | 22   | -11 | -2 | 0   | 141  | 150  | -8  | 0  | 0  | 25   | 62   | -2  | 2  | 0   | 625  | 563  | 3     | 4   | 0  | 521  | 411  |
| -13 | -4 | 0 | -9   | 11   | -10 | -2 | 0   | 30   | 121  | -7  | 0  | 0  | 96   | 322  | -1  | 2  | 0   | 1174 | 1388 | 6     | 4   | 0  | 78   | 56   |
| -12 | -4 | 0 | 3    | -9   | -2  | 0  | 222 | 234  | -6   | 0   | 0  | 0  | 198  | 176  | 0   | 2  | 0   | 465  | 413  | 7     | 4   | 0  | 289  | 271  |
| -11 | -4 | 0 | 1    | 10   | -8  | -2 | 0   | 1    | 5    | -5  | 0  | 0  | 559  | 558  | 1   | 2  | 0   | 72   | 104  | 8     | 4   | 0  | 472  | 472  |
| -10 | -4 | 0 | 160  | 176  | -7  | -2 | 0   | 221  | 256  | -4  | 0  | 0  | 54   | 83   | 2   | 2  | 0   | 231  | 255  | 9     | 4   | 0  | 18   | 5    |
| -9  | -4 | 0 | 237  | 259  | -6  | -2 | 0   | 600  | 709  | -3  | 0  | 0  | -2   | 8    | 3   | 2  | 0   | 1342 | 1293 | 10    | 4   | 0  | 111  | 120  |
| -8  | -4 | 0 | 47   | 76   | -5  | -2 | 0   | 76   | 50   | -2  | 0  | 0  | 3667 | 3262 | 4   | 2  | 0   | 3    | 2    | 11    | 4   | 0  | 97   | 99   |
| -7  | -4 | 0 | 86   | 81   | -4  | -2 | 0   | 452  | 503  | -1  | 0  | 0  | 894  | 1031 | 5   | 2  | 0   | 11   | 14   | 12    | 4   | 0  | 2    | 9    |
| -6  | -4 | 0 | 1963 | 2017 | -3  | -2 | 0   | 196  | 250  | 0   | 0  | 0  | 702  | 1780 | 6   | 2  | 0   | 1663 | 1511 | -16   | 5   | 0  | 8    | 2    |
| -5  | -4 | 0 | 88   | 24   | -2  | -2 | 0   | 5050 | 4647 | 1   | 0  | 0  | 180  | 7    | 7   | 2  | 0   | 152  | 132  | -16   | 5   | 0  | 63   | 63   |
| -4  | -4 | 0 | 341  | 527  | -1  | 0  | 20  | 1202 | 2    | 2   | 0  | 0  | 666  | 939  | 9   | 2  | 0   | 11   | 87   | -14   | 5   | 0  | 45   | 33   |
| -3  | -4 | 0 | 198  | 240  | 0   | -2 | 0   | 44   | 60   | 3   | 0  | 0  | 752  | 698  | 9   | 2  | 0   | 33   | 27   | -13   | 5   | 0  | -2   | 1    |
| -2  | -4 | 0 | 220  | 128  | 1   | -2 | 0   | 784  | 929  | 4   | 0  | 0  | 145  | 150  | 10  | 2  | 0   | 212  | 198  | -12   | 5   | 0  | 81   | 45   |
| -1  | -4 | 0 | 78   | 72   | 2   | -2 | 0   | 343  | 349  | 5   | 0  | 0  | 9    | 14   | 11  | 2  | 0   | 25   | 19   | -11   | 5   | 0  | 240  | 194  |
| -10 | 5  | 0 | 50   | 46   | 1   | 7  | 0   | -1   | 1    | -8  | 10 | 0  | 123  | 107  | -4  | 13 | 0   | 17   | 34   | 6-17  | 9   | 0  | -12  | 0    |
| -9  | 5  | 0 | 350  | 377  | 2   | 7  | 0   | 716  | 651  | -7  | 10 | 0  | 105  | 99   | -3  | 13 | 0   | 42   | 40   | 7-17  | 9   | 0  | 13   | 0    |
| -8  | 5  | 0 | 11   | 3    | 3   | 7  | 0   | 114  | 116  | -6  | 10 | 0  | -2   | 4    | -2  | 13 | 0   | 40   | 50   | 8-17  | 9   | 0  | 19   | 0    |
| -7  | 5  | 0 | 803  | 741  | 4   | 7  | 0   | 11   | 1    | -5  | 10 | 0  | 23   | 1    | -1  | 13 | 0   | 90   | 98   | 9-17  | 9   | 0  | -10  | 1    |
| -6  | 5  | 0 | 258  | 217  | 5   | 7  | 0   | 13   | 21   | -4  | 10 | 0  | 25   | 18   | 0   | 13 | 0   | -5   | 7    | -2-16 | 9   | 0  | 30   | 24   |
| -5  | 5  | 0 | 8    | 9    | 6   | 7  | 0   | 372  | 327  | -3  | 10 | 0  | 112  | 125  | 1   | 13 | 0   | -3   | 5    | -1-16 | 9   | 0  | 11   | 9    |
| -4  | 5  | 0 | 366  | 387  | 7   | 7  | 0   | 97   | 97   | -2  | 10 | 0  | 75   | 93   | 3   | 13 | 0   | 46   | 45   | 0-16  | 9   | 0  | 6    | 11   |
| -3  | 5  | 0 | 23   | 16   | 7   | 7  | 0   | -1   | 3    | -1  | 10 | 0  | 177  | 138  | 3   | 13 | 0   | 22   | 16   | 1-16  | 9   | 0  | -3   | 2    |
| -2  | 5  | 0 | 410  | 511  | 9   | 7  | 0   | 84   | 101  | 0   | 10 | 0  | 128  | 137  | 4   | 13 | 0   | -5   | 1    | 2-16  | 9   | 0  | 1    | 3    |
| -1  | 5  | 0 | 570  | 503  | 10  | 7  | 0   | 51   | 54   | 1   | 10 | 0  | 0    | 4    | 5   | 13 | 0   | 16   | 15   | 3-16  | 9   | 0  | -2   | 1    |
| 0   | 5  | 0 | 14   | 45   | -15 | 8  | 0   | 23   | 1    | 2   | 10 | 0  | 209  | 199  | 6   | 13 | 0   | 0    | 0    | 4-16  | 9   | 0  | 21   | 9    |
| 1   | 5  | 0 | 64   | 58   | -14 | 8  | 0   | 9    | 31   | 3   | 10 | 0  | 143  | 123  | -10 | 14 | 0   | 12   | 0    | 5-16  | 9   | 0  | 11   | 10   |
| 2   | 5  | 0 | 3512 | 3228 | -13 | 8  | 0   | 32   | 33   | 4   | 10 | 0  | 7    | 16   | -9  | 14 | 0   | 2    | 4    | 6-16  | 9   | 0  | 0    | 6    |
| 3   | 5  | 0 | 2108 | 2050 | -12 | 8  | 0   | -5   | 1    | 5   | 10 | 0  | 46   | 46   | -8  | 14 | 0   | 4    | 0    | 7-16  | 9   | 0  | -2   | 2    |
| 4   | 5  | 0 | 1324 | 1304 | -11 | 8  | 0   | 11   | 21   | 6   | 10 | 0  | 230  | 203  | -7  | 14 | 0   | -1   | 4    | 8-16  | 9   | 0  | -6   | 0    |
| 5   | 5  | 0 | 209  | 195  | -10 | 8  | 0   | 82   | 106  | 7   | 10 | 0  | 8    | 5    | -7  | 14 | 0   | -7   | 1    | 9-16  | 9   | 0  | -1   | 1    |
| 6   | 5  | 0 | 26   | 16   | -9  | 8  | 0   | 131  | 114  | -8  | 10 | 0  | 9    | 5    | -5  | 14 | 0   | -5   | 0    | 10-16 | 9   | 0  | 14   | 0    |
| 7   | 5  | 0 | 10   | 19   | -8  | 0  | 0   | 13   | 27   | -13 | 11 | 0  | -13  | 10   | -4  | 14 | 0   | 16   | 13   | -4-15 | 9   | 0  | 1    | 7    |
| 8   | 5  | 0 | 61   | 63   | -7  | 0  | 0   | -5   | 6    | -12 | 11 | 0  | -4   | 27   | -3  | 14 | 0   | -4   | 10   | -3-15 | 9   | 0  | 3    | 3    |
| 9   | 5  | 0 | 204  | 189  | -6  | 0  | 0   | 368  | 272  | -11 | 11 | 0  | -9   | 0    | -2  | 14 | 0   | -5   | 1    | -2-15 | 9   | 0  | 3    | 3    |
| 10  | 5  | 0 | 65   | 55   | -5  | 0  | 0   | 0    | 3    | -10 | 11 | 0  | 25   | 23   | -1  | 14 | 0   | -1   | 1    | -1-15 | 9   | 0  | 6    | 0    |
| 11  | 5  | 0 | -5   | 0    | -4  | 8  | 0   | 9    | 5    | -9  | 11 | 0  | 104  | 105  | 0   | 14 | 0   | 19   | 14   | 0-15  | 9   | 0  | 3    | 4    |
| -16 | 6  | 8 | -1   | 3    | -3  | 0  | 0   | 222  | 228  | -8  | 11 | 0  | 27   | 27   | 1   | 14 | 0   | -1   | 11   | 1-15  | 9   | 0  | 40   | 47   |
| -15 | 6  | 8 | -5   | 3    | -2  | 0  | 0   | 549  | 576  | -7  | 11 | 0  | 21   | 5    | 2   | 14 | 0   | 25   | 1    | 2-15  | 9   | 0  | 11   | 0    |
| -14 | 6  | 8 | 54   | 39   | -1  | 8  | 0   | 59   | 39   | -6  | 11 | 0  | 34   | 38   | 3   | 14 | 0   | -8   | 8    | 3-15  | 9   | 0  | 2    | 0    |
| -13 | 6  | 8 | 30   | 38   | 0   | 8  | 0   | -3   | 2    | -5  | 11 | 0  | 31   | 58   | 4   | 14 | 0   | -9   | 7    | 4-15  | 9   | 0  | 13   | 16   |
| -12 | 6  | 8 | 107  | 96   | 8   | 8  | 0   | 107  | 109  | -4  | 11 | 0  | 20   | 59   | 5   | 14 | 0   | -15  | 0    | 5-15  | 9   | 0  | 21   | 0    |
| -11 | 6  | 8 | 28   | 6    | 2   | 8  | 0   | 172  | 192  | -3  | 11 | 0  | 86   | 59   | 6   | 14 | 0   | -1   | 4    | 6-15  | 9   | 0  | -5   | 0    |
| -10 | 6  | 8 | 225  | 235  | 3   | 8  | 0   | 208  | 202  | -2  | 11 | 0  | 194  | 163  | -8  | 15 | 0   | -1   | 1    | 7-15  | 9   | 0  | 25   | 9    |
| -9  | 6  | 8 | 19   | 13   | 4   | 8  | 0   | 5    | 3    | -1  | 11 | 0  | 48   | 51   | -7  | 15 | 0   | 48   | 2    | 8-15  | 9   | 0  | 3    | 2    |
| -8  | 6  | 8 | 28   | 56   | 5   | 8  | 0   | 199  | 215  | 0   | 11 | 0  | 18   | 16   | -6  | 15 | 0   | 1    | 9-15 | 9     | 0   | -4 | 1    |      |
| -7  | 6  | 8 | 590  | 645  | 6   | 8  | 0   | 29   | 16   | 1   | 11 | 0  | 148  | 127  | -5  | 15 | 0   | 23   | 7    | 10-15 | 9   | 0  | 23   | 31   |
| -6  | 6  | 8 | 306  | 265  | 7   | 8  | 0   | 13   | 11   | 2   | 11 | 0  | 157  | 142  | -4  | 15 | 0   | 13   | 10   | 11-15 | 9   | 0  | -6   | 11   |
| -5  | 6  | 8 | -3   | 1    | 8   | 8  | 0   | 47   | 70   | 3   | 11 | 0  | -3   | 8    | -3  | 15 | 0   | 10   | 4    | 6-14  | 9   | 0  | 8    | 2    |
| -4  | 6  | 8 | 59   | 59   | 9   | 8  | 0   | 35   | 44   | 4   | 11 | 0  | 15   | 26   | -2  | 15 | 0   | 6    | 15   | -5-14 | 9   | 0  | 11   | 9    |
| -3  | 6  | 8 | 1039 | 972  | 10  | 8  | 0   | 0    | 0    | 5   | -1 | 13 | 17   | 22   | 0   | 15 | 0   | 4    | 22   | -4-14 | 9   | 0  | 10   | 2    |
| -2  | 6  | 8 | 216  | 254  | -14 | 9  | 0   | 7    | 10   | 6   | 11 | 0  | 19   | 26   | 0   | 15 | 0   | 2    | 16   | -3-14 | 9   | 0  | 8    | 6    |
| -1  | 6  | 8 | 570  | 456  | -13 | 9  | 0   | 12   | 12   | 7   | 11 | 0  | 6    | 6    | 1   | 15 | 0   | 19   | 0    | -2-14 | 9   | 0  | 1    | 7    |
| 0   | 6  | 8 | 101  | 70   | -12 | 9  | 0   | 33   | 8    | 8   | 11 | 0  | -2   | 8    | 2   | 15 | 0   | -17  | 7    | -1-14 | 9   | 0  | 10   | 7    |
| 1   | 6  | 8 | 743  | 795  | -11 | 9  | 0   | 56   | 28   | -12 | 12 | 0  | -12  | 0    | 3   | 15 | 0   | -12  | 18   | 0-14  | 9   | 0  | 50   | 52   |
| 2   | 6  | 8 | 506  | 470  | -10 | 9  | 0   | 101  | 103  | -11 | 12 | 0  | 2    | 5    | 4   | 15 | 0   | -3   | 5    | 1-14  | 9   | 0  | 5    | 1    |
| 3   | 6  | 8 | 34   | 27   | -9  | 9  | 0   | 48   | 45   | -10 | 12 | 0  | 0    | 1    | 5   | 15 | 0   | -19  | 1    | 2-14  | 9   | 0  | 10   | 16   |
| 4   | 6  | 8 | 41   | 39   | -8  | 9  | 0   | 30   | 18   | -9  | 12 | 0  | 4    | 1    | -5  | 16 | 0   | 1    | 3    | 3-14  | 9   | 0  | 8    | 1    |
| 5   | 6  | 8 | 102  | 103  | -7  | 9  | 0   | 162  | 197  | -8  | 12 | 0  | 39   | 21   | -4  | 16 | 0   | -13  | 0    | 4-14  | 9   | 0  | 8    | 0    |
| 6   | 6  | 8 | 34   | 43   | -6  | 9  | 0   | 454  | 414  | -7  | 12 | 0  | 24   | 10   | -3  | 16 | 0   | 31   | 5    | 5-14  | 9   | 0  | 18   | 11   |
| 7   | 6  | 8 | 181  | 164  | -5  | 9  | 0   | 43   | 45   | -6  | 12 | 0  | -2   | 1    | -2  | 16 | 0   | -17  | 0    | 6-14  | 9   | 0  | 9    | 1    |
| 8   | 6  | 8 | 93   | 102  | -4  | 9  | 0   | 64   | 73   | -5  | 12 | 0  | 3    | 1    | 16  | 0  | -17 | 0    | -14  | 9     | 0</ |    |      |      |

Table A.3, continued

| M      | K | L    | Obe  | Calc  | M | K    | L    | Obe   | Calc | M    | K    | L     | Obe | Calc | M    | K     | L | Obe  | Calc | M | K | L | Obe | Calc | M | K | L | Obe | Calc |
|--------|---|------|------|-------|---|------|------|-------|------|------|------|-------|-----|------|------|-------|---|------|------|---|---|---|-----|------|---|---|---|-----|------|
| -4-12  | 9 | 75   | 79   | 11-10 | 9 | 8    | 11   | -9-7  | 9    | 26   | 23   | -4-5  | 9   | 458  | 456  | -1-3  | 9 | 3    | 0    |   |   |   |     |      |   |   |   |     |      |
| -3-12  | 9 | 34   | 24   | 12-10 | 9 | 2    | 13   | -8-7  | 9    | 10   | 2    | -3-5  | 9   | 44   | 58   | 0-3   | 9 | 36   | 22   |   |   |   |     |      |   |   |   |     |      |
| -2-12  | 9 | 14   | 7    | 13-10 | 9 | 30   | 1    | -7-7  | 9    | 81   | 71   | -2-5  | 9   | 1164 | 1033 | 1-3   | 9 | 342  | 311  |   |   |   |     |      |   |   |   |     |      |
| -1-12  | 9 | 130  | 132  | -13-9 | 9 | 40   | 4    | -6-7  | 9    | 51   | 60   | -1-5  | 9   | 14   | 12   | 2-3   | 9 | 413  | 679  |   |   |   |     |      |   |   |   |     |      |
| 0-12   | 9 | 16   | 19   | -12-9 | 9 | 23   | 12   | -5-7  | 9    | 6    | 0    | 0-5   | 9   | 25   | 67   | 3-3   | 9 | 267  | 274  |   |   |   |     |      |   |   |   |     |      |
| 1-12   | 9 | 86   | 65   | -11-9 | 9 | 21   | 34   | -4-7  | 9    | 258  | 232  | 1-5   | 9   | 842  | 652  | 4-3   | 9 | 497  | 522  |   |   |   |     |      |   |   |   |     |      |
| 2-12   | 9 | 0    | 6    | -10-9 | 9 | 27   | 10   | -3-7  | 9    | 105  | 128  | 2-5   | 9   | 243  | 200  | 5-3   | 9 | 156  | 139  |   |   |   |     |      |   |   |   |     |      |
| 3-12   | 9 | 22   | 8    | -9-9  | 9 | 5    | 2    | -2-7  | 9    | 67   | 52   | 3-5   | 9   | 14   | 34   | 6-3   | 9 | -3   | 0    |   |   |   |     |      |   |   |   |     |      |
| 4-12   | 9 | 12   | 13   | -7-9  | 9 | -1   | 1    | 0-7   | 9    | 92   | 115  | 4-5   | 9   | 178  | 158  | 7-3   | 9 | 0    | 5    |   |   |   |     |      |   |   |   |     |      |
| 5-12   | 9 | 24   | 36   | -6-9  | 9 | 19   | 5    | 1-7   | 9    | 126  | 80   | 6-5   | 9   | 66   | 79   | 8-3   | 9 | 5    | 12   |   |   |   |     |      |   |   |   |     |      |
| 6-12   | 9 | 18   | 22   | -5-9  | 9 | 4    | 1    | 2-7   | 9    | 166  | 142  | 7-5   | 9   | 366  | 340  | 10-3  | 9 | 64   | 77   |   |   |   |     |      |   |   |   |     |      |
| 7-12   | 9 | 14   | 0    | -4-9  | 9 | 29   | 10   | 3-7   | 9    | 211  | 243  | 8-5   | 9   | 75   | 71   | 11-3  | 9 | 170  | 152  |   |   |   |     |      |   |   |   |     |      |
| 8-12   | 9 | 5    | 19   | -3-9  | 9 | 22   | 25   | 4-7   | 9    | 803  | 752  | 9-5   | 9   | -1   | 3    | 12-3  | 9 | 120  | 113  |   |   |   |     |      |   |   |   |     |      |
| 9-12   | 9 | -5   | 0    | -2-9  | 9 | 330  | 331  | 5-7   | 9    | 170  | 185  | 10-5  | 9   | 79   | 72   | 13-3  | 9 | -3   | 2    |   |   |   |     |      |   |   |   |     |      |
| 10-12  | 9 | 2    | 3    | -1-9  | 9 | 457  | 434  | 6-7   | 9    | 141  | 168  | 11-5  | 9   | 89   | 78   | 14-3  | 9 | 59   | 42   |   |   |   |     |      |   |   |   |     |      |
| 11-12  | 9 | 61   | 4    | 0-9   | 9 | 28   | 26   | 7-7   | 9    | 168  | 146  | 12-5  | 9   | 14   | 13   | 15-3  | 9 | 90   | 35   |   |   |   |     |      |   |   |   |     |      |
| 12-12  | 9 | 0    | 2    | 2-9   | 9 | 114  | 95   | 8-7   | 9    | 52   | 71   | 13-5  | 9   | -19  | 0    | 16-2  | 9 | 19   | 0    |   |   |   |     |      |   |   |   |     |      |
| -1-11  | 9 | 13   | 24   | 3-9   | 9 | 17   | 31   | 10-7  | 9    | 268  | 219  | -16-4 | 9   | 6    | 8    | -14-2 | 9 | 35   | 51   |   |   |   |     |      |   |   |   |     |      |
| -2-11  | 9 | 31   | 23   | 4-9   | 9 | 169  | 145  | 11-7  | 9    | 36   | 47   | -15-4 | 9   | 25   | 36   | -13-2 | 9 | 33   | 25   |   |   |   |     |      |   |   |   |     |      |
| -3-11  | 9 | 28   | 32   | 5-9   | 9 | 33   | 40   | 12-7  | 9    | 8    | 1    | -14-4 | 9   | 39   | 41   | -12-2 | 9 | -3   | 1    |   |   |   |     |      |   |   |   |     |      |
| -4-11  | 9 | 0    | 12   | 6-9   | 9 | 145  | 143  | 13-7  | 9    | 15   | 34   | -13-4 | 9   | -5   | 2    | -11-2 | 9 | 149  | 144  |   |   |   |     |      |   |   |   |     |      |
| -5-11  | 9 | 85   | 84   | 7-9   | 9 | 126  | 105  | 14-7  | 9    | 29   | 12   | -12-4 | 9   | 1    | 1    | -10-2 | 9 | 155  | 115  |   |   |   |     |      |   |   |   |     |      |
| -6-11  | 9 | 89   | 99   | 8-9   | 9 | 44   | 55   | -15-6 | 9    | 16   | 1    | -11-4 | 9   | 90   | 89   | -9-2  | 9 | 9    | 6    |   |   |   |     |      |   |   |   |     |      |
| -7-11  | 9 | 15   | 13   | 9-9   | 9 | 192  | 170  | -14-6 | 9    | 9    | 0    | -10-4 | 9   | 4    | 0    | -8-2  | 9 | 299  | 309  |   |   |   |     |      |   |   |   |     |      |
| -8-11  | 9 | 12   | 20   | 10-9  | 9 | 245  | 208  | -13-6 | 9    | 68   | 26   | -9-4  | 9   | 56   | 62   | -7-2  | 9 | 551  | 534  |   |   |   |     |      |   |   |   |     |      |
| -9-11  | 9 | 190  | 162  | 11-9  | 9 | 8    | 8    | -12-6 | 9    | 17   | 1    | -8-4  | 9   | 275  | 270  | -6-2  | 9 | 66   | 63   |   |   |   |     |      |   |   |   |     |      |
| -10-11 | 9 | 50   | 61   | 12-9  | 9 | 13   | 11   | -11-6 | 9    | -4   | 1    | -7-4  | 9   | 32   | 36   | -5-2  | 9 | 260  | 243  |   |   |   |     |      |   |   |   |     |      |
| -11-11 | 9 | 11   | 10   | 13-9  | 9 | 16   | 20   | -10-6 | 9    | 29   | 26   | -6-4  | 9   | 0    | 1    | -4-2  | 9 | 2378 | 2515 |   |   |   |     |      |   |   |   |     |      |
| 0-11   | 9 | 75   | 76   | 14-9  | 9 | 9    | 1    | -9-6  | 9    | 84   | 71   | -5-4  | 9   | 98   | 129  | -3-2  | 9 | 555  | 537  |   |   |   |     |      |   |   |   |     |      |
| 1-11   | 9 | 91   | 62   | -14-8 | 9 | 8    | 1    | -8-6  | 9    | 139  | 150  | -4-4  | 9   | 2    | 8    | -2-2  | 9 | 556  | 536  |   |   |   |     |      |   |   |   |     |      |
| 2-11   | 9 | 6    | 16   | -13-8 | 9 | 46   | 34   | -7-6  | 9    | -1   | 3    | -3-4  | 9   | 179  | 212  | -1-2  | 9 | 2478 | 2495 |   |   |   |     |      |   |   |   |     |      |
| 3-11   | 9 | 105  | 105  | -12-8 | 9 | 30   | 25   | -6-6  | 9    | 17   | 12   | -2-4  | 9   | 425  | 404  | 0-2   | 9 | 749  | 753  |   |   |   |     |      |   |   |   |     |      |
| 4-11   | 9 | 189  | 157  | -11-8 | 9 | -1   | 1    | -5-6  | 9    | 643  | 612  | -1-4  | 9   | 2135 | 1965 | 1-2   | 9 | 78   | 105  |   |   |   |     |      |   |   |   |     |      |
| 5-11   | 9 | 23   | 29   | -10-8 | 9 | 185  | 161  | -4-6  | 9    | 19   | 9    | 0-4   | 9   | 446  | 386  | 2-2   | 9 | 312  | 312  |   |   |   |     |      |   |   |   |     |      |
| 6-11   | 9 | 22   | 20   | -9-8  | 9 | 158  | 125  | -3-6  | 9    | 70   | 78   | 1-4   | 9   | 56   | 47   | 3-2   | 9 | 694  | 681  |   |   |   |     |      |   |   |   |     |      |
| 7-11   | 9 | 87   | 71   | -8-8  | 9 | 45   | 50   | -2-6  | 9    | 1092 | 899  | 2-4   | 9   | 1170 | 1097 | 4-2   | 9 | 1074 | 1195 |   |   |   |     |      |   |   |   |     |      |
| 8-11   | 9 | 26   | 18   | -7-8  | 9 | 56   | 51   | -1-6  | 9    | 310  | 416  | 3-4   | 9   | 1393 | 1178 | 5-2   | 9 | 143  | 144  |   |   |   |     |      |   |   |   |     |      |
| 9-11   | 9 | 18   | 10   | -6-8  | 9 | 10   | 1    | 0-6   | 9    | 18   | 9    | 4-4   | 9   | 52   | 52   | 6-2   | 9 | 469  | 357  |   |   |   |     |      |   |   |   |     |      |
| 10-11  | 9 | 10   | 16   | -5-8  | 9 | 133  | 134  | 1-6   | 9    | 451  | 335  | 5-4   | 9   | 117  | 108  | 7-2   | 9 | 609  | 516  |   |   |   |     |      |   |   |   |     |      |
| 11-11  | 9 | 27   | 7    | -4-8  | 9 | 18   | 26   | 2-6   | 9    | 245  | 274  | 6-4   | 9   | 225  | 185  | 8-2   | 9 | 279  | 297  |   |   |   |     |      |   |   |   |     |      |
| 12-11  | 9 | -8   | 2    | -3-8  | 9 | 743  | 642  | 4-6   | 9    | 10   | 8    | 0-4   | 9   | 30   | 28   | 10-2  | 9 | 378  | 380  |   |   |   |     |      |   |   |   |     |      |
| -1-10  | 9 | 13   | 2    | -1-8  | 9 | 58   | 56   | 5-6   | 9    | 10   | 8    | 9-4   | 9   | 132  | 124  | 11-2  | 9 | 41   | 34   |   |   |   |     |      |   |   |   |     |      |
| -2-10  | 9 | 5    | 16   | 0-8   | 9 | 3    | 4    | 6-6   | 9    | 8    | 3    | 10-4  | 9   | 293  | 241  | 12-2  | 9 | -2   | 0    |   |   |   |     |      |   |   |   |     |      |
| -3-10  | 9 | 18   | 18   | 1-8   | 9 | 384  | 288  | 7-6   | 9    | 63   | 74   | 11-4  | 9   | 14   | 13   | 13-2  | 9 | 53   | 50   |   |   |   |     |      |   |   |   |     |      |
| -4-10  | 9 | 21   | 29   | 2-8   | 9 | 89   | 90   | 8-6   | 9    | 50   | 53   | 12-4  | 9   | 76   | 81   | -16-1 | 9 | -6   | 0    |   |   |   |     |      |   |   |   |     |      |
| -5-10  | 9 | 36   | 34   | 3-8   | 9 | 183  | 168  | 9-6   | 9    | 59   | 55   | 13-4  | 9   | 50   | 52   | -15-1 | 9 | -1   | 11   |   |   |   |     |      |   |   |   |     |      |
| -6-10  | 9 | 9    | 9    | 4-8   | 9 | 137  | 112  | 10-6  | 9    | 12   | 15   | 14-4  | 9   | 10   | 3    | -14-1 | 9 | -1   | 1    |   |   |   |     |      |   |   |   |     |      |
| -7-10  | 9 | 11   | 10   | 5-8   | 9 | 94   | 72   | 11-6  | 9    | 37   | 36   | -17-3 | 9   | -13  | 0    | -13-1 | 9 | -2   | 10   |   |   |   |     |      |   |   |   |     |      |
| -8-10  | 9 | 80   | 63   | 6-8   | 9 | -1   | 1    | 12-6  | 9    | 95   | 69   | -16-3 | 9   | 9    | 1    | -12-1 | 9 | 39   | 36   |   |   |   |     |      |   |   |   |     |      |
| -9-10  | 9 | 33   | 13   | 7-8   | 9 | 62   | 51   | 13-6  | 9    | 29   | 45   | -15-3 | 9   | 2    | 3    | -11-1 | 9 | 34   | 38   |   |   |   |     |      |   |   |   |     |      |
| -10-10 | 9 | 5    | 1    | -4-8  | 9 | 683  | 673  | 3-3   | 9    | 1853 | 1866 | -15-6 | 9   | -4   | 22   | -1-8  | 9 | 298  | 268  |   |   |   |     |      |   |   |   |     |      |
| -11-10 | 9 | 31   | 28   | -3-8  | 9 | 4    | 6    | 4-3   | 9    | 92   | 85   | -14-6 | 9   | 28   | 20   | 0-8   | 9 | 251  | 223  |   |   |   |     |      |   |   |   |     |      |
| -12-10 | 9 | 57   | 94   | -2-8  | 9 | 119  | 237  | 5-3   | 9    | 246  | 178  | -13-6 | 9   | 53   | 42   | 1-8   | 9 | 229  | 256  |   |   |   |     |      |   |   |   |     |      |
| -1-9   | 9 | 50   | 61   | -1-8  | 9 | 1976 | 1705 | 6-3   | 9    | 123  | 128  | -12-6 | 9   | 38   | 34   | 2-8   | 9 | 33   | 25   |   |   |   |     |      |   |   |   |     |      |
| -2-9   | 9 | 1    | 1    | 0-8   | 9 | 1414 | 1440 | 7-3   | 9    | 467  | 454  | -11-6 | 9   | 238  | 196  | 3-8   | 9 | 16   | 18   |   |   |   |     |      |   |   |   |     |      |
| -3-9   | 9 | 599  | 682  | 1-8   | 9 | 41   | 11   | 8-3   | 9    | 12   | 4    | -10-6 | 9   | 5    | 21   | 4-8   | 9 | 188  | 183  |   |   |   |     |      |   |   |   |     |      |
| -4-9   | 9 | 329  | 265  | 2-8   | 9 | 29   | 24   | 9-3   | 9    | 66   | 63   | -9-6  | 9   | 2    | 4    | 5-8   | 9 | 14   | 16   |   |   |   |     |      |   |   |   |     |      |
| -5-9   | 9 | 15   | 17   | 3-8   | 9 | 1562 | 1482 | 10-3  | 9    | 261  | 228  | -8-6  | 9   | 143  | 128  | 6-8   | 9 | 199  | 182  |   |   |   |     |      |   |   |   |     |      |
| -6-9   | 9 | 1248 | 1203 | 4-8   | 9 | 163  | 165  | 11-3  | 9    | 187  | 165  | -7-6  | 9   | 71   | 77   | 7-8   | 9 | 91   | 91   |   |   |   |     |      |   |   |   |     |      |
| -7-9   | 9 | 476  | 538  | 5-8   | 9 | 72   | 71   | 12-3  | 9    | 4    | 6    | -6-6  | 9   | 5    | 7    | 8-8   | 9 | -6   | 6    |   |   |   |     |      |   |   |   |     |      |
| -8-9   | 9 | 89   | 98   | 6-8   | 9 | 800  | 769  | -16-4 | 9    | 39   | 8    | -5-6  | 9   | 449  | 361  | 9-8   | 9 | 0    | 7    |   |   |   |     |      |   |   |   |     |      |
| -9-9   | 9 | 373  | 478  | 7-8   | 9 | 519  | 412  | -15-4 | 9    | 46   | 31   | -4-6  | 9   | 81   | 56   | -14-9 | 9 | 31   | 9    |   |   |   |     |      |   |   |   |     |      |
| -10-9  | 9 | 572  | 503  | 8-8   | 9 | 46   | 67   | -14-4 | 9    | 15   | 12   | -3-6  | 9   | 11   | 15   | -13-9 | 9 | 16   | 1    |   |   |   |     |      |   |   |   |     |      |
| -11-9  | 9 | 499  | 541  | 9-8   | 9 | 303  | 256  | -13-4 | 9    | 13   | 16   | -2-6  | 9   | 385  | 372  | -12-9 | 9 | 31   | 14   |   |   |   |     |      |   |   |   |     |      |
| -12-9  | 9 | 4    | 3    | 10-8  | 9 | 190  | 222  | -12-4 | 9    | 37   | 30   | -1-6  | 9   | 323  | 354  | -11-9 | 9 | 27   | 3    |   |   |   |     |      |   |   |   |     |      |
| -1-8   | 9 | 11   | 6    | 11-8  | 9 | 8    | 5    | -11-4 | 9    |      |      |       |     |      |      |       |   |      |      |   |   |   |     |      |   |   |   |     |      |

Table A.3, continued

| M   | K  | L | Obs  | Calc | M   | K   | L  | Obs | Calc | M   | K   | L  | Obs | Calc | M   | K   | L  | Obs | Calc | M   | K  | L  | Obs | Calc | M   | K  | L | Obs  | Calc |
|-----|----|---|------|------|-----|-----|----|-----|------|-----|-----|----|-----|------|-----|-----|----|-----|------|-----|----|----|-----|------|-----|----|---|------|------|
| 11  | 0  | 9 | 133  | 125  | -12 | 3   | 9  | 8   | 18   | -3  | 5   | 9  | 351 | 301  | 10  | 7   | 9  | 24  | 13   | 4   | 10 | 9  | 65  | 38   | 11  | 0  | 9 | 133  | 125  |
| 12  | 0  | 9 | 12   | 10   | -11 | 3   | 9  | 315 | 314  | -2  | 5   | 9  | 356 | 356  | -15 | 8   | 9  | -13 | 5    | 5   | 10 | 9  | 27  | 40   | 12  | 0  | 9 | 12   | 10   |
| 13  | 0  | 9 | 9    | 15   | -10 | 3   | 9  | 239 | 197  | -1  | 5   | 9  | 11  | 1    | -14 | 8   | 9  | 13  | 1    | 6   | 10 | 9  | -4  | 2    | 13  | 0  | 9 | 9    | 15   |
| -14 | 1  | 9 | 14   | 4    | -9  | 3   | 9  | 74  | 79   | 0   | 5   | 9  | 96  | 104  | -13 | 8   | 9  | 15  | 0    | 7   | 10 | 9  | 0   | 41   | -14 | 1  | 9 | 14   | 4    |
| -15 | 1  | 9 | 70   | 73   | -8  | 3   | 9  | 190 | 147  | 1   | 5   | 9  | 633 | 564  | -12 | 8   | 9  | -6  | 1    | -13 | 11 | 9  | -4  | 10   | -15 | 1  | 9 | 70   | 73   |
| -14 | 1  | 9 | 43   | 98   | -7  | 3   | 9  | 629 | 587  | 2   | 5   | 9  | 490 | 480  | -11 | 8   | 9  | 2   | 10   | -12 | 11 | 9  | -15 | 2    | -14 | 1  | 9 | 43   | 98   |
| -13 | 1  | 9 | -5   | 12   | -6  | 3   | 9  | 21  | 4    | 3   | 5   | 9  | 14  | 32   | -10 | 8   | 9  | 53  | 76   | -11 | 11 | 9  | 23  | 11   | -13 | 1  | 9 | -5   | 12   |
| -12 | 1  | 9 | 27   | 4    | -5  | 3   | 9  | 34  | 38   | 4   | 5   | 9  | 197 | 155  | -9  | 8   | 9  | 9   | 7    | -10 | 11 | 9  | 21  | 1    | -12 | 1  | 9 | 27   | 4    |
| -11 | 1  | 9 | 125  | 124  | -4  | 3   | 9  | 692 | 561  | 5   | 5   | 9  | 8   | 1    | -8  | 8   | 9  | 24  | 54   | -9  | 11 | 9  | 17  | 6    | -11 | 1  | 9 | 125  | 124  |
| -10 | 1  | 9 | 49   | 36   | -3  | 3   | 9  | 60  | 63   | 6   | 5   | 9  | 6   | 1    | -7  | 8   | 9  | 161 | 130  | -8  | 11 | 9  | 23  | 31   | -10 | 1  | 9 | 49   | 36   |
| -9  | 1  | 9 | 7    | 0    | -2  | 3   | 9  | -2  | 1    | 7   | 5   | 9  | 458 | 429  | -6  | 8   | 9  | 84  | 82   | -7  | 11 | 9  | 2   | 0    | -9  | 1  | 9 | 7    | 0    |
| -8  | 1  | 9 | 91   | 113  | -1  | 3   | 9  | 170 | 176  | 8   | 5   | 9  | 54  | 46   | -5  | 8   | 9  | 27  | 17   | -6  | 11 | 9  | 4   | 5    | -8  | 1  | 9 | 91   | 113  |
| -7  | 1  | 9 | 20   | 18   | 0   | 3   | 9  | 212 | 284  | 9   | 5   | 9  | -1  | 7    | -4  | 8   | 9  | 19  | 21   | -5  | 11 | 9  | 108 | 80   | -7  | 1  | 9 | 20   | 18   |
| -6  | 1  | 9 | 7    | 17   | 1   | 3   | 9  | 17  | 15   | 10  | 5   | 9  | 30  | 39   | -5  | 8   | 9  | 230 | 210  | -4  | 11 | 9  | 188 | 179  | -6  | 1  | 9 | 7    | 17   |
| -5  | 1  | 9 | 1813 | 1559 | 2   | 5   | 9  | 799 | 741  | 11  | 5   | 9  | 38  | 26   | -2  | 8   | 9  | 13  | 3    | -3  | 11 | 9  | 4   | 11   | -5  | 1  | 9 | 1813 | 1559 |
| -2  | 11 | 9 | 89   | 82   | -1  | 15  | 9  | -14 | 2    | 10  | -14 | 10 | 18  | 20   | 13  | -11 | 10 | -19 | 2    | 2   | -8 | 10 | 1   | 1    | -2  | 11 | 9 | 89   | 82   |
| -1  | 11 | 9 | 222  | 201  | 0   | 15  | 9  | 120 | 12   | 11  | -14 | 10 | -16 | 2    | -11 | -10 | 10 | 3   | 6    | 3   | -8 | 10 | 139 | 124  | -1  | 11 | 9 | 222  | 201  |
| 0   | 11 | 9 | 35   | 36   | 1   | 15  | 9  | 57  | 8    | -6  | -13 | 10 | -11 | 17   | -10 | -10 | 10 | -3  | 0    | 4   | -8 | 10 | 6   | 4    | 0   | 11 | 9 | 35   | 36   |
| 1   | 11 | 9 | -1   | 1    | 2   | 15  | 9  | -19 | 0    | -5  | -13 | 10 | 68  | 24   | -9  | -10 | 10 | 35  | 27   | 5   | -8 | 10 | 136 | 148  | 1   | 11 | 9 | -1   | 1    |
| 2   | 11 | 9 | 29   | 40   | 3   | 15  | 9  | -14 | 3    | -4  | -13 | 10 | -8  | 2    | -8  | -10 | 10 | 8   | 11   | 6   | -8 | 10 | 392 | 357  | 2   | 11 | 9 | 29   | 40   |
| 3   | 11 | 9 | 69   | 70   | 4   | 15  | 9  | 51  | 12   | -3  | -13 | 10 | -3  | 1    | -7  | -10 | 10 | -2  | 2    | 7   | -8 | 10 | 80  | 70   | 3   | 11 | 9 | 69   | 70   |
| 4   | 11 | 9 | 25   | 26   | -3  | 16  | 9  | -18 | 5    | -2  | -13 | 10 | 1   | 1    | -6  | -10 | 10 | -10 | 3    | 8   | -8 | 10 | 14  | 9    | 4   | 11 | 9 | 25   | 26   |
| 5   | 11 | 9 | 25   | 1    | -2  | 16  | 9  | 33  | 0    | -1  | -13 | 10 | 8   | 2    | -5  | -10 | 10 | 2   | 13   | 9   | -8 | 10 | 177 | 139  | 5   | 11 | 9 | 25   | 1    |
| 6   | 11 | 9 | 10   | 30   | -1  | 16  | 9  | 42  | 1    | 0   | -13 | 10 | -1  | 1    | -4  | -10 | 10 | 10  | 30   | 10  | -8 | 10 | 46  | 51   | 6   | 11 | 9 | 10   | 30   |
| 7   | 11 | 9 | 40   | 10   | 0   | 16  | 9  | -19 | 1    | 1   | -13 | 10 | 62  | 62   | -3  | -10 | 10 | 7   | 29   | 11  | -8 | 10 | 0   | 4    | 7   | 11 | 9 | 40   | 10   |
| -11 | 12 | 9 | 1    | 3    | -1  | 18  | 10 | -11 | 0    | 2   | -13 | 10 | 31  | 35   | -2  | -10 | 10 | 295 | 264  | 12  | -8 | 10 | 25  | 17   | -11 | 12 | 9 | 1    | 3    |
| -10 | 12 | 9 | -5   | 1    | 0   | -18 | 10 | 3   | 0    | 3   | -13 | 10 | 14  | 12   | -1  | -10 | 10 | 351 | 320  | 13  | -8 | 10 | 13  | 32   | -10 | 12 | 9 | -5   | 1    |
| -9  | 12 | 9 | -6   | 2    | 1   | -18 | 10 | -7  | 0    | 4   | -13 | 10 | 1   | 1    | 0   | -10 | 10 | 19  | 11   | -14 | -7 | 10 | 6   | 1    | -9  | 12 | 9 | -6   | 2    |
| -8  | 12 | 9 | 8    | 2    | 2   | -18 | 10 | -8  | 0    | 5   | -13 | 10 | 8   | 0    | 1   | -10 | 10 | 231 | 175  | -13 | -7 | 10 | -6  | 10   | -8  | 12 | 9 | 8    | 2    |
| -7  | 12 | 9 | 32   | 23   | 3   | -18 | 10 | 21  | 1    | 6   | -13 | 10 | 11  | 12   | 2   | -10 | 10 | 251 | 284  | -12 | -7 | 10 | 25  | 21   | -7  | 12 | 9 | 32   | 23   |
| -6  | 12 | 9 | 30   | 37   | 4   | -18 | 10 | 52  | 0    | 7   | -13 | 10 | 17  | 3    | 3   | -10 | 10 | 51  | 40   | -11 | -7 | 10 | 5   | 3    | -6  | 12 | 9 | 30   | 37   |
| -5  | 12 | 9 | 38   | 29   | 5   | -18 | 10 | 7   | 0    | 8   | -13 | 10 | 11  | 0    | 4   | -10 | 10 | 14  | 8    | -10 | -7 | 10 | 0   | 1    | -5  | 12 | 9 | 38   | 29   |
| -4  | 12 | 9 | 12   | 1    | 6   | -18 | 10 | 6   | 3    | 9   | -13 | 10 | 45  | 23   | 5   | -10 | 10 | 266 | 247  | -9  | -7 | 10 | 2   | 1    | -4  | 12 | 9 | 12   | 1    |
| -3  | 12 | 9 | 69   | 58   | 8   | -18 | 10 | -9  | 3    | 10  | -13 | 10 | 1   | 0    | 6   | -10 | 10 | 153 | 123  | -8  | -7 | 10 | 154 | 165  | -3  | 12 | 9 | 69   | 58   |
| -2  | 12 | 9 | 70   | 61   | -1  | -17 | 10 | -3  | 1    | 11  | -13 | 10 | -5  | 4    | 7   | -10 | 10 | 0   | 2    | -7  | -7 | 10 | 310 | 276  | -2  | 12 | 9 | 70   | 61   |
| -1  | 12 | 9 | 23   | 19   | 0   | -17 | 10 | -5  | 0    | 12  | -13 | 10 | 14  | 1    | 8   | -10 | 10 | 78  | 61   | -6  | -7 | 10 | 667 | 613  | -1  | 12 | 9 | 23   | 19   |
| 0   | 12 | 9 | -1   | 1    | 1   | -17 | 10 | 8   | 15   | -8  | -12 | 10 | -1  | 2    | 9   | -10 | 10 | 78  | 77   | -5  | -7 | 10 | 103 | 125  | 0   | 12 | 9 | -1   | 1    |
| 1   | 12 | 9 | 49   | 40   | 2   | -17 | 10 | 54  | 16   | -7  | -12 | 10 | 23  | 22   | 10  | -10 | 10 | 40  | 50   | -4  | -7 | 10 | 130 | 137  | 1   | 12 | 9 | 49   | 40   |
| 2   | 12 | 9 | 31   | 33   | 3   | -17 | 10 | 12  | 1    | -6  | -12 | 10 | 39  | 76   | 11  | -10 | 10 | -4  | 0    | -3  | -7 | 10 | 203 | 197  | 2   | 12 | 9 | 31   | 33   |
| 3   | 12 | 9 | 2    | 6    | 4   | -17 | 10 | 3   | 0    | -5  | -12 | 10 | -8  | 0    | 12  | -10 | 10 | 18  | 10   | -2  | -7 | 10 | 244 | 257  | 3   | 12 | 9 | 2    | 6    |
| 4   | 12 | 9 | 13   | 15   | 5   | -17 | 10 | -12 | 1    | -4  | -12 | 10 | 41  | 1    | 13  | -10 | 10 | 7   | 2    | -1  | -7 | 10 | 538 | 422  | 4   | 12 | 9 | 13   | 15   |
| 5   | 12 | 9 | -5   | 3    | 6   | -17 | 10 | 112 | 0    | -3  | -12 | 10 | 54  | 52   | -12 | -9  | 10 | 22  | 2    | 0   | -7 | 10 | 48  | 23   | 5   | 12 | 9 | -5   | 3    |
| 6   | 12 | 9 | 31   | 8    | 7   | -17 | 10 | 49  | 0    | -2  | -12 | 10 | 27  | 19   | -11 | -9  | 10 | 10  | 2    | 1   | -7 | 10 | 11  | 27   | 6   | 12 | 9 | 31   | 8    |
| -10 | 13 | 9 | 40   | 3    | 8   | -17 | 10 | -10 | 0    | -1  | -12 | 10 | 13  | 18   | -10 | -9  | 10 | 10  | 13   | 2   | -7 | 10 | 564 | 495  | -10 | 13 | 9 | 40   | 3    |
| -9  | 13 | 9 | 40   | 1    | 0   | -16 | 10 | 44  | 70   | 0   | -12 | 10 | 9   | 2    | -9  | -9  | 10 | 47  | 55   | 3   | -7 | 10 | 106 | 113  | -9  | 13 | 9 | 40   | 1    |
| -8  | 13 | 9 | 10   | 8    | 1   | -16 | 10 | 26  | 25   | 1   | -12 | 10 | 1   | 4    | -8  | -9  | 10 | 5   | 0    | 4   | -7 | 10 | 7   | 1    | -8  | 13 | 9 | 10   | 8    |
| -7  | 13 | 9 | -4   | 22   | 2   | -16 | 10 | -5  | 0    | 2   | -12 | 10 | 0   | 0    | -7  | -9  | 10 | 12  | 9    | 5   | -7 | 10 | -1  | 3    | -7  | 13 | 9 | -4   | 22   |
| -6  | 13 | 9 | -5   | 0    | 3   | -16 | 10 | -8  | 11   | 3   | -12 | 10 | 20  | 16   | -6  | -9  | 10 | 146 | 137  | 6   | -7 | 10 | 35  | 38   | -6  | 13 | 9 | -5   | 0    |
| -5  | 13 | 9 | 29   | 15   | 4   | -16 | 10 | 0   | 2    | 4   | -12 | 10 | 3   | 5    | -5  | -9  | 10 | 19  | 15   | 7   | -7 | 10 | 101 | 106  | -5  | 13 | 9 | 29   | 15   |
| -4  | 13 | 9 | 61   | 48   | 5   | -16 | 10 | -2  | 0    | 5   | -12 | 10 | 30  | 33   | -4  | -9  | 10 | -7  | 1    | 8   | -7 | 10 | 149 | 139  | -4  | 13 | 9 | 61   | 48   |
| -3  | 13 | 9 | 28   | 7    | 6   | -16 | 10 | 19  | 14   | 6   | -12 | 10 | -2  | 2    | -3  | -9  | 10 | 247 | 217  | 9   | -7 | 10 | 7   | 13   | -3  | 13 | 9 | 28   | 7    |
| -2  | 13 | 9 | 15   | 1    | 7   | -16 | 10 | 28  | 11   | 7   | -12 | 10 | 2   | 0    | -1  | -9  | 10 | -1  | 4    | 10  | -7 | 10 | 1   | 6    | -2  | 13 | 9 | 15   | 1    |
| -1  | 13 | 9 | 2    | 15   | 8   | -16 | 10 | 3   | 3    | 8   | -12 | 10 | 5   | 12   | 0   | -9  | 10 | 137 | 152  | 11  | -7 | 10 | 114 | 97   | -1  | 13 | 9 | 2    | 15   |
| 0   | 13 | 9 | 42   | 50   | 9   | -16 | 10 | 15  | 4    | 9   | -12 | 10 | 4   | 8    | 1   | -9  | 10 | 62  | 59   | 12  | -7 | 10 | 94  | 85   | 0   | 13 | 9 | 42   | 50   |
| 1   | 13 | 9 | 20   | 26   | -2  | -15 | 10 | 5   | 21   | 10  | -12 | 10 | 18  | 16   | 2   | -9  | 10 | 79  | 84   | 13  | -7 | 10 | -5  | 8    | 1   | 13 | 9 | 20   | 26   |
| 2   | 13 | 9 | 13   | 5    | -1  | -15 | 10 | 28  | 28   | 11  | -12 | 10 | 13  | 5    | 3   | -9  | 10 | 58  | 50   | -14 | -6 | 10 | 2   | 11   | 2   | 13 | 9 | 13   | 5    |
| 3   | 13 | 9 | 79   | 52   | 0   | -15 | 10 | 0   | 0    | 12  | -12 | 10 | 42  | 2    | 4   | -9  | 10 | 209 | 158  | -13 | -6 | 10 | 1   | 1    | 3   | 13 | 9 | 79   | 52   |
| 4   | 13 | 9 | 27   | 15   | 1   | -15 | 10 | 56  | 58   | 13  | -12 | 10 | -7  | 1    | 5   | -9  | 10 | 121 | 124  | -12 | -6 | 10 | -4  | 10   | 4   | 13 | 9 | 27   | 15   |
| 5   | 13 | 9 | 23   | 5    | 2   | -15 | 10 | 37  | 29   | -10 | -11 | 10 | 2   | 21   | 6   | -9  | 10 | 8   | 9    | -11 | -6 | 10 | 7   | 1    | 5   | 13 | 9 | 23   | 5    |
| 6   | 13 | 9 | 33   | 7    | 3   | -15 | 10 | 3   | 5    | -9  | -11 | 10 | 2   | 0    | 7   | -9  | 10 | 77  | 72   | -10 | -6 | 10 | -3  | 4    | 6   | 13 | 9 |      |      |

Table A.3, continued

| M   | K  | L  | Obe  | Calc | M   | K  | L  | Obe  | Calc | M   | K  | L  | Obe  | Calc | M   | K   | L  | Obe  | Calc |
|-----|----|----|------|------|-----|----|----|------|------|-----|----|----|------|------|-----|-----|----|------|------|
| 6   | -5 | 10 | 436  | 372  | 12  | -3 | 10 | 72   | 63   | -12 | 0  | 10 | 43   | 22   | -5  | 2   | 10 | 359  | 343  |
| 7   | -5 | 10 | 19   | 12   | 13  | -3 | 10 | 91   | 49   | -11 | 0  | 10 | 66   | 29   | -4  | 2   | 10 | 598  | 635  |
| 8   | -5 | 10 | 133  | 125  | -16 | -2 | 10 | 24   | 3    | -10 | 0  | 10 | 56   | 35   | -3  | 2   | 10 | 91   | 69   |
| 9   | -5 | 10 | 79   | 97   | -15 | -2 | 10 | -9   | 9    | -9  | 0  | 10 | 9    | 1    | -2  | 2   | 10 | -2   | 1    |
| 10  | -5 | 10 | 19   | 31   | -14 | -2 | 10 | 24   | 8    | -8  | 0  | 10 | 123  | 132  | -1  | 2   | 10 | 27   | 49   |
| 11  | -5 | 10 | 35   | 38   | -13 | -2 | 10 | 29   | 26   | -7  | 0  | 10 | 357  | 385  | 0   | 2   | 10 | 5    | 2    |
| 12  | -5 | 10 | 50   | 45   | -12 | -2 | 10 | 36   | 22   | -6  | 0  | 10 | 117  | 125  | 1   | 2   | 10 | -1   | 0    |
| 13  | -5 | 10 | -1   | 2    | -11 | -2 | 10 | 17   | 28   | -5  | 0  | 10 | 161  | 140  | 2   | 2   | 10 | 1153 | 1232 |
| -16 | -4 | 10 | 25   | 0    | -10 | -2 | 10 | 73   | 65   | -4  | 0  | 10 | 1043 | 1099 | 3   | 2   | 10 | 1079 | 971  |
| -15 | -4 | 10 | 8    | 5    | -9  | -2 | 10 | 84   | 84   | -3  | 0  | 10 | 1    | 0    | 4   | 2   | 10 | 372  | 439  |
| -14 | -4 | 10 | 27   | 33   | -8  | -2 | 10 | 45   | 81   | -2  | 0  | 10 | 563  | 525  | 5   | 2   | 10 | 8    | 18   |
| -13 | -4 | 10 | -3   | 17   | -7  | -2 | 10 | 12   | 11   | -1  | 0  | 10 | 548  | 553  | 6   | 2   | 10 | 453  | 415  |
| -12 | -4 | 10 | 98   | 94   | -6  | -2 | 10 | 519  | 523  | 0   | 0  | 10 | 170  | 167  | 7   | 2   | 10 | 243  | 224  |
| -11 | -4 | 10 | 41   | 30   | -5  | -2 | 10 | 18   | 34   | 1   | 0  | 10 | 40   | 49   | 8   | 2   | 10 | 1    | 0    |
| -10 | -4 | 10 | 133  | 126  | -4  | -2 | 10 | 29   | 27   | 2   | 0  | 10 | 725  | 742  | 9   | 2   | 10 | 358  | 314  |
| -9  | -4 | 10 | 70   | 71   | -3  | -2 | 10 | 1452 | 1386 | 3   | 12 | 10 | 217  | 210  | 10  | 2   | 10 | 165  | 164  |
| -8  | -4 | 10 | 5    | 5    | -2  | -2 | 10 | 18   | 12   | 4   | 0  | 10 | 11   | 15   | 11  | 2   | 10 | 79   | 89   |
| -7  | -4 | 10 | 171  | 153  | -1  | -2 | 10 | 10   | 10   | 5   | 0  | 10 | 158  | 122  | 12  | 2   | 10 | 83   | 7    |
| -6  | -4 | 10 | 192  | 179  | 0   | -2 | 10 | 3    | 1    | 6   | 0  | 10 | 67   | 52   | -16 | 3   | 10 | 12   | 6    |
| -5  | -4 | 10 | 79   | 72   | 1   | -2 | 10 | 997  | 1031 | 7   | 0  | 10 | 35   | 19   | -13 | 3   | 10 | -7   | 3    |
| -4  | -4 | 10 | 9    | 6    | 2   | -2 | 10 | 369  | 395  | 8   | 0  | 10 | 30   | 48   | -14 | 3   | 10 | 26   | 15   |
| -3  | -4 | 10 | 1531 | 1457 | 3   | -2 | 10 | 106  | 125  | 9   | 0  | 10 | 308  | 341  | -13 | 3   | 10 | 50   | 51   |
| -2  | -4 | 10 | 47   | 81   | 4   | -2 | 10 | 310  | 288  | 10  | 0  | 10 | 8    | 10   | -12 | 3   | 10 | 22   | 50   |
| -1  | -4 | 10 | 3    | 12   | 5   | -2 | 10 | 220  | 245  | 11  | 0  | 10 | 0    | 6    | -11 | 3   | 10 | -6   | 1    |
| 0   | -4 | 10 | 793  | 652  | 6   | -2 | 10 | -4   | 8    | 12  | 0  | 10 | 37   | 13   | -10 | 3   | 10 | 148  | 113  |
| 1   | -4 | 10 | 268  | 312  | 7   | -2 | 10 | 36   | 34   | 13  | 0  | 10 | -6   | 1    | -9  | 3   | 10 | 184  | 161  |
| 2   | -4 | 10 | 277  | 265  | 8   | -2 | 10 | 0    | 6    | -16 | 1  | 10 | 2    | 33   | -8  | 3   | 10 | 85   | 79   |
| 3   | -4 | 10 | 292  | 273  | 9   | -2 | 10 | 43   | 29   | -15 | 1  | 10 | -8   | 9    | -7  | 3   | 10 | 225  | 164  |
| 4   | -4 | 10 | 149  | 145  | 10  | -2 | 10 | -5   | 0    | -14 | 1  | 10 | 8    | 0    | -6  | 3   | 10 | 149  | 121  |
| 5   | -4 | 10 | 450  | 402  | 11  | -2 | 10 | 130  | 110  | -13 | 1  | 10 | 17   | 17   | -5  | 3   | 10 | 39   | 37   |
| 6   | -4 | 10 | 41   | 32   | 12  | -2 | 10 | 34   | 39   | -12 | 1  | 10 | -1   | 1    | -4  | 3   | 10 | 29   | 25   |
| 7   | -4 | 10 | 227  | 220  | 13  | -2 | 10 | 4    | 1    | -11 | 1  | 10 | 121  | 104  | -3  | 3   | 10 | 334  | 275  |
| 8   | -4 | 10 | 55   | 54   | -16 | -1 | 10 | -8   | 2    | -10 | 1  | 10 | 51   | 44   | -2  | 3   | 10 | 50   | 44   |
| 9   | -4 | 10 | 2    | 4    | -15 | -1 | 10 | 7    | 12   | -9  | 1  | 10 | 77   | 82   | -1  | 3   | 10 | 182  | 156  |
| 10  | -4 | 10 | 58   | 55   | -14 | -1 | 10 | 11   | 17   | -8  | 1  | 10 | 834  | 708  | 0   | 3   | 10 | 448  | 372  |
| 11  | -4 | 10 | 88   | 91   | -13 | -1 | 10 | 51   | 40   | -7  | 1  | 10 | 19   | 28   | 1   | 3   | 10 | 284  | 329  |
| 12  | -4 | 10 | 5    | 3    | -12 | -1 | 10 | 16   | 4    | -6  | 1  | 10 | 496  | 502  | 2   | 3   | 10 | 56   | 21   |
| 13  | -4 | 10 | -10  | 5    | -11 | -1 | 10 | 56   | 49   | -5  | 1  | 10 | -3   | 1    | 3   | 3   | 10 | 1280 | 1077 |
| -16 | -3 | 10 | 37   | 1    | -10 | -1 | 10 | 186  | 173  | -4  | 1  | 10 | 172  | 172  | 4   | 1   | 10 | 56   | 56   |
| -15 | -3 | 10 | 14   | 26   | -9  | -1 | 10 | 4    | 11   | -3  | 1  | 10 | 770  | 783  | 5   | 3   | 10 | 601  | 600  |
| -14 | -3 | 10 | 19   | 11   | -8  | -1 | 10 | 85   | 67   | -2  | 1  | 10 | 788  | 813  | 6   | 3   | 10 | 35   | 37   |
| -13 | -3 | 10 | -1   | 3    | -7  | -1 | 10 | 0    | 5    | -1  | 1  | 10 | 535  | 455  | 7   | 3   | 10 | 79   | 70   |
| -12 | -3 | 10 | 68   | 60   | -6  | -1 | 10 | -1   | 6    | 0   | 1  | 10 | 119  | 118  | 8   | 3   | 10 | 155  | 160  |
| -4  | 6  | 10 | 13   | 19   | -11 | 9  | 10 | 5    | 13   | -2  | 12 | 10 | 38   | 9    | 7   | -16 | 11 | 27   | 7    |
| -3  | 6  | 10 | 389  | 320  | -10 | 9  | 10 | 9    | 18   | -1  | 12 | 10 | 48   | 62   | 8   | -16 | 11 | -10  | 7    |
| -2  | 6  | 10 | 451  | 428  | -9  | 9  | 10 | -7   | 0    | 0   | 12 | 10 | 68   | 61   | -2  | -15 | 11 | 31   | 18   |
| -1  | 6  | 10 | -2   | 0    | -8  | 9  | 10 | 8    | 12   | 1   | 12 | 10 | 7    | 9    | -1  | -15 | 11 | -6   | 2    |
| 0   | 6  | 10 | 469  | 507  | -7  | 9  | 10 | 3    | 1    | 2   | 12 | 10 | 36   | 15   | 0   | -15 | 11 | 14   | 7    |
| 1   | 6  | 10 | 919  | 849  | -6  | 9  | 10 | 8    | 1    | 3   | 12 | 10 | 102  | 85   | 1   | -15 | 11 | -4   | 0    |
| 2   | 6  | 10 | 915  | 852  | -5  | 9  | 10 | 5    | 8    | 4   | 12 | 10 | 54   | 31   | 2   | -15 | 11 | 28   | 23   |
| 3   | 6  | 10 | 133  | 141  | -4  | 9  | 10 | 75   | 88   | 5   | 12 | 10 | 14   | 0    | 3   | -15 | 11 | 5    | 15   |
| 4   | 6  | 10 | 223  | 225  | -3  | 9  | 10 | 128  | 140  | -9  | 13 | 10 | 51   | 27   | 4   | -15 | 11 | 26   | 17   |
| 5   | 6  | 10 | 149  | 161  | -2  | 9  | 10 | 2    | 7    | -8  | 13 | 10 | 7    | 4    | 5   | -15 | 11 | 0    | 0    |
| 6   | 6  | 10 | 36   | 29   | -1  | 9  | 10 | 40   | 36   | -7  | 13 | 10 | 13   | 0    | 6   | -15 | 11 | 0    | 7    |
| 7   | 6  | 10 | 123  | 116  | 0   | 9  | 10 | 26   | 20   | -6  | 13 | 10 | 18   | 6    | 7   | -15 | 11 | -1   | 9    |
| 8   | 6  | 10 | 143  | 138  | 1   | 9  | 10 | 3    | 2    | -5  | 13 | 10 | -5   | 4    | 8   | -15 | 11 | -8   | 0    |
| 9   | 6  | 10 | 14   | 0    | 2   | 9  | 10 | 7    | 3    | -4  | 13 | 10 | -8   | 4    | -4  | -14 | 11 | 0    | 9    |
| 10  | 6  | 10 | 17   | 22   | 3   | 9  | 10 | 104  | 103  | -3  | 13 | 10 | 12   | 7    | -3  | -14 | 11 | -8   | 3    |
| -15 | 7  | 10 | -12  | 9    | 4   | 9  | 10 | 67   | 56   | -2  | 13 | 10 | 8    | 28   | -2  | -14 | 11 | -8   | 1    |
| -14 | 7  | 10 | -8   | 8    | 5   | 9  | 10 | 1    | 4    | -1  | 13 | 10 | 8    | 11   | -1  | -14 | 11 | -8   | 0    |
| -13 | 7  | 10 | 13   | 16   | 6   | 9  | 10 | 128  | 143  | 0   | 13 | 10 | -2   | 9    | 0   | -14 | 11 | 37   | 20   |
| -12 | 7  | 10 | 28   | 15   | 7   | 9  | 10 | -7   | 28   | 1   | 13 | 10 | 40   | 40   | 1   | -14 | 11 | 35   | 44   |
| -11 | 7  | 10 | 11   | 17   | -13 | 10 | 10 | -17  | 0    | 2   | 13 | 10 | 45   | 35   | 2   | -14 | 11 | 47   | 40   |
| -10 | 7  | 10 | -4   | 1    | -12 | 10 | 10 | 28   | 8    | 3   | 13 | 10 | 25   | 2    | 3   | -14 | 11 | 9    | 8    |
| -9  | 7  | 10 | 21   | 37   | -11 | 10 | 10 | 14   | 6    | 4   | 13 | 10 | -12  | 1    | 4   | -14 | 11 | 3    | 3    |
| -8  | 7  | 10 | 61   | 56   | -10 | 10 | 10 | -7   | 3    | 5   | 13 | 10 | 3    | 11   | 5   | -14 | 11 | -1   | 4    |
| -7  | 7  | 10 | 30   | 36   | -9  | 10 | 10 | -8   | 9    | -8  | 14 | 10 | 83   | 1    | 6   | -14 | 11 | -3   | 2    |
| -6  | 7  | 10 | 15   | 11   | -8  | 10 | 10 | 39   | 23   | -7  | 14 | 10 | -13  | 3    | 7   | -14 | 11 | 10   | 6    |
| -5  | 7  | 10 | 207  | 174  | -7  | 10 | 10 | 2    | 2    | -6  | 14 | 10 | -11  | 1    | 8   | -14 | 11 | 14   | 35   |
| -4  | 7  | 10 | 70   | 83   | -6  | 10 | 10 | 23   | 27   | -5  | 14 | 10 | 12   | 6    | 9   | -14 | 11 | 22   | 26   |
| -3  | 7  | 10 | 307  | 318  | -5  | 10 | 10 | 105  | 89   | -4  | 14 | 10 | 72   | 16   | -6  | -13 | 11 | -13  | 0    |
| -2  | 7  | 10 | 0    | 6    | -4  | 10 | 10 | 77   | 88   | -3  | 14 | 10 | 50   | 28   | -5  | -13 | 11 | 4    | 2    |
| -1  | 7  | 10 | 366  | 337  | -3  | 10 | 10 | 94   | 30   | -2  | 14 | 10 | 2    | 4    | -4  | -13 | 11 | 1    | 6    |
| 0   | 7  | 10 | 861  | 828  | -2  | 10 | 10 | 57   | 37   | -1  | 14 | 10 | -7   | 6    | -3  | -13 | 11 | 26   | 9    |
| 1   | 7  | 10 | 970  | 828  | -1  | 10 | 10 | 75   | 73   | 0   | 14 | 10 | -1   | 18   | -2  | -13 | 11 | 80   | 41   |
| 2   | 7  | 10 | 234  | 241  | 0   | 10 | 10 | 12   | 7    | 1   | 14 | 10 | -2   | 3    | -1  | -13 | 11 | 2    | 0    |
| 3   | 7  | 10 | 35   | 18   | 1   | 10 | 10 | 6    | 13   | 2   | 14 | 10 | 23   | 2    | 0   | -13 | 11 | 11   | 8    |
| 4   | 7  | 10 | -2   | 4    | 2   | 10 | 10 | 89   | 82   | 3   | 14 | 10 | 45   | 17   | 1   | -13 | 11 | 2    | 0    |
| 5   | 7  | 10 | 16   | 12   | 3   | 10 | 10 | 58   | 55   | 4   | 14 | 10 | -41  | 13   | 2   | -13 | 11 | 10   | 11   |
| 6   | 7  | 10 | 138  | 142  | 4   | 10 | 10 | 1    | 0    | -6  | 15 | 10 | -13  | 11   | 3   | -13 | 11 | -1   | 3    |
| 7   | 7  | 10 | 137  | 117  | 5   | 10 | 10 | 25   | 26   | -5  | 15 | 10 | 57   | 37   | 4   | -13 | 11 | 16   | 9    |
| 8   | 7  | 10 | 1    | 0    | 6   | 10 | 10 | 12   | 4    | -4  | 15 | 10 | 33   | 32   | 5   | -13 | 11 | 20   | 15   |
| 9   | 7  | 10 | 30   | 46   | -12 | 11 | 10 | -10  | 12   | -3  | 15 | 10 | 38   | 4    | 6   | -13 | 11 | 3    | 0    |
| -14 | 8  | 10 | -1   | 7    | -11 | 11 | 10 | -17  | 1    | -2  | 15 | 10 | 0    | 2    | 7   | -13 | 11 | 16   | 18   |
| -13 | 8  | 10 | -5   | 2    | -10 | 11 | 10 | 21   | 4    | -1  | 15 | 10 | -9   | 2    | 8   | -13 | 11 | 19   | 29   |
| -12 | 8  | 10 | 9    | 7    | -9  | 11 | 10 | 13   | 16   | 0   | 15 | 10 | 16   | 0    | 9   | -13 | 11 | 12   | 14   |
| -11 | 8  | 10 | 1    | 10   | -8  | 11 | 10 | 9    | 9    | 1   | 15 | 10 | 43   | 0    | 10  | -13 | 11 | 5    | 4    |
| -10 | 8  | 10 | 51   | 45   | -7  | 11 | 10 | 8    | 8    | 2   | 15 | 10 | -9   | 9</  |     |     |    |      |      |

Table A.3, continued

| M   | K  | L  | Obs | Calc | M   | K  | L  | Obs  | Calc | M    | K  | L   | Obs  | Calc  | M   | K  | L  | Obs  | Calc | M   | K   | L   | Obs  | Calc |
|-----|----|----|-----|------|-----|----|----|------|------|------|----|-----|------|-------|-----|----|----|------|------|-----|-----|-----|------|------|
| 7   | 8  | 10 | 45  | 41   | -7  | 12 | 10 | 5    | 12   | 2-16 | 11 | 29  | 18   | 9-12  | 11  | 17 | 12 | 5    | -9   | 11  | 224 | 184 |      |      |
| 8   | 8  | 10 | 95  | 84   | -6  | 12 | 10 | -7   | 2    | 3-16 | 11 | 18  | 2    | 10-12 | 11  | 56 | 48 | 6    | -9   | 11  | 135 | 122 |      |      |
| -14 | 9  | 10 | 36  | 0    | -5  | 12 | 10 | 20   | 17   | 4-16 | 11 | 9   | 1    | 11-12 | 11  | 8  | 22 | 7    | -9   | 11  | 6   | 6   |      |      |
| -13 | 9  | 10 | -10 | 5    | -4  | 12 | 10 | 56   | 59   | 5-16 | 11 | -8  | 0    | 12-12 | 11  | -1 | 3  | 8    | -9   | 11  | 5   | 9   |      |      |
| -12 | 9  | 10 | 17  | 0    | -3  | 12 | 10 | 13   | 8    | 6-16 | 11 | -11 | 2    | -8-11 | 11  | 16 | 20 | 9    | -9   | 11  | 15  | 19  |      |      |
| 10  | -9 | 11 | 39  | 13   | -5  | -6 | 11 | 637  | 536  | 3    | -4 | 11  | 223  | 230   | 9   | -2 | 11 | 97   | 73   | -13 | 1   | 11  | 10   |      |
| 11  | -7 | 11 | 18  | 4    | -4  | -6 | 11 | 56   | 77   | 4    | -4 | 11  | 96   | 99    | 10  | -2 | 11 | 214  | 255  | -12 | 1   | 11  | 18   |      |
| 12  | -9 | 11 | 2   | 13   | -3  | -6 | 11 | 61   | 54   | 5    | -4 | 11  | 6    | 3     | 11  | -2 | 11 | -8   | 0    | -11 | 1   | 11  | 8    |      |
| 13  | -9 | 11 | -17 | 8    | -2  | -6 | 11 | 1702 | 1391 | 6    | -4 | 11  | 140  | 140   | 12  | -2 | 11 | 37   | 7    | -10 | 1   | 11  | 6    |      |
| -12 | -9 | 11 | 16  | 4    | -1  | -6 | 11 | 3    | 23   | 7    | -4 | 11  | 86   | 79    | 13  | -2 | 11 | 11   | 20   | -9  | 1   | 11  | 3    |      |
| -11 | -9 | 11 | 30  | 27   | 0   | -6 | 11 | 26   | 14   | 8    | -4 | 11  | 15   | 9     | -16 | -1 | 11 | 11   | 21   | -8  | 1   | 11  | 1202 |      |
| -10 | -9 | 11 | 3   | 3    | 1   | -6 | 11 | 37   | 23   | 9    | -4 | 11  | 42   | 38    | -15 | -1 | 11 | 10   | 8    | -7  | 1   | 11  | 761  |      |
| -9  | -9 | 11 | 5   | 0    | 2   | -6 | 11 | -1   | 1    | 10   | -4 | 11  | 106  | 90    | -14 | -1 | 11 | 0    | 1    | -6  | 1   | 11  | -4   |      |
| -8  | -9 | 11 | 8   | 3    | 3   | -6 | 11 | 5    | 7    | 11   | -4 | 11  | 1    | 5     | -13 | -1 | 11 | 27   | 25   | -5  | 1   | 11  | 624  |      |
| -7  | -9 | 11 | 78  | 131  | 4   | -6 | 11 | 365  | 363  | 12   | -4 | 11  | 2    | 24    | -12 | -1 | 11 | 46   | 42   | -4  | 1   | 11  | 834  |      |
| -6  | -9 | 11 | 120 | 90   | 5   | -6 | 11 | 419  | 403  | 13   | -4 | 11  | -7   | 22    | -11 | -1 | 11 | 36   | 6    | -3  | 1   | 11  | 140  |      |
| -5  | -9 | 11 | 28  | 27   | 6   | -6 | 11 | 113  | 87   | -16  | -3 | 11  | 7    | 10    | -10 | -1 | 11 | 55   | 49   | -2  | 1   | 11  | 161  |      |
| -4  | -9 | 11 | 27  | 71   | 7   | -6 | 11 | 74   | 72   | -15  | -3 | 11  | -7   | 0     | -9  | -1 | 11 | 8    | 18   | -1  | 1   | 11  | 82   |      |
| -3  | -9 | 11 | 69  | 44   | 8   | -6 | 11 | 162  | 134  | -14  | -3 | 11  | 0    | 10    | -8  | -1 | 11 | 15   | 1    | 0   | 1   | 11  | 263  |      |
| -2  | -9 | 11 | 463 | 468  | 9   | -6 | 11 | 20   | 36   | -13  | -3 | 11  | 26   | 41    | -7  | -1 | 11 | 2    | 1    | 1   | 1   | 11  | 2    |      |
| -1  | -9 | 11 | 50  | 50   | 10  | -6 | 11 | 20   | 12   | -12  | -3 | 11  | 29   | 31    | -6  | -1 | 11 | 462  | 417  | 2   | 1   | 11  | 2385 |      |
| 0   | -9 | 11 | -4  | 4    | 11  | -6 | 11 | -1   | 17   | -11  | -3 | 11  | -3   | 6     | -5  | -1 | 11 | 271  | 265  | 3   | 1   | 11  | 107  |      |
| 1   | -9 | 11 | 338 | 252  | 12  | -6 | 11 | 32   | 33   | -10  | -3 | 11  | 146  | 116   | -4  | -1 | 11 | -2   | 12   | 4   | 1   | 11  | 0    |      |
| 2   | -9 | 11 | 41  | 27   | 13  | -6 | 11 | 2    | 12   | -9   | -3 | 11  | 10   | 6     | -3  | -1 | 11 | 24   | 7    | 5   | 1   | 11  | 121  |      |
| 3   | -9 | 11 | 29  | 27   | -15 | -5 | 11 | 9    | 3    | -8   | -3 | 11  | 19   | 19    | -2  | -1 | 11 | 568  | 518  | 6   | 1   | 11  | 526  |      |
| 4   | -9 | 11 | 134 | 125  | -14 | -5 | 11 | 18   | 25   | -7   | -3 | 11  | 26   | 18    | -1  | -1 | 11 | 28   | 44   | 7   | 1   | 11  | 69   |      |
| 5   | -9 | 11 | -2  | 1    | -13 | -5 | 11 | 26   | 20   | -6   | -3 | 11  | 107  | 87    | 0   | -1 | 11 | 6    | 0    | 8   | 1   | 11  | 16   |      |
| 6   | -9 | 11 | -1  | 1    | -12 | -5 | 11 | 15   | 26   | -5   | -3 | 11  | 4    | 9     | 1   | -1 | 11 | 814  | 767  | 9   | 1   | 11  | 209  |      |
| 7   | -9 | 11 | 119 | 99   | -11 | -5 | 11 | 49   | 54   | -4   | -3 | 11  | 103  | 99    | 2   | -1 | 11 | 380  | 376  | 10  | 1   | 11  | 71   |      |
| 8   | -9 | 11 | 44  | 48   | -10 | -5 | 11 | 77   | 57   | -3   | -3 | 11  | 464  | 428   | 3   | -1 | 11 | 28   | 25   | 11  | 1   | 11  | 30   |      |
| 9   | -9 | 11 | 16  | 9    | -9  | -5 | 11 | 20   | 27   | -2   | -3 | 11  | 74   | 73    | 4   | -1 | 11 | 1    | 3    | 12  | 1   | 11  | -15  |      |
| 10  | -9 | 11 | 3   | 1    | -8  | -5 | 11 | 7    | 6    | -1   | -3 | 11  | 380  | 375   | 5   | -1 | 11 | 34   | 14   | -16 | 2   | 11  | -10  |      |
| 11  | -9 | 11 | 19  | 23   | -7  | -5 | 11 | 123  | 123  | 0    | -3 | 11  | 50   | 65    | 6   | -1 | 11 | 45   | 68   | -15 | 2   | 11  | -1   |      |
| 12  | -9 | 11 | 19  | 3    | -6  | -5 | 11 | 0    | 7    | 1    | -3 | 11  | 1561 | 1431  | 7   | -1 | 11 | 241  | 303  | -14 | 2   | 11  | 16   |      |
| 13  | -9 | 11 | 33  | 15   | -5  | -5 | 11 | 3    | 2    | 2    | -3 | 11  | 44   | 38    | 8   | -1 | 11 | 270  | 299  | -13 | 2   | 11  | 73   |      |
| -13 | -7 | 11 | -2  | 1    | -4  | -5 | 11 | 56   | 64   | 3    | -3 | 11  | 4    | 3     | 9   | -1 | 11 | 507  | 472  | -12 | 2   | 11  | 21   |      |
| -12 | -7 | 11 | 15  | 22   | -3  | -5 | 11 | 374  | 350  | 4    | -3 | 11  | 321  | 344   | 10  | -1 | 11 | -4   | 1    | -11 | 2   | 11  | 35   |      |
| -11 | -7 | 11 | 2   | 3    | -2  | -5 | 11 | 34   | 14   | 5    | -3 | 11  | 50   | 29    | 11  | -1 | 11 | 41   | 42   | -10 | 2   | 11  | 83   |      |
| -10 | -7 | 11 | 18  | 24   | -1  | -5 | 11 | 543  | 513  | 6    | -3 | 11  | 4    | 9     | 12  | -1 | 11 | 95   | 45   | -9  | 2   | 11  | 106  |      |
| -9  | -7 | 11 | 139 | 131  | 0   | -5 | 11 | 188  | 204  | 7    | -3 | 11  | 89   | 77    | -16 | 0  | 11 | 91   | 13   | -8  | 2   | 11  | 91   |      |
| -8  | -7 | 11 | 240 | 198  | 1   | -5 | 11 | 738  | 589  | 8    | -3 | 11  | 35   | 31    | -15 | 0  | 11 | 16   | 1    | -7  | 1   | 11  | 960  |      |
| -7  | -7 | 11 | 75  | 81   | 2   | -5 | 11 | 40   | 23   | 9    | -3 | 11  | 207  | 166   | -14 | 0  | 11 | 25   | 4    | -6  | 2   | 11  | 86   |      |
| -6  | -7 | 11 | 22  | 55   | 3   | -5 | 11 | 104  | 123  | 10   | -3 | 11  | 11   | 9     | -13 | 0  | 11 | 36   | 28   | -5  | 2   | 11  | 123  |      |
| -5  | -7 | 11 | 297 | 262  | 4   | -5 | 11 | 577  | 562  | 11   | -3 | 11  | 111  | 91    | -12 | 0  | 11 | -4   | 0    | -4  | 2   | 11  | 250  |      |
| -4  | -7 | 11 | 257 | 224  | 5   | -5 | 11 | 18   | 9    | 12   | -3 | 11  | 14   | 22    | -11 | 0  | 11 | 87   | 71   | -3  | 2   | 11  | 212  |      |
| -3  | -7 | 11 | 21  | 9    | 6   | -5 | 11 | 28   | 33   | 13   | -3 | 11  | -11  | 0     | -10 | 0  | 11 | 114  | 113  | -2  | 2   | 11  | 311  |      |
| -2  | -7 | 11 | 36  | 54   | 7   | -5 | 11 | 396  | 375  | -16  | -2 | 11  | 8    | 0     | -9  | 0  | 11 | 103  | 84   | -1  | 2   | 11  | 10   |      |
| -1  | -7 | 11 | 274 | 255  | 8   | -5 | 11 | 10   | 2    | -15  | -2 | 11  | 18   | 11    | -8  | 0  | 11 | 131  | 150  | 0   | 2   | 11  | 64   |      |
| 0   | -7 | 11 | 12  | 13   | 9   | -5 | 11 | 5    | 1    | -14  | -2 | 11  | 21   | 8     | -7  | 0  | 11 | 395  | 412  | 1   | 2   | 11  | 518  |      |
| 1   | -7 | 11 | 76  | 67   | 10  | -5 | 11 | 72   | 56   | -13  | -2 | 11  | -6   | 0     | -6  | 0  | 11 | 54   | 35   | 2   | 2   | 11  | 750  |      |
| 2   | -7 | 11 | 3   | 1    | 11  | -5 | 11 | 7    | 11   | -12  | -2 | 11  | 12   | 9     | -5  | 0  | 11 | 18   | 28   | 3   | 2   | 11  | 475  |      |
| 3   | -7 | 11 | -1  | 4    | 12  | -5 | 11 | 8    | 0    | -11  | -2 | 11  | 140  | 109   | -4  | 1  | 11 | 270  | 270  | 4   | 2   | 11  | 449  |      |
| 4   | -7 | 11 | 33  | 39   | 13  | -5 | 11 | 17   | 2    | -10  | -2 | 11  | 20   | 29    | 3   | 0  | 11 | 277  | 269  | 5   | 2   | 11  | 164  |      |
| 5   | -7 | 11 | 177 | 171  | -15 | -4 | 11 | 37   | 12   | -9   | -2 | 11  | -2   | 3     | -2  | 0  | 11 | 42   | 24   | 6   | 2   | 11  | 73   |      |
| 6   | -7 | 11 | 194 | 200  | -14 | -4 | 11 | -7   | 0    | -8   | -2 | 11  | 213  | 202   | -1  | 0  | 11 | 132  | 124  | 7   | 2   | 11  | 165  |      |
| 7   | -7 | 11 | 78  | 72   | -13 | -4 | 11 | -2   | 4    | -7   | -2 | 11  | 48   | 53    | 0   | 0  | 11 | 401  | 444  | 8   | 2   | 11  | 143  |      |
| 8   | -7 | 11 | 78  | 82   | -12 | -4 | 11 | 26   | 31   | -6   | -2 | 11  | 355  | 324   | 1   | 0  | 11 | 1462 | 1327 | 9   | 2   | 11  | 40   |      |
| 9   | -7 | 11 | 62  | 67   | -11 | -4 | 11 | 121  | 112  | -5   | -2 | 11  | 1185 | 1147  | 2   | 0  | 11 | 175  | 156  | 10  | 2   | 11  | 4    |      |
| 10  | -7 | 11 | 110 | 102  | -10 | -4 | 11 | 5    | 3    | -4   | -2 | 11  | 930  | 934   | 3   | 0  | 11 | 1887 | 1781 | 11  | 2   | 11  | 43   |      |
| 11  | -7 | 11 | 0   | 1    | -9  | -4 | 11 | 12   | 1    | -3   | -2 | 11  | 103  | 110   | 4   | 0  | 11 | 309  | 249  | -15 | 3   | 11  | -7   |      |
| 12  | -7 | 11 | 9   | 24   | -8  | -4 | 11 | 94   | 85   | -2   | -2 | 11  | 89   | 102   | 5   | 0  | 11 | 26   | 33   | -14 | 3   | 11  | 69   |      |
| 13  | -7 | 11 | 23  | 35   | -7  | -4 | 11 | -2   | 0    | -1   | -2 | 11  | 94   | 87    | 6   | 0  | 11 | 789  | 723  | -13 | 3   | 11  | -7   |      |
| -14 | -6 | 11 | 6   | 3    | -6  | -4 | 11 | 90   | 115  | 0    | -2 | 11  | 339  | 289   | 7   | 0  | 11 | 483  | 542  | -12 | 3   | 11  | 0    |      |
| -13 | -6 | 11 | 32  | 14   | -5  | -4 | 11 | 193  | 184  | -3   | -2 | 11  | 42   | 57    | 8   | 0  | 11 | 63   | 50   | -11 | 3   | 11  | 124  |      |
| -12 | -6 | 11 | 67  | 67   | -4  | -4 | 11 | 199  | 191  | 2    | -2 | 11  | 137  | 132   | 9   | 0  | 11 | 3    | 3    | -10 | 3   | 11  | -5   |      |
| -11 | -6 | 11 | 36  | 30   | -3  | -4 | 11 | 88   | 92   | 3    | -2 | 11  | 311  | 253   | 10  | 0  | 11 | 116  | 110  | -9  | 3   | 11  | 95   |      |
| -10 | -6 | 11 | 118 | 105  | -2  | -4 | 11 | 791  | 697  | 4    | -2 | 11  | 429  | 384   | 11  | 0  | 11 | 41   | 41   | -8  | 3   | 11  | 654  |      |
| -9  | -6 | 11 | 34  | 35   | -1  | -4 | 11 | 95   | 115  | 5    | -2 | 11  | -3   | 8     | 12  | 0  | 11 | -7   | 1    | -7  | 3   | 11  | 100  |      |
| -8  | -6 | 11 | 93  | 92   | 0   | -4 | 11 | 428  | 378  | 6    | -2 | 11  | 343  | 257   | -16 | 1  | 11 | 3    | 10   | -6  | 3   | 11  | 46   |      |
| -7  | -6 | 11 | 9   | 5    | 1   | -4 | 11 | 26   | 28   | 7    | -2 | 11  | 67   | 50    | -15 | 1  | 11 | 13   | 19   | -5  | 3   | 11  | 403  |      |
| -6  | -6 | 11 | 101 | 92   | 2   | -4 | 11 | 377  | 410  | 8    | -2 | 11  | 114  | 77    | -14 | 1  | 11 | 71   | 43   | -4  | 3   | 11  | 622  |      |
| -5  | -6 | 11 | 216 | 192  | 10  | 5  | 11 | 25   | 22   | 5    | 8  | 11  | 47   | 30    | -2  | 12 | 11 | 15   | 24   | -4  | -14 | 12  | -11  |      |
| -4  | -6 | 11 | 5   | 3    | -14 | 6  | 11 | -4   | 2    | 6    | 8  | 11  | 150  | 184   | -1  | 12 | 11 | -5   | 3    | -3  | -14 | 12  | 34   |      |
| -3  | -6 | 11 | 287 | 264  | -13 | 6  | 11 | 35   |      |      |    |     |      |       |     |    |    |      |      |     |     |     |      |      |

Table A.3, continued

| H   | K   | L  | Obs | Calc | H   | K  | L  | Obs | Calc | H   | K  | L  | Obs | Calc | H   | K   | L  | Obs | Calc  | H     | K    | L   | Obs  | Calc | H | K | L | Obs | Calc |   |   |   |
|-----|-----|----|-----|------|-----|----|----|-----|------|-----|----|----|-----|------|-----|-----|----|-----|-------|-------|------|-----|------|------|---|---|---|-----|------|---|---|---|
| -   | -   | -  | -   | -    | -   | -  | -  | -   | -    | -   | -  | -  | -   | -    | -   | -   | -  | -   | -     | -     | -    | -   | -    | -    | - | - | - | -   | -    |   |   |   |
| 3   | 4   | 11 | 87  | 76   | -6  | 7  | 11 | 107 | 93   | -2  | 10 | 11 | 16  | 17   | -4  | 15  | 11 | 0   | 3     | -1-12 | 12   | -9  | 1    | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| 4   | 4   | 11 | 126 | 125  | -5  | 7  | 11 | 221 | 208  | -1  | 10 | 11 | 17  | 22   | -3  | 15  | 11 | 41  | 4     | 0-12  | 12   | 8   | 16   | 0    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| 5   | 4   | 11 | 286 | 262  | -4  | 7  | 11 | 20  | 200  | 0   | 10 | 11 | 136 | 138  | 2   | 15  | 11 | 97  | 4     | 3-12  | 12   | 8   | 16   | 0    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| 6   | 4   | 11 | 47  | 41   | 1   | 7  | 11 | 305 | 289  | 1   | 10 | 11 | 145 | 148  | -1  | 15  | 11 | -10 | 1     | 2-12  | 12   | -4  | 1    | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| 7   | 4   | 11 | 56  | 56   | -7  | 7  | 11 | 365 | 359  | 2   | 10 | 11 | 114 | 104  | 6   | 0   | 15 | 11  | 49    | 1     | 3-12 | 12  | 10   | 11   | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| 8   | 4   | 11 | 169 | 156  | -1  | 7  | 11 | 110 | 96   | 3   | 10 | 11 | 114 | 104  | 1   | 15  | 11 | 61  | 4     | 4-12  | 12   | 32  | 29   | 11   | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| 9   | 4   | 11 | 125 | 129  | 0   | 7  | 11 | -3  | 1    | 4   | 10 | 11 | 112 | 106  | 2   | -12 | 12 | -5  | 1     | 5-12  | 12   | 2   | 32   | 30   | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| 10  | 4   | 11 | 4   | 0    | 1   | 7  | 11 | 24  | 29   | 5   | 10 | 11 | 15  | 1    | 3   | -12 | 12 | -7  | 0     | 6-12  | 12   | 3   | 32   | 30   | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -15 | 5   | 11 | 5   | 2    | 2   | 7  | 11 | 2   | 7    | -11 | 11 | 11 | 83  | 37   | 4   | -12 | 12 | 25  | 3     | 7-12  | 12   | 5   | 16   | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -14 | 5   | 11 | 24  | 33   | 3   | 7  | 11 | 42  | 57   | -10 | 11 | 11 | 33  | 29   | 5   | -12 | 12 | -10 | 4     | 8-12  | 12   | 11  | 19   | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -13 | 5   | 11 | 0   | 24   | 4   | 7  | 11 | 198 | 198  | -9  | 11 | 11 | -11 | 1    | 1   | -12 | 12 | -10 | 5     | 9-12  | 12   | 15  | 2    | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -12 | 5   | 11 | 44  | 79   | 5   | 7  | 11 | 52  | 11   | -11 | 11 | -5 | 0   | 2    | -12 | 12  | 46 | 5   | 10-12 | 12    | 15   | 2   | 1    | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -11 | 5   | 11 | 38  | 44   | 6   | 7  | 11 | 18  | 6    | 7   | 11 | 0  | 3   | 1    | -12 | 12  | 46 | 5   | 11-12 | 12    | 13   | 26  | 1    | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -10 | 5   | 11 | 18  | 1    | 7   | 7  | 11 | 132 | 135  | -6  | 11 | 11 | 3   | 5    | 4   | -17 | 12 | 32  | 4     | -7-11 | 12   | 10  | 16   | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -9  | 5   | 11 | 20  | 25   | 8   | 7  | 11 | 44  | 44   | -5  | 11 | 11 | 2   | 19   | 5   | -17 | 12 | 25  | 4     | -6-11 | 12   | 34  | 14   | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -8  | 5   | 11 | 25  | 20   | -13 | 8  | 11 | -10 | 3    | -4  | 11 | 11 | 15  | 14   | 6   | -17 | 12 | 5   | 0     | -5-11 | 12   | 44  | 14   | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -7  | 5   | 11 | 224 | 177  | -12 | 8  | 11 | 4   | 2    | -3  | 11 | 11 | 9   | 0    | 1   | -16 | 12 | -7  | 5     | -4-11 | 12   | 15  | 1    | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -6  | 5   | 11 | 95  | 93   | -11 | 8  | 11 | 27  | 21   | -2  | 11 | 11 | 83  | 64   | 2   | -16 | 12 | -9  | 5     | -3-11 | 12   | 11  | 0    | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -5  | 5   | 11 | 14  | 9    | -10 | 8  | 11 | -6  | 2    | -1  | 11 | 11 | 89  | 86   | 3   | -16 | 12 | 8   | 3     | -2-11 | 12   | -7  | 1    | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -4  | 5   | 11 | 24  | 1    | -9  | 8  | 11 | 9   | 19   | 0   | 11 | 11 | 55  | 47   | 4   | -16 | 12 | 21  | 0     | 1-11  | 12   | 23  | 7    | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -3  | 5   | 11 | 102 | 91   | -8  | 8  | 11 | 92  | 98   | 1   | 11 | 11 | 15  | 13   | 4   | -16 | 12 | 10  | 0     | 0-11  | 12   | -6  | 1    | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -2  | 5   | 11 | 35  | 37   | -7  | 8  | 11 | 5   | 11   | 2   | 11 | 11 | 14  | 25   | 6   | -16 | 12 | 11  | 0     | -1-11 | 12   | -1  | 7    | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -1  | 5   | 11 | 75  | 74   | 5   | 8  | 11 | 14  | 1    | 3   | 11 | 11 | 71  | 55   | 7   | -16 | 12 | 15  | 0     | 2-11  | 12   | 7   | 2    | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| 0   | 5   | 11 | 469 | 459  | -5  | 8  | 11 | 112 | 111  | 4   | 11 | 11 | 10  | 7    | -2  | -15 | 12 | -14 | 7     | 3-11  | 12   | 47  | 52   | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| 1   | 5   | 11 | 229 | 207  | -4  | 8  | 11 | 265 | 241  | 5   | 11 | 11 | 15  | 0    | -1  | -15 | 12 | 10  | 2     | 4-11  | 12   | 14  | 5    | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| 2   | 5   | 11 | 5   | 0    | -3  | 8  | 11 | 33  | 42   | -10 | 12 | 11 | 27  | 11   | 0   | -15 | 12 | -7  | 4     | 5-11  | 12   | 8   | 5    | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| 3   | 5   | 11 | -2  | 2    | -2  | 8  | 11 | 22  | 14   | -9  | 12 | 11 | 28  | 7    | 1   | -15 | 12 | 4   | 3     | 6-11  | 12   | 31  | 43   | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| 4   | 5   | 11 | 355 | 300  | -1  | 8  | 11 | 186 | 138  | -8  | 12 | 11 | 16  | 1    | 2   | -15 | 12 | 9   | 0     | 7-11  | 12   | 23  | 24   | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| 5   | 5   | 11 | 19  | 15   | 0   | 8  | 11 | 27  | 31   | -7  | 12 | 11 | 7   | 4    | 3   | -15 | 12 | 14  | 6     | 8-11  | 12   | 15  | 4    | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| 6   | 5   | 11 | 21  | 5    | 1   | 8  | 11 | 11  | 15   | -6  | 12 | 11 | 22  | 27   | 4   | -15 | 12 | 7   | 5     | 9-11  | 12   | 13  | 10   | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| 7   | 5   | 11 | 249 | 232  | 2   | 8  | 11 | 133 | 116  | -5  | 12 | 11 | 30  | 7    | 5   | -15 | 12 | 7   | 7     | 10-11 | 12   | -7  | 1    | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| 8   | 5   | 11 | 60  | 64   | 4   | 8  | 11 | 44  | 40   | -3  | 12 | 11 | 17  | 18   | 7   | -15 | 12 | 7   | 4     | 11-11 | 12   | -2  | 2    | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -8  | -10 | 12 | 0   | 3    | 10  | -8 | 12 | 13  | 13   | -5  | -5 | 12 | 117 | 99   | 6   | -3  | 12 | 381 | 313   | -15   | 0    | 12  | 33   | 10   | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -7  | -10 | 12 | -1  | 1    | 11  | -8 | 12 | 16  | 34   | -4  | -5 | 12 | 221 | 198  | 7   | -3  | 12 | 99  | 95    | -14   | 0    | 12  | 21   | 0    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -6  | -10 | 12 | 106 | 61   | 12  | -8 | 12 | 141 | 98   | -3  | -5 | 12 | 205 | 178  | 8   | -3  | 12 | 3   | 5     | -13   | 0    | 12  | 8    | 4    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -5  | -10 | 12 | 50  | 36   | 13  | -8 | 12 | 43  | 17   | -2  | -5 | 12 | 97  | 83   | 9   | -3  | 12 | 153 | 140   | -12   | 0    | 12  | 29   | 23   | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -4  | -10 | 12 | 46  | 32   | -12 | -7 | 12 | 44  | 56   | -1  | -5 | 12 | 4   | 9    | 10  | -3  | 12 | 10  | 35    | -11   | 0    | 12  | 15   | 6    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -3  | -10 | 12 | 20  | 3    | -11 | -7 | 12 | 8   | 9    | 0   | -5 | 12 | 217 | 223  | 11  | -3  | 12 | 28  | 2     | -10   | 0    | 12  | 41   | 15   | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -2  | -10 | 12 | -3  | 3    | -10 | -7 | 12 | 19  | 20   | 1   | -5 | 12 | 175 | 166  | 12  | -3  | 12 | 18  | 5     | -9    | 0    | 12  | 84   | 36   | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| -1  | -10 | 12 | 18  | 25   | -9  | -7 | 12 | 1   | 4    | 2   | -7 | 12 | -1  | 32   | -15 | -2  | 12 | -12 | 7     | -8    | 12   | 401 | 366  | 1    | 1 | 1 | 1 | 1   | 1    | 1 | 1 |   |
| 0   | -10 | 12 | 31  | 59   | 8   | -7 | 12 | 0   | 6    | 3   | -8 | 12 | 25  | 32   | -15 | -2  | 12 | 7   | 1     | -7    | 0    | 12  | 2    | 1    | 1 | 1 | 1 | 1   | 1    | 1 |   |   |
| 1   | -10 | 12 | 27  | 19   | -7  | -7 | 12 | 42  | 80   | 4   | -5 | 12 | 203 | 177  | -14 | -2  | 12 | -4  | 3     | -6    | 0    | 12  | 44   | 54   | 1 | 1 | 1 | 1   | 1    | 1 | 1 |   |
| 2   | -10 | 12 | 21  | 32   | -6  | -7 | 12 | 227 | 192  | 5   | -5 | 12 | 239 | 223  | -13 | -2  | 12 | 39  | 29    | -5    | 0    | 12  | 21   | 14   | 1 | 1 | 1 | 1   | 1    | 1 | 1 |   |
| 3   | -10 | 12 | 0   | 2    | -5  | -7 | 12 | 6   | 4    | 6   | -5 | 12 | 177 | 175  | -12 | -2  | 12 | 24  | 24    | -4    | 0    | 12  | 169  | 187  | 1 | 1 | 1 | 1   | 1    | 1 | 1 |   |
| 4   | -10 | 12 | 61  | 63   | -4  | -7 | 12 | 9   | 5    | 7   | -5 | 12 | 13  | 5    | -11 | -2  | 12 | 43  | 33    | -3    | 0    | 12  | 3    | 1    | 1 | 1 | 1 | 1   | 1    | 1 | 1 |   |
| 5   | -10 | 12 | 11  | 23   | -3  | -7 | 12 | 267 | 239  | 8   | -5 | 12 | 4   | 9    | -10 | -2  | 12 | 144 | 111   | -2    | 0    | 12  | 394  | 78   | 1 | 1 | 1 | 1   | 1    | 1 | 1 |   |
| 6   | -10 | 12 | 11  | 15   | -2  | -7 | 12 | 369 | 331  | 9   | -5 | 12 | 25  | 27   | -9  | -2  | 12 | 8   | 4     | -1    | 0    | 12  | 839  | 295  | 1 | 1 | 1 | 1   | 1    | 1 | 1 |   |
| 7   | -10 | 12 | 4   | -2   | 0   | -1 | -7 | 12  | 102  | 72  | 10 | -5 | 12  | 26   | 32  | -8  | -2 | 12  | 213   | 178   | 0    | 12  | 261  | 21   | 1 | 1 | 1 | 1   | 1    | 1 | 1 |   |
| 8   | -10 | 12 | 4   | 7    | 0   | -7 | 12 | 57  | 45   | 11  | -5 | 12 | 71  | 12   | 7   | -2  | 12 | 36  | 47    | 1     | 12   | 236 | 256  | 1    | 1 | 1 | 1 | 1   | 1    | 1 | 1 |   |
| 9   | -10 | 12 | 3   | 3    | 1   | -7 | 12 | 9   | 6    | 12  | -7 | 12 | 12  | 32   | -7  | -2  | 12 | 740 | 670   | 2     | 0    | 12  | 559  | 474  | 1 | 1 | 1 | 1   | 1    | 1 | 1 | 1 |
| 10  | -10 | 12 | 0   | 0    | 2   | -7 | 12 | 48  | 48   | -14 | -4 | 12 | -5  | 9    | -5  | -2  | 12 | 8   | 1     | 3     | 0    | 12  | 1006 | 994  | 1 | 1 | 1 | 1   | 1    | 1 | 1 | 1 |
| 11  | -10 | 12 | -5  | 7    | 3   | -7 | 12 | 118 | 112  | -13 | -4 | 12 | -6  | 5    | -4  | -2  | 12 | 40  | 19    | 4     | 0    | 12  | 3    | 10   | 1 | 1 | 1 | 1   | 1    | 1 | 1 |   |
| 12  | -10 | 12 | -7  | 10   | 4   | -7 | 12 | 62  | 46   | -12 | -4 | 12 | 20  | 9    | -3  | -2  | 12 | 539 | 570   | 5     | 0    | 12  | 114  | 115  | 1 | 1 | 1 | 1   | 1    | 1 | 1 | 1 |
| -10 | -9  | 12 | 1   | 5    | 5   | -7 | 12 | 23  | 18   | -11 | -4 | 12 | 0   | 6    | -2  | -2  | 12 | 262 | 275   | 6     | 0    | 12  | 245  | 219  | 1 | 1 | 1 | 1   | 1    | 1 | 1 | 1 |
| -9  | -9  | 12 | 0   | 0    | 6   | -7 | 12 | -1  | 1    | -10 | -4 | 12 | 72  | 71   | -1  | -2  | 12 | 4   | 8     | 7     | 0    | 12  | 55   | 41   | 1 | 1 | 1 | 1   | 1    | 1 | 1 |   |
| -8  | -9  | 12 | 1   | 3    | 7   | -7 | 12 | 53  | 67   | -9  | -4 | 12 | 3   | 0    | 0   | -2  | 12 | 37  | 27    | 8     | 0    | 12  | 40   | 46   | 1 | 1 | 1 | 1   | 1    | 1 | 1 |   |
| -7  | -9  | 12 | 36  | 5    | 8   | -7 | 12 | 64  | 58   | -8  | -4 | 12 | -2  | 0    | 1   | -2  | 12 | 43  | 53    | 9     | 0    | 12  | 49   | 75   | 1 | 1 | 1 | 1   | 1    | 1 | 1 |   |
| -6  | -9  | 12 | 32  | 37   | 9   | -7 | 12 | 25  | 22   | -7  | -4 | 12 | 2   | 1    | 2   | -   |    |     |       |       |      |     |      |      |   |   |   |     |      |   |   |   |



Table A.3, continued

| M     | K  | L  | Obe | Calc | M   | K  | L  | Obe | Calc | M   | K  | L   | Obe  | Calc | M     | K  | L   | Obe | Calc  | M     | K   | L   | Obe | Calc |
|-------|----|----|-----|------|-----|----|----|-----|------|-----|----|-----|------|------|-------|----|-----|-----|-------|-------|-----|-----|-----|------|
| 1     | 2  | 12 | 106 | 89   | -10 | 5  | 12 | -2  | 10   | -12 | 8  | 12  | -15  | 3    | 1     | 11 | 12  | 8   | 20    | -1-13 | 13  | -9  | 7   |      |
| 2     | 2  | 12 | 33  | 24   | -9  | 5  | 12 | 74  | 58   | -11 | 8  | 12  | -7   | 2    | 2     | 11 | 12  | 1   | 3     | 0-13  | 13  | 34  | 28  |      |
| 3     | 2  | 12 | 12  | 15   | -8  | 5  | 12 | 47  | 50   | -10 | 8  | 12  | -9   | 2    | 3     | 11 | 12  | 52  | 15    | 1-13  | 13  | 41  | 39  |      |
| 4     | 2  | 12 | 49  | 43   | -7  | 5  | 12 | 10  | 3    | -9  | 8  | 12  | 13   | 8    | 4     | 11 | 12  | 29  | 18    | 2-13  | 13  | -9  | 1   |      |
| 5     | 2  | 12 | 77  | 104  | -6  | 5  | 12 | 149 | 103  | -8  | 8  | 12  | 0    | 0    | -9    | 12 | 12  | 60  | 17    | 3-13  | 13  | -9  | 4   |      |
| 6     | 2  | 12 | 346 | 290  | -5  | 5  | 12 | 30  | 52   | -7  | 8  | 12  | 30   | 16   | -8    | 12 | 12  | 32  | 3     | 4-13  | 13  | 28  | 34  |      |
| 7     | 2  | 12 | 22  | 32   | -4  | 5  | 12 | 136 | 150  | -6  | 8  | 12  | 199  | 176  | -7    | 12 | 12  | 6   | 5     | 5-13  | 13  | 0   | 0   |      |
| 8     | 2  | 12 | 21  | 31   | -3  | 5  | 12 | 74  | 74   | -5  | 8  | 12  | 69   | 67   | -6    | 12 | 12  | 12  | 4     | 6-13  | 13  | 53  | 29  |      |
| 9     | 2  | 12 | 40  | 26   | -2  | 5  | 12 | 144 | 129  | -4  | 8  | 12  | -2   | 7    | -5    | 12 | 12  | 58  | 44    | 7-13  | 13  | 41  | 49  |      |
| 10    | 2  | 12 | 54  | 56   | -1  | 5  | 12 | 122 | 116  | -3  | 8  | 12  | 308  | 266  | -4    | 12 | 12  | 54  | 21    | -6-12 | 13  | 15  | 1   |      |
| 11    | 2  | 12 | -15 | 3    | 0   | 5  | 12 | 5   | 1    | -2  | 8  | 12  | 343  | 279  | -3    | 12 | 12  | -9  | 2     | -5-12 | 13  | 4   | 17  |      |
| -15   | 3  | 12 | -9  | 1    | 1   | 5  | 12 | 88  | 99   | -1  | 8  | 12  | 109  | 124  | -2    | 12 | 12  | 13  | 4     | -4-12 | 13  | 23  | 15  |      |
| -14   | 3  | 12 | 40  | 51   | 2   | 5  | 12 | 179 | 164  | 0   | 8  | 12  | 12   | 0    | -1    | 12 | 12  | 12  | 8     | -3-12 | 13  | 17  | 1   |      |
| -13   | 3  | 12 | 0   | 3    | 3   | 5  | 12 | 29  | 18   | 1   | 8  | 12  | 63   | 52   | 0     | 12 | 12  | 16  | 3     | -2-12 | 13  | -10 | 2   |      |
| -12   | 3  | 12 | 8   | 8    | 4   | 5  | 12 | 1   | 4    | 2   | 8  | 12  | 29   | 24   | 1     | 12 | 12  | -11 | 1     | -1-12 | 13  | 23  | 26  |      |
| -11   | 3  | 12 | 60  | 42   | 5   | 5  | 12 | 121 | 153  | 3   | 8  | 12  | 29   | 15   | 2     | 12 | 12  | 17  | 5     | 0-12  | 13  | 13  | 5   |      |
| -10   | 3  | 12 | 90  | 79   | 6   | 5  | 12 | 96  | 86   | 4   | 8  | 12  | 79   | 101  | 3     | 12 | 12  | -9  | 9     | 1-12  | 13  | 11  | 0   |      |
| -9    | 3  | 12 | 85  | 89   | 7   | 5  | 12 | 0   | 4    | 5   | 8  | 12  | 81   | 86   | -8    | 13 | 12  | -10 | 2     | 2-12  | 13  | 2   | 7   |      |
| -8    | 3  | 12 | 9   | 7    | 8   | 5  | 12 | -3  | 6    | 6   | 8  | 12  | -10  | 2    | -7    | 13 | 12  | 24  | 0     | 3-12  | 13  | -3  | 10  |      |
| -7    | 3  | 12 | 184 | 150  | 9   | 5  | 12 | -17 | 12   | -12 | 9  | 12  | 29   | 0    | -6    | 13 | 12  | 31  | 2     | 4-12  | 13  | 4   | 7   |      |
| -6    | 3  | 12 | 361 | 313  | -14 | 6  | 12 | -8  | 1    | -11 | 9  | 12  | -5   | 11   | -5    | 13 | 12  | -7  | 0     | 5-12  | 13  | 66  | 70  |      |
| -5    | 3  | 12 | 168 | 189  | -13 | 6  | 12 | 43  | 12   | -10 | 9  | 12  | 53   | 54   | -4    | 13 | 12  | 9   | 1     | 6-12  | 13  | 92  | 72  |      |
| -4    | 3  | 12 | 375 | 347  | -12 | 6  | 12 | 1   | 4    | -9  | 9  | 12  | -2   | 2    | -3    | 13 | 12  | -14 | 5     | 7-12  | 13  | 20  | 26  |      |
| -3    | 3  | 12 | 18  | 2    | -11 | 6  | 12 | -7  | 1    | -8  | 9  | 12  | 27   | 15   | -2    | 13 | 12  | 39  | 15    | 8-12  | 13  | -5  | 1   |      |
| -2    | 3  | 12 | 18  | 22   | -10 | 6  | 12 | 23  | 24   | -7  | 9  | 12  | 25   | 24   | -1    | 13 | 12  | -18 | 1     | -7-11 | 13  | 32  | 11  |      |
| -1    | 3  | 12 | -2  | 0    | -9  | 6  | 12 | 5   | 0    | -6  | 9  | 12  | -1   | 1    | 0     | 13 | 12  | 5   | 0     | -6-11 | 13  | 75  | 36  |      |
| 0     | 3  | 12 | 185 | 162  | -8  | 6  | 12 | 44  | 33   | -5  | 9  | 12  | 14   | 12   | 1     | 13 | 12  | 10  | 0     | -5-11 | 13  | 14  | 46  |      |
| 1     | 3  | 12 | 107 | 107  | -7  | 6  | 12 | 22  | 24   | -4  | 9  | 12  | 60   | 74   | 2     | 13 | 12  | -9  | 0     | -4-11 | 13  | 55  | 7   |      |
| 2     | 3  | 12 | 90  | 68   | -6  | 6  | 12 | 39  | 16   | -3  | 9  | 12  | 90   | 103  | 3     | 13 | 12  | -15 | 9     | -3-11 | 13  | -9  | 0   |      |
| 3     | 3  | 12 | 44  | 60   | -5  | 6  | 12 | -4  | 0    | -2  | 9  | 12  | 88   | 87   | -6    | 14 | 12  | 20  | 3     | -2-11 | 13  | 0   | 18  |      |
| 4     | 3  | 12 | 116 | 113  | -4  | 6  | 12 | 41  | 54   | -1  | 9  | 12  | 1    | 3    | -5    | 14 | 12  | -17 | 0     | -1-11 | 13  | 3   | 0   |      |
| 5     | 3  | 12 | 386 | 294  | -3  | 6  | 12 | 558 | 527  | 0   | 9  | 12  | 36   | 20   | -4    | 14 | 12  | -10 | 3     | 0-11  | 13  | 13  | 3   |      |
| 6     | 3  | 12 | 13  | 8    | -2  | 6  | 12 | 29  | 35   | 1   | 9  | 12  | 14   | 14   | -3    | 14 | 12  | 9   | 4     | 1-11  | 13  | -1  | 14  |      |
| 7     | 3  | 12 | 114 | 98   | -1  | 6  | 12 | -2  | 0    | 2   | 9  | 12  | 21   | 5    | -2    | 14 | 12  | -10 | 1     | 2-11  | 13  | 5   | 7   |      |
| 8     | 3  | 12 | 242 | 227  | 0   | 6  | 12 | 76  | 88   | 3   | 9  | 12  | 101  | 105  | -1    | 14 | 12  | -3  | 6     | 3-11  | 13  | 2   | 0   |      |
| 9     | 3  | 12 | 50  | 43   | 1   | 6  | 12 | 17  | 23   | 4   | 9  | 12  | 35   | 61   | 0     | 14 | 12  | 47  | 9     | 4-11  | 13  | 28  | 23  |      |
| 10    | 3  | 12 | -1  | 4    | 2   | 6  | 12 | 10  | 13   | 5   | 9  | 12  | 13   | 1    | 1     | 14 | 12  | -18 | 10    | 5-11  | 13  | 4   | 1   |      |
| -15   | 4  | 12 | 73  | 8    | 3   | 6  | 12 | 22  | 32   | -12 | 10 | 12  | 0    | 8    | 2     | 14 | 12  | 30  | 3     | 6-11  | 13  | 9   | 0   |      |
| -14   | 4  | 12 | 0   | 2    | 4   | 6  | 12 | 100 | 104  | -11 | 10 | 12  | 1    | 22   | 3-18  | 13 | -10 | 10  | 7-11  | 13    | 14  | 13  |     |      |
| -13   | 4  | 12 | -1  | 0    | 5   | 6  | 12 | 54  | 49   | -10 | 10 | 12  | 2    | 1    | 3-17  | 13 | 9   | 6   | 8-11  | 13    | 20  | 16  |     |      |
| -12   | 4  | 12 | 22  | 0    | 6   | 6  | 12 | 175 | 165  | -9  | 10 | 12  | 48   | 33   | 4-17  | 13 | -10 | 7   | 9-11  | 13    | -6  | 3   |     |      |
| -11   | 4  | 12 | 6   | 16   | 7   | 6  | 12 | 46  | 53   | -8  | 10 | 12  | 27   | 1    | 3-16  | 13 | -13 | 1   | 10-11 | 13    | 19  | 1   |     |      |
| -10   | 4  | 12 | 24  | 16   | 8   | 6  | 12 | 11  | 8    | -7  | 10 | 12  | 11   | 1    | 4-16  | 13 | 27  | 0   | 11-11 | 13    | 70  | 17  |     |      |
| -9    | 4  | 12 | -1  | 6    | -14 | 7  | 12 | 6   | 26   | -6  | 10 | 12  | 21   | 18   | 5-16  | 13 | 0   | 0   | -8-10 | 13    | 25  | 13  |     |      |
| -8    | 4  | 12 | 114 | 93   | -13 | 7  | 12 | 37  | 16   | -5  | 10 | 12  | 34   | 23   | -1-15 | 13 | -17 | 1   | -7-10 | 13    | 18  | 17  |     |      |
| -7    | 4  | 12 | 151 | 127  | -12 | 7  | 12 | 6   | 0    | -4  | 10 | 12  | 23   | 17   | 0-15  | 13 | -1  | 0   | -6-10 | 13    | 14  | 4   |     |      |
| -6    | 4  | 12 | 14  | 2    | -11 | 7  | 12 | 16  | 2    | -3  | 10 | 12  | 1    | 1    | 1-15  | 13 | 26  | 0   | -5-10 | 13    | 20  | 6   |     |      |
| -5    | 4  | 12 | 0   | 1    | -10 | 7  | 12 | 8   | 3    | -2  | 10 | 12  | 18   | 12   | 2-15  | 13 | 28  | 2   | -4-10 | 13    | 40  | 19  |     |      |
| -4    | 4  | 12 | -2  | 7    | -9  | 7  | 12 | 19  | 30   | -1  | 10 | 12  | 12   | 9    | 3-15  | 13 | 16  | 0   | -3-10 | 13    | 4   | 0   |     |      |
| -3    | 4  | 12 | 84  | 101  | -8  | 7  | 12 | 67  | 67   | 0   | 10 | 12  | 27   | 14   | 4-15  | 13 | 1   | 1   | -2-10 | 13    | 23  | 0   |     |      |
| -2    | 4  | 12 | 25  | 40   | -7  | 7  | 12 | 33  | 32   | 1   | 10 | 12  | 42   | 61   | 5-15  | 13 | 10  | 0   | -1-10 | 13    | 163 | 128 |     |      |
| -1    | 4  | 12 | 77  | 64   | -6  | 7  | 12 | 18  | 15   | 2   | 10 | 12  | 69   | 62   | 6-15  | 13 | 17  | 3   | 0-10  | 13    | 15  | 15  |     |      |
| 0     | 4  | 12 | 343 | 306  | -5  | 7  | 12 | 189 | 178  | 3   | 10 | 12  | -1   | 6    | -3-14 | 13 | -8  | 0   | 1-10  | 13    | 8   | 0   |     |      |
| 1     | 4  | 12 | 23  | 29   | -4  | 7  | 12 | 407 | 392  | 4   | 10 | 12  | -12  | 2    | -2-14 | 13 | -8  | 7   | 2-10  | 13    | 15  | 6   |     |      |
| 2     | 4  | 12 | 1   | 3    | -3  | 7  | 12 | 10  | 0    | 5   | 10 | 12  | 32   | 36   | -1-14 | 13 | -12 | 6   | 3-10  | 13    | 12  | 22  |     |      |
| 3     | 4  | 12 | 226 | 192  | -2  | 7  | 12 | 88  | 103  | -10 | 11 | 12  | -5   | 7    | 0-14  | 13 | 22  | 1   | 4-10  | 13    | 13  | 4   |     |      |
| 4     | 4  | 12 | 139 | 173  | -1  | 7  | 12 | 242 | 240  | -9  | 11 | 12  | -1   | 0    | 1-14  | 13 | -11 | 3   | 5-10  | 13    | 17  | 4   |     |      |
| 5     | 4  | 12 | 2   | 2    | 0   | 7  | 12 | 21  | 25   | -8  | 11 | 12  | 9    | 2    | 2-14  | 13 | 9   | 1   | 6-10  | 13    | 18  | 7   |     |      |
| 6     | 4  | 12 | 132 | 92   | 1   | 7  | 12 | 41  | 24   | -7  | 11 | 12  | 9    | 3    | 3-14  | 13 | -3  | 0   | 7-10  | 13    | 24  | 24  |     |      |
| 7     | 4  | 12 | 207 | 202  | 2   | 7  | 12 | 116 | 106  | -6  | 11 | 12  | 50   | 42   | 4-14  | 13 | 18  | 5   | 8-10  | 13    | 15  | 1   |     |      |
| 8     | 4  | 12 | 94  | 85   | 3   | 7  | 12 | 85  | 85   | -5  | 11 | 12  | 5    | 4    | 5-14  | 13 | 19  | 22  | 9-10  | 13    | 3   | 0   |     |      |
| 10-10 | 13 | 8  | 1   | 7    | -7  | 13 | 42 | 43  | -4   | -4  | 13 | 2   | 1    | 7    | -2    | 13 | 143 | 100 | -8    | 1     | 13  | 53  | 27  |      |
| 11-10 | 13 | 32 | 0   | 8    | -7  | 13 | 4  | 2   | -3   | -4  | 13 | 25  | 33   | 8    | -2    | 13 | 19  | 6   | -8    | 1     | 13  | 96  | 100 |      |
| 12-10 | 13 | 2  | 3   | 9    | -7  | 13 | -6 | 0   | -2   | -4  | 13 | 222 | 203  | 9    | -2    | 13 | 70  | 79  | -7    | 1     | 13  | -5  | 2   |      |
| -9    | 9  | 13 | -9  | 19   | 10  | -7 | 13 | 37  | 18   | -1  | -4 | 13  | -1   | 1    | 10    | -2 | 13  | 90  | 94    | -6    | 1   | 13  | 0   | 0    |
| -8    | 9  | 13 | 2   | 16   | 11  | -7 | 13 | 32  | 1    | 0   | -4 | 13  | 4    | 8    | 11    | -2 | 13  | -2  | 9     | -5    | 1   | 13  | 89  | 82   |
| -7    | 9  | 13 | 33  | 0    | 12  | -7 | 13 | 29  | 15   | 1   | -4 | 13  | 433  | 418  | -15   | -1 | 13  | 29  | 1     | -4    | 1   | 13  | -1  | 4    |
| -6    | 9  | 13 | 24  | 2    | -12 | -6 | 13 | 11  | 15   | 2   | -4 | 13  | 1821 | 1639 | -14   | -1 | 13  | 4   | 11    | -3    | 1   | 13  | 0   | 0    |
| -5    | 9  | 13 | 86  | 95   | -11 | -6 | 13 | 21  | 15   | 3   | -4 | 13  | 314  | 299  | -13   | -1 | 13  | 51  | 41    | -2    | 1   | 13  | 367 | 298  |
| -4    | 9  | 13 | 43  | 42   | -10 | -6 | 13 | 180 | 162  | 4   | -4 | 13  | 3    | 10   | -12   | -1 | 13  | 14  | 16    | -1    | 1   | 13  | 71  | 93   |
| -3    | 9  | 13 | 13  | 10   | -9  | -6 | 13 | 37  | 41   | 5   | -4 | 13  | 169  | 156  | -11   | -1 | 13  | -4  | 0     | 0     | 1   | 13  | 28  | 24   |
| -2    | 9  | 13 | 213 | 254  | -8  | -6 | 13 | 22  | 33   | 6   | -4 | 13  | 192  | 176  | -10   | -1 | 13  | 30  | 14    | 1     | 1   | 13  | 65  | 42   |
| -1    | 9  | 13 | 144 | 133  | -7  | -6 | 13 | 32  | 5    | 7   | -4 | 13  | -4   | 1    | -9    | -1 | 13  | 12  | 2     | 2     | 1   | 13  | 317 | 274  |
| 0     | 9  | 13 | -1  | 0    | -6  | -6 |    |     |      |     |    |     |      |      |       |    |     |     |       |       |     |     |     |      |

Table A.3, continued

| M   | K  | L  | Obe | Calc | M   | K  | L  | Obe | Calc | M   | K  | L  | Obe | Calc | M   | K   | L   | Obe | Calc | M   | K  | L  | Obe | Calc | M  | K | L | Obe | Calc | M | K | L | Obe | Calc |
|-----|----|----|-----|------|-----|----|----|-----|------|-----|----|----|-----|------|-----|-----|-----|-----|------|-----|----|----|-----|------|----|---|---|-----|------|---|---|---|-----|------|
| 8   | -8 | 13 | 7   | 4    | -1  | -5 | 13 | 2   | 3    | 12  | -3 | 13 | 77  | 0    | -4  | 0   | 13  | 92  | 85   | 8   | -2 | 13 | 24  | 43   |    |   |   |     |      |   |   |   |     |      |
| 9   | -8 | 13 | -5  | 2    | 0   | -5 | 13 | 244 | 246  | -15 | -2 | 13 | 11  | 15   | -3  | 0   | 13  | 31  | 18   | 9   | 2  | 13 | -4  | 6    |    |   |   |     |      |   |   |   |     |      |
| 10  | -8 | 13 | 30  | 9    | 1   | -5 | 13 | 174 | 201  | -14 | -2 | 13 | 27  | 28   | -2  | 0   | 13  | 8   | 15   | 10  | 2  | 13 | 36  | 64   |    |   |   |     |      |   |   |   |     |      |
| 11  | -8 | 13 | 3   | 21   | 2   | -5 | 13 | 543 | 506  | -13 | -2 | 13 | 10  | 1    | -1  | 0   | 13  | 243 | 261  | -15 | 3  | 13 | 20  | 4    |    |   |   |     |      |   |   |   |     |      |
| 12  | -8 | 13 | 28  | 2    | 3   | -5 | 13 | 571 | 559  | -12 | -2 | 13 | 22  | 6    | 0   | 0   | 13  | 157 | 139  | -14 | 3  | 13 | 10  | 0    |    |   |   |     |      |   |   |   |     |      |
| -11 | -7 | 13 | 5   | 2    | 4   | -5 | 13 | 149 | 116  | -11 | -2 | 13 | 40  | 17   | 1   | 0   | 13  | 30  | 19   | -13 | 3  | 13 | 15  | 1    |    |   |   |     |      |   |   |   |     |      |
| -10 | -7 | 13 | 1   | 6    | 5   | -5 | 13 | -3  | 3    | -10 | -2 | 13 | 14  | 3    | 2   | 0   | 13  | 126 | 112  | -12 | 3  | 13 | 17  | 13   |    |   |   |     |      |   |   |   |     |      |
| -9  | -7 | 13 | 56  | 51   | 6   | -5 | 13 | 111 | 125  | -9  | -2 | 13 | 29  | 20   | 3   | 0   | 13  | 40  | 44   | -11 | 3  | 13 | 38  | 43   |    |   |   |     |      |   |   |   |     |      |
| -8  | -7 | 13 | 22  | 56   | 7   | -5 | 13 | 76  | 66   | -8  | -2 | 13 | 238 | 211  | 4   | 0   | 13  | -4  | 7    | -9  | 3  | 13 | 11  | 10   |    |   |   |     |      |   |   |   |     |      |
| -7  | -7 | 13 | 3   | 10   | 8   | -5 | 13 | 56  | 41   | -7  | -2 | 13 | 521 | 466  | 5   | 0   | 13  | 5   | 20   | -8  | 3  | 13 | 220 | 195  |    |   |   |     |      |   |   |   |     |      |
| -6  | -7 | 13 | 0   | 25   | 9   | -5 | 13 | 10  | 13   | -6  | -2 | 13 | 6   | 1    | 6   | 0   | 13  | 237 | 321  | -7  | 3  | 13 | 134 | 124  |    |   |   |     |      |   |   |   |     |      |
| -5  | -7 | 13 | 290 | 266  | 10  | -5 | 13 | 8   | 25   | -5  | -2 | 13 | 349 | 318  | 7   | 0   | 13  | 238 | 234  | -6  | 3  | 13 | -3  | 4    |    |   |   |     |      |   |   |   |     |      |
| -4  | -7 | 13 | 69  | 58   | 11  | -5 | 13 | -6  | 3    | -4  | -2 | 13 | 190 | 178  | 8   | 0   | 13  | -5  | 3    | -5  | 3  | 13 | 42  | 21   |    |   |   |     |      |   |   |   |     |      |
| -3  | -7 | 13 | 27  | 17   | 12  | -5 | 13 | 35  | 0    | -3  | -2 | 13 | 189 | 154  | 9   | 0   | 13  | 5   | 1    | -4  | 3  | 13 | 62  | 60   |    |   |   |     |      |   |   |   |     |      |
| -2  | -7 | 13 | 135 | 119  | -13 | -4 | 13 | 37  | 25   | -2  | -2 | 13 | 291 | 244  | 10  | 0   | 13  | 108 | 99   | -3  | 3  | 13 | 237 | 262  |    |   |   |     |      |   |   |   |     |      |
| -1  | -7 | 13 | 88  | 83   | -12 | -4 | 13 | 54  | 36   | -1  | -2 | 13 | 390 | 379  | 11  | 0   | 13  | -14 | 4    | -2  | 3  | 13 | 66  | 70   |    |   |   |     |      |   |   |   |     |      |
| 0   | -7 | 13 | 9   | 21   | -11 | -4 | 13 | 91  | 91   | 0   | -2 | 13 | 48  | 38   | -16 | 1   | 13  | 5   | 0    | -1  | 3  | 13 | 52  |      |    |   |   |     |      |   |   |   |     |      |
| 1   | -7 | 13 | -3  | 24   | -10 | -4 | 13 | 4   | 3    | 1   | -2 | 13 | 251 | 268  | -15 | 1   | 13  | -7  | 2    | 0   | 3  | 13 | 452 | 371  |    |   |   |     |      |   |   |   |     |      |
| 2   | -7 | 13 | 266 | 240  | -9  | -4 | 13 | 9   | 15   | 2   | -2 | 13 | 994 | 919  | -14 | 1   | 13  | -3  | 12   | 1   | 3  | 13 | 4   | 19   |    |   |   |     |      |   |   |   |     |      |
| 3   | -7 | 13 | 176 | 202  | -8  | -4 | 13 | 9   | 7    | 3   | -2 | 13 | 149 | 172  | -13 | 1   | 13  | 38  | 10   | 2   | 3  | 13 | 217 | 178  |    |   |   |     |      |   |   |   |     |      |
| 4   | -7 | 13 | 2   | 7    | -7  | -4 | 13 | 280 | 305  | 4   | -2 | 13 | 3   | 0    | -12 | 1   | 13  | -7  | 6    | 3   | 3  | 13 | 343 | 320  |    |   |   |     |      |   |   |   |     |      |
| 5   | -7 | 13 | 32  | 32   | -6  | -4 | 13 | 70  | 85   | 5   | -2 | 13 | 0   | 2    | -11 | 1   | 13  | 14  | 9    | 4   | 3  | 13 | 44  | 45   |    |   |   |     |      |   |   |   |     |      |
| 6   | -7 | 13 | 42  | 53   | -5  | -4 | 13 | 264 | 230  | 6   | -2 | 13 | 288 | 239  | -10 | 1   | 13  | 40  | 23   | 5   | 3  | 13 | 15  | 22   |    |   |   |     |      |   |   |   |     |      |
| 7   | 3  | 13 | 251 | 209  | 2   | 6  | 13 | 128 | 138  | -6  | 10 | 13 | 15  | 16   | -6  | -12 | 14  | 8   | 7    | -8  | -8 | 14 | 40  | 1    |    |   |   |     |      |   |   |   |     |      |
| 6   | 3  | 13 | 120 | 96   | 3   | 6  | 13 | 106 | 116  | -5  | 10 | 13 | 32  | 4    | -5  | -12 | 14  | 50  | 0    | -7  | -8 | 14 | 40  | 0    |    |   |   |     |      |   |   |   |     |      |
| 8   | 3  | 13 | -7  | 0    | 4   | 6  | 13 | 0   | 6    | -4  | 10 | 13 | 12  | 5    | -4  | -12 | 14  | 3   | 2    | -6  | -8 | 14 | -9  | 0    |    |   |   |     |      |   |   |   |     |      |
| 9   | 3  | 13 | 11  | 2    | 5   | 6  | 13 | 86  | 115  | -3  | 10 | 13 | 9   | 0    | -3  | -12 | 14  | 15  | 23   | -5  | -8 | 14 | 4   | 20   |    |   |   |     |      |   |   |   |     |      |
| -14 | 4  | 13 | 7   | 0    | 6   | 6  | 13 | 31  | 18   | -2  | 10 | 13 | 3   | 3    | -2  | -12 | 14  | 45  | 26   | -4  | -8 | 14 | 12  | 19   |    |   |   |     |      |   |   |   |     |      |
| -13 | 4  | 13 | 4   | 1    | 7   | 6  | 13 | -9  | 3    | -1  | 10 | 13 | 51  | 54   | -1  | -12 | 14  | -7  | 3    | -3  | -8 | 14 | 18  | 46   |    |   |   |     |      |   |   |   |     |      |
| -12 | 4  | 13 | 8   | 10   | -13 | 7  | 13 | -7  | 1    | 0   | 10 | 13 | 21  | 22   | 0   | -12 | 14  | 13  | 31   | -2  | -8 | 14 | 61  | 62   |    |   |   |     |      |   |   |   |     |      |
| -11 | 4  | 13 | 2   | 0    | -12 | 7  | 13 | 11  | 0    | 1   | 10 | 13 | 21  | 2    | 1   | -12 | 14  | 9   | 12   | -1  | -8 | 14 | 48  | 27   |    |   |   |     |      |   |   |   |     |      |
| -10 | 4  | 13 | 83  | 63   | -11 | 7  | 13 | 14  | 0    | 2   | 10 | 13 | -7  | 3    | 2   | -12 | 14  | 2   | 7    | 0   | -8 | 14 | 9   | 0    |    |   |   |     |      |   |   |   |     |      |
| -9  | 4  | 13 | 5   | 24   | -10 | 7  | 13 | -1  | 7    | 3   | 10 | 13 | 69  | 62   | 3   | -12 | 14  | 3   | 19   | 1   | -8 | 14 | -4  | 3    |    |   |   |     |      |   |   |   |     |      |
| -8  | 4  | 13 | 9   | 7    | -9  | 7  | 13 | -1  | 9    | 4   | 10 | 13 | 17  | 31   | 4   | -12 | 14  | 37  | 23   | 2   | -8 | 14 | 41  | 42   |    |   |   |     |      |   |   |   |     |      |
| -7  | 4  | 13 | 34  | 37   | -8  | 7  | 13 | 1   | 2    | -10 | 11 | 13 | -17 | 1    | -7  | -11 | 14  | -15 | 1    | 3   | -8 | 14 | 149 | 124  |    |   |   |     |      |   |   |   |     |      |
| -6  | 4  | 13 | 44  | 49   | -7  | 7  | 13 | 18  | 17   | -9  | 11 | 13 | 23  | 14   | -6  | -11 | 14  | 31  | 2    | 4   | -8 | 14 | 3   | 6    |    |   |   |     |      |   |   |   |     |      |
| -5  | 4  | 13 | 64  | 61   | -6  | 7  | 13 | 64  | 70   | -8  | 11 | 13 | 1   | 5    | -9  | -11 | 14  | 47  | 18   | 5   | -8 | 14 | 14  | 6    |    |   |   |     |      |   |   |   |     |      |
| -4  | 4  | 13 | 41  | 63   | -5  | 7  | 13 | 4   | 10   | -7  | 11 | 13 | -13 | 9    | -4  | -11 | 14  | 22  | 16   | -8  | -8 | 14 | 16  | 35   |    |   |   |     |      |   |   |   |     |      |
| -3  | 4  | 13 | 217 | 259  | -4  | 7  | 13 | 50  | 58   | -6  | 11 | 13 | -5  | 7    | -3  | -11 | 14  | 2   | 0    | 7   | -8 | 14 | 12  | 8    |    |   |   |     |      |   |   |   |     |      |
| -2  | 4  | 13 | 247 | 217  | -3  | 7  | 13 | 174 | 167  | -5  | 11 | 13 | 17  | 31   | -2  | -11 | 14  | 2   | 10   | 8   | -8 | 14 | 2   | 0    |    |   |   |     |      |   |   |   |     |      |
| -1  | 4  | 13 | -1  | 6    | -2  | 7  | 13 | 174 | 165  | -4  | 11 | 13 | -7  | 1    | -1  | -11 | 14  | 30  | 47   | 9   | -8 | 14 | 17  | 0    |    |   |   |     |      |   |   |   |     |      |
| 0   | 4  | 13 | 60  | 68   | -1  | 7  | 13 | 10  | 2    | -3  | 11 | 13 | 7   | 4    | 0   | -11 | 14  | 37  | 12   | 10  | -8 | 14 | 10  | 2    |    |   |   |     |      |   |   |   |     |      |
| 1   | 4  | 13 | 353 | 306  | 0   | 7  | 13 | 46  | 13   | -2  | 11 | 13 | 60  | 47   | 1   | -11 | 14  | 33  | 0    | 11  | -8 | 14 | 2   | 3    |    |   |   |     |      |   |   |   |     |      |
| 2   | 4  | 13 | 61  | 39   | 1   | 7  | 13 | 152 | 140  | -1  | 11 | 13 | 8   | 29   | 2   | -11 | 14  | 0   | 9    | -9  | -7 | 14 | 18  | 0    |    |   |   |     |      |   |   |   |     |      |
| 3   | 4  | 13 | 10  | 10   | 2   | 7  | 13 | 0   | 13   | 0   | 11 | 13 | 7   | 0    | 3   | -11 | 14  | 28  | 28   | -8  | -7 | 14 | 68  | 34   |    |   |   |     |      |   |   |   |     |      |
| 4   | 4  | 13 | 54  | 65   | 3   | 7  | 13 | 63  | 62   | 1   | 11 | 13 | -12 | 1    | 4   | -11 | 14  | -2  | 0    | -7  | -7 | 14 | 9   | 4    |    |   |   |     |      |   |   |   |     |      |
| 5   | 4  | 13 | 163 | 135  | 4   | 7  | 13 | 183 | 158  | 2   | 11 | 13 | 35  | 30   | 5   | -11 | 14  | 1   | 3    | -6  | -7 | 14 | 61  | 32   |    |   |   |     |      |   |   |   |     |      |
| 6   | 4  | 13 | 51  | 39   | 5   | 7  | 13 | 38  | 38   | 3   | 11 | 13 | 21  | 10   | 6   | -5  | 14  | 7   | 8    | -5  | -7 | 14 | 13  | 0    |    |   |   |     |      |   |   |   |     |      |
| 7   | 4  | 13 | 115 | 76   | 6   | 7  | 13 | 12  | 38   | -8  | 12 | 13 | -15 | 1    | 7   | -11 | 14  | -5  | 1    | -4  | -7 | 14 | -6  | 0    |    |   |   |     |      |   |   |   |     |      |
| 8   | 4  | 13 | 22  | 11   | -12 | 8  | 13 | 42  | 10   | -7  | 12 | 13 | 1   | 0    | 8   | -11 | 14  | -8  | 4    | -2  | -7 | 14 | 53  | 40   |    |   |   |     |      |   |   |   |     |      |
| 9   | 4  | 13 | 48  | 15   | -11 | 8  | 13 | 17  | 21   | -6  | 12 | 13 | 5   | 1    | -7  | -10 | 14  | 46  | 2    | -2  | -7 | 14 | 37  | 15   |    |   |   |     |      |   |   |   |     |      |
| -14 | 5  | 13 | 8   | 2    | -10 | 8  | 13 | 5   | 29   | -5  | 12 | 13 | -14 | 0    | -6  | -10 | 14  | -1  | 20   | -1  | -7 | 14 | 4   | 8    |    |   |   |     |      |   |   |   |     |      |
| -13 | 5  | 13 | 14  | 2    | -9  | 8  | 13 | 12  | 13   | -4  | 12 | 13 | 43  | 19   | -5  | -10 | 14  | 13  | 7    | 0   | -7 | 14 | 115 | 113  |    |   |   |     |      |   |   |   |     |      |
| -12 | 5  | 13 | 1   | 5    | -8  | 8  | 13 | 35  | 35   | -3  | 12 | 13 | 35  | 32   | -4  | -10 | 14  | -4  | 0    | 1   | -7 | 14 | 75  | 69   |    |   |   |     |      |   |   |   |     |      |
| -11 | 5  | 13 | 23  | 23   | -7  | 8  | 13 | 12  | 24   | -2  | 12 | 13 | 32  | 51   | -3  | -10 | 14  | 41  | 29   | 2   | -7 | 14 | 73  | 65   |    |   |   |     |      |   |   |   |     |      |
| -10 | 5  | 13 | 14  | 14   | -6  | 8  | 13 | -4  | 7    | -1  | 12 | 13 | 10  | 0    | -2  | -10 | 14  | 4   | 21   | 3   | -7 | 14 | 34  | 31   |    |   |   |     |      |   |   |   |     |      |
| -9  | 5  | 13 | 33  | 19   | -5  | 8  | 13 | 25  | 25   | 0   | 12 | 13 | -11 | 18   | 4   | -1  | -10 | 14  | 0    | 2   | 4  | -7 | 14  | 55   | 52 |   |   |     |      |   |   |   |     |      |
| -8  | 5  | 13 | 103 | 102  | -4  | 8  | 13 | 103 | 78   | 1   | 12 | 13 | 28  | 18   | 0   | -10 | 14  | 69  | 44   | 5   | -7 | 14 | 27  | 22   |    |   |   |     |      |   |   |   |     |      |
| -7  | 5  | 13 | 76  | 71   | -3  | 8  | 13 | 97  | 108  | 2   | 12 | 13 | 18  | 10   | 1   | -10 |     |     |      |     |    |    |     |      |    |   |   |     |      |   |   |   |     |      |

Table A.3, continued

| M   | K  | L  | Obs | Calc | M   | K   | L  | Obs | Calc | M   | K  | L  | Obs | Calc | M   | K  | L  | Obs | Calc | M   | K  | L  | Obs | Calc |
|-----|----|----|-----|------|-----|-----|----|-----|------|-----|----|----|-----|------|-----|----|----|-----|------|-----|----|----|-----|------|
| 5   | -5 | 14 | 143 | 111  | -5  | -2  | 14 | 66  | 48   | 8   | 0  | 14 | 105 | 142  | -2  | 3  | 14 | 90  | 99   | -2  | 6  | 14 | 17  | 20   |
| 6   | -5 | 14 | 10  | 14   | -4  | -2  | 14 | 53  | 45   | 9   | 0  | 14 | -7  | 15   | -1  | 3  | 14 | 23  | 16   | -1  | 6  | 14 | 72  | 59   |
| 7   | -5 | 14 | 4   | 0    | -3  | -2  | 14 | 55  | 77   | 10  | 0  | 14 | -10 | 0    | 0   | 3  | 14 | 324 | 275  | 0   | 6  | 14 | 163 | 159  |
| 8   | -5 | 14 | 95  | 80   | -2  | -2  | 14 | 102 | 97   | -15 | 1  | 14 | -6  | 0    | 1   | 3  | 14 | 204 | 200  | 1   | 6  | 14 | 136 | 133  |
| 9   | -5 | 14 | 65  | 94   | -1  | -2  | 14 | 18  | 18   | -14 | 1  | 14 | 15  | 2    | 2   | 3  | 14 | -1  | 4    | 2   | 6  | 14 | 8   | 4    |
| 10  | -5 | 14 | 5   | 4    | 0   | -2  | 14 | 72  | 69   | -13 | 1  | 14 | -6  | 1    | 3   | 3  | 14 | 20  | 18   | 3   | 6  | 14 | 147 | 114  |
| 11  | -5 | 14 | 25  | 5    | 1   | -2  | 14 | 54  | 72   | -12 | 1  | 14 | 21  | 2    | 4   | 3  | 14 | 61  | 34   | 4   | 6  | 14 | 86  | 66   |
| 12  | -5 | 14 | 2   | 11   | 2   | -2  | 14 | 6   | 27   | -11 | 1  | 14 | 11  | 12   | 5   | 3  | 14 | 150 | 100  | 5   | 6  | 14 | 92  | 76   |
| -12 | -4 | 14 | -1  | 0    | 3   | -2  | 14 | 499 | 473  | -10 | 1  | 14 | 61  | 50   | 6   | 3  | 14 | 28  | 22   | 6   | 6  | 14 | 0   | 5    |
| -11 | -4 | 14 | 13  | 11   | 4   | -2  | 14 | 93  | 72   | -9  | 1  | 14 | 52  | 4    | 7   | 3  | 14 | 108 | 96   | -12 | 7  | 14 | -16 | 11   |
| -10 | -4 | 14 | 18  | 28   | 5   | -2  | 14 | 70  | 71   | -8  | 1  | 14 | 17  | 11   | 8   | 3  | 14 | 56  | 29   | -11 | 7  | 14 | -8  | 12   |
| -9  | -4 | 14 | 0   | 3    | 6   | -2  | 14 | 13  | 10   | -7  | 1  | 14 | 149 | 123  | 9   | 3  | 14 | 14  | 1    | -10 | 7  | 14 | -8  | 7    |
| -8  | -4 | 14 | 21  | 9    | 7   | -2  | 14 | 59  | 57   | -6  | 1  | 14 | 27  | 15   | -13 | 4  | 14 | -1  | 1    | -9  | 7  | 14 | 54  | 48   |
| -7  | -4 | 14 | 79  | 82   | 8   | -2  | 14 | 50  | 27   | -5  | 1  | 14 | 17  | 10   | -12 | 4  | 14 | 31  | 12   | -8  | 7  | 14 | 10  | 12   |
| -6  | -4 | 14 | 48  | 50   | 9   | -2  | 14 | -6  | 5    | -4  | 1  | 14 | 12  | 1    | -11 | 4  | 14 | 3   | 21   | -7  | 7  | 14 | -6  | 3    |
| -5  | -4 | 14 | 29  | 30   | 10  | -2  | 14 | 3   | 3    | -3  | 1  | 14 | 199 | 107  | -10 | 4  | 14 | 14  | 4    | -6  | 7  | 14 | 9   | 3    |
| -4  | -4 | 14 | 56  | 49   | 11  | -2  | 14 | 7   | 19   | -2  | 1  | 14 | 2   | 10   | -9  | 4  | 14 | 17  | 27   | -5  | 7  | 14 | 49  | 30   |
| -3  | -4 | 14 | 18  | 13   | -14 | -1  | 14 | 33  | 3    | -1  | 1  | 14 | 64  | 65   | -8  | 4  | 14 | 99  | 104  | -4  | 7  | 14 | 20  | 31   |
| -2  | -4 | 14 | 68  | 32   | -13 | -1  | 14 | 21  | 9    | 0   | 1  | 14 | 364 | 310  | -7  | 4  | 14 | 115 | 129  | -3  | 7  | 14 | 6   | 14   |
| -1  | -4 | 14 | 48  | 40   | -12 | -1  | 14 | 5   | 7    | 1   | 1  | 14 | 32  | 30   | -6  | 4  | 14 | 43  | 39   | -2  | 7  | 14 | 24  | 2    |
| 0   | -4 | 14 | 111 | 103  | -11 | -1  | 14 | 12  | 8    | 2   | 1  | 14 | -3  | 0    | -5  | 4  | 14 | 24  | 13   | -1  | 7  | 14 | 26  | 35   |
| 1   | -4 | 14 | 22  | 25   | -10 | -1  | 14 | 37  | 29   | 3   | 1  | 14 | 325 | 254  | -4  | 4  | 14 | 144 | 177  | 0   | 7  | 14 | -4  | 0    |
| 2   | -4 | 14 | 102 | 104  | -9  | -1  | 14 | 73  | 66   | 4   | 1  | 14 | 169 | 215  | -3  | 4  | 14 | 100 | 100  | 1   | 7  | 14 | 39  | 34   |
| 3   | -4 | 14 | 871 | 802  | -8  | -1  | 14 | 173 | 169  | 5   | 1  | 14 | 43  | 25   | -2  | 4  | 14 | 20  | 21   | 2   | 7  | 14 | 91  | 93   |
| 4   | -4 | 14 | 52  | 44   | -7  | -1  | 14 | 130 | 124  | 6   | 1  | 14 | -7  | 4    | -1  | 4  | 14 | 332 | 292  | 3   | 7  | 14 | 5   | 20   |
| 5   | -4 | 14 | 13  | 23   | -6  | -1  | 14 | 2   | 2    | 7   | 1  | 14 | 184 | 139  | 0   | 4  | 14 | 158 | 163  | 4   | 7  | 14 | 4   | 0    |
| 6   | -4 | 14 | 27  | 27   | -5  | -1  | 14 | 105 | 97   | 8   | 1  | 14 | 27  | 12   | 1   | 4  | 14 | 32  | 30   | 5   | 7  | 14 | 3   | 9    |
| 7   | -4 | 14 | 44  | 40   | -4  | -1  | 14 | 130 | 124  | 9   | 1  | 14 | -1  | 0    | 2   | 4  | 14 | 112 | 101  | -12 | 8  | 14 | 8   | 1    |
| 8   | -4 | 14 | 2   | 3    | -3  | -1  | 14 | 12  | 10   | 10  | 1  | 14 | -19 | 18   | 3   | 4  | 14 | 135 | 133  | -11 | 8  | 14 | 13  | 2    |
| 9   | -4 | 14 | 16  | 16   | -2  | -1  | 14 | 5   | 0    | -15 | 2  | 14 | 10  | 4    | 4   | 4  | 14 | 66  | 47   | -10 | 8  | 14 | 36  | 36   |
| 10  | -4 | 14 | -8  | 12   | -1  | -1  | 14 | 186 | 171  | -14 | 2  | 14 | -3  | 0    | 5   | 4  | 14 | 13  | 7    | -9  | 8  | 14 | 57  | 21   |
| 11  | -4 | 14 | 34  | 4    | 0   | -1  | 14 | 46  | 60   | -13 | 2  | 14 | -8  | 0    | 6   | 4  | 14 | 98  | 8    | 8   | 14 | -4 | 1   | 1    |
| -13 | -3 | 14 | 2   | 1    | 1   | -1  | 14 | 66  | 72   | -12 | 2  | 14 | 18  | 15   | 7   | 4  | 14 | 41  | 2    | -7  | 8  | 14 | -6  | 0    |
| -12 | -3 | 14 | 17  | 6    | 2   | -1  | 14 | 15  | 19   | -11 | 2  | 14 | 20  | 31   | 8   | 4  | 14 | -4  | 0    | -6  | 8  | 14 | 70  | 62   |
| -11 | -3 | 14 | 5   | 7    | 3   | -1  | 14 | 23  | 25   | -10 | 2  | 14 | 17  | 6    | -13 | 5  | 14 | 53  | 17   | -5  | 8  | 14 | 31  | 42   |
| -10 | -3 | 14 | 11  | 0    | 4   | -1  | 14 | -4  | 1    | -9  | 2  | 14 | 52  | 22   | -12 | 5  | 14 | 14  | 12   | -4  | 8  | 14 | 0   | 0    |
| -9  | -3 | 14 | 90  | 94   | 5   | -1  | 14 | 27  | 27   | -8  | 2  | 14 | 54  | 64   | -11 | 5  | 14 | 17  | 13   | -3  | 8  | 14 | 23  | 1    |
| -8  | -3 | 14 | 408 | 397  | 6   | -1  | 14 | 169 | 143  | -7  | 2  | 14 | 43  | 39   | -10 | 5  | 14 | 8   | 2    | -2  | 8  | 14 | 1   | 1    |
| -7  | -3 | 14 | 138 | 120  | 7   | -1  | 14 | 78  | 97   | -6  | 2  | 14 | 23  | 30   | -9  | 5  | 14 | 0   | 20   | -1  | 8  | 14 | 36  | 55   |
| -6  | -3 | 14 | 7   | 9    | 8   | -1  | 14 | 30  | 13   | -5  | 2  | 14 | 65  | 61   | -8  | 5  | 14 | 35  | 25   | 0   | 8  | 14 | 144 | 149  |
| -5  | -3 | 14 | 106 | 83   | 9   | -1  | 14 | 5   | 11   | -4  | 2  | 14 | 200 | 204  | -7  | 5  | 14 | 23  | 20   | 1   | 8  | 14 | 34  | 35   |
| -4  | -3 | 14 | 85  | 82   | 10  | -1  | 14 | 39  | 25   | -3  | 2  | 14 | 17  | 21   | -6  | 5  | 14 | 32  | 23   | 2   | 8  | 14 | 0   | 14   |
| -3  | -3 | 14 | 93  | 86   | 11  | -1  | 14 | 6   | 0    | -2  | 2  | 14 | 58  | 44   | -5  | 5  | 14 | -2  | 1    | 3   | 8  | 14 | 18  | 25   |
| -2  | -3 | 14 | 50  | 60   | -15 | 0   | 14 | 11  | 2    | -1  | 2  | 14 | 52  | 51   | -4  | 4  | 14 | -3  | 10   | 4   | 8  | 14 | 87  | 44   |
| -1  | -3 | 14 | 180 | 175  | -14 | 0   | 14 | 27  | 27   | 0   | 2  | 14 | 13  | 17   | -3  | 5  | 14 | 82  | 83   | -11 | 9  | 14 | 26  | 6    |
| 0   | -3 | 14 | 4   | 0    | -13 | 0   | 14 | -7  | 4    | 1   | 2  | 14 | 14  | 12   | -2  | 5  | 14 | 60  | 40   | -10 | 9  | 14 | -1  | 2    |
| 1   | -3 | 14 | 59  | 56   | -12 | 0   | 14 | 6   | 4    | 2   | 2  | 14 | 221 | 212  | -1  | 5  | 14 | 0   | 1    | -9  | 9  | 14 | 60  | 24   |
| 2   | -3 | 14 | 999 | 885  | -11 | 0   | 14 | -2  | 9    | 3   | 2  | 14 | 121 | 138  | 0   | 5  | 14 | 3   | 7    | -8  | 9  | 14 | 13  | 14   |
| 3   | -3 | 14 | 5   | 3    | -10 | 0   | 14 | 31  | 70   | 4   | 2  | 14 | 28  | 21   | 1   | 5  | 14 | 37  | 52   | -7  | 9  | 14 | 5   | 8    |
| 4   | -3 | 14 | 0   | 2    | -9  | 0   | 14 | 89  | 84   | 5   | 2  | 14 | 43  | 50   | 2   | 5  | 14 | 141 | 118  | -6  | 9  | 14 | -8  | 0    |
| 5   | -3 | 14 | 6   | 10   | -8  | 0   | 14 | 44  | 42   | 6   | 2  | 14 | 181 | 168  | 3   | 5  | 14 | 4   | 4    | -5  | 9  | 14 | 47  | 39   |
| -4  | 9  | 14 | 37  | 34   | -2  | -11 | 15 | 8   | 18   | 0   | -7 | 15 | 104 | 119  | 1   | -4 | 15 | 166 | 147  | -3  | -1 | 15 | 42  | 19   |
| -3  | 9  | 14 | 2   | 0    | -1  | -11 | 15 | -6  | 14   | 1   | -7 | 15 | 12  | 12   | 2   | -4 | 15 | 14  | 5    | -2  | -1 | 15 | 155 | 160  |
| -2  | 9  | 14 | -6  | 4    | 0   | -11 | 15 | 28  | 19   | 2   | -7 | 15 | 94  | 96   | 3   | -4 | 15 | 69  | 62   | -1  | -1 | 15 | 38  | 31   |
| -1  | 9  | 14 | 28  | 34   | 1   | -11 | 15 | 32  | 27   | 3   | -7 | 15 | 213 | 200  | 4   | -4 | 15 | 37  | 37   | 0   | -1 | 15 | 1   | 5    |
| 0   | 9  | 14 | 26  | 8    | 2   | -11 | 15 | 8   | 0    | 4   | -7 | 15 | 0   | 3    | 5   | -4 | 15 | 79  | 69   | 1   | -1 | 15 | 235 | 209  |
| 1   | 9  | 14 | 9   | 4    | 3   | -11 | 15 | 24  | 14   | 5   | -7 | 15 | 28  | 31   | 6   | -4 | 15 | 69  | 70   | 2   | -1 | 15 | 83  | 97   |
| 2   | 9  | 14 | 16  | 15   | -7  | -10 | 15 | 17  | 0    | 6   | -7 | 15 | 51  | 49   | 7   | -4 | 15 | -5  | 1    | 3   | -1 | 15 | 8   | 7    |
| 3   | 9  | 14 | 82  | 71   | -6  | -10 | 15 | -14 | 0    | 7   | -7 | 15 | 43  | 1    | 8   | -4 | 15 | -3  | 12   | 4   | -1 | 15 | 213 | 166  |
| -10 | 10 | 14 | 19  | 3    | -5  | -10 | 15 | 47  | 8    | 8   | -7 | 15 | 68  | 53   | 9   | -4 | 15 | 0   | 12   | 5   | -1 | 15 | 29  | 40   |
| -9  | 10 | 14 | 43  | 23   | -4  | -10 | 15 | 9   | 8    | 9   | -7 | 15 | 106 | 124  | 10  | -4 | 15 | -3  | 3    | 6   | -1 | 15 | 52  | 36   |
| -8  | 10 | 14 | 79  | 11   | -3  | -10 | 15 | -10 | 1    | 10  | -7 | 15 | 39  | 31   | 11  | -4 | 15 | 32  | 31   | 7   | -1 | 15 | 109 | 91   |
| -7  | 10 | 14 | 8   | 2    | -2  | -10 | 15 | 6   | 30   | 11  | -7 | 15 | 20  | 0    | -11 | -3 | 15 | 20  | 3    | 8   | -1 | 15 | 119 | 77   |
| -6  | 10 | 14 | 4   | 8    | -1  | -10 | 15 | 20  | 29   | -9  | -6 | 15 | 31  | 17   | -10 | -3 | 15 | 14  | 9    | 9   | -1 | 15 | -5  | 7    |
| -5  | 10 | 14 | 32  | 22   | 0   | -10 | 15 | 7   | 19   | -8  | -6 | 15 | 109 | 89   | -9  | -3 | 15 | -3  | 2    | 10  | -1 | 15 | 48  | 34   |
| -4  | 10 | 14 | 0   | 1    | 1   | -10 | 15 | -2  | 0    | -7  | -6 | 15 | -3  | 11   | -9  | -3 | 15 | 36  | 27   | -13 | 0  | 15 | 0   | 2    |
| -3  | 10 | 14 | 5   | 2    | 2   | -10 | 15 | 5   | 29   | -6  | -5 | 15 | 29  | 14   | 7   | -2 | 15 | 56  | 48   | -12 | 0  | 15 | 34  | 3    |
| -2  | 10 | 14 | 22  | 25   | 3   | -10 | 15 | 36  | 41   | -5  | -6 | 15 | 25  | 22   | -6  | -3 | 15 | 25  | 14   | -11 | 0  | 15 | 14  | 9    |
| -1  | 10 | 14 | 20  | 12   | 4   | -10 | 15 | 3   | 10   | -4  | -6 | 15 | 27  | 0    | -5  | -3 | 15 | 2   | 0    | -10 | 0  | 15 | 4   | 3    |
| 0   | 10 | 14 | 17  | 2    | 5   | -10 | 15 | 1   | 4    | -3  | -6 | 15 | 0   | 3    | -4  | -3 | 15 | 17  | 11   | -9  | 0  | 15 | 16  | 13   |
| 1   | 10 | 14 | -8  | 2    | 6   | -10 | 15 | 7   | 2    | -2  | -6 | 15 | 49  | 35   | -3  | -3 | 15 | 35  | 58   | -8  | 0  | 15 | 89  | 60   |
| 2   | 10 | 14 | 8   | 51   | 7   | -10 | 15 | -9  | 0    | -1  | -6 | 15 |     |      |     |    |    |     |      |     |    |    |     |      |

Table A.3, continued

| M   | K   | L  | Obe | Calc | M   | K  | L  | Obe | Calc | M   | K   | L  | Obe | Calc | M   | K  | L  | Obe | Calc | M   | K  | L  | Obe | Calc |
|-----|-----|----|-----|------|-----|----|----|-----|------|-----|-----|----|-----|------|-----|----|----|-----|------|-----|----|----|-----|------|
| -13 | 13  | 15 | 26  | 6    | 7   | -8 | 15 | 0   | 4    | 10  | -5  | 15 | 25  | 9    | 7   | -2 | 15 | 14  | 5    | 3   | 1  | 15 | 23  | 29   |
| -13 | 12  | 15 | -6  | 6    | 8   | -8 | 15 | -6  | 0    | 11  | -5  | 15 | -1  | 1    | 8   | -2 | 15 | 24  | 40   | 4   | 1  | 15 | 17  | 15   |
| -13 | 12  | 15 | -11 | 2    | 9   | -8 | 15 | -7  | 0    | -10 | -4  | 15 | -4  | 5    | 9   | -2 | 15 | -4  | 3    | 5   | 1  | 15 | 78  | 60   |
| -13 | 12  | 15 | -3  | 0    | 10  | -8 | 15 | 15  | 12   | -9  | -4  | 15 | 38  | 31   | 10  | -2 | 15 | -3  | 2    | 6   | 1  | 15 | 61  | 85   |
| -13 | 12  | 15 | 14  | 29   | -9  | -7 | 15 | -2  | 4    | -8  | -4  | 15 | 127 | 128  | -12 | -1 | 15 | 18  | 0    | 7   | 1  | 15 | 21  | 32   |
| -13 | 12  | 15 | 38  | 35   | -8  | -7 | 15 | -7  | 2    | -7  | -4  | 15 | -1  | 1    | -11 | -1 | 15 | 6   | 5    | 8   | 1  | 15 | 68  | 41   |
| 0   | -12 | 15 | -10 | 5    | -7  | -7 | 15 | 62  | 57   | -6  | -4  | 15 | 30  | 28   | -10 | -1 | 15 | 76  | 24   | 9   | 1  | 15 | 38  | 28   |
| 1   | -12 | 15 | 19  | 0    | -6  | -7 | 15 | 1   | 0    | -5  | -4  | 15 | 113 | 106  | -9  | -1 | 15 | 37  | 33   | -13 | 2  | 15 | -15 | 5    |
| 2   | -12 | 15 | 8   | 5    | -5  | -7 | 15 | 111 | 92   | -4  | -4  | 15 | 0   | 0    | -8  | -1 | 15 | 19  | 13   | -12 | 2  | 15 | -5  | 0    |
| -6  | -11 | 15 | 41  | 4    | -4  | -7 | 15 | 64  | 60   | -3  | -4  | 15 | 3   | 8    | -7  | -1 | 15 | 41  | 41   | -11 | 2  | 15 | -1  | 6    |
| -9  | -11 | 15 | -12 | 5    | -3  | -7 | 15 | 6   | 9    | -2  | -4  | 15 | 10  | 8    | -6  | -1 | 15 | 138 | 114  | -10 | 2  | 15 | -10 | 24   |
| -4  | -11 | 15 | -10 | 8    | -2  | -7 | 15 | 4   | 12   | -1  | -4  | 15 | 50  | 54   | -5  | -1 | 15 | 54  | 60   | -9  | 2  | 15 | -3  | 0    |
| -3  | -11 | 15 | 19  | 22   | -1  | -7 | 15 | 37  | 40   | 0   | -4  | 15 | 102 | 112  | -4  | -1 | 15 | -1  | 2    | -8  | 2  | 15 | 32  | 27   |
| -7  | 2   | 15 | 27  | 22   | -6  | 5  | 15 | 8   | 0    | -6  | 9   | 15 | 18  | 2    | 4   | -9 | 16 | 10  | 0    | 0   | -5 | 16 | -1  | 2    |
| -6  | 2   | 15 | 19  | 18   | -5  | 5  | 15 | 9   | 12   | -5  | 9   | 15 | 3   | 20   | 5   | -9 | 16 | -1  | 3    | 1   | -5 | 16 | 15  | 9    |
| -5  | 2   | 15 | 37  | 40   | -4  | 5  | 15 | 57  | 47   | -4  | 9   | 15 | -7  | 1    | -8  | -8 | 16 | 33  | 17   | 2   | -5 | 16 | 18  | 19   |
| -4  | 2   | 15 | 99  | 112  | -3  | 5  | 15 | 47  | 43   | -3  | 9   | 15 | 0   | 0    | -7  | -8 | 16 | 97  | 64   | 3   | -5 | 16 | 79  | 89   |
| -3  | 2   | 15 | 207 | 205  | -2  | 5  | 15 | -4  | 1    | -2  | 9   | 15 | 17  | 13   | -6  | -8 | 16 | 7   | 1    | 4   | -5 | 16 | 21  | 12   |
| -2  | 2   | 15 | 15  | 17   | -1  | 5  | 15 | 172 | 148  | -1  | 9   | 15 | -8  | 1    | -5  | -8 | 16 | -9  | 5    | 5   | -5 | 16 | 33  | 38   |
| -1  | 2   | 15 | 68  | 58   | 0   | 5  | 15 | 137 | 140  | 0   | 9   | 15 | -5  | 2    | -4  | -8 | 16 | 8   | 10   | 6   | -5 | 16 | 4   | 0    |
| 0   | 2   | 15 | 78  | 73   | 1   | 5  | 15 | 6   | 5    | 1   | 9   | 15 | 17  | 18   | -3  | -8 | 16 | 23  | 18   | 7   | -5 | 16 | 4   | 14   |
| 1   | 2   | 15 | 37  | 33   | 2   | 5  | 15 | 20  | 17   | -9  | 10  | 15 | 32  | 0    | -2  | -8 | 16 | 36  | 36   | 8   | -5 | 16 | 37  | 36   |
| 2   | 2   | 15 | 46  | 38   | 3   | 5  | 15 | 69  | 73   | -8  | 10  | 15 | 14  | 8    | -1  | -8 | 16 | 24  | 33   | 9   | -5 | 16 | 24  | 2    |
| 3   | 2   | 15 | 49  | 44   | 4   | 5  | 15 | 55  | 35   | -7  | 10  | 15 | -4  | 20   | 0   | -8 | 16 | -1  | 0    | 10  | -5 | 16 | -9  | 0    |
| 4   | 2   | 15 | 157 | 118  | 5   | 5  | 15 | 33  | 39   | -6  | 10  | 15 | 47  | 45   | 2   | -8 | 16 | -5  | 6    | -9  | -4 | 16 | -1  | 5    |
| 5   | 2   | 15 | 28  | 17   | 6   | 5  | 15 | 52  | 2    | -5  | 10  | 15 | 100 | 58   | 2   | -8 | 16 | 114 | 90   | -8  | -4 | 16 | 28  | 34   |
| 6   | 2   | 15 | 46  | 43   | -12 | 6  | 15 | 10  | 6    | -4  | 10  | 15 | 32  | 7    | 3   | -8 | 16 | 2   | 7    | -7  | -4 | 16 | 18  | 10   |
| 7   | 2   | 15 | 34  | 25   | -11 | 6  | 15 | 8   | 9    | -3  | 10  | 15 | -8  | 11   | 4   | -8 | 16 | 3   | 8    | -6  | -4 | 16 | 0   | 0    |
| 8   | 2   | 15 | 19  | 20   | -10 | 6  | 15 | 12  | 2    | -2  | 10  | 15 | -13 | 5    | 5   | -8 | 16 | 16  | 25   | -5  | -4 | 16 | -1  | 4    |
| -13 | 3   | 15 | -12 | 0    | -9  | 6  | 15 | 43  | 67   | -1  | 10  | 15 | 25  | 14   | 6   | -8 | 16 | 17  | 0    | -4  | -4 | 16 | 1   | 2    |
| -12 | 3   | 15 | 16  | 7    | -8  | 6  | 15 | -4  | 7    | 0   | 10  | 15 | 5   | 24   | 7   | -8 | 16 | 5   | 10   | -3  | -4 | 16 | 22  | 42   |
| -11 | 3   | 15 | -7  | 9    | -7  | 6  | 15 | 2   | 2    | -8  | 11  | 15 | 16  | 11   | 8   | -8 | 16 | 27  | 36   | -2  | -4 | 16 | 129 | 135  |
| -10 | 3   | 15 | 13  | 4    | -6  | 6  | 15 | 24  | 24   | -7  | 11  | 15 | 43  | 10   | -8  | -7 | 16 | 14  | 29   | -1  | -4 | 16 | 305 | 277  |
| -9  | 3   | 15 | 7   | 4    | -5  | 6  | 15 | 41  | 39   | -6  | 11  | 15 | 19  | 5    | -7  | -7 | 16 | 11  | 3    | 0   | -4 | 16 | 101 | 99   |
| -8  | 3   | 15 | 64  | 49   | -1  | 6  | 15 | -1  | 1    | -5  | 11  | 15 | 16  | 11   | -6  | -7 | 16 | 9   | 10   | 1   | -4 | 16 | -1  | 0    |
| -7  | 3   | 15 | 44  | 37   | -3  | 6  | 15 | 18  | 12   | -4  | 11  | 15 | 50  | 3    | -5  | -7 | 16 | 8   | 1    | 2   | -4 | 16 | 11  | 5    |
| -6  | 3   | 15 | -3  | 0    | -2  | 6  | 15 | 41  | 48   | -3  | 11  | 15 | 16  | 15   | -4  | -7 | 16 | 15  | 16   | 3   | -4 | 16 | 2   | 1    |
| -5  | 3   | 15 | 88  | 83   | -1  | 6  | 15 | 26  | 19   | -2  | 11  | 15 | -7  | 16   | -3  | -7 | 16 | 56  | 40   | 4   | -4 | 16 | 8   | 4    |
| -4  | 3   | 15 | 33  | 42   | 0   | 6  | 15 | 37  | 24   | -1  | 11  | 15 | 15  | 6    | -2  | -7 | 16 | 11  | 8    | 5   | -4 | 16 | 12  | 6    |
| -3  | 3   | 15 | 11  | 0    | 1   | 6  | 15 | 89  | 72   | -6  | 12  | 15 | 30  | 26   | -1  | -7 | 16 | 6   | 6    | 6   | -4 | 16 | 41  | 24   |
| -2  | 3   | 15 | 19  | 11   | 2   | 6  | 15 | 47  | 48   | -5  | 12  | 15 | 15  | 0    | 0   | -7 | 16 | 22  | 22   | 7   | -4 | 16 | 27  | 20   |
| -1  | 3   | 15 | 23  | 22   | 3   | 6  | 15 | 0   | 7    | -4  | 12  | 15 | -17 | 24   | 1   | -7 | 16 | 102 | 79   | 8   | -4 | 16 | 12  | 1    |
| 0   | 3   | 15 | 29  | 19   | 4   | 6  | 15 | 31  | 4    | -3  | 12  | 15 | 7   | 17   | 2   | -7 | 16 | 0   | 3    | 9   | -4 | 16 | 17  | 6    |
| 1   | 3   | 15 | 8   | 3    | 5   | 6  | 15 | 47  | 10   | -2  | 12  | 15 | 3   | 7    | 3   | -7 | 16 | 106 | 114  | 10  | -4 | 16 | 23  | 7    |
| 2   | 3   | 15 | 137 | 105  | -12 | 7  | 15 | 0   | 2    | -3  | -13 | 16 | 1   | 1    | 4   | -7 | 16 | 8   | 27   | -10 | -3 | 16 | 10  | 4    |
| 3   | 3   | 15 | 182 | 192  | -11 | 7  | 15 | 14  | 9    | -2  | -13 | 16 | 20  | 6    | 5   | -7 | 16 | 20  | 6    | 5   | -7 | 16 | 21  | 14   |
| 4   | 3   | 15 | 18  | 2    | -10 | 7  | 15 | 4   | 25   | -4  | -12 | 16 | -15 | 2    | 6   | -7 | 16 | 0   | 4    | -8  | -3 | 16 | 22  | 27   |
| 5   | 3   | 15 | 61  | 44   | -9  | 7  | 15 | 2   | 0    | -3  | -12 | 16 | 42  | 15   | 7   | -7 | 16 | 24  | 20   | -7  | -3 | 16 | 4   | 1    |
| 6   | 3   | 15 | 1   | 9    | -8  | 7  | 15 | -2  | 13   | -2  | -12 | 16 | -9  | 0    | 8   | -7 | 16 | 24  | 23   | -6  | -3 | 16 | 39  | 34   |
| 7   | 3   | 15 | 15  | 25   | -7  | 7  | 15 | 26  | 12   | -1  | -12 | 16 | -4  | 9    | 9   | -7 | 16 | -14 | 0    | -5  | -3 | 16 | 20  | 15   |
| 8   | 3   | 15 | 41  | 8    | -6  | 7  | 15 | 66  | 50   | 0   | -12 | 16 | 15  | 13   | -9  | -6 | 16 | 20  | 12   | -4  | -3 | 16 | 17  | 13   |
| -13 | 4   | 15 | 56  | 26   | -5  | 7  | 15 | -1  | 4    | -6  | -11 | 16 | 2   | 10   | -8  | -6 | 16 | 131 | 106  | -3  | -3 | 16 | 59  | 54   |
| -12 | 4   | 15 | 14  | 5    | -4  | 7  | 15 | 31  | 24   | -5  | -11 | 16 | 9   | 8    | -7  | -6 | 16 | 99  | 78   | -2  | -3 | 16 | 245 | 202  |
| -11 | 4   | 15 | -6  | 0    | -3  | 7  | 15 | 15  | 18   | -4  | -11 | 16 | 11  | 10   | -6  | -6 | 16 | 18  | 4    | -1  | -3 | 16 | 213 | 202  |
| -10 | 4   | 15 | -8  | 2    | -2  | 7  | 15 | 0   | 3    | -3  | -11 | 16 | 10  | 0    | -5  | -6 | 16 | 21  | 26   | 0   | -3 | 16 | 0   | 0    |
| -9  | 4   | 15 | 11  | 26   | -1  | 7  | 15 | 24  | 37   | -2  | -11 | 16 | -4  | 5    | -4  | -6 | 16 | 40  | 31   | 1   | -3 | 16 | 21  | 18   |
| -8  | 4   | 15 | 18  | 6    | 0   | 7  | 15 | 52  | 53   | -1  | -11 | 16 | -6  | 0    | -3  | -6 | 16 | 8   | 1    | 2   | -3 | 16 | 11  | 3    |
| -7  | 4   | 15 | 1   | 4    | 1   | 7  | 15 | -4  | 7    | 0   | -11 | 16 | 14  | 2    | -2  | -6 | 16 | 11  | 1    | 3   | -3 | 16 | 39  | 39   |
| -6  | 4   | 15 | 13  | 5    | 2   | 7  | 15 | 7   | 2    | 1   | -11 | 16 | 7   | 9    | -1  | -6 | 16 | 36  | 51   | 4   | -3 | 16 | 6   | 0    |
| -5  | 4   | 15 | 9   | 2    | 3   | 7  | 15 | 62  | 50   | -7  | -10 | 16 | -5  | 0    | 0   | -6 | 16 | 113 | 98   | 5   | -3 | 16 | 29  | 31   |
| -4  | 4   | 15 | 63  | 57   | 4   | 7  | 15 | 83  | 65   | -6  | -10 | 16 | 4   | 6    | 1   | -6 | 16 | 6   | 3    | 6   | -3 | 16 | 13  | 10   |
| -3  | 4   | 15 | 108 | 117  | -11 | 8  | 15 | 33  | 8    | -5  | -10 | 16 | -1  | 0    | 2   | -6 | 16 | 243 | 247  | 7   | -3 | 16 | -5  | 1    |
| -2  | 4   | 15 | 99  | 100  | -10 | 8  | 15 | 25  | 0    | -4  | -10 | 16 | -10 | 1    | 3   | -6 | 16 | 4   | 13   | 8   | -3 | 16 | 19  | 24   |
| -1  | 4   | 15 | 21  | 29   | -9  | 8  | 15 | 13  | 16   | -3  | -10 | 16 | 0   | 15   | 4   | -6 | 16 | -4  | 2    | 9   | -3 | 16 | -8  | 0    |
| 0   | 4   | 15 | 72  | 63   | -8  | 8  | 15 | 16  | 15   | -2  | -10 | 16 | 7   | 0    | 5   | -6 | 16 | 8   | 3    | 10  | -3 | 16 | 58  | 23   |
| 1   | 4   | 15 | 130 | 120  | -7  | 8  | 15 | 22  | 10   | -1  | -10 | 16 | 9   | 2    | 6   | -6 | 16 | 14  | 23   | -10 | -2 | 16 | 30  | 8    |
| 2   | 4   | 15 | 35  | 33   | -6  | 8  | 15 | -6  | 0    | 0   | -10 | 16 | 20  | 23   | 7   | -6 | 16 | 3   | 1    | -9  | -2 | 16 | 17  | 14   |
| 3   | 4   | 15 | 45  | 13   | -5  | 8  | 15 | 19  | 28   | 1   | -10 | 16 | 28  | 20   | 8   | -6 | 16 | 21  | 12   | -8  | -2 | 16 | 1   | 0    |
| 4   | 4   | 15 | 109 | 116  | -4  | 8  | 15 | 24  | 22   | -2  | -10 | 16 | 13  | 20   | 9   | -6 | 16 | 27  | 32   | -7  | -2 | 16 | 42  | 37   |
| 5   | 4   | 15 | 70  | 73   | -3  | 8  | 15 | -4  | 0    | -7  | -9  | 16 | 5   | 3    | 10  | -6 | 16 | 29  | 18   | -6  | -2 | 16 | 64  | 58   |
| 6   | 4   | 15 | -4  | 0    | -2  | 8  | 15 | 0   | 11   | -6  | -9  | 16 | 21  | 3    | -9  | -5 | 16 | 3   | 8    | -5  | -2 | 16 | 9   | 9    |
| 7   | 4   | 15 | -13 | 6    | -1  | 8  | 15 | 14  | 35   | -5  | -9  | 16 | -1  | 23   | -8  | -5 | 16 | 6   | 1    | -4  | -2 | 16 | 0   | 1    |
| -13 | 5   | 15 | 46  | 1    | 0   |    |    |     |      |     |     |    |     |      |     |    |    |     |      |     |    |    |     |      |

Table A.3, continued

| M   | K   | L  | Obs | Calc | M   | K | L  | Obs | Calc | M   | K  | L  | Obs | Calc | M  | K  | L  | Obs | Calc | M   | K  | L  | Obs | Calc |
|-----|-----|----|-----|------|-----|---|----|-----|------|-----|----|----|-----|------|----|----|----|-----|------|-----|----|----|-----|------|
| 7   | -1  | 16 | 8   | 13   | -12 | 3 | 16 | 6   | 3    | -2  | 6  | 16 | -1  | 6    | -2 | -9 | 17 | 26  | 22   | -5  | -4 | 17 | 0   | 0    |
| 8   | -1  | 16 | 17  | 4    | -11 | 3 | 16 | -6  | 0    | -1  | 6  | 16 | 38  | 32   | -1 | -9 | 17 | 11  | 1    | -4  | -4 | 17 | 7   | 9    |
| 9   | -1  | 16 | 6   | 22   | -10 | 3 | 16 | 29  | 19   | 0   | 6  | 16 | -1  | 5    | 0  | -9 | 17 | 5   | 4    | -3  | -4 | 17 | 14  | 13   |
| -11 | 0   | 16 | -2  | 3    | -9  | 3 | 16 | 60  | 39   | 1   | 6  | 16 | 0   | 2    | -7 | -8 | 17 | 8   | 35   | -2  | -4 | 17 | 55  | 53   |
| -10 | 0   | 16 | 1   | 19   | -8  | 3 | 16 | -3  | 2    | 2   | 6  | 16 | 2   | 1    | -6 | -8 | 17 | 8   | 2    | -1  | -4 | 17 | 3   | 0    |
| -9  | 0   | 16 | 28  | 18   | -7  | 3 | 16 | 11  | 12   | 3   | 6  | 16 | 74  | 51   | -5 | -8 | 17 | -9  | 5    | 0   | -4 | 17 | -1  | 0    |
| -8  | 0   | 16 | -6  | 0    | -6  | 3 | 16 | 20  | 15   | 4   | 6  | 16 | 5   | 27   | -4 | -8 | 17 | 22  | 14   | 1   | -4 | 17 | 63  | 57   |
| -7  | 0   | 16 | 18  | 1    | -5  | 3 | 16 | 9   | 1    | -11 | 7  | 16 | 12  | 15   | -3 | -8 | 17 | 15  | 18   | 2   | -4 | 17 | 69  | 67   |
| -6  | 0   | 16 | 13  | 19   | -4  | 3 | 16 | 67  | 56   | -10 | 7  | 16 | -13 | 13   | 0  | -8 | 17 | -6  | 0    | 3   | -4 | 17 | 72  | 44   |
| -5  | 0   | 16 | 27  | 28   | -3  | 3 | 16 | 50  | 54   | -9  | 7  | 16 | 15  | 5    | -1 | -8 | 17 | 32  | 21   | 4   | -4 | 17 | -4  | 1    |
| -4  | 0   | 16 | 31  | 35   | -2  | 3 | 16 | 29  | 30   | -8  | 7  | 16 | 12  | 5    | 0  | -8 | 17 | 5   | 9    | 5   | -4 | 17 | 13  | 21   |
| -3  | 0   | 16 | 69  | 66   | -1  | 3 | 16 | 33  | 39   | -7  | 7  | 16 | 4   | 2    | 1  | -8 | 17 | 9   | 5    | 6   | -4 | 17 | 70  | 34   |
| -2  | 0   | 16 | 37  | 43   | 0   | 3 | 16 | 248 | 246  | -6  | 7  | 16 | 25  | 4    | -8 | -7 | 17 | 41  | 25   | 7   | -4 | 17 | -7  | 3    |
| -1  | 0   | 16 | 4   | 9    | 1   | 3 | 16 | 175 | 172  | -5  | 7  | 16 | 2   | 2    | -7 | -7 | 17 | -16 | 0    | 8   | -4 | 17 | 5   | 7    |
| 0   | 0   | 16 | 96  | 86   | 2   | 3 | 16 | 29  | 47   | -4  | 7  | 16 | 1   | 1    | -6 | -7 | 17 | -11 | 25   | 9   | -4 | 17 | 36  | 7    |
| 1   | 0   | 16 | 64  | 110  | 3   | 3 | 16 | 67  | 59   | -3  | 7  | 16 | 19  | 7    | -5 | -7 | 17 | 23  | 43   | -8  | -3 | 17 | 3   | 7    |
| 2   | 0   | 16 | 82  | 48   | 4   | 3 | 16 | 69  | 60   | -2  | 7  | 16 | 39  | 35   | -4 | -7 | 17 | 32  | 12   | -7  | -3 | 17 | 7   | 9    |
| 3   | 0   | 16 | 8   | 0    | 5   | 3 | 16 | 14  | 26   | -1  | 7  | 16 | 38  | 44   | -3 | -7 | 17 | 0   | 0    | -6  | -3 | 17 | -1  | 1    |
| 4   | 0   | 16 | 8   | 17   | 6   | 3 | 16 | 16  | 0    | 0   | 7  | 16 | 0   | 2    | -2 | -7 | 17 | 20  | 25   | -5  | -3 | 17 | 7   | 5    |
| 5   | 0   | 16 | 65  | 64   | 7   | 3 | 16 | -12 | 10   | 1   | 7  | 16 | 23  | 1    | -1 | -7 | 17 | -7  | 13   | -4  | -3 | 17 | 10  | 7    |
| 6   | 0   | 16 | 26  | 1    | -12 | 4 | 16 | 20  | 8    | -2  | 7  | 16 | 32  | 60   | 0  | -7 | 17 | 5   | 7    | -3  | -3 | 17 | 89  | 79   |
| 7   | 0   | 16 | 26  | 45   | -11 | 4 | 16 | 17  | 18   | -10 | 8  | 16 | 23  | 9    | 1  | -7 | 17 | 15  | 18   | -2  | -3 | 17 | 8   | 1    |
| 8   | 0   | 16 | 4   | 21   | -10 | 4 | 16 | 28  | 28   | -9  | 8  | 16 | -4  | 5    | 2  | -7 | 17 | 22  | 14   | -1  | -3 | 17 | 58  | 57   |
| 9   | 0   | 16 | 33  | 3    | -9  | 4 | 16 | -5  | 2    | -8  | 8  | 16 | 3   | 0    | 3  | -7 | 17 | 26  | 31   | 0   | -3 | 17 | 77  | 68   |
| -12 | 1   | 16 | -9  | 20   | -8  | 4 | 16 | 18  | 4    | -7  | 8  | 16 | 31  | 5    | 4  | -7 | 17 | 11  | 9    | 1   | -3 | 17 | 21  | 27   |
| -11 | 1   | 16 | -1  | 20   | -7  | 4 | 16 | 0   | 0    | -6  | 8  | 16 | 4   | 9    | 5  | -7 | 17 | 25  | 13   | 2   | -3 | 17 | 7   | 0    |
| -10 | 1   | 16 | 14  | 15   | -6  | 4 | 16 | 9   | 0    | -5  | 8  | 16 | 8   | 15   | 6  | -7 | 17 | 26  | 9    | 3   | -3 | 17 | 0   | 16   |
| -9  | 1   | 16 | 16  | 0    | -5  | 4 | 16 | -5  | 3    | -4  | 8  | 16 | -6  | 10   | -8 | -6 | 17 | 26  | 8    | 4   | -3 | 17 | 5   | 11   |
| -8  | 1   | 16 | 13  | 24   | -4  | 4 | 16 | -4  | 12   | -3  | 8  | 16 | 19  | 20   | -7 | -6 | 17 | 74  | 63   | 5   | -3 | 17 | 12  | 0    |
| -7  | 1   | 16 | 29  | 20   | -3  | 4 | 16 | 0   | 1    | -2  | 8  | 16 | 8   | 19   | -6 | -6 | 17 | 27  | 40   | 6   | -3 | 17 | 8   | 3    |
| -6  | 1   | 16 | 8   | 14   | -2  | 4 | 16 | 9   | 4    | -1  | 8  | 16 | 24  | 0    | -5 | -6 | 17 | 16  | 4    | 7   | -3 | 17 | 23  | 14   |
| -5  | 1   | 16 | 19  | 12   | -1  | 4 | 16 | 80  | 87   | 0   | 8  | 16 | 12  | 11   | -4 | -6 | 17 | 9   | 13   | 6   | -3 | 17 | 1   | 9    |
| -4  | 1   | 16 | 87  | 81   | 0   | 4 | 16 | 64  | 50   | -9  | 9  | 16 | 13  | 3    | -6 | -6 | 17 | 19  | 21   | 9   | -3 | 17 | 4   | 12   |
| -3  | 1   | 16 | 47  | 46   | 1   | 4 | 16 | -3  | 0    | -8  | 9  | 16 | -12 | 14   | -2 | -6 | 17 | 46  | 52   | -9  | -2 | 17 | 14  | 12   |
| -2  | 1   | 16 | -3  | 0    | 2   | 4 | 16 | 26  | 25   | -7  | 9  | 16 | 18  | 30   | -1 | -6 | 17 | 17  | 3    | -8  | -2 | 17 | 36  | 33   |
| -1  | 1   | 16 | 85  | 87   | 3   | 4 | 16 | 26  | 51   | -6  | 9  | 16 | 59  | 69   | 0  | -6 | 17 | 3   | 8    | -7  | -2 | 17 | 5   | 2    |
| 0   | 1   | 16 | 37  | 39   | 4   | 4 | 16 | 27  | 2    | -5  | 9  | 16 | -1  | 18   | 1  | -6 | 17 | 49  | 55   | -6  | -2 | 17 | 0   | 0    |
| 1   | 1   | 16 | -4  | 1    | 5   | 4 | 16 | 11  | 5    | -4  | 9  | 16 | 2   | 0    | 2  | -6 | 17 | 27  | 40   | -5  | -2 | 17 | 4   | 5    |
| 2   | 1   | 16 | 26  | 46   | 6   | 4 | 16 | -9  | 9    | -2  | 9  | 16 | 31  | 12   | 3  | -6 | 17 | 27  | 3    | -4  | -2 | 17 | -3  | 1    |
| 3   | 1   | 16 | 133 | 127  | -12 | 5 | 16 | 59  | 0    | -1  | 9  | 16 | 11  | 19   | 4  | -6 | 17 | -4  | 0    | -3  | -2 | 17 | 9   | 9    |
| 4   | 1   | 16 | 49  | 59   | -11 | 5 | 16 | 9   | 0    | -8  | 10 | 16 | 10  | 1    | 5  | -6 | 17 | 22  | 0    | -2  | -2 | 17 | 164 | 144  |
| -1  | -2  | 17 | 105 | 95   | 6   | 1 | 17 | -9  | 5    | -3  | 5  | 17 | 22  | 18   | -2 | -6 | 18 | -5  | 6    | -4  | -1 | 18 | 79  | 78   |
| 0   | -2  | 17 | 3   | 0    | 7   | 1 | 17 | 9   | 2    | -2  | 5  | 17 | 22  | 8    | -3 | -5 | 18 | 9   | 0    | -3  | -1 | 18 | 0   | 0    |
| 1   | -2  | 17 | 19  | 18   | -12 | 2 | 17 | 27  | 0    | -1  | 5  | 17 | 18  | 10   | -7 | -5 | 18 | 10  | 3    | -2  | -1 | 18 | 2   | 1    |
| 2   | -2  | 17 | 42  | 30   | -11 | 2 | 17 | -4  | 5    | 0   | 5  | 17 | 17  | 0    | -6 | -5 | 18 | 30  | 16   | -1  | -1 | 18 | 56  | 51   |
| 3   | -2  | 17 | 41  | 35   | -10 | 2 | 17 | 54  | 44   | 1   | 5  | 17 | -4  | 0    | -5 | -5 | 18 | 0   | 1    | 0   | -1 | 18 | 21  | 9    |
| 4   | -2  | 17 | 9   | 1    | -9  | 2 | 17 | 34  | 20   | 2   | 5  | 17 | 45  | 6    | -4 | -5 | 18 | -8  | 1    | 1   | -1 | 18 | -4  | 2    |
| 5   | -2  | 17 | 30  | 16   | -8  | 2 | 17 | 26  | 10   | 3   | 5  | 17 | 55  | 40   | -3 | -5 | 18 | 14  | 3    | 2   | -1 | 18 | 40  | 21   |
| 6   | -2  | 17 | 40  | 49   | -7  | 2 | 17 | 12  | 14   | 4   | 5  | 17 | 47  | 1    | -2 | -5 | 18 | 24  | 22   | 3   | -1 | 18 | 39  | 36   |
| 7   | -2  | 17 | 8   | 9    | -6  | 2 | 17 | 7   | 9    | -11 | 6  | 17 | 0   | 10   | -1 | -5 | 18 | 2   | 2    | 4   | -1 | 18 | 18  | 6    |
| 8   | -2  | 17 | 4   | 15   | -5  | 2 | 17 | 12  | 0    | -10 | 6  | 17 | -2  | 1    | 0  | -5 | 18 | 26  | 25   | 5   | -1 | 18 | -4  | 21   |
| 9   | -2  | 17 | 20  | 28   | -4  | 2 | 17 | 38  | 30   | -9  | 6  | 17 | -1  | 0    | 1  | -5 | 18 | 38  | 50   | 6   | -1 | 18 | 10  | 4    |
| -10 | -1  | 17 | -8  | 2    | -3  | 2 | 17 | 34  | 34   | -8  | 6  | 17 | 6   | 0    | 2  | -5 | 18 | 33  | 50   | 7   | -1 | 18 | -11 | 23   |
| -9  | -1  | 17 | 3   | 2    | -2  | 2 | 17 | 7   | 6    | -7  | 6  | 17 | 10  | 0    | 3  | -5 | 18 | 19  | 5    | -8  | 0  | 18 | 9   | 0    |
| -8  | -1  | 17 | 3   | 4    | -1  | 2 | 17 | 67  | 80   | -6  | 6  | 17 | 5   | 2    | 4  | -5 | 18 | -2  | 3    | -7  | 0  | 18 | 9   | 0    |
| -7  | -1  | 17 | 4   | 5    | 0   | 2 | 17 | 260 | 234  | -5  | 6  | 17 | -1  | 1    | 5  | -5 | 18 | 35  | 29   | -6  | 0  | 18 | 12  | 17   |
| -6  | -1  | 17 | -2  | 2    | 1   | 2 | 17 | 58  | 38   | -4  | 6  | 17 | 0   | 6    | -8 | -4 | 18 | 11  | 13   | -5  | 0  | 18 | 8   | 15   |
| -5  | -1  | 17 | 16  | 21   | 2   | 2 | 17 | -1  | 0    | -3  | 6  | 17 | -1  | 8    | -7 | -4 | 18 | -1  | 0    | -4  | 0  | 18 | 3   | 3    |
| -4  | -1  | 17 | 144 | 148  | 3   | 2 | 17 | 27  | 40   | -2  | 6  | 17 | 45  | 32   | -6 | -4 | 18 | 16  | 6    | -3  | 0  | 18 | 0   | 5    |
| -3  | -1  | 17 | 179 | 189  | 4   | 2 | 17 | 5   | 23   | -1  | 6  | 17 | -4  | 4    | -5 | -4 | 18 | 30  | 21   | -2  | 0  | 18 | 12  | 4    |
| -2  | -1  | 17 | 50  | 49   | 5   | 2 | 17 | 18  | 10   | 0   | 6  | 17 | 18  | 3    | -4 | -4 | 18 | 45  | 38   | -1  | 0  | 18 | 3   | 3    |
| -1  | -1  | 17 | 5   | 3    | 6   | 2 | 17 | 8   | 3    | 1   | 6  | 17 | -11 | 7    | -3 | -4 | 18 | 67  | 63   | 0   | 0  | 18 | 36  | 33   |
| 0   | -1  | 17 | 33  | 39   | 7   | 2 | 17 | 6   | 32   | 2   | 6  | 17 | 22  | 48   | -2 | -4 | 18 | 12  | 4    | 1   | 0  | 18 | 19  | 24   |
| 1   | -1  | 17 | 43  | 31   | -12 | 3 | 17 | 20  | 3    | -10 | 7  | 17 | 19  | 3    | -1 | -4 | 18 | 13  | 17   | 2   | 0  | 18 | 6   | 21   |
| 2   | -1  | 17 | 10  | 0    | -11 | 3 | 17 | 11  | 16   | -9  | 7  | 17 | 26  | 1    | 0  | -4 | 18 | 43  | 35   | 3   | 0  | 18 | -11 | 6    |
| 3   | -1  | 17 | 6   | 1    | -10 | 3 | 17 | -6  | 1    | -8  | 7  | 17 | 20  | 6    | 1  | -4 | 18 | 6   | 7    | 4   | 0  | 18 | 72  | 57   |
| 4   | -1  | 17 | 15  | 23   | -9  | 3 | 17 | 11  | 28   | -7  | 7  | 17 | 16  | 21   | 2  | -4 | 18 | 55  | 19   | 5   | 0  | 18 | 27  | 19   |
| 5   | -1  | 17 | 12  | 8    | -8  | 3 | 17 | 24  | 12   | -6  | 7  | 17 | 11  | 33   | 3  | -4 | 18 | 45  | 24   | 6   | 0  | 18 | 23  | 2    |
| 6   | -1  | 17 | 5   | 14   | -7  | 3 | 17 | 14  | 1    | -5  | 7  | 17 | 30  | 9    | 4  | -4 | 18 | 11  | 4    | 7   | 0  | 18 | 28  | 22   |
| 7   | -1  | 17 | 9   | 5    | -6  | 3 | 17 | 14  | 5    | -4  | 7  | 17 | 7   | 23   | 5  | -4 | 18 | -6  | 1    | -12 | 1  | 18 | -15 | 8    |
| 8   | -1  | 17 | 15  | 2    | -5  | 3 | 17 | 27  | 18   | -3  | 7  | 17 | 26  | 34   | 6  | -4 | 18 | 64  | 46   | -11 | 1  | 18 | -7  | 13   |
| -10 | 0   | 17 | -7  | 2    | -4  | 3 | 17 | -3  | 0    | -2  | 7  | 17 | -3  | 5    | 7  | -4 | 18 | -9  | 7    | -10 | 1  | 18 | 23  | 28   |
| -9  | 0   | 17 | -7  | 1    | -3  | 3 | 17 | -3  | 4    | -1  | 7  | 17 | 0   | 12   | -7 | -3 | 18 | 4   | 0    | -9  | 1  | 18 | 8   | 0    |
| -8  | 0</ |    |     |      |     |   |    |     |      |     |    |    |     |      |    |    |    |     |      |     |    |    |     |      |

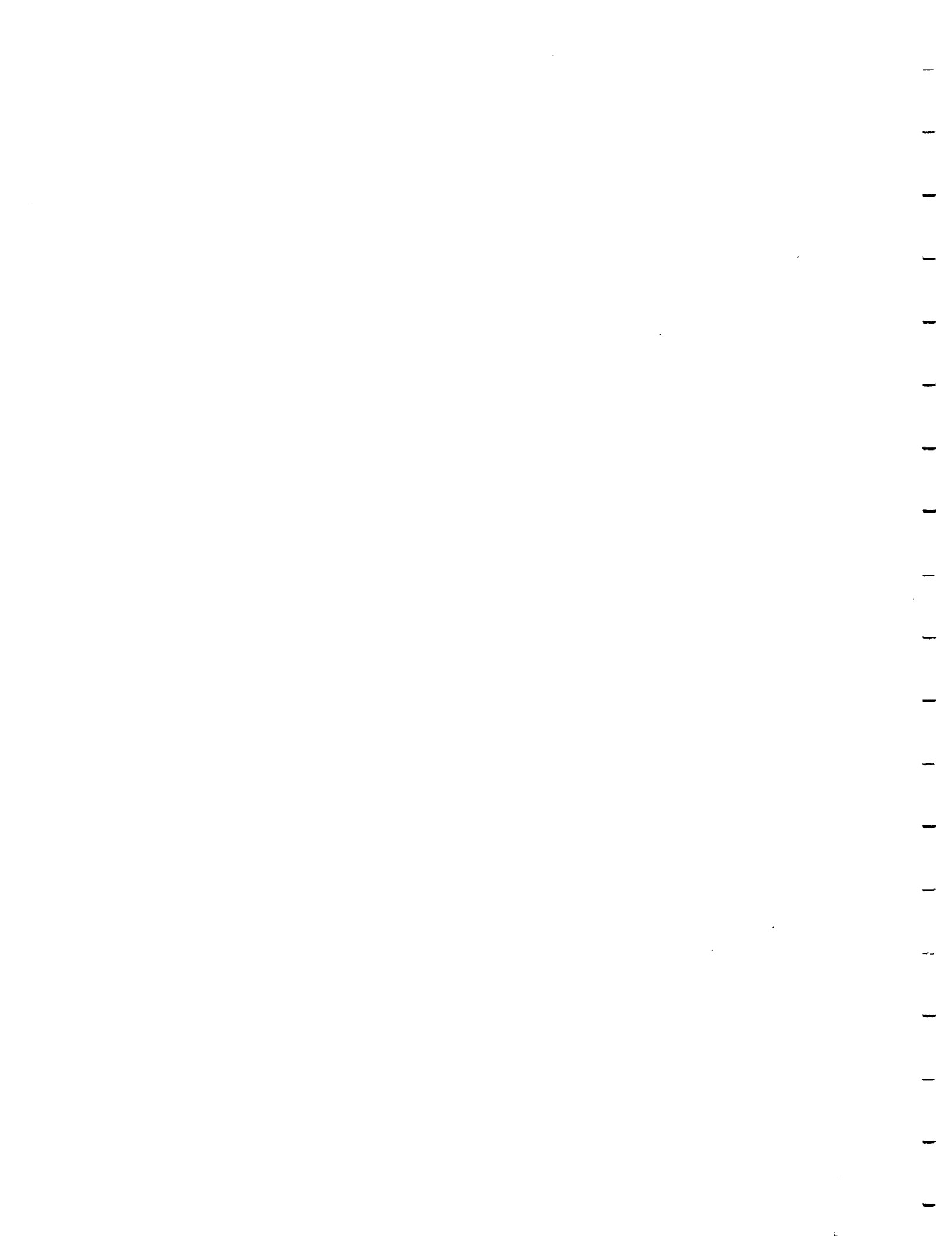
Table A.3, continued

| H   | K | L  | Obs | Calc | H   | K  | L  | Obs | Calc | H   | K  | L  | Obs | Calc | H   | K  | L  | Obs | Calc | H   | K | L  | Obs | Calc |
|-----|---|----|-----|------|-----|----|----|-----|------|-----|----|----|-----|------|-----|----|----|-----|------|-----|---|----|-----|------|
| 3   | 1 | 17 | 18  | 11   | -6  | 5  | 17 | -5  | 0    | -5  | -6 | 18 | 0   | 19   | -7  | -1 | 18 | -5  | 0    | 5   | 2 | 18 | 54  | 46   |
| 4   | 1 | 17 | 56  | 37   | -5  | 5  | 17 | 17  | 6    | -4  | -6 | 18 | -8  | 7    | -6  | -1 | 18 | 48  | 29   | 6   | 2 | 18 | -13 | 20   |
| 5   | 1 | 17 | 50  | 47   | -4  | 5  | 17 | 5   | 20   | -3  | -6 | 18 | 9   | 16   | -5  | -1 | 18 | 96  | 107  | -11 | 3 | 18 | -17 | 1    |
| -10 | 3 | 18 | -1  | 16   | -7  | -4 | 19 | 34  | 5    | 4   | 1  | 19 | 19  | 26   | -7  | 0  | 20 | 45  | 34   |     |   |    |     |      |
| -9  | 3 | 18 | 14  | 3    | -7  | -3 | 19 | 11  | 2    | 5   | 1  | 19 | 23  | 4    | -6  | 0  | 20 | 19  | 29   |     |   |    |     |      |
| -8  | 3 | 18 | 14  | 5    | -6  | -3 | 19 | -5  | 4    | -11 | 2  | 19 | -18 | 2    | -10 | 1  | 20 | -15 | 1    |     |   |    |     |      |
| -7  | 3 | 18 | 22  | 11   | -3  | -3 | 19 | 16  | 13   | -10 | 2  | 19 | -14 | 5    | -9  | 1  | 20 | -11 | 6    |     |   |    |     |      |
| -6  | 3 | 18 | 6   | 12   | -2  | -3 | 19 | 5   | 0    | -9  | 2  | 19 | -6  | 4    | -8  | 1  | 20 | -23 | 10   |     |   |    |     |      |
| -5  | 3 | 18 | 24  | 3    | -1  | -3 | 19 | 0   | 29   | -8  | 2  | 19 | 36  | 3    | -7  | 1  | 20 | 0   | 14   |     |   |    |     |      |
| -4  | 3 | 18 | 13  | 18   | 0   | -3 | 19 | 54  | 40   | -7  | 2  | 19 | 27  | 3    | -1  | 1  | 20 | 15  | 7    |     |   |    |     |      |
| -3  | 3 | 18 | 16  | 19   | 1   | -3 | 19 | -6  | 1    | -6  | 2  | 19 | 5   | 1    | 0   | 1  | 20 | -3  | 0    |     |   |    |     |      |
| -2  | 3 | 18 | -1  | 3    | 2   | -3 | 19 | 8   | 6    | -5  | 2  | 19 | 23  | 5    | 1   | 1  | 20 | -3  | 0    |     |   |    |     |      |
| -1  | 3 | 18 | 63  | 38   | 3   | -3 | 19 | 42  | 40   | -4  | 2  | 19 | 18  | 16   | -8  | 2  | 20 | 31  | 0    |     |   |    |     |      |
| 0   | 3 | 18 | 22  | 38   | -3  | -2 | 19 | 81  | 36   | -3  | 2  | 19 | -8  | 4    | -3  | 2  | 20 | -9  | 10   |     |   |    |     |      |
| 1   | 3 | 18 | -4  | 0    | -4  | -2 | 19 | 27  | 9    | -2  | 2  | 19 | 13  | 0    | -2  | 2  | 20 | 35  | 15   |     |   |    |     |      |
| 2   | 3 | 18 | -13 | 1    | -3  | -2 | 19 | 17  | 5    | -1  | 2  | 19 | 29  | 20   | -1  | 2  | 20 | -14 | 6    |     |   |    |     |      |
| 3   | 3 | 18 | 0   | 16   | -2  | -2 | 19 | 30  | 21   | 0   | 2  | 19 | -4  | 2    | 0   | 2  | 20 | 8   | 3    |     |   |    |     |      |
| 4   | 3 | 18 | 10  | 30   | -1  | -2 | 19 | 43  | 34   | 1   | 2  | 19 | 14  | 0    | 1   | 2  | 20 | 53  | 2    |     |   |    |     |      |
| 5   | 3 | 18 | 0   | 2    | 0   | -2 | 19 | 10  | 2    | 2   | 2  | 19 | -6  | 0    | 2   | 2  | 20 | 41  | 17   |     |   |    |     |      |
| -11 | 4 | 18 | -4  | 8    | 1   | -2 | 19 | 38  | 22   | 3   | 2  | 19 | -10 | 25   | -4  | 3  | 20 | 52  | 21   |     |   |    |     |      |
| -10 | 4 | 18 | 22  | 1    | 2   | -2 | 19 | 26  | 13   | 4   | 2  | 19 | 32  | 4    | -3  | 3  | 20 | -13 | 9    |     |   |    |     |      |
| -9  | 4 | 18 | -8  | 8    | 3   | -2 | 19 | 25  | 14   | -10 | 3  | 19 | 6   | 0    | -2  | 3  | 20 | -11 | 6    |     |   |    |     |      |
| -8  | 4 | 18 | 5   | 1    | 4   | -2 | 19 | -8  | 3    | -9  | 3  | 19 | -12 | 8    | -1  | 3  | 20 | -16 | 6    |     |   |    |     |      |
| -7  | 4 | 18 | 13  | 8    | 5   | -2 | 19 | 11  | 3    | -8  | 3  | 19 | -7  | 1    | 0   | 3  | 20 | 15  | 14   |     |   |    |     |      |
| -6  | 4 | 18 | 13  | 3    | -7  | -1 | 19 | 46  | 8    | -7  | 3  | 19 | -7  | 1    | -4  | 4  | 20 | 18  | 3    |     |   |    |     |      |
| -5  | 4 | 18 | 2   | 2    | -6  | -1 | 19 | 18  | 4    | -6  | 3  | 19 | 1   | 1    | -3  | 4  | 20 | 17  | 0    |     |   |    |     |      |
| -4  | 4 | 18 | 5   | 0    | -5  | -1 | 19 | -5  | 1    | -5  | 3  | 19 | -6  | 2    | -2  | 4  | 20 | 43  | 4    |     |   |    |     |      |
| -3  | 4 | 18 | -5  | 3    | -4  | -1 | 19 | 9   | 22   | -4  | 3  | 19 | 2   | 4    | -1  | 4  | 20 | 0   | 0    |     |   |    |     |      |
| -2  | 4 | 18 | 17  | 24   | -3  | -1 | 19 | 22  | 18   | -3  | 3  | 19 | 39  | 15   |     |    |    |     |      |     |   |    |     |      |
| -1  | 4 | 18 | 45  | 51   | -2  | -1 | 19 | 18  | 9    | -2  | 3  | 19 | 33  | 64   |     |    |    |     |      |     |   |    |     |      |
| 0   | 4 | 18 | 8   | 6    | -1  | -1 | 19 | 11  | 0    | -1  | 3  | 19 | 22  | 42   |     |    |    |     |      |     |   |    |     |      |
| 1   | 4 | 18 | 35  | 2    | 0   | -1 | 19 | 45  | 43   | 0   | 3  | 19 | 16  | 10   |     |    |    |     |      |     |   |    |     |      |
| 2   | 4 | 18 | 10  | 20   | 1   | -1 | 19 | 15  | 5    | 1   | 3  | 19 | 4   | 0    |     |    |    |     |      |     |   |    |     |      |
| 3   | 4 | 18 | 9   | 10   | 2   | -1 | 19 | -2  | 1    | 2   | 3  | 19 | 56  | 23   |     |    |    |     |      |     |   |    |     |      |
| 4   | 4 | 18 | -15 | 14   | 3   | -1 | 19 | -11 | 12   | 3   | 3  | 19 | -10 | 4    |     |    |    |     |      |     |   |    |     |      |
| -10 | 5 | 18 | -1  | 2    | 4   | -1 | 19 | -12 | 11   | -9  | 4  | 19 | 29  | 1    |     |    |    |     |      |     |   |    |     |      |
| -9  | 5 | 18 | 8   | 0    | 5   | -1 | 19 | 19  | 1    | -8  | 4  | 19 | 20  | 3    |     |    |    |     |      |     |   |    |     |      |
| -8  | 5 | 18 | -5  | 0    | 6   | -1 | 19 | 25  | 3    | -7  | 4  | 19 | 5   | 3    |     |    |    |     |      |     |   |    |     |      |
| -7  | 5 | 18 | 5   | 0    | -10 | 0  | 19 | 25  | 7    | -6  | 4  | 19 | 31  | 27   |     |    |    |     |      |     |   |    |     |      |
| -6  | 5 | 18 | -7  | 4    | -9  | 0  | 19 | 21  | 4    | -5  | 4  | 19 | -7  | 11   |     |    |    |     |      |     |   |    |     |      |
| -5  | 5 | 18 | -6  | 1    | -8  | 0  | 19 | -6  | 4    | -4  | 4  | 19 | 12  | 27   |     |    |    |     |      |     |   |    |     |      |
| -4  | 5 | 18 | 12  | 16   | -7  | 0  | 19 | -3  | 0    | -3  | 4  | 19 | 4   | 38   |     |    |    |     |      |     |   |    |     |      |
| -3  | 5 | 18 | 32  | 27   | -6  | 0  | 19 | 2   | 0    | -2  | 4  | 19 | 39  | 42   |     |    |    |     |      |     |   |    |     |      |
| -2  | 5 | 18 | 31  | 40   | -5  | 0  | 19 | -5  | 10   | -1  | 4  | 19 | -1  | 2    |     |    |    |     |      |     |   |    |     |      |
| -1  | 5 | 18 | -13 | 0    | -4  | 0  | 19 | 20  | 8    | 0   | 4  | 19 | 19  | 9    |     |    |    |     |      |     |   |    |     |      |
| 0   | 5 | 18 | 0   | 1    | -3  | 0  | 19 | 5   | 1    | 1   | 4  | 19 | -11 | 21   |     |    |    |     |      |     |   |    |     |      |
| 1   | 5 | 18 | 0   | 14   | -2  | 0  | 19 | -5  | 2    | 2   | 4  | 19 | -11 | 3    |     |    |    |     |      |     |   |    |     |      |
| 2   | 5 | 18 | 60  | 28   | -1  | 0  | 19 | 21  | 15   | -9  | 5  | 19 | -9  | 9    |     |    |    |     |      |     |   |    |     |      |
| -10 | 6 | 18 | 31  | 1    | 0   | 0  | 19 | 14  | 4    | -8  | 5  | 19 | 7   | 3    |     |    |    |     |      |     |   |    |     |      |
| -9  | 6 | 18 | -17 | 7    | 1   | 0  | 19 | 30  | 25   | -7  | 5  | 19 | 5   | 5    |     |    |    |     |      |     |   |    |     |      |
| -8  | 6 | 18 | 41  | 6    | 2   | 0  | 19 | 11  | 11   | -6  | 5  | 19 | 10  | 27   |     |    |    |     |      |     |   |    |     |      |
| -7  | 6 | 18 | 14  | 11   | 3   | 0  | 19 | 42  | 21   | -5  | 5  | 19 | 50  | 19   |     |    |    |     |      |     |   |    |     |      |
| -6  | 6 | 18 | 30  | 43   | 4   | 0  | 19 | 20  | 0    | -4  | 5  | 19 | -1  | 8    |     |    |    |     |      |     |   |    |     |      |
| -5  | 6 | 18 | 13  | 2    | 5   | 0  | 19 | 46  | 15   | -3  | 5  | 19 | -11 | 5    |     |    |    |     |      |     |   |    |     |      |
| -4  | 6 | 18 | 0   | 9    | -11 | 1  | 19 | -14 | 0    | -2  | 5  | 19 | -2  | 1    |     |    |    |     |      |     |   |    |     |      |
| -3  | 6 | 18 | 1   | 15   | -10 | 1  | 19 | -2  | 10   | -1  | 5  | 19 | 17  | 11   |     |    |    |     |      |     |   |    |     |      |
| -2  | 6 | 18 | -10 | 1    | -9  | 1  | 19 | 4   | 4    | 0   | 5  | 19 | 14  | 2    |     |    |    |     |      |     |   |    |     |      |
| -1  | 6 | 18 | 51  | 13   | -8  | 1  | 19 | -9  | 2    | -8  | 6  | 19 | 34  | 2    |     |    |    |     |      |     |   |    |     |      |
| 0   | 6 | 18 | 21  | 13   | -7  | 1  | 19 | 17  | 0    | -5  | 6  | 19 | 85  | 42   |     |    |    |     |      |     |   |    |     |      |
| -9  | 7 | 18 | -12 | 7    | -6  | 1  | 19 | 11  | 6    | -4  | 6  | 19 | 0   | 8    |     |    |    |     |      |     |   |    |     |      |
| -8  | 7 | 18 | 30  | 0    | -5  | 1  | 19 | 16  | 4    | -3  | 6  | 19 | 39  | 0    |     |    |    |     |      |     |   |    |     |      |
| -7  | 7 | 18 | -16 | 0    | -4  | 1  | 19 | 15  | 3    | -6  | -2 | 20 | -11 | 2    |     |    |    |     |      |     |   |    |     |      |
| -6  | 7 | 18 | -6  | 19   | -3  | 1  | 19 | 9   | 15   | -9  | -1 | 20 | -8  | 7    |     |    |    |     |      |     |   |    |     |      |
| -5  | 7 | 18 | 63  | 67   | -2  | 1  | 19 | -6  | 3    | -8  | -1 | 20 | -8  | 0    |     |    |    |     |      |     |   |    |     |      |
| -4  | 7 | 18 | 15  | 0    | -1  | 1  | 19 | 12  | 0    | -7  | -1 | 20 | -4  | 5    |     |    |    |     |      |     |   |    |     |      |
| -3  | 7 | 18 | 2   | 0    | 0   | 1  | 19 | 33  | 12   | -6  | -1 | 20 | 15  | 12   |     |    |    |     |      |     |   |    |     |      |
| -2  | 7 | 18 | -9  | 0    | 1   | 1  | 19 | 13  | 0    | -10 | 0  | 20 | -15 | 1    |     |    |    |     |      |     |   |    |     |      |
| -1  | 7 | 18 | 55  | 19   | 2   | 1  | 19 | -13 | 2    | -9  | 0  | 20 | -5  | 2    |     |    |    |     |      |     |   |    |     |      |
| -6  | 8 | 18 | 0   | 48   | 3   | 1  | 19 | -1  | 3    | -8  | 0  | 20 | 10  | 22   |     |    |    |     |      |     |   |    |     |      |

a. Reflections flagged with an asterisk were considered unobserved.

Table A.4. Atomic Multiplicities for [Cu(dptmp)<sub>2</sub>]PF<sub>6</sub>·THF.

| Name   | Multiplicity | Name   | Multiplicity | Name   | Multiplicity |
|--------|--------------|--------|--------------|--------|--------------|
| ----   | -----        | ----   | -----        | ----   | -----        |
| Cu     | 1.000        | P(1)   | 1.000        | F(1)   | 1.000        |
| F(2)   | 1.000        | F(3)   | 1.000        | F(4)   | 1.000        |
| F(5)   | 1.000        | F(6)   | 1.000        | O(301) | 1.000        |
| N(11)  | 1.000        | N(21)  | 1.000        | N(112) | 1.000        |
| N(212) | 1.000        | C(12)  | 1.000        | C(13)  | 1.000        |
| C(14)  | 1.000        | C(15)  | 1.000        | C(16)  | 1.000        |
| C(17)  | 1.000        | C(18)  | 1.000        | C(19)  | 1.000        |
| C(22)  | 1.000        | C(23)  | 1.000        | C(24)  | 1.000        |
| C(25)  | 1.000        | C(26)  | 1.000        | C(27)  | 1.000        |
| C(28)  | 1.000        | C(29)  | 1.000        | C(110) | 1.000        |
| C(111) | 1.000        | C(113) | 1.000        | C(114) | 1.000        |
| C(115) | 1.000        | C(116) | 1.000        | C(117) | 1.000        |
| C(118) | 1.000        | C(121) | 1.000        | C(122) | 1.000        |
| C(123) | 1.000        | C(124) | 1.000        | C(125) | 1.000        |
| C(126) | 1.000        | C(131) | 1.000        | C(132) | 1.000        |
| C(133) | 1.000        | C(134) | 1.000        | C(135) | 1.000        |
| C(136) | 1.000        | C(210) | 1.000        | C(211) | 1.000        |
| C(213) | 1.000        | C(214) | 1.000        | C(215) | 1.000        |
| C(216) | 1.000        | C(217) | 1.000        | C(218) | 1.000        |
| C(221) | 1.000        | C(222) | 1.000        | C(223) | 1.000        |
| C(224) | 1.000        | C(225) | 1.000        | C(226) | 1.000        |
| C(231) | 1.000        | C(232) | 1.000        | C(233) | 1.000        |
| C(234) | 1.000        | C(235) | 1.000        | C(236) | 1.000        |
| C(302) | 1.000        | C(303) | 1.000        | C(304) | 1.000        |
| C(305) | 1.000        | H(16)  | 1.000        | H(17)  | 1.000        |
| H(26)  | 1.000        | H(27)  | 1.000        | H(11A) | 1.000        |
| H(11B) | 1.000        | H(11C) | 1.000        | H(11D) | 1.000        |
| H(11E) | 1.000        | H(11F) | 1.000        | H(11G) | 1.000        |
| H(11H) | 1.000        | H(11I) | 1.000        | H(11J) | 1.000        |
| H(11K) | 1.000        | H(11L) | 1.000        | H(122) | 1.000        |
| H(123) | 1.000        | H(124) | 1.000        | H(125) | 1.000        |
| H(126) | 1.000        | H(132) | 1.000        | H(133) | 1.000        |
| H(134) | 1.000        | H(135) | 1.000        | H(136) | 1.000        |
| H(21A) | 1.000        | H(21B) | 1.000        | H(21C) | 1.000        |
| H(21D) | 1.000        | H(21E) | 1.000        | H(21F) | 1.000        |
| H(21G) | 1.000        | H(21H) | 1.000        | H(21I) | 1.000        |
| H(21J) | 1.000        | H(21K) | 1.000        | H(21L) | 1.000        |
| H(222) | 1.000        | H(223) | 1.000        | H(224) | 1.000        |
| H(225) | 1.000        | H(226) | 1.000        | H(232) | 1.000        |
| H(233) | 1.000        | H(234) | 1.000        | H(235) | 1.000        |
| H(236) | 1.000        | H(30A) | 1.000        | H(30B) | 1.000        |
| H(30C) | 1.000        | H(30D) | 1.000        | H(30E) | 1.000        |
| H(30F) | 1.000        | H(30G) | 1.000        | H(30H) | 1.000        |





**Appendix B: Crystal Data for [Cu(tmp)<sub>2</sub>]BPh<sub>4</sub>**

**Table B.1. Anisotropic temperature factor coefficients - U's<sup>a</sup> for [Cu(tmp)<sub>2</sub>]BPh<sub>4</sub>.**

| Name   | U(1,1)      | U(2,2)     | U(3,3)     | U(1,2)      | U(1,3)      | U(2,3)      |
|--------|-------------|------------|------------|-------------|-------------|-------------|
| Cu     | 0.02901(19) | 0.0909(3)  | 0.0675(3)  | 0.01038(16) | 0.00946(16) | 0.0006(2)   |
| N(11)  | 0.0327(12)  | 0.0647(14) | 0.0473(14) | 0.0005(9)   | 0.0090(10)  | 0.0047(11)  |
| N(21)  | 0.0378(12)  | 0.0650(14) | 0.0529(15) | 0.0091(10)  | 0.0086(11)  | 0.0044(12)  |
| N(112) | 0.0377(12)  | 0.0616(13) | 0.0518(14) | 0.0054(10)  | 0.0081(10)  | -0.0022(11) |
| N(212) | 0.0381(12)  | 0.0650(14) | 0.0492(14) | 0.0019(10)  | 0.0066(10)  | -0.0013(11) |
| C(12)  | 0.0502(17)  | 0.0686(18) | 0.0476(17) | -0.0100(13) | 0.0074(13)  | -0.0007(14) |
| C(13)  | 0.070(2)    | 0.0618(17) | 0.0490(18) | -0.0033(15) | 0.0199(16)  | 0.0032(14)  |
| C(14)  | 0.0612(19)  | 0.0535(16) | 0.0579(19) | 0.0089(13)  | 0.0276(15)  | 0.0089(14)  |
| C(15)  | 0.0399(15)  | 0.0534(15) | 0.0586(18) | 0.0079(11)  | 0.0190(13)  | 0.0093(13)  |
| C(16)  | 0.0380(16)  | 0.080(2)   | 0.088(3)   | 0.0153(14)  | 0.0222(16)  | 0.0069(19)  |
| C(17)  | 0.0271(14)  | 0.083(2)   | 0.093(3)   | 0.0052(14)  | 0.0093(15)  | 0.014(2)    |
| C(18)  | 0.0342(14)  | 0.0596(16) | 0.0593(18) | 0.0000(11)  | 0.0019(12)  | 0.0116(14)  |
| C(19)  | 0.0478(17)  | 0.0600(17) | 0.064(2)   | -0.0070(13) | -0.0060(15) | 0.0115(15)  |
| C(22)  | 0.0573(19)  | 0.076(2)   | 0.0578(19) | 0.0091(15)  | 0.0116(15)  | 0.0090(16)  |
| C(23)  | 0.088(3)    | 0.0579(18) | 0.060(2)   | -0.0052(16) | 0.0306(19)  | -0.0046(15) |
| C(24)  | 0.064(2)    | 0.0625(18) | 0.081(2)   | -0.0143(15) | 0.0338(18)  | -0.0193(17) |
| C(25)  | 0.0420(16)  | 0.0576(16) | 0.078(2)   | -0.0068(12) | 0.0208(15)  | -0.0144(16) |
| C(26)  | 0.0279(15)  | 0.086(2)   | 0.119(3)   | -0.0035(14) | 0.0147(17)  | -0.017(2)   |
| C(27)  | 0.0361(16)  | 0.077(2)   | 0.108(3)   | 0.0112(14)  | -0.0007(18) | -0.008(2)   |
| C(28)  | 0.0382(15)  | 0.0555(16) | 0.073(2)   | 0.0094(12)  | -0.0055(14) | -0.0166(15) |
| C(29)  | 0.069(2)    | 0.0510(17) | 0.063(2)   | 0.0140(14)  | -0.0163(16) | -0.0106(15) |
| C(31)  | 0.0415(14)  | 0.0465(14) | 0.0498(16) | 0.0057(11)  | 0.0009(12)  | 0.0002(12)  |
| C(32)  | 0.0504(16)  | 0.0555(16) | 0.0490(16) | 0.0103(12)  | 0.0041(13)  | 0.0009(13)  |
| C(33)  | 0.0587(19)  | 0.070(2)   | 0.064(2)   | 0.0249(15)  | 0.0033(16)  | -0.0058(16) |
| C(34)  | 0.069(2)    | 0.0470(16) | 0.090(3)   | 0.0162(15)  | -0.0046(19) | -0.0011(16) |
| C(35)  | 0.062(2)    | 0.0493(16) | 0.098(3)   | 0.0016(14)  | 0.0073(19)  | 0.0108(17)  |
| C(36)  | 0.0505(17)  | 0.0531(16) | 0.085(2)   | 0.0049(13)  | 0.0180(16)  | 0.0067(15)  |
| C(41)  | 0.0343(13)  | 0.0532(15) | 0.0461(16) | 0.0069(11)  | 0.0042(11)  | 0.0044(12)  |
| C(42)  | 0.0438(15)  | 0.0602(16) | 0.0520(17) | 0.0083(12)  | 0.0088(13)  | 0.0111(13)  |
| C(43)  | 0.0477(17)  | 0.092(2)   | 0.0428(18) | 0.0129(15)  | 0.0057(13)  | 0.0158(16)  |
| C(44)  | 0.0420(16)  | 0.090(2)   | 0.0495(19) | 0.0049(14)  | 0.0045(13)  | -0.0137(16) |
| C(45)  | 0.0514(17)  | 0.0643(17) | 0.0539(19) | 0.0033(13)  | 0.0046(14)  | -0.0121(15) |
| C(46)  | 0.0591(18)  | 0.0557(16) | 0.0433(16) | 0.0018(13)  | 0.0048(13)  | 0.0016(13)  |
| C(51)  | 0.0499(15)  | 0.0416(13) | 0.0424(15) | 0.0068(11)  | 0.0058(12)  | 0.0058(11)  |
| C(52)  | 0.0545(17)  | 0.0502(15) | 0.0582(19) | 0.0098(13)  | -0.0009(14) | -0.0077(13) |
| C(53)  | 0.0507(18)  | 0.0682(19) | 0.080(2)   | 0.0182(15)  | -0.0010(16) | -0.0105(17) |
| C(54)  | 0.0505(18)  | 0.0695(19) | 0.071(2)   | 0.0091(14)  | -0.0051(16) | -0.0021(17) |
| C(55)  | 0.065(2)    | 0.076(2)   | 0.061(2)   | 0.0039(16)  | -0.0084(16) | -0.0120(16) |
| C(56)  | 0.0549(18)  | 0.0663(18) | 0.0540(18) | 0.0116(14)  | 0.0025(14)  | -0.0137(14) |
| C(61)  | 0.0618(18)  | 0.0427(14) | 0.0472(17) | 0.0054(12)  | 0.0138(14)  | -0.0009(12) |
| C(62)  | 0.090(3)    | 0.0607(18) | 0.055(2)   | 0.0082(16)  | 0.0154(18)  | 0.0117(15)  |
| C(63)  | 0.158(5)    | 0.074(2)   | 0.074(3)   | 0.007(3)    | 0.043(3)    | 0.023(2)    |
| C(64)  | 0.148(5)    | 0.073(2)   | 0.096(3)   | -0.026(3)   | 0.065(3)    | 0.002(2)    |
| C(65)  | 0.096(3)    | 0.077(2)   | 0.098(3)   | -0.030(2)   | 0.047(3)    | -0.020(2)   |
| C(66)  | 0.064(2)    | 0.0681(19) | 0.066(2)   | -0.0071(15) | 0.0177(17)  | -0.0033(16) |
| C(110) | 0.070(2)    | 0.0616(17) | 0.0553(19) | -0.0051(15) | -0.0007(16) | 0.0021(15)  |
| C(111) | 0.0535(18)  | 0.0713(19) | 0.0574(19) | 0.0074(14)  | 0.0072(15)  | -0.0068(16) |
| C(113) | 0.0303(12)  | 0.0526(14) | 0.0510(16) | 0.0042(10)  | 0.0071(11)  | 0.0088(12)  |
| C(114) | 0.0316(13)  | 0.0533(15) | 0.0497(16) | 0.0030(10)  | 0.0118(11)  | 0.0092(12)  |
| C(115) | 0.110(3)    | 0.092(3)   | 0.069(2)   | -0.009(2)   | 0.021(2)    | -0.020(2)   |
| C(116) | 0.092(3)    | 0.073(2)   | 0.082(3)   | 0.0240(18)  | 0.042(2)    | 0.0073(18)  |
| C(117) | 0.062(2)    | 0.093(3)   | 0.092(3)   | -0.0192(18) | -0.013(2)   | 0.006(2)    |
| C(118) | 0.105(3)    | 0.088(3)   | 0.076(3)   | -0.011(2)   | -0.009(2)   | -0.019(2)   |
| C(210) | 0.081(2)    | 0.0588(18) | 0.0521(19) | 0.0028(16)  | -0.0041(16) | -0.0036(14) |
| C(211) | 0.0590(19)  | 0.0693(18) | 0.0505(18) | -0.0042(15) | 0.0081(15)  | 0.0004(15)  |
| C(213) | 0.0305(13)  | 0.0501(14) | 0.0533(17) | 0.0014(10)  | 0.0023(11)  | -0.0089(12) |
| C(214) | 0.0321(13)  | 0.0521(15) | 0.0573(17) | 0.0011(11)  | 0.0091(12)  | -0.0105(13) |
| C(215) | 0.136(4)    | 0.093(3)   | 0.077(3)   | -0.003(3)   | 0.045(3)    | 0.011(2)    |
| C(216) | 0.088(3)    | 0.102(3)   | 0.122(4)   | -0.037(2)   | 0.057(3)    | -0.014(3)   |
| C(217) | 0.095(3)    | 0.084(3)   | 0.106(3)   | 0.037(2)    | -0.036(2)   | -0.007(2)   |

Table B.1, continued

| Name   | U(1,1)     | U(2,2)     | U(3,3)     | U(1,2)     | U(1,3)     | U(2,3)     |
|--------|------------|------------|------------|------------|------------|------------|
| -----  | -----      | -----      | -----      | -----      | -----      | -----      |
| C(218) | 0.142(4)   | 0.079(2)   | 0.069(3)   | 0.009(2)   | 0.007(3)   | 0.017(2)   |
| B      | 0.0465(17) | 0.0462(16) | 0.0428(17) | 0.0062(13) | 0.0051(13) | 0.0031(13) |

a The form of the anisotropic temperature factor is:  
 $\exp[-2\pi \{h^2 a'^2 U(1,1) + k^2 b'^2 U(2,2) + l^2 c'^2 U(3,3) + 2hka'b'U(1,2) + 2hla'c'U(1,3) + 2klb'c'U(2,3)\}]$  where  $a'$ ,  $b'$ , and  $c'$  are reciprocal lattice constants.

Table B.2. Torsion angles in degrees for [Cu(tmp)<sub>2</sub>]BPh<sub>4</sub>

| Atom 1 | Atom 2 | Atom 3 | Atom 4 | Angle           |
|--------|--------|--------|--------|-----------------|
| =====  | =====  | =====  | =====  | =====           |
| N(21)  | Cu     | N(11)  | C(12)  | -56.41 ( 0.27)  |
| N(21)  | Cu     | N(11)  | C(114) | 125.00 ( 0.18)  |
| N(112) | Cu     | N(11)  | C(12)  | 178.85 ( 0.25)  |
| N(112) | Cu     | N(11)  | C(114) | 0.26 ( 0.18)    |
| N(212) | Cu     | N(11)  | C(12)  | 44.79 ( 0.26)   |
| N(212) | Cu     | N(11)  | C(114) | -133.80 ( 0.18) |
| N(11)  | Cu     | N(21)  | C(22)  | -59.84 ( 0.28)  |
| N(11)  | Cu     | N(21)  | C(214) | 116.44 ( 0.19)  |
| N(112) | Cu     | N(21)  | C(22)  | 44.79 ( 0.27)   |
| N(112) | Cu     | N(21)  | C(214) | -138.94 ( 0.18) |
| N(212) | Cu     | N(21)  | C(22)  | -179.56 ( 0.26) |
| N(212) | Cu     | N(21)  | C(214) | -3.29 ( 0.19)   |
| N(11)  | Cu     | N(112) | C(111) | -179.71 ( 0.26) |
| N(11)  | Cu     | N(112) | C(113) | -1.32 ( 0.18)   |
| N(21)  | Cu     | N(112) | C(111) | 52.20 ( 0.27)   |
| N(21)  | Cu     | N(112) | C(113) | -129.41 ( 0.18) |
| N(212) | Cu     | N(112) | C(111) | -58.22 ( 0.29)  |
| N(212) | Cu     | N(112) | C(113) | 120.17 ( 0.19)  |
| N(11)  | Cu     | N(212) | C(211) | 51.78 ( 0.27)   |
| N(11)  | Cu     | N(212) | C(213) | -124.34 ( 0.18) |
| N(21)  | Cu     | N(212) | C(211) | 178.87 ( 0.26)  |
| N(21)  | Cu     | N(212) | C(213) | 2.74 ( 0.19)    |
| N(112) | Cu     | N(212) | C(211) | -53.85 ( 0.29)  |
| N(112) | Cu     | N(212) | C(213) | 130.02 ( 0.19)  |
| Cu     | N(11)  | C(12)  | C(13)  | 178.93 ( 0.21)  |
| C(114) | N(11)  | C(12)  | C(13)  | -2.53 ( 0.41)   |
| Cu     | N(11)  | C(114) | C(15)  | 178.68 ( 0.22)  |
| Cu     | N(11)  | C(114) | C(113) | 0.82 ( 0.30)    |
| C(12)  | N(11)  | C(114) | C(15)  | -0.12 ( 0.40)   |
| C(12)  | N(11)  | C(114) | C(113) | -177.99 ( 0.25) |
| Cu     | N(21)  | C(22)  | C(23)  | 175.73 ( 0.23)  |
| C(214) | N(21)  | C(22)  | C(23)  | -0.42 ( 0.43)   |
| Cu     | N(21)  | C(214) | C(25)  | -175.07 ( 0.23) |
| Cu     | N(21)  | C(214) | C(213) | 3.33 ( 0.32)    |
| C(22)  | N(21)  | C(214) | C(25)  | 1.75 ( 0.41)    |
| C(22)  | N(21)  | C(214) | C(213) | -179.84 ( 0.28) |
| Cu     | N(112) | C(111) | C(110) | 177.14 ( 0.23)  |
| C(113) | N(112) | C(111) | C(110) | -1.21 ( 0.43)   |
| Cu     | N(112) | C(113) | C(18)  | -176.09 ( 0.23) |
| Cu     | N(112) | C(113) | C(114) | 2.16 ( 0.31)    |
| C(111) | N(112) | C(113) | C(18)  | 2.56 ( 0.40)    |
| C(111) | N(112) | C(113) | C(114) | -179.19 ( 0.25) |
| Cu     | N(212) | C(211) | C(210) | -179.73 ( 0.22) |
| C(213) | N(212) | C(211) | C(210) | -3.74 ( 0.43)   |
| Cu     | N(212) | C(213) | C(28)  | 177.07 ( 0.23)  |
| Cu     | N(212) | C(213) | C(214) | -1.81 ( 0.31)   |
| C(211) | N(212) | C(213) | C(28)  | 0.33 ( 0.40)    |
| C(211) | N(212) | C(213) | C(214) | -178.55 ( 0.26) |
| N(11)  | C(12)  | C(13)  | C(14)  | 2.25 ( 0.45)    |
| N(11)  | C(12)  | C(13)  | C(115) | -179.04 ( 0.29) |
| C(12)  | C(13)  | C(14)  | C(15)  | 0.72 ( 0.43)    |
| C(12)  | C(13)  | C(14)  | C(116) | -179.84 ( 0.29) |
| C(115) | C(13)  | C(14)  | C(15)  | -177.91 ( 0.30) |
| C(115) | C(13)  | C(14)  | C(116) | 1.53 ( 0.48)    |
| C(13)  | C(14)  | C(15)  | C(16)  | 175.59 ( 0.29)  |
| C(13)  | C(14)  | C(15)  | C(114) | -3.09 ( 0.43)   |
| C(116) | C(14)  | C(15)  | C(16)  | -3.84 ( 0.47)   |
| C(116) | C(14)  | C(15)  | C(114) | 177.48 ( 0.28)  |
| C(14)  | C(15)  | C(16)  | C(17)  | -179.14 ( 0.33) |
| C(114) | C(15)  | C(16)  | C(17)  | -0.44 ( 0.47)   |
| C(14)  | C(15)  | C(114) | N(11)  | 2.89 ( 0.43)    |
| C(14)  | C(15)  | C(114) | C(113) | -179.32 ( 0.27) |
| C(16)  | C(15)  | C(114) | N(11)  | -175.89 ( 0.27) |
| C(16)  | C(15)  | C(114) | C(113) | 1.90 ( 0.42)    |

Table B.2, continued

| Atom 1 | Atom 2 | Atom 3 | Atom 4 | Angle           |
|--------|--------|--------|--------|-----------------|
| C(15)  | C(16)  | C(17)  | C(18)  | -1.33 ( 0.55)   |
| C(16)  | C(17)  | C(18)  | C(19)  | -179.24 ( 0.33) |
| C(16)  | C(17)  | C(18)  | C(113) | 1.57 ( 0.50)    |
| C(17)  | C(18)  | C(19)  | C(110) | 179.10 ( 0.31)  |
| C(17)  | C(18)  | C(19)  | C(117) | -1.53 ( 0.50)   |
| C(113) | C(18)  | C(19)  | C(110) | -1.73 ( 0.45)   |
| C(113) | C(18)  | C(19)  | C(117) | 177.65 ( 0.30)  |
| C(17)  | C(18)  | C(113) | N(112) | 178.09 ( 0.29)  |
| C(17)  | C(18)  | C(113) | C(114) | -0.08 ( 0.42)   |
| C(19)  | C(18)  | C(113) | N(112) | -1.14 ( 0.45)   |
| C(19)  | C(18)  | C(113) | C(114) | -179.31 ( 0.28) |
| C(18)  | C(19)  | C(110) | C(111) | 2.97 ( 0.45)    |
| C(18)  | C(19)  | C(110) | C(118) | -178.17 ( 0.30) |
| C(117) | C(19)  | C(110) | C(111) | -176.41 ( 0.30) |
| C(117) | C(19)  | C(110) | C(118) | 2.45 ( 0.50)    |
| N(21)  | C(22)  | C(23)  | C(24)  | -1.42 ( 0.48)   |
| N(21)  | C(22)  | C(23)  | C(215) | 179.46 ( 0.30)  |
| C(22)  | C(23)  | C(24)  | C(25)  | 1.89 ( 0.46)    |
| C(22)  | C(23)  | C(24)  | C(216) | -178.60 ( 0.31) |
| C(215) | C(23)  | C(24)  | C(25)  | -179.04 ( 0.31) |
| C(215) | C(23)  | C(24)  | C(216) | 0.47 ( 0.51)    |
| C(23)  | C(24)  | C(25)  | C(26)  | -179.46 ( 0.34) |
| C(23)  | C(24)  | C(25)  | C(214) | -0.68 ( 0.46)   |
| C(216) | C(24)  | C(25)  | C(26)  | 1.03 ( 0.53)    |
| C(216) | C(24)  | C(25)  | C(214) | 179.82 ( 0.32)  |
| C(24)  | C(25)  | C(26)  | C(27)  | -179.27 ( 0.36) |
| C(214) | C(25)  | C(26)  | C(27)  | 1.92 ( 0.55)    |
| C(24)  | C(25)  | C(214) | N(21)  | -1.23 ( 0.46)   |
| C(24)  | C(25)  | C(214) | C(213) | -179.59 ( 0.29) |
| C(26)  | C(25)  | C(214) | N(21)  | 177.65 ( 0.30)  |
| C(26)  | C(25)  | C(214) | C(213) | -0.70 ( 0.45)   |
| C(25)  | C(26)  | C(27)  | C(28)  | -0.96 ( 0.62)   |
| C(26)  | C(27)  | C(28)  | C(29)  | 179.54 ( 0.37)  |
| C(26)  | C(27)  | C(28)  | C(213) | -1.24 ( 0.55)   |
| C(27)  | C(28)  | C(29)  | C(210) | 176.37 ( 0.33)  |
| C(27)  | C(28)  | C(29)  | C(217) | -2.68 ( 0.51)   |
| C(213) | C(28)  | C(29)  | C(210) | -2.84 ( 0.46)   |
| C(213) | C(28)  | C(29)  | C(217) | 178.11 ( 0.30)  |
| C(27)  | C(28)  | C(213) | N(212) | -176.39 ( 0.29) |
| C(27)  | C(28)  | C(213) | C(214) | 2.43 ( 0.46)    |
| C(29)  | C(28)  | C(213) | N(212) | 2.87 ( 0.45)    |
| C(29)  | C(28)  | C(213) | C(214) | -178.31 ( 0.28) |
| C(28)  | C(29)  | C(210) | C(211) | -0.19 ( 0.46)   |
| C(28)  | C(29)  | C(210) | C(218) | -178.55 ( 0.30) |
| C(217) | C(29)  | C(210) | C(211) | 178.84 ( 0.30)  |
| C(217) | C(29)  | C(210) | C(218) | 0.49 ( 0.50)    |
| C(36)  | C(31)  | C(32)  | C(33)  | -0.24 ( 0.43)   |
| B      | C(31)  | C(32)  | C(33)  | 175.17 ( 0.28)  |
| C(32)  | C(31)  | C(36)  | C(35)  | -0.06 ( 0.44)   |
| B      | C(31)  | C(36)  | C(35)  | -175.64 ( 0.30) |
| C(32)  | C(31)  | B      | C(41)  | 115.35 ( 0.30)  |
| C(32)  | C(31)  | B      | C(51)  | -124.63 ( 0.28) |
| C(32)  | C(31)  | B      | C(61)  | -2.95 ( 0.38)   |
| C(36)  | C(31)  | B      | C(41)  | -69.53 ( 0.34)  |
| C(36)  | C(31)  | B      | C(51)  | 50.50 ( 0.35)   |
| C(36)  | C(31)  | B      | C(61)  | 172.18 ( 0.27)  |
| C(31)  | C(32)  | C(33)  | C(34)  | 0.33 ( 0.49)    |
| C(32)  | C(33)  | C(34)  | C(35)  | -0.09 ( 0.56)   |
| C(33)  | C(34)  | C(35)  | C(36)  | -0.20 ( 0.54)   |
| C(34)  | C(35)  | C(36)  | C(31)  | 0.28 ( 0.54)    |
| C(46)  | C(41)  | C(42)  | C(43)  | -0.31 ( 0.39)   |
| B      | C(41)  | C(42)  | C(43)  | 176.99 ( 0.26)  |
| C(42)  | C(41)  | C(46)  | C(45)  | 0.37 ( 0.42)    |
| B      | C(41)  | C(46)  | C(45)  | -177.09 ( 0.27) |

Table B.2, continued

| Atom 1 | Atom 2 | Atom 3 | Atom 4 | Angle           |
|--------|--------|--------|--------|-----------------|
| -----  | -----  | -----  | -----  | -----           |
| C(42)  | C(41)  | B      | C(31)  | 21.25 ( 0.37)   |
| C(42)  | C(41)  | B      | C(51)  | -98.03 ( 0.29)  |
| C(42)  | C(41)  | B      | C(61)  | 142.27 ( 0.26)  |
| C(46)  | C(41)  | B      | C(31)  | -161.58 ( 0.24) |
| C(46)  | C(41)  | B      | C(51)  | 79.14 ( 0.29)   |
| C(46)  | C(41)  | B      | C(61)  | -40.56 ( 0.32)  |
| C(41)  | C(42)  | C(43)  | C(44)  | -0.26 ( 0.42)   |
| C(42)  | C(43)  | C(44)  | C(45)  | 0.77 ( 0.43)    |
| C(43)  | C(44)  | C(45)  | C(46)  | -0.71 ( 0.44)   |
| C(44)  | C(45)  | C(46)  | C(41)  | 0.13 ( 0.46)    |
| C(56)  | C(51)  | C(52)  | C(53)  | 0.41 ( 0.41)    |
| B      | C(51)  | C(52)  | C(53)  | -179.32 ( 0.27) |
| C(52)  | C(51)  | C(56)  | C(55)  | 0.04 ( 0.45)    |
| B      | C(51)  | C(56)  | C(55)  | 179.79 ( 0.28)  |
| C(52)  | C(51)  | B      | C(31)  | -143.45 ( 0.26) |
| C(52)  | C(51)  | B      | C(41)  | -21.30 ( 0.34)  |
| C(52)  | C(51)  | B      | C(61)  | 95.16 ( 0.31)   |
| C(56)  | C(51)  | B      | C(31)  | 36.84 ( 0.33)   |
| C(56)  | C(51)  | B      | C(41)  | 158.98 ( 0.24)  |
| C(56)  | C(51)  | B      | C(61)  | -84.55 ( 0.29)  |
| C(51)  | C(52)  | C(53)  | C(54)  | -0.40 ( 0.49)   |
| C(52)  | C(53)  | C(54)  | C(55)  | -0.08 ( 0.49)   |
| C(53)  | C(54)  | C(55)  | C(56)  | 0.52 ( 0.48)    |
| C(54)  | C(55)  | C(56)  | C(51)  | -0.52 ( 0.47)   |
| C(66)  | C(61)  | C(62)  | C(63)  | -0.82 ( 0.46)   |
| B      | C(61)  | C(62)  | C(63)  | -177.70 ( 0.31) |
| C(62)  | C(61)  | C(66)  | C(65)  | 1.47 ( 0.47)    |
| B      | C(61)  | C(66)  | C(65)  | 178.46 ( 0.31)  |
| C(62)  | C(61)  | B      | C(31)  | -115.84 ( 0.31) |
| C(62)  | C(61)  | B      | C(41)  | 122.06 ( 0.30)  |
| C(62)  | C(61)  | B      | C(51)  | 3.79 ( 0.38)    |
| C(66)  | C(61)  | B      | C(31)  | 67.46 ( 0.34)   |
| C(66)  | C(61)  | B      | C(41)  | -54.64 ( 0.34)  |
| C(66)  | C(61)  | B      | C(51)  | -172.91 ( 0.25) |
| C(61)  | C(62)  | C(63)  | C(64)  | -0.04 ( 0.56)   |
| C(62)  | C(63)  | C(64)  | C(65)  | 0.32 ( 0.66)    |
| C(63)  | C(64)  | C(65)  | C(66)  | 0.31 ( 0.65)    |
| C(64)  | C(65)  | C(66)  | C(61)  | -1.27 ( 0.59)   |
| C(19)  | C(110) | C(111) | N(112) | -1.59 ( 0.48)   |
| C(118) | C(110) | C(111) | N(112) | 179.50 ( 0.30)  |
| N(112) | C(113) | C(114) | N(11)  | -2.02 ( 0.38)   |
| N(112) | C(113) | C(114) | C(15)  | -179.94 ( 0.29) |
| C(18)  | C(113) | C(114) | N(11)  | 176.25 ( 0.26)  |
| C(18)  | C(113) | C(114) | C(15)  | -1.66 ( 0.43)   |
| C(29)  | C(210) | C(211) | N(212) | 3.73 ( 0.48)    |
| C(218) | C(210) | C(211) | N(212) | -177.82 ( 0.29) |
| N(212) | C(213) | C(214) | N(21)  | -1.02 ( 0.39)   |
| N(212) | C(213) | C(214) | C(25)  | 177.42 ( 0.26)  |
| C(28)  | C(213) | C(214) | N(21)  | -179.91 ( 0.29) |
| C(28)  | C(213) | C(214) | C(25)  | -1.47 ( 0.45)   |

Table B.3. Structure factors ( $F^2_{\text{obs}}$  &  $F^2_{\text{calc}}$ )<sup>a</sup> for  $[\text{Cu}(\text{tmp})_2]\text{BPh}_4$ .

| M  | K | L | Obs   | Calc  | M   | K | L | Obs   | Calc  | M  | K | L | Obs | Calc | M   | K  | L | Obs   | Calc  | M   | K | L | Obs   | Calc  |
|----|---|---|-------|-------|-----|---|---|-------|-------|----|---|---|-----|------|-----|----|---|-------|-------|-----|---|---|-------|-------|
| 4  | 0 | 0 | 51102 | 54965 | 12  | 3 | 0 | 1082  | 1142  | 11 | 6 | 0 | 905 | 869  | 14  | 9  | 0 | -11   | 8     | -12 | 1 | 1 | 29    | 18    |
| 6  | 0 | 0 | 21571 | 21824 | 13  | 3 | 0 | 2324  | 2369  | 12 | 6 | 0 | 253 | 293  | 15  | 9  | 0 | 12    | 2     | -11 | 1 | 1 | 97    | 100   |
| 8  | 0 | 0 | 8741  | 8758  | 14  | 3 | 0 | 996   | 1042  | 13 | 6 | 0 | 5   | 6    | 16  | 9  | 0 | -3    | 1     | -10 | 1 | 1 | 942   | 834   |
| 10 | 0 | 0 | 8782  | 8962  | 15  | 3 | 0 | 99    | 100   | 14 | 6 | 0 | 104 | 91   | 17  | 9  | 0 | 1     | 3     | -9  | 1 | 1 | 236   | 288   |
| 12 | 0 | 0 | 7350  | 7772  | 16  | 3 | 0 | 674   | 766   | 15 | 6 | 0 | 98  | 98   | 18  | 9  | 0 | 78    | 7     | -8  | 1 | 1 | 585   | 425   |
| 14 | 0 | 0 | 2354  | 2169  | 17  | 3 | 0 | 105   | 102   | 16 | 6 | 0 | 88  | 113  | 0   | 10 | 0 | 4     | 47    | -7  | 1 | 1 | 1607  | 1557  |
| 16 | 0 | 0 | 297   | 339   | 18  | 3 | 0 | 136   | 78    | 17 | 6 | 0 | 71  | 60   | 1   | 10 | 0 | 258   | 275   | -6  | 1 | 1 | 875   | 792   |
| 18 | 0 | 0 | 561   | 566   | 19  | 3 | 0 | -14   | 6     | 18 | 6 | 0 | 131 | 148  | 2   | 10 | 0 | 118   | 150   | -5  | 1 | 1 | 5302  | 5719  |
| 20 | 0 | 0 | 1385  | 1268  | 20  | 3 | 0 | 266   | 254   | 19 | 6 | 0 | 53  | 103  | 3   | 10 | 0 | 16    | 15    | -4  | 1 | 1 | 561   | 557   |
| 22 | 0 | 0 | -2    | 112   | 21  | 3 | 0 | 20    | 9     | 20 | 6 | 0 | 144 | 75   | 4   | 10 | 0 | 70    | 75    | -3  | 1 | 1 | 1078  | 1137  |
| 1  | 1 | 0 | 513   | 1158  | 22  | 3 | 0 | 10    | 86    | 21 | 6 | 0 | 63  | 39   | 5   | 10 | 0 | 31    | 87    | -2  | 1 | 1 | 113   | 154   |
| 2  | 1 | 0 | 143   | 173   | 0   | 4 | 0 | 117   | 117   | 1  | 7 | 0 | 32  | 32   | 6   | 10 | 0 | 38    | 45    | -1  | 1 | 1 | 87    | 147   |
| 3  | 1 | 0 | 2078  | 2176  | 1   | 4 | 0 | 7555  | 7953  | 2  | 7 | 0 | 688 | 676  | 7   | 10 | 0 | 371   | 461   | 1   | 1 | 1 | 6594  | 12989 |
| 4  | 1 | 0 | 734   | 836   | 2   | 4 | 0 | 250   | 243   | 3  | 7 | 0 | 682 | 620  | 8   | 10 | 0 | 5     | 3     | 2   | 1 | 1 | 3579  | 3846  |
| 5  | 1 | 0 | 374   | 418   | 3   | 4 | 0 | 7275  | 7622  | 4  | 7 | 0 | 538 | 535  | 9   | 10 | 0 | 118   | 123   | 3   | 1 | 1 | 20    | 7     |
| 6  | 1 | 0 | 1257  | 1236  | 4   | 4 | 0 | 235   | 185   | 5  | 7 | 0 | 28  | 16   | 10  | 10 | 0 | 135   | 147   | 4   | 1 | 1 | 2583  | 2812  |
| 7  | 1 | 0 | 1675  | 1567  | 5   | 4 | 0 | 14325 | 14683 | 6  | 7 | 0 | 101 | 106  | 11  | 10 | 0 | 49    | 20    | 5   | 1 | 1 | 454   | 404   |
| 8  | 1 | 0 | 775   | 540   | 6   | 4 | 0 | 41    | 42    | 7  | 7 | 0 | 6   | 16   | 12  | 10 | 0 | 14    | 18    | 6   | 1 | 1 | 9990  | 10214 |
| 9  | 1 | 0 | 2091  | 1988  | 7   | 4 | 0 | 8171  | 8404  | 8  | 7 | 0 | 43  | 44   | 13  | 10 | 0 | -14   | 27    | 7   | 1 | 1 | 9216  | 8542  |
| 10 | 1 | 0 | 2012  | 1970  | 8   | 4 | 0 | 130   | 163   | 9  | 7 | 0 | -4  | 1    | 14  | 10 | 0 | -4    | 1     | 8   | 1 | 1 | 4078  | 4000  |
| 11 | 1 | 0 | 35    | 38    | 9   | 4 | 0 | 2036  | 2173  | 10 | 7 | 0 | 7   | 5    | 1   | 11 | 0 | 87    | 5     | 9   | 1 | 1 | -1    | 2     |
| 12 | 1 | 0 | 1844  | 1659  | 10  | 4 | 0 | 115   | 108   | 11 | 7 | 0 | -4  | 1    | 2   | 11 | 0 | 170   | 3     | 10  | 1 | 1 | 3846  | 3765  |
| 13 | 1 | 0 | 127   | 103   | 11  | 4 | 0 | 1353  | 1193  | 12 | 7 | 0 | 32  | 54   | 3   | 11 | 0 | 170   | 163   | 11  | 1 | 1 | 41    | 39    |
| 14 | 1 | 0 | 771   | 701   | 12  | 4 | 0 | 578   | 487   | 13 | 7 | 0 | 166 | 158  | 4   | 11 | 0 | 45    | 48    | 12  | 1 | 1 | 595   | 573   |
| 15 | 1 | 0 | 476   | 453   | 13  | 4 | 0 | 1085  | 1109  | 14 | 7 | 0 | 166 | 63   | 5   | 11 | 0 | 2     | 25    | 13  | 1 | 1 | 229   | 229   |
| 16 | 1 | 0 | 22    | 35    | 14  | 4 | 0 | 22    | 0     | 15 | 7 | 0 | 24  | 54   | 6   | 11 | 0 | 42    | 40    | 14  | 1 | 1 | 5388  | 5034  |
| 17 | 1 | 0 | 19    | 9     | 15  | 4 | 0 | 96    | 60    | 16 | 7 | 0 | 16  | 7    | 7   | 11 | 0 | -27   | 2     | 15  | 1 | 1 | 10    | 8     |
| 18 | 1 | 0 | 132   | 156   | 16  | 4 | 0 | -10   | 7     | 17 | 7 | 0 | 93  | 31   | 8   | 11 | 0 | -32   | 33    | 16  | 1 | 1 | 23    | 24    |
| 19 | 1 | 0 | -9    | 6     | 17  | 4 | 0 | 493   | 511   | 18 | 7 | 0 | 0   | 6    | 9   | 11 | 0 | 141   | 58    | 17  | 1 | 1 | 28    | 0     |
| 20 | 1 | 0 | 93    | 105   | 18  | 4 | 0 | -18   | 2     | 19 | 7 | 0 | 29  | 1    | 2   | 12 | 0 | 53    | 2     | 18  | 1 | 1 | 86    | 54    |
| 21 | 1 | 0 | 8     | 1     | 19  | 4 | 0 | 485   | 524   | 20 | 7 | 0 | -12 | 0    | 3   | 12 | 0 | 56    | 3     | 19  | 1 | 1 | 18    | 49    |
| 22 | 1 | 0 | 28    | 5     | 20  | 4 | 0 | 127   | 36    | 21 | 7 | 0 | -5  | 7    | 4   | 12 | 0 | -40   | 1     | 20  | 1 | 1 | 20    | 77    |
| 0  | 2 | 0 | 4526  | 4921  | 21  | 4 | 0 | 124   | 141   | 0  | 8 | 0 | 921 | 735  | 5   | 12 | 0 | 12    | 26    | 21  | 1 | 1 | 41    | 6     |
| 1  | 2 | 0 | 2280  | 2399  | 22  | 4 | 0 | 1     | 12    | 1  | 8 | 0 | 108 | 62   | 6   | 12 | 0 | 56    | 29    | 22  | 1 | 1 | 99    | 27    |
| 2  | 2 | 0 | 26126 | 32171 | 1   | 5 | 0 | 94    | 83    | 2  | 8 | 0 | 49  | 28   | 7   | 12 | 0 | 83    | 20    | -22 | 2 | 1 | -5    | 21    |
| 3  | 2 | 0 | 2396  | 2397  | 2   | 5 | 0 | 103   | 97    | 3  | 8 | 0 | -6  | 8    | 8   | 12 | 0 | -3    | 13    | -21 | 2 | 1 | 28    | 34    |
| 4  | 2 | 0 | 2821  | 3057  | 3   | 5 | 0 | 898   | 826   | 4  | 8 | 0 | 145 | 176  | -21 | 0  | 1 | 584   | 664   | -20 | 2 | 1 | 226   | 250   |
| 5  | 2 | 0 | 101   | 150   | 4   | 5 | 0 | 635   | 556   | 5  | 8 | 0 | 177 | 178  | -19 | 0  | 1 | 543   | 552   | -19 | 2 | 1 | 107   | 61    |
| 6  | 2 | 0 | 173   | 219   | 5   | 5 | 0 | 1496  | 1590  | 6  | 8 | 0 | 106 | 94   | -17 | 0  | 1 | 1167  | 1082  | -18 | 2 | 1 | 116   | 127   |
| 7  | 2 | 0 | 6195  | 6450  | 6   | 5 | 0 | 145   | 120   | 7  | 8 | 0 | 216 | 188  | -15 | 0  | 1 | 35    | 52    | -17 | 2 | 1 | 485   | 401   |
| 8  | 2 | 0 | 5589  | 5380  | 7   | 5 | 0 | 196   | 167   | 8  | 8 | 0 | 383 | 367  | -13 | 0  | 1 | 5043  | 5029  | -16 | 2 | 1 | 80    | 96    |
| 9  | 2 | 0 | 656   | 695   | 8   | 5 | 0 | 67    | 42    | 9  | 8 | 0 | 11  | 1    | -11 | 0  | 1 | 2528  | 2557  | -15 | 2 | 1 | 118   | 114   |
| 10 | 2 | 0 | 1876  | 1953  | 9   | 5 | 0 | 416   | 407   | 10 | 8 | 0 | 55  | 34   | -9  | 0  | 1 | 327   | 457   | -14 | 2 | 1 | 526   | 479   |
| 11 | 2 | 0 | 412   | 403   | 10  | 5 | 0 | 31    | 26    | 11 | 8 | 0 | 278 | 282  | -7  | 0  | 1 | 3216  | 2667  | -13 | 2 | 1 | 1895  | 1890  |
| 12 | 2 | 0 | 3896  | 4013  | 11  | 5 | 0 | 1094  | 1090  | 12 | 8 | 0 | 176 | 160  | -5  | 0  | 1 | 29437 | 28703 | -12 | 2 | 1 | 2942  | 2962  |
| 13 | 2 | 0 | 3388  | 3536  | 12  | 5 | 0 | 74    | 34    | 13 | 8 | 0 | 291 | 89   | -3  | 0  | 1 | 7184  | 8050  | -11 | 2 | 1 | 1382  | 1352  |
| 14 | 2 | 0 | 324   | 265   | 13  | 5 | 0 | 93    | 86    | 14 | 8 | 0 | 66  | 333  | 3   | 0  | 1 | 29773 | 33969 | -10 | 2 | 1 | 839   | 1102  |
| 15 | 2 | 0 | 130   | 101   | 14  | 5 | 0 | 6     | 3     | 15 | 8 | 0 | 66  | 23   | 5   | 0  | 1 | 1462  | 1360  | -9  | 2 | 1 | 4096  | 4052  |
| 16 | 2 | 0 | 480   | 466   | 15  | 5 | 0 | 968   | 1049  | 16 | 8 | 0 | 154 | 115  | 7   | 0  | 1 | 4120  | 4505  | -8  | 2 | 1 | 13350 | 13198 |
| 17 | 2 | 0 | 1006  | 973   | 16  | 5 | 0 | 32    | 0     | 17 | 8 | 0 | -2  | 0    | 9   | 0  | 1 | 7599  | 7576  | -7  | 2 | 1 | 2998  | 3123  |
| 18 | 2 | 0 | 470   | 419   | 17  | 5 | 0 | 149   | 186   | 18 | 8 | 0 | 124 | 89   | 11  | 0  | 1 | 2242  | 2332  | -6  | 2 | 1 | 3084  | 3251  |
| 19 | 2 | 0 | 429   | 441   | 18  | 5 | 0 | 44    | 39    | 19 | 8 | 0 | 4   | 2    | 13  | 0  | 1 | 9914  | 10102 | -5  | 2 | 1 | 206   | 207   |
| 20 | 2 | 0 | 381   | 380   | 19  | 5 | 0 | 98    | 95    | 20 | 8 | 0 | 47  | 13   | 15  | 0  | 1 | 260   | 324   | -4  | 2 | 1 | 10233 | 10809 |
| 21 | 2 | 0 | 213   | 240   | 20  | 5 | 0 | 88    | 82    | 1  | 9 | 0 | 7   | 16   | 17  | 0  | 1 | 1845  | 1872  | -3  | 2 | 1 | 7562  | 7693  |
| 22 | 2 | 0 | -4    | 22    | 21  | 5 | 0 | -13   | 2     | 2  | 9 | 0 | 4   | 2    | 19  | 0  | 1 | 645   | 636   | -2  | 2 | 1 | 11427 | 12947 |
| 1  | 3 | 0 | 1398  | 1491  | 0   | 6 | 0 | 3374  | 3188  | 3  | 9 | 0 | 162 | 166  | 21  | 0  | 1 | 630   | 600   | -1  | 2 | 1 | 16566 | 17745 |
| 2  | 3 | 0 | 419   | 430   | 1   | 6 | 0 | 1365  | 1370  | 4  | 9 | 0 | 307 | 195  | -21 | 1  | 1 | 58    | 0     | 2   | 1 | 1 | 12550 | 4597  |
| 3  | 3 | 0 | 12    | 17    | 2   | 6 | 0 | 43    | 38    | 5  | 9 | 0 | 89  | 77   | -20 | 1  | 1 | 81    | 120   | 2   | 2 | 1 | 4419  | 4523  |
| 4  | 3 | 0 | 41    | 36    | 3   | 6 | 0 | 128   | 113   | 6  | 9 | 0 | 89  | 77   | -20 | 1  | 1 | 81    | 120   | 2   | 2 | 1 | 4419  | 4523  |
| 5  | 3 | 0 | 1795  | 1822  | 4   | 6 | 0 | 1765  | 1770  | 7  | 9 | 0 | 4   | 0    | -19 | 1  | 1 | 23    | 33    | 3   | 2 | 1 | 684   | 757   |
| 6  | 3 | 0 | 32    | 69    | 5   | 6 | 0 | 899   | 812   | 8  | 9 | 0 | 8   | 10   | -18 | 1  | 1 | 290   | 326   | 4   | 2 | 1 | 6875  | 7280  |
| 7  | 3 | 0 | 4325  | 3883  | 6   | 6 | 0 | 443   | 486   | 9  | 9 | 0 | 372 | 335  | -17 | 1  | 1 | 58    | 23    | 5   | 2 | 1 | 1673  | 1766  |
| 8  | 3 | 0 | 374   | 346   | 7   | 6 | 0 | 36    | 16    | 10 | 9 | 0 | 20  | 1    | -16 | 1  | 1 | 224   | 189   | 6   | 2 | 1 | 4590  | 4947  |
| 9  | 3 | 0 | 115   | 132   | 8   | 6 | 0 | 17    | 18    | 11 | 9 | 0 | 31  | 29   | -15 | 1  | 1 | 777   | 708   | 7   | 2 | 1 | 2713  | 2857  |
| 10 | 3 | 0 | 49    | 15    | 9   | 6 | 0 | 156   | 152   | 12 | 9 | 0 | 41  | 50   | -14 | 1  | 1 | 1583  | 1513  | 8   | 2 | 1 | 669   | 702   |
| 11 | 3 | 0 | 108   | 81    | 10  | 6 | 0 | 48    | 63    | 13 | 9 | 0 | 62  | 47   | -13 | 1  | 1 | 1815  | 1815  | 9   | 2 | 1 | 3625  | 3522  |
| 12 | 3 | 0 | 1813  | 1976  | -14 | 4 | 1 | 866   | 829   | 9  | 5 | 1 | 806 | 724  | -11 | 7  | 1 | 188   | 156   | 13  | 8 | 1 | 314   | 277   |
| 13 | 3 | 0 | 2442  | 2383  | -13 | 4 | 1 | 80    | 76    | 10 | 5 | 1 | 35  | 40   | -10 | 7  | 1 | 8     | 5     | 14  | 8 | 1 | 45    | 20    |
| 14 | 3 | 0 | 817   | 767   | -12 | 4 | 1 | 1784  | 1758  | 11 | 5 | 1 | 927 | 887  | -9  | 7  |   |       |       |     |   |   |       |       |

Table B.3, continued

| H   | K  | L | Obs  | Calc | H   | K | L | Obs  | Calc | H   | K | L | Obs  | Calc | H   | K | L | Obs   | Calc  | H   | K  | L    | Obs  | Calc |
|-----|----|---|------|------|-----|---|---|------|------|-----|---|---|------|------|-----|---|---|-------|-------|-----|----|------|------|------|
| 2   | 3  | 1 | 4    | 4    | -20 | 5 | 1 | -4   | 7    | 3   | 6 | 1 | 1076 | 1162 | -16 | 0 | 1 | 4     | 14    | 11  | 9  | 1    | 249  | 279  |
| 3   | 3  | 1 | 994  | 1122 | -19 | 5 | 1 | 8    | 9    | 4   | 6 | 1 | 96   | 88   | -15 | 0 | 1 | 50    | 76    | 12  | 9  | 1    | 102  | 70   |
| 4   | 3  | 1 | 339  | 326  | -18 | 5 | 1 | 32   | 1    | 5   | 6 | 1 | 2298 | 2274 | -14 | 0 | 1 | 32    | 33    | 13  | 9  | 1    | 119  | 111  |
| 5   | 3  | 1 | 689  | 629  | -17 | 5 | 1 | 103  | 115  | 6   | 6 | 1 | 356  | 328  | -13 | 0 | 1 | 272   | 235   | 14  | 9  | 1    | 46   | 16   |
| 6   | 3  | 1 | 33   | 28   | -16 | 5 | 1 | -10  | 1    | 7   | 6 | 1 | 663  | 692  | -12 | 0 | 1 | 9     | 15    | 15  | 9  | 1    | 66   | 78   |
| 7   | 3  | 1 | 3666 | 3796 | -15 | 5 | 1 | 224  | 254  | 8   | 6 | 1 | 425  | 459  | -11 | 0 | 1 | 21    | 28    | 16  | 9  | 1    | -15  | 1    |
| 8   | 3  | 1 | 5892 | 5910 | -14 | 5 | 1 | 26   | 5    | 9   | 6 | 1 | 1488 | 1444 | -10 | 0 | 1 | 4     | 0     | 17  | 9  | 1    | 28   | 18   |
| 9   | 3  | 1 | 1094 | 1177 | -13 | 5 | 1 | 17   | 22   | 10  | 6 | 1 | 6    | 42   | -9  | 0 | 1 | 396   | 343   | 18  | 9  | 1    | 52   | 16   |
| 10  | 3  | 1 | 45   | 31   | -12 | 5 | 1 | 669  | 667  | 11  | 6 | 1 | 448  | 434  | -8  | 0 | 1 | 194   | 177   | -14 | 10 | 1    | 95   | 108  |
| 11  | 3  | 1 | 221  | 265  | -11 | 5 | 1 | 108  | 121  | 12  | 6 | 1 | 153  | 133  | -7  | 0 | 1 | 621   | 630   | -13 | 10 | 1    | 15   | 0    |
| 12  | 3  | 1 | 125  | 125  | -10 | 5 | 1 | 375  | 392  | 13  | 6 | 1 | 529  | 549  | -6  | 0 | 1 | 13    | 23    | -12 | 10 | 1    | 77   | 103  |
| 13  | 3  | 1 | 60   | 70   | -9  | 5 | 1 | 28   | 40   | 14  | 6 | 1 | 40   | 36   | -5  | 0 | 1 | 888   | 938   | -11 | 10 | 1    | 18   | 7    |
| 14  | 3  | 1 | 131  | 138  | -8  | 5 | 1 | 265  | 212  | 15  | 6 | 1 | 125  | 117  | -4  | 0 | 1 | 81    | 85    | -10 | 10 | 1    | 40   | 59   |
| 15  | 3  | 1 | 32   | 32   | -7  | 5 | 1 | 901  | 758  | 16  | 6 | 1 | 114  | 107  | -3  | 0 | 1 | 298   | 350   | -9  | 10 | 1    | 19   | 18   |
| 16  | 3  | 1 | 79   | 45   | -6  | 5 | 1 | 222  | 203  | 17  | 6 | 1 | 240  | 271  | -2  | 0 | 1 | 53    | 43    | -8  | 10 | 1    | 0    | 0    |
| 17  | 3  | 1 | 431  | 551  | -5  | 5 | 1 | 1662 | 1517 | 18  | 6 | 1 | 76   | 61   | -1  | 0 | 1 | 1424  | 1345  | -7  | 10 | 1    | 24   | 2    |
| 18  | 3  | 1 | 65   | 53   | -4  | 5 | 1 | 94   | 11   | 19  | 6 | 1 | 51   | 23   | 0   | 0 | 1 | 404   | 314   | -6  | 10 | 1    | 198  | 164  |
| 19  | 3  | 1 | 65   | 85   | -3  | 5 | 1 | 94   | 61   | 20  | 6 | 1 | 27   | 27   | 1   | 0 | 1 | 363   | 342   | -5  | 10 | 1    | -6   | 4    |
| 20  | 3  | 1 | -13  | 14   | -2  | 5 | 1 | 958  | 854  | 21  | 6 | 1 | -10  | 23   | 2   | 0 | 1 | 48    | 46    | -4  | 10 | 1    | 71   | 1    |
| 21  | 3  | 1 | 53   | 83   | -1  | 5 | 1 | 95   | 66   | -21 | 7 | 1 | -3   | 4    | 3   | 0 | 1 | 283   | 260   | -3  | 10 | 1    | 13   | 7    |
| 22  | 3  | 1 | 33   | 12   | 0   | 5 | 1 | 360  | 304  | -20 | 7 | 1 | 6    | 4    | 4   | 0 | 1 | 195   | 75    | -2  | 10 | 1    | 82   | 74   |
| -22 | 4  | 1 | 95   | 114  | 1   | 5 | 1 | 183  | 180  | -19 | 7 | 1 | 13   | 11   | 5   | 0 | 1 | 411   | 402   | -1  | 10 | 1    | 73   | 26   |
| -21 | 4  | 1 | 27   | 14   | 2   | 5 | 1 | 291  | 206  | -18 | 7 | 1 | 25   | 35   | 6   | 0 | 1 | 8     | 1     | 0   | 10 | 1    | 13   | 2    |
| -20 | 4  | 1 | 471  | 528  | 3   | 5 | 1 | 210  | 166  | -17 | 7 | 1 | 13   | 0    | 7   | 0 | 1 | 28    | 40    | 1   | 10 | 1    | -23  | 0    |
| -19 | 4  | 1 | 104  | 41   | 4   | 5 | 1 | 141  | 151  | -16 | 7 | 1 | 27   | 1    | 8   | 0 | 1 | 98    | 98    | 2   | 10 | 1    | 146  | 140  |
| -18 | 4  | 1 | 405  | 416  | 5   | 5 | 1 | 57   | 46   | -15 | 7 | 1 | 117  | 141  | 9   | 0 | 1 | 110   | 118   | 3   | 10 | 1    | 32   | 29   |
| -17 | 4  | 1 | 35   | 39   | 6   | 5 | 1 | 455  | 388  | -14 | 7 | 1 | -2   | 7    | 10  | 0 | 1 | 55    | 64    | 4   | 10 | 1    | -37  | 9    |
| -16 | 4  | 1 | 576  | 529  | 7   | 5 | 1 | 158  | 174  | -13 | 7 | 1 | 126  | 150  | 11  | 0 | 1 | 17    | 10    | 5   | 10 | 1    | 135  | 121  |
| -15 | 4  | 1 | 50   | 10   | 8   | 5 | 1 | 190  | 131  | -12 | 7 | 1 | -6   | 3    | 12  | 0 | 1 | 270   | 317   | 6   | 10 | 1    | 353  | 293  |
| 7   | 10 | 1 | 158  | 36   | -18 | 1 | 2 | -4   | 0    | 3   | 2 | 2 | 1852 | 2045 | -20 | 4 | 2 | 54    | 5     | 3   | 5  | 2    | 1220 | 978  |
| 8   | 10 | 1 | 29   | 6    | -17 | 1 | 2 | 107  | 100  | 4   | 2 | 2 | 25   | 8    | -19 | 4 | 2 | 626   | 693   | 4   | 5  | 2    | 172  | 184  |
| 9   | 10 | 1 | 5    | 8    | -16 | 1 | 2 | 187  | 205  | 5   | 2 | 2 | 1425 | 1504 | -18 | 4 | 2 | 23    | 0     | 5   | 2  | 3001 | 2987 |      |
| 10  | 10 | 1 | 35   | 17   | -15 | 1 | 2 | 120  | 117  | 6   | 2 | 2 | 3172 | 3677 | -17 | 4 | 2 | 1292  | 1269  | 6   | 5  | 2    | 325  | 282  |
| 11  | 10 | 1 | 89   | 70   | -14 | 1 | 2 | 381  | 429  | 7   | 2 | 2 | 5440 | 5308 | -16 | 4 | 2 | 34    | 35    | 7   | 5  | 2    | 5    | 1    |
| 12  | 10 | 1 | 116  | 107  | -13 | 1 | 2 | 1281 | 1265 | 8   | 2 | 2 | 5216 | 5039 | -15 | 4 | 2 | 861   | 747   | 8   | 5  | 2    | 1490 | 1503 |
| 13  | 10 | 1 | -1   | 3    | -12 | 1 | 2 | 228  | 235  | 9   | 2 | 2 | 464  | 384  | -14 | 4 | 2 | -2    | 2     | 9   | 5  | 2    | 1091 | 948  |
| 14  | 10 | 1 | 0    | 3    | -11 | 1 | 2 | 155  | 132  | 10  | 2 | 2 | 2306 | 2316 | -13 | 4 | 2 | 1745  | 1691  | 10  | 5  | 2    | 98   | 77   |
| -9  | 11 | 1 | -12  | 1    | -10 | 1 | 2 | 278  | 264  | 11  | 2 | 2 | 1256 | 1313 | -12 | 4 | 2 | 27    | 10    | 11  | 5  | 2    | 67   | 62   |
| -8  | 11 | 1 | 31   | 2    | -9  | 1 | 2 | 26   | 2    | 12  | 2 | 2 | 1692 | 1603 | -11 | 4 | 2 | 2571  | 2674  | 12  | 5  | 2    | 12   | 1    |
| -7  | 11 | 1 | -3   | 0    | -8  | 1 | 2 | 2779 | 3027 | 13  | 2 | 2 | 1136 | 1076 | -10 | 4 | 2 | 187   | 140   | 13  | 5  | 2    | 67   | 62   |
| -6  | 11 | 1 | 76   | 70   | -7  | 1 | 2 | 803  | 777  | 14  | 2 | 2 | 98   | 90   | -9  | 4 | 2 | 2258  | 2229  | 14  | 5  | 2    | 13   | 3    |
| -5  | 11 | 1 | 113  | 94   | -6  | 1 | 2 | 288  | 215  | 15  | 2 | 2 | 54   | 109  | -8  | 4 | 2 | 266   | 240   | 15  | 5  | 2    | 4    | 19   |
| -4  | 11 | 1 | 48   | 38   | -5  | 1 | 2 | 1299 | 1287 | 16  | 2 | 2 | 437  | 373  | -7  | 4 | 2 | 3498  | 3734  | 16  | 5  | 2    | 163  | 138  |
| -3  | 11 | 1 | 127  | 144  | -4  | 1 | 2 | 3384 | 3505 | 17  | 2 | 2 | 251  | 208  | -6  | 4 | 2 | 1013  | 986   | 17  | 5  | 2    | 42   | 20   |
| -2  | 11 | 1 | -7   | 20   | -3  | 1 | 2 | 5176 | 5675 | 18  | 2 | 2 | 180  | 177  | -5  | 4 | 2 | 19538 | 20030 | 18  | 5  | 2    | 133  | 137  |
| -1  | 11 | 1 | 153  | 176  | -2  | 1 | 2 | 6994 | 7383 | 19  | 2 | 2 | 62   | 12   | -4  | 4 | 2 | 2588  | 2443  | 19  | 5  | 2    | 62   | 89   |
| 0   | 11 | 1 | 32   | 38   | -1  | 1 | 2 | 1543 | 2245 | 20  | 2 | 2 | 249  | 245  | -3  | 4 | 2 | 2124  | 2341  | 20  | 5  | 2    | 80   | 132  |
| 1   | 11 | 1 | 100  | 64   | 0   | 1 | 2 | 3496 | 7272 | 21  | 2 | 2 | 56   | 43   | -2  | 4 | 2 | 1269  | 1115  | 21  | 5  | 2    | 39   | 26   |
| 2   | 11 | 1 | 65   | 100  | 1   | 1 | 2 | 141  | 127  | 22  | 2 | 2 | -44  | 1    | -1  | 4 | 2 | 6477  | 6745  | -21 | 6  | 2    | 16   | 13   |
| 3   | 11 | 1 | 18   | 21   | 2   | 1 | 2 | -3   | 5129 | -22 | 3 | 2 | 53   | 11   | 0   | 4 | 2 | 680   | 632   | -20 | 6  | 2    | -33  | 2    |
| 4   | 11 | 1 | 99   | 87   | 3   | 1 | 2 | 305  | 324  | -21 | 3 | 2 | 42   | 2    | 1   | 4 | 2 | 2322  | 2700  | -19 | 6  | 2    | 57   | 16   |
| 5   | 11 | 1 | 36   | 68   | 4   | 1 | 2 | 4664 | 5087 | -20 | 3 | 2 | 13   | 10   | 2   | 4 | 2 | 7     | 2     | -18 | 6  | 2    | 407  | 430  |
| 6   | 11 | 1 | 46   | 5    | 5   | 1 | 2 | 122  | 128  | -19 | 3 | 2 | 50   | 4    | 3   | 4 | 2 | 652   | 804   | -17 | 6  | 2    | 89   | 98   |
| 7   | 11 | 1 | 12   | 110  | 6   | 1 | 2 | 1443 | 1236 | -18 | 3 | 2 | 18   | 7    | 4   | 4 | 2 | 253   | 238   | -16 | 6  | 2    | 139  | 133  |
| 8   | 11 | 1 | -36  | 5    | 7   | 1 | 2 | 2584 | 2516 | -17 | 3 | 2 | 27   | 0    | 5   | 4 | 2 | 3058  | 3275  | -15 | 6  | 2    | 85   | 80   |
| 9   | 11 | 1 | 78   | 2    | 8   | 1 | 2 | 2307 | 1901 | -16 | 3 | 2 | 43   | 18   | 6   | 4 | 2 | 1224  | 1035  | -14 | 6  | 2    | 149  | 162  |
| -8  | 12 | 1 | 239  | 8    | 9   | 1 | 2 | 1729 | 1582 | -15 | 3 | 2 | 345  | 323  | 7   | 4 | 2 | 3206  | 3283  | -13 | 6  | 2    | 142  | 146  |
| -7  | 12 | 1 | 117  | 36   | 10  | 1 | 2 | 1721 | 1598 | -14 | 3 | 2 | 173  | 130  | 8   | 4 | 2 | 343   | 317   | -12 | 6  | 2    | 575  | 583  |
| -6  | 12 | 1 | 73   | 89   | 11  | 1 | 2 | 79   | 48   | -13 | 3 | 2 | 62   | 37   | 9   | 4 | 2 | 577   | 534   | -11 | 6  | 2    | 11   | 17   |
| -5  | 12 | 1 | 122  | 144  | 12  | 1 | 2 | 187  | 141  | -12 | 3 | 2 | 302  | 346  | 10  | 4 | 2 | 258   | 230   | -10 | 6  | 2    | 480  | 497  |
| -4  | 12 | 1 | 663  | 35   | 13  | 1 | 2 | 1429 | 1342 | -11 | 3 | 2 | 839  | 792  | 11  | 4 | 2 | 1768  | 1674  | -9  | 6  | 2    | 81   | 87   |
| -3  | 12 | 1 | 15   | 43   | 14  | 1 | 2 | 420  | 354  | -10 | 3 | 2 | 62   | 40   | 12  | 4 | 2 | 174   | 133   | -8  | 6  | 2    | 468  | 487  |
| -2  | 12 | 1 | 151  | 29   | 15  | 1 | 2 | 145  | 71   | -9  | 3 | 2 | 163  | 164  | 13  | 4 | 2 | 3151  | 3055  | -7  | 6  | 2    | 766  | 763  |
| -1  | 12 | 1 | -36  | 42   | 16  | 1 | 2 | 348  | 380  | -8  | 3 | 2 | 286  | 267  | 14  | 4 | 2 | 360   | 371   | -6  | 6  | 2    | 609  | 686  |
| 2   | 12 | 1 | 46   | 41   | 17  | 1 | 2 | 91   | 93   | -7  | 3 | 2 | 3582 | 3400 | 15  | 4 | 2 | 24    | 3     | -5  | 6  | 2    | 550  | 622  |
| 3   | 12 | 1 | 85   | 16   | 18  | 1 | 2 | 8    | 1    | -6  | 3 | 2 | 505  | 540  | 16  | 4 | 2 | 54    | 43    | -4  | 6  | 2    | 542  | 630  |
| 4   | 12 | 1 | 77   | 32   | 19  | 1 | 2 | 140  | 136  | -5  | 3 | 2 | 274  | 273  | 17  | 4 | 2 | 253   | 259   | -3  | 6  | 2    | 564  | 622  |
| 5   | 12 | 1 | 7    | 22   | 20  | 1 | 2 | 83   | 91   | -4  | 3 | 2 | 0    | 1    | 16  | 4 | 2 | 6     | 0     | -2  | 6  | 2    | 222  | 171  |
| 6   | 12 | 1 | 162  | 8    | 21  | 1 | 2 | 40   | 22   | -3  | 3 | 2 | 289  | 264  | 19  | 4 | 2 | 240   | 266   | -1  | 6  | 2    | 142  | 91   |
| 7   | 12 | 1 | -12  | 0    | 22  | 1 | 2 | -14  | 13   | -2  | 3 | 2 | 2149 | 2199 | 20  | 4 | 2 | 32    | 0     | 0   |    |      |      |      |

Table B.3, continued

| M   | K | L  | Obe  | Calc | M   | K  | L | Obe | Calc | M   | K  | L  | Obe   | Calc  | M   | K  | L | Obe  | Calc  | M   | K  | L   | Obe  | Calc  | M     | K | L | Obe | Calc | M | K | L | Obe | Calc |
|-----|---|----|------|------|-----|----|---|-----|------|-----|----|----|-------|-------|-----|----|---|------|-------|-----|----|-----|------|-------|-------|---|---|-----|------|---|---|---|-----|------|
| -9  | 7 | 2  | 22   | 34   | 15  | 8  | 2 | 22  | 30   | 8   | 10 | 2  | 59    | 59    | -15 | 1  | 3 | 945  | 949   | 7   | 2  | 3   | 1204 | 1086  |       |   |   |     |      |   |   |   |     |      |
| -9  | 7 | 2  | 60   | 60   | 16  | 8  | 2 | 207 | 154  | 9   | 10 | 2  | 15    | 10    | -14 | 1  | 3 | 261  | 250   | 0   | 2  | 3   | 6    | 11    |       |   |   |     |      |   |   |   |     |      |
| -7  | 2 | -9 | 1    | 1    | 17  | 0  | 2 | -5  | 0    | 10  | 10 | 2  | 36    | 50    | -13 | 1  | 3 | 1938 | 1822  | 9   | 2  | 3   | 1518 | 1455  |       |   |   |     |      |   |   |   |     |      |
| -6  | 7 | 2  | -5   | 5    | 18  | 0  | 2 | 172 | 88   | 11  | 10 | 2  | 3     | 17    | -12 | 1  | 3 | 589  | 636   | 10  | 2  | 3   | 1647 | 1723  |       |   |   |     |      |   |   |   |     |      |
| -5  | 7 | 2  | 19   | 11   | 19  | 0  | 2 | 9   | 21   | 12  | 10 | 2  | 3     | 9     | -11 | 1  | 3 | 23   | 16    | 11  | 2  | 3   | 749  | 726   |       |   |   |     |      |   |   |   |     |      |
| -4  | 7 | 2  | 190  | 162  | 20  | 0  | 2 | -26 | 13   | 13  | 10 | 2  | 36    | 29    | -10 | 1  | 3 | 132  | 194   | 12  | 2  | 3   | 1261 | 1202  |       |   |   |     |      |   |   |   |     |      |
| -3  | 7 | 2  | 186  | 195  | -18 | 9  | 2 | 99  | 0    | 14  | 10 | 2  | 24    | 7     | -9  | 1  | 3 | 2564 | 2250  | 13  | 2  | 3   | 354  | 389   |       |   |   |     |      |   |   |   |     |      |
| -2  | 7 | 2  | 1489 | 1315 | -17 | 9  | 2 | 34  | 0    | -9  | 11 | 2  | 4     | 26    | -8  | 1  | 3 | 393  | 331   | 14  | 2  | 3   | 508  | 453   |       |   |   |     |      |   |   |   |     |      |
| -1  | 7 | 2  | -2   | 8    | -16 | 9  | 2 | 18  | 6    | -8  | 11 | 2  | 31    | 54    | -7  | 1  | 3 | 170  | 160   | 15  | 2  | 3   | -18  | 6     |       |   |   |     |      |   |   |   |     |      |
| 0   | 7 | 2  | -12  | 0    | -15 | 9  | 2 | 23  | 4    | -7  | 11 | 2  | 45    | 0     | -6  | 1  | 3 | 4042 | 4256  | 16  | 2  | 3   | 125  | 154   |       |   |   |     |      |   |   |   |     |      |
| 1   | 7 | 2  | 20   | 2    | -14 | 9  | 2 | 26  | 0    | -6  | 11 | 2  | 34    | 60    | -5  | 1  | 3 | 77   | 101   | 17  | 2  | 3   | 467  | 485   |       |   |   |     |      |   |   |   |     |      |
| 2   | 7 | 2  | 353  | 370  | -13 | 9  | 2 | 2   | 0    | -5  | 11 | 2  | 103   | 103   | -4  | 1  | 3 | 6982 | 7769  | 18  | 2  | 3   | 263  | 268   |       |   |   |     |      |   |   |   |     |      |
| 3   | 7 | 2  | 577  | 566  | -12 | 9  | 2 | 14  | 27   | -4  | 11 | 2  | 287   | 76    | -3  | 1  | 3 | 2409 | 2505  | 19  | 2  | 3   | 350  | 363   |       |   |   |     |      |   |   |   |     |      |
| 4   | 7 | 2  | 416  | 445  | -11 | 9  | 2 | 80  | 95   | -3  | 11 | 2  | 58    | 64    | -2  | 1  | 3 | -3   | 20854 | 20  | 2  | 3   | 141  | 132   |       |   |   |     |      |   |   |   |     |      |
| 5   | 7 | 2  | 343  | 312  | -10 | 9  | 2 | 3   | 5    | -2  | 11 | 2  | 3     | 4     | -1  | 1  | 3 | 4331 | 5109  | 21  | 2  | 3   | 24   | 2     |       |   |   |     |      |   |   |   |     |      |
| 6   | 7 | 2  | 57   | 48   | -9  | 9  | 2 | 100 | 79   | -1  | 11 | 2  | 27    | 47    | 0   | 1  | 3 | 1730 | 1876  | 22  | 2  | 3   | 501  | 12    |       |   |   |     |      |   |   |   |     |      |
| 7   | 7 | 2  | 554  | 509  | -8  | 9  | 2 | 17  | 12   | 0   | 11 | 2  | -21   | 0     | 1   | 1  | 3 | -2   | 22475 | -22 | 3  | 3   | 18   | 83    |       |   |   |     |      |   |   |   |     |      |
| 8   | 7 | 2  | 0    | 1    | -7  | 9  | 2 | 152 | 167  | 1   | 11 | 2  | 34    | 13    | 2   | 1  | 3 | 4968 | 5667  | -21 | 3  | 3   | 76   | 46    |       |   |   |     |      |   |   |   |     |      |
| 9   | 7 | 2  | 61   | 75   | -6  | 9  | 2 | 40  | 30   | 2   | 11 | 2  | 13    | 0     | 3   | 1  | 3 | 225  | 261   | -20 | 3  | 3   | 100  | 68    |       |   |   |     |      |   |   |   |     |      |
| 10  | 7 | 2  | 60   | 63   | -5  | 9  | 2 | 74  | 4    | 3   | 11 | 2  | 69    | 50    | 4   | 1  | 3 | 4103 | 4429  | -19 | 3  | 3   | 28   | 44    |       |   |   |     |      |   |   |   |     |      |
| 11  | 7 | 2  | 1132 | 995  | -4  | 9  | 2 | 60  | 111  | 4   | 11 | 2  | 32    | 9     | 5   | 1  | 3 | 846  | 894   | -18 | 3  | 3   | 26   | 92    |       |   |   |     |      |   |   |   |     |      |
| 12  | 7 | 2  | 18   | 9    | -3  | 9  | 2 | 23  | 3    | 5   | 11 | 2  | 92    | 75    | 6   | 1  | 3 | 4312 | 4668  | -17 | 3  | 3   | 86   | 92    |       |   |   |     |      |   |   |   |     |      |
| 13  | 7 | 2  | 19   | 4    | -2  | 9  | 2 | -3  | 26   | 6   | 11 | 2  | -59   | 23    | 7   | 1  | 3 | 190  | 165   | -16 | 3  | 3   | 59   | 61    |       |   |   |     |      |   |   |   |     |      |
| 14  | 7 | 2  | 171  | 216  | 1   | 9  | 2 | 218 | 165  | 7   | 11 | 2  | 6     | 1     | 8   | 1  | 3 | 115  | 154   | -15 | 3  | 3   | 51   | 60    |       |   |   |     |      |   |   |   |     |      |
| 15  | 7 | 2  | 63   | 14   | 0   | 9  | 2 | 4   | 0    | 6   | 11 | 2  | 28    | 63    | 9   | 1  | 3 | 74   | 46    | -14 | 3  | 3   | 107  | 63    |       |   |   |     |      |   |   |   |     |      |
| 16  | 7 | 2  | 13   | 10   | 1   | 9  | 2 | 26  | 18   | 9   | 11 | 2  | 40    | 48    | 10  | 1  | 3 | 1311 | 1489  | -13 | 3  | 3   | 445  | 472   |       |   |   |     |      |   |   |   |     |      |
| 17  | 7 | 2  | 29   | 40   | 2   | 9  | 2 | 0   | 2    | -8  | 12 | 2  | -95   | 6     | 11  | 1  | 3 | 834  | 725   | -12 | 3  | 3   | 484  | 478   |       |   |   |     |      |   |   |   |     |      |
| 18  | 7 | 2  | 80   | 6    | 3   | 9  | 2 | 43  | 53   | -7  | 12 | 2  | -7    | 35    | 12  | 1  | 3 | 571  | 615   | -11 | 3  | 3   | 2908 | 2593  |       |   |   |     |      |   |   |   |     |      |
| 19  | 7 | 2  | 17   | 4    | 4   | 9  | 2 | 7   | 23   | -6  | 12 | 2  | 80    | 118   | 13  | 1  | 3 | 74   | 24    | -10 | 3  | 3   | 2474 | 2415  |       |   |   |     |      |   |   |   |     |      |
| 20  | 7 | 2  | 16   | 3    | 5   | 9  | 2 | 99  | 48   | -5  | 12 | 2  | 233   | 31    | 14  | 1  | 3 | 3803 | 3795  | -9  | 3  | 3   | 3442 | 4940  |       |   |   |     |      |   |   |   |     |      |
| 21  | 7 | 2  | 94   | 17   | 6   | 9  | 2 | 69  | 65   | -4  | 12 | 2  | 403   | 3     | 15  | 1  | 3 | 838  | 833   | -8  | 3  | 3   | 5791 | 5776  |       |   |   |     |      |   |   |   |     |      |
| -20 | 0 | 2  | 10   | 16   | 7   | 9  | 2 | 179 | 158  | -3  | 12 | 2  | 5     | 4     | 16  | 1  | 3 | 128  | 152   | -7  | 3  | 3   | 1213 | 1234  |       |   |   |     |      |   |   |   |     |      |
| -19 | 0 | 2  | 41   | 4    | 8   | 9  | 2 | 62  | 61   | -2  | 12 | 2  | 55    | 39    | 17  | 1  | 3 | 186  | 196   | -6  | 3  | 3   | 520  | 439   |       |   |   |     |      |   |   |   |     |      |
| -18 | 0 | 2  | 12   | 29   | 9   | 9  | 2 | -9  | 3    | 2   | 12 | 2  | 55    | 36    | 18  | 1  | 3 | 287  | 358   | -5  | 3  | 3   | 78   | 104   |       |   |   |     |      |   |   |   |     |      |
| -17 | 0 | 2  | 38   | 13   | 10  | 9  | 2 | -3  | 39   | 4   | 3  | 12 | 2     | 212   | 35  | 19 | 1 | 3    | 93    | 71  | -4 | 3   | 3    | 10743 | 11507 |   |   |     |      |   |   |   |     |      |
| -16 | 0 | 2  | 122  | 111  | 11  | 9  | 2 | 121 | 94   | 4   | 12 | 2  | -53   | 7     | 20  | 1  | 3 | 324  | 311   | -3  | 3  | 3   | 435  | 390   |       |   |   |     |      |   |   |   |     |      |
| -15 | 0 | 2  | 46   | 7    | 12  | 9  | 2 | 142 | 120  | 5   | 12 | 2  | 90    | 67    | 21  | 1  | 3 | 53   | 41    | -2  | 3  | 3   | 1035 | 1239  |       |   |   |     |      |   |   |   |     |      |
| -14 | 0 | 2  | 160  | 223  | 13  | 9  | 2 | 19  | 21   | 6   | 12 | 2  | 279   | 107   | -22 | 2  | 3 | 152  | 148   | -1  | 3  | 3   | 492  | 475   |       |   |   |     |      |   |   |   |     |      |
| -13 | 0 | 2  | 68   | 73   | 14  | 9  | 2 | 27  | 14   | 7   | 12 | 2  | -33   | 7     | -21 | 2  | 3 | 209  | 198   | 0   | 3  | 3   | 1259 | 1306  |       |   |   |     |      |   |   |   |     |      |
| -12 | 0 | 2  | 248  | 270  | 15  | 9  | 2 | 59  | 46   | -21 | 0  | 3  | 490   | 397   | -20 | 2  | 3 | 1120 | 1151  | 1   | 3  | 3   | 322  | 358   |       |   |   |     |      |   |   |   |     |      |
| -11 | 0 | 2  | 8    | 5    | 16  | 9  | 2 | 19  | 8    | -19 | 0  | 3  | 204   | 140   | -19 | 2  | 3 | 406  | 425   | 2   | 3  | 3   | 1713 | 1869  |       |   |   |     |      |   |   |   |     |      |
| -10 | 0 | 2  | 275  | 236  | 17  | 9  | 2 | 27  | 0    | -17 | 0  | 3  | 732   | 625   | -18 | 2  | 3 | 951  | 1087  | 3   | 3  | 3   | 233  | 233   |       |   |   |     |      |   |   |   |     |      |
| -9  | 0 | 2  | 5    | 1    | 18  | 9  | 2 | -21 | 0    | -15 | 0  | 3  | 36    | 11    | -17 | 2  | 3 | 631  | 615   | 4   | 3  | 3   | 6001 | 6001  |       |   |   |     |      |   |   |   |     |      |
| -8  | 0 | 2  | 223  | 242  | -15 | 10 | 2 | 33  | 16   | -13 | 0  | 3  | 2004  | 1968  | -16 | 2  | 3 | 179  | 166   | 5   | 3  | 3   | 42   | 45    |       |   |   |     |      |   |   |   |     |      |
| -7  | 0 | 2  | 11   | 0    | -14 | 10 | 2 | -10 | 13   | -11 | 0  | 3  | 603   | 669   | -15 | 2  | 3 | 45   | 57    | 6   | 3  | 3   | 3237 | 3072  |       |   |   |     |      |   |   |   |     |      |
| -6  | 0 | 2  | 117  | 113  | -13 | 10 | 2 | 262 | 344  | -9  | 0  | 3  | 603   | 669   | -15 | 2  | 3 | 3122 | 3005  | 7   | 3  | 3   | 752  | 736   |       |   |   |     |      |   |   |   |     |      |
| -5  | 0 | 2  | 11   | 6    | -12 | 10 | 2 | 24  | 6    | -7  | 0  | 3  | 438   | 556   | -13 | 2  | 3 | 2616 | 2615  | 8   | 3  | 3   | 1635 | 1793  |       |   |   |     |      |   |   |   |     |      |
| -4  | 0 | 2  | 138  | 105  | -11 | 10 | 2 | 62  | 41   | -5  | 0  | 3  | 1277  | 1052  | -12 | 2  | 3 | 5381 | 5184  | 9   | 3  | 3   | 423  | 428   |       |   |   |     |      |   |   |   |     |      |
| -3  | 0 | 2  | 15   | 1    | -10 | 10 | 2 | 9   | 11   | -3  | 0  | 3  | 1876  | 1864  | -11 | 2  | 3 | 685  | 740   | 10  | 3  | 3   | 832  | 932   |       |   |   |     |      |   |   |   |     |      |
| -2  | 0 | 2  | 278  | 318  | -9  | 10 | 2 | 20  | 19   | 3   | 0  | 3  | 72205 | 80140 | -10 | 2  | 3 | 2283 | 2484  | 11  | 3  | 3   | 148  | 122   |       |   |   |     |      |   |   |   |     |      |
| -1  | 0 | 2  | 9    | 2    | -8  | 10 | 2 | 50  | 0    | 5   | 0  | 3  | 6273  | 6006  | -9  | 2  | 3 | 40   | 15    | 12  | 3  | 518 | 539  |       |       |   |   |     |      |   |   |   |     |      |
| 0   | 0 | 2  | 592  | 508  | -7  | 10 | 2 | 212 | 232  | 7   | 0  | 3  | 17328 | 16987 | -8  | 2  | 3 | 8397 | 7966  | 13  | 3  | 3   | 61   | 61    |       |   |   |     |      |   |   |   |     |      |
| 1   | 0 | 2  | 458  | 438  | -6  | 10 | 2 | 53  | 1    | 9   | 0  | 3  | 1511  | 1766  | -7  | 2  | 3 | 4822 | 4920  | 14  | 3  | 3   | 446  | 477   |       |   |   |     |      |   |   |   |     |      |
| 2   | 0 | 2  | 242  | 265  | -5  | 10 | 2 | 123 | 200  | 11  | 0  | 3  | 3083  | 3039  | -6  | 2  | 3 | 1846 | 2064  | 15  | 3  | 3   | 77   | 14    |       |   |   |     |      |   |   |   |     |      |
| 3   | 0 | 2  | 74   | 65   | -4  | 10 | 2 | 164 | 181  | 13  | 0  | 3  | 1612  | 1605  | -5  | 2  | 3 | 571  | 734   | 16  | 3  | 3   | 619  | 668   |       |   |   |     |      |   |   |   |     |      |
| 4   | 0 | 2  | 1479 | 1606 | -3  | 10 | 2 | 4   | 14   | 15  | 0  | 3  | 146   | 43    | -4  | 2  | 3 | 355  | 343   | 17  | 3  | 3   | 33   | 39    |       |   |   |     |      |   |   |   |     |      |
| 5   | 0 | 2  | 40   | 47   | -2  | 10 | 2 | 245 | 209  | 17  | 0  | 3  | 856   | 867   | -3  | 2  | 3 | 131  | 163   | 18  | 3  | 3   | 604  | 598   |       |   |   |     |      |   |   |   |     |      |
| 6   | 0 | 2  | 873  | 898  | -1  | 10 | 2 | 173 | 168  | 19  | 0  | 3  | 586   | 509   | -2  | 2  | 3 | 344  | 244</ |     |    |     |      |       |       |   |   |     |      |   |   |   |     |      |



Table B.3, continued

| H   | K | L | Obs   | Calc  | H   | K | L | Obs   | Calc  | H   | K | L | Obs  | Calc | H   | K  | L | Obs  | Calc | H   | K  | L | Obs   | Calc  | H | K | L | Obs | Calc |
|-----|---|---|-------|-------|-----|---|---|-------|-------|-----|---|---|------|------|-----|----|---|------|------|-----|----|---|-------|-------|---|---|---|-----|------|
| 21  | 4 | 3 | 22    | 10    | 0   | 6 | 3 | 1182  | 1071  | -18 | 9 | 3 | 24   | 0    | 9   | 9  | 3 | 17   | 1    | 3   | 12 | 3 | 200   | 5     |   |   |   |     |      |
| -22 | 5 | 3 | 17    | 2     | 1   | 6 | 3 | 920   | 965   | -17 | 9 | 3 | 49   | 120  | 10  | 9  | 3 | 13   | 0    | 4   | 12 | 3 | 65    | 19    |   |   |   |     |      |
| -21 | 5 | 3 | 9     | 12    | 2   | 6 | 3 | 1164  | 1229  | -16 | 9 | 3 | 6    | 15   | 11  | 9  | 3 | 24   | 23   | 5   | 12 | 3 | 46    | 0     |   |   |   |     |      |
| -20 | 5 | 3 | 3     | 20    | 3   | 6 | 3 | 30    | 28    | -15 | 9 | 3 | 97   | 116  | 12  | 9  | 3 | 7    | 0    | 6   | 12 | 3 | 80    | 4     |   |   |   |     |      |
| -19 | 5 | 3 | 19    | 26    | 4   | 6 | 3 | 3821  | 3634  | -14 | 9 | 3 | 76   | 69   | 13  | 9  | 3 | 66   | 29   | 7   | 12 | 3 | 41    | 29    |   |   |   |     |      |
| -18 | 5 | 3 | 23    | 2     | 5   | 6 | 3 | 2181  | 2179  | -13 | 9 | 3 | 466  | 409  | 14  | 9  | 3 | 0    | 0    | -22 | 0  | 4 | 53    | 141   |   |   |   |     |      |
| -17 | 5 | 3 | 32    | 32    | 6   | 6 | 3 | 89    | 95    | -12 | 9 | 3 | 59   | 49   | 15  | 9  | 3 | -15  | 1    | -20 | 0  | 4 | 2032  | 2148  |   |   |   |     |      |
| -16 | 5 | 3 | 39    | 79    | 7   | 6 | 3 | 377   | 360   | -11 | 9 | 3 | 207  | 287  | 16  | 9  | 3 | 67   | 9    | -18 | 0  | 4 | 2103  | 2037  |   |   |   |     |      |
| -15 | 5 | 3 | 375   | 383   | 8   | 6 | 3 | 56    | 46    | -10 | 9 | 3 | 45   | 55   | 17  | 9  | 3 | 12   | 13   | -16 | 0  | 4 | 1831  | 1833  |   |   |   |     |      |
| -14 | 5 | 3 | 206   | 214   | 9   | 6 | 3 | 51    | 34    | -9  | 9 | 3 | 36   | 57   | 18  | 9  | 3 | 105  | 6    | -14 | 0  | 4 | 8299  | 7888  |   |   |   |     |      |
| -13 | 5 | 3 | 209   | 182   | 10  | 6 | 3 | 469   | 441   | -8  | 9 | 3 | 105  | 111  | -14 | 10 | 3 | -14  | 6    | -12 | 0  | 4 | 9723  | 9453  |   |   |   |     |      |
| -12 | 5 | 3 | 782   | 729   | 11  | 6 | 3 | 117   | 113   | -7  | 9 | 3 | 609  | 617  | -13 | 10 | 3 | 19   | 0    | -10 | 0  | 4 | 10871 | 10681 |   |   |   |     |      |
| -11 | 5 | 3 | 18    | 6     | 12  | 6 | 3 | 234   | 220   | -6  | 9 | 3 | 165  | 147  | -12 | 10 | 3 | 64   | 75   | -8  | 0  | 4 | 4850  | 5191  |   |   |   |     |      |
| -10 | 5 | 3 | 145   | 162   | 13  | 6 | 3 | 174   | 186   | -5  | 9 | 3 | 6    | 4    | -11 | 10 | 3 | 36   | 8    | -6  | 0  | 4 | 9543  | 10244 |   |   |   |     |      |
| -9  | 5 | 3 | 428   | 398   | 14  | 6 | 3 | 169   | 173   | -4  | 9 | 3 | 504  | 508  | -10 | 10 | 3 | 162  | 209  | -4  | 0  | 4 | 12976 | 14367 |   |   |   |     |      |
| -8  | 5 | 3 | 28    | 6     | 15  | 6 | 3 | 11    | 6     | -3  | 9 | 3 | 22   | 25   | -9  | 10 | 3 | 26   | 17   | -2  | 0  | 4 | 690   | 668   |   |   |   |     |      |
| -7  | 5 | 3 | 25    | 12    | 16  | 6 | 3 | 146   | 154   | -2  | 9 | 3 | 12   | 25   | -8  | 10 | 3 | 35   | 22   | 0   | 0  | 4 | 2544  | 29726 |   |   |   |     |      |
| -6  | 5 | 3 | 422   | 385   | 17  | 6 | 3 | 29    | 23    | -1  | 9 | 3 | 544  | 446  | -7  | 10 | 3 | 72   | 47   | 2   | 0  | 4 | 7139  | 7826  |   |   |   |     |      |
| -5  | 5 | 3 | 2799  | 2682  | 18  | 6 | 3 | 77    | 96    | 0   | 9 | 3 | 56   | 47   | -6  | 10 | 3 | 160  | 103  | 4   | 0  | 4 | 158   | 156   |   |   |   |     |      |
| -4  | 5 | 3 | 613   | 585   | 19  | 6 | 3 | 61    | 34    | 1   | 9 | 3 | 249  | 258  | -5  | 10 | 3 | 131  | 196  | 6   | 0  | 4 | 360   | 415   |   |   |   |     |      |
| -3  | 5 | 3 | 803   | 742   | 20  | 6 | 3 | 22    | 20    | 2   | 9 | 3 | 17   | 2    | -4  | 10 | 3 | 162  | 42   | 8   | 0  | 4 | 24320 | 22032 |   |   |   |     |      |
| 10  | 0 | 4 | 761   | 862   | -6  | 2 | 4 | 1082  | 977   | 15  | 3 | 4 | 70   | 70   | -1  | 5  | 4 | 11   | 4    | 16  | 6  | 4 | 7     | 3     |   |   |   |     |      |
| 12  | 0 | 4 | 2457  | 2474  | -5  | 2 | 4 | 545   | 648   | 16  | 3 | 4 | 1054 | 1095 | -6  | 5  | 4 | 298  | 342  | 17  | 6  | 4 | 16    | 21    |   |   |   |     |      |
| 14  | 0 | 4 | 120   | 84    | -4  | 2 | 4 | 5359  | 6046  | 17  | 3 | 4 | -11  | 35   | -5  | 5  | 4 | 1824 | 1928 | 18  | 6  | 4 | 5     | 8     |   |   |   |     |      |
| 16  | 0 | 4 | 465   | 480   | -3  | 2 | 4 | 14063 | 14560 | 18  | 3 | 4 | 365  | 353  | -4  | 5  | 4 | 506  | 458  | 19  | 6  | 4 | 141   | 146   |   |   |   |     |      |
| 18  | 0 | 4 | 103   | 119   | -2  | 2 | 4 | 34198 | 36752 | 19  | 3 | 4 | 30   | 4    | -3  | 5  | 4 | 230  | 196  | 20  | 6  | 4 | 6     | 9     |   |   |   |     |      |
| 20  | 0 | 4 | 367   | 325   | -1  | 2 | 4 | 3134  | 3427  | 20  | 3 | 4 | 305  | 350  | -2  | 5  | 4 | 315  | 206  | 21  | 6  | 4 | 37    | 19    |   |   |   |     |      |
| -22 | 1 | 4 | 56    | 54    | 0   | 2 | 4 | 28732 | 30714 | 21  | 3 | 4 | -34  | 1    | -1  | 5  | 4 | 75   | 103  | -21 | 7  | 4 | 19    | 1     |   |   |   |     |      |
| -21 | 1 | 4 | 43    | 7     | 1   | 2 | 4 | 46289 | 50039 | -22 | 4 | 4 | -87  | 10   | 0   | 5  | 4 | 25   | 22   | -20 | 7  | 4 | 53    | 27    |   |   |   |     |      |
| -20 | 1 | 4 | 1     | 7     | 2   | 2 | 4 | 4154  | 2541  | -21 | 4 | 4 | 292  | 328  | 1   | 5  | 4 | 60   | 66   | -19 | 7  | 4 | -23   | 0     |   |   |   |     |      |
| -19 | 1 | 4 | 4     | 1     | 3   | 2 | 4 | 1316  | 1379  | -20 | 4 | 4 | -7   | 7    | 2   | 5  | 4 | 402  | 345  | -18 | 7  | 4 | -16   | 1     |   |   |   |     |      |
| -18 | 1 | 4 | 28    | 9     | 4   | 2 | 4 | 978   | 924   | -19 | 4 | 4 | 537  | 510  | 3   | 5  | 4 | 1715 | 1628 | -17 | 7  | 4 | 33    | 12    |   |   |   |     |      |
| -17 | 1 | 4 | 28    | 19    | 5   | 2 | 4 | 3461  | 3529  | -18 | 4 | 4 | -1   | 0    | 4   | 5  | 4 | 3472 | 3433 | -16 | 7  | 4 | 105   | 83    |   |   |   |     |      |
| -16 | 1 | 4 | 723   | 746   | 6   | 2 | 4 | 8580  | 8443  | -17 | 4 | 4 | 1147 | 1099 | 5   | 5  | 4 | 340  | 331  | -15 | 7  | 4 | 37    | 19    |   |   |   |     |      |
| -15 | 1 | 4 | 64    | 49    | 7   | 2 | 4 | 620   | 509   | -16 | 4 | 4 | -1   | 1    | 6   | 5  | 4 | 345  | 360  | -14 | 7  | 4 | 24    | 14    |   |   |   |     |      |
| -14 | 1 | 4 | 129   | 86    | 8   | 2 | 4 | 492   | 603   | -15 | 4 | 4 | 484  | 478  | 7   | 5  | 4 | 11   | 3    | -13 | 7  | 4 | 26    | 6     |   |   |   |     |      |
| -13 | 1 | 4 | 1448  | 1368  | 9   | 2 | 4 | 351   | 328   | -14 | 4 | 4 | 37   | 10   | 8   | 5  | 4 | 3616 | 3478 | -12 | 7  | 4 | 116   | 144   |   |   |   |     |      |
| -12 | 1 | 4 | 15    | 18    | 10  | 2 | 4 | 2250  | 2106  | -13 | 4 | 4 | 2166 | 2118 | 9   | 5  | 4 | 370  | 312  | -11 | 7  | 4 | 55    | 53    |   |   |   |     |      |
| -11 | 1 | 4 | 201   | 203   | 11  | 2 | 4 | 285   | 290   | -12 | 4 | 4 | 126  | 136  | 10  | 5  | 4 | 1043 | 981  | -10 | 7  | 4 | 35    | 36    |   |   |   |     |      |
| -10 | 1 | 4 | 44    | 15    | 12  | 2 | 4 | 1294  | 1078  | -11 | 4 | 4 | 1785 | 1725 | 11  | 5  | 4 | 1636 | 1594 | -9  | 7  | 4 | 418   | 343   |   |   |   |     |      |
| -9  | 1 | 4 | 382   | 359   | 13  | 2 | 4 | 1466  | 1445  | -10 | 4 | 4 | 32   | 39   | 12  | 5  | 4 | 145  | 115  | -8  | 7  | 4 | 126   | 103   |   |   |   |     |      |
| -8  | 1 | 4 | 736   | 713   | 14  | 2 | 4 | 89    | 90    | -9  | 4 | 4 | 3722 | 3773 | 13  | 5  | 4 | 153  | 152  | -7  | 7  | 4 | 513   | 501   |   |   |   |     |      |
| -7  | 1 | 4 | 229   | 222   | 15  | 2 | 4 | 30    | 6     | -8  | 4 | 4 | 495  | 494  | 14  | 5  | 4 | 295  | 274  | -6  | 7  | 4 | 100   | 103   |   |   |   |     |      |
| -6  | 1 | 4 | 3727  | 3952  | 16  | 2 | 4 | 232   | 217   | -7  | 4 | 4 | 3086 | 3068 | 15  | 5  | 4 | 119  | 100  | -5  | 7  | 4 | 361   | 353   |   |   |   |     |      |
| -5  | 1 | 4 | 1051  | 1197  | 17  | 2 | 4 | 243   | 262   | -6  | 4 | 4 | 641  | 590  | 16  | 5  | 4 | 444  | 481  | -4  | 7  | 4 | 113   | 123   |   |   |   |     |      |
| -4  | 1 | 4 | 39    | 30    | 18  | 2 | 4 | 195   | 215   | -5  | 4 | 4 | 1203 | 1162 | 17  | 5  | 4 | 113  | 84   | -3  | 7  | 4 | 445   | 452   |   |   |   |     |      |
| -3  | 1 | 4 | 3809  | 3966  | 19  | 2 | 4 | 103   | 95    | -4  | 4 | 4 | 2994 | 2995 | 18  | 5  | 4 | 217  | 277  | -2  | 7  | 4 | 81    | 72    |   |   |   |     |      |
| -2  | 1 | 4 | 694   | 700   | 20  | 2 | 4 | 290   | 271   | -3  | 4 | 4 | 3451 | 3923 | 19  | 5  | 4 | 147  | 91   | -1  | 7  | 4 | 501   | 479   |   |   |   |     |      |
| -1  | 1 | 4 | 37    | 19    | 21  | 2 | 4 | 124   | 147   | -2  | 4 | 4 | 1181 | 1089 | 20  | 5  | 4 | 42   | 105  | 0   | 7  | 4 | 109   | 124   |   |   |   |     |      |
| 0   | 1 | 4 | 242   | 249   | 22  | 2 | 4 | 35    | 14    | -1  | 4 | 4 | 505  | 305  | 21  | 5  | 4 | 41   | 35   | 1   | 7  | 4 | 433   | 425   |   |   |   |     |      |
| 1   | 1 | 4 | 1578  | 1687  | -22 | 3 | 4 | 46    | 0     | 0   | 4 | 4 | 19   | 8    | -21 | 6  | 4 | 190  | 17   | 2   | 7  | 4 | 2     | 2     |   |   |   |     |      |
| 2   | 1 | 4 | 12354 | 13410 | -21 | 3 | 4 | 42    | 0     | 1   | 4 | 4 | 1699 | 1777 | -20 | 6  | 4 | 31   | 4    | 3   | 7  | 4 | 274   | 279   |   |   |   |     |      |
| 3   | 1 | 4 | 4300  | 4247  | -20 | 3 | 4 | 15    | 3     | 2   | 4 | 4 | 22   | 13   | -19 | 6  | 4 | 75   | 60   | 4   | 7  | 4 | 2     | 0     |   |   |   |     |      |
| 4   | 1 | 4 | 6839  | 7254  | -19 | 3 | 4 | 36    | 43    | 3   | 4 | 4 | 7404 | 7919 | -18 | 6  | 4 | 439  | 408  | 5   | 7  | 4 | 28    | 16    |   |   |   |     |      |
| 5   | 1 | 4 | 7683  | 7622  | -18 | 3 | 4 | 23    | 35    | 4   | 4 | 4 | 83   | 65   | -17 | 6  | 4 | 91   | 95   | 6   | 7  | 4 | 14    | 5     |   |   |   |     |      |
| 6   | 1 | 4 | 1120  | 1077  | -17 | 3 | 4 | 15    | 5     | 5   | 4 | 4 | 292  | 306  | -16 | 6  | 4 | 55   | 37   | 7   | 7  | 4 | 213   | 239   |   |   |   |     |      |
| 7   | 1 | 4 | 6191  | 5887  | -16 | 3 | 4 | 65    | 64    | 6   | 4 | 4 | 48   | 25   | -15 | 6  | 4 | 112  | 84   | 8   | 7  | 4 | 260   | 236   |   |   |   |     |      |
| 8   | 1 | 4 | 28    | 3     | -15 | 3 | 4 | 541   | 534   | 7   | 4 | 4 | 1339 | 1414 | -14 | 6  | 4 | 31   | 22   | 9   | 7  | 4 | 73    | 51    |   |   |   |     |      |
| 9   | 1 | 4 | 84    | 184   | -14 | 3 | 4 | 137   | 141   | 8   | 4 | 4 | 72   | 49   | -13 | 6  | 4 | 187  | 164  | 10  | 7  | 4 | 57    | 58    |   |   |   |     |      |
| 10  | 1 | 4 | 27    | 39    | -13 | 3 | 4 | 1960  | 1842  | 9   | 4 | 4 | 455  | 454  | -12 | 6  | 4 | 159  | 158  | 11  | 7  | 4 | 45    | 41    |   |   |   |     |      |
| 11  | 1 | 4 | 2176  | 2230  | -12 | 3 | 4 | 38    | 28    | 10  | 4 | 4 | 84   | 76   | -11 | 6  | 4 | 664  | 668  | 12  | 7  | 4 | 212   | 202   |   |   |   |     |      |
| 12  | 1 | 4 | 55    | 74    | -11 | 3 | 4 | 13    | 0     | 11  | 4 | 4 | 272  | 310  | -10 | 6  | 4 | 123  | 131  | 13  | 7  | 4 | 420   | 396   |   |   |   |     |      |
| 13  | 1 | 4 | 4839  | 478   |     |   |   |       |       |     |   |   |      |      |     |    |   |      |      |     |    |   |       |       |   |   |   |     |      |

Table B.3, continued

| M   | K  | L | Obs  | Calc | M   | K  | L | Obs   | Calc  | M   | K | L | Obs   | Calc  | M   | K  | L    | Obs  | Calc | M   | K | L   | Obs  | Calc |
|-----|----|---|------|------|-----|----|---|-------|-------|-----|---|---|-------|-------|-----|----|------|------|------|-----|---|-----|------|------|
| 14  | 8  | 4 | 35   | 14   | 8   | 10 | 4 | 4     | 4     | -15 | 1 | 5 | 1120  | 1129  | 9   | 2  | 5    | 844  | 1004 | -13 | 4 | 5   | 451  | 493  |
| 15  | 8  | 4 | 14   | 27   | 9   | 10 | 4 | 30    | 7     | -14 | 1 | 5 | 6406  | 6074  | 10  | 2  | 5    | 1009 | 1069 | -12 | 4 | 5   | 3748 | 3600 |
| 16  | 8  | 4 | 94   | 67   | 10  | 10 | 4 | 35    | 4     | -13 | 1 | 5 | 770   | 762   | 11  | 2  | 5    | 427  | 428  | -11 | 4 | 5   | 96   | 72   |
| 17  | 8  | 4 | -24  | 1    | 11  | 10 | 4 | -11   | 4     | -12 | 1 | 5 | 1132  | 1067  | 12  | 2  | 5    | 1625 | 1636 | -10 | 4 | 5   | 1004 | 992  |
| 18  | 8  | 4 | -16  | 3    | 12  | 10 | 4 | 9     | 2     | -11 | 1 | 5 | 10    | 16    | 13  | 2  | 5    | 527  | 500  | -9  | 4 | 5   | 455  | 330  |
| 19  | 8  | 4 | 51   | 86   | 13  | 10 | 4 | 24    | 0     | -10 | 1 | 5 | 5321  | 5241  | 14  | 2  | 5    | 112  | 97   | -8  | 4 | 5   | 2695 | 2800 |
| -18 | 9  | 4 | 35   | 4    | -9  | 11 | 4 | -36   | 18    | -9  | 1 | 5 | 42    | 43    | 15  | 2  | 5    | 30   | 47   | -7  | 4 | 5   | 1446 | 1434 |
| -17 | 9  | 4 | -22  | 9    | -8  | 11 | 4 | -38   | 32    | -8  | 1 | 5 | 446   | 547   | 16  | 2  | 5    | -18  | 1    | -6  | 4 | 5   | 1795 | 1763 |
| -16 | 9  | 4 | 13   | 5    | -7  | 11 | 4 | -20   | 8     | -7  | 1 | 5 | 4261  | 4166  | 17  | 2  | 5    | 92   | 86   | -5  | 4 | 5   | 217  | 231  |
| -15 | 9  | 4 | 19   | 2    | -6  | 11 | 4 | 140   | 44    | -6  | 1 | 5 | 4271  | 4194  | 18  | 2  | 5    | 78   | 59   | -4  | 4 | 5   | 3603 | 3636 |
| -14 | 9  | 4 | 24   | 0    | -5  | 11 | 4 | 100   | 2     | -5  | 1 | 5 | 5011  | 5471  | 19  | 2  | 5    | 140  | 194  | -3  | 4 | 5   | 1752 | 1603 |
| -13 | 9  | 4 | 236  | 262  | -4  | 11 | 4 | 18    | 1     | -4  | 1 | 5 | 6860  | 7569  | 20  | 2  | 5    | 32   | 27   | -2  | 4 | 5   | 1588 | 1388 |
| -12 | 9  | 4 | 97   | 112  | -3  | 11 | 4 | 9     | 0     | -3  | 1 | 5 | 3007  | 2830  | 21  | 2  | 5    | -9   | 15   | -1  | 4 | 5   | 297  | 6    |
| -11 | 9  | 4 | 18   | 8    | -2  | 11 | 4 | 5     | 22    | -2  | 1 | 5 | 22694 | 24504 | -22 | 3  | 5    | 268  | 61   | 0   | 4 | 5   | 4634 | 4851 |
| -10 | 9  | 4 | 22   | 6    | -1  | 11 | 4 | 49    | 12    | -1  | 1 | 5 | 356   | 385   | -21 | 3  | 5    | 98   | 82   | 1   | 4 | 5   | 7569 | 7610 |
| -9  | 9  | 4 | 143  | 134  | 0   | 11 | 4 | 305   | 309   | 0   | 1 | 5 | 42032 | 45466 | -20 | 3  | 5    | 29   | 8    | 2   | 4 | 5   | 36   | 8    |
| -8  | 9  | 4 | 87   | 117  | 1   | 11 | 4 | 19    | 0     | 1   | 1 | 5 | 31    | 34    | -19 | 3  | 5    | 240  | 237  | 3   | 4 | 5   | 351  | 324  |
| -7  | 9  | 4 | 32   | 41   | 2   | 11 | 4 | 90    | 47    | 2   | 1 | 5 | 10391 | 11126 | -18 | 3  | 5    | 9    | 2    | 4   | 4 | 5   | 773  | 828  |
| -6  | 9  | 4 | 92   | 99   | 3   | 11 | 4 | 15    | 4     | 3   | 1 | 5 | 1531  | 1504  | -17 | 3  | 5    | 704  | 716  | 5   | 4 | 5   | 568  | 527  |
| -5  | 9  | 4 | 62   | 63   | 4   | 11 | 4 | 88    | 8     | 4   | 1 | 5 | 7512  | 7613  | -16 | 3  | 5    | -2   | 4    | 6   | 4 | 5   | 328  | 342  |
| -4  | 9  | 4 | -13  | 19   | 5   | 11 | 4 | 5     | 15    | 5   | 1 | 5 | 4972  | 5071  | -15 | 3  | 5    | 10   | 2    | 7   | 4 | 5   | 564  | 484  |
| -3  | 9  | 4 | 28   | 12   | 6   | 11 | 4 | 96    | 73    | 6   | 1 | 5 | 9006  | 8783  | -14 | 3  | 5    | 239  | 256  | 9   | 4 | 5   | 289  | 256  |
| -2  | 9  | 4 | 24   | 29   | 7   | 11 | 4 | 99    | 0     | 7   | 1 | 5 | 112   | 14    | -13 | 3  | 5    | 4    | 8    | 1   | 4 | 5   | 17   | 36   |
| -1  | 9  | 4 | 47   | 123  | 8   | 11 | 4 | 6     | 13    | 8   | 1 | 5 | 2032  | 2010  | -12 | 3  | 5    | 573  | 553  | 10  | 4 | 5   | 797  | 795  |
| 0   | 9  | 4 | 420  | 405  | 9   | 11 | 4 | 116   | 13    | 9   | 1 | 5 | 501   | 386   | -11 | 3  | 5    | 478  | 500  | 11  | 4 | 5   | 1958 | 1921 |
| 1   | 9  | 4 | 5    | 34   | -7  | 12 | 4 | -69   | 64    | 10  | 1 | 5 | 1773  | 1826  | -10 | 3  | 5    | 164  | 168  | 12  | 4 | 5   | 2267 | 2096 |
| 2   | 9  | 4 | 234  | 204  | -6  | 12 | 4 | 55    | 54    | 11  | 1 | 5 | 28    | 40    | -9  | 3  | 5    | 1504 | 1628 | 13  | 4 | 5   | 28   | 2    |
| 3   | 9  | 4 | 122  | 127  | -5  | 12 | 4 | 136   | 2     | 12  | 1 | 5 | 1145  | 1169  | -8  | 3  | 5    | 254  | 222  | 14  | 4 | 5   | 264  | 261  |
| 4   | 9  | 4 | 147  | 143  | -4  | 12 | 4 | 0     | 19    | 13  | 1 | 5 | 117   | 74    | -7  | 3  | 5    | 5656 | 5787 | 15  | 4 | 5   | 100  | 109  |
| 5   | 9  | 4 | 23   | 25   | -3  | 12 | 4 | -52   | 20    | 14  | 1 | 5 | 1018  | 798   | -6  | 3  | 5    | 363  | 356  | 16  | 4 | 5   | 186  | 179  |
| 6   | 9  | 4 | 241  | 226  | -2  | 12 | 4 | 65    | 66    | 15  | 1 | 5 | 1507  | 1713  | -5  | 3  | 5    | 1780 | 1671 | 17  | 4 | 5   | -2   | 1    |
| 7   | 9  | 4 | 36   | 13   | -1  | 12 | 4 | 88    | 60    | 16  | 1 | 5 | 574   | 528   | -4  | 3  | 5    | 439  | 413  | 18  | 4 | 5   | 179  | 170  |
| 8   | 9  | 4 | 66   | 68   | 3   | 12 | 4 | -3    | 1     | 17  | 1 | 5 | 321   | 379   | -3  | 3  | 5    | 249  | 252  | 20  | 4 | 5   | 149  | 60   |
| 9   | 9  | 4 | 34   | 16   | 4   | 12 | 4 | 133   | 61    | 18  | 1 | 5 | 321   | 379   | -2  | 3  | 5    | 547  | 773  | 21  | 4 | 5   | -1   | 2    |
| 10  | 9  | 4 | 187  | 152  | 5   | 12 | 4 | -10   | 0     | 19  | 1 | 5 | 458   | 478   | 0   | 3  | 5    | 2233 | 2329 | -21 | 5 | 5   | 90   | 3    |
| 11  | 9  | 4 | 44   | 10   | 6   | 12 | 4 | -69   | 0     | 20  | 1 | 5 | 18    | 5     | 1   | 3  | 3038 | 3242 | -20  | 5   | 5 | -10 | 2    |      |
| 12  | 9  | 4 | 42   | 45   | 7   | 12 | 4 | -65   | 1     | 21  | 1 | 5 | 18    | 5     | 1   | 3  | 3038 | 3242 | -19  | 5   | 5 | 273 | 302  |      |
| 13  | 9  | 4 | 6    | 8    | -21 | 0  | 5 | 281   | 173   | -22 | 2 | 5 | 228   | 229   | 2   | 3  | 5    | 130  | 125  | -19 | 5 | 5   | -9   | 15   |
| 14  | 9  | 4 | 62   | 107  | -19 | 0  | 5 | 206   | 161   | -21 | 2 | 5 | 385   | 370   | 3   | 3  | 5    | 4890 | 4894 | -18 | 5 | 5   | 55   | 37   |
| 15  | 9  | 4 | 75   | 1    | -17 | 0  | 5 | 731   | 553   | -20 | 2 | 5 | 863   | 906   | 4   | 3  | 5    | 76   | 86   | -17 | 5 | 5   | 25   | 3    |
| 16  | 9  | 4 | 45   | 16   | -15 | 0  | 5 | 481   | 515   | -19 | 2 | 5 | 237   | 241   | 5   | 3  | 5    | 3759 | 3628 | -16 | 5 | 5   | 441  | 482  |
| 17  | 9  | 4 | 28   | 3    | -13 | 0  | 5 | 6525  | 6415  | -18 | 2 | 5 | 352   | 355   | 6   | 3  | 5    | 519  | 519  | -15 | 5 | 5   | 32   | 6    |
| 18  | 9  | 4 | 64   | 88   | -11 | 0  | 5 | 2362  | 2211  | -17 | 2 | 5 | 376   | 301   | 7   | 3  | 5    | 1095 | 1199 | -14 | 5 | 5   | 14   | 6    |
| -15 | 10 | 4 | 124  | 113  | -9  | 0  | 5 | 6716  | 7080  | -16 | 2 | 5 | 376   | 229   | 8   | 3  | 5    | 30   | 16   | -13 | 5 | 5   | 193  | 166  |
| -14 | 10 | 4 | 80   | 69   | -7  | 0  | 5 | 9027  | 10082 | -15 | 2 | 5 | 161   | 147   | 9   | 3  | 5    | 1851 | 2012 | -12 | 5 | 5   | 211  | 168  |
| -13 | 10 | 4 | 200  | 223  | -5  | 0  | 5 | 3001  | 2836  | -14 | 2 | 5 | 971   | 912   | 10  | 3  | 5    | 35   | 28   | -11 | 5 | 5   | 55   | 24   |
| -12 | 10 | 4 | 24   | 4    | -3  | 0  | 5 | 38034 | 41237 | -13 | 2 | 5 | 719   | 632   | 11  | 3  | 5    | 2472 | 2201 | -10 | 5 | 5   | 262  | 246  |
| -11 | 10 | 4 | 35   | 15   | -1  | 0  | 5 | 4736  | 5053  | -12 | 2 | 5 | 4247  | 3926  | 12  | 3  | 5    | 244  | 199  | -9  | 5 | 5   | 1069 | 1079 |
| -10 | 10 | 4 | 39   | 44   | 1   | 0  | 5 | 610   | 486   | -11 | 2 | 5 | 406   | 410   | 13  | 3  | 5    | 669  | 652  | -8  | 5 | 5   | 11   | 3    |
| -9  | 10 | 4 | 11   | 1    | 3   | 0  | 5 | 582   | 441   | -10 | 2 | 5 | 4079  | 4022  | 14  | 3  | 5    | 20   | 4    | -7  | 5 | 5   | 355  | 40   |
| -8  | 5  | 5 | 55   | 33   | 17  | 6  | 5 | 44    | 38    | 0   | 8 | 5 | 58    | 54    | -5  | 10 | 5    | 4    | 15   | 16  | 0 | 6   | 4    | 40   |
| -7  | 5  | 5 | 504  | 529  | 18  | 6  | 5 | 58    | 26    | 1   | 8 | 5 | 331   | 348   | -4  | 10 | 5    | 93   | 60   | 18  | 0 | 6   | -14  | 30   |
| -6  | 5  | 5 | 2706 | 2629 | 19  | 6  | 5 | 6     | 3     | 2   | 8 | 5 | 91    | 87    | -3  | 10 | 5    | 12   | 19   | 20  | 0 | 6   | -29  | 4    |
| -5  | 5  | 5 | 4364 | 4114 | 20  | 6  | 5 | 4     | 52    | 3   | 8 | 5 | 382   | 402   | -2  | 10 | 5    | 0    | 1    | -22 | 1 | 6   | 6    | 5    |
| -4  | 5  | 5 | 139  | 105  | -21 | 7  | 5 | -35   | 1     | 4   | 8 | 5 | 10    | 3     | -1  | 10 | 5    | 156  | 169  | -21 | 1 | 6   | 41   | 38   |
| -3  | 5  | 5 | 421  | 431  | -20 | 7  | 5 | 19    | 3     | 5   | 8 | 5 | 363   | 369   | 0   | 10 | 5    | 6    | 13   | -20 | 1 | 6   | 66   | 21   |
| -2  | 5  | 5 | 18   | 3    | -19 | 7  | 5 | 16    | 32    | 6   | 8 | 5 | 182   | 168   | 1   | 10 | 5    | 6    | 33   | -19 | 1 | 6   | 56   | 64   |
| -1  | 5  | 5 | 86   | 110  | -18 | 7  | 5 | -16   | 3     | 7   | 8 | 5 | 899   | 846   | 2   | 10 | 5    | 25   | 5    | -18 | 1 | 6   | 103  | 83   |
| 0   | 5  | 5 | 1035 | 958  | -17 | 7  | 5 | 36    | 2     | 8   | 8 | 5 | 285   | 257   | 3   | 10 | 5    | 36   | 19   | -17 | 1 | 6   | 23   | 26   |
| 1   | 5  | 5 | 608  | 678  | -16 | 7  | 5 | 10    | 1     | 9   | 8 | 5 | 162   | 143   | 4   | 10 | 5    | 112  | 125  | -16 | 1 | 6   | 10   | 16   |
| 2   | 5  | 5 | 1256 | 1183 | -15 | 7  | 5 | 137   | 93    | 10  | 8 | 5 | 195   | 194   | 5   | 10 | 5    | -37  | 9    | -15 | 1 | 6   | 3003 | 3127 |
| 3   | 5  | 5 | 444  | 521  | -14 | 7  | 5 | 305   | 343   | 11  | 8 | 5 | 272   | 275   | 6   | 10 | 5    | 91   | 92   | -14 | 1 | 6   | 1594 | 1520 |
| 4   | 5  | 5 | 85   | 95   | -13 | 7  | 5 | 25    | 45    | 12  | 8 | 5 | 0     | 24    | 7   | 10 | 5    | 109  | 128  | -13 | 1 | 6   | 29   | 15   |
| 5   | 5  | 5 | 2522 | 2346 | -12 | 7  | 5 | -10   | 3     | 13  | 8 | 5 | 87    | 55    | 8   | 10 | 5    | 5    | 4    | -12 | 1 | 6   | 236  | 247  |
| 6   | 5  | 5 | 1121 | 978  | -11 | 7  | 5 | 143   | 137   | 14  | 8 | 5 | 57    | 50    | 9   | 10 | 5    | -27  | 18   | -11 | 1 | 6   | 195  | 234  |
| 7   | 5  | 5 | 721  | 788  | -10 | 7  | 5 | 432   | 377   | 15  | 8 | 5 | 104   | 85    | 10  | 10 | 5    | 34   | 7    | -10 | 1 | 6   | 346  | 189  |
| 8   | 5  | 5 | 32   | 6    | -9  | 7  | 5 | 28    | 26    | 16  | 8 | 5 | 22    | 46    | 11  | 10 | 5    | 33   | 25   | -9  | 1 | 6   | 3869 | 3755 |
| 9   | 5  | 5 | 2066 | 2026 | -8  | 7  | 5 | 12    | 10    | 17  | 8 | 5 | 33    | 22    | 12  | 10 | 5    | 47   | 2    | -7  | 1 | 6   | 98   | 108  |
| 10  | 5  | 5 | 898  | 924  | -7  | 7  | 5 | 142   | 149   | 18  | 8 | 5 | 39    | 3     | 13  | 10 | 5    | -45  | 28   | -6  | 1 | 6   | 51   | 37   |
| 11  | 5  | 5 | 103  | 122  | -6  | 7  | 5 | 122   | 106   | 19  | 8 | 5 | 94    | 63    | -9  | 11 | 5    | 24   | 7    | -5  |   |     |      |      |

Table B.3, continued

| M   | K | L | Obs   | Calc  | M   | K | L | Obs  | Calc | M   | K  | L | Obs  | Calc | M   | K | L | Obs   | Calc  | M   | K  | L | Obs  | Calc |
|-----|---|---|-------|-------|-----|---|---|------|------|-----|----|---|------|------|-----|---|---|-------|-------|-----|----|---|------|------|
| 4   | 6 | 5 | 143   | 176   | -13 | 8 | 5 | 71   | 93   | 15  | 8  | 5 | 53   | 14   | -10 | 0 | 6 | 945   | 983   | -16 | 2  | 6 | 452  | 498  |
| 5   | 6 | 5 | 632   | 585   | -12 | 8 | 5 | 0    | 1    | 16  | 9  | 5 | 64   | 35   | -8  | 0 | 6 | 7442  | 7526  | -15 | 2  | 6 | 297  | 300  |
| 6   | 6 | 5 | 155   | 175   | -11 | 8 | 5 | 424  | 369  | 17  | 9  | 5 | 2    | 1    | -6  | 0 | 6 | 1429  | 1216  | -14 | 2  | 6 | 1847 | 1790 |
| 7   | 6 | 5 | 1375  | 1444  | -10 | 8 | 5 | 307  | 310  | -15 | 10 | 5 | 54   | 17   | -4  | 0 | 6 | 9     | 16    | -13 | 2  | 6 | 3858 | 3652 |
| 8   | 6 | 5 | 350   | 324   | -9  | 8 | 5 | 96   | 79   | -14 | 10 | 5 | 129  | 92   | -2  | 0 | 6 | 10266 | 10745 | -12 | 2  | 6 | 1366 | 1317 |
| 9   | 6 | 5 | 19    | 12    | -8  | 8 | 5 | 163  | 138  | -13 | 10 | 5 | -13  | 1    | 0   | 0 | 6 | 83    | 65    | -11 | 2  | 6 | 3239 | 3116 |
| 10  | 6 | 5 | 53    | 64    | -7  | 8 | 5 | 216  | 232  | -12 | 10 | 5 | 216  | 201  | 2   | 0 | 6 | 14543 | 15249 | -10 | 2  | 6 | 541  | 547  |
| 11  | 6 | 5 | 801   | 722   | -6  | 8 | 5 | 104  | 80   | -11 | 10 | 5 | 32   | 49   | 4   | 0 | 6 | 9819  | 10287 | -9  | 2  | 6 | 2874 | 2756 |
| 12  | 6 | 5 | 1     | 4     | -5  | 8 | 5 | 405  | 396  | -10 | 10 | 5 | 0    | 1    | 6   | 0 | 6 | 6010  | 5722  | -8  | 2  | 6 | 1216 | 1048 |
| 13  | 6 | 5 | 766   | 883   | -4  | 8 | 5 | 3    | 7    | -9  | 10 | 5 | 23   | 6    | 8   | 0 | 6 | 1788  | 1610  | -7  | 2  | 6 | 7118 | 6792 |
| 14  | 6 | 5 | 142   | 141   | -3  | 8 | 5 | 7    | 5    | -8  | 10 | 5 | 145  | 126  | 10  | 0 | 6 | 843   | 815   | -6  | 2  | 6 | 41   | 18   |
| 15  | 6 | 5 | 22    | 6     | -2  | 8 | 5 | 99   | 81   | -7  | 10 | 5 | 69   | 66   | 12  | 0 | 6 | 24    | 2     | -5  | 2  | 6 | 688  | 691  |
| 16  | 6 | 5 | 120   | 136   | -1  | 8 | 5 | 476  | 451  | -6  | 10 | 5 | 264  | 245  | 12  | 0 | 6 | 56    | 12    | -4  | 2  | 6 | 3213 | 3579 |
| -2  | 2 | 6 | 2623  | 2804  | 19  | 3 | 6 | 66   | 62   | -3  | 5  | 6 | 73   | 48   | -21 | 7 | 6 | 6     | 2     | 4   | 8  | 6 | 42   | 37   |
| -2  | 2 | 6 | 1407  | 1402  | 20  | 3 | 6 | 401  | 446  | -2  | 5  | 6 | 2944 | 2771 | -20 | 7 | 6 | -1    | 2     | 5   | 8  | 6 | 1142 | 1097 |
| -1  | 2 | 6 | 423   | 412   | 21  | 3 | 6 | 28   | 5    | -1  | 5  | 6 | 190  | 191  | -19 | 7 | 6 | 69    | 78    | 6   | 8  | 6 | 787  | 773  |
| 0   | 2 | 6 | 10981 | 11335 | -22 | 4 | 6 | -71  | 3    | 0   | 5  | 6 | 255  | 311  | -18 | 7 | 6 | 28    | 25    | 7   | 8  | 6 | 6    | 7    |
| 1   | 2 | 6 | 16480 | 17007 | -21 | 4 | 6 | 132  | 140  | 1   | 5  | 6 | 1349 | 1308 | -17 | 7 | 6 | 44    | 8     | 8   | 8  | 6 | 176  | 159  |
| 2   | 2 | 6 | 210   | 223   | -20 | 4 | 6 | 104  | 69   | 2   | 5  | 6 | 184  | 219  | -16 | 7 | 6 | 58    | 68    | 9   | 8  | 6 | 265  | 265  |
| 3   | 2 | 6 | 733   | 715   | -19 | 4 | 6 | 351  | 326  | 3   | 5  | 6 | 1314 | 1429 | -15 | 7 | 6 | 62    | 94    | 10  | 8  | 6 | 26   | 8    |
| 4   | 2 | 6 | 2453  | 2486  | -18 | 4 | 6 | 13   | 0    | 4   | 5  | 6 | 732  | 730  | -14 | 7 | 6 | 59    | 58    | 11  | 8  | 6 | 84   | 73   |
| 5   | 2 | 6 | 126   | 125   | -17 | 4 | 6 | 690  | 705  | 5   | 5  | 6 | 215  | 220  | -13 | 7 | 6 | 87    | 95    | 12  | 8  | 6 | 22   | 4    |
| 6   | 2 | 6 | 3173  | 3060  | -16 | 4 | 6 | -6   | 4    | 6   | 5  | 6 | 887  | 858  | -12 | 7 | 6 | 28    | 24    | 13  | 8  | 6 | 14   | 3    |
| 7   | 2 | 6 | 146   | 87    | -15 | 4 | 6 | 229  | 183  | 7   | 5  | 6 | 211  | 181  | -11 | 7 | 6 | 130   | 77    | 14  | 8  | 6 | 38   | 19   |
| 8   | 2 | 6 | 22    | 44    | -14 | 4 | 6 | 213  | 236  | 8   | 5  | 6 | 1809 | 1717 | -10 | 7 | 6 | 4     | 7     | 15  | 8  | 6 | 3    | 2    |
| 9   | 2 | 6 | 1081  | 1125  | -13 | 4 | 6 | 1229 | 1251 | 9   | 5  | 6 | 1926 | 1918 | -9  | 7 | 6 | 86    | 98    | 16  | 8  | 6 | 41   | 35   |
| 10  | 2 | 6 | 178   | 207   | -12 | 4 | 6 | 364  | 322  | 10  | 5  | 6 | 567  | 542  | -8  | 7 | 6 | 68    | 37    | 17  | 8  | 6 | 17   | 0    |
| 11  | 2 | 6 | 5     | 1     | -11 | 4 | 6 | 224  | 206  | 11  | 5  | 6 | 34   | 7    | -7  | 7 | 6 | 56    | 47    | 18  | 8  | 6 | 8    | 0    |
| 12  | 2 | 6 | 578   | 620   | -10 | 4 | 6 | 13   | 3    | 12  | 5  | 6 | 54   | 52   | -6  | 7 | 6 | 165   | 137   | 19  | 8  | 6 | 75   | 1    |
| 13  | 2 | 6 | 462   | 435   | -9  | 4 | 6 | 927  | 865  | 13  | 5  | 6 | 1075 | 1072 | -5  | 7 | 6 | 811   | 768   | -18 | 9  | 6 | 90   | 0    |
| 14  | 2 | 6 | 220   | 239   | -8  | 4 | 6 | 141  | 161  | 14  | 5  | 6 | 28   | 3    | -4  | 7 | 6 | 178   | 182   | -17 | 9  | 6 | 26   | 9    |
| 15  | 2 | 6 | 797   | 862   | -7  | 4 | 6 | 396  | 424  | 15  | 5  | 6 | 49   | 1    | -3  | 7 | 6 | 783   | 747   | -16 | 9  | 6 | 39   | 10   |
| 16  | 2 | 6 | 216   | 176   | -6  | 4 | 6 | 514  | 386  | 16  | 5  | 6 | 44   | 65   | -2  | 7 | 6 | 21    | 4     | -15 | 9  | 6 | 72   | 30   |
| 17  | 2 | 6 | 10    | 35    | -5  | 4 | 6 | 1980 | 1991 | 17  | 5  | 6 | 54   | 84   | -1  | 7 | 6 | 213   | 173   | -14 | 9  | 6 | 8    | 5    |
| 18  | 2 | 6 | 117   | 138   | -4  | 4 | 6 | 233  | 173  | 18  | 5  | 6 | 8    | 12   | 0   | 7 | 6 | 58    | 61    | -13 | 9  | 6 | 63   | 96   |
| 19  | 2 | 6 | 33    | 25    | -3  | 4 | 6 | 3959 | 4063 | 19  | 5  | 6 | 20   | 41   | 1   | 7 | 6 | 454   | 378   | -12 | 9  | 6 | 3    | 5    |
| 20  | 2 | 6 | 40    | 28    | -2  | 4 | 6 | 791  | 761  | 20  | 5  | 6 | 58   | 38   | 2   | 7 | 6 | 5     | 1     | -11 | 9  | 6 | 60   | 71   |
| 21  | 2 | 6 | 108   | 8     | -1  | 4 | 6 | 7030 | 6953 | -21 | 6  | 6 | 197  | 28   | 3   | 7 | 6 | 844   | 854   | -10 | 9  | 6 | 32   | 20   |
| -22 | 3 | 6 | 158   | 47    | 0   | 4 | 6 | 6052 | 6238 | -20 | 6  | 6 | 5    | 6    | 4   | 7 | 6 | -7    | 1     | -9  | 9  | 6 | 44   | 22   |
| -21 | 3 | 6 | 81    | 26    | 1   | 4 | 6 | 2726 | 2584 | -19 | 6  | 6 | 30   | 11   | 5   | 7 | 6 | 105   | 75    | -8  | 9  | 6 | 8    | 10   |
| -20 | 3 | 6 | 56    | 76    | 2   | 4 | 6 | 15   | 2    | -18 | 6  | 6 | 351  | 345  | 6   | 7 | 6 | -1    | 0     | -7  | 9  | 6 | 39   | 20   |
| -19 | 3 | 6 | 38    | 30    | 3   | 4 | 6 | 360  | 260  | -17 | 6  | 6 | 30   | 28   | 7   | 7 | 6 | 252   | 266   | -6  | 9  | 6 | 104  | 137  |
| -18 | 3 | 6 | 23    | 6     | 4   | 4 | 6 | 3895 | 3559 | -16 | 6  | 6 | 252  | 257  | 8   | 7 | 6 | 569   | 578   | -5  | 9  | 6 | 43   | 18   |
| -17 | 3 | 6 | 29    | 0     | 5   | 4 | 6 | 617  | 664  | -15 | 6  | 6 | 28   | 3    | 9   | 7 | 6 | 52    | 41    | -4  | 9  | 6 | 185  | 189  |
| -16 | 3 | 6 | 664   | 632   | 6   | 4 | 6 | 520  | 618  | -14 | 6  | 6 | 256  | 278  | 10  | 7 | 6 | 128   | 131   | -3  | 9  | 6 | 15   | 0    |
| -15 | 3 | 6 | 20    | 30    | 7   | 4 | 6 | 347  | 337  | -13 | 6  | 6 | 3    | 1    | 11  | 7 | 6 | 1280  | 1198  | -2  | 9  | 6 | 393  | 408  |
| -14 | 3 | 6 | 974   | 1011  | 8   | 4 | 6 | 236  | 304  | -12 | 6  | 6 | 288  | 304  | 12  | 7 | 6 | 45    | 77    | -1  | 9  | 6 | 737  | 724  |
| -13 | 3 | 6 | 997   | 990   | 9   | 4 | 6 | 447  | 388  | -11 | 6  | 6 | -1   | 1    | 13  | 7 | 6 | 158   | 150   | 0   | 9  | 6 | 231  | 174  |
| -12 | 3 | 6 | 1600  | 1684  | 10  | 4 | 6 | 100  | 117  | -10 | 6  | 6 | 577  | 550  | 14  | 7 | 6 | 57    | 60    | 1   | 9  | 6 | 578  | 491  |
| -11 | 3 | 6 | 250   | 260   | 11  | 4 | 6 | 129  | 137  | -9  | 6  | 6 | 149  | 118  | 15  | 7 | 6 | 378   | 426   | 2   | 9  | 6 | 59   | 28   |
| -10 | 3 | 6 | 1658  | 1676  | 12  | 4 | 6 | 64   | 56   | -8  | 6  | 6 | 283  | 361  | 16  | 7 | 6 | 53    | 35    | 3   | 9  | 6 | 114  | 116  |
| -9  | 3 | 6 | 50    | 46    | 13  | 4 | 6 | 651  | 616  | -7  | 6  | 6 | 696  | 627  | 17  | 7 | 6 | 338   | 362   | 4   | 9  | 6 | 49   | 67   |
| -8  | 3 | 6 | 903   | 941   | 14  | 4 | 6 | 21   | 40   | -6  | 6  | 6 | 838  | 829  | 18  | 7 | 6 | 76    | 20    | 5   | 9  | 6 | 46   | 42   |
| -7  | 3 | 6 | 332   | 277   | 15  | 4 | 6 | 39   | 17   | -5  | 6  | 6 | 369  | 361  | 19  | 7 | 6 | 156   | 200   | 6   | 9  | 6 | 132  | 112  |
| -6  | 3 | 6 | 9010  | 8647  | 16  | 4 | 6 | 134  | 76   | -4  | 6  | 6 | 25   | 18   | 20  | 7 | 6 | 22    | 18    | 7   | 9  | 6 | 54   | 29   |
| -5  | 3 | 6 | 95    | 61    | 17  | 4 | 6 | -22  | 7    | -3  | 6  | 6 | 54   | 40   | -20 | 8 | 6 | 23    | 11    | 8   | 9  | 6 | 15   | 0    |
| -4  | 3 | 6 | 3023  | 2974  | 18  | 4 | 6 | 84   | 127  | -2  | 6  | 6 | 17   | 32   | -19 | 8 | 6 | 6     | 6     | 10  | 9  | 6 | 26   | 32   |
| -3  | 3 | 6 | 1421  | 1529  | 19  | 4 | 6 | 15   | 6    | -1  | 6  | 6 | 52   | 59   | -18 | 8 | 6 | 42    | 92    | 10  | 9  | 6 | -12  | 8    |
| -2  | 3 | 6 | 5397  | 5974  | 20  | 4 | 6 | 45   | 8    | 0   | 6  | 6 | 56   | 32   | -17 | 8 | 6 | 34    | 12    | 11  | 9  | 6 | 42   | 1    |
| -1  | 3 | 6 | 1089  | 1237  | 21  | 4 | 6 | 55   | 0    | 1   | 6  | 6 | 126  | 116  | -16 | 8 | 6 | 87    | 37    | 12  | 9  | 6 | 25   | 2    |
| 0   | 3 | 6 | 10124 | 9786  | -22 | 5 | 6 | -38  | 29   | 2   | 6  | 6 | 21   | 20   | -15 | 8 | 6 | 24    | 49    | 13  | 9  | 6 | 36   | 8    |
| 1   | 3 | 6 | 2367  | 2148  | -21 | 5 | 6 | 161  | 61   | 3   | 6  | 6 | 683  | 605  | -14 | 8 | 6 | 316   | 288   | 14  | 9  | 6 | 36   | 15   |
| 2   | 3 | 6 | 5694  | 6592  | -20 | 5 | 6 | 82   | 68   | 4   | 6  | 6 | 98   | 99   | -13 | 8 | 6 | 85    | 73    | 15  | 9  | 6 | 1    | 3    |
| 3   | 3 | 6 | 7     | 8     | -19 | 5 | 6 | 26   | 51   | 5   | 6  | 6 | 557  | 542  | -12 | 8 | 6 | 288   | 293   | 16  | 9  | 6 | -9   | 16   |
| 4   | 3 | 6 | 1660  | 1834  | -18 | 5 | 6 | 144  | 112  | 6   | 6  | 6 | 8    | 4    | -11 | 8 | 6 | 36    | 31    | 17  | 9  | 6 | 30   | 3    |
| 5   | 3 | 6 | 490   | 427   | -17 | 5 | 6 | 169  | 197  | 7   | 6  | 6 | 65   | 91   | -10 | 8 | 6 | 74    | 64    | -15 | 10 | 6 | 31   | 1    |
| 6   | 3 | 6 | 892   | 976   | -16 | 5 | 6 | 200  | 215  | 8   | 6  | 6 | 42   | 41   | -9  | 8 | 6 | 0     | 4     | -14 | 10 | 6 | 19   | 41   |
| 7   | 3 | 6 | 1729  | 1673  | -15 | 5 | 6 | 42   | 24   | 9   | 6  | 6 | 128  | 130  | -8  | 8 | 6 | 35    | 20    | -13 | 10 | 6 | -5   | 1    |
| 8   | 3 | 6 | 3506  | 3515  | -14 | 5 | 6 | 157  | 116  | 10  | 6  | 6 | 797  | 814  | -7  | 8 | 6 | 145   | 145   | -12 | 10 | 6 | -1   | 7    |
| 9   | 3 | 6 | 1089  | 957   | -13 | 5 | 6 | 79   | 66   | 11  | 6  | 6 | 56   | 11   | -6  | 8 | 6 | 197   | 199   | -11 | 10 | 6 | 22   | 8    |
| 10  | 3 | 6 |       |       |     |   |   |      |      |     |    |   |      |      |     |   |   |       |       |     |    |   |      |      |

Table B.3, continued

| M   | K  | L | Obs   | Calc  | M   | K | L | Obs   | Calc  | M   | K  | L | Obs   | Calc  | M  | K | L | Obs   | Calc  | M   | K | L | Obs  | Calc |
|-----|----|---|-------|-------|-----|---|---|-------|-------|-----|----|---|-------|-------|----|---|---|-------|-------|-----|---|---|------|------|
| 0   | 11 | 6 | 73    | 29    | 6   | 1 | 7 | 12951 | 13176 | -16 | 3  | 7 | 81    | 69    | 6  | 4 | 7 | 1633  | 1669  | -13 | 6 | 7 | 139  | 138  |
| 1   | 11 | 6 | 72    | 25    | 7   | 1 | 7 | 3166  | 3240  | -15 | 3  | 7 | 225   | 220   | 7  | 4 | 7 | 13    | 30    | -12 | 6 | 7 | 348  | 307  |
| 2   | 11 | 6 | 28    | 1     | 8   | 1 | 7 | 58    | 128   | -14 | 3  | 7 | 1422  | 1399  | 8  | 4 | 7 | 420   | 434   | -11 | 6 | 7 | 18   | 11   |
| 3   | 11 | 6 | 15    | 0     | 9   | 1 | 7 | 4140  | 4212  | -12 | 3  | 7 | 276   | 257   | 10 | 4 | 7 | 52    | 62    | -10 | 6 | 7 | 457  | 493  |
| 4   | 11 | 6 | 10    | 0     | 10  | 1 | 7 | 92    | 97    | -11 | 3  | 7 | 510   | 505   | 11 | 4 | 7 | 271   | 280   | -9  | 6 | 7 | 2    | 8    |
| 5   | 11 | 6 | 12    | 23    | 11  | 1 | 7 | 3600  | 3455  | -10 | 3  | 7 | 311   | 258   | 12 | 4 | 7 | 168   | 169   | -8  | 6 | 7 | 341  | 374  |
| 6   | 11 | 6 | 21    | 0     | 12  | 1 | 7 | 285   | 267   | -9  | 3  | 7 | 3325  | 3360  | 13 | 4 | 7 | 266   | 280   | -7  | 6 | 7 | 159  | 197  |
| 7   | 11 | 6 | -35   | 16    | 13  | 1 | 7 | 1091  | 1040  | -8  | 3  | 7 | -5    | 1     | 14 | 4 | 7 | 315   | 307   | -6  | 6 | 7 | 143  | 131  |
| 8   | 11 | 6 | -15   | 0     | 14  | 1 | 7 | 137   | 162   | -7  | 3  | 7 | 3716  | 3876  | 15 | 4 | 7 | 19    | 20    | -5  | 6 | 7 | 775  | 819  |
| -7  | 12 | 6 | 191   | 29    | 15  | 1 | 7 | 1957  | 1968  | -6  | 3  | 7 | 2148  | 1916  | 16 | 4 | 7 | 47    | 33    | -4  | 6 | 7 | 17   | 0    |
| -6  | 12 | 6 | 39    | 0     | 16  | 1 | 7 | 145   | 99    | -5  | 3  | 7 | 3266  | 3162  | 17 | 4 | 7 | -12   | 2     | -3  | 6 | 7 | 1167 | 1311 |
| -5  | 12 | 6 | 4     | 1     | 17  | 1 | 7 | 720   | 722   | -4  | 3  | 7 | 4811  | 4575  | 18 | 4 | 7 | 11    | 2     | -2  | 6 | 7 | 355  | 404  |
| -4  | 12 | 6 | 77    | 13    | 18  | 1 | 7 | 46    | 29    | -3  | 3  | 7 | 10139 | 10106 | 19 | 4 | 7 | 68    | 5     | -1  | 6 | 7 | 744  | 735  |
| -3  | 12 | 6 | 77    | 0     | 19  | 1 | 7 | 586   | 509   | -2  | 3  | 7 | 6241  | 6784  | 20 | 4 | 7 | 7     | 3     | 0   | 6 | 7 | 0    | 1    |
| -2  | 12 | 6 | 149   | 1     | 20  | 1 | 7 | 55    | 13    | -1  | 3  | 7 | 11514 | 11905 | 21 | 4 | 7 | 39    | 80    | 1   | 6 | 7 | 1017 | 1102 |
| 6   | 12 | 6 | 93    | 2     | 21  | 1 | 7 | 36    | 4     | 0   | 3  | 7 | 41    | 28    | 21 | 5 | 7 | -80   | 37    | 2   | 6 | 7 | 29   | 24   |
| -21 | 0  | 7 | 797   | 933   | -22 | 2 | 7 | 125   | 105   | 1   | 3  | 7 | 7533  | 8098  | 22 | 5 | 7 | 23    | 1     | 3   | 6 | 7 | 925  | 1124 |
| -19 | 0  | 7 | 341   | 379   | -21 | 2 | 7 | 305   | 296   | 2   | 3  | 7 | 912   | 940   | 23 | 5 | 7 | 91    | 56    | 4   | 6 | 7 | 1118 | 1180 |
| -17 | 0  | 7 | 1027  | 934   | -20 | 2 | 7 | 152   | 113   | 3   | 3  | 7 | 881   | 852   | 24 | 5 | 7 | 17    | 0     | 6   | 6 | 7 | 280  | 261  |
| -15 | 0  | 7 | 53    | 21    | -19 | 2 | 7 | 212   | 166   | 4   | 3  | 7 | 35    | 24    | 24 | 5 | 7 | 123   | 146   | 7   | 6 | 7 | 939  | 969  |
| -13 | 0  | 7 | 7377  | 7436  | -18 | 2 | 7 | 220   | 207   | 5   | 3  | 7 | 1974  | 1908  | 25 | 5 | 7 | 10    | 15    | 8   | 6 | 7 | 290  | 275  |
| -11 | 0  | 7 | 1966  | 1951  | -17 | 2 | 7 | 16    | 9     | 6   | 3  | 7 | 391   | 429   | 26 | 5 | 7 | 204   | 191   | 9   | 6 | 7 | 630  | 622  |
| -9  | 0  | 7 | 4833  | 4887  | -16 | 2 | 7 | 585   | 595   | 7   | 3  | 7 | 490   | 558   | 27 | 5 | 7 | 105   | 191   | 10  | 6 | 7 | 3    | 5    |
| -7  | 0  | 7 | 13212 | 14309 | -15 | 2 | 7 | 25    | 3     | 8   | 3  | 7 | 1406  | 1246  | 28 | 5 | 7 | 36    | 191   | 11  | 6 | 7 | 28   | 11   |
| -5  | 0  | 7 | 31    | 29    | -14 | 2 | 7 | 924   | 806   | 9   | 3  | 7 | 492   | 419   | 29 | 5 | 7 | 36    | 23    | 12  | 6 | 7 | 431  | 479  |
| -3  | 0  | 7 | 7987  | 8333  | -12 | 2 | 7 | 311   | 265   | 10  | 3  | 7 | 963   | 940   | 30 | 5 | 7 | 1104  | 1068  | 13  | 6 | 7 | 694  | 697  |
| -1  | 0  | 7 | 6207  | 6838  | -11 | 2 | 7 | 599   | 681   | 11  | 3  | 7 | 21    | 7     | 30 | 5 | 7 | 59    | 60    | 14  | 6 | 7 | 155  | 158  |
| 1   | 0  | 7 | 571   | 512   | -10 | 2 | 7 | 1003  | 1009  | 12  | 3  | 7 | 280   | 264   | 31 | 5 | 7 | 2504  | 2331  | 15  | 6 | 7 | -8   | 15   |
| 3   | 0  | 7 | 1621  | 1713  | -9  | 2 | 7 | 130   | 129   | 13  | 3  | 7 | 480   | 516   | 32 | 5 | 7 | 1981  | 1842  | 16  | 6 | 7 | 13   | 2    |
| 7   | 0  | 7 | 4727  | 4358  | -8  | 2 | 7 | 17    | 23    | 14  | 3  | 7 | 21    | 1     | 33 | 5 | 7 | 976   | 1097  | 17  | 6 | 7 | -4   | 0    |
| 9   | 0  | 7 | 4     | 3     | -7  | 2 | 7 | 1106  | 925   | 15  | 3  | 7 | 462   | 490   | 33 | 5 | 7 | 37    | 36    | 18  | 6 | 7 | 27   | 10   |
| 11  | 0  | 7 | 257   | 263   | -6  | 2 | 7 | 8366  | 8542  | 16  | 3  | 7 | 30    | 10    | 34 | 5 | 7 | 2151  | 2106  | 19  | 6 | 7 | -9   | 1    |
| 13  | 0  | 7 | 41    | 10    | -5  | 2 | 7 | 1769  | 1634  | 17  | 3  | 7 | 111   | 67    | 35 | 5 | 7 | 18    | 25    | 20  | 6 | 7 | 105  | 7    |
| 15  | 0  | 7 | 2     | 1     | -4  | 2 | 7 | 116   | 110   | 18  | 3  | 7 | 27    | 41    | 36 | 5 | 7 | 1234  | 1359  | 21  | 7 | 7 | 16   | 1    |
| 17  | 0  | 7 | 116   | 133   | -3  | 2 | 7 | 1543  | 1610  | 19  | 3  | 7 | 269   | 289   | 36 | 5 | 7 | 543   | 475   | 22  | 7 | 7 | -7   | 1    |
| 19  | 0  | 7 | 179   | 72    | -2  | 2 | 7 | 121   | 96    | 20  | 3  | 7 | 105   | 6     | 37 | 5 | 7 | 1973  | 1965  | 23  | 7 | 7 | -19  | 0    |
| 21  | 0  | 7 | -82   | 7     | -1  | 2 | 7 | 6038  | 5730  | 21  | 3  | 7 | 2     | 11    | 0  | 5 | 7 | 104   | 141   | -18 | 7 | 7 | 58   | 56   |
| 22  | 1  | 7 | 86    | 123   | 0   | 2 | 7 | 7550  | 7712  | -22 | 4  | 7 | 185   | 170   | 1  | 5 | 7 | 29    | 5     | -17 | 7 | 7 | 52   | 3    |
| -21 | 1  | 7 | -3    | 5     | 1   | 2 | 7 | 2208  | 2129  | -21 | 4  | 7 | -11   | 1     | 2  | 5 | 7 | 234   | 205   | -16 | 7 | 7 | 28   | 12   |
| -20 | 1  | 7 | 387   | 398   | 2   | 2 | 7 | 167   | 108   | -20 | 4  | 7 | 116   | 139   | 3  | 5 | 7 | 672   | 614   | -15 | 7 | 7 | 5    | 13   |
| -19 | 1  | 7 | 9     | 13    | 3   | 2 | 7 | 399   | 443   | -19 | 4  | 7 | 228   | 261   | 4  | 5 | 7 | 164   | 146   | -14 | 7 | 7 | 209  | 208  |
| -13 | 7  | 7 | 76    | 125   | 12  | 0 | 7 | 36    | 39    | 7   | 10 | 7 | 40    | 15    | -8 | 1 | 8 | 1867  | 1701  | 14  | 2 | 8 | 76   | 49   |
| -12 | 7  | 7 | 119   | 94    | 13  | 0 | 7 | 37    | 4     | 8   | 10 | 7 | 85    | 53    | -7 | 1 | 8 | 18316 | 18684 | 15  | 2 | 8 | 180  | 130  |
| -11 | 7  | 7 | 68    | 37    | 14  | 0 | 7 | 8     | 1     | 9   | 10 | 7 | -6    | 12    | -6 | 1 | 8 | 329   | 417   | 16  | 2 | 8 | 69   | 39   |
| -10 | 7  | 7 | 322   | 327   | 15  | 0 | 7 | 40    | 48    | 10  | 10 | 7 | -13   | 10    | -5 | 1 | 8 | 8737  | 7127  | 17  | 2 | 8 | 74   | 38   |
| -9  | 7  | 7 | 656   | 628   | 16  | 0 | 7 | 26    | 13    | 11  | 10 | 7 | 25    | 6     | -4 | 1 | 8 | 10208 | 10341 | 19  | 2 | 8 | 89   | 2    |
| -8  | 7  | 7 | 62    | 49    | 17  | 0 | 7 | -19   | 4     | 12  | 10 | 7 | -5    | 8     | -2 | 3 | 1 | 160   | 174   | 20  | 2 | 8 | 15   | 25   |
| -6  | 7  | 7 | 7     | 5     | 18  | 0 | 7 | 26    | 30    | -8  | 11 | 7 | 19    | 8     | -1 | 1 | 8 | 1370  | 1171  | -22 | 3 | 8 | 314  | 69   |
| -5  | 7  | 7 | 951   | 870   | 19  | 0 | 7 | 85    | 28    | -7  | 11 | 7 | -47   | 19    | 0  | 1 | 8 | 810   | 709   | -21 | 3 | 8 | 60   | 1    |
| -4  | 7  | 7 | 1477  | 1457  | -17 | 9 | 7 | 7     | 13    | -6  | 11 | 7 | -54   | 1     | 1  | 1 | 8 | 2029  | 2178  | -20 | 3 | 8 | 295  | 293  |
| -3  | 7  | 7 | 62    | 44    | -16 | 9 | 7 | 74    | 25    | -5  | 11 | 7 | 45    | 34    | 2  | 1 | 8 | 1101  | 1231  | -19 | 3 | 8 | 55   | 84   |
| -2  | 7  | 7 | 1949  | 1895  | -15 | 9 | 7 | 62    | 1     | -4  | 11 | 7 | 31    | 32    | 3  | 1 | 8 | 1483  | 1811  | -18 | 3 | 8 | 520  | 575  |
| -1  | 7  | 7 | 101   | 101   | -14 | 9 | 7 | 207   | 192   | -3  | 11 | 7 | 19    | 3     | 4  | 1 | 8 | 895   | 1001  | -17 | 3 | 8 | 65   | 22   |
| 0   | 7  | 7 | 1248  | 1257  | -13 | 9 | 7 | 76    | 34    | -2  | 11 | 7 | -1    | 0     | 5  | 1 | 8 | 2831  | 3043  | -16 | 3 | 8 | 1208 | 1168 |
| 1   | 7  | 7 | 74    | 63    | -12 | 9 | 7 | 73    | 63    | -1  | 11 | 7 | 224   | 215   | 6  | 1 | 8 | 1253  | 1200  | -15 | 3 | 8 | 41   | 37   |
| 2   | 7  | 7 | 610   | 566   | -11 | 9 | 7 | 44    | 35    | 0   | 11 | 7 | 61    | 5     | 7  | 1 | 8 | 4953  | 4780  | -14 | 3 | 8 | 53   | 54   |
| 3   | 7  | 7 | 92    | 87    | -10 | 9 | 7 | 94    | 109   | 1   | 11 | 7 | 111   | 78    | 8  | 1 | 8 | 408   | 379   | -13 | 3 | 8 | 869  | 843  |
| 4   | 7  | 7 | 608   | 559   | -9  | 9 | 7 | 23    | 17    | 2   | 11 | 7 | 49    | 17    | 9  | 1 | 8 | 894   | 1052  | -12 | 3 | 8 | 1507 | 1506 |
| 5   | 7  | 7 | 186   | 178   | -8  | 9 | 7 | 14    | 4     | 3   | 11 | 7 | 19    | 20    | 10 | 1 | 8 | 58    | 18    | -11 | 3 | 8 | 100  | 132  |
| 6   | 7  | 7 | 141   | 99    | -7  | 9 | 7 | 68    | 50    | 4   | 11 | 7 | -32   | 1     | 11 | 1 | 8 | 393   | 451   | -10 | 3 | 8 | 732  | 790  |
| 7   | 7  | 7 | 374   | 401   | -6  | 9 | 7 | 247   | 250   | 5   | 11 | 7 | 47    | 48    | 12 | 1 | 8 | 286   | 210   | -9  | 3 | 8 | 74   | 110  |
| 8   | 7  | 7 | 408   | 379   | -5  | 9 | 7 | 17    | 2     | 6   | 11 | 7 | 44    | 4     | 13 | 1 | 8 | 615   | 541   | -8  | 3 | 8 | 754  | 824  |
| 9   | 7  | 7 | 505   | 518   | -4  | 9 | 7 | -1    | 1     | 7   | 11 | 7 | 35    | 9     | 14 | 1 | 8 | 630   | 615   | -7  | 3 | 8 | 9    | 8    |
| 10  | 7  | 7 | 5     | 12    | -3  | 9 | 7 | 20    | 20    | 8   | 11 | 7 | 108   | 14    | 15 | 1 | 8 | 208   | 149   | -6  | 3 | 8 | 3265 | 3341 |
| 11  | 7  | 7 | 29    | 28    | -2  | 9 | 7 | 188   | 154   | -7  | 12 | 7 | 9     | 4     | 16 | 1 | 8 | 206   | 209   | -5  | 3 | 8 | 700  | 782  |
| 12  | 7  | 7 | 103   | 109   | -1  | 9 | 7 | 71    | 65    | -6  | 12 | 7 | -62   | 0     | 17 | 1 | 8 | 491   | 519   | -4  | 3 | 8 | 28   | 36   |
| 13  | 7  | 7 | 12    | 59    | 0   | 9 | 7 | 51    | 43    | -5  | 12 | 7 | 335   | 0     | 18 | 1 | 8 | 81    | 114   | -3  | 3 | 8 | 2352 | 2352 |
| 14  | 7  | 7 | -13   | 6     | 1   | 9 | 7 | 130   | 125   | -4  | 12 | 7 | -43   | 7     | 19 | 1 | 8 | 421   | 352   | -2  | 3 | 8 | 1972 | 2704 |
| 15  | 7  | 7 | -9    | 30    | 2   | 9 | 7 | 138   | 129   | -3  | 12 | 7 | 41    | 41    | 20 | 1 | 8 | 16    | 21    | -1  | 3 | 8 | 3588 | 3259 |
| 16  | 7  | 7 | 36    | 20    | 3   | 9 | 7 | 13    | 1     | -22 | 0  | 8 | 6     | 1     | 21 | 1 | 8 |       |       |     |   |   |      |      |

Table B.3, continued

| M   | K | L | Obs  | Calc | M   | K  | L | Obs | Calc | M   | K | L | Obs  | Calc | M   | K  | L | Obs | Calc | M   | K  | L | Obs   | Calc  |
|-----|---|---|------|------|-----|----|---|-----|------|-----|---|---|------|------|-----|----|---|-----|------|-----|----|---|-------|-------|
| 7   | 0 | 7 | 14   | 9    | 2   | 10 | 7 | 48  | 70   | -13 | 1 | 8 | 1273 | 1275 | 9   | 2  | 8 | 20  | 0    | -11 | 4  | 8 | 129   | 147   |
| 8   | 0 | 7 | 628  | 599  | 3   | 10 | 7 | 57  | 79   | -12 | 1 | 8 | 689  | 718  | 10  | 2  | 8 | -6  | 1    | -10 | 4  | 8 | 160   | 180   |
| 9   | 0 | 7 | 18   | 11   | 4   | 10 | 7 | 11  | 2    | -11 | 1 | 8 | 2736 | 2704 | 11  | 2  | 8 | 450 | 425  | -9  | 4  | 8 | 92    | 95    |
| 10  | 0 | 7 | 55   | 60   | 5   | 10 | 7 | -8  | 1    | -10 | 1 | 8 | 1386 | 1441 | 12  | 2  | 8 | 19  | 26   | -8  | 4  | 8 | 46    | 52    |
| 11  | 0 | 7 | 73   | 79   | 6   | 10 | 7 | 27  | 50   | -9  | 1 | 8 | 14   | 10   | 13  | 2  | 8 | 67  | 57   | -7  | 4  | 8 | 164   | 223   |
| -6  | 4 | 8 | 123  | 111  | 10  | 5  | 8 | 270 | 285  | 0   | 7 | 8 | 420  | 412  | -12 | 9  | 8 | 41  | 7    | 2   | 11 | 8 | 1     | 50    |
| -5  | 4 | 8 | 297  | 293  | 19  | 5  | 8 | 16  | 20   | 1   | 7 | 8 | 511  | 488  | -11 | 9  | 8 | 17  | 17   | 3   | 11 | 8 | 96    | 53    |
| -4  | 4 | 8 | 311  | 324  | 20  | 5  | 8 | 48  | 65   | 2   | 7 | 8 | 514  | 473  | -10 | 9  | 8 | 208 | 188  | 4   | 11 | 8 | 28    | 3     |
| -3  | 4 | 8 | 2538 | 2096 | -21 | 6  | 8 | -32 | 0    | 3   | 7 | 8 | 1001 | 903  | -9  | 9  | 8 | 122 | 87   | 5   | 11 | 8 | 47    | 12    |
| -2  | 4 | 8 | 783  | 845  | -20 | 6  | 8 | 5   | 30   | 4   | 7 | 8 | 1014 | 1086 | -8  | 9  | 8 | 61  | 55   | 6   | 11 | 8 | 60    | 56    |
| -1  | 4 | 8 | 6593 | 6585 | -19 | 6  | 8 | 3   | 0    | 5   | 7 | 8 | 195  | 152  | -7  | 9  | 8 | 86  | 66   | 7   | 11 | 8 | 154   | 20    |
| 0   | 4 | 8 | 2189 | 2038 | -18 | 6  | 8 | 148 | 82   | 6   | 7 | 8 | 1    | 1    | -6  | 9  | 8 | 130 | 111  | 8   | 11 | 8 | 0     | 93    |
| 1   | 4 | 8 | 266  | 273  | -17 | 6  | 8 | 13  | 18   | 7   | 7 | 8 | 2233 | 2073 | -5  | 9  | 8 | 42  | 40   | -3  | 12 | 8 | 42    | 2     |
| 2   | 4 | 8 | 610  | 627  | -16 | 6  | 8 | 56  | 63   | 8   | 7 | 8 | 596  | 648  | -4  | 9  | 8 | 11  | 0    | -5  | 12 | 8 | 39    | 1     |
| 3   | 4 | 8 | 265  | 217  | -15 | 6  | 8 | 54  | 28   | 9   | 7 | 8 | 1882 | 1809 | -3  | 9  | 8 | 60  | 68   | -4  | 12 | 8 | 10    | 14    |
| 4   | 4 | 8 | 185  | 138  | -14 | 6  | 8 | 352 | 319  | 10  | 7 | 8 | 21   | 0    | -2  | 9  | 8 | 66  | 95   | -3  | 12 | 8 | 122   | 3     |
| 5   | 4 | 8 | 1182 | 1070 | -13 | 6  | 8 | 81  | 65   | 11  | 7 | 8 | 474  | 481  | -1  | 9  | 8 | 12  | 5    | -21 | 0  | 9 | 634   | 610   |
| 6   | 4 | 8 | 631  | 560  | -12 | 6  | 8 | 294 | 263  | 12  | 7 | 8 | 12   | 7    | 0   | 9  | 8 | 147 | 117  | -19 | 0  | 9 | 363   | 335   |
| 7   | 4 | 8 | 771  | 669  | -11 | 6  | 8 | 199 | 218  | 13  | 7 | 8 | 160  | 129  | 1   | 9  | 8 | 86  | 98   | -17 | 0  | 9 | 1125  | 1204  |
| 8   | 4 | 8 | 398  | 396  | -10 | 6  | 8 | 119 | 104  | 14  | 7 | 8 | 129  | 165  | 2   | 9  | 8 | 41  | 50   | -15 | 0  | 9 | 1127  | 1236  |
| 9   | 4 | 8 | 6    | 31   | -9  | 6  | 8 | 5   | 8    | 15  | 7 | 8 | 156  | 167  | 3   | 9  | 8 | 15  | 4    | -13 | 0  | 9 | 44    | 46    |
| 10  | 4 | 8 | 169  | 195  | -8  | 6  | 8 | 896 | 892  | 16  | 7 | 8 | 7    | 30   | 4   | 9  | 8 | 225 | 234  | -11 | 0  | 9 | 988   | 922   |
| 11  | 4 | 8 | 122  | 105  | -7  | 6  | 8 | 406 | 403  | 17  | 7 | 8 | -3   | 82   | 5   | 9  | 8 | 19  | 1    | -9  | 0  | 9 | 1360  | 1209  |
| 12  | 4 | 8 | 88   | 54   | -6  | 6  | 8 | 194 | 205  | 18  | 7 | 8 | 35   | 15   | 6   | 9  | 8 | 18  | 27   | -7  | 0  | 9 | 407   | 351   |
| 13  | 4 | 8 | 168  | 248  | -5  | 6  | 8 | 26  | 18   | 19  | 7 | 8 | 3    | 68   | 7   | 9  | 8 | 78  | 55   | -6  | 0  | 9 | 1436  | 1490  |
| 14  | 4 | 8 | 37   | 23   | -4  | 6  | 8 | 766 | 718  | -20 | 8 | 8 | -10  | 30   | 8   | 9  | 8 | 145 | 151  | -3  | 0  | 9 | 755   | 882   |
| 15  | 4 | 8 | 15   | 14   | -3  | 6  | 8 | 21  | 29   | -19 | 8 | 8 | 29   | 4    | 9   | 9  | 8 | 48  | 41   | -1  | 0  | 9 | 73    | 77    |
| 16  | 4 | 8 | 214  | 260  | -2  | 6  | 8 | 143 | 135  | -18 | 8 | 8 | 12   | 25   | 10  | 9  | 8 | 12  | 1    | 1   | 0  | 9 | 1969  | 2363  |
| 17  | 4 | 8 | 129  | 77   | -1  | 6  | 8 | 47  | 42   | -17 | 8 | 8 | 101  | 111  | 11  | 9  | 8 | 140 | 147  | 3   | 0  | 9 | 447   | 390   |
| 18  | 4 | 8 | 103  | 61   | 0   | 6  | 8 | 688 | 609  | -16 | 8 | 8 | -1   | 17   | 12  | 9  | 8 | 4   | 9    | 5   | 0  | 9 | 11563 | 10991 |
| 19  | 4 | 8 | 28   | 14   | 1   | 6  | 8 | 6   | 11   | -15 | 8 | 8 | 31   | 19   | 13  | 9  | 8 | 59  | 43   | 7   | 0  | 9 | 1248  | 1095  |
| 20  | 4 | 8 | -23  | 0    | 2   | 6  | 8 | 59  | 33   | -14 | 8 | 8 | -10  | 2    | 14  | 9  | 8 | 44  | 2    | 9   | 0  | 9 | 267   | 176   |
| -21 | 5 | 8 | 17   | 1    | 3   | 6  | 8 | 20  | 4    | -13 | 8 | 8 | 66   | 45   | 15  | 9  | 8 | 23  | 23   | 11  | 0  | 9 | 4     | 18    |
| -20 | 5 | 8 | 32   | 31   | 4   | 6  | 8 | 21  | 29   | -12 | 8 | 8 | 82   | 103  | 16  | 9  | 8 | 41  | 20   | 13  | 0  | 9 | 152   | 168   |
| -19 | 5 | 8 | 154  | 145  | 5   | 6  | 8 | 0   | 1    | -11 | 8 | 8 | 23   | 0    | -14 | 10 | 8 | -30 | 0    | 15  | 0  | 9 | 277   | 295   |
| -18 | 5 | 8 | 256  | 219  | 6   | 6  | 8 | 27  | 31   | -10 | 8 | 8 | 3    | 2    | -13 | 10 | 8 | 45  | 39   | 17  | 0  | 9 | 62    | 11    |
| -17 | 5 | 8 | 43   | 41   | 7   | 6  | 8 | 84  | 115  | -9  | 8 | 8 | 92   | 101  | -12 | 10 | 8 | 33  | 9    | 19  | 0  | 9 | 0     | 1     |
| -16 | 5 | 8 | 234  | 245  | 8   | 6  | 8 | 6   | 10   | -8  | 8 | 8 | 10   | 6    | -11 | 10 | 8 | 49  | 24   | -22 | 1  | 9 | 5     | 30    |
| -15 | 5 | 8 | 145  | 121  | 9   | 6  | 8 | 28  | 14   | -7  | 8 | 8 | 168  | 125  | -10 | 10 | 8 | -12 | 0    | -21 | 1  | 9 | 37    | 10    |
| -14 | 5 | 8 | 117  | 111  | 10  | 6  | 8 | 366 | 371  | -6  | 8 | 8 | 747  | 760  | -9  | 10 | 8 | 76  | 86   | -20 | 1  | 9 | 342   | 345   |
| -13 | 5 | 8 | 19   | 30   | 11  | 6  | 8 | 4   | 15   | -5  | 8 | 8 | 78   | 83   | -8  | 10 | 8 | 12  | 24   | -19 | 1  | 9 | 37    | 36    |
| -12 | 5 | 8 | 160  | 153  | 12  | 6  | 8 | 318 | 316  | -4  | 8 | 8 | 353  | 407  | -7  | 10 | 8 | 68  | 78   | -18 | 1  | 9 | 517   | 501   |
| -11 | 5 | 8 | 660  | 660  | 13  | 6  | 8 | 45  | 48   | -3  | 8 | 8 | 83   | 88   | -6  | 10 | 8 | 14  | 2    | -17 | 1  | 9 | 33    | 16    |
| -10 | 5 | 8 | 1964 | 1771 | 14  | 6  | 8 | 44  | 32   | -2  | 8 | 8 | 249  | 232  | -5  | 10 | 8 | 64  | 74   | -16 | 1  | 9 | 1163  | 1051  |
| -9  | 5 | 8 | 295  | 2928 | 15  | 6  | 8 | 13  | 3    | -1  | 8 | 8 | 489  | 543  | -4  | 10 | 8 | 80  | 65   | -15 | 1  | 9 | 16    | 6     |
| -8  | 5 | 8 | 323  | 323  | 16  | 6  | 8 | 44  | 35   | 0   | 8 | 8 | 104  | 102  | -3  | 10 | 8 | 11  | 22   | -14 | 1  | 9 | 5377  | 4859  |
| -7  | 5 | 8 | 868  | 793  | 17  | 6  | 8 | 22  | 5    | 1   | 8 | 8 | 58   | 62   | -2  | 10 | 8 | 79  | 76   | -13 | 1  | 9 | 671   | 646   |
| -6  | 5 | 8 | 459  | 463  | 18  | 6  | 8 | 3   | 3    | 2   | 8 | 8 | 143  | 153  | -1  | 10 | 8 | 42  | 19   | -12 | 1  | 9 | 422   | 470   |
| -5  | 5 | 8 | 652  | 608  | 19  | 6  | 8 | 31  | 47   | 3   | 8 | 8 | 15   | 0    | 0   | 10 | 8 | 2   | 5    | -11 | 1  | 9 | 392   | 359   |
| -4  | 5 | 8 | 1936 | 2064 | 20  | 6  | 8 | 569 | 18   | 4   | 8 | 8 | 153  | 173  | 1   | 10 | 8 | 34  | 16   | -10 | 1  | 9 | 773   | 888   |
| -3  | 5 | 8 | 2264 | 2351 | -21 | 7  | 8 | -10 | 1    | 5   | 8 | 8 | 751  | 767  | 2   | 10 | 8 | 117 | 82   | -9  | 1  | 9 | 218   | 245   |
| -2  | 5 | 8 | 1633 | 1716 | -20 | 7  | 8 | 3   | 9    | 6   | 8 | 8 | 462  | 510  | 3   | 10 | 8 | 70  | 63   | -8  | 1  | 9 | 1334  | 1745  |
| -1  | 5 | 8 | 506  | 513  | -19 | 7  | 8 | 79  | 23   | 7   | 8 | 8 | 6    | 9    | 4   | 10 | 8 | 9   | 18   | -7  | 1  | 9 | 2546  | 2412  |
| 0   | 5 | 8 | 925  | 905  | -18 | 7  | 8 | -7  | 11   | 8   | 8 | 8 | 49   | 37   | 5   | 10 | 8 | -1  | 1    | -6  | 1  | 9 | 17277 | 16450 |
| 1   | 5 | 8 | 467  | 466  | -17 | 7  | 8 | 11  | 4    | 9   | 8 | 8 | 70   | 88   | 6   | 10 | 8 | -2  | 2    | -5  | 1  | 9 | 90    | 58    |
| 2   | 5 | 8 | 1306 | 1282 | -16 | 7  | 8 | 21  | 31   | 10  | 8 | 8 | 7    | 1    | 7   | 10 | 8 | -4  | 3    | -4  | 1  | 9 | 1028  | 1179  |
| 3   | 5 | 8 | 306  | 327  | -15 | 7  | 8 | 164 | 152  | 11  | 8 | 8 | 37   | 45   | 8   | 10 | 8 | -2  | 0    | -3  | 1  | 9 | 34    | 46    |
| 4   | 5 | 8 | 1641 | 1662 | -14 | 7  | 8 | 26  | 5    | 12  | 8 | 8 | -6   | 9    | 9   | 10 | 8 | 7   | 18   | -2  | 1  | 9 | 7409  | 7816  |
| 5   | 5 | 8 | 1136 | 1233 | -13 | 7  | 8 | 273 | 280  | 13  | 8 | 8 | 17   | 16   | 10  | 10 | 8 | -7  | 0    | -1  | 1  | 9 | 1210  | 1201  |
| 6   | 5 | 8 | 1302 | 1395 | -12 | 7  | 8 | 30  | 3    | 14  | 8 | 8 | 8    | 12   | 11  | 10 | 8 | 34  | 0    | 0   | 1  | 9 | 4321  | 4566  |
| 7   | 5 | 8 | 257  | 236  | -11 | 7  | 8 | 592 | 570  | 15  | 8 | 8 | 14   | 31   | 12  | 10 | 8 | 1   | 1    | 1   | 1  | 9 | 517   | 493   |
| 8   | 5 | 8 | 411  | 395  | -10 | 7  | 8 | 232 | 251  | 16  | 8 | 8 | -7   | 0    | -8  | 11 | 8 | 70  | 60   | 2   | 1  | 9 | 17496 | 18801 |
| 9   | 5 | 8 | 108  | 128  | -9  | 7  | 8 | -4  | 2    | 17  | 8 | 8 | 49   | 43   | -7  | 11 | 8 | 32  | 20   | 3   | 1  | 9 | 95    | 91    |
| 10  | 5 | 8 | 315  | 273  | -8  | 7  | 8 | 539 | 547  | 18  | 8 | 8 | -5   | 3    | -6  | 11 | 8 | 87  | 9    | 4   | 1  | 9 | 11862 | 11979 |
| 11  | 5 | 8 | 1407 | 1442 | -7  | 7  | 8 | 97  | 78   | 19  | 8 | 8 | 39   | 37   | -5  | 11 | 8 | -11 | 17   | 5   | 1  | 9 | 443   | 522   |
| 12  | 5 | 8 | 1360 | 1244 | -6  | 7  | 8 | 143 | 124  | -18 | 9 | 8 | 138  | 0    | -4  | 11 | 8 | 110 | 4    | 6   | 1  | 9 | 29413 | 28642 |
| 13  | 5 | 8 | 410  | 410  | -5  | 7  | 8 | 318 | 333  | -17 | 9 | 8 | 20   | 14   | -3  | 11 | 8 | 0   | 15   | 7   | 1  | 9 | 1093  | 792   |
| 14  | 5 | 8 | 580  | 568  | -4  | 7  | 8 | 69  | 60   | -16 | 9 | 8 | 58   | 1    | -2  | 11 | 8 | 53  | 22   | 8   | 1  | 9 | 1617  | 1743  |
| 15  | 5 | 8 | 5    | 5    | -3  | 7  | 8 | 173 | 166  | -15 | 9 | 8 | 21   | 0    | -1  | 11 | 8 | 22  | 2    | 9   | 1  | 9 | 510   | 284   |
| 16  | 5 | 8 | 462  | 509  | -2  | 7  | 8 | 211 | 220  | -14 | 9 | 8 | -1   | 14   | 0   | 11 | 8 | 192 | 251  | 10  | 1  | 9 | 2508  | 2446  |
| 17  | 5 | 8 | 1    | 1    | -1  | 7  | 8 | 55  | 40   | -13 | 9 |   |      |      |     |    |   |     |      |     |    |   |       |       |

Table B.3, continued

| M   | K | L | Obs  | Calc | M   | K | L  | Obs   | Calc  | M   | K | L  | Obs   | Calc  | M   | K | L  | Obs   | Calc  |
|-----|---|---|------|------|-----|---|----|-------|-------|-----|---|----|-------|-------|-----|---|----|-------|-------|
| 1   | 2 | 9 | 135  | 169  | -19 | 4 | 9  | 84    | 55    | 5   | 5 | 9  | 2095  | 1934  | -12 | 7 | 9  | 358   | 355   |
| 2   | 2 | 9 | 266  | 254  | -18 | 4 | 9  | 427   | 464   | 6   | 5 | 9  | 671   | 635   | -11 | 7 | 9  | 8     | 15    |
| 3   | 2 | 9 | 558  | 527  | -17 | 4 | 9  | 61    | 25    | 7   | 5 | 9  | 1889  | 1964  | -10 | 7 | 9  | 642   | 662   |
| 4   | 2 | 9 | 426  | 417  | -16 | 4 | 9  | 34    | 26    | 8   | 5 | 9  | 95    | 96    | -9  | 7 | 9  | -5    | 6     |
| 5   | 2 | 9 | 97   | 86   | -15 | 4 | 9  | 260   | 281   | 9   | 5 | 9  | 70    | 24    | -8  | 7 | 9  | 157   | 145   |
| 6   | 2 | 9 | 943  | 872  | -14 | 4 | 9  | 1415  | 1343  | 10  | 5 | 9  | 88    | 113   | -7  | 7 | 9  | 226   | 296   |
| 7   | 2 | 9 | 2927 | 2512 | -13 | 4 | 9  | 471   | 432   | 11  | 5 | 9  | 625   | 525   | -6  | 7 | 9  | 1110  | 1097  |
| 8   | 2 | 9 | 1494 | 1291 | -12 | 4 | 9  | 474   | 495   | 12  | 5 | 9  | 482   | 444   | -5  | 7 | 9  | 37    | 42    |
| 9   | 2 | 9 | 17   | 20   | -11 | 4 | 9  | 23    | 7     | 13  | 5 | 9  | 254   | 242   | -4  | 7 | 9  | 101   | 100   |
| 10  | 2 | 9 | 67   | 84   | -10 | 4 | 9  | 444   | 423   | 14  | 5 | 9  | 74    | 46    | -3  | 7 | 9  | 934   | 976   |
| 11  | 2 | 9 | 66   | 67   | -9  | 4 | 9  | 14    | 16    | 15  | 5 | 9  | 126   | 131   | -2  | 7 | 9  | 461   | 425   |
| 12  | 2 | 9 | -4   | 5    | -8  | 4 | 9  | 5     | 7     | 16  | 5 | 9  | 5     | 13    | -1  | 7 | 9  | 690   | 694   |
| 13  | 2 | 9 | 79   | 79   | -7  | 4 | 9  | 420   | 340   | 17  | 5 | 9  | -14   | 19    | 0   | 7 | 9  | 247   | 237   |
| 14  | 2 | 9 | 430  | 487  | -6  | 4 | 9  | 34    | 14    | 18  | 5 | 9  | -10   | 22    | 2   | 7 | 9  | 222   | 213   |
| 15  | 2 | 9 | 39   | 15   | -5  | 4 | 9  | 62    | 51    | 19  | 5 | 9  | 44    | 49    | 28  | 3 | 7  | 144   | 122   |
| 16  | 2 | 9 | 184  | 107  | -4  | 4 | 9  | 1213  | 1075  | 20  | 5 | 9  | 49    | 28    | 4   | 7 | 9  | 14    | 22    |
| 17  | 2 | 9 | 16   | 8    | -3  | 4 | 9  | 4281  | 4327  | -21 | 6 | 9  | -10   | 62    | 19  | 5 | 7  | 532   | 561   |
| 18  | 2 | 9 | 233  | 208  | -2  | 4 | 9  | 1161  | 1286  | -20 | 6 | 9  | 62    | 19    | 5   | 7 | 9  | 5     | 3     |
| 19  | 2 | 9 | -7   | 3    | -1  | 4 | 9  | 203   | 216   | -19 | 6 | 9  | -14   | 4     | 6   | 7 | 9  | 10    | 18    |
| 20  | 2 | 9 | 30   | 12   | 0   | 4 | 9  | 29037 | 26408 | -18 | 6 | 9  | 21    | 0     | 7   | 7 | 9  | 60    | 73    |
| -22 | 3 | 9 | 306  | 50   | 1   | 4 | 9  | 2156  | 2264  | -17 | 6 | 9  | 184   | 184   | 8   | 7 | 9  | 16    | 10    |
| -21 | 3 | 9 | 217  | 205  | 2   | 4 | 9  | 1984  | 1742  | -16 | 6 | 9  | 24    | 0     | 9   | 7 | 9  | 196   | 198   |
| -20 | 3 | 9 | 43   | 3    | 3   | 4 | 9  | 139   | 93    | -15 | 6 | 9  | 70    | 59    | 10  | 7 | 9  | 92    | 92    |
| -19 | 3 | 9 | 489  | 437  | 4   | 4 | 9  | 10    | 1     | -14 | 6 | 9  | -12   | 753   | 11  | 7 | 9  | 11    | 3     |
| -18 | 3 | 9 | 73   | 52   | 5   | 4 | 9  | 303   | 273   | -13 | 6 | 9  | 670   | 101   | 13  | 7 | 9  | 99    | 126   |
| -17 | 3 | 9 | 958  | 977  | 6   | 4 | 9  | 148   | 138   | -12 | 6 | 9  | 85    | 130   | 14  | 7 | 9  | -17   | 5     |
| -16 | 3 | 9 | 265  | 283  | 7   | 4 | 9  | 140   | 111   | -11 | 6 | 9  | 120   | 130   | 15  | 7 | 9  | 28    | 9     |
| -15 | 3 | 9 | 46   | 23   | 8   | 4 | 9  | -3    | 8     | -10 | 6 | 9  | 139   | 140   | 16  | 7 | 9  | 47    | 27    |
| -14 | 3 | 9 | 169  | 186  | 9   | 4 | 9  | 162   | 158   | -9  | 6 | 9  | 134   | 189   | 17  | 7 | 9  | 32    | 4     |
| -13 | 3 | 9 | 1193 | 1123 | 10  | 4 | 9  | 215   | 235   | -8  | 6 | 9  | 182   | 2046  | 18  | 7 | 9  | 81    | 98    |
| -12 | 3 | 9 | 191  | 176  | 11  | 4 | 9  | 236   | 291   | -7  | 6 | 9  | 1867  | 47    | 19  | 7 | 9  | -19   | 3     |
| -11 | 3 | 9 | 2014 | 1955 | 12  | 4 | 9  | 412   | 424   | -6  | 6 | 9  | 66    | 359   | -20 | 8 | 9  | -49   | 0     |
| -10 | 3 | 9 | 5    | 1    | 13  | 4 | 9  | 80    | 41    | -5  | 6 | 9  | 382   | 53    | -19 | 8 | 9  | 24    | 52    |
| -9  | 3 | 9 | 1854 | 1820 | 14  | 4 | 9  | 66    | 24    | -4  | 6 | 9  | 80    | 6     | 14  | 3 | 10 | 1288  | 1373  |
| -8  | 3 | 9 | 13   | 0    | 2   | 0 | 10 | 6740  | 6764  | -9  | 2 | 10 | 21    | 14    | 15  | 3 | 10 | 12    | 1     |
| -7  | 3 | 9 | 15   | 42   | 4   | 0 | 10 | 1262  | 1074  | -8  | 2 | 10 | 13    | 884   | 16  | 3 | 10 | 11    | 37    |
| -6  | 3 | 9 | 38   | 25   | 6   | 0 | 10 | 293   | 298   | -7  | 2 | 10 | 969   | 358   | 17  | 3 | 10 | 124   | 129   |
| -5  | 3 | 9 | 23   | 3    | 8   | 0 | 10 | 377   | 339   | -6  | 2 | 10 | 391   | 136   | 18  | 3 | 10 | 74    | 156   |
| -4  | 3 | 9 | 65   | 0    | 10  | 0 | 10 | 4     | 3     | -5  | 2 | 10 | 164   | 1032  | 19  | 3 | 10 | 43    | 11    |
| -3  | 3 | 9 | 25   | 0    | 12  | 0 | 10 | 53    | 73    | -4  | 2 | 10 | 1112  | 1121  | 20  | 3 | 10 | 170   | 185   |
| -2  | 3 | 9 | 265  | 6    | 14  | 0 | 10 | 567   | 649   | -3  | 2 | 10 | 1212  | 3431  | -22 | 4 | 10 | -11   | 13    |
| -1  | 3 | 9 | 3    | 0    | 16  | 0 | 10 | 194   | 257   | -2  | 2 | 10 | 3688  | 719   | -21 | 4 | 10 | 120   | 51    |
| 0   | 3 | 9 | 59   | 1    | 18  | 0 | 10 | 49    | 17    | -1  | 2 | 10 | 778   | 1613  | -20 | 4 | 10 | 49    | 41    |
| 1   | 3 | 9 | -3   | 1    | 20  | 0 | 10 | 156   | 231   | 0   | 2 | 10 | 1740  | 3587  | -19 | 4 | 10 | 8     | 3     |
| 2   | 3 | 9 | -10  | 1    | -22 | 1 | 10 | 31    | 12    | 1   | 2 | 10 | 3674  | 974   | -18 | 4 | 10 | 46    | 55    |
| 3   | 3 | 9 | 10   | 0    | -21 | 1 | 10 | 151   | 194   | 2   | 2 | 10 | 1073  | 404   | -17 | 4 | 10 | 66    | 87    |
| 4   | 3 | 9 | 1    | 0    | -19 | 1 | 10 | 80    | 53    | 3   | 2 | 10 | 531   | 129   | -16 | 4 | 10 | 2     | 4     |
| 5   | 3 | 9 | 25   | 16   | -18 | 1 | 10 | 205   | 289   | 4   | 2 | 10 | 125   | 0     | -15 | 4 | 10 | 17    | 50    |
| 6   | 3 | 9 | 16   | 25   | -17 | 1 | 10 | 212   | 215   | 6   | 2 | 10 | 99    | 125   | -14 | 4 | 10 | 5     | 21    |
| 7   | 3 | 9 | -4   | 0    | -16 | 1 | 10 | 367   | 373   | 7   | 2 | 10 | 77    | 55    | -13 | 4 | 10 | 314   | 305   |
| 8   | 3 | 9 | 15   | 8    | -15 | 1 | 10 | 1110  | 1194  | 8   | 2 | 10 | 166   | 167   | -12 | 4 | 10 | 345   | 280   |
| 9   | 3 | 9 | 172  | 159  | -14 | 1 | 10 | 1362  | 1269  | 9   | 2 | 10 | 481   | 402   | -11 | 4 | 10 | 61    | 29    |
| 10  | 3 | 9 | 17   | 20   | -13 | 1 | 10 | 374   | 301   | 10  | 2 | 10 | -3    | 19    | -10 | 4 | 10 | 327   | 331   |
| 11  | 3 | 9 | 58   | 73   | -12 | 1 | 10 | 245   | 234   | 11  | 2 | 10 | 31    | 1     | -9  | 4 | 10 | 38    | 40    |
| 12  | 3 | 9 | 92   | 110  | -11 | 1 | 10 | 881   | 954   | 12  | 2 | 10 | 45    | 40    | -8  | 4 | 10 | 4     | 16    |
| 13  | 3 | 9 | 4    | 10   | -10 | 1 | 10 | 932   | 937   | 13  | 2 | 10 | 23    | 58    | -6  | 4 | 10 | 6     | 0     |
| 14  | 3 | 9 | 20   | 24   | -9  | 1 | 10 | 45    | 41    | 14  | 2 | 10 | 76    | 148   | -5  | 4 | 10 | 187   | 175   |
| 15  | 3 | 9 | 104  | 126  | -8  | 1 | 10 | 228   | 213   | 15  | 2 | 10 | 151   | 5     | -4  | 4 | 10 | 304   | 249   |
| 16  | 3 | 9 | 8    | 14   | -7  | 1 | 10 | 7374  | 7450  | 16  | 2 | 10 | -1    | 30    | -3  | 4 | 10 | 3672  | 3429  |
| 17  | 3 | 9 | 12   | 6    | -6  | 1 | 10 | 5079  | 5202  | 17  | 2 | 10 | 16    | 1     | -2  | 4 | 10 | 8322  | 7965  |
| 18  | 3 | 9 | 20   | 19   | -5  | 1 | 10 | 1805  | 2101  | 18  | 2 | 10 | -19   | 3     | -1  | 4 | 10 | 23338 | 22754 |
| 19  | 3 | 9 | 24   | 5    | -4  | 1 | 10 | 935   | 984   | 19  | 2 | 10 | -5    | 2     | 0   | 4 | 10 | 10788 | 10273 |
| 20  | 3 | 9 | 82   | 104  | -3  | 1 | 10 | 2379  | 2732  | 20  | 2 | 10 | -31   | 83    | 1   | 4 | 10 | 631   | 481   |
| 21  | 3 | 9 | 57   | 54   | -2  | 1 | 10 | 1565  | 1398  | -22 | 3 | 10 | 224   | 0     | 2   | 4 | 10 | 456   | 371   |
| 22  | 3 | 9 | 76   | 19   | -1  | 1 | 10 | 3504  | 3949  | -21 | 3 | 10 | 53    | 323   | 3   | 4 | 10 | 40    | 37    |
| 23  | 3 | 9 | -8   | 12   | 0   | 1 | 10 | 2398  | 2627  | -20 | 3 | 10 | 384   | 62    | 4   | 4 | 10 | 8     | 24    |
| 24  | 3 | 9 | -23  | 2    | 1   | 1 | 10 | 116   | 125   | -19 | 3 | 10 | 65    | 289   | 5   | 4 | 10 | 3     | 13    |
| 25  | 3 | 9 | 47   | 2    | 2   | 1 | 10 | 2402  | 2467  | -18 | 3 | 10 | 267   | 18    | 6   | 4 | 10 | 96    | 90    |
| 26  | 3 | 9 | 16   | 11   | 3   | 1 | 10 | 1608  | 1839  | -17 | 3 | 10 | 54    | 771   | 7   | 4 | 10 | 469   | 485   |
| 27  | 3 | 9 | 6    | 1    | 4   | 1 | 10 | 714   | 688   | -16 | 3 | 10 | 859   | 385   | 8   | 4 | 10 | 406   | 405   |
| 28  | 3 | 9 | 34   | 0    | 5   | 1 | 10 | 3290  | 2997  | -15 | 3 | 10 | 355   | 409   | 9   | 4 | 10 | 243   | 257   |
| 29  | 3 | 9 | -17  | 4    | 6   | 1 | 10 | 1955  | 1889  | -14 | 3 | 10 | 475   | 8     | 10  | 4 | 10 | 90    | 59    |
| 30  | 3 | 9 | -6   | 0    | 7   | 1 | 10 | 645   | 638   | -13 | 3 | 10 | 15    | 1470  | 11  | 4 | 10 | 188   | 222   |
| 31  | 3 | 9 | 11   | 0    | 8   | 1 | 10 | 2867  | 2910  | -12 | 3 | 10 | 1541  | 427   | 12  | 4 | 10 | 420   | 454   |
| 32  | 3 | 9 | 80   | 41   | 9   | 1 | 10 | 184   | 213   | -11 | 3 | 10 | 454   | 2643  | 13  | 4 | 10 | -4    | 0     |
| 33  | 3 | 9 | 47   | 52   | 10  | 1 | 10 | 1077  | 1005  | -10 | 3 | 10 | 2702  | 16    | 14  | 4 | 10 | 5     | 7     |
| 34  | 3 | 9 | 0    | 1    | 11  | 1 | 10 | 1494  | 1451  | -9  | 3 | 10 | 28    | 5124  | 15  | 4 | 10 | 421   | 415   |
| 35  | 3 | 9 | 38   | 0    | 12  | 1 | 10 | 296   | 231   | -8  | 3 | 10 | 5088  | 114   | 16  | 4 | 10 | 75    | 107   |
| 36  | 3 | 9 | -6   | 13   | 13  | 1 | 10 | 560   | 465   | -7  | 3 | 10 | 123   | 1496  | 17  | 4 | 10 | 38    | 17    |
| 37  | 3 | 9 | -17  | 4    | 14  | 1 | 10 | 24    | 2     | -6  | 3 | 10 | 1413  | 1064  | 18  | 4 | 10 | -2    | 2     |
| 38  | 3 | 9 | 15   | 4    | 15  | 1 | 10 | 1361  | 1402  | -5  | 3 | 10 | 916   | 10242 | 19  | 4 | 10 | 73    | 2     |
| 39  | 3 | 9 | -5   | 31   | 16  | 1 | 10 | 502   | 499   | -4  | 3 | 10 | 10259 | 12525 | 20  | 4 | 10 | 23    | 2     |
| 40  | 3 | 9 | 16   | 0    | 17  | 1 | 10 | 619   | 591   | -3  | 3 | 10 | 13687 | 6561  | -21 | 5 | 10 | -6    | 40    |
| 41  | 3 | 9 | -38  | 2    | 18  | 1 | 10 | 92    | 73    | -2  | 3 | 10 | 6231  | 3439  | -20 | 5 | 10 | 151   | 142   |
| 42  | 3 | 9 | -66  | 1    | 19  | 1 | 10 | 434   | 398   | -1  | 3 | 10 | 3461  | 7666  | -19 | 5 | 10 | 48    | 51    |
| 43  | 3 | 9 | 23   | 6    | 20  | 1 | 10 | -41   | 9     | 0   | 3 | 10 | 7601  | 100   | -18 | 5 | 10 | 111   | 83    |
| 44  | 3 |   |      |      |     |   |    |       |       |     |   |    |       |       |     |   |    |       |       |

Table B.3, continued

| M   | K | L  | Obs  | Calc | M   | K  | L  | Obs | Calc | M   | K  | L  | Obs  | Calc | M   | K  | L    | Obs  | Calc  | M   | K  | L  | Obs  | Calc |
|-----|---|----|------|------|-----|----|----|-----|------|-----|----|----|------|------|-----|----|------|------|-------|-----|----|----|------|------|
| -19 | 7 | 10 | 73   | 122  | 7   | 8  | 10 | 238 | 219  | 5   | 10 | 10 | 11   | 1    | -3  | 1  | 11   | 1872 | 1938  | -22 | 3  | 11 | -34  | 17   |
| -18 | 7 | 10 | 20   | 13   | 8   | 8  | 10 | 120 | 118  | 6   | 10 | 10 | 24   | 18   | -2  | 1  | 11   | 4384 | 4706  | -21 | 3  | 11 | 121  | 140  |
| -17 | 7 | 10 | 78   | 50   | 9   | 8  | 10 | 148 | 171  | 7   | 10 | 10 | 16   | 3    | -1  | 1  | 11   | 21   | 31    | -20 | 3  | 11 | 43   | 33   |
| -16 | 7 | 10 | -3   | 4    | 10  | 8  | 10 | 59  | 31   | 8   | 10 | 10 | 27   | 5    | 0   | 1  | 11   | 9668 | 10264 | -19 | 3  | 11 | 495  | 483  |
| -15 | 7 | 10 | 117  | 121  | 11  | 8  | 10 | 109 | 133  | 9   | 10 | 10 | 11   | 16   | 1   | 1  | 11   | 211  | 166   | -18 | 3  | 11 | 65   | 82   |
| -14 | 7 | 10 | 12   | 3    | 12  | 8  | 10 | 32  | 16   | 10  | 10 | 10 | 54   | 20   | 2   | 1  | 11   | 5066 | 5294  | -17 | 3  | 11 | 864  | 849  |
| -13 | 7 | 10 | 258  | 233  | 13  | 8  | 10 | 0   | 3    | 11  | 10 | 10 | 12   | 15   | 3   | 1  | 11   | 63   | 51    | -16 | 3  | 11 | 352  | 359  |
| -12 | 7 | 10 | 156  | 155  | 14  | 8  | 10 | 7   | 20   | 12  | 10 | 10 | -49  | 4    | 4   | 1  | 11   | 2419 | 2489  | -15 | 3  | 11 | 1547 | 1519 |
| -11 | 7 | 10 | 219  | 203  | 15  | 8  | 10 | 67  | 54   | -8  | 11 | 10 | -4   | 59   | 5   | 1  | 11   | 251  | 186   | -14 | 3  | 11 | 131  | 112  |
| -10 | 7 | 10 | 698  | 763  | 16  | 8  | 10 | -13 | 1    | -7  | 11 | 10 | -18  | 1    | 6   | 1  | 11   | 7131 | 7129  | -13 | 3  | 11 | 976  | 871  |
| -9  | 7 | 10 | 524  | 442  | 17  | 8  | 10 | 8   | 0    | -6  | 11 | 10 | 21   | 19   | 7   | 1  | 11   | 1479 | 1284  | -12 | 3  | 11 | 77   | 51   |
| -8  | 7 | 10 | 94   | 0    | 18  | 8  | 10 | 55  | 2    | -5  | 11 | 10 | 25   | 5    | 8   | 1  | 11   | 1514 | 1631  | -11 | 3  | 11 | 1149 | 1166 |
| -7  | 7 | 10 | 802  | 812  | -18 | 9  | 10 | 189 | 5    | -4  | 11 | 10 | 92   | 0    | 9   | 1  | 11   | 167  | 159   | -10 | 3  | 11 | 17   | 2    |
| -6  | 7 | 10 | 1194 | 1257 | -17 | 9  | 10 | -2  | 14   | -3  | 11 | 10 | 52   | 30   | 10  | 1  | 11   | 686  | 725   | -9  | 3  | 11 | 1127 | 1084 |
| -5  | 7 | 10 | 781  | 770  | -16 | 9  | 10 | 36  | 1    | -2  | 11 | 10 | 67   | 32   | 11  | 1  | 11   | 75   | 67    | -8  | 3  | 11 | 85   | 59   |
| -4  | 7 | 10 | 24   | 32   | -15 | 9  | 10 | 137 | 118  | -1  | 11 | 10 | 42   | 18   | 12  | 1  | 11   | 1146 | 1180  | -7  | 3  | 11 | 2020 | 2050 |
| -3  | 7 | 10 | 2765 | 2593 | -14 | 9  | 10 | 141 | 58   | 0   | 11 | 10 | 119  | 83   | 13  | 1  | 11   | 27   | 12    | -6  | 3  | 11 | 1180 | 1092 |
| -2  | 7 | 10 | 60   | 35   | -13 | 9  | 10 | 44  | 47   | 1   | 11 | 10 | 84   | 5    | 14  | 1  | 11   | 263  | 236   | -5  | 3  | 11 | 698  | 847  |
| -1  | 7 | 10 | 4611 | 4579 | -12 | 9  | 10 | 46  | 58   | 2   | 11 | 10 | 30   | 0    | 15  | 1  | 11   | -9   | 1     | -4  | 3  | 11 | 947  | 918  |
| 0   | 7 | 10 | 466  | 466  | -11 | 9  | 10 | 37  | 36   | 3   | 11 | 10 | 33   | 39   | 16  | 1  | 11   | 819  | 836   | -3  | 3  | 11 | 513  | 526  |
| 1   | 7 | 10 | 3060 | 2963 | -10 | 9  | 10 | 34  | 19   | 4   | 11 | 10 | 75   | 66   | 17  | 1  | 11   | 134  | 135   | -2  | 3  | 11 | 3987 | 3869 |
| 2   | 7 | 10 | 496  | 490  | -9  | 9  | 10 | 12  | 8    | 5   | 11 | 10 | 21   | 4    | 18  | 1  | 11   | 225  | 179   | -1  | 3  | 11 | 565  | 741  |
| 3   | 7 | 10 | 1527 | 1478 | -8  | 9  | 10 | 10  | 24   | 6   | 11 | 10 | -17  | 9    | 19  | 1  | 11   | 42   | 28    | 0   | 3  | 11 | 119  | 114  |
| 4   | 7 | 10 | 198  | 192  | -7  | 9  | 10 | 53  | 40   | 7   | 11 | 10 | -34  | 0    | 20  | 1  | 11   | -55  | 56    | 1   | 3  | 11 | 55   | 81   |
| 5   | 7 | 10 | 447  | 550  | -6  | 9  | 10 | 5   | 2    | -5  | 12 | 10 | 122  | 3    | -21 | 2  | 11   | 19   | 33    | 2   | 3  | 11 | 124  | 190  |
| 6   | 7 | 10 | 184  | 165  | -5  | 9  | 10 | 300 | 294  | -4  | 12 | 10 | 84   | 21   | -20 | 2  | 11   | 242  | 238   | 3   | 3  | 11 | 685  | 779  |
| 7   | 7 | 10 | 1492 | 1439 | -4  | 9  | 10 | 0   | 1    | -21 | 0  | 11 | 322  | 255  | -19 | 2  | 11   | -17  | 1     | 4   | 3  | 11 | 1152 | 1096 |
| 8   | 7 | 10 | 55   | 26   | -3  | 9  | 10 | 173 | 183  | -19 | 0  | 11 | 110  | 74   | -18 | 2  | 11   | 170  | 156   | 5   | 3  | 11 | 2026 | 1935 |
| 9   | 7 | 10 | 190  | 208  | -2  | 9  | 10 | 4   | 10   | -17 | 0  | 11 | 468  | 370  | -17 | 2  | 11   | 88   | 61    | 6   | 3  | 11 | 14   | 1    |
| 10  | 7 | 10 | 441  | 446  | -1  | 9  | 10 | 27  | 24   | -15 | 0  | 11 | 23   | 9    | -16 | 2  | 11   | 48   | 52    | 7   | 3  | 11 | 856  | 863  |
| 11  | 7 | 10 | 638  | 658  | 0   | 9  | 10 | -4  | 0    | -13 | 0  | 11 | 225  | 217  | -15 | 2  | 11   | 42   | 21    | 8   | 3  | 11 | 53   | 40   |
| 12  | 7 | 10 | 112  | 112  | 1   | 9  | 10 | 499 | 530  | -11 | 0  | 11 | 8    | 20   | -14 | 2  | 11   | 244  | 230   | 9   | 3  | 11 | 917  | 924  |
| 13  | 7 | 10 | 12   | 3    | 2   | 9  | 10 | 55  | 59   | -9  | 0  | 11 | 879  | 886  | -13 | 2  | 11   | 6    | 1     | 10  | 3  | 11 | 519  | 568  |
| 14  | 7 | 10 | 66   | 61   | 3   | 9  | 10 | 196 | 170  | -7  | 0  | 11 | 1600 | 1526 | -12 | 2  | 11   | 72   | 43    | 11  | 3  | 11 | 70   | 32   |
| 15  | 7 | 10 | 66   | 80   | 4   | 9  | 10 | 52  | 48   | -5  | 0  | 11 | 4019 | 3435 | -11 | 2  | 11   | 23   | 14    | 12  | 3  | 11 | 39   | 17   |
| 16  | 7 | 10 | 17   | 21   | 5   | 9  | 10 | 24  | 29   | -3  | 0  | 11 | 766  | 797  | -10 | 2  | 11   | 9    | 5     | 13  | 3  | 11 | 1654 | 1545 |
| 17  | 7 | 10 | 8    | 9    | 6   | 9  | 10 | 21  | 14   | -1  | 0  | 11 | 96   | 72   | -9  | 2  | 11   | 727  | 628   | 14  | 3  | 11 | 42   | 68   |
| 18  | 7 | 10 | -9   | 16   | 7   | 9  | 10 | 122 | 99   | 1   | 0  | 11 | 1381 | 1303 | -8  | 2  | 11   | 169  | 136   | 15  | 3  | 11 | 126  | 141  |
| 19  | 7 | 10 | -14  | 146  | 8   | 9  | 10 | -8  | 0    | 3   | 0  | 11 | 2531 | 2518 | -7  | 2  | 11   | 91   | 113   | 16  | 3  | 11 | 228  | 210  |
| -20 | 8 | 10 | 23   | 19   | 9   | 9  | 10 | 173 | 176  | 5   | 0  | 11 | 3507 | 3487 | -6  | 2  | 11   | 27   | 18    | 17  | 3  | 11 | 75   | 112  |
| -19 | 8 | 10 | 33   | 31   | 10  | 9  | 10 | 17  | 17   | 7   | 0  | 11 | 6036 | 5748 | -5  | 2  | 11   | 246  | 259   | 18  | 3  | 11 | 53   | 99   |
| -18 | 8 | 10 | 28   | 81   | 11  | 9  | 10 | 41  | 12   | 9   | 0  | 11 | -18  | 4    | -4  | 2  | 11   | 1763 | 1568  | 19  | 3  | 11 | 45   | 59   |
| -17 | 8 | 10 | 65   | 52   | 12  | 9  | 10 | 38  | 2    | 11  | 0  | 11 | 20   | 18   | -3  | 2  | 11   | 2524 | 2407  | -21 | 4  | 11 | 13   | 11   |
| -16 | 8 | 10 | 53   | 5    | 13  | 9  | 10 | 59  | 37   | 13  | 0  | 11 | -2   | 27   | -2  | 2  | 11   | 493  | 482   | -20 | 4  | 11 | -12  | 5    |
| -15 | 8 | 10 | 3    | 16   | 14  | 9  | 10 | 39  | 9    | 15  | 0  | 11 | 196  | 273  | -1  | 2  | 11   | 807  | 833   | -19 | 4  | 11 | 31   | 20   |
| -14 | 8 | 10 | 17   | 16   | 15  | 9  | 10 | 116 | 4    | 17  | 0  | 11 | 48   | 3    | 0   | 2  | 11   | 163  | 89    | -18 | 4  | 11 | -1   | 39   |
| -13 | 8 | 10 | 96   | 54   | 16  | 9  | 10 | 116 | 1    | -22 | 1  | 11 | 131  | 73   | 1   | 2  | 11   | 4547 | 3903  | -17 | 4  | 11 | 38   | 18   |
| -12 | 8 | 10 | 43   | 5    | -14 | 10 | 10 | 257 | 1    | -22 | 1  | 11 | 28   | 166  | 2   | 2  | 11   | 4442 | 3664  | -16 | 4  | 11 | 32   | 30   |
| -11 | 8 | 10 | 36   | 21   | -13 | 10 | 10 | -3  | 7    | -21 | 1  | 11 | 436  | 32   | 2   | 11 | 3328 | 2920 | -15   | 4   | 11 | 2  | 20   |      |
| -10 | 8 | 10 | 105  | 80   | -12 | 10 | 10 | 36  | 0    | -20 | 1  | 11 | 436  | 524  | 4   | 2  | 11   | 469  | 398   | -14 | 4  | 11 | 273  | 291  |
| -9  | 8 | 10 | 42   | 55   | -11 | 10 | 10 | 32  | 22   | -19 | 1  | 11 | 94   | 94   | 5   | 2  | 11   | 387  | 429   | -13 | 4  | 11 | 142  | 84   |
| -8  | 8 | 10 | 47   | 35   | -10 | 10 | 10 | -8  | 0    | -18 | 1  | 11 | 292  | 284  | 6   | 2  | 11   | 294  | 271   | -12 | 4  | 11 | 167  | 204  |
| -7  | 8 | 10 | 474  | 439  | -9  | 10 | 10 | 32  | 12   | -17 | 1  | 11 | 811  | 804  | 7   | 2  | 11   | 18   | 27    | -11 | 4  | 11 | 12   | 12   |
| -6  | 8 | 10 | 260  | 257  | -8  | 10 | 10 | 20  | 7    | -16 | 1  | 11 | 792  | 770  | 8   | 2  | 11   | 733  | 652   | -10 | 4  | 11 | 102  | 92   |
| -5  | 8 | 10 | 612  | 617  | -7  | 10 | 10 | 0   | 5    | -15 | 1  | 11 | 520  | 497  | 9   | 2  | 11   | 127  | 141   | -9  | 4  | 11 | 293  | 265  |
| -4  | 8 | 10 | 0    | 12   | -6  | 10 | 10 | 20  | 32   | -14 | 1  | 11 | 3050 | 2997 | 10  | 2  | 11   | 242  | 217   | -8  | 4  | 11 | 90   | 68   |
| -3  | 8 | 10 | 19   | 7    | -5  | 10 | 10 | 8   | 5    | -13 | 1  | 11 | 1600 | 1491 | 11  | 2  | 11   | 76   | 88    | -7  | 4  | 11 | 37   | 21   |
| -2  | 8 | 10 | 5    | 5    | -4  | 10 | 10 | 6   | 2    | -12 | 1  | 11 | 1820 | 1776 | 12  | 2  | 11   | 251  | 275   | -6  | 4  | 11 | 326  | 305  |
| -1  | 8 | 10 | 154  | 161  | -3  | 10 | 10 | 34  | 22   | -11 | 1  | 11 | 679  | 679  | 13  | 2  | 11   | 3    | 7     | -5  | 4  | 11 | 26   | 30   |
| 0   | 8 | 10 | 372  | 362  | -2  | 10 | 10 | -5  | 1    | -10 | 1  | 11 | 1923 | 1855 | 14  | 2  | 11   | 358  | 327   | -4  | 4  | 11 | 279  | 324  |
| 1   | 8 | 10 | 10   | 7    | -1  | 10 | 10 | 36  | 35   | -9  | 1  | 11 | 76   | 84   | 15  | 2  | 11   | 6    | 17    | 3   | 4  | 11 | 783  | 832  |
| 2   | 8 | 10 | 157  | 151  | 0   | 10 | 10 | 1   | 2    | -8  | 1  | 11 | 3723 | 3733 | 16  | 2  | 11   | 124  | 107   | -2  | 4  | 11 | 1202 | 1241 |
| 3   | 8 | 10 | 0    | 0    | 1   | 10 | 10 | 34  | 4    | -7  | 1  | 11 | 4962 | 4779 | 17  | 2  | 11   | 6    | 7     | -1  | 4  | 11 | 1627 | 1300 |
| 4   | 8 | 10 | 545  | 506  | -17 | 6  | 11 | 55  | 56   | 8   | 7  | 11 | 989  | 964  | -1  | 9  | 11   | 34   | 19    | -8  | 0  | 12 | 3644 | 3529 |
| 1   | 4 | 11 | 3073 | 2751 | -16 | 6  | 11 | 28  | 41   | 9   | 7  | 11 | 19   | 1    | 0   | 9  | 11   | 41   | 38    | -6  | 0  | 12 | 1859 | 1462 |
| 2   | 4 | 11 | 788  | 797  | -15 | 6  | 11 | 55  | 23   | 10  | 7  | 11 | 197  | 186  | 1   | 9  | 11   | 95   | 83    | -4  | 0  | 12 | 902  | 1000 |
| 3   | 4 | 11 | 242  | 244  | -14 | 6  | 11 | 131 | 147  | 11  | 7  | 11 | 117  | 116  | 2   | 9  | 11   | 44   | 33    | -2  | 0  | 12 | 284  | 303  |
| 4   | 4 | 11 | 5    | 7    | -13 | 6  | 11 | 624 | 652  | 12  | 7  | 11 | 410  | 413  | 3   | 9  | 11   | 20   | 33    | 0   | 0  | 12 | 2100 | 2126 |
| 5   | 4 | 11 | 318  | 326  | -12 | 6  | 11 | 9   | 0</  |     |    |    |      |      |     |    |      |      |       |     |    |    |      |      |

Table B.3, continued

| M   | K | L  | Obe  | Calc | M   | K | L  | Obe  | Calc | M   | K | L  | Obe  | Calc | M   | K  | L  | Obe  | Calc | M   | K | L  | Obe   | Calc  |
|-----|---|----|------|------|-----|---|----|------|------|-----|---|----|------|------|-----|----|----|------|------|-----|---|----|-------|-------|
| -1  | 5 | 11 | 3969 | 3817 | -10 | 7 | 11 | 111  | 94   | 10  | 8 | 11 | 143  | 120  | 8   | 10 | 11 | 10   | 26   | 4   | 1 | 12 | 113   | 113   |
| 0   | 5 | 11 | 733  | 677  | -17 | 7 | 11 | 0    | 12   | 11  | 8 | 11 | 21   | 6    | 9   | 10 | 11 | 33   | 33   | 5   | 1 | 12 | 10869 | 10801 |
| 1   | 5 | 11 | 1910 | 2132 | -16 | 7 | 11 | 79   | 78   | 12  | 8 | 11 | 21   | 28   | 10  | 10 | 11 | 10   | 0    | 6   | 1 | 12 | 1309  | 1314  |
| 2   | 5 | 11 | 729  | 759  | -15 | 7 | 11 | 47   | 24   | 13  | 8 | 11 | 18   | 17   | 11  | 10 | 11 | -20  | 4    | 7   | 1 | 12 | 3675  | 3611  |
| 3   | 5 | 11 | 107  | 206  | -14 | 7 | 11 | 36   | 53   | 14  | 8 | 11 | 62   | 39   | -7  | 11 | 11 | 72   | 69   | 8   | 1 | 12 | 382   | 334   |
| 4   | 5 | 11 | -4   | 1    | -13 | 7 | 11 | 10   | 1    | 15  | 8 | 11 | 24   | 21   | -6  | 11 | 11 | 31   | 30   | 9   | 1 | 12 | 2899  | 2854  |
| 5   | 5 | 11 | 59   | 65   | -12 | 7 | 11 | 181  | 146  | 16  | 8 | 11 | 6    | 0    | -5  | 11 | 11 | 36   | 0    | 10  | 1 | 12 | 0     | 2     |
| 6   | 5 | 11 | 28   | 35   | -12 | 7 | 11 | 102  | 118  | 17  | 8 | 11 | 17   | 0    | -4  | 11 | 11 | 23   | 1    | 11  | 1 | 12 | 440   | 325   |
| 7   | 5 | 11 | 1659 | 1617 | -10 | 7 | 11 | 335  | 262  | 18  | 8 | 11 | 189  | 8    | -3  | 11 | 11 | 15   | 1    | 12  | 1 | 12 | 72    | 75    |
| 8   | 5 | 11 | 499  | 501  | -9  | 7 | 11 | 16   | 13   | -10 | 9 | 11 | 160  | 38   | -2  | 11 | 11 | 17   | 3    | 13  | 1 | 12 | 98    | 106   |
| 9   | 5 | 11 | 48   | 55   | -8  | 7 | 11 | 11   | 22   | -17 | 9 | 11 | 21   | 10   | -1  | 11 | 11 | -3   | 66   | 14  | 1 | 12 | 50    | 59    |
| 10  | 5 | 11 | 783  | 764  | -7  | 7 | 11 | 413  | 396  | -16 | 9 | 11 | 5    | 1    | 0   | 11 | 11 | -6   | 9    | 15  | 1 | 12 | 419   | 396   |
| 11  | 5 | 11 | 328  | 325  | -6  | 7 | 11 | 335  | 359  | -15 | 9 | 11 | -27  | 9    | 1   | 11 | 11 | 29   | 88   | 16  | 1 | 12 | 89    | 23    |
| 12  | 5 | 11 | 60   | 66   | -5  | 7 | 11 | 6    | 19   | -14 | 9 | 11 | 7    | 24   | 2   | 11 | 11 | 12   | 0    | 17  | 1 | 12 | 147   | 192   |
| 13  | 5 | 11 | 584  | 585  | -4  | 7 | 11 | 761  | 767  | -13 | 9 | 11 | 39   | 25   | 3   | 11 | 11 | 26   | 0    | 19  | 1 | 12 | 59    | 26    |
| 14  | 5 | 11 | 286  | 348  | -3  | 7 | 11 | 97   | 112  | -12 | 9 | 11 | -1   | 17   | 4   | 11 | 11 | -4   | 0    | 19  | 1 | 12 | 201   | 167   |
| 15  | 5 | 11 | 60   | 81   | -2  | 7 | 11 | 17   | 14   | -11 | 9 | 11 | 135  | 130  | 8   | 11 | 11 | -4   | 17   | -23 | 2 | 12 | -28   | 1     |
| 16  | 5 | 11 | 0    | 0    | -1  | 7 | 11 | 137  | 150  | -10 | 9 | 11 | 62   | 50   | 6   | 11 | 11 | -27  | 3    | -20 | 2 | 12 | 11    | 8     |
| 17  | 5 | 11 | 161  | 151  | 0   | 7 | 11 | 30   | 23   | -9  | 9 | 11 | 139  | 144  | 7   | 11 | 11 | 35   | 11   | -19 | 2 | 12 | 126   | 110   |
| 18  | 5 | 11 | 26   | 6    | 1   | 7 | 11 | 48   | 32   | -8  | 9 | 11 | 18   | 15   | -22 | 0  | 12 | -4   | 1    | -10 | 2 | 12 | 80    | 97    |
| 19  | 5 | 11 | 51   | 136  | 2   | 7 | 11 | 12   | 2    | -7  | 9 | 11 | 15   | 14   | -20 | 0  | 12 | 133  | 132  | -17 | 2 | 12 | 89    | 71    |
| 20  | 5 | 11 | 77   | 24   | 3   | 7 | 11 | 58   | 58   | -6  | 9 | 11 | 286  | 267  | -18 | 0  | 12 | 146  | 153  | -16 | 2 | 12 | 267   | 262   |
| -21 | 6 | 11 | 40   | 45   | 4   | 7 | 11 | 70   | 48   | -5  | 9 | 11 | 258  | 235  | -16 | 0  | 12 | 232  | 142  | -15 | 2 | 12 | 168   | 194   |
| -20 | 6 | 11 | 40   | 21   | 5   | 7 | 11 | 115  | 122  | -4  | 9 | 11 | 74   | 63   | -14 | 0  | 12 | 69   | 88   | -14 | 2 | 12 | 237   | 204   |
| -19 | 6 | 11 | 53   | 48   | 6   | 7 | 11 | 489  | 513  | -3  | 9 | 11 | 45   | 45   | -12 | 0  | 12 | 6    | 18   | -13 | 2 | 12 | 381   | 370   |
| -18 | 6 | 11 | 38   | 0    | 7   | 7 | 11 | 228  | 196  | -2  | 9 | 11 | 8    | 1    | -10 | 0  | 12 | 406  | 374  | -12 | 2 | 12 | 32    | 5     |
| -17 | 2 | 12 | 29   | 20   | 14  | 3 | 12 | 403  | 442  | -4  | 5 | 12 | 1208 | 1193 | -20 | 7  | 12 | 8    | 11   | 8   | 0 | 12 | 4     | 2     |
| -16 | 2 | 12 | 33   | 18   | 15  | 3 | 12 | 196  | 180  | -3  | 5 | 12 | 166  | 159  | -19 | 7  | 12 | 127  | 115  | 9   | 0 | 12 | 132   | 84    |
| -9  | 2 | 12 | 229  | 202  | 16  | 3 | 12 | 261  | 175  | -2  | 5 | 12 | 4056 | 6094 | -18 | 7  | 12 | 37   | 18   | 10  | 9 | 12 | 17    | 8     |
| -8  | 2 | 12 | 551  | 466  | 17  | 3 | 12 | 77   | 44   | -1  | 5 | 12 | 2439 | 2366 | -17 | 7  | 12 | 209  | 211  | 11  | 8 | 12 | 76    | 100   |
| -7  | 2 | 12 | 901  | 797  | 18  | 3 | 12 | 53   | 47   | 0   | 5 | 12 | 3630 | 3637 | -16 | 7  | 12 | 25   | 24   | 12  | 8 | 12 | 302   | 347   |
| -6  | 2 | 12 | 686  | 642  | 19  | 3 | 12 | -10  | 26   | 1   | 5 | 12 | 2655 | 2699 | -15 | 7  | 12 | 203  | 205  | 13  | 8 | 12 | 56    | 35    |
| -5  | 2 | 12 | 182  | 201  | -21 | 4 | 12 | 32   | 14   | 2   | 5 | 12 | 600  | 549  | -14 | 7  | 12 | 225  | 240  | 14  | 8 | 12 | 37    | 25    |
| -4  | 2 | 12 | 997  | 1080 | -20 | 4 | 12 | 60   | 26   | 3   | 5 | 12 | 294  | 274  | -13 | 7  | 12 | 432  | 414  | 15  | 8 | 12 | -8    | 2     |
| -3  | 2 | 12 | 1017 | 945  | -19 | 4 | 12 | 24   | 20   | 4   | 5 | 12 | 1156 | 1169 | -12 | 7  | 12 | 252  | 242  | 16  | 8 | 12 | 21    | 0     |
| -2  | 2 | 12 | 3502 | 2987 | -18 | 4 | 12 | 70   | 61   | 5   | 5 | 12 | 828  | 845  | -11 | 7  | 12 | 708  | 762  | 17  | 8 | 12 | -6    | 14    |
| -1  | 2 | 12 | 5334 | 4542 | -17 | 4 | 12 | 9    | 0    | 6   | 5 | 12 | 1223 | 1308 | -10 | 7  | 12 | 379  | 372  | 18  | 8 | 12 | 32    | 1     |
| 0   | 2 | 12 | 324  | 249  | -16 | 4 | 12 | -10  | 3    | 7   | 5 | 12 | 135  | 143  | -9  | 7  | 12 | 1125 | 1033 | -10 | 9 | 12 | 30    | 3     |
| 1   | 2 | 12 | 64   | 31   | -15 | 4 | 12 | 26   | 18   | 8   | 5 | 12 | 1182 | 1066 | -8  | 7  | 12 | 55   | 55   | -17 | 9 | 12 | -13   | 0     |
| 2   | 2 | 12 | 127  | 165  | -14 | 4 | 12 | 22   | 30   | 9   | 5 | 12 | 18   | 27   | -7  | 7  | 12 | 646  | 668  | -16 | 9 | 12 | 6     | 5     |
| 3   | 2 | 12 | 853  | 928  | -13 | 4 | 12 | 189  | 200  | 10  | 5 | 12 | 478  | 399  | -6  | 7  | 12 | 335  | 342  | -15 | 9 | 12 | 33    | 3     |
| 4   | 2 | 12 | 1407 | 1397 | -12 | 4 | 12 | 32   | 1    | 11  | 5 | 12 | 36   | 66   | -5  | 7  | 12 | 550  | 510  | -14 | 9 | 12 | 31    | 3     |
| 5   | 2 | 12 | 44   | 81   | -11 | 4 | 12 | 15   | 9    | 12  | 5 | 12 | 424  | 416  | -4  | 7  | 12 | 130  | 160  | -13 | 9 | 12 | 21    | 0     |
| 6   | 2 | 12 | 151  | 152  | -10 | 4 | 12 | 21   | 13   | 13  | 5 | 12 | 100  | 68   | -3  | 7  | 12 | 96   | 63   | -12 | 9 | 12 | 12    | 1     |
| 7   | 2 | 12 | 28   | 31   | -9  | 4 | 12 | 487  | 457  | 14  | 5 | 12 | 147  | 236  | -2  | 7  | 12 | 161  | 161  | -11 | 9 | 12 | -4    | 1     |
| 8   | 2 | 12 | 554  | 533  | -8  | 4 | 12 | 67   | 75   | 15  | 5 | 12 | 21   | 32   | -1  | 7  | 12 | 81   | 71   | -10 | 9 | 12 | 19    | 12    |
| 9   | 2 | 12 | 119  | 88   | -7  | 4 | 12 | 114  | 105  | 16  | 5 | 12 | 49   | 1    | 0   | 7  | 12 | 60   | 46   | -9  | 9 | 12 | 31    | 38    |
| 10  | 2 | 12 | 136  | 156  | -6  | 4 | 12 | 171  | 196  | 17  | 5 | 12 | 66   | 12   | 1   | 7  | 12 | 62   | 45   | -8  | 9 | 12 | 39    | 26    |
| 11  | 2 | 12 | 61   | 55   | -5  | 4 | 12 | 1052 | 987  | 18  | 5 | 12 | 72   | 59   | 2   | 7  | 12 | -3   | 17   | -7  | 9 | 12 | 28    | 18    |
| 12  | 2 | 12 | 192  | 191  | -4  | 4 | 12 | 346  | 354  | 19  | 5 | 12 | -13  | 40   | 3   | 7  | 12 | 75   | 63   | -6  | 9 | 12 | 30    | 28    |
| 13  | 2 | 12 | -20  | 9    | -3  | 4 | 12 | 1101 | 997  | 20  | 5 | 12 | -13  | 38   | 4   | 7  | 12 | -9   | 89   | -4  | 9 | 12 | 140   | 125   |
| 14  | 2 | 12 | 21   | 30   | -2  | 4 | 12 | 2541 | 2303 | -21 | 6 | 12 | 18   | 9    | 5   | 7  | 12 | 88   | 89   | -4  | 9 | 12 | 16    | 5     |
| 15  | 2 | 12 | 227  | 209  | -1  | 4 | 12 | 28   | 37   | -20 | 6 | 12 | 26   | 5    | 6   | 7  | 12 | 22   | 20   | -3  | 9 | 12 | 29    | 29    |
| 16  | 2 | 12 | 24   | 28   | 0   | 4 | 12 | 41   | 36   | -19 | 6 | 12 | 73   | 14   | 7   | 7  | 12 | 103  | 159  | -2  | 9 | 12 | 149   | 138   |
| 17  | 2 | 12 | 81   | 84   | 1   | 4 | 12 | 1939 | 1860 | -18 | 6 | 12 | -1   | 1    | 8   | 7  | 12 | 71   | 61   | -1  | 9 | 12 | 83    | 74    |
| 18  | 2 | 12 | 59   | 57   | 2   | 4 | 12 | 182  | 151  | -17 | 6 | 12 | 13   | 3    | 9   | 7  | 12 | 70   | 58   | 0   | 9 | 12 | 31    | 25    |
| 19  | 2 | 12 | -36  | 10   | 3   | 4 | 12 | 143  | 144  | -16 | 6 | 12 | 184  | 145  | 10  | 7  | 12 | 123  | 126  | 1   | 9 | 12 | 78    | 58    |
| -21 | 3 | 12 | -1   | 4    | 4   | 4 | 12 | 309  | 256  | -15 | 6 | 12 | 38   | 19   | 11  | 7  | 12 | 223  | 239  | 2   | 9 | 12 | -1    | 2     |
| -20 | 3 | 12 | 523  | 568  | 5   | 4 | 12 | 419  | 473  | -14 | 6 | 12 | 109  | 122  | 12  | 7  | 12 | 34   | 18   | 3   | 9 | 12 | 138   | 127   |
| -19 | 3 | 12 | 26   | 25   | 6   | 4 | 12 | 17   | 9    | -13 | 6 | 12 | 17   | 6    | 13  | 7  | 12 | -6   | 4    | 4   | 9 | 12 | 21    | 31    |
| -18 | 3 | 12 | 514  | 490  | 7   | 4 | 12 | 179  | 142  | -12 | 6 | 12 | 118  | 150  | 14  | 7  | 12 | 15   | 3    | 5   | 9 | 12 | 28    | 9     |
| -17 | 3 | 12 | 70   | 112  | 8   | 4 | 12 | 408  | 471  | -11 | 6 | 12 | 593  | 581  | 15  | 7  | 12 | 0    | 1    | 6   | 9 | 12 | 4     | 12    |
| -16 | 3 | 12 | 621  | 675  | 9   | 4 | 12 | 373  | 359  | -10 | 6 | 12 | 28   | 37   | 16  | 7  | 12 | 18   | 9    | 7   | 9 | 12 | 110   | 132   |
| -15 | 3 | 12 | 815  | 839  | 10  | 4 | 12 | 41   | 41   | -9  | 6 | 12 | 848  | 896  | 17  | 7  | 12 | 43   | 11   | 8   | 9 | 12 | 186   | 208   |
| -14 | 3 | 12 | 2560 | 2382 | 11  | 4 | 12 | -10  | 24   | -8  | 6 | 12 | 593  | 470  | 18  | 7  | 12 | -4   | 24   | 9   | 9 | 12 | 18    | 3     |
| -13 | 3 | 12 | -5   | 6    | 12  | 4 | 12 | 39   | 28   | -7  | 6 | 12 | 587  | 555  | -19 | 8  | 12 | 51   | 19   | 10  | 9 | 12 | 5     | 1     |
| -12 | 3 | 12 | 1381 | 1361 | 13  | 4 | 12 | 22   | 31   | -6  | 6 | 12 | 1156 | 1247 | -18 | 8  | 12 | 37   | 4    | 11  | 9 | 12 | 24    | 6     |
| -11 | 3 | 12 | -12  | 6    | 14  | 4 | 12 | 2    | 8    | -5  | 6 | 12 | 475  | 482  | -17 | 8  | 12 | 72   | 12   | 12  | 9 | 12 | 72    | 35    |
| -10 | 3 | 12 | 2751 | 2600 | 15  | 4 | 12 | 138  | 128  | -4  | 6 | 12 | 92   | 73   | -16 | 8  | 12 | 105  | 56   | 13  |   |    |       |       |



Table B.3, continued

| M   | K  | L  | Obe  | Calc | M   | K  | L    | Obe  | Calc | M | K  | L    | Obe  | Calc | M | K  | L    | Obe  | Calc | M  | K  | L    | Obe  | Calc |
|-----|----|----|------|------|-----|----|------|------|------|---|----|------|------|------|---|----|------|------|------|----|----|------|------|------|
| 0   | 11 | 12 | 29   | 17   | 15  | 13 | 30   | 1    | -1   | 3 | 13 | 389  | 465  | -19  | 5 | 13 | 152  | 169  | 6    | 6  | 13 | 39   | 17   |      |
| 1   | 11 | 12 | 45   | 1    | 16  | 13 | 431  | 491  | 0    | 3 | 13 | 868  | 749  | -18  | 5 | 13 | 73   | 98   | 7    | 6  | 13 | 550  | 495  |      |
| 2   | 11 | 12 | 7    | 6    | 17  | 13 | 24   | 10   | 1    | 3 | 13 | 1915 | 1032 | -17  | 5 | 13 | 218  | 201  | 8    | 6  | 13 | 44   | 50   |      |
| 3   | 11 | 12 | 37   | 3    | 18  | 13 | 131  | 173  | 2    | 3 | 13 | 922  | 849  | -16  | 5 | 13 | 270  | 280  | 9    | 6  | 13 | 252  | 225  |      |
| 4   | 11 | 12 | -1   | 2    | 19  | 13 | -46  | 13   | 3    | 3 | 13 | 2041 | 2153 | -15  | 5 | 13 | 93   | 100  | 10   | 6  | 13 | 47   | 30   |      |
| 5   | 11 | 12 | 120  | 2    | -21 | 2  | 32   | 6    | 4    | 3 | 13 | 572  | 523  | -14  | 5 | 13 | -4   | 6    | 11   | 6  | 13 | 86   | 85   |      |
| 6   | 11 | 12 | 58   | 0    | -20 | 2  | 64   | 65   | 5    | 3 | 13 | 1980 | 1872 | -13  | 5 | 13 | 1555 | 1530 | 12   | 6  | 13 | 18   | 12   |      |
| 7   | 11 | 12 | -1   | 1    | -19 | 2  | 54   | 34   | 6    | 3 | 13 | 1466 | 1253 | -12  | 5 | 13 | 331  | 270  | 13   | 6  | 13 | 32   | 24   |      |
| -21 | 0  | 13 | -33  | 10   | -18 | 2  | 167  | 203  | 7    | 3 | 13 | 2313 | 2153 | -11  | 5 | 13 | 845  | 780  | 14   | 6  | 13 | 120  | 225  |      |
| -19 | 0  | 13 | -16  | 12   | -17 | 2  | 142  | 178  | 8    | 3 | 13 | 322  | 303  | -10  | 5 | 13 | 275  | 319  | 15   | 6  | 13 | 82   | 111  |      |
| -17 | 0  | 13 | 5    | 0    | -16 | 2  | 29   | 26   | 9    | 3 | 13 | 3    | 10   | -9   | 5 | 13 | 24   | 4    | 16   | 6  | 13 | 13   | 4    |      |
| -15 | 0  | 13 | 122  | 161  | -15 | 2  | 406  | 417  | 10   | 3 | 13 | 172  | 160  | -8   | 5 | 13 | 131  | 131  | 17   | 6  | 13 | 49   | 24   |      |
| -13 | 0  | 13 | 28   | 31   | -14 | 2  | 36   | 38   | 11   | 3 | 13 | 1357 | 1357 | -7   | 5 | 13 | 332  | 266  | 18   | 6  | 13 | 11   | 2    |      |
| -11 | 0  | 13 | 74   | 39   | -13 | 2  | 107  | 80   | 12   | 3 | 13 | 160  | 161  | -6   | 5 | 13 | 279  | 259  | -20  | 7  | 13 | -18  | 35   |      |
| -9  | 0  | 13 | 3    | 24   | -12 | 2  | 15   | 19   | 13   | 3 | 13 | 1011 | 937  | -5   | 5 | 13 | 110  | 155  | -19  | 7  | 13 | -1   | 8    |      |
| -7  | 0  | 13 | 6638 | 6558 | -11 | 2  | 180  | 200  | 14   | 3 | 13 | 104  | 74   | -4   | 5 | 13 | 170  | 179  | -18  | 7  | 13 | 93   | 55   |      |
| -5  | 0  | 13 | 1734 | 1536 | -10 | 2  | 377  | 375  | 15   | 3 | 13 | 190  | 175  | -3   | 5 | 13 | 379  | 423  | -17  | 7  | 13 | 26   | 13   |      |
| -3  | 0  | 13 | 583  | 592  | -9  | 2  | 216  | 192  | 16   | 3 | 13 | 121  | 139  | -2   | 5 | 13 | 116  | 121  | -16  | 7  | 13 | 53   | 13   |      |
| -1  | 0  | 13 | 735  | 771  | -8  | 2  | 22   | 2    | 17   | 3 | 13 | 200  | 194  | -1   | 5 | 13 | 1833 | 1674 | -15  | 7  | 13 | 93   | 124  |      |
| 1   | 0  | 13 | 49   | 42   | -7  | 2  | 462  | 444  | 18   | 3 | 13 | 11   | 15   | 0    | 5 | 13 | 2509 | 2374 | -14  | 7  | 13 | 9    | 4    |      |
| 3   | 0  | 13 | 759  | 702  | -6  | 2  | 378  | 392  | 19   | 3 | 13 | 190  | 132  | 1    | 5 | 13 | 97   | 100  | -13  | 7  | 13 | 88   | 12   |      |
| 5   | 0  | 13 | 158  | 108  | -5  | 2  | 331  | 381  | -21  | 4 | 13 | 0    | 4    | 2    | 5 | 13 | 1040 | 1040 | -12  | 7  | 13 | 3    | 2    |      |
| 7   | 0  | 13 | 86   | 94   | -4  | 2  | 1390 | 1276 | -20  | 4 | 13 | 12   | 3    | 3    | 5 | 13 | 42   | 55   | -11  | 7  | 13 | 70   | 55   |      |
| 9   | 0  | 13 | 223  | 226  | -3  | 2  | 3101 | 2982 | -19  | 4 | 13 | 16   | 3    | 4    | 5 | 13 | 72   | 75   | -10  | 7  | 13 | 233  | 242  |      |
| 11  | 0  | 13 | 83   | 45   | -2  | 2  | 26   | 43   | -18  | 4 | 13 | -13  | 8    | 5    | 5 | 13 | 134  | 181  | -9   | 7  | 13 | 52   | 60   |      |
| 13  | 0  | 13 | 321  | 277  | -1  | 2  | 298  | 296  | -17  | 4 | 13 | 15   | 13   | 6    | 5 | 13 | 809  | 800  | -8   | 7  | 13 | 137  | 138  |      |
| 15  | 0  | 13 | 370  | 458  | 0   | 2  | 18   | 21   | -16  | 4 | 13 | 76   | 87   | 7    | 5 | 13 | 473  | 471  | -7   | 7  | 13 | 32   | 4    |      |
| 17  | 0  | 13 | 287  | 230  | 1   | 2  | 775  | 516  | -15  | 4 | 13 | -4   | 0    | 8    | 5 | 13 | 8    | 19   | -6   | 7  | 13 | 346  | 343  |      |
| 19  | 0  | 13 | 228  | 325  | 2   | 2  | 3356 | 3215 | -14  | 4 | 13 | 91   | 93   | 9    | 5 | 13 | 234  | 218  | -5   | 7  | 13 | 252  | 259  |      |
| -22 | 1  | 13 | 222  | 116  | 3   | 2  | 331  | 289  | -13  | 4 | 13 | 21   | 8    | 10   | 5 | 13 | 6    | 10   | -4   | 7  | 13 | 422  | 411  |      |
| -21 | 1  | 13 | 109  | 128  | 4   | 2  | 1353 | 1471 | -12  | 4 | 13 | 22   | 5    | 11   | 5 | 13 | 27   | 20   | -3   | 7  | 13 | 170  | 163  |      |
| -20 | 1  | 13 | 486  | 509  | 5   | 2  | 8    | 26   | -11  | 4 | 13 | 156  | 160  | 12   | 5 | 13 | 3    | 6    | -2   | 7  | 13 | 923  | 874  |      |
| -19 | 1  | 13 | 143  | 98   | 6   | 2  | 1295 | 1251 | -10  | 4 | 13 | 871  | 862  | 13   | 5 | 13 | 245  | 218  | -1   | 7  | 13 | 28   | 46   |      |
| -18 | 1  | 13 | 766  | 722  | 7   | 2  | 589  | 606  | -9   | 4 | 13 | 273  | 299  | 14   | 5 | 13 | 181  | 195  | 0    | 7  | 13 | 753  | 704  |      |
| -17 | 1  | 13 | 80   | 61   | 8   | 2  | 660  | 641  | -8   | 4 | 13 | 52   | 37   | 15   | 5 | 13 | -13  | 6    | 1    | 7  | 13 | 119  | 94   |      |
| -16 | 1  | 13 | 1368 | 1245 | 9   | 2  | 51   | 10   | -7   | 4 | 13 | 11   | 13   | 16   | 5 | 13 | 4    | 2    | 2    | 7  | 13 | 784  | 750  |      |
| -15 | 1  | 13 | 11   | 1    | 10  | 2  | 141  | 128  | -6   | 4 | 13 | 528  | 524  | 17   | 5 | 13 | 62   | 22   | 3    | 7  | 13 | 37   | 31   |      |
| -14 | 1  | 13 | 728  | 649  | 11  | 2  | 106  | 75   | -5   | 4 | 13 | 634  | 546  | 18   | 5 | 13 | 49   | 33   | 4    | 7  | 13 | 1008 | 912  |      |
| -13 | 1  | 13 | 50   | 53   | 12  | 2  | 23   | 7    | -4   | 4 | 13 | 866  | 889  | 19   | 5 | 13 | 67   | 41   | 5    | 7  | 13 | 6    | 0    |      |
| -12 | 1  | 13 | 1106 | 1013 | 13  | 2  | 79   | 82   | -3   | 4 | 13 | 0    | 2    | -21  | 6 | 13 | 34   | 29   | 6    | 7  | 13 | 348  | 349  |      |
| -11 | 1  | 13 | 23   | 28   | 14  | 2  | 120  | 126  | -2   | 4 | 13 | 114  | 82   | -20  | 6 | 13 | -19  | 2    | 7    | 7  | 13 | 15   | 0    |      |
| -10 | 1  | 13 | 1746 | 1775 | 15  | 2  | 159  | 158  | -1   | 4 | 13 | 48   | 35   | -19  | 6 | 13 | 10   | 7    | 8    | 7  | 13 | 158  | 169  |      |
| -9  | 1  | 13 | 709  | 565  | 16  | 2  | 69   | 109  | 0    | 4 | 13 | 758  | 790  | -18  | 6 | 13 | 31   | 11   | 9    | 7  | 13 | 233  | 162  |      |
| -8  | 1  | 13 | 5915 | 5756 | 17  | 2  | 37   | 12   | 1    | 4 | 13 | 68   | 106  | -17  | 6 | 13 | -9   | 16   | 10   | 7  | 13 | 106  | 133  |      |
| -7  | 1  | 13 | 915  | 930  | 18  | 2  | 58   | 62   | 2    | 4 | 13 | 641  | 572  | -16  | 6 | 13 | 3    | 4    | 11   | 7  | 13 | 102  | 120  |      |
| -6  | 1  | 13 | 6670 | 6852 | 19  | 2  | -48  | 26   | 3    | 4 | 13 | 74   | 61   | -15  | 6 | 13 | 31   | 35   | -12  | 7  | 13 | 57   | 142  |      |
| -5  | 1  | 13 | 26   | 51   | -21 | 3  | 40   | 23   | 4    | 4 | 13 | 1716 | 1535 | -14  | 6 | 13 | 35   | 40   | 13   | 7  | 13 | 12   | 0    |      |
| -4  | 1  | 13 | 4266 | 4126 | -20 | 3  | 24   | 1    | 5    | 4 | 13 | 83   | 37   | -13  | 6 | 13 | 184  | 183  | 14   | 7  | 13 | 36   | 26   |      |
| -3  | 1  | 13 | 336  | 327  | -19 | 3  | 331  | 268  | 6    | 4 | 13 | 41   | 28   | -12  | 6 | 13 | 150  | 112  | 15   | 7  | 13 | 44   | 47   |      |
| -2  | 1  | 13 | 1332 | 1178 | -18 | 3  | 68   | 3    | 7    | 4 | 13 | -3   | 2    | -11  | 6 | 13 | 203  | 215  | 16   | 7  | 13 | -17  | 2    |      |
| -1  | 1  | 13 | 425  | 257  | -17 | 3  | 41   | 14   | 8    | 4 | 13 | 13   | 1    | -10  | 6 | 13 | 133  | 105  | 17   | 7  | 13 | -17  | 1    |      |
| 0   | 1  | 13 | 90   | 210  | -16 | 3  | 458  | 459  | 9    | 4 | 13 | 181  | 164  | -9   | 6 | 13 | 417  | 339  | 18   | 7  | 13 | -6   | 121  |      |
| 1   | 1  | 13 | 1264 | 1140 | -15 | 3  | 496  | 459  | 10   | 4 | 13 | 728  | 682  | -8   | 6 | 13 | 357  | 339  | -19  | 8  | 13 | -6   | 10   |      |
| 2   | 1  | 13 | 177  | 228  | -14 | 3  | 113  | 117  | 11   | 4 | 13 | 113  | 136  | -7   | 6 | 13 | 60   | 50   | -18  | 8  | 13 | 38   | 13   |      |
| 3   | 1  | 13 | 2026 | 2113 | -13 | 3  | 46   | 34   | 12   | 4 | 13 | 285  | 258  | -6   | 6 | 13 | 351  | 353  | -17  | 8  | 13 | 22   | 0    |      |
| -16 | 8  | 13 | 9    | 11   | 14  | 9  | -9   | 1    | -16  | 1 | 14 | 139  | 72   | 9    | 2 | 14 | 1693 | 1688 | -6   | 4  | 14 | 318  | 315  |      |
| -15 | 8  | 13 | 0    | 5    | 15  | 9  | 92   | 2    | -15  | 1 | 14 | 89   | 64   | 10   | 2 | 14 | 1003 | 983  | -5   | 4  | 14 | 15   | 4    |      |
| -14 | 8  | 13 | 9    | 0    | -14 | 10 | 29   | 5    | -14  | 1 | 14 | 724  | 646  | 11   | 2 | 14 | 70   | 46   | 4    | 14 | 41 | 49   |      |      |
| -13 | 8  | 13 | -1   | 0    | -13 | 10 | 26   | 1    | -13  | 1 | 14 | 91   | 69   | 12   | 2 | 14 | -13  | 3    | -3   | 4  | 14 | 648  | 667  |      |
| -12 | 8  | 13 | 19   | 38   | -12 | 10 | -21  | 11   | -12  | 1 | 14 | 717  | 727  | 13   | 2 | 14 | 26   | 25   | -2   | 4  | 14 | 8    | 2    |      |
| -11 | 8  | 13 | 32   | 45   | -11 | 10 | 33   | 0    | -11  | 1 | 14 | 335  | 347  | 14   | 2 | 14 | 125  | 118  | -1   | 4  | 14 | 54   | 54   |      |
| -10 | 8  | 13 | 2    | 10   | -10 | 10 | 63   | 46   | -10  | 1 | 14 | 732  | 786  | 15   | 2 | 14 | 334  | 329  | 0    | 4  | 14 | 10   | 16   |      |
| -9  | 8  | 13 | -4   | 1    | -9  | 10 | 14   | 12   | -9   | 1 | 14 | 697  | 779  | 16   | 2 | 14 | 132  | 60   | 1    | 4  | 14 | 161  | 128  |      |
| -8  | 8  | 13 | 14   | 15   | -8  | 10 | 94   | 82   | -8   | 1 | 14 | 9    | 11   | 17   | 2 | 14 | 98   | 51   | 2    | 4  | 14 | 265  | 197  |      |
| -7  | 8  | 13 | 26   | 7    | -7  | 10 | 16   | 22   | -7   | 1 | 14 | 3365 | 3144 | 18   | 2 | 14 | 17   | 3    | 3    | 4  | 14 | 1367 | 1345 |      |
| -6  | 8  | 13 | 203  | 226  | -6  | 10 | 83   | 49   | -6   | 1 | 14 | 6195 | 5951 | 19   | 2 | 14 | 41   | 41   | 4    | 4  | 14 | 189  | 169  |      |
| -5  | 8  | 13 | 89   | 76   | -5  | 10 | 24   | 16   | -5   | 1 | 14 | 2643 | 2581 | -21  | 3 | 14 | -19  | 16   | 5    | 4  | 14 | 560  | 520  |      |
| -4  | 8  | 13 | 721  | 750  | -4  | 10 | 19   | 40   | -4   | 1 | 14 | 498  | 499  | -20  | 3 | 14 | 405  | 468  | 6    | 4  | 14 | 412  | 388  |      |
| -3  | 8  | 13 | -1   | 3    | -3  | 10 | 11   | 3    | -3   | 1 | 14 | 3282 | 3399 | -19  | 3 | 14 | 13   | 6    | 7    | 4  | 14 | 350  | 323  |      |
| -2  | 8  | 13 | 214  | 235  | -2  | 10 | 18   | 27   | -2   | 1 | 14 | 80   | 126  | -18  | 3 | 14 | 543  | 576  | 8    | 4  | 14 | 100  | 75   |      |
| -1  | 8  | 13 | 43   | 28   | -1  | 10 | 1    | 0    | -1   | 1 | 14 | 1925 | 1951 | -17  | 3 | 14 | 51   | 48   | 9    | 4  | 14 | 464  | 411  |      |
| 0   | 8  | 13 | 7    | 3    | 0   |    |      |      |      |   |    |      |      |      |   |    |      |      |      |    |    |      |      |      |

Table B.3, continued

| M   | K | L  | Obs  | Calc | M   | K | L  | Obs  | Calc | M   | K  | L  | Obs  | Calc | M   | K   | L  | Obs  | Calc | M   | K | L  | Obs  | Calc |
|-----|---|----|------|------|-----|---|----|------|------|-----|----|----|------|------|-----|-----|----|------|------|-----|---|----|------|------|
| -4  | 9 | 13 | 41   | 29   | -4  | 0 | 14 | 153  | 174  | -9  | 2  | 14 | 117  | 151  | 16  | 3   | 14 | 77   | 89   | -1  | 5 | 14 | 375  | 405  |
| -3  | 9 | 13 | 45   | 39   | -2  | 0 | 14 | 1453 | 1494 | -8  | 2  | 14 | 1021 | 876  | 17  | 3   | 14 | 36   | 38   | 0   | 5 | 14 | 1767 | 1800 |
| -2  | 9 | 13 | 14   | 5    | 0   | 0 | 14 | 83   | 17   | -7  | 2  | 14 | 70   | 50   | 18  | 3   | 14 | 55   | 18   | 1   | 5 | 14 | 705  | 699  |
| -1  | 9 | 13 | 201  | 229  | 2   | 0 | 14 | 1876 | 1856 | -6  | 2  | 14 | 370  | 394  | -21 | 4   | 14 | -32  | 37   | 2   | 5 | 14 | 527  | 610  |
| 0   | 9 | 13 | 270  | 294  | 4   | 0 | 14 | 2976 | 3360 | -5  | 2  | 14 | 168  | 222  | -20 | 4   | 14 | 20   | 4    | 3   | 5 | 14 | 76   | 37   |
| 1   | 9 | 13 | 56   | 45   | 6   | 0 | 14 | 2337 | 2438 | -4  | 2  | 14 | 646  | 716  | -19 | 4   | 14 | 70   | 30   | 4   | 5 | 14 | -1   | 3    |
| 2   | 9 | 13 | 245  | 295  | 8   | 0 | 14 | 256  | 247  | -3  | 2  | 14 | 236  | 247  | -18 | 4   | 14 | 46   | 70   | 5   | 5 | 14 | -2   | 3    |
| 3   | 9 | 13 | 4    | 9    | 10  | 0 | 14 | 247  | 286  | -2  | 2  | 14 | 1041 | 977  | -17 | 4   | 14 | 65   | 47   | 6   | 5 | 14 | 628  | 611  |
| 4   | 9 | 13 | 47   | 33   | 12  | 0 | 14 | 99   | 86   | -1  | 2  | 14 | 1433 | 1295 | -16 | 4   | 14 | 17   | 0    | 7   | 5 | 14 | 2    | 9    |
| 5   | 9 | 13 | 28   | 16   | 14  | 0 | 14 | 137  | 199  | 0   | 2  | 14 | 1607 | 1574 | -15 | 4   | 14 | 181  | 240  | 8   | 5 | 14 | 62   | 64   |
| 6   | 9 | 13 | 10   | 15   | 16  | 0 | 14 | 55   | 85   | 1   | 2  | 14 | 604  | 606  | -14 | 4   | 14 | 19   | 1    | 9   | 5 | 14 | 25   | 11   |
| 7   | 9 | 13 | -2   | 6    | 18  | 0 | 14 | 137  | 185  | 2   | 2  | 14 | 350  | 332  | -13 | 4   | 14 | 51   | 69   | 10  | 5 | 14 | 204  | 197  |
| 8   | 9 | 13 | 134  | 131  | -22 | 1 | 14 | 32   | 27   | 3   | 2  | 14 | 347  | 362  | -12 | 4   | 14 | 110  | 140  | 11  | 5 | 14 | 5    | 17   |
| 9   | 9 | 13 | 24   | 37   | -21 | 1 | 14 | 127  | 153  | 4   | 2  | 14 | -11  | 8    | -11 | 4   | 14 | 62   | 56   | 12  | 5 | 14 | 200  | 191  |
| 10  | 9 | 13 | 51   | 5    | -20 | 1 | 14 | 181  | 217  | 5   | 2  | 14 | 45   | 69   | -10 | 4   | 14 | 21   | 40   | 13  | 5 | 14 | 215  | 199  |
| 11  | 9 | 13 | 19   | 30   | -19 | 1 | 14 | 479  | 387  | 6   | 2  | 14 | 2142 | 876  | -8  | 4   | 14 | 209  | 262  | 15  | 5 | 14 | 52   | 12   |
| 12  | 9 | 13 | 11   | 1    | -18 | 1 | 14 | 480  | 465  | 7   | 2  | 14 | 893  | 2    | -7  | 4   | 14 | 144  | 115  | 16  | 5 | 14 | 83   | 23   |
| 13  | 9 | 13 | 30   | 29   | -17 | 1 | 14 | 492  | 483  | 8   | 2  | 14 | 11   | 19   | 3   | 0   | 15 | 4459 | 4518 | -3  | 2 | 15 | 244  | 259  |
| 14  | 9 | 13 | 28   | 3    | 4   | 7 | 14 | 20   | 36   | -3  | 9  | 14 | 14   | 28   | 6   | 0   | 15 | 2832 | 2841 | -2  | 2 | 15 | 233  | 258  |
| 15  | 9 | 13 | 47   | 87   | 6   | 7 | 14 | 117  | 117  | -2  | 9  | 14 | 25   | 20   | 7   | 0   | 15 | 2913 | 3097 | -1  | 2 | 15 | 334  | 323  |
| 16  | 9 | 13 | 0    | 54   | 6   | 7 | 14 | -16  | 3    | -1  | 9  | 14 | 14   | 20   | 7   | 0   | 15 | 2913 | 3097 | -1  | 2 | 15 | 245  | 257  |
| 17  | 9 | 13 | 11   | 5    | 7   | 7 | 14 | 27   | 44   | 0   | 9  | 14 | 8    | 8    | 9   | 0   | 15 | 566  | 635  | 0   | 2 | 15 | 22   | 18   |
| 18  | 9 | 13 | 11   | 2    | 8   | 7 | 14 | 1    | 14   | 1   | 9  | 14 | 0    | 13   | 11  | 0   | 15 | 261  | 274  | 1   | 2 | 15 | 529  | 479  |
| 19  | 9 | 13 | 4    | 0    | 9   | 7 | 14 | 58   | 78   | 2   | 9  | 14 | 7    | 7    | 13  | 0   | 15 | 179  | 114  | 2   | 2 | 15 | 1458 | 1374 |
| 20  | 9 | 13 | 209  | 138  | 10  | 7 | 14 | 29   | 46   | 3   | 9  | 14 | 62   | 89   | 15  | 0   | 15 | 399  | 347  | 3   | 3 | 15 | 744  | 808  |
| -16 | 6 | 14 | 62   | 2    | 11  | 7 | 14 | 152  | 135  | 4   | 9  | 14 | 22   | 6    | -21 | 1   | 15 | 29   | 71   | 5   | 2 | 15 | 755  | 770  |
| -15 | 6 | 14 | -5   | 57   | 12  | 7 | 14 | 20   | 7    | 5   | 9  | 14 | 7    | 0    | -20 | 1   | 15 | 293  | 340  | 6   | 2 | 15 | 408  | 457  |
| -14 | 6 | 14 | 114  | 84   | 13  | 7 | 14 | 1    | 30   | 6   | 9  | 14 | 21   | 40   | -19 | 1   | 15 | 59   | 24   | 7   | 2 | 15 | 320  | 292  |
| -13 | 6 | 14 | 160  | 150  | 14  | 7 | 14 | 15   | 6    | 7   | 9  | 14 | 43   | 4    | -18 | 1   | 15 | 546  | 530  | 8   | 2 | 15 | 1887 | 1870 |
| -12 | 6 | 14 | 30   | 29   | 15  | 7 | 14 | -4   | 7    | 8   | 9  | 14 | 28   | 54   | -17 | 1   | 15 | 362  | 357  | 9   | 2 | 15 | 133  | 107  |
| -11 | 6 | 14 | 16   | 19   | 16  | 7 | 14 | -26  | 1    | 9   | 9  | 14 | 59   | 56   | -16 | 1   | 15 | 906  | 912  | 10  | 2 | 15 | 819  | 782  |
| -10 | 6 | 14 | 14   | 0    | 17  | 7 | 14 | -13  | 4    | 10  | 9  | 14 | 59   | 53   | -15 | 1   | 15 | -1   | 1    | 11  | 2 | 15 | 597  | 675  |
| -9  | 6 | 14 | 17   | 4    | -19 | 8 | 14 | -5   | 35   | 11  | 9  | 14 | 30   | 71   | -14 | 1   | 15 | 732  | 684  | 12  | 2 | 15 | 21   | 2    |
| -8  | 6 | 14 | 6    | 18   | -18 | 8 | 14 | 110  | 34   | 12  | 9  | 14 | 20   | 4    | -13 | 1   | 15 | 126  | 105  | 13  | 2 | 15 | 215  | 230  |
| -7  | 6 | 14 | 152  | 121  | -17 | 8 | 14 | 16   | 2    | 13  | 9  | 14 | -20  | 29   | -12 | 1   | 15 | 1621 | 1527 | 14  | 2 | 15 | 296  | 298  |
| -6  | 6 | 14 | 482  | 539  | -16 | 8 | 14 | 58   | 20   | 14  | 9  | 14 | -7   | 8    | -11 | 1   | 15 | 134  | 132  | 15  | 2 | 15 | 220  | 219  |
| -5  | 6 | 14 | 299  | 304  | -15 | 8 | 14 | 7    | 1    | -13 | 10 | 14 | -44  | 7    | -10 | 1   | 15 | 410  | 418  | 16  | 2 | 15 | 323  | 256  |
| -4  | 6 | 14 | 228  | 184  | -14 | 8 | 14 | -5   | 14   | -12 | 10 | 14 | 4    | 34   | -9  | 1   | 15 | 395  | 400  | 17  | 2 | 15 | 51   | 99   |
| -3  | 6 | 14 | 2382 | 2454 | -13 | 8 | 14 | 33   | 4    | -11 | 10 | 14 | 107  | 15   | -8  | 1   | 15 | 2027 | 1972 | 18  | 2 | 15 | -16  | 43   |
| -2  | 6 | 14 | 1177 | 1100 | -12 | 3 | 14 | 44   | 13   | -10 | 10 | 14 | 28   | 9    | -7  | 1   | 15 | 28   | 2    | -21 | 3 | 15 | 36   | 25   |
| -1  | 6 | 14 | 1923 | 1932 | -11 | 0 | 14 | 46   | 43   | -9  | 10 | 14 | 7    | 1    | -6  | 1   | 15 | 1370 | 1453 | -20 | 3 | 15 | 9    | 2    |
| 0   | 6 | 14 | 1452 | 1414 | -10 | 0 | 14 | 219  | 227  | -8  | 10 | 14 | 25   | 71   | -5  | 1   | 15 | 1483 | 1450 | -19 | 3 | 15 | 103  | 170  |
| 1   | 6 | 14 | 1838 | 1675 | -9  | 0 | 14 | 142  | 108  | -7  | 10 | 14 | 67   | 5    | -4  | 1   | 15 | 2301 | 2342 | -18 | 3 | 15 | 70   | 92   |
| 2   | 6 | 14 | 644  | 595  | -8  | 9 | 14 | 35   | 10   | -6  | 10 | 14 | 23   | 2    | -3  | 1   | 15 | -7   | 3    | -17 | 3 | 15 | 0    | 25   |
| 3   | 6 | 14 | -1   | 5    | -7  | 8 | 14 | 49   | 39   | -5  | 10 | 14 | -1   | 6    | -2  | 1   | 15 | 319  | 368  | -16 | 3 | 15 | 70   | 99   |
| 4   | 6 | 14 | 88   | 48   | -6  | 8 | 14 | 54   | 51   | -4  | 10 | 14 | 6    | 21   | -2  | 1   | 15 | 288  | 250  | -15 | 3 | 15 | 1008 | 993  |
| 5   | 6 | 14 | 80   | 97   | -5  | 8 | 14 | 329  | 341  | -3  | 10 | 14 | 4    | 1    | -1  | 1   | 15 | 492  | 474  | -14 | 3 | 15 | 94   | 137  |
| 6   | 6 | 14 | 52   | 48   | -4  | 8 | 14 | 105  | 101  | -2  | 10 | 14 | -14  | 10   | 0   | 1   | 15 | 2    | 19   | -13 | 3 | 15 | 609  | 563  |
| 7   | 6 | 14 | 0    | 2    | -3  | 8 | 14 | 6    | 33   | 0   | 10 | 14 | 24   | 11   | 2   | 1   | 15 | 2577 | 2487 | -12 | 3 | 15 | 10   | 10   |
| 8   | 6 | 14 | 172  | 153  | -2  | 8 | 14 | 29   | 401  | 1   | 10 | 14 | 4    | 5    | 3   | 1   | 15 | 207  | 179  | -11 | 3 | 15 | 1807 | 1710 |
| 9   | 6 | 14 | -9   | 8    | -1  | 8 | 14 | 367  | 27   | 2   | 10 | 14 | -10  | 10   | 4   | 1   | 15 | 2441 | 2387 | -10 | 3 | 15 | 134  | 131  |
| 10  | 6 | 14 | 204  | 195  | 0   | 8 | 14 | 21   | 27   | 2   | 10 | 14 | 24   | 20   | 5   | 1   | 15 | 23   | 32   | -9  | 3 | 15 | 114  | 107  |
| 11  | 6 | 14 | 51   | 17   | 1   | 8 | 14 | 56   | 39   | 3   | 10 | 14 | 24   | 58   | 6   | 1   | 15 | 1809 | 1827 | -8  | 3 | 15 | 64   | 62   |
| 12  | 6 | 14 | 34   | 11   | 2   | 8 | 14 | 83   | 93   | 4   | 10 | 14 | 50   | 10   | 7   | 1   | 15 | 143  | 116  | -7  | 3 | 15 | 4839 | 4593 |
| 13  | 6 | 14 | 74   | 90   | 3   | 8 | 14 | 22   | 24   | 5   | 10 | 14 | 19   | 1    | 8   | 1   | 15 | 2921 | 2967 | -6  | 3 | 15 | 377  | 355  |
| 14  | 6 | 14 | 82   | 81   | 4   | 8 | 14 | 85   | 105  | 6   | 10 | 14 | 36   | 9    | 9   | 1   | 15 | 153  | 133  | -5  | 3 | 15 | 1860 | 1765 |
| 15  | 6 | 14 | 8    | 0    | 5   | 8 | 14 | 14   | 15   | 7   | 10 | 14 | 10   | 8    | 10  | 1   | 15 | 1470 | 1517 | -4  | 3 | 15 | 35   | 25   |
| 16  | 6 | 14 | 77   | 67   | 6   | 8 | 14 | 33   | 23   | 8   | 10 | 14 | 35   | 6    | 11  | 1   | 15 | -8   | 1    | -3  | 3 | 15 | 1291 | 1326 |
| 17  | 6 | 14 | 49   | 0    | 7   | 8 | 14 | 37   | 50   | 9   | 10 | 14 | 35   | 5    | 12  | 1   | 15 | 323  | 325  | -2  | 3 | 15 | 35   | 12   |
| 18  | 6 | 14 | 36   | 8    | 8   | 8 | 14 | 268  | 221  | -6  | 11 | 14 | 210  | 10   | 13  | 1   | 15 | 28   | 58   | -1  | 3 | 15 | 1258 | 1256 |
| -20 | 7 | 14 | 37   | 11   | 9   | 8 | 14 | 92   | 110  | -5  | 11 | 14 | 55   | 16   | 14  | 1   | 15 | 362  | 343  | 0   | 3 | 15 | 7    | 3    |
| -19 | 7 | 14 | 152  | 134  | 10  | 8 | 14 | 129  | 105  | -4  | 11 | 14 | 36   | 1    | 15  | 1   | 15 | 35   | 71   | 1   | 3 | 15 | 636  | 545  |
| -18 | 7 | 14 | 33   | 10   | 11  | 8 | 14 | 79   | 91   | -3  | 11 | 14 | -8   | 5    | 16  | 1   | 15 | 233  | 190  | 2   | 3 | 15 | 77   | 94   |
| -17 | 7 | 14 | 106  | 182  | 12  | 8 | 14 | 13   | 2    | -2  | 11 | 14 | 8    | 0    | 17  | 1   | 15 | 36   | 4    | 3   | 3 | 15 | 1525 | 1550 |
| -16 | 7 | 14 | 64   | 11   | 13  | 8 | 14 | 19   | 1    | -1  | 11 | 14 | 30   | 13   | 18  | 1   | 15 | -11  | 30   | 4   | 3 | 15 | 412  | 388  |
| -15 | 7 | 14 | 16   | 9    | 14  | 8 | 14 | 114  | 115  | 0   | 11 | 14 | 24   | 6    | -21 | 2   | 15 | -9   | 22   | 5   | 3 | 15 | 1706 | 1595 |
| -14 | 7 | 14 | 138  | 126  | 15  | 8 | 14 | -1   | 9    | 1   | 11 | 14 | 49   | 23   | -20 | 2   | 15 | 11   | 28   | 6   | 3 | 15 | 342  | 315  |
| -13 | 7 | 14 | 372  | 432  | 16  | 8 | 14 | 1    | 3    | 2   | 11 | 14 | -1   | 36   | 17  | -19 | 2  | 15   | 67   | 7   | 3 | 15 | 542  | 487  |
| -12 | 7 | 14 | -20  | 2    | 17  | 8 | 14 | 13   | 1    | 3   | 11 | 14 | 89   | 1    | -19 | 2   | 15 | -9   | 14   | 8   | 3 | 15 |      |      |

Table B.3, continued

| M   | K | L  | Obs  | Calc | M   | K | L  | Obs  | Calc | M   | K | L  | Obs | Calc | M   | K  | L  | Obs | Calc | M   | K | L  | Obs  | Calc |
|-----|---|----|------|------|-----|---|----|------|------|-----|---|----|-----|------|-----|----|----|-----|------|-----|---|----|------|------|
| 1   | 4 | 15 | 88   | 96   | -15 | 6 | 15 | 180  | 187  | 13  | 7 | 15 | -1  | 26   | 9   | 9  | 15 | -11 | 8    | -15 | 1 | 16 | 313  | 323  |
| 2   | 4 | 15 | 781  | 749  | -14 | 6 | 15 | 65   | 29   | 14  | 7 | 15 | 13  | 6    | 10  | 9  | 15 | 11  | 47   | -14 | 1 | 16 | 0    | 6    |
| 3   | 4 | 15 | 73   | 28   | -13 | 6 | 15 | 58   | 33   | 15  | 7 | 15 | 53  | 11   | 11  | 9  | 15 | 109 | 146  | -13 | 1 | 16 | 446  | 372  |
| 4   | 4 | 15 | 1502 | 1318 | -12 | 6 | 15 | 107  | 105  | 16  | 7 | 15 | 58  | 1    | 12  | 9  | 15 | 44  | 7    | -12 | 1 | 16 | 81   | 51   |
| 5   | 4 | 15 | 154  | 156  | -11 | 6 | 15 | 308  | 288  | 17  | 7 | 15 | 24  | 4    | 13  | 9  | 15 | 19  | 2    | -11 | 1 | 16 | 533  | 524  |
| 6   | 4 | 15 | 4    | 6    | -10 | 6 | 15 | 326  | 373  | -18 | 8 | 15 | -7  | 11   | 14  | 9  | 15 | 104 | 4    | -10 | 1 | 16 | 63   | 61   |
| 7   | 4 | 15 | 540  | 809  | -9  | 6 | 15 | 169  | 175  | -17 | 8 | 15 | 54  | 57   | -13 | 10 | 15 | 94  | 15   | -9  | 1 | 16 | 312  | 290  |
| 8   | 4 | 15 | 616  | 666  | -8  | 6 | 15 | 731  | 671  | -16 | 8 | 15 | 20  | 16   | -12 | 10 | 15 | 109 | 1    | -8  | 1 | 16 | 10   | 1    |
| 9   | 4 | 15 | 12   | 5    | -7  | 6 | 15 | 7    | 7    | -15 | 8 | 15 | 22  | 12   | -11 | 10 | 15 | -2  | 9    | -7  | 1 | 16 | 3956 | 3742 |
| 10  | 4 | 15 | 378  | 363  | -6  | 6 | 15 | 11   | 21   | -14 | 8 | 15 | 13  | 20   | -10 | 10 | 15 | -34 | 0    | -6  | 1 | 16 | 17   | 4    |
| 11  | 4 | 15 | 42   | 46   | -5  | 6 | 15 | 146  | 138  | -13 | 8 | 15 | 60  | 15   | -9  | 10 | 15 | 32  | 2    | -5  | 1 | 16 | 1457 | 1258 |
| 12  | 4 | 15 | 266  | 236  | -4  | 6 | 15 | 548  | 543  | -12 | 8 | 15 | 97  | 110  | -8  | 10 | 15 | -1  | 3    | -4  | 1 | 16 | 135  | 98   |
| 13  | 4 | 15 | 53   | 24   | -3  | 6 | 15 | 2489 | 2382 | -11 | 8 | 15 | 221 | 210  | -7  | 10 | 15 | -2  | 4    | -3  | 1 | 16 | 1444 | 1418 |
| 14  | 4 | 15 | 200  | 175  | -2  | 6 | 15 | 1669 | 1603 | -10 | 8 | 15 | 32  | 0    | -6  | 10 | 15 | 43  | 43   | -2  | 1 | 16 | 72   | 57   |
| 15  | 4 | 15 | 59   | 52   | -1  | 6 | 15 | 78   | 55   | -9  | 8 | 15 | 84  | 75   | -5  | 10 | 15 | 95  | 120  | -1  | 1 | 16 | 406  | 427  |
| 16  | 4 | 15 | 3    | 3    | 0   | 6 | 15 | 1269 | 1282 | -8  | 8 | 15 | 83  | 108  | -4  | 10 | 15 | 31  | 24   | 0   | 1 | 16 | 370  | 429  |
| 17  | 4 | 15 | 45   | 26   | 1   | 6 | 15 | 1364 | 1284 | -7  | 8 | 15 | 126 | 131  | -3  | 10 | 15 | 19  | 27   | 1   | 1 | 16 | 127  | 122  |
| 18  | 4 | 15 | -40  | 19   | 2   | 6 | 15 | 84   | 79   | -6  | 8 | 15 | 0   | 0    | -2  | 10 | 15 | 6   | 0    | 2   | 1 | 16 | 420  | 353  |
| 19  | 4 | 15 | 28   | 41   | 3   | 6 | 15 | 388  | 338  | -5  | 8 | 15 | 38  | 45   | -1  | 10 | 15 | 27  | 34   | -3  | 1 | 16 | 399  | 320  |
| 20  | 4 | 15 | 183  | 12   | 4   | 6 | 15 | 0    | 6    | -4  | 8 | 15 | 79  | 101  | 0   | 10 | 15 | 24  | 14   | 4   | 1 | 16 | 163  | 155  |
| 21  | 4 | 15 | 19   | 1    | 5   | 6 | 15 | 162  | 155  | -3  | 8 | 15 | 165 | 153  | 1   | 10 | 15 | 48  | 36   | 5   | 1 | 16 | 209  | 172  |
| -20 | 5 | 15 | 133  | 20   | 6   | 6 | 15 | 49   | 61   | -2  | 8 | 15 | 8   | 6    | 2   | 10 | 15 | 21  | 24   | 6   | 1 | 16 | 189  | 203  |
| -19 | 5 | 15 | 139  | 74   | 7   | 6 | 15 | 167  | 164  | -1  | 8 | 15 | 79  | 55   | 3   | 10 | 15 | 39  | 32   | 7   | 1 | 16 | 33   | 18   |
| -18 | 5 | 15 | 133  | 56   | 8   | 6 | 15 | 89   | 78   | 0   | 8 | 15 | 15  | 17   | 4   | 10 | 15 | 26  | 11   | 8   | 1 | 16 | 1147 | 1244 |
| -17 | 5 | 15 | 156  | 147  | 9   | 6 | 15 | 14   | 30   | 1   | 8 | 15 | 321 | 330  | 5   | 10 | 15 | -4  | 10   | 9   | 1 | 16 | 50   | 31   |
| -16 | 5 | 15 | 133  | 97   | 10  | 6 | 15 | 75   | 75   | 2   | 8 | 15 | 0   | 3    | 6   | 10 | 15 | 2   | 1    | 10  | 1 | 16 | 93   | 61   |
| -15 | 5 | 15 | 238  | 252  | 11  | 6 | 15 | 32   | 24   | 3   | 8 | 15 | 221 | 160  | 7   | 10 | 15 | 6   | 4    | 11  | 1 | 16 | 45   | 72   |
| -14 | 5 | 15 | 297  | 301  | 12  | 6 | 15 | 223  | 178  | 4   | 8 | 15 | 65  | 50   | 8   | 10 | 15 | 42  | 29   | 12  | 1 | 16 | 465  | 471  |
| -13 | 5 | 15 | 445  | 464  | 13  | 6 | 15 | -5   | 3    | 5   | 8 | 15 | 231 | 166  | 9   | 10 | 15 | 39  | 4    | 13  | 1 | 16 | 89   | 36   |
| -12 | 5 | 15 | 69   | 46   | 14  | 6 | 15 | 75   | 99   | 6   | 8 | 15 | -11 | 0    | -5  | 11 | 15 | -64 | 23   | 14  | 1 | 16 | 28   | 4    |
| -11 | 5 | 15 | 471  | 571  | 15  | 6 | 15 | 135  | 144  | 7   | 8 | 15 | 36  | 42   | -4  | 11 | 15 | -43 | 1    | 15  | 1 | 16 | 79   | 58   |
| -10 | 5 | 15 | 104  | 92   | 16  | 6 | 15 | 37   | 9    | 8   | 8 | 15 | 9   | 0    | -3  | 11 | 15 | 40  | 9    | 16  | 1 | 16 | 72   | 1    |
| -9  | 5 | 15 | -1   | 2    | 17  | 6 | 15 | 31   | 3    | 9   | 8 | 15 | 113 | 112  | -2  | 11 | 15 | 66  | 6    | 17  | 1 | 16 | 20   | 16   |
| -8  | 5 | 15 | 695  | 683  | -20 | 7 | 15 | 77   | 56   | 10  | 8 | 15 | -16 | 3    | -1  | 11 | 15 | 17  | 8    | 18  | 1 | 16 | 81   | 4    |
| -7  | 5 | 15 | 41   | 47   | -19 | 7 | 15 | 10   | 1    | 11  | 8 | 15 | 79  | 105  | 0   | 11 | 15 | -10 | 22   | -21 | 2 | 16 | 34   | 12   |
| -6  | 5 | 15 | 22   | 14   | -18 | 7 | 15 | 3    | 16   | 12  | 8 | 15 | 43  | 10   | 1   | 11 | 15 | 43  | 0    | -20 | 2 | 16 | 65   | 76   |
| -5  | 5 | 15 | 12   | 2    | -17 | 7 | 15 | -23  | 6    | 13  | 8 | 15 | 32  | 0    | 2   | 11 | 15 | -30 | 23   | -19 | 2 | 16 | 4    | 6    |
| -4  | 5 | 15 | 105  | 108  | -16 | 7 | 15 | 3    | 4    | 14  | 8 | 15 | 60  | 6    | 3   | 11 | 15 | 35  | 22   | -18 | 2 | 16 | 89   | 38   |
| -3  | 5 | 15 | 441  | 374  | -15 | 7 | 15 | 6    | 2    | 15  | 8 | 15 | 108 | 10   | 4   | 11 | 15 | 51  | 1    | -17 | 2 | 16 | 21   | 13   |
| -2  | 5 | 15 | 871  | 905  | -14 | 7 | 15 | 21   | 11   | 16  | 8 | 15 | 5   | 7    | 5   | 11 | 15 | 11  | 30   | -16 | 2 | 16 | 350  | 339  |
| -1  | 5 | 15 | 1490 | 1485 | -13 | 7 | 15 | 52   | 57   | -7  | 8 | 15 | 74  | 12   | -20 | 1  | 16 | 188 | 160  | -15 | 2 | 16 | -14  | 3    |
| 0   | 5 | 15 | 467  | 453  | -12 | 7 | 15 | 431  | 420  | -16 | 9 | 15 | -39 | 4    | -14 | 0  | 16 | 97  | 117  | -14 | 0 | 16 | 69   | 44   |
| 1   | 5 | 15 | 147  | 176  | -11 | 7 | 15 | 10   | 10   | -15 | 9 | 15 | 83  | 0    | -16 | 0  | 16 | 320 | 376  | -13 | 2 | 16 | 26   | 39   |
| 2   | 5 | 15 | 39   | 23   | -10 | 7 | 15 | 112  | 114  | -14 | 9 | 15 | 44  | 35   | -14 | 0  | 16 | 677 | 694  | -12 | 2 | 16 | 13   | 2    |
| 3   | 5 | 15 | 515  | 534  | -9  | 7 | 15 | 16   | 13   | -13 | 9 | 15 | 22  | 23   | -12 | 0  | 16 | 123 | 102  | -11 | 2 | 16 | 18   | 21   |
| 4   | 5 | 15 | 255  | 295  | -8  | 7 | 15 | 284  | 299  | -12 | 9 | 15 | 51  | 3    | -10 | 0  | 16 | 31  | 17   | -10 | 2 | 16 | 286  | 272  |
| 5   | 5 | 15 | 317  | 367  | -7  | 7 | 15 | 23   | 20   | -11 | 9 | 15 | -21 | 1    | -8  | 0  | 16 | 699 | 702  | -9  | 2 | 16 | 308  | 274  |
| -8  | 2 | 16 | 34   | 25   | 19  | 3 | 16 | 124  | 2    | 1   | 5 | 16 | -10 | 4    | -11 | 7  | 16 | 36  | 29   | -14 | 9 | 16 | -12  | 1    |
| -7  | 2 | 16 | 843  | 777  | 20  | 3 | 16 | 75   | 24   | 2   | 5 | 16 | 73  | 59   | -10 | 7  | 16 | 32  | 6    | -13 | 9 | 16 | 33   | 34   |
| -6  | 2 | 16 | 349  | 396  | 21  | 3 | 16 | 53   | 0    | 3   | 5 | 16 | 16  | 0    | -9  | 7  | 16 | 24  | 4    | -12 | 9 | 16 | 11   | 9    |
| -5  | 2 | 16 | 35   | 9    | 22  | 3 | 16 | -2   | 0    | 4   | 5 | 16 | 17  | 30   | -8  | 7  | 16 | 19  | 0    | -11 | 9 | 16 | 94   | 82   |
| -4  | 2 | 16 | 627  | 524  | -20 | 4 | 16 | 76   | 41   | 5   | 5 | 16 | 95  | 921  | -7  | 7  | 16 | 37  | 39   | -10 | 9 | 16 | 54   | 17   |
| -3  | 2 | 16 | 127  | 101  | -19 | 4 | 16 | 7    | 4    | 6   | 5 | 16 | 569 | 577  | -6  | 7  | 16 | 54  | 85   | -9  | 9 | 16 | 47   | 5    |
| -2  | 2 | 16 | 940  | 971  | -18 | 4 | 16 | -1   | 6    | 7   | 5 | 16 | 194 | 202  | -5  | 7  | 16 | 62  | 57   | -8  | 9 | 16 | 66   | 70   |
| -1  | 2 | 16 | 500  | 539  | -17 | 4 | 16 | 115  | 118  | 8   | 5 | 16 | 62  | 51   | -4  | 7  | 16 | 358 | 365  | -7  | 9 | 16 | 2    | 2    |
| 0   | 2 | 16 | 2873 | 2701 | -16 | 4 | 16 | 20   | 0    | 9   | 5 | 16 | -7  | 0    | -3  | 7  | 16 | 18  | 24   | -6  | 9 | 16 | 18   | 10   |
| 1   | 2 | 16 | 120  | 109  | -15 | 4 | 16 | 316  | 327  | 10  | 5 | 16 | 22  | 29   | -2  | 7  | 16 | 80  | 122  | -5  | 9 | 16 | 15   | 18   |
| 2   | 2 | 16 | 503  | 451  | -14 | 4 | 16 | 156  | 126  | 11  | 5 | 16 | 20  | 3    | -1  | 7  | 16 | 277 | 331  | -4  | 9 | 16 | 14   | 1    |
| 3   | 2 | 16 | 81   | 100  | -13 | 4 | 16 | 3    | 20   | 12  | 5 | 16 | 11  | 14   | 0   | 7  | 16 | 126 | 138  | -3  | 9 | 16 | 10   | 9    |
| 4   | 2 | 16 | 143  | 143  | -12 | 4 | 16 | 79   | 68   | 13  | 5 | 16 | 0   | 2    | 1   | 7  | 16 | 389 | 459  | -2  | 9 | 16 | 15   | 14   |
| 5   | 2 | 16 | 615  | 592  | -11 | 4 | 16 | 538  | 503  | 14  | 5 | 16 | 24  | 32   | 2   | 7  | 16 | 126 | 86   | -1  | 9 | 16 | 14   | 33   |
| 6   | 2 | 16 | 1048 | 1037 | -10 | 4 | 16 | 137  | 136  | 15  | 5 | 16 | 38  | 10   | 3   | 7  | 16 | 13  | 4    | 0   | 9 | 16 | 71   | 80   |
| 7   | 2 | 16 | 42   | 35   | -9  | 4 | 16 | 220  | 249  | 16  | 5 | 16 | 43  | 15   | 4   | 7  | 16 | -14 | 2    | 1   | 9 | 16 | 61   | 68   |
| 8   | 2 | 16 | 354  | 358  | -8  | 4 | 16 | 452  | 468  | 17  | 5 | 16 | -4  | 18   | 5   | 7  | 16 | -29 | 0    | 2   | 9 | 16 | 23   | 11   |
| 9   | 2 | 16 | 406  | 418  | -7  | 4 | 16 | 2    | 9    | 18  | 5 | 16 | 16  | 1    | 6   | 7  | 16 | 17  | 0    | 3   | 9 | 16 | 23   | 11   |
| 10  | 2 | 16 | 266  | 265  | -6  | 4 | 16 | 36   | 57   | 19  | 5 | 16 | -11 | 4    | 9   | 7  | 16 | -3  | 5    | 4   | 9 | 16 | 39   | 0    |
| 11  | 2 | 16 | 69   | 51   | -5  | 4 | 16 | 1013 | 875  | -20 | 6 | 16 | 24  | 24   | 8   | 7  | 16 | 25  | 11   | 5   | 9 | 16 | -4   | 1    |
| 12  | 2 | 16 | 68   | 58   | -4  | 4 | 16 | 1217 | 1207 | -19 | 6 | 16 | -22 | 3    | 9   | 7  | 16 | 0   | 11   | 6   | 9 | 16 | 60   | 25   |
| 13  | 2 | 16 | 26   | 3    | -3  | 4 | 16 | 482  | 474  | -18 | 6 | 16 | 13  | 0    | 10  | 7  | 16 | 11  | 12   | 7   | 9 | 16 | 36   | 37   |
| 14  | 2 | 16 | 346  | 354  | -2  | 4 | 16 | 106  | 97   | -17 | 6 | 16 | 9   |      |     |    |    |     |      |     |   |    |      |      |

Table B.3, continued

| H   | K | L  | Obs  | Calc | H   | K | L  | Obs  | Calc | H   | K | L  | Obs  | Calc | H   | K | L  | Obs | Calc |
|-----|---|----|------|------|-----|---|----|------|------|-----|---|----|------|------|-----|---|----|-----|------|
| 9   | 3 | 16 | 53   | 41   | -9  | 5 | 16 | 29   | 19   | 17  | 6 | 16 | 49   | 1    | 10  | 8 | 16 | 97  | 94   |
| 10  | 3 | 16 | 256  | 233  | -8  | 5 | 16 | 105  | 113  | -20 | 7 | 16 | -92  | 2    | 11  | 8 | 16 | 32  | 23   |
| 11  | 3 | 16 | 81   | 45   | -7  | 5 | 16 | 495  | 444  | -19 | 7 | 16 | 249  | 154  | 12  | 8 | 16 | 27  | 0    |
| 12  | 3 | 16 | 67   | 109  | -6  | 5 | 16 | 2524 | 2527 | -18 | 7 | 16 | 53   | 42   | 13  | 8 | 16 | 35  | 0    |
| 13  | 3 | 16 | -9   | 8    | -5  | 5 | 16 | 282  | 338  | -17 | 7 | 16 | 36   | 27   | 14  | 8 | 16 | 50  | 60   |
| 14  | 3 | 16 | 6    | 1    | -4  | 5 | 16 | 104  | 109  | -16 | 7 | 16 | 53   | 22   | 15  | 8 | 16 | 6   | 22   |
| 15  | 3 | 16 | 108  | 114  | -3  | 5 | 16 | 114  | 85   | -15 | 7 | 16 | 8    | 5    | 16  | 8 | 16 | 199 | 35   |
| 16  | 3 | 16 | 32   | 42   | -2  | 5 | 16 | 941  | 970  | -14 | 7 | 16 | 161  | 144  | -17 | 9 | 16 | -39 | 12   |
| 17  | 3 | 16 | 55   | 9    | -1  | 5 | 16 | -3   | 1    | -13 | 7 | 16 | 134  | 157  | -16 | 9 | 16 | 25  | 28   |
| 18  | 3 | 16 | 116  | 42   | 0   | 5 | 16 | 37   | 46   | -12 | 7 | 16 | 80   | 62   | -15 | 9 | 16 | 82  | 20   |
| -7  | 0 | 17 | 2310 | 2325 | -6  | 2 | 17 | 1327 | 1298 | 22  | 3 | 17 | -10  | 14   | 4   | 5 | 17 | 97  | 102  |
| -8  | 0 | 17 | 4035 | 4194 | -5  | 2 | 17 | 1189 | 1172 | -20 | 4 | 17 | 37   | 1    | 5   | 8 | 17 | 476 | 547  |
| -9  | 0 | 17 | 6443 | 5562 | -4  | 2 | 17 | 770  | 832  | -19 | 4 | 17 | 4    | 2    | 6   | 5 | 17 | 17  | 28   |
| -1  | 0 | 17 | 1248 | 1016 | -3  | 2 | 17 | 72   | 98   | -18 | 4 | 17 | -10  | 1    | 7   | 5 | 17 | 10  | 26   |
| 1   | 0 | 17 | 85   | 35   | -2  | 2 | 17 | 1677 | 1558 | -17 | 4 | 17 | 23   | 70   | 8   | 5 | 17 | 32  | 59   |
| 3   | 0 | 17 | 2157 | 2351 | -1  | 2 | 17 | 363  | 367  | -16 | 4 | 17 | 606  | 699  | 9   | 5 | 17 | 99  | 76   |
| 5   | 0 | 17 | 1509 | 1475 | 0   | 2 | 17 | 1883 | 1867 | -15 | 4 | 17 | 97   | 89   | 10  | 5 | 17 | 21  | 28   |
| 7   | 0 | 17 | 987  | 715  | 1   | 2 | 17 | 1248 | 1198 | -14 | 4 | 17 | 201  | 225  | 11  | 5 | 17 | 72  | 63   |
| 9   | 0 | 17 | 314  | 315  | 2   | 2 | 17 | 790  | 799  | -13 | 4 | 17 | 20   | 3    | 12  | 5 | 17 | -15 | 0    |
| 11  | 0 | 17 | 31   | 37   | 3   | 2 | 17 | 147  | 154  | -12 | 4 | 17 | 684  | 630  | 13  | 5 | 17 | 8   | 1    |
| 13  | 0 | 17 | 78   | 25   | 4   | 2 | 17 | 822  | 820  | -11 | 4 | 17 | 45   | 34   | 14  | 5 | 17 | 25  | 37   |
| 15  | 0 | 17 | 88   | 36   | 5   | 2 | 17 | 1183 | 1162 | -10 | 4 | 17 | 872  | 886  | 15  | 5 | 17 | 40  | 17   |
| 17  | 0 | 17 | -3   | 14   | 6   | 2 | 17 | 52   | 46   | -9  | 4 | 17 | 9    | 12   | 16  | 5 | 17 | -31 | 3    |
| -21 | 1 | 17 | -1   | 43   | 7   | 2 | 17 | 84   | 91   | -8  | 4 | 17 | 137  | 108  | 17  | 5 | 17 | 72  | 16   |
| -20 | 1 | 17 | 202  | 287  | 8   | 2 | 17 | 1216 | 1281 | -7  | 4 | 17 | 632  | 602  | 18  | 5 | 17 | 51  | 43   |
| -19 | 1 | 17 | 101  | 57   | 9   | 2 | 17 | 440  | 494  | -6  | 4 | 17 | 23   | 3    | 19  | 5 | 17 | -29 | 41   |
| -18 | 1 | 17 | 373  | 359  | 10  | 2 | 17 | 574  | 604  | -5  | 4 | 17 | 1472 | 1382 | -20 | 6 | 17 | 162 | 51   |
| -17 | 1 | 17 | 104  | 48   | 11  | 2 | 17 | 45   | 35   | -4  | 4 | 17 | 2446 | 2696 | -19 | 6 | 17 | -4  | 20   |
| -16 | 1 | 17 | 666  | 592  | 12  | 2 | 17 | 384  | 334  | -3  | 4 | 17 | 117  | 109  | -18 | 6 | 17 | -1  | 5    |
| -15 | 1 | 17 | 195  | 220  | 13  | 2 | 17 | 156  | 182  | -2  | 4 | 17 | 885  | 1028 | -17 | 6 | 17 | 146 | 157  |
| -14 | 1 | 17 | 79   | 50   | 14  | 2 | 17 | 276  | 261  | -1  | 4 | 17 | 13   | 13   | -16 | 6 | 17 | 236 | 167  |
| -13 | 1 | 17 | 155  | 109  | 15  | 2 | 17 | 219  | 236  | 0   | 4 | 17 | 1738 | 1496 | -15 | 6 | 17 | 62  | 53   |
| -12 | 1 | 17 | 34   | 18   | 16  | 2 | 17 | 164  | 147  | 1   | 4 | 17 | 22   | 26   | -14 | 6 | 17 | -8  | 13   |
| -11 | 1 | 17 | 380  | 336  | 17  | 2 | 17 | -31  | 17   | 2   | 4 | 17 | 1777 | 1853 | -13 | 6 | 17 | 63  | 75   |
| -10 | 1 | 17 | 369  | 344  | -20 | 3 | 17 | 11   | 1    | 3   | 4 | 17 | 418  | 458  | -12 | 6 | 17 | 131 | 131  |
| -9  | 1 | 17 | 194  | 185  | -19 | 3 | 17 | 176  | 189  | 4   | 4 | 17 | 294  | 312  | -10 | 6 | 17 | 155 | 172  |
| -8  | 1 | 17 | 849  | 758  | -18 | 3 | 17 | 48   | 2    | 5   | 4 | 17 | 7    | 2    | -10 | 6 | 17 | 48  | 48   |
| -7  | 1 | 17 | 100  | 95   | -17 | 3 | 17 | 284  | 246  | 6   | 4 | 17 | 18   | 4    | -9  | 6 | 17 | 318 | 269  |
| -6  | 1 | 17 | 789  | 817  | -16 | 3 | 17 | 0    | 7    | 17  | 4 | 17 | 461  | 428  | -8  | 6 | 17 | 14  | 19   |
| -5  | 1 | 17 | 273  | 320  | -15 | 3 | 17 | 467  | 457  | 8   | 4 | 17 | 594  | 579  | -7  | 6 | 17 | 203 | 173  |
| -4  | 1 | 17 | 1483 | 1377 | -14 | 3 | 17 | 208  | 223  | 9   | 4 | 17 | 179  | 202  | -6  | 6 | 17 | 393 | 358  |
| -3  | 1 | 17 | 566  | 610  | -13 | 3 | 17 | 799  | 754  | 10  | 4 | 17 | 179  | 134  | -5  | 6 | 17 | 16  | 12   |
| -2  | 1 | 17 | 903  | 929  | -12 | 3 | 17 | 315  | 329  | 11  | 4 | 17 | 25   | 2    | -4  | 6 | 17 | 170 | 161  |
| -1  | 1 | 17 | 20   | 6    | -11 | 3 | 17 | 302  | 307  | 12  | 4 | 17 | 92   | 86   | -3  | 6 | 17 | 330 | 305  |
| 0   | 1 | 17 | 508  | 515  | -10 | 3 | 17 | 330  | 379  | 13  | 4 | 17 | 18   | 6    | -2  | 6 | 17 | -10 | 1    |
| 1   | 1 | 17 | 68   | 67   | -9  | 3 | 17 | 251  | 245  | 14  | 4 | 17 | 86   | 71   | -1  | 6 | 17 | 6   | 3    |
| 2   | 1 | 17 | 758  | 881  | -8  | 3 | 17 | -1   | 1    | 15  | 4 | 17 | 45   | 42   | 0   | 6 | 17 | 394 | 429  |
| 3   | 1 | 17 | 52   | 41   | -7  | 3 | 17 | 4402 | 4219 | 16  | 4 | 17 | 121  | 91   | 1   | 6 | 17 | 21  | 13   |
| 4   | 1 | 17 | 475  | 468  | -6  | 3 | 17 | 53   | 65   | 17  | 4 | 17 | -33  | 0    | 2   | 6 | 17 | 21  | 1    |
| 5   | 1 | 17 | 34   | 38   | -5  | 3 | 17 | 566  | 609  | 18  | 4 | 17 | 13   | 5    | 3   | 6 | 17 | 32  | 24   |
| 6   | 1 | 17 | 307  | 308  | -4  | 3 | 17 | 253  | 211  | 19  | 4 | 17 | 11   | 3    | 4   | 6 | 17 | 120 | 135  |
| 7   | 1 | 17 | 771  | 808  | -3  | 3 | 17 | 873  | 843  | 20  | 4 | 17 | 128  | 167  | 5   | 6 | 17 | 148 | 153  |
| 8   | 1 | 17 | 476  | 484  | -2  | 3 | 17 | 369  | 346  | -20 | 5 | 17 | 175  | 37   | 6   | 6 | 17 | 126 | 92   |
| 9   | 1 | 17 | 1037 | 1008 | -1  | 3 | 17 | 894  | 788  | -19 | 5 | 17 | -10  | 1    | 7   | 6 | 17 | 9   | 15   |
| 10  | 1 | 17 | -5   | 5    | 0   | 3 | 17 | 54   | 50   | -18 | 5 | 17 | 6    | 14   | 8   | 6 | 17 | 50  | 72   |
| 11  | 1 | 17 | 62   | 47   | 1   | 3 | 17 | 88   | 75   | -17 | 5 | 17 | 42   | 2    | 9   | 6 | 17 | 127 | 156  |
| 12  | 1 | 17 | 14   | 1    | 2   | 3 | 17 | 521  | 478  | -16 | 5 | 17 | 13   | 18   | 10  | 6 | 17 | 242 | 203  |
| 13  | 1 | 17 | 44   | 47   | 3   | 3 | 17 | 194  | 174  | -15 | 5 | 17 | 149  | 194  | 11  | 6 | 17 | 56  | 69   |
| 14  | 1 | 17 | 290  | 255  | 4   | 3 | 17 | 126  | 85   | -14 | 5 | 17 | 147  | 110  | 12  | 6 | 17 | 21  | 26   |
| 15  | 1 | 17 | 66   | 12   | 5   | 3 | 17 | 605  | 618  | -13 | 5 | 17 | 0    | 4    | 13  | 6 | 17 | 108 | 117  |
| 16  | 1 | 17 | -2   | 18   | 6   | 3 | 17 | 28   | 0    | -12 | 5 | 17 | -53  | 54   | 14  | 6 | 17 | 57  | 81   |
| 17  | 1 | 17 | -10  | 14   | 7   | 3 | 17 | 392  | 357  | -11 | 5 | 17 | -3   | 4    | 15  | 6 | 17 | 135 | 101  |
| -20 | 2 | 17 | 51   | 54   | 8   | 3 | 17 | 279  | 300  | -10 | 5 | 17 | 116  | 130  | 16  | 6 | 17 | -18 | 0    |
| -19 | 2 | 17 | 102  | 51   | 9   | 3 | 17 | -5   | 15   | -9  | 5 | 17 | 8    | 3    | 17  | 6 | 17 | 45  | 14   |
| -18 | 2 | 17 | 38   | 38   | 10  | 3 | 17 | 39   | 25   | -8  | 5 | 17 | 399  | 387  | -19 | 7 | 17 | 160 | 12   |
| -17 | 2 | 17 | 43   | 36   | 11  | 3 | 17 | 13   | 0    | -7  | 5 | 17 | 367  | 401  | -18 | 7 | 17 | 22  | 81   |
| -16 | 2 | 17 | 138  | 182  | 12  | 3 | 17 | 88   | 25   | -6  | 5 | 17 | 359  | 303  | -17 | 7 | 17 | 2   | 2    |
| -15 | 2 | 17 | 576  | 593  | 13  | 3 | 17 | -20  | 3    | -5  | 5 | 17 | 558  | 543  | -16 | 7 | 17 | 9   | 4    |
| -14 | 2 | 17 | 275  | 283  | 14  | 3 | 17 | 94   | 80   | -4  | 5 | 17 | 18   | 34   | -15 | 7 | 17 | 42  | 1    |
| -13 | 2 | 17 | 111  | 88   | 15  | 3 | 17 | 2    | 5    | -3  | 5 | 17 | 21   | 3    | -14 | 7 | 17 | 124 | 108  |
| -12 | 2 | 17 | 849  | 887  | 16  | 3 | 17 | 58   | 47   | -2  | 5 | 17 | 171  | 159  | -13 | 7 | 17 | -5  | 1    |
| -11 | 2 | 17 | 64   | 50   | 17  | 3 | 17 | 3    | 0    | -1  | 5 | 17 | 77   | 63   | -12 | 7 | 17 | 208 | 154  |
| -10 | 2 | 17 | 643  | 595  | 18  | 3 | 17 | 153  | 12   | 0   | 5 | 17 | 33   | 36   | -11 | 7 | 17 | 108 | 97   |
| -9  | 2 | 17 | 2901 | 2910 | 19  | 3 | 17 | 40   | 31   | 1   | 5 | 17 | 29   | 34   | -10 | 7 | 17 | 210 | 258  |
| -8  | 2 | 17 | 1445 | 1434 | 20  | 3 | 17 | 169  | 11   | 2   | 5 | 17 | 48   | 35   | -9  | 7 | 17 | 79  | 14   |
| -7  | 2 | 17 | 228  | 218  | 21  | 3 | 17 | -29  | 5    | 3   | 5 | 17 | 24   | 10   | -8  | 7 | 17 | 381 | 367  |
| -6  | 2 | 17 | 24   | 36   | 6   | 0 | 18 | 5721 | 5527 | 2   | 2 | 18 | 251  | 218  | -13 | 4 | 18 | 173 | 154  |
| -5  | 2 | 17 | 2    | 2    | 8   | 0 | 18 | 2866 | 2527 | 3   | 2 | 18 | 645  | 670  | -12 | 4 | 18 | 14  | 2    |
| -4  | 2 | 17 | 7    | 0    | 10  | 0 | 18 | 2034 | 1941 | 4   | 2 | 18 | 835  | 844  | -11 | 4 | 18 | 135 | 132  |
| -3  | 2 | 17 | 64   | 85   | 12  | 0 | 18 | 570  | 590  | 5   | 2 | 18 | 213  | 232  | -10 | 4 | 18 | -2  | 0    |
| -2  | 2 | 17 | 15   | 17   | 14  | 0 | 18 | 761  | 729  | 6   | 2 | 18 | 132  | 123  | -9  | 4 | 18 | 132 | 119  |
| -1  | 2 | 17 | 24   | 26   | 16  | 0 | 18 | 141  | 167  | 7   | 2 | 18 | 26   | 57   | -8  | 4 | 18 | 389 | 389  |
| 0   | 2 | 17 | 29   | 15   | -20 | 1 | 18 | 42   | 73   | 8   | 2 | 18 | 22   | 10   | -7  | 4 | 18 | 380 | 350  |
| 1   | 2 | 17 | 27   | 17   | -19 | 1 | 18 | 168  | 134  | 9   | 2 | 18 | 1035 | 1032 | -6  | 4 | 18 | 329 | 349  |
| 2   | 2 | 17 | 38   | 45   | -18 | 1 | 18 | 121  | 111  | 10  | 2 | 18 | 333  | 338  | -5  | 4 | 18 | 202 | 203  |
| 3   | 2 | 17 | 5    | 6    | -17 | 1 |    |      |      |     |   |    |      |      |     |   |    |     |      |

Table B.3, continued

| M   | K  | L  | Obs  | Calc | M   | K  | L  | Obs  | Calc | M   | K | L  | Obs | Calc | M   | K  | L  | Obs  | Calc | M   | K  | L   | Obs | Calc |
|-----|----|----|------|------|-----|----|----|------|------|-----|---|----|-----|------|-----|----|----|------|------|-----|----|-----|-----|------|
| -8  | 10 | 17 | -24  | 0    | 1   | 1  | 18 | 0    | 2    | -10 | 3 | 18 | 132 | 106  | 14  | 4  | 18 | 43   | 29   | 1   | 6  | 18  | 25  | 26   |
| -7  | 10 | 17 | 11   | 0    | 2   | 1  | 18 | 27   | 26   | -9  | 3 | 18 | 55  | 58   | 15  | 4  | 18 | 63   | 84   | 2   | 6  | 18  | 102 | 54   |
| -6  | 10 | 17 | 8    | 2    | 3   | 1  | 18 | 264  | 241  | -8  | 3 | 18 | 408 | 386  | 16  | 4  | 18 | 26   | 53   | 3   | 6  | 18  | -19 | 6    |
| -5  | 10 | 17 | 34   | 3    | 4   | 1  | 18 | 20   | 18   | -7  | 3 | 18 | -6  | 12   | 17  | 4  | 18 | 32   | 41   | 4   | 6  | 18  | 545 | 549  |
| -4  | 10 | 17 | 56   | 20   | 5   | 1  | 18 | 89   | 86   | -6  | 3 | 18 | 995 | 995  | 18  | 4  | 18 | 156  | 29   | 5   | 6  | 18  | 93  | 87   |
| -3  | 10 | 17 | 2    | 1    | 6   | 1  | 18 | 19   | 25   | -5  | 3 | 18 | -12 | 17   | 18  | 4  | 18 | 126  | 16   | 6   | 6  | 18  | 171 | 152  |
| -2  | 10 | 17 | 9    | 3    | 7   | 1  | 18 | 579  | 543  | -4  | 3 | 18 | 12  | 2    | 20  | 4  | 18 | -94  | 2    | 7   | 6  | 18  | 13  | 3    |
| -1  | 10 | 17 | -3   | 0    | 8   | 1  | 18 | 1244 | 1217 | -3  | 3 | 18 | 127 | 133  | -20 | 5  | 18 | -29  | 43   | 8   | 6  | 18  | 33  | 12   |
| 0   | 10 | 17 | -4   | 2    | 9   | 1  | 18 | 53   | 36   | -2  | 3 | 18 | 134 | 133  | -19 | 5  | 18 | 161  | 59   | 9   | 6  | 18  | 9   | 4    |
| 1   | 10 | 17 | 29   | 4    | 10  | 1  | 18 | 220  | 190  | -1  | 3 | 18 | 69  | 67   | -18 | 5  | 18 | 121  | 6    | 10  | 6  | 18  | 0   | 27   |
| 2   | 10 | 17 | 29   | 0    | 11  | 1  | 18 | 65   | 58   | 0   | 3 | 18 | 64  | 70   | -17 | 5  | 18 | 70   | 26   | 11  | 6  | 18  | 122 | 86   |
| 3   | 10 | 17 | 11   | 10   | 12  | 1  | 18 | 25   | 45   | 1   | 3 | 18 | 98  | 81   | -16 | 5  | 18 | 43   | 109  | 12  | 6  | 18  | 24  | 6    |
| 4   | 10 | 17 | 28   | 16   | 13  | 1  | 18 | 188  | 246  | 2   | 3 | 18 | 28  | 18   | -15 | 5  | 18 | 50   | 29   | 13  | 6  | 18  | 36  | 59   |
| 5   | 10 | 17 | 41   | 3    | 14  | 1  | 18 | 70   | 20   | 3   | 3 | 18 | 76  | 74   | -14 | 5  | 18 | 142  | 192  | 14  | 6  | 18  | 70  | 40   |
| 6   | 10 | 17 | -12  | 13   | 15  | 1  | 18 | -33  | 39   | 4   | 3 | 18 | 87  | 75   | -13 | 5  | 18 | 13   | 3    | 15  | 6  | 18  | 29  | 0    |
| 7   | 10 | 17 | 50   | 3    | 16  | 1  | 18 | 41   | 27   | 5   | 3 | 18 | 580 | 594  | -12 | 5  | 18 | 41   | 10   | 16  | 6  | 18  | 82  | 2    |
| 8   | 10 | 17 | 9    | 3    | 17  | 1  | 18 | 0    | 0    | 6   | 3 | 18 | 950 | 853  | -11 | 5  | 18 | 224  | 239  | 17  | 6  | 18  | 9   | 4    |
| -3  | 11 | 17 | 6    | 0    | -20 | 2  | 18 | 3    | 23   | 7   | 3 | 18 | -16 | 0    | -10 | 5  | 18 | 23   | 1    | -19 | 7  | 18  | 451 | 64   |
| -2  | 11 | 17 | 24   | 0    | -19 | 2  | 18 | 63   | 38   | 8   | 3 | 18 | -2  | 7    | -9  | 5  | 18 | 81   | 82   | -18 | 7  | 18  | 134 | 34   |
| -1  | 11 | 17 | 70   | 19   | -18 | 2  | 18 | 88   | 70   | 9   | 3 | 18 | -1  | 0    | -8  | 5  | 18 | 145  | 181  | -17 | 7  | 18  | 96  | 4    |
| 0   | 11 | 17 | 16   | 5    | -17 | 2  | 18 | 74   | 100  | 10  | 3 | 18 | 54  | 0    | -7  | 5  | 18 | 590  | 623  | -16 | 7  | 18  | 36  | 16   |
| 1   | 11 | 17 | 32   | 4    | -16 | 2  | 18 | 161  | 170  | 11  | 3 | 18 | 57  | 50   | -6  | 5  | 18 | 70   | 83   | -15 | 7  | 18  | 41  | 17   |
| 2   | 11 | 17 | -20  | 12   | -15 | 2  | 18 | 130  | 131  | 12  | 3 | 18 | 20  | 0    | -5  | 5  | 18 | -2   | 1    | -14 | 7  | 18  | 26  | 23   |
| 3   | 11 | 17 | 14   | 22   | -14 | 2  | 18 | 37   | 57   | 13  | 3 | 18 | 60  | 65   | -4  | 5  | 18 | 36   | 12   | -13 | 7  | 18  | 53  | 92   |
| 4   | 11 | 17 | 54   | 8    | -13 | 2  | 18 | 64   | 48   | 14  | 3 | 18 | -7  | 0    | -3  | 5  | 18 | 574  | 558  | -12 | 7  | 18  | 32  | 58   |
| 5   | 11 | 17 | 41   | 1    | -12 | 2  | 18 | 82   | 72   | 15  | 3 | 18 | 49  | 1    | -2  | 5  | 18 | 92   | 87   | -11 | 7  | 18  | 28  | 20   |
| -20 | 0  | 18 | 46   | 226  | -11 | 2  | 18 | 451  | 464  | 16  | 3 | 18 | 27  | 8    | -1  | 5  | 18 | 12   | 44   | -10 | 7  | 18  | 52  | 41   |
| -18 | 0  | 18 | 132  | 67   | -10 | 2  | 18 | 1522 | 1430 | 17  | 3 | 18 | -24 | 26   | 0   | 5  | 18 | 56   | 61   | -9  | 7  | 18  | 94  | 97   |
| -16 | 0  | 18 | 593  | 639  | -9  | 2  | 18 | 121  | 117  | 18  | 3 | 18 | -12 | 4    | 1   | 5  | 18 | 9    | 21   | -8  | 7  | 18  | 48  | 12   |
| -14 | 0  | 18 | 157  | 158  | -8  | 2  | 18 | 1138 | 1137 | 19  | 3 | 18 | -52 | 11   | 2   | 5  | 18 | -14  | 1    | -7  | 7  | 18  | 39  | 38   |
| -12 | 0  | 18 | 141  | 107  | -7  | 2  | 18 | 1480 | 1486 | 20  | 3 | 18 | 116 | 1    | 3   | 5  | 18 | 79   | 110  | -6  | 7  | 18  | 163 | 186  |
| -10 | 0  | 18 | 1580 | 1473 | -6  | 2  | 18 | 431  | 432  | 21  | 3 | 18 | -82 | 25   | 4   | 5  | 18 | 24   | 4    | -5  | 7  | 18  | 19  | 15   |
| -8  | 0  | 18 | 1576 | 1578 | -5  | 2  | 18 | 1086 | 940  | -20 | 4 | 18 | -46 | 10   | 5   | 5  | 18 | 5    | 1    | -4  | 7  | 18  | 17  | 29   |
| -6  | 0  | 18 | 1274 | 1327 | -4  | 2  | 18 | 480  | 436  | -19 | 4 | 18 | -35 | 24   | 6   | 5  | 18 | 154  | 139  | -3  | 7  | 18  | 120 | 128  |
| -4  | 0  | 18 | 3691 | 3696 | -3  | 2  | 18 | 533  | 466  | -18 | 4 | 18 | 12  | 53   | 7   | 5  | 18 | 257  | 263  | -2  | 7  | 18  | 1   | 1    |
| -2  | 0  | 18 | 386  | 409  | -2  | 2  | 18 | 86   | 73   | -17 | 4 | 18 | 106 | 84   | 8   | 5  | 18 | -15  | 0    | -1  | 7  | 18  | 578 | 668  |
| 0   | 0  | 18 | 247  | 142  | -1  | 2  | 18 | 1114 | 1092 | -16 | 4 | 18 | 16  | 39   | 9   | 5  | 18 | 26   | 2    | 0   | 7  | 18  | 79  | 83   |
| 2   | 0  | 18 | 3375 | 2976 | 0   | 2  | 18 | 20   | 50   | -15 | 4 | 18 | 745 | 735  | 10  | 5  | 18 | 24   | 12   | 1   | 7  | 18  | 66  | 64   |
| 4   | 0  | 18 | 3867 | 3789 | 1   | 2  | 18 | 444  | 400  | -14 | 4 | 18 | 36  | 16   | 11  | 5  | 18 | 11   | 8    | 2   | 7  | 18  | 15  | 4    |
| 3   | 7  | 18 | 243  | 165  | 4   | 9  | 18 | 6    | 0    | -12 | 1 | 18 | 106 | 107  | 17  | 2  | 18 | 28   | 45   | -1  | 4  | 19  | 262 | 240  |
| 4   | 7  | 18 | 4    | 0    | 5   | 9  | 18 | 2    | 1    | -11 | 1 | 18 | 11  | 8    | 18  | 2  | 18 | 86   | 6    | 0   | 19 | 305 | 250 |      |
| 5   | 7  | 18 | 19   | 1    | 6   | 9  | 18 | 6    | 1    | -10 | 1 | 18 | 390 | 369  | 19  | 2  | 18 | 13   | 1    | 1   | 4  | 19  | 21  | 7    |
| 6   | 7  | 18 | -2   | 0    | 7   | 9  | 18 | -26  | 0    | -9  | 1 | 18 | 22  | 25   | 20  | 2  | 18 | -22  | 12   | 2   | 4  | 19  | 269 | 231  |
| 7   | 7  | 18 | -2   | 3    | 8   | 9  | 18 | 32   | 16   | -8  | 1 | 18 | 74  | 70   | 21  | 2  | 18 | 65   | 59   | 3   | 4  | 19  | 36  | 4    |
| 8   | 7  | 18 | 12   | 4    | 9   | 9  | 18 | 41   | 2    | -7  | 1 | 18 | 89  | 110  | -20 | 3  | 18 | 29   | 3    | 4   | 4  | 19  | 28  | 11   |
| 9   | 7  | 18 | 7    | 11   | 10  | 9  | 18 | -1   | 1    | -6  | 1 | 18 | 677 | 649  | -19 | 3  | 18 | 105  | 136  | 5   | 4  | 19  | -16 | 0    |
| 10  | 7  | 18 | 12   | 16   | 11  | 9  | 18 | -4   | 40   | -5  | 1 | 18 | 15  | 23   | -18 | 3  | 18 | 69   | 13   | 6   | 4  | 19  | 366 | 390  |
| 11  | 7  | 18 | 57   | 38   | 12  | 9  | 18 | 109  | 19   | -4  | 1 | 18 | 175 | 207  | -17 | 3  | 18 | 86   | 87   | 7   | 4  | 19  | 198 | 158  |
| 12  | 7  | 18 | 74   | 62   | -11 | 10 | 18 | 65   | 4    | -3  | 1 | 18 | 29  | 25   | -16 | 3  | 18 | 88   | 80   | 8   | 4  | 19  | 160 | 148  |
| 13  | 7  | 18 | 48   | 6    | -10 | 10 | 18 | -8   | 1    | -2  | 1 | 18 | 182 | 189  | -15 | 3  | 18 | 142  | 156  | 9   | 4  | 19  | 49  | 10   |
| 14  | 7  | 18 | 1    | 23   | -9  | 10 | 18 | -7   | 10   | -1  | 1 | 18 | 16  | 0    | -14 | 3  | 18 | 12   | 0    | 10  | 4  | 19  | 143 | 150  |
| 15  | 7  | 18 | -20  | 10   | -8  | 10 | 18 | -26  | 8    | 0   | 1 | 18 | 56  | 59   | -13 | 3  | 18 | 94   | 81   | 11  | 4  | 19  | -1  | 4    |
| -17 | 8  | 18 | -4   | 0    | -7  | 10 | 18 | 17   | 37   | 1   | 1 | 18 | 4   | 36   | -12 | 3  | 18 | 15   | 4    | 12  | 4  | 19  | 61  | 9    |
| -16 | 8  | 18 | 73   | 46   | -6  | 10 | 18 | 12   | 6    | 2   | 1 | 18 | 388 | 354  | -11 | 3  | 18 | 140  | 131  | 13  | 4  | 19  | 95  | 71   |
| -15 | 8  | 18 | 36   | 24   | -5  | 10 | 18 | 21   | 10   | 3   | 1 | 18 | 80  | 87   | -10 | 3  | 18 | 0    | 11   | 14  | 4  | 19  | 97  | 81   |
| -14 | 8  | 18 | 2    | 0    | -4  | 10 | 18 | 37   | 10   | 4   | 1 | 18 | 180 | 187  | -9  | 3  | 18 | 378  | 383  | 15  | 4  | 19  | 57  | 3    |
| -13 | 8  | 18 | 15   | 39   | -3  | 10 | 18 | 0    | 1    | 5   | 1 | 18 | 27  | 15   | -8  | 3  | 18 | 27   | 50   | 16  | 4  | 19  | 81  | 76   |
| -12 | 8  | 18 | 138  | 149  | -2  | 10 | 18 | 82   | 46   | 6   | 1 | 18 | 977 | 929  | -7  | 3  | 18 | 1520 | 1443 | 17  | 4  | 19  | -27 | 3    |
| -11 | 8  | 18 | 15   | 11   | -1  | 10 | 18 | 0    | 0    | 7   | 1 | 18 | 29  | 6    | -6  | 3  | 18 | 39   | 26   | 18  | 4  | 19  | -11 | 43   |
| -10 | 8  | 18 | 112  | 122  | 0   | 10 | 18 | 13   | 2    | 8   | 1 | 18 | 71  | 58   | -5  | 3  | 18 | 66   | 69   | 19  | 4  | 19  | 38  | 66   |
| -9  | 8  | 18 | 0    | 0    | 1   | 10 | 18 | 19   | 2    | 9   | 1 | 18 | -11 | 0    | -4  | 3  | 18 | 450  | 443  | 20  | 4  | 19  | 28  | 73   |
| -8  | 8  | 18 | 116  | 82   | 2   | 10 | 18 | 43   | 9    | 10  | 1 | 18 | -1  | 2    | -3  | 3  | 18 | 231  | 227  | -19 | 5  | 19  | 28  | 25   |
| -7  | 8  | 18 | 27   | 0    | 3   | 10 | 18 | 24   | 19   | 11  | 1 | 18 | 359 | 385  | -2  | 3  | 18 | 52   | 25   | -18 | 5  | 19  | 47  | 44   |
| -6  | 8  | 18 | 295  | 258  | 4   | 10 | 18 | 24   | 50   | 12  | 1 | 18 | 18  | 2    | -1  | 3  | 18 | 40   | 32   | -17 | 5  | 19  | 29  | 0    |
| -5  | 8  | 18 | 10   | 4    | 5   | 10 | 18 | -2   | 19   | 13  | 1 | 18 | 47  | 78   | 0   | 19 | 14 | 30   | 10   | -16 | 5  | 19  | 15  | 5    |
| -4  | 8  | 18 | 273  | 311  | 6   | 10 | 18 | -10  | 6    | 14  | 1 | 18 | 32  | 0    | 1   | 3  | 18 | 38   | 24   | -15 | 5  | 19  | 192 | 223  |
| -3  | 8  | 18 | 216  | 265  | 7   | 10 | 18 | 0    | 17   | 15  | 1 | 18 | 119 | 55   | 2   | 3  | 18 | 83   | 39   | -14 | 5  | 19  | 225 | 280  |
| -2  | 8  | 18 | -8   | 1    | 8   | 10 | 18 | 96   | 12   | 16  | 1 | 18 | -2  | 24   | 3   | 3  | 18 | 30   | 1    | -13 | 5  | 19  | 34  | 28   |
| -1  | 8  | 18 | -6   | 0    | -4  | 11 | 18 | -22  | 4    | -20 | 2 | 18 | 76  | 95   | 4   | 3  | 18 | 18   | 9    | -12 | 5  | 19  | 12  | 1    |
| 0   | 8  | 18 | 146  | 103  | -3  | 11 | 18 | -56  | 19   | -19 | 2 | 18 | 83  | 126  | 5   | 3  | 18 | 309  | 279  | -11 | 5  | 19  | 49  | 44   |

Table B.3, continued

| M   | K | L  | Obs | Calc | M   | K  | L  | Obs | Calc | M   | K  | L  | Obs  | Calc | M   | K  | L  | Obs  | Calc | M   | K   | L  | Obs  | Calc |
|-----|---|----|-----|------|-----|----|----|-----|------|-----|----|----|------|------|-----|----|----|------|------|-----|-----|----|------|------|
| 2   | 9 | 10 | 8   | 1    | -14 | 1  | 19 | 346 | 349  | 15  | 2  | 19 | 7    | 1    | -3  | 4  | 19 | 1170 | 1101 | -15 | 6   | 19 | 45   | 56   |
| 3   | 9 | 10 | 6   | 0    | -13 | 1  | 19 | 173 | 203  | 16  | 2  | 19 | 93   | 99   | -2  | 4  | 19 | 324  | 316  | -14 | 6   | 19 | -10  | 17   |
| -13 | 6 | 19 | 54  | 29   | -17 | 0  | 19 | 10  | 31   | -5  | 10 | 19 | 25   | 21   | 3   | 1  | 20 | 34   | 11   | -7  | 3   | 20 | 115  | 122  |
| -12 | 6 | 19 | 3   | 0    | -16 | 0  | 19 | -41 | 13   | -4  | 10 | 19 | 52   | 25   | 4   | 1  | 20 | 44   | 29   | -6  | 3   | 20 | 135  | 223  |
| -11 | 6 | 19 | 88  | 134  | -15 | 0  | 19 | 18  | 1    | -3  | 10 | 19 | 5    | 0    | 5   | 1  | 20 | 23   | 3    | -5  | 3   | 20 | 72   | 60   |
| -10 | 6 | 19 | 113 | 104  | -14 | 0  | 19 | 15  | 3    | -2  | 10 | 19 | 42   | 25   | 6   | 1  | 20 | 588  | 575  | -4  | 3   | 20 | 29   | 13   |
| -9  | 6 | 19 | 32  | 20   | -13 | 0  | 19 | 98  | 36   | -1  | 10 | 19 | 12   | 11   | 7   | 1  | 20 | 38   | 11   | -3  | 3   | 20 | 30   | 2    |
| -8  | 6 | 19 | 180 | 205  | -12 | 0  | 19 | 7   | 20   | 0   | 10 | 19 | 34   | 3    | 8   | 1  | 20 | 200  | 186  | -2  | 3   | 20 | 256  | 245  |
| -7  | 6 | 19 | 23  | 35   | -11 | 0  | 19 | 12  | 2    | 1   | 10 | 19 | 25   | 21   | 9   | 1  | 20 | 358  | 396  | -1  | 3   | 20 | 74   | 43   |
| -6  | 6 | 19 | 53  | 35   | -10 | 0  | 19 | 40  | 60   | 2   | 10 | 19 | 11   | 29   | 10  | 1  | 20 | 13   | 14   | 0   | 3   | 20 | 17   | 3    |
| -5  | 6 | 19 | 212 | 176  | -9  | 0  | 19 | 68  | 73   | 3   | 10 | 19 | -25  | 13   | 11  | 1  | 20 | 35   | 30   | -1  | 3   | 20 | 5    | 4    |
| -4  | 6 | 19 | 744 | 768  | -8  | 0  | 19 | 4   | 0    | 4   | 10 | 19 | 32   | 17   | 12  | 1  | 20 | 99   | 77   | 2   | 3   | 20 | 37   | 22   |
| -3  | 6 | 19 | 45  | 54   | -7  | 0  | 19 | 26  | 5    | 10  | 19 | 12 | 8    | 13   | 1   | 20 | 91 | 84   | 3    | 3   | 20  | 52 | 56   |      |
| -2  | 6 | 19 | 133 | 131  | -6  | 0  | 19 | 30  | 2    | 6   | 10 | 19 | 19   | 0    | 14  | 1  | 20 | -2   | 0    | 4   | 3   | 20 | 94   | 89   |
| -1  | 6 | 19 | 663 | 739  | -5  | 0  | 19 | 134 | 172  | 7   | 10 | 19 | 16   | 0    | 15  | 1  | 20 | 0    | 2    | 5   | 3   | 20 | 76   | 78   |
| 0   | 6 | 19 | 288 | 340  | -4  | 0  | 19 | 0   | 7    | 8   | 10 | 19 | -7   | 62   | 16  | 1  | 20 | -8   | 1    | 6   | 3   | 20 | 333  | 308  |
| 1   | 6 | 19 | 242 | 225  | -3  | 0  | 19 | 209 | 210  | -5  | 11 | 19 | -67  | 0    | -19 | 2  | 20 | 28   | 47   | 7   | 3   | 20 | 57   | 70   |
| 2   | 6 | 19 | 114 | 81   | -2  | 0  | 19 | 243 | 274  | -4  | 11 | 19 | 165  | 6    | -18 | 2  | 20 | 105  | 83   | 8   | 3   | 20 | 24   | 3    |
| 3   | 6 | 19 | 422 | 377  | -1  | 0  | 19 | 42  | 56   | -3  | 11 | 19 | 5    | 3    | -17 | 2  | 20 | 67   | 75   | 9   | 3   | 20 | 57   | 43   |
| 4   | 6 | 19 | 395 | 389  | 0   | 0  | 19 | 268 | 294  | -2  | 11 | 19 | 35   | 1    | -16 | 2  | 20 | 240  | 267  | 10  | 3   | 20 | 18   | 11   |
| 5   | 6 | 19 | 572 | 497  | 1   | 0  | 19 | 800 | 852  | -1  | 11 | 19 | 62   | 7    | -15 | 2  | 20 | 409  | 447  | 11  | 3   | 20 | -7   | 3    |
| 6   | 6 | 19 | 23  | 12   | 2   | 0  | 19 | 100 | 88   | 0   | 11 | 19 | 60   | 1    | -14 | 2  | 20 | 12   | 29   | 12  | 3   | 20 | -1   | 21   |
| 7   | 6 | 19 | 141 | 140  | 3   | 0  | 19 | 37  | 27   | 1   | 11 | 19 | 32   | 0    | -13 | 2  | 20 | 46   | 49   | 13  | 3   | 20 | 5    | 6    |
| 8   | 6 | 19 | 165 | 110  | 4   | 0  | 19 | 27  | 8    | 2   | 11 | 19 | 11   | 19   | -12 | 2  | 20 | 67   | 47   | 14  | 3   | 20 | 58   | 41   |
| 9   | 6 | 19 | 203 | 169  | 5   | 0  | 19 | 107 | 83   | 3   | 11 | 19 | 183  | 4    | -11 | 2  | 20 | 901  | 888  | 15  | 3   | 20 | 50   | 45   |
| 10  | 6 | 19 | 4   | 13   | 6   | 0  | 19 | 19  | 15   | 4   | 11 | 19 | 26   | 0    | -10 | 2  | 20 | 534  | 535  | 16  | 3   | 20 | 82   | 50   |
| 11  | 6 | 19 | 18  | 22   | 7   | 0  | 19 | -2  | 7    | -1  | 12 | 19 | -16  | 14   | -9  | 2  | 20 | 59   | 60   | 17  | 3   | 20 | 12   | 11   |
| 12  | 6 | 19 | -7  | 20   | 8   | 0  | 19 | -6  | 5    | 0   | 12 | 19 | 143  | 12   | -8  | 2  | 20 | 61   | 60   | 18  | 3   | 20 | -11  | 5    |
| 13  | 6 | 19 | 149 | 143  | 9   | 0  | 19 | 5   | 42   | -18 | 0  | 20 | 147  | 171  | -7  | 2  | 20 | 264  | 232  | 19  | 3   | 20 | 17   | 5    |
| 14  | 6 | 19 | 41  | 11   | 10  | 0  | 19 | 46  | 2    | -16 | 0  | 20 | 448  | 431  | -6  | 2  | 20 | 32   | 10   | 20  | 3   | 20 | 36   | 13   |
| 15  | 6 | 19 | 15  | 25   | 11  | 0  | 19 | 36  | 12   | -14 | 0  | 20 | 364  | 366  | -5  | 2  | 20 | 420  | 426  | -19 | 4   | 20 | 2    | 15   |
| 16  | 6 | 19 | 16  | 1    | 12  | 0  | 19 | 45  | 29   | -12 | 0  | 20 | 543  | 518  | -4  | 2  | 20 | 105  | 147  | -18 | 4   | 20 | 66   | 60   |
| 17  | 6 | 19 | 72  | 21   | 13  | 0  | 19 | -25 | 15   | -10 | 0  | 20 | 967  | 873  | -3  | 2  | 20 | 1131 | 1078 | -17 | 4   | 20 | 66   | 48   |
| -19 | 7 | 19 | 20  | 6    | 14  | 0  | 19 | 50  | 2    | -8  | 0  | 20 | 2637 | 2477 | -2  | 2  | 20 | 0    | 3    | -16 | 4   | 20 | -9   | 1    |
| -18 | 7 | 19 | 45  | 92   | -16 | 9  | 19 | 35  | 0    | -6  | 0  | 20 | 4278 | 3953 | -1  | 2  | 20 | 63   | 22   | 15  | 4   | 20 | 102  | 109  |
| -17 | 7 | 19 | 20  | 56   | -15 | 9  | 19 | -20 | 1    | -4  | 0  | 20 | 3906 | 3604 | 0   | 2  | 20 | 1369 | 1240 | -14 | 4   | 20 | -26  | 42   |
| -16 | 7 | 19 | 0   | 2    | -14 | 1  | 19 | -36 | 13   | -2  | 0  | 20 | 4077 | 4067 | 1   | 2  | 20 | 188  | 132  | -13 | 4   | 20 | 280  | 291  |
| -15 | 7 | 19 | -3  | 0    | -13 | 1  | 19 | 156 | 116  | 0   | 0  | 20 | 1798 | 2009 | 2   | 2  | 20 | 1345 | 1292 | -12 | 4   | 20 | 45   | 35   |
| -14 | 7 | 19 | 57  | 57   | -12 | 9  | 19 | 36  | 0    | 2   | 0  | 20 | 3142 | 3081 | 3   | 2  | 20 | 194  | 143  | -11 | 4   | 20 | 945  | 932  |
| -13 | 7 | 19 | 17  | 1    | -11 | 9  | 19 | 11  | 29   | 4   | 0  | 20 | 2470 | 2396 | 4   | 2  | 20 | 1034 | 1001 | -10 | 4   | 20 | 29   | 3    |
| -12 | 7 | 19 | 115 | 128  | -10 | 9  | 19 | 75  | 67   | 6   | 0  | 20 | 919  | 944  | 5   | 2  | 20 | 137  | 150  | -9  | 4   | 20 | 1605 | 1505 |
| -11 | 7 | 19 | 8   | 1    | -9  | 9  | 19 | 14  | 2    | 8   | 0  | 20 | 379  | 410  | 6   | 2  | 20 | 64   | 68   | -8  | 4   | 20 | 63   | 1    |
| -10 | 7 | 19 | 11  | 28   | -8  | 9  | 19 | 14  | 7    | 10  | 0  | 20 | 2290 | 2225 | 7   | 2  | 20 | 460  | 477  | -7  | 4   | 20 | 749  | 685  |
| -9  | 7 | 19 | 13  | 1    | -7  | 9  | 19 | 12  | 12   | 12  | 0  | 20 | 205  | 222  | 8   | 2  | 20 | 657  | 631  | -6  | 4   | 20 | 14   | 18   |
| -8  | 7 | 19 | 32  | 0    | -6  | 9  | 19 | 71  | 44   | 14  | 0  | 20 | 439  | 345  | 9   | 2  | 20 | 52   | 70   | -5  | 4   | 20 | 279  | 330  |
| -7  | 7 | 19 | 27  | 14   | -5  | 9  | 19 | 14  | 5    | 16  | 0  | 20 | 77   | 162  | 10  | 2  | 20 | 206  | 214  | -4  | 4   | 20 | 206  | 192  |
| -6  | 7 | 19 | 53  | 47   | -4  | 9  | 19 | 1   | 1    | -19 | 1  | 20 | 3    | 32   | 11  | 2  | 20 | 36   | 61   | -3  | 4   | 20 | 306  | 358  |
| -5  | 7 | 19 | 3   | 0    | -3  | 9  | 19 | 13  | 0    | -18 | 1  | 20 | 5    | 9    | 12  | 2  | 20 | 210  | 189  | -2  | 4   | 20 | 314  | 281  |
| -4  | 7 | 19 | 116 | 102  | -2  | 9  | 19 | 15  | 14   | -17 | 1  | 20 | 113  | 99   | 13  | 2  | 20 | 29   | 26   | -1  | 4   | 20 | 1098 | 1168 |
| -3  | 7 | 19 | 133 | 132  | -1  | 9  | 19 | 24  | 32   | -16 | 1  | 20 | 229  | 245  | 14  | 2  | 20 | 312  | 310  | 0   | 4   | 20 | -2   | 8    |
| -2  | 7 | 19 | -11 | 14   | 0   | 9  | 19 | 41  | 38   | -15 | 1  | 20 | 26   | 14   | 15  | 2  | 20 | 42   | 45   | 1   | 4   | 20 | 468  | 540  |
| -1  | 7 | 19 | 22  | 15   | 1   | 9  | 19 | 52  | 69   | -14 | 1  | 20 | 11   | 19   | 16  | 2  | 20 | 14   | 19   | 2   | 4   | 20 | 118  | 73   |
| 0   | 7 | 19 | 47  | 59   | 2   | 9  | 19 | 36  | 5    | -13 | 1  | 20 | 11   | 0    | 17  | 2  | 20 | 121  | 50   | 3   | 4   | 20 | 459  | 503  |
| 1   | 7 | 19 | 27  | 29   | 3   | 9  | 19 | 16  | 0    | -12 | 1  | 20 | 71   | 80   | 18  | 2  | 20 | 100  | 26   | 4   | 4   | 20 | 0    | 16   |
| 2   | 7 | 19 | 15  | 5    | 4   | 9  | 19 | 6   | 3    | -11 | 1  | 20 | 15   | 18   | 19  | 2  | 20 | -62  | 21   | 5   | 4   | 20 | 244  | 284  |
| 3   | 7 | 19 | 46  | 9    | 5   | 9  | 19 | 0   | 1    | -10 | 1  | 20 | 116  | 125  | 20  | 2  | 20 | -32  | 27   | 6   | 4   | 20 | 44   | 54   |
| 4   | 7 | 19 | 23  | 3    | 6   | 9  | 19 | -23 | 17   | -9  | 1  | 20 | 175  | 190  | -19 | 3  | 20 | 52   | 0    | 7   | 4   | 20 | 568  | 547  |
| 5   | 7 | 19 | -11 | 5    | 7   | 9  | 19 | 28  | 1    | -8  | 1  | 20 | 588  | 538  | -18 | 3  | 20 | 66   | 77   | 8   | 4   | 20 | 28   | 39   |
| 6   | 7 | 19 | 16  | 6    | 8   | 9  | 19 | 0   | 0    | -7  | 1  | 20 | 220  | 256  | -17 | 3  | 20 | -25  | 2    | 9   | 4   | 20 | 56   | 66   |
| 7   | 7 | 19 | -1  | 7    | 9   | 9  | 19 | 14  | 11   | -6  | 1  | 20 | 64   | 72   | -16 | 3  | 20 | 58   | 24   | 10  | 4   | 20 | -20  | 0    |
| 8   | 7 | 19 | -1  | 11   | 10  | 9  | 19 | 5   | 1    | -5  | 1  | 20 | -6   | 2    | -15 | 3  | 20 | 32   | 9    | 11  | 4   | 20 | 114  | 81   |
| 9   | 7 | 19 | 27  | 1    | 11  | 9  | 19 | 178 | 3    | -4  | 1  | 20 | 224  | 216  | -14 | 3  | 20 | 15   | 33   | 12  | 4   | 20 | 85   | 56   |
| 10  | 7 | 19 | 19  | 0    | -11 | 10 | 19 | -5  | 27   | -3  | 1  | 20 | 5    | 5    | -13 | 3  | 20 | 47   | 71   | 13  | 4   | 20 | 62   | 44   |
| 11  | 7 | 19 | -2  | 9    | -10 | 10 | 19 | 148 | 51   | -2  | 1  | 20 | 61   | 49   | -12 | 3  | 20 | 1    | 34   | 14  | 4   | 20 | 0    | 15   |
| 12  | 7 | 19 | 25  | 39   | -9  | 10 | 19 | -14 | 0    | -1  | 1  | 20 | 55   | 60   | -11 | 3  | 20 | -5   | 1    | 15  | 4   | 20 | 13   | 45   |
| 13  | 7 | 19 | 15  | 10   | -8  | 10 | 19 | 39  | 19   | 0   | 1  | 20 | 64   | 26   | -10 | 3  | 20 | 84   | 90   | 16  | 4   | 20 | 36   | 0    |
| 14  | 7 | 19 | 9   | 63   | -7  | 10 | 19 | -27 | 16   | 1   | 1  | 20 | -19  | 9    | -9  | 3  | 20 | 126  | 122  | 17  | 4   | 20 | -49  | 3    |
| 15  | 7 | 19 | 58  | 6    | -6  | 10 | 19 | 18  | 27   | 2   | 1  | 20 | 2    | 12   | -8  | 3  | 20 | 21   | 115  | -10 | 2   | 21 | 303  | 289  |
| 19  | 4 | 20 | 73  | 130  | 8   | 6  | 20 | 0   | 13   | 7   | 0  | 20 | 70   | 4    | -17 | 0  | 21 | 204  | 218  | -9  | 2   | 21 | 1193 | 1206 |
| -19 | 5 | 20 | 57  | 78   | 9   | 6  | 20 | 129 | 122  | 8   | 0  | 20 | -24  | 22   | -15 | 0  | 21 | 88   | 78   | -8  | 2</ |    |      |      |

Table B.3, continued

| H   | K | L  | Obs  | Calc | H   | K | L  | Obs | Calc | H   | K  | L  | Obs | Calc | H   | K  | L  | Obs  | Calc | H   | K | L  | Obs  | Calc | H | K | L | Obs | Calc |
|-----|---|----|------|------|-----|---|----|-----|------|-----|----|----|-----|------|-----|----|----|------|------|-----|---|----|------|------|---|---|---|-----|------|
| 15  | 5 | 20 | 47   | 4    | 8   | 7 | 20 | 45  | 7    | -9  | 10 | 20 | 23  | 19   | -2  | 1  | 21 | 10   | 1    | -15 | 3 | 21 | 26   | 79   |   |   |   |     |      |
| 16  | 5 | 20 | 3169 | 4    | 9   | 7 | 20 | -2  | 8    | -8  | 10 | 20 | 10  | 10   | -1  | 1  | 21 | 306  | 277  | -14 | 3 | 21 | -6   | 0    |   |   |   |     |      |
| 17  | 5 | 20 | -2   | 0    | 10  | 7 | 20 | 30  | 30   | -7  | 10 | 20 | 51  | 52   | 0   | 1  | 21 | 24   | 31   | -13 | 3 | 21 | 91   | 93   |   |   |   |     |      |
| 18  | 5 | 20 | -14  | 3    | 11  | 7 | 20 | 47  | 1    | -6  | 10 | 20 | -23 | 1    | 1   | 1  | 21 | 143  | 99   | -12 | 3 | 21 | 25   | 38   |   |   |   |     |      |
| -19 | 6 | 20 | 349  | 36   | 12  | 7 | 20 | 29  | 13   | -5  | 10 | 20 | 86  | 102  | 2   | 1  | 21 | 347  | 298  | -11 | 3 | 21 | 45   | 58   |   |   |   |     |      |
| -18 | 6 | 20 | 18   | 3    | 13  | 7 | 20 | 11  | 0    | -4  | 10 | 20 | 33  | 0    | 3   | 1  | 21 | 221  | 196  | -10 | 3 | 21 | 33   | 5    |   |   |   |     |      |
| -17 | 6 | 20 | 126  | 159  | 14  | 7 | 20 | 4   | 16   | -3  | 10 | 20 | 85  | 69   | 4   | 1  | 21 | 559  | 650  | -9  | 3 | 21 | 22   | 32   |   |   |   |     |      |
| -16 | 6 | 20 | 88   | 119  | 15  | 7 | 20 | 97  | 43   | -2  | 10 | 20 | 27  | 6    | 5   | 1  | 21 | 875  | 917  | -8  | 3 | 21 | -8   | 22   |   |   |   |     |      |
| -15 | 6 | 20 | 59   | 3    | -16 | 8 | 20 | 8   | 0    | -1  | 10 | 20 | 40  | 3    | 6   | 1  | 21 | 15   | 1    | -7  | 3 | 21 | 1160 | 1224 |   |   |   |     |      |
| -14 | 6 | 20 | 69   | 50   | -15 | 8 | 20 | 56  | 34   | 0   | 10 | 20 | 15  | 58   | 7   | 1  | 21 | 395  | 407  | -6  | 3 | 21 | 1048 | 1096 |   |   |   |     |      |
| -13 | 6 | 20 | 14   | 8    | -14 | 8 | 20 | -18 | 3    | 1   | 10 | 20 | -23 | 19   | 8   | 1  | 21 | 604  | 630  | -5  | 3 | 21 | 6    | 0    |   |   |   |     |      |
| -12 | 6 | 20 | 133  | 108  | -13 | 8 | 20 | -40 | 8    | 2   | 10 | 20 | 49  | 6    | 9   | 1  | 21 | 27   | 2    | -4  | 3 | 21 | 325  | 338  |   |   |   |     |      |
| -11 | 6 | 20 | 27   | 5    | -12 | 8 | 20 | 19  | 39   | 3   | 10 | 20 | 52  | 30   | 10  | 1  | 21 | 107  | 109  | -3  | 3 | 21 | 48   | 45   |   |   |   |     |      |
| -10 | 6 | 20 | 196  | 210  | -11 | 8 | 20 | 9   | 8    | 4   | 10 | 20 | 7   | 7    | 11  | 1  | 21 | 56   | 65   | -2  | 3 | 21 | 126  | 138  |   |   |   |     |      |
| -9  | 6 | 20 | 46   | 39   | -10 | 8 | 20 | 16  | 0    | 5   | 10 | 20 | 5   | 1    | 12  | 1  | 21 | -4   | 12   | -1  | 3 | 21 | 310  | 296  |   |   |   |     |      |
| -8  | 6 | 20 | 22   | 33   | -9  | 8 | 20 | 22  | 24   | 6   | 10 | 20 | -1  | 1    | 13  | 1  | 21 | 12   | 3    | 0   | 3 | 21 | 6    | 10   |   |   |   |     |      |
| -7  | 6 | 20 | 273  | 279  | -8  | 8 | 20 | 39  | 35   | 7   | 10 | 20 | 24  | 1    | 14  | 1  | 21 | 48   | 13   | 1   | 3 | 21 | 144  | 159  |   |   |   |     |      |
| -6  | 6 | 20 | 391  | 427  | -7  | 8 | 20 | 26  | 31   | -6  | 11 | 20 | 75  | 7    | 15  | 1  | 21 | 5    | 1    | 2   | 3 | 21 | 12   | 1    |   |   |   |     |      |
| -5  | 6 | 20 | 49   | 58   | -6  | 8 | 20 | 33  | 1    | -5  | 11 | 20 | -3  | 7    | 16  | 1  | 21 | 109  | 107  | 3   | 3 | 21 | 112  | 75   |   |   |   |     |      |
| -4  | 6 | 20 | 444  | 380  | -5  | 8 | 20 | 55  | 66   | -4  | 11 | 20 | 5   | 6    | 17  | 1  | 21 | 116  | 7    | 4   | 3 | 21 | 31   | 60   |   |   |   |     |      |
| -3  | 6 | 20 | 42   | 49   | -4  | 8 | 20 | 398 | 415  | -3  | 11 | 20 | -1  | 5    | 18  | 1  | 21 | -8   | 26   | 5   | 3 | 21 | 122  | 125  |   |   |   |     |      |
| -2  | 6 | 20 | 85   | 80   | -3  | 8 | 20 | 143 | 141  | -2  | 11 | 20 | -54 | 8    | 19  | 1  | 21 | -56  | 1    | 6   | 3 | 21 | 106  | 116  |   |   |   |     |      |
| -1  | 6 | 20 | 10   | 20   | -2  | 8 | 20 | 11  | 1    | -1  | 11 | 20 | -48 | 2    | -19 | 2  | 21 | 51   | 10   | 7   | 3 | 21 | 47   | 32   |   |   |   |     |      |
| 0   | 6 | 20 | 83   | 92   | -1  | 8 | 20 | 12  | 0    | 0   | 11 | 20 | 5   | 6    | -18 | 2  | 21 | 120  | 74   | 8   | 3 | 21 | 34   | 7    |   |   |   |     |      |
| 1   | 6 | 20 | 95   | 68   | 0   | 8 | 20 | 116 | 99   | 1   | 11 | 20 | 36  | 0    | -17 | 2  | 21 | 45   | 64   | 9   | 3 | 21 | 17   | 39   |   |   |   |     |      |
| 2   | 6 | 20 | 16   | 17   | 1   | 8 | 20 | 42  | 51   | 2   | 11 | 20 | -36 | 0    | -16 | 2  | 21 | 322  | 316  | 10  | 3 | 21 | -1   | 4    |   |   |   |     |      |
| 3   | 6 | 20 | 137  | 93   | 2   | 8 | 20 | 13  | 23   | 3   | 11 | 20 | -37 | 0    | -15 | 2  | 21 | 211  | 180  | 11  | 3 | 21 | 49   | 20   |   |   |   |     |      |
| 4   | 6 | 20 | 21   | 34   | 3   | 8 | 20 | 32  | 21   | 4   | 11 | 20 | 8   | 0    | -14 | 2  | 21 | 397  | 442  | 12  | 3 | 21 | -10  | 5    |   |   |   |     |      |
| 5   | 6 | 20 | 210  | 196  | 4   | 8 | 20 | 28  | 0    | -2  | 12 | 20 | -10 | 7    | -13 | 2  | 21 | 150  | 138  | 13  | 3 | 21 | 54   | 35   |   |   |   |     |      |
| 6   | 6 | 20 | 24   | 12   | 5   | 8 | 20 | -9  | 1    | -1  | 12 | 20 | 43  | 0    | -12 | 2  | 21 | 416  | 429  | 14  | 3 | 21 | 41   | 4    |   |   |   |     |      |
| 7   | 6 | 20 | 49   | 55   | 6   | 8 | 20 | -6  | 1    | 0   | 12 | 20 | 16  | 0    | -11 | 2  | 21 | 463  | 492  | 15  | 3 | 21 | 70   | 12   |   |   |   |     |      |
| 16  | 3 | 21 | 4    | 23   | 4   | 5 | 21 | 65  | 74   | -2  | 7  | 21 | 10  | 1    | 4   | 9  | 21 | 1    | 7    | -10 | 1 | 22 | 406  | 434  |   |   |   |     |      |
| 17  | 3 | 21 | 62   | 2    | 5   | 5 | 21 | 0   | 0    | -1  | 7  | 21 | 39  | 33   | 5   | 9  | 21 | 79   | 20   | -9  | 1 | 22 | 287  | 322  |   |   |   |     |      |
| 18  | 3 | 21 | -19  | 6    | 6   | 5 | 21 | 70  | 26   | 0   | 7  | 21 | 7   | 0    | 6   | 9  | 21 | 14   | 28   | -8  | 1 | 22 | 84   | 72   |   |   |   |     |      |
| 19  | 3 | 21 | 75   | 1    | 7   | 5 | 21 | 126 | 96   | 1   | 7  | 21 | 34  | 16   | 7   | 9  | 21 | 21   | 15   | -7  | 1 | 22 | 241  | 231  |   |   |   |     |      |
| 20  | 3 | 21 | -41  | 1    | 8   | 5 | 21 | 44  | 6    | 2   | 7  | 21 | 124 | 107  | 8   | 9  | 21 | -2   | 13   | -6  | 1 | 22 | 517  | 534  |   |   |   |     |      |
| -19 | 4 | 21 | -54  | 14   | 9   | 5 | 21 | -1  | 1    | 3   | 7  | 21 | 51  | 31   | 9   | 9  | 21 | 16   | 2    | -5  | 1 | 22 | 96   | 87   |   |   |   |     |      |
| -18 | 4 | 21 | 57   | 70   | 10  | 5 | 21 | 19  | 1    | 4   | 7  | 21 | 36  | 39   | 10  | 9  | 21 | 36   | 0    | -4  | 1 | 22 | 717  | 685  |   |   |   |     |      |
| -17 | 4 | 21 | 40   | 20   | 11  | 5 | 21 | -11 | 8    | 5   | 7  | 21 | 40  | 36   | -10 | 10 | 21 | 7    | 27   | -3  | 1 | 22 | 112  | 120  |   |   |   |     |      |
| -16 | 4 | 21 | 104  | 86   | 12  | 5 | 21 | 72  | 76   | 6   | 7  | 21 | -15 | 0    | -9  | 10 | 21 | -48  | 4    | -2  | 1 | 22 | 437  | 427  |   |   |   |     |      |
| -15 | 4 | 21 | 49   | 33   | 13  | 5 | 21 | -5  | 8    | 7   | 7  | 21 | 41  | 1    | -8  | 10 | 21 | 51   | 1    | -1  | 1 | 22 | 38   | 30   |   |   |   |     |      |
| -14 | 4 | 21 | 175  | 167  | 14  | 5 | 21 | -32 | 37   | 8   | 7  | 21 | 51  | 35   | -7  | 10 | 21 | -16  | 2    | 0   | 1 | 22 | 151  | 171  |   |   |   |     |      |
| -13 | 4 | 21 | 31   | 14   | 15  | 5 | 21 | 37  | 0    | 9   | 7  | 21 | 8   | 3    | -6  | 10 | 21 | 2    | 15   | 1   | 1 | 22 | 35   | 44   |   |   |   |     |      |
| -12 | 4 | 21 | 49   | 54   | 16  | 5 | 21 | 70  | 2    | 10  | 7  | 21 | 87  | 26   | -5  | 10 | 21 | 34   | 2    | 2   | 1 | 22 | 182  | 154  |   |   |   |     |      |
| -11 | 4 | 21 | 45   | 16   | 17  | 5 | 21 | -26 | 1    | 11  | 7  | 21 | 28  | 22   | -4  | 10 | 21 | 29   | 2    | 3   | 1 | 22 | 52   | 6    |   |   |   |     |      |
| -10 | 4 | 21 | 325  | 285  | 18  | 5 | 21 | 33  | 0    | 12  | 7  | 21 | -13 | 2    | -3  | 10 | 21 | 31   | 3    | 4   | 1 | 22 | 237  | 233  |   |   |   |     |      |
| -9  | 4 | 21 | 24   | 18   | -18 | 6 | 21 | 18  | 27   | 13  | 7  | 21 | -9  | 3    | -2  | 10 | 21 | 3    | 12   | 5   | 1 | 22 | 37   | 46   |   |   |   |     |      |
| -8  | 4 | 21 | 927  | 860  | -17 | 6 | 21 | 29  | 8    | 14  | 7  | 21 | 72  | 0    | -1  | 10 | 21 | 42   | 8    | 6   | 1 | 22 | 414  | 451  |   |   |   |     |      |
| -7  | 4 | 21 | 24   | 11   | -16 | 6 | 21 | 73  | 116  | -16 | 8  | 21 | -10 | 8    | 0   | 10 | 21 | -5   | 12   | 7   | 1 | 22 | 41   | 37   |   |   |   |     |      |
| -6  | 4 | 21 | -8   | 3    | -15 | 6 | 21 | 158 | 162  | -15 | 8  | 21 | -20 | 11   | 1   | 10 | 21 | 29   | 21   | 8   | 1 | 22 | 1002 | 937  |   |   |   |     |      |
| -5  | 4 | 21 | 117  | 117  | -14 | 6 | 21 | 27  | 0    | -14 | 8  | 21 | 4   | 7    | 2   | 10 | 21 | -8   | 2    | 9   | 1 | 22 | 56   | 57   |   |   |   |     |      |
| -4  | 4 | 21 | 513  | 507  | -13 | 6 | 21 | 85  | 113  | -13 | 8  | 21 | 123 | 102  | 3   | 10 | 21 | 58   | 0    | 10  | 1 | 22 | 63   | 88   |   |   |   |     |      |
| -3  | 4 | 21 | 19   | 24   | -12 | 6 | 21 | 88  | 93   | -12 | 8  | 21 | 0   | 3    | 4   | 10 | 21 | 43   | 8    | 11  | 1 | 22 | 40   | 32   |   |   |   |     |      |
| -2  | 4 | 21 | 299  | 292  | -11 | 6 | 21 | 246 | 254  | -11 | 8  | 21 | 7   | 34   | 5   | 10 | 21 | 13   | 0    | 12  | 1 | 22 | 58   | 25   |   |   |   |     |      |
| -1  | 4 | 21 | 12   | 4    | -10 | 6 | 21 | -1  | 16   | -10 | 8  | 21 | -1  | 1    | 6   | 10 | 21 | -4   | 1    | 13  | 1 | 22 | 19   | 35   |   |   |   |     |      |
| 0   | 4 | 21 | 796  | 775  | -9  | 6 | 21 | 63  | 73   | -9  | 8  | 21 | 11  | 19   | 7   | 10 | 21 | -24  | 5    | 14  | 1 | 22 | -9   | 4    |   |   |   |     |      |
| 1   | 4 | 21 | -14  | 1    | -8  | 6 | 21 | 94  | 94   | -8  | 8  | 21 | 31  | 0    | -7  | 11 | 21 | 51   | 4    | 15  | 1 | 22 | 36   | 3    |   |   |   |     |      |
| 2   | 4 | 21 | 132  | 82   | -7  | 6 | 21 | 132 | 112  | -7  | 8  | 21 | -11 | 19   | -6  | 11 | 21 | 31   | 1    | 17  | 1 | 22 | -44  | 7    |   |   |   |     |      |
| 3   | 4 | 21 | 167  | 160  | -6  | 6 | 21 | 301 | 361  | -6  | 8  | 21 | -9  | 2    | -5  | 11 | 21 | 1    | 5    | 18  | 1 | 22 | -43  | 5    |   |   |   |     |      |
| 4   | 4 | 21 | 699  | 650  | -5  | 6 | 21 | 249 | 220  | -5  | 8  | 21 | 5   | 2    | -4  | 11 | 21 | 47   | 0    | 19  | 1 | 22 | -40  | 0    |   |   |   |     |      |
| 5   | 4 | 21 | 5    | 1    | -4  | 6 | 21 | -8  | 4    | -4  | 8  | 21 | 83  | 106  | -3  | 11 | 21 | 21   | 12   | -19 | 2 | 22 | 101  | 47   |   |   |   |     |      |
| 6   | 4 | 21 | 497  | 496  | -3  | 6 | 21 | 25  | 48   | -3  | 8  | 21 | 323 | 321  | -2  | 11 | 21 | 47   | 2    | -18 | 2 | 22 | 113  | 82   |   |   |   |     |      |
| 7   | 4 | 21 | 97   | 87   | -2  | 6 | 21 | -2  | 2    | -2  | 8  | 21 | 31  | 49   | -1  | 11 | 21 | 3563 | 0    | -17 | 2 | 22 | 222  | 224  |   |   |   |     |      |
| 8   | 4 | 21 | 281  | 306  | -1  | 6 | 21 | 76  | 70   | -1  | 8  | 21 | -11 | 2    | 0   | 11 | 21 | -36  | 7    | -16 | 2 | 22 | 88   | 62   |   |   |   |     |      |
| 9   | 4 | 21 | 11   | 5    | 0   | 6 | 21 | -7  |      |     |    |    |     |      |     |    |    |      |      |     |   |    |      |      |   |   |   |     |      |

Table B.3, continued

| M   | K | L  | Obe  | Calc | M   | K | L  | Obe   | Calc | M   | K | L  | Obe | Calc | M   | K  | L  | Obe | Calc | M   | K   | L  | Obe  | Calc |     |
|-----|---|----|------|------|-----|---|----|-------|------|-----|---|----|-----|------|-----|----|----|-----|------|-----|-----|----|------|------|-----|
| -14 | 3 | 22 | 27   | 19   | 14  | 4 | 22 | 5     | 19   | 6   | 6 | 22 | 110 | 114  | 8   | 8  | 22 | 53  | 21   | -11 | 0   | 23 | 734  | 632  |     |
| -13 | 3 | 22 | 5    | 12   | 15  | 4 | 22 | 72    | 18   | 7   | 6 | 22 | 39  | 45   | 9   | 8  | 22 | -30 | 5    | -9  | 0   | 23 | 113  | 77   |     |
| -12 | 3 | 22 | 26   | 6    | 16  | 4 | 22 | 81    | 1    | 8   | 6 | 22 | 93  | 83   | 10  | 8  | 22 | 12  | 20   | -7  | 0   | 23 | 209  | 199  |     |
| -11 | 3 | 22 | 134  | 114  | 17  | 4 | 22 | 39    | 7    | 9   | 6 | 22 | 111 | 0    | 11  | 8  | 22 | 15  | 7    | -5  | 0   | 23 | 1624 | 1538 |     |
| -10 | 3 | 22 | 25   | 0    | 18  | 4 | 22 | 35    | 11   | 10  | 6 | 22 | -28 | 10   | 12  | 8  | 22 | 131 | 2    | -3  | 0   | 23 | 829  | 834  |     |
| -9  | 3 | 22 | 164  | 169  | 19  | 4 | 22 | -2    | 1    | 11  | 6 | 22 | 26  | 11   | -14 | 9  | 22 | 74  | 2    | -1  | 0   | 23 | 847  | 784  |     |
| -8  | 3 | 22 | -14  | 15   | -10 | 5 | 22 | 46    | 18   | 12  | 6 | 22 | 17  | 9    | -13 | 9  | 22 | 22  | 0    | 1   | 0   | 23 | 943  | 853  |     |
| -7  | 3 | 22 | 34   | 28   | -17 | 5 | 22 | 3     | 3    | 13  | 6 | 22 | 63  | 37   | -12 | 9  | 22 | 75  | 57   | 3   | 0   | 23 | 1312 | 1353 |     |
| -6  | 3 | 22 | 128  | 128  | -16 | 5 | 22 | -15   | 15   | 14  | 6 | 22 | 94  | 15   | -11 | 9  | 22 | 31  | 2    | 5   | 0   | 23 | 245  | 208  |     |
| -5  | 3 | 22 | 32   | 25   | -15 | 5 | 22 | -5    | 10   | 15  | 6 | 22 | 80  | 6    | -10 | 9  | 22 | 32  | 5    | 7   | 0   | 23 | 169  | 149  |     |
| -4  | 3 | 22 | 39   | 48   | -14 | 5 | 22 | -22   | 7    | 16  | 6 | 22 | -4  | 10   | -9  | 9  | 22 | -23 | 5    | 9   | 0   | 23 | 777  | 696  |     |
| -3  | 3 | 22 | 47   | 53   | -13 | 5 | 22 | 16    | 5    | -17 | 7 | 22 | 6   | 13   | -9  | 9  | 22 | -5  | 1    | 11  | 0   | 23 | 180  | 125  |     |
| -2  | 3 | 22 | 455  | 481  | -12 | 5 | 22 | -3    | 11   | -16 | 7 | 22 | 48  | 49   | -7  | 9  | 22 | 30  | 33   | 13  | 0   | 23 | 135  | 175  |     |
| -1  | 3 | 22 | 303  | 268  | -11 | 5 | 22 | -17   | 18   | -18 | 7 | 22 | 113 | 12   | -6  | 9  | 22 | 14  | 3    | 15  | 0   | 23 | 80   | 74   |     |
| 0   | 3 | 22 | 423  | 411  | -10 | 5 | 22 | 58    | 6    | -14 | 7 | 22 | 45  | 13   | -5  | 9  | 22 | 14  | 53   | 17  | 0   | 23 | 402  | 85   |     |
| 1   | 3 | 22 | 137  | 184  | -9  | 5 | 22 | 68    | 39   | -13 | 7 | 22 | -21 | 13   | -4  | 9  | 22 | 30  | 47   | -18 | 1   | 23 | -1   | 8    |     |
| 2   | 3 | 22 | 16   | 27   | -8  | 5 | 22 | 179   | 228  | -12 | 7 | 22 | 30  | 2    | -3  | 9  | 22 | 11  | 1    | -17 | 1   | 23 | 8    | 2    |     |
| 3   | 3 | 22 | 76   | 79   | -7  | 5 | 22 | -17   | 0    | -11 | 7 | 22 | 58  | 24   | -2  | 9  | 22 | 23  | 38   | -16 | 1   | 23 | 30   | 25   |     |
| 4   | 3 | 22 | -3   | 0    | -6  | 5 | 22 | 25    | 21   | -10 | 7 | 22 | 35  | 4    | -1  | 9  | 22 | 11  | 45   | -15 | 1   | 23 | 70   | 83   |     |
| 5   | 3 | 22 | 38   | 16   | -5  | 5 | 22 | 220   | 259  | -9  | 7 | 22 | 16  | 2    | 0   | 9  | 22 | 80  | 128  | -14 | 1   | 23 | 2    | 3    |     |
| 6   | 3 | 22 | 112  | 84   | -4  | 5 | 22 | 208   | 183  | -8  | 7 | 22 | -19 | 7    | 1   | 9  | 22 | 15  | 12   | -13 | 1   | 23 | 31   | 12   |     |
| 7   | 3 | 22 | 22   | 19   | -3  | 5 | 22 | 0     | 20   | -7  | 7 | 22 | 10  | 0    | 2   | 9  | 22 | 11  | 0    | -12 | 1   | 23 | -12  | 11   |     |
| 8   | 3 | 22 | -9   | 2    | -2  | 5 | 22 | 8     | 8    | -6  | 7 | 22 | 36  | 5    | 3   | 9  | 22 | 53  | 13   | -11 | 1   | 23 | 52   | 46   |     |
| 9   | 3 | 22 | 30   | 7    | -1  | 5 | 22 | -1    | 3    | -5  | 7 | 22 | 15  | 6    | 4   | 9  | 22 | -20 | 1    | -10 | 1   | 23 | 607  | 542  |     |
| 10  | 3 | 22 | -21  | 15   | 0   | 5 | 22 | 20    | 0    | -4  | 7 | 22 | 42  | 44   | 5   | 9  | 22 | 30  | 0    | -9  | 1   | 23 | 10   | 29   |     |
| 11  | 3 | 22 | -12  | 3    | 1   | 5 | 22 | 126   | 103  | -3  | 7 | 22 | 57  | 76   | 6   | 9  | 22 | 19  | 21   | -8  | 1   | 23 | 940  | 574  |     |
| 12  | 3 | 22 | 32   | 11   | 2   | 5 | 22 | 0     | 8    | -2  | 7 | 22 | 36  | 34   | 7   | 9  | 22 | 4   | 0    | -7  | 1   | 23 | 231  | 213  |     |
| 13  | 3 | 22 | 9    | 12   | 3   | 5 | 22 | 91    | 109  | -1  | 7 | 22 | 101 | 81   | 8   | 9  | 22 | 21  | 1    | -6  | 1   | 23 | 116  | 129  |     |
| 14  | 3 | 22 | 11   | 0    | 4   | 5 | 22 | 19    | 0    | 0   | 7 | 22 | 39  | 4    | 9   | 9  | 22 | 18  | 3    | -5  | 1   | 23 | 112  | 91   |     |
| 15  | 3 | 22 | 50   | 4    | 5   | 5 | 22 | -7    | 0    | 1   | 7 | 22 | -9  | 8    | -10 | 10 | 22 | 50  | 2    | -4  | 1   | 23 | 739  | 742  |     |
| 16  | 3 | 22 | 34   | 2    | 6   | 5 | 22 | -1    | 23   | 2   | 7 | 22 | 86  | 89   | -9  | 10 | 22 | 2   | 35   | -3  | 1   | 23 | 24   | 8    |     |
| 17  | 3 | 22 | -2   | 9    | 7   | 5 | 22 | 5     | 0    | 3   | 7 | 22 | 114 | 113  | -8  | 10 | 22 | 42  | 35   | -2  | 1   | 23 | 525  | 561  |     |
| 18  | 3 | 22 | 59   | 4    | 8   | 5 | 22 | -6    | 6    | 4   | 7 | 22 | 43  | 1    | -7  | 10 | 22 | -26 | 6    | -1  | 1   | 23 | 27   | 6    |     |
| 19  | 3 | 22 | 109  | 0    | 9   | 5 | 22 | 13    | 1    | 5   | 7 | 22 | -16 | 0    | -6  | 10 | 22 | 17  | 24   | 0   | 1   | 23 | 190  | 234  |     |
| -18 | 4 | 22 | 62   | 4    | 10  | 5 | 22 | -2    | 2    | 6   | 7 | 22 | 50  | 26   | -5  | 10 | 22 | -21 | 0    | 1   | 1   | 23 | 13   | 9    |     |
| -17 | 4 | 22 | 176  | 270  | 11  | 5 | 22 | -30   | 80   | 12  | 5 | 22 | 7   | 35   | -4  | 10 | 22 | -4  | 10   | 2   | 1   | 23 | 123  | 138  |     |
| -16 | 4 | 22 | 72   | 80   | 12  | 5 | 22 | 7     | 0    | 8   | 7 | 22 | 25  | 22   | -3  | 10 | 22 | 91  | 105  | 3   | 1   | 23 | 19   | 8    |     |
| -15 | 4 | 22 | 126  | 158  | 13  | 5 | 22 | 51    | 21   | 9   | 7 | 22 | 20  | 26   | -2  | 10 | 22 | 32  | 22   | 4   | 1   | 23 | 551  | 561  |     |
| -14 | 4 | 22 | 19   | 5    | 14  | 5 | 22 | -27   | 10   | 10  | 7 | 22 | 11  | 7    | -1  | 10 | 22 | 1   | 7    | 5   | 1   | 23 | 113  | 94   |     |
| -13 | 4 | 22 | 201  | 217  | 15  | 5 | 22 | -22   | 11   | 11  | 7 | 22 | 53  | 1    | 0   | 10 | 22 | 34  | 30   | 6   | 1   | 23 | 25   | 38   |     |
| -12 | 4 | 22 | 9    | 0    | 16  | 5 | 22 | -51   | 1    | 12  | 7 | 22 | -31 | 0    | 1   | 10 | 22 | 27  | 77   | 7   | 1   | 23 | 82   | 58   |     |
| -11 | 4 | 22 | 85   | 33   | 17  | 5 | 22 | 10    | 14   | 13  | 7 | 22 | 43  | 43   | 2   | 10 | 22 | 28  | 1    | 8   | 1   | 23 | 992  | 1132 |     |
| -10 | 4 | 22 | 191  | 154  | -18 | 6 | 22 | 156   | 33   | 14  | 7 | 22 | -31 | 7    | 3   | 10 | 22 | 41  | 7    | 9   | 1   | 23 | 300  | 314  |     |
| -9  | 4 | 22 | 641  | 623  | -17 | 6 | 22 | 91    | 59   | -15 | 8 | 22 | 72  | 1    | 4   | 10 | 22 | 63  | 5    | 10  | 1   | 23 | 233  | 204  |     |
| -8  | 4 | 22 | -18  | 2    | -16 | 6 | 22 | 133   | 73   | -14 | 8 | 22 | -11 | 28   | 5   | 10 | 22 | 76  | 0    | 11  | 1   | 23 | 55   | 32   |     |
| -7  | 4 | 22 | 1159 | 1132 | -15 | 6 | 22 | 4     | 2    | -13 | 8 | 22 | 38  | 81   | -7  | 11 | 22 | -38 | 9    | 13  | 1   | 23 | 125  | 136  |     |
| -6  | 4 | 22 | 228  | 287  | -14 | 6 | 22 | 106   | 85   | -12 | 8 | 22 | 69  | 24   | -6  | 11 | 22 | 92  | 0    | 14  | 1   | 23 | 36   | 61   |     |
| -5  | 4 | 22 | 418  | 379  | -13 | 6 | 22 | -6    | 1    | -11 | 8 | 22 | 69  | 52   | -5  | 11 | 22 | -22 | 4    | 15  | 1   | 23 | 49   | 3    |     |
| -4  | 4 | 22 | 71   | 77   | -12 | 6 | 22 | 57    | 45   | -10 | 8 | 22 | 40  | 14   | -4  | 11 | 22 | -35 | 0    | 17  | 1   | 23 | 42   | 2    |     |
| -3  | 4 | 22 | 255  | 181  | -11 | 6 | 22 | 17    | 3    | -9  | 8 | 22 | 19  | 12   | -3  | 11 | 22 | -3  | 3    | 18  | 1   | 23 | 31   | 6    |     |
| -2  | 4 | 22 | 18   | 12   | -10 | 6 | 22 | 112   | 62   | -8  | 8 | 22 | 22  | 0    | -2  | 11 | 22 | -41 | 3    | -18 | 2   | 23 | 167  | 97   |     |
| -1  | 4 | 22 | 332  | 319  | -9  | 6 | 22 | 1     | 0    | -7  | 8 | 22 | -9  | 12   | -1  | 11 | 22 | 42  | 0    | -17 | 2   | 23 | 88   | 105  |     |
| 0   | 4 | 22 | 70   | 77   | -8  | 6 | 22 | -8    | 3    | -6  | 8 | 22 | 44  | 37   | 4   | 0  | 11 | 22  | -21  | 1   | -16 | 2  | 23   | 341  | 374 |
| 1   | 4 | 22 | 248  | 226  | -7  | 6 | 22 | 56    | 62   | -5  | 8 | 22 | 37  | 101  | 1   | 11 | 22 | 3   | 4    | -15 | 2   | 23 | 82   | 100  |     |
| 2   | 4 | 22 | -6   | 0    | -6  | 6 | 22 | 23    | 39   | -4  | 8 | 22 | 113 | 14   | 2   | 11 | 22 | 28  | 0    | -14 | 2   | 23 | 307  | 282  |     |
| 3   | 4 | 22 | 113  | 82   | -5  | 6 | 22 | 122   | 136  | -3  | 8 | 22 | 28  | 16   | 3   | 11 | 22 | -7  | 0    | -13 | 2   | 23 | 103  | 84   |     |
| 4   | 4 | 22 | 2    | 2    | -4  | 6 | 22 | 25    | 1    | -2  | 8 | 22 | 15  | 0    | 1   | 4  | 11 | 22  | -46  | 4   | -12 | 2  | 23   | 141  | 133 |
| 5   | 4 | 22 | 196  | 195  | -3  | 6 | 22 | 70    | 96   | -1  | 8 | 22 | 0   | 71   | 5   | 11 | 22 | 19  | 0    | -11 | 2   | 23 | 142  | 185  |     |
| 6   | 4 | 22 | 11   | 21   | 2   | 6 | 22 | -10   | 111  | 1   | 8 | 22 | 27  | 16   | -4  | 12 | 22 | 35  | 4    | -10 | 2   | 23 | 518  | 513  |     |
| 7   | 4 | 22 | 181  | 118  | -1  | 6 | 22 | 129   | 17   | 12  | 5 | 23 | 18  | 27   | 10  | 7  | 23 | 83  | 5    | 1   | 10  | 23 | 43   | 48   |     |
| -9  | 2 | 23 | 238  | 210  | -17 | 4 | 23 | 36    | 32   | 13  | 5 | 23 | -32 | 43   | 11  | 7  | 23 | 15  | 1    | 2   | 10  | 23 | 21   | 37   |     |
| -8  | 2 | 23 | 511  | 493  | -16 | 4 | 23 | 8     | 77   | 14  | 5 | 23 | 99  | 25   | 12  | 7  | 23 | 9   | 3    | 3   | 10  | 23 | 17   | 11   |     |
| -7  | 2 | 23 | 492  | 465  | -15 | 4 | 23 | 53    | 2    | 15  | 5 | 23 | -34 | 6    | 13  | 7  | 23 | 62  | 1    | 4   | 10  | 23 | 22   | 6    |     |
| -6  | 2 | 23 | 53   | 77   | -14 | 4 | 23 | -10   | 34   | 16  | 5 | 23 | 53  | 2    | -15 | 8  | 23 | 62  | 10   | 5   | 10  | 23 | 28   | 13   |     |
| -5  | 2 | 23 | 197  | 194  | -13 | 4 | 23 | 41    | 71   | 17  | 5 | 23 | 24  | 13   | -14 | 8  | 23 | -41 | 1    | 6   | 10  | 23 | 84   | 6    |     |
| -4  | 2 | 23 | 1319 | 1227 | -12 | 4 | 23 | 63    | 47   | -17 | 6 | 23 | -18 | 149  | -12 | 8  | 23 | -17 | 0    | -8  | 11  | 23 | -8   | 0    |     |
| -3  | 2 | 23 | 41   | 7    | -11 | 4 | 23 | 36    | 110  | -16 | 6 | 23 | 85  | 90   | -11 | 8  | 23 | -15 | 5    | -6  | 11  | 23 | 30   | 0    |     |
| -2  | 2 | 23 | 382  | 302  | -10 | 4 | 23 | 108   | 8    | -15 | 6 | 23 | 135 | 9    | -10 | 8  | 23 | 2   | 5    | -5  | 11  | 23 | -34  | 13   |     |
| -1  | 2 | 23 | 11   | 4    | -9  | 4 | 23 | 13    | 615  | -14 | 6 | 23 | 68  | 39   | -9  | 8  | 23 | 40  | 22   | -4  | 11  | 23 | -36  | 2    |     |
| 0   | 2 | 23 | 9    | 2    | -8  | 4 | 23 | 546   | 521  | -12 | 6 | 23 | 60  | 8    | -8  | 8  | 23 | -4  | 15   | -3  | 11  | 23 | -5   | 0    |     |
| 1   | 2 | 23 | 452  | 398  | -7  | 4 | 23 | 103</ |      |     |   |    |     |      |     |    |    |     |      |     |     |    |      |      |     |



Table B.3, continued

| H   | K | L  | Obs  | Calc | H   | K | L  | Obs | Calc | H   | K | L  | Obs | Calc | H   | K  | L  | Obs | Calc | H   | K  | L  | Obs | Calc |    |
|-----|---|----|------|------|-----|---|----|-----|------|-----|---|----|-----|------|-----|----|----|-----|------|-----|----|----|-----|------|----|
| -3  | 3 | 23 | 27   | 30   | -11 | 5 | 23 | 10  | 26   | -13 | 7 | 23 | 37  | 56   | -2  | 9  | 23 | 44  | 35   | -18 | 1  | 24 | 101 | 24   |    |
| -2  | 3 | 23 | 15   | 2    | -10 | 5 | 23 | 4   | 1    | -12 | 7 | 23 | 64  | 17   | -1  | 9  | 23 | 17  | 25   | -17 | 1  | 24 | 9   | 3    |    |
| -1  | 3 | 23 | 150  | 171  | -9  | 5 | 23 | -14 | 2    | -11 | 7 | 23 | 30  | 7    | 0   | 9  | 23 | 3   | 0    | -16 | 1  | 24 | -13 | 15   |    |
| 0   | 3 | 23 | 13   | 3    | -8  | 5 | 23 | 19  | 0    | -10 | 7 | 23 | 16  | 12   | 1   | 9  | 23 | 32  | 2    | -15 | 1  | 24 | 44  | 40   |    |
| 1   | 3 | 23 | 225  | 209  | -7  | 5 | 23 | 1   | 3    | -9  | 7 | 23 | 55  | 54   | 2   | 9  | 23 | -12 | 0    | -14 | 1  | 24 | 18  | 4    |    |
| 2   | 3 | 23 | -24  | 0    | -6  | 5 | 23 | 60  | 99   | -8  | 7 | 23 | -9  | 12   | 3   | 9  | 23 | 45  | 67   | -13 | 1  | 24 | 5   | 12   |    |
| 3   | 3 | 23 | 93   | 67   | -5  | 5 | 23 | 27  | 23   | -7  | 7 | 23 | 3   | 5    | 4   | 9  | 23 | 7   | 2    | -12 | 1  | 24 | 4   | 22   |    |
| 4   | 3 | 23 | -3   | 19   | -4  | 5 | 23 | 8   | 4    | -6  | 7 | 23 | 39  | 32   | 5   | 9  | 23 | 8   | 17   | -11 | 1  | 24 | -15 | 11   |    |
| 5   | 3 | 23 | 182  | 138  | -3  | 5 | 23 | 191 | 203  | -5  | 7 | 23 | 34  | 15   | 6   | 9  | 23 | 33  | 4    | -10 | 1  | 24 | 77  | 109  |    |
| 6   | 3 | 23 | 45   | 3    | -2  | 5 | 23 | 45  | 52   | -4  | 7 | 23 | -10 | 5    | 7   | 9  | 23 | 15  | 0    | -9  | 1  | 24 | 251 | 260  |    |
| 7   | 3 | 23 | 144  | 116  | -1  | 5 | 23 | 28  | 3    | -3  | 7 | 23 | 28  | 4    | 9   | 9  | 23 | -24 | 8    | -8  | 1  | 24 | 20  | 32   |    |
| 8   | 3 | 23 | 22   | 6    | 0   | 5 | 23 | 38  | 61   | -2  | 7 | 23 | 3   | 4    | 9   | 9  | 23 | 276 | 3    | -7  | 1  | 24 | 295 | 321  |    |
| 9   | 3 | 23 | 50   | 27   | 1   | 5 | 23 | -14 | 1    | -1  | 7 | 23 | 19  | 7    | -10 | 10 | 23 | 33  | 1    | -6  | 1  | 24 | 155 | 164  |    |
| 10  | 3 | 23 | -5   | 1    | 2   | 5 | 23 | 73  | 20   | 0   | 7 | 23 | 7   | 3    | -9  | 10 | 23 | -26 | 0    | -5  | 1  | 24 | 96  | 70   |    |
| 11  | 3 | 23 | 76   | 85   | 3   | 5 | 23 | 35  | 48   | 1   | 7 | 23 | 16  | 43   | -8  | 10 | 23 | 117 | 1    | -4  | 1  | 24 | -4  | 5    |    |
| 12  | 3 | 23 | 35   | 1    | 4   | 5 | 23 | 4   | 1    | 2   | 7 | 23 | 37  | 34   | -7  | 10 | 23 | -43 | 9    | -3  | 1  | 24 | 12  | 3    |    |
| 13  | 3 | 23 | 40   | 5    | 5   | 5 | 23 | 74  | 45   | 3   | 7 | 23 | 13  | 10   | -6  | 10 | 23 | 80  | 0    | -2  | 1  | 24 | -3  | 6    |    |
| 14  | 3 | 23 | -40  | 2    | 6   | 5 | 23 | -21 | 16   | 4   | 7 | 23 | 32  | 7    | -5  | 10 | 23 | -14 | 3    | -1  | 1  | 24 | 5   | 23   |    |
| 15  | 3 | 23 | 29   | 45   | 7   | 5 | 23 | 105 | 93   | 5   | 7 | 23 | 106 | 55   | -4  | 10 | 23 | 25  | 58   | 0   | 1  | 24 | 50  | 62   |    |
| 16  | 3 | 23 | 16   | 15   | 8   | 5 | 23 | 11  | 19   | 6   | 7 | 23 | 15  | 92   | -5  | 10 | 23 | 17  | 28   | 1   | 1  | 24 | 21  | 37   |    |
| 17  | 3 | 23 | 11   | 6    | 9   | 5 | 23 | 22  | 30   | 7   | 7 | 23 | -6  | 0    | -2  | 10 | 23 | -14 | 18   | 2   | 1  | 24 | 14  | 1    |    |
| 18  | 3 | 23 | -3   | 2    | 10  | 5 | 23 | 4   | 15   | 8   | 7 | 23 | 74  | 28   | -1  | 10 | 23 | -34 | 5    | 3   | 1  | 24 | 70  | 72   |    |
| -18 | 4 | 23 | 79   | 48   | 11  | 5 | 23 | -25 | 1    | 9   | 7 | 23 | 82  | 3    | 0   | 10 | 23 | 35  | 16   | 4   | 1  | 24 | 93  | 75   |    |
| 5   | 1 | 24 | 87   | 65   | 0   | 3 | 24 | 53  | 22   | -5  | 5 | 24 | 15  | 0    | -6  | 7  | 24 | 164 | 173  | 7   | 9  | 24 | 13  | 21   |    |
| 6   | 1 | 24 | 15   | 2    | 1   | 3 | 24 | 6   | 36   | -4  | 5 | 24 | 3   | 18   | -5  | 7  | 24 | 41  | 42   | 8   | 9  | 24 | -36 | 0    |    |
| 7   | 1 | 24 | 41   | 34   | 2   | 3 | 24 | 160 | 153  | -3  | 5 | 24 | 1   | 4    | -4  | 7  | 24 | -1  | 4    | -10 | 10 | 24 | 43  | 0    |    |
| 8   | 1 | 24 | 69   | 52   | 3   | 3 | 24 | 65  | 38   | -2  | 5 | 24 | 24  | 26   | -3  | 7  | 24 | 18  | 0    | -9  | 10 | 24 | 131 | 4    |    |
| 9   | 1 | 24 | 181  | 139  | 4   | 3 | 24 | 131 | 80   | -1  | 5 | 24 | 28  | 42   | -2  | 7  | 24 | 56  | 50   | -8  | 10 | 24 | -19 | 0    |    |
| 10  | 1 | 24 | 103  | 143  | 5   | 3 | 24 | 41  | 37   | 0   | 5 | 24 | 10  | 6    | -1  | 7  | 24 | 31  | 11   | -7  | 10 | 24 | 43  | 6    |    |
| 11  | 1 | 24 | 42   | 28   | 6   | 3 | 24 | 21  | 9    | 1   | 5 | 24 | 33  | 29   | 0   | 7  | 24 | 9   | 4    | -6  | 10 | 24 | 77  | 0    |    |
| 12  | 1 | 24 | 41   | 8    | 7   | 3 | 24 | 32  | 27   | 2   | 5 | 24 | 5   | 5    | 1   | 7  | 24 | 8   | 22   | -5  | 10 | 24 | -29 | 0    |    |
| 13  | 1 | 24 | 32   | 1    | 8   | 3 | 24 | 113 | 65   | 3   | 5 | 24 | 78  | 120  | 2   | 7  | 24 | 9   | 3    | -4  | 10 | 24 | -28 | 21   |    |
| 14  | 1 | 24 | 39   | 28   | 9   | 3 | 24 | 45  | 15   | 4   | 5 | 24 | 19  | 9    | 3   | 7  | 24 | 88  | 79   | -3  | 10 | 24 | -27 | 31   |    |
| 15  | 1 | 24 | 47   | 25   | 10  | 3 | 24 | 11  | 13   | 5   | 5 | 24 | 72  | 63   | 4   | 7  | 24 | -2  | 26   | -2  | 10 | 24 | 18  | 60   |    |
| 16  | 1 | 24 | -80  | 1    | 11  | 3 | 24 | 25  | 3    | 6   | 5 | 24 | 90  | 93   | 5   | 7  | 24 | -15 | 1    | -1  | 10 | 24 | 32  | 15   |    |
| 17  | 1 | 24 | 43   | 12   | 12  | 3 | 24 | 39  | 58   | 7   | 5 | 24 | 165 | 161  | 6   | 7  | 24 | 19  | 8    | 0   | 10 | 24 | 31  | 89   |    |
| -18 | 2 | 24 | 18   | 27   | 13  | 3 | 24 | -48 | 1    | 8   | 5 | 24 | 37  | 10   | 7   | 7  | 24 | -3  | 21   | 1   | 10 | 24 | 22  | 24   |    |
| -17 | 2 | 24 | 16   | 6    | 14  | 3 | 24 | -79 | 9    | 9   | 5 | 24 | 84  | 35   | 8   | 7  | 24 | 14  | 0    | 2   | 10 | 24 | 68  | 12   |    |
| -16 | 2 | 24 | 18   | 24   | 15  | 3 | 24 | -28 | 8    | 10  | 5 | 24 | 83  | 2    | 9   | 7  | 24 | -26 | 3    | 3   | 10 | 24 | 57  | 2    |    |
| -15 | 2 | 24 | 78   | 120  | 16  | 3 | 24 | 42  | 13   | 11  | 5 | 24 | 49  | 9    | 10  | 7  | 24 | 15  | 0    | 4   | 10 | 24 | 9   | 0    |    |
| -14 | 2 | 24 | 78   | 82   | 17  | 3 | 24 | 44  | 1    | 12  | 5 | 24 | -16 | 0    | 11  | 7  | 24 | 12  | 3    | 5   | 10 | 24 | 0   | 5    |    |
| -13 | 2 | 24 | 114  | 99   | -17 | 4 | 24 | 230 | 264  | 13  | 5 | 24 | 12  | 60   | 12  | 7  | 24 | -6  | 0    | 6   | 10 | 24 | -18 | 0    |    |
| -12 | 2 | 24 | 154  | 112  | -16 | 4 | 24 | 29  | 0    | 14  | 5 | 24 | -66 | 18   | 13  | 7  | 24 | 9   | 0    | -8  | 11 | 24 | -40 | 0    |    |
| -11 | 2 | 24 | 80   | 118  | -15 | 4 | 24 | 18  | 22   | 15  | 5 | 24 | -53 | 10   | -14 | 8  | 24 | 31  | 2    | -7  | 11 | 24 | 30  | 4    |    |
| -10 | 2 | 24 | 407  | 396  | -14 | 4 | 24 | 88  | 51   | 16  | 5 | 24 | 56  | 3    | -13 | 8  | 24 | 31  | 19   | -6  | 11 | 24 | 10  | 1    |    |
| -9  | 2 | 24 | 368  | 371  | -13 | 4 | 24 | 33  | 49   | 17  | 5 | 24 | 67  | 1    | -12 | 8  | 24 | -30 | 13   | -5  | 11 | 24 | 9   | 2    |    |
| -8  | 2 | 24 | 1372 | 1344 | -12 | 4 | 24 | 79  | 43   | -17 | 6 | 24 | 194 | 32   | -11 | 8  | 24 | 77  | 8    | -4  | 11 | 24 | 9   | 7    |    |
| -7  | 2 | 24 | 21   | 23   | -11 | 4 | 24 | 287 | 329  | -16 | 6 | 24 | -33 | 5    | -10 | 8  | 24 | 22  | 7    | -3  | 11 | 24 | 315 | 3    |    |
| -6  | 2 | 24 | 421  | 420  | -10 | 4 | 24 | 2   | 1    | -15 | 6 | 24 | 47  | 21   | -9  | 8  | 24 | 0   | 1    | -2  | 11 | 24 | -4  | 0    |    |
| -5  | 2 | 24 | 19   | 7    | -9  | 4 | 24 | 369 | 344  | -14 | 6 | 24 | 94  | 28   | -8  | 8  | 24 | 48  | 25   | -1  | 11 | 24 | 8   | 6    |    |
| -4  | 2 | 24 | 14   | 13   | -8  | 4 | 24 | 2   | 0    | -13 | 6 | 24 | 107 | 79   | -7  | 8  | 24 | 10  | 1    | 0   | 11 | 24 | 71  | 22   |    |
| -3  | 2 | 24 | 1148 | 1024 | -7  | 4 | 24 | 62  | 45   | -12 | 6 | 24 | 13  | 1    | -6  | 8  | 24 | 27  | 0    | 1   | 11 | 24 | -13 | 3    |    |
| -2  | 2 | 24 | 4    | 9    | -6  | 4 | 24 | 40  | 65   | -11 | 6 | 24 | 23  | 17   | -5  | 8  | 24 | 34  | 13   | 2   | 11 | 24 | 51  | 11   |    |
| -1  | 2 | 24 | 141  | 155  | -5  | 4 | 24 | 252 | 234  | -10 | 6 | 24 | 88  | 53   | -4  | 8  | 24 | 6   | 15   | 3   | 11 | 24 | -40 | 0    |    |
| 0   | 2 | 24 | 212  | 203  | -4  | 4 | 24 | -12 | 0    | -9  | 6 | 24 | 183 | 130  | -3  | 8  | 24 | 31  | 2    | 4   | 11 | 24 | -24 | 16   |    |
| 1   | 2 | 24 | 199  | 193  | -3  | 4 | 24 | 37  | 34   | -8  | 6 | 24 | 76  | 30   | -2  | 8  | 24 | 92  | 90   | 5   | 11 | 24 | 58  | 1    |    |
| 2   | 2 | 24 | 62   | 64   | -2  | 4 | 24 | 144 | 160  | -7  | 6 | 24 | 49  | 46   | -1  | 8  | 24 | 26  | 7    | 6   | 11 | 24 | 245 | 3    |    |
| 3   | 2 | 24 | 130  | 99   | -1  | 4 | 24 | 23  | 20   | -6  | 4 | 24 | 113 | 112  | 0   | 8  | 24 | 1   | 2    | -4  | 12 | 24 | -17 | 0    |    |
| 4   | 2 | 24 | 26   | 3    | 0   | 4 | 24 | 39  | 59   | -5  | 6 | 24 | 19  | 9    | 1   | 8  | 24 | 14  | 15   | -3  | 12 | 24 | 13  | 0    |    |
| 5   | 2 | 24 | 279  | 250  | 1   | 4 | 24 | 112 | 93   | -4  | 6 | 24 | 63  | 64   | 2   | 8  | 24 | 5   | 18   | -2  | 12 | 24 | 28  | 5    |    |
| 6   | 2 | 24 | 8    | 2    | 2   | 4 | 24 | 14  | 13   | -3  | 6 | 24 | 12  | 7    | 3   | 8  | 24 | 11  | 19   | -17 | 0  | 25 | 52  | 46   |    |
| 7   | 2 | 24 | 5    | 13   | 3   | 4 | 24 | 160 | 127  | -2  | 6 | 24 | 41  | 59   | 4   | 8  | 24 | 62  | 76   | -15 | 0  | 25 | 238 | 222  |    |
| 8   | 2 | 24 | 506  | 432  | 4   | 4 | 24 | -1  | 1    | -1  | 6 | 24 | 36  | 8    | 5   | 8  | 24 | -2  | 1    | -13 | 0  | 25 | 106 | 36   |    |
| 9   | 2 | 24 | 242  | 232  | 5   | 4 | 24 | 76  | 28   | 0   | 6 | 24 | 37  | 39   | 6   | 8  | 24 | 21  | 2    | -11 | 0  | 25 | 451 | 436  |    |
| 10  | 2 | 24 | 121  | 110  | 6   | 4 | 24 | 22  | 101  | 1   | 6 | 24 | 24  | 6    | 15  | 7  | 8  | 24  | 15   | 12  | -9 | 0  | 25  | 32   | 27 |
| 11  | 2 | 24 | -3   | 14   | 7   | 4 | 24 | 96  | 40   | 2   | 6 | 24 | 12  | 32   | 8   | 8  | 24 | 11  | 32   | -7  | 0  | 25 | 73  | 118  |    |
| 12  | 2 | 24 | 66   | 69   | 8   | 4 | 24 | -6  | 15   | 3   | 6 | 24 | 9   | 6    | 9   | 8  | 24 | -36 | 13   | -5  | 0  | 25 | 28  | 37   |    |
| 13  | 2 | 24 | 12   | 9    | 4   | 4 | 24 | -11 | 12   | 4   | 6 | 24 | 37  | 38   | 10  | 8  | 24 | -23 | 8    | -3  | 0  | 25 | 269 | 253  |    |
| 15  | 2 | 24 | -13  | 51   | 10  | 4 | 24 | 39  | 19   | 5   | 6 | 24 | 32  | 28   | 11  | 8  | 24 | 0   | 0    | -1  | 0  | 25 | 587 | 597  |    |
| 16  | 2 | 24 | 99   | 0    | 11  | 4 | 24 | 19  | 1    | 6   | 6 | 24 | 105 | 41   | -13 | 9  | 24 | 129 | 0    | 1   | 0  | 25 | 541 | 565  |    |
| 17  | 2 | 24 | 97   | 9    | 12  | 4 | 24 | -11 | 21   | 7   | 6 | 24 | 49  | 26   | -12 | 9  | 24 | 33  | 1    | 3   | 0  | 25 | 411 | 398  |    |
| -18 |   |    |      |      |     |   |    |     |      |     |   |    |     |      |     |    |    |     |      |     |    |    |     |      |    |

Table B.3, continued

| M   | K | L  | Obs | Calc | M   | K | L  | Obs | Calc | M   | K | L  | Obs | Calc | M   | K | L  | Obs | Calc | M   | K  | L  | Obs | Calc |
|-----|---|----|-----|------|-----|---|----|-----|------|-----|---|----|-----|------|-----|---|----|-----|------|-----|----|----|-----|------|
| 0   | 1 | 25 | 211 | 174  | 3   | 3 | 25 | 137 | 171  | -2  | 5 | 25 | -6  | 9    | -1  | 7 | 25 | 45  | 3    | -4  | 10 | 25 | -45 | 33   |
| 9   | 1 | 25 | 125 | 97   | 4   | 3 | 25 | 127 | 156  | -1  | 5 | 25 | 56  | 25   | 0   | 7 | 25 | 82  | 52   | -3  | 10 | 25 | 96  | 7    |
| 10  | 1 | 25 | 11  | 10   | 5   | 3 | 25 | 197 | 193  | 0   | 5 | 25 | 25  | 9    | 1   | 7 | 25 | 4   | 9    | -2  | 10 | 25 | 99  | 0    |
| 11  | 1 | 25 | 4   | 22   | 6   | 3 | 25 | 12  | 17   | 1   | 5 | 25 | 0   | 7    | 2   | 7 | 25 | 53  | 59   | -1  | 10 | 25 | 49  | 1    |
| 12  | 1 | 25 | 10  | 18   | 7   | 3 | 25 | -1  | 11   | 2   | 5 | 25 | 22  | 21   | 3   | 7 | 25 | 0   | 1    | 0   | 10 | 25 | 15  | 13   |
| 13  | 1 | 25 | 17  | 0    | 8   | 3 | 25 | 80  | 35   | 3   | 5 | 25 | -10 | 6    | 4   | 7 | 25 | 135 | 151  | 1   | 10 | 25 | 40  | 0    |
| 14  | 1 | 25 | 184 | 4    | 9   | 3 | 25 | 81  | 83   | 4   | 5 | 25 | 43  | 13   | 5   | 7 | 25 | 16  | 1    | 2   | 10 | 25 | 18  | 4    |
| 15  | 1 | 25 | 63  | 44   | 10  | 3 | 25 | 53  | 21   | 5   | 5 | 25 | 58  | 17   | 6   | 7 | 25 | 53  | 46   | 3   | 10 | 25 | 50  | 8    |
| 16  | 1 | 25 | 71  | 34   | 11  | 3 | 25 | 31  | 10   | 6   | 5 | 25 | 21  | 1    | 7   | 7 | 25 | 7   | 40   | 4   | 10 | 25 | -20 | 8    |
| 17  | 1 | 25 | 93  | 1    | 12  | 3 | 25 | 76  | 8    | 7   | 5 | 25 | 30  | 29   | 8   | 7 | 25 | 58  | 36   | 5   | 10 | 25 | 0   | 8    |
| -18 | 2 | 25 | 134 | 132  | 13  | 3 | 25 | 67  | 2    | 8   | 5 | 25 | 50  | 0    | 9   | 7 | 25 | 72  | 10   | 6   | 10 | 25 | 34  | 1    |
| -17 | 2 | 25 | 89  | 51   | 14  | 3 | 25 | -12 | 18   | 9   | 5 | 25 | 74  | 23   | 10  | 7 | 25 | -5  | 0    | 7   | 10 | 25 | 0   | 0    |
| -16 | 2 | 25 | 65  | 84   | 15  | 3 | 25 | 33  | 0    | 10  | 5 | 25 | 16  | 10   | 11  | 7 | 25 | -42 | 5    | -7  | 11 | 25 | -6  | 3    |
| -15 | 2 | 25 | 5   | 9    | 16  | 3 | 25 | 98  | 12   | 11  | 5 | 25 | 0   | 1    | 12  | 7 | 25 | 28  | 21   | -6  | 11 | 25 | 93  | 3    |
| -14 | 2 | 25 | 73  | 85   | 17  | 3 | 25 | -21 | 0    | 12  | 5 | 25 | -6  | 0    | 13  | 7 | 25 | 7   | 2    | -5  | 11 | 25 | -20 | 15   |
| -13 | 2 | 25 | -5  | 1    | -18 | 4 | 25 | 20  | 26   | 13  | 5 | 25 | -10 | 18   | -13 | 8 | 25 | 13  | 30   | -4  | 11 | 25 | 19  | 18   |
| -12 | 2 | 25 | 84  | 76   | -17 | 4 | 25 | -9  | 9    | 14  | 5 | 25 | 10  | 9    | -12 | 8 | 25 | 12  | 6    | -3  | 11 | 25 | -27 | 18   |
| -11 | 2 | 25 | 37  | 13   | -16 | 4 | 25 | 116 | 123  | 15  | 5 | 25 | 85  | 4    | -11 | 8 | 25 | 21  | 47   | -2  | 11 | 25 | 8   | 0    |
| -10 | 2 | 25 | 70  | 83   | -15 | 4 | 25 | -4  | 24   | 16  | 5 | 25 | -23 | 8    | -10 | 8 | 25 | -20 | 7    | -1  | 11 | 25 | 5   | 1    |
| -9  | 2 | 25 | 62  | 45   | -14 | 4 | 25 | 7   | 20   | -16 | 6 | 25 | -48 | 1    | -9  | 8 | 25 | 70  | 5    | 0   | 11 | 25 | 72  | 9    |
| -8  | 2 | 25 | 34  | 40   | -13 | 4 | 25 | 54  | 8    | -15 | 6 | 25 | 173 | 71   | -8  | 8 | 25 | 25  | 9    | 1   | 11 | 25 | -56 | 2    |
| -7  | 2 | 25 | 32  | 49   | -12 | 4 | 25 | 56  | 72   | -14 | 6 | 25 | 60  | 0    | -7  | 8 | 25 | 37  | 53   | 2   | 11 | 25 | 34  | 0    |
| -6  | 2 | 25 | 7   | 17   | -11 | 4 | 25 | 31  | 33   | -13 | 6 | 25 | 132 | 92   | -6  | 8 | 25 | 28  | 40   | -18 | 0  | 26 | 42  | 59   |
| -5  | 2 | 25 | 34  | 11   | -10 | 4 | 25 | 135 | 131  | -12 | 6 | 25 | 31  | 41   | -5  | 8 | 25 | 7   | 1    | -16 | 0  | 26 | 169 | 272  |
| -4  | 2 | 25 | 30  | 32   | -9  | 4 | 25 | 2   | 7    | -11 | 6 | 25 | 44  | 1    | -4  | 8 | 25 | 6   | 35   | -14 | 0  | 26 | 310 | 335  |
| -3  | 2 | 25 | 45  | 10   | -8  | 4 | 25 | 247 | 217  | -10 | 6 | 25 | 7   | 3    | -3  | 8 | 25 | -7  | 2    | -12 | 0  | 26 | 341 | 286  |
| -2  | 2 | 25 | 189 | 202  | -7  | 4 | 25 | 66  | 21   | -9  | 6 | 25 | 45  | 56   | -2  | 8 | 25 | 35  | 2    | -10 | 0  | 26 | 153 | 139  |
| -1  | 2 | 25 | 4   | 26   | -6  | 4 | 25 | 113 | 80   | -8  | 6 | 25 | -6  | 3    | -1  | 8 | 25 | -9  | 15   | -8  | 0  | 26 | 280 | 358  |
| 0   | 2 | 25 | 61  | 49   | -5  | 4 | 25 | -8  | 2    | -7  | 6 | 25 | 16  | 20   | 0   | 8 | 25 | 7   | 2    | -6  | 0  | 26 | -1  | 52   |
| 1   | 2 | 25 | 98  | 72   | -4  | 4 | 25 | 429 | 424  | -6  | 6 | 25 | 35  | 1    | 1   | 8 | 25 | -4  | 5    | -4  | 0  | 26 | 370 | 420  |
| 2   | 2 | 25 | 48  | 36   | -3  | 4 | 25 | 13  | 29   | -5  | 6 | 25 | 0   | 2    | 2   | 8 | 25 | -10 | 10   | -2  | 0  | 26 | 147 | 176  |
| 3   | 2 | 25 | 75  | 44   | -2  | 4 | 25 | 40  | 22   | -4  | 6 | 25 | 7   | 22   | 3   | 8 | 25 | 13  | 39   | 0   | 0  | 26 | 236 | 198  |
| 4   | 2 | 25 | 235 | 212  | -1  | 4 | 25 | 25  | 15   | -3  | 6 | 25 | 25  | 1    | 4   | 8 | 25 | 13  | 7    | 2   | 0  | 26 | 250 | 228  |
| 5   | 2 | 25 | 2   | 8    | 0   | 4 | 25 | 257 | 254  | -2  | 6 | 25 | 16  | 52   | 5   | 8 | 25 | 0   | 20   | 4   | 0  | 26 | 264 | 299  |
| 6   | 2 | 25 | 183 | 207  | 1   | 4 | 25 | 132 | 210  | -1  | 6 | 25 | 24  | 5    | 6   | 8 | 25 | 26  | 2    | 6   | 0  | 26 | 42  | 7    |
| 7   | 2 | 25 | 16  | 1    | 2   | 4 | 25 | 249 | 210  | 0   | 6 | 25 | 49  | 25   | 7   | 8 | 25 | 16  | 14   | 8   | 0  | 26 | 187 | 155  |
| 8   | 2 | 25 | 1   | 4    | 3   | 4 | 25 | 0   | 0    | 1   | 6 | 25 | 38  | 5    | 8   | 8 | 25 | 77  | 1    | 10  | 0  | 26 | -3  | 4    |
| 9   | 2 | 25 | 201 | 182  | 4   | 4 | 25 | 135 | 138  | 2   | 6 | 25 | 43  | 75   | 9   | 8 | 25 | -34 | 9    | 12  | 0  | 26 | -23 | 2    |
| 10  | 2 | 25 | 130 | 126  | 5   | 4 | 25 | 139 | 76   | 3   | 6 | 25 | 62  | 28   | 10  | 8 | 25 | 166 | 2    | 14  | 0  | 26 | -3  | 29   |
| 11  | 2 | 25 | 7   | 34   | 6   | 4 | 25 | 172 | 130  | 4   | 6 | 25 | 27  | 19   | 11  | 8 | 25 | -3  | 9    | -19 | 1  | 26 | 48  | 2    |
| 12  | 2 | 25 | 32  | 5    | 7   | 4 | 25 | 27  | 20   | 5   | 6 | 25 | 15  | 21   | -12 | 8 | 25 | 38  | 0    | -18 | 26 | 16 | 42  |      |
| 13  | 2 | 25 | 15  | 23   | 8   | 4 | 25 | 167 | 148  | 6   | 5 | 25 | -5  | 1    | -11 | 9 | 25 | 3   | 0    | -17 | 1  | 26 | 43  | 5    |
| 14  | 2 | 25 | -19 | 1    | 9   | 4 | 25 | 87  | 19   | 7   | 6 | 25 | 70  | 38   | -10 | 9 | 25 | 10  | 0    | -16 | 1  | 26 | 9   | 79   |
| 15  | 2 | 25 | -34 | 16   | 10  | 4 | 25 | 51  | 10   | 8   | 6 | 25 | 48  | 32   | -9  | 9 | 25 | -31 | 4    | -15 | 1  | 26 | 84  | 94   |
| 16  | 2 | 25 | 8   | 5    | 11  | 4 | 25 | 6   | 0    | 9   | 6 | 25 | 121 | 33   | -8  | 9 | 25 | 3   | 0    | -14 | 1  | 26 | 2   | 0    |
| -17 | 3 | 25 | 58  | 34   | 12  | 4 | 25 | 28  | 12   | 10  | 6 | 25 | -16 | 1    | -7  | 9 | 25 | 69  | 2    | -13 | 1  | 26 | -17 | 1    |
| -18 | 3 | 25 | 4   | 24   | 13  | 4 | 25 | 15  | 24   | 11  | 6 | 25 | 36  | 5    | -6  | 9 | 25 | 12  | 2    | -12 | 1  | 26 | -8  | 16   |
| -19 | 3 | 25 | -11 | 13   | 14  | 4 | 25 | 3   | 33   | 12  | 6 | 25 | -22 | 2    | -5  | 9 | 25 | 41  | 24   | -11 | 1  | 26 | 66  | 53   |
| -20 | 3 | 25 | 50  | 42   | 15  | 4 | 25 | 23  | 1    | 13  | 6 | 25 | -8  | 1    | -4  | 9 | 25 | 26  | 27   | -10 | 1  | 26 | 62  | 75   |
| -21 | 3 | 25 | 9   | 0    | 16  | 4 | 25 | -9  | 10   | 14  | 6 | 25 | 59  | 6    | -3  | 9 | 25 | -3  | 14   | -9  | 1  | 26 | 349 | 408  |
| -22 | 3 | 25 | 29  | 24   | 17  | 4 | 25 | -16 | 0    | 15  | 6 | 25 | -20 | 1    | -2  | 9 | 25 | -4  | 1    | -8  | 1  | 26 | 37  | 1    |
| -23 | 3 | 25 | 16  | 1    | -17 | 5 | 25 | 56  | 0    | -16 | 7 | 25 | -20 | 5    | -1  | 9 | 25 | -23 | 0    | -7  | 1  | 26 | 624 | 590  |
| -24 | 3 | 25 | 122 | 153  | -11 | 5 | 25 | 22  | 13   | -14 | 5 | 25 | -5  | 2    | -11 | 7 | 26 | 104 | 4    | 6   | 9  | 26 | 38  | 12   |
| -25 | 3 | 25 | 28  | 38   | -10 | 5 | 25 | 108 | 99   | -13 | 5 | 26 | 0   | 6    | -10 | 7 | 26 | 2   | 9    | 7   | 9  | 26 | -49 | 5    |
| -26 | 3 | 25 | 401 | 409  | -9  | 5 | 26 | -14 | 2    | -12 | 5 | 26 | -4  | 7    | -9  | 7 | 26 | 24  | 73   | 8   | 9  | 26 | -18 | 3    |
| -27 | 3 | 25 | 14  | 26   | -8  | 5 | 26 | 86  | 75   | -11 | 5 | 26 | 32  | 16   | -8  | 7 | 26 | 68  | 1    | -8  | 10 | 26 | 1   | 0    |
| -28 | 3 | 25 | 381 | 384  | -7  | 5 | 26 | 19  | 3    | -10 | 5 | 26 | 53  | 42   | -7  | 7 | 26 | 6   | 1    | -7  | 10 | 26 | 17  | 1    |
| -29 | 3 | 25 | 128 | 145  | -6  | 5 | 26 | 543 | 561  | -9  | 5 | 26 | 47  | 41   | -6  | 7 | 26 | 0   | 0    | -6  | 10 | 26 | 32  | 5    |
| -30 | 3 | 25 | 26  | 30   | -5  | 5 | 26 | 13  | 4    | -8  | 5 | 26 | 28  | 2    | -5  | 7 | 26 | 94  | 78   | -5  | 10 | 26 | 136 | 0    |
| -31 | 3 | 25 | 107 | 130  | -4  | 5 | 26 | 189 | 189  | -7  | 5 | 26 | 92  | 60   | -4  | 7 | 26 | 35  | 0    | -4  | 10 | 26 | -52 | 44   |
| -32 | 3 | 25 | 45  | 44   | -3  | 5 | 26 | -6  | 2    | -6  | 5 | 26 | 15  | 6    | -3  | 7 | 26 | 10  | 6    | -3  | 10 | 26 | -22 | 21   |
| -33 | 3 | 25 | 164 | 124  | -2  | 5 | 26 | -19 | 38   | -5  | 5 | 26 | 56  | 62   | -2  | 7 | 26 | 28  | 5    | -2  | 10 | 26 | -33 | 0    |
| -34 | 3 | 25 | 154 | 102  | -1  | 5 | 26 | 33  | 12   | -3  | 5 | 26 | 12  | 51   | -7  | 7 | 26 | 29  | 2    | -1  | 10 | 26 | 9   | 2    |
| -35 | 3 | 25 | 268 | 352  | 0   | 5 | 26 | 50  | 20   | -2  | 5 | 26 | 26  | 21   | 0   | 7 | 26 | 18  | 3    | 0   | 10 | 26 | -21 | 7    |
| -36 | 3 | 25 | 20  | 37   | 1   | 5 | 26 | 73  | 89   | -1  | 5 | 26 | -2  | 28   | 1   | 7 | 26 | 53  | 0    | 1   | 10 | 26 | -28 | 8    |
| -37 | 3 | 25 | 138 | 110  | 2   | 5 | 26 | 73  | 89   | -1  | 5 | 26 | -2  | 10   | 2   | 7 | 26 | -26 | 5    | 2   | 10 | 26 | -21 | 14   |
| -38 | 3 | 25 | 18  | 6    | 3   | 5 | 26 | 4   | 11   | 0   | 5 | 26 | 35  | 3    | 3   | 7 | 26 | -1  | 4    | 3   | 10 | 26 | 32  | 1    |
| -39 | 3 | 25 | 83  | 129  | 4   | 5 | 26 | 56  | 112  | 1   | 5 | 26 | 62  | 81   | 4   | 7 | 26 | 18  | 10   | 4   | 10 | 26 | 12  | 3    |
| -40 | 3 | 25 | 2   | 1    | 5   | 5 | 26 | 74  | 42   | 2   | 5 | 26 | 26  | 22   | 5   | 7 | 26 | -14 | 1    | 5   | 10 | 26 | 12  | 4    |
| -41 | 3 | 25 | 74  | 87   | 6   | 5 | 26 | 251 | 223  | 3   | 5 | 26 | 2   | 22   | 6   | 7 | 26 | 4   | 7    | 6   | 10 | 26 | -28 | 3    |
| -42 | 3 | 25 | 19  | 6    | 7   | 5 | 26 | 16  | 20   | 4   | 5 | 26 | 13  | 14   | 7   | 7 | 26 | 107 | 28   | 7   | 10 | 26 | -2  | 1    |
| -43 | 3 | 25 | 24  |      |     |   |    |     |      |     |   |    |     |      |     |   |    |     |      |     |    |    |     |      |

Table B.3, continued

| M   | K | L  | Obs | Calc | M   | K | L  | Obs | Calc | M   | K | L  | Obs | Calc | M   | K  | L  | Obs | Calc | M   | K  | L  | Obs  | Calc |
|-----|---|----|-----|------|-----|---|----|-----|------|-----|---|----|-----|------|-----|----|----|-----|------|-----|----|----|------|------|
| 9   | 2 | 26 | 12  | 4    | 5   | 4 | 26 | 53  | 19   | 4   | 6 | 26 | -1  | 1    | -9  | 9  | 26 | 21  | 5    | -12 | 1  | 27 | 308  | 356  |
| 10  | 2 | 26 | 30  | 17   | 6   | 4 | 26 | 31  | 1    | 5   | 6 | 26 | 111 | 115  | -8  | 9  | 26 | -5  | 0    | -11 | 1  | 27 | 6    | 27   |
| 11  | 2 | 26 | 22  | 14   | 7   | 4 | 26 | 8   | 0    | 6   | 6 | 26 | -10 | 2    | -7  | 9  | 26 | 2   | 0    | -10 | 1  | 27 | 560  | 673  |
| 12  | 2 | 26 | 17  | 23   | 8   | 4 | 26 | 126 | 14   | 7   | 6 | 26 | 21  | 17   | -6  | 9  | 26 | -31 | 12   | -9  | 1  | 27 | 60   | 75   |
| 13  | 2 | 26 | 13  | 0    | 9   | 4 | 26 | 37  | 17   | 8   | 6 | 26 | -6  | 0    | -5  | 9  | 26 | 44  | 20   | -8  | 1  | 27 | 39   | 10   |
| 14  | 2 | 26 | 22  | 0    | 10  | 4 | 26 | 4   | 9    | 9   | 6 | 26 | 39  | 34   | -4  | 9  | 26 | 126 | 12   | -7  | 1  | 27 | 190  | 208  |
| 15  | 2 | 26 | 27  | 3    | 11  | 4 | 26 | -18 | 1    | 10  | 6 | 26 | -18 | 3    | -3  | 9  | 26 | 100 | 14   | -6  | 1  | 27 | 11   | 15   |
| 16  | 2 | 26 | 32  | 1    | 12  | 4 | 26 | 56  | 0    | 11  | 6 | 26 | 70  | 13   | -2  | 9  | 26 | 52  | 3    | -5  | 1  | 27 | 5    | 1    |
| -18 | 3 | 26 | 69  | 8    | 13  | 4 | 26 | -46 | 1    | 12  | 6 | 26 | 653 | 8    | -1  | 9  | 26 | 9   | 9    | -4  | 1  | 27 | 255  | 239  |
| -17 | 3 | 26 | 95  | 13   | 14  | 4 | 26 | -21 | 4    | 13  | 6 | 26 | 75  | 25   | 0   | 9  | 26 | 23  | 1    | -3  | 1  | 27 | 7    | 47   |
| -16 | 3 | 26 | 11  | 13   | 15  | 4 | 26 | 36  | 2    | 14  | 6 | 26 | -25 | 0    | 1   | 9  | 26 | -29 | 0    | -2  | 1  | 27 | 343  | 326  |
| -15 | 3 | 26 | -24 | 5    | 16  | 4 | 26 | 7   | 0    | -15 | 7 | 26 | -31 | 19   | 2   | 9  | 26 | 35  | 13   | -1  | 1  | 27 | 91   | 84   |
| -14 | 3 | 26 | 88  | 58   | -17 | 5 | 26 | 88  | 2    | -14 | 7 | 26 | -13 | 4    | 3   | 9  | 26 | -6  | 6    | 0   | 1  | 27 | 224  | 213  |
| -13 | 3 | 26 | 32  | 0    | -16 | 5 | 26 | 42  | 4    | -13 | 7 | 26 | 68  | 17   | 4   | 9  | 26 | -4  | 6    | 1   | 1  | 27 | -3   | 7    |
| -12 | 3 | 26 | 43  | 52   | -15 | 5 | 26 | -5  | 10   | -12 | 7 | 26 | -1  | 23   | 5   | 9  | 26 | 2   | 2    | 2   | 1  | 27 | 131  | 128  |
| 3   | 1 | 27 | 109 | 38   | -1  | 3 | 27 | -15 | 1    | -2  | 5 | 27 | -4  | 0    | 4   | 7  | 27 | 45  | 5    | -1  | 1  | 27 | 65   | 8    |
| 4   | 1 | 27 | 24  | 37   | 0   | 3 | 27 | 83  | 0    | -1  | 5 | 27 | 115 | 139  | 5   | 7  | 27 | 5   | 4    | 0   | 11 | 27 | 28   | 11   |
| 5   | 1 | 27 | 171 | 199  | 1   | 3 | 27 | 32  | 36   | 0   | 5 | 27 | 35  | 6    | 6   | 7  | 27 | 15  | 0    | -18 | 0  | 28 | -40  | 8    |
| 6   | 1 | 27 | -15 | 4    | 2   | 3 | 27 | -5  | 4    | 1   | 5 | 27 | 52  | 68   | 7   | 7  | 27 | -12 | 2    | -16 | 0  | 28 | 75   | 22   |
| 7   | 1 | 27 | 46  | 33   | 3   | 3 | 27 | 88  | 132  | 2   | 5 | 27 | 7   | 2    | 8   | 7  | 27 | 53  | 5    | -14 | 0  | 28 | 14   | 28   |
| 8   | 1 | 27 | 320 | 272  | 4   | 3 | 27 | -24 | 11   | 3   | 5 | 27 | 87  | 100  | 9   | 7  | 27 | -32 | 4    | -12 | 0  | 28 | 61   | 1    |
| 9   | 1 | 27 | 26  | 21   | 5   | 3 | 27 | 5   | 3    | 4   | 5 | 27 | 3   | 9    | 10  | 7  | 27 | -9  | 0    | -10 | 0  | 28 | 90   | 27   |
| 10  | 1 | 27 | 235 | 159  | 6   | 3 | 27 | 134 | 141  | 5   | 5 | 27 | 139 | 102  | 11  | 7  | 27 | -11 | 0    | -8  | 0  | 28 | 499  | 398  |
| 11  | 1 | 27 | -15 | 6    | 7   | 3 | 27 | 149 | 121  | 6   | 5 | 27 | 161 | 119  | 12  | 7  | 27 | 6   | 0    | -6  | 0  | 28 | 1085 | 1062 |
| 12  | 1 | 27 | 15  | 59   | 8   | 3 | 27 | 1   | 1    | 7   | 5 | 27 | -11 | 23   | -12 | 8  | 27 | 227 | 1    | -4  | 0  | 28 | -14  | 11   |
| 13  | 1 | 27 | 45  | 12   | 9   | 3 | 27 | 10  | 19   | 8   | 5 | 27 | 96  | 40   | -11 | 8  | 27 | 13  | 1    | -2  | 0  | 28 | -23  | 5    |
| 14  | 1 | 27 | 26  | 28   | 10  | 3 | 27 | -19 | 10   | 9   | 5 | 27 | 66  | 70   | -10 | 8  | 27 | -1  | 11   | 0   | 0  | 28 | 65   | 0    |
| 15  | 1 | 27 | 184 | 1    | 11  | 3 | 27 | 69  | 8    | 10  | 5 | 27 | -7  | 4    | -9  | 8  | 27 | -19 | 3    | 2   | 0  | 28 | -20  | 1    |
| -19 | 2 | 27 | 19  | 1    | 12  | 3 | 27 | -16 | 12   | 11  | 5 | 27 | -11 | 11   | -8  | 8  | 27 | 16  | 4    | 4   | 0  | 28 | 68   | 17   |
| -18 | 2 | 27 | 48  | 4    | 13  | 3 | 27 | 43  | 9    | 12  | 5 | 27 | 63  | 32   | -7  | 8  | 27 | 2   | 7    | 6   | 0  | 28 | 187  | 251  |
| -17 | 2 | 27 | 24  | 54   | 14  | 3 | 27 | 131 | 4    | 13  | 5 | 27 | 184 | 8    | 6   | 8  | 27 | 14  | 2    | 8   | 0  | 28 | 111  | 49   |
| -16 | 2 | 27 | -15 | 1    | 15  | 3 | 27 | 22  | 14   | 14  | 5 | 27 | 24  | 5    | -5  | 8  | 27 | 2   | 13   | 10  | 0  | 28 | 17   | 2    |
| -15 | 2 | 27 | -5  | 9    | -18 | 4 | 27 | -55 | 26   | 15  | 5 | 27 | 87  | 7    | -4  | 8  | 27 | 57  | 8    | 12  | 0  | 28 | -43  | 3    |
| -14 | 2 | 27 | 44  | 18   | -17 | 4 | 27 | 98  | 6    | -15 | 6 | 27 | -7  | 5    | -3  | 8  | 27 | -6  | 2    | 14  | 0  | 28 | 189  | 41   |
| -13 | 2 | 27 | 26  | 12   | -16 | 4 | 27 | 30  | 27   | -14 | 6 | 27 | 26  | 2    | -2  | 8  | 27 | 38  | 0    | -19 | 1  | 28 | -6   | 5    |
| -12 | 2 | 27 | 32  | 16   | -15 | 4 | 27 | 39  | 39   | -13 | 6 | 27 | 14  | 7    | -1  | 8  | 27 | 3   | 4    | -18 | 1  | 28 | 27   | 12   |
| -11 | 2 | 27 | 23  | 27   | -14 | 4 | 27 | 16  | 8    | -12 | 6 | 27 | 21  | 0    | 0   | 8  | 27 | 28  | 2    | -17 | 1  | 28 | 38   | 49   |
| -10 | 2 | 27 | 119 | 135  | -13 | 4 | 27 | 23  | 0    | -11 | 6 | 27 | 23  | 1    | 1   | 8  | 27 | 3   | 2    | -16 | 1  | 28 | 16   | 6    |
| -9  | 2 | 27 | -19 | 2    | -12 | 4 | 27 | -7  | 59   | -10 | 6 | 27 | 125 | 90   | 2   | 8  | 27 | 18  | 14   | -15 | 1  | 28 | -18  | 10   |
| -8  | 2 | 27 | 51  | 39   | -11 | 4 | 27 | 71  | 13   | -9  | 6 | 27 | -17 | 8    | 3   | 8  | 27 | 19  | 1    | -14 | 1  | 28 | 55   | 20   |
| -7  | 2 | 27 | 813 | 807  | -10 | 4 | 27 | 107 | 133  | -8  | 6 | 27 | 48  | 65   | 4   | 8  | 27 | -12 | 20   | -15 | 1  | 28 | 52   | 54   |
| -6  | 2 | 27 | 1   | 8    | -9  | 4 | 27 | 12  | 2    | -7  | 6 | 27 | 90  | 10   | 5   | 8  | 27 | 13  | 1    | -12 | 1  | 28 | 0    | 0    |
| -5  | 2 | 27 | 176 | 227  | -8  | 4 | 27 | 91  | 66   | -6  | 6 | 27 | 38  | 1    | 6   | 8  | 27 | 47  | 2    | -11 | 1  | 28 | 237  | 202  |
| -4  | 2 | 27 | 6   | 0    | -7  | 4 | 27 | 31  | 8    | -5  | 6 | 27 | 77  | 61   | 7   | 8  | 27 | -4  | 0    | -10 | 1  | 28 | 7    | 17   |
| -3  | 2 | 27 | 2   | 16   | -6  | 4 | 27 | 112 | 124  | -4  | 6 | 27 | 18  | 2    | 8   | 8  | 27 | -23 | 7    | -9  | 1  | 28 | 109  | 119  |
| -2  | 2 | 27 | 38  | 22   | -5  | 4 | 27 | 7   | 2    | -3  | 6 | 27 | 2   | 14   | 9   | 8  | 27 | -5  | 0    | -8  | 1  | 28 | 5    | 1    |
| -1  | 2 | 27 | 69  | 81   | -4  | 4 | 27 | 153 | 153  | -2  | 6 | 27 | 20  | 4    | 10  | 8  | 27 | 0   | 0    | -7  | 1  | 28 | 6    | 32   |
| 0   | 2 | 27 | 54  | 48   | -3  | 4 | 27 | 56  | 51   | -1  | 6 | 27 | 29  | 1    | -10 | 9  | 27 | -19 | 18   | -6  | 1  | 28 | 54   | 69   |
| 1   | 2 | 27 | 13  | 22   | -2  | 4 | 27 | -1  | 9    | 0   | 6 | 27 | -14 | 4    | -9  | 9  | 27 | -22 | 5    | -5  | 1  | 28 | 254  | 259  |
| 2   | 2 | 27 | 22  | 3    | -1  | 4 | 27 | 19  | 2    | 1   | 6 | 27 | 24  | 4    | -8  | 9  | 27 | -2  | 4    | -4  | 1  | 28 | 15   | 1    |
| 3   | 2 | 27 | -23 | 6    | 0   | 4 | 27 | 27  | 5    | 2   | 6 | 27 | 22  | 13   | -7  | 9  | 27 | -15 | 1    | -3  | 1  | 28 | 201  | 145  |
| 4   | 2 | 27 | 114 | 141  | 1   | 4 | 27 | 58  | 30   | 3   | 6 | 27 | -19 | 12   | -6  | 9  | 27 | -11 | 9    | -2  | 1  | 28 | 8    | 5    |
| 5   | 2 | 27 | 33  | 48   | 2   | 4 | 27 | 110 | 145  | 4   | 6 | 27 | 0   | 0    | -5  | 9  | 27 | -8  | 1    | -1  | 1  | 28 | 142  | 148  |
| 6   | 2 | 27 | -1  | 5    | 3   | 4 | 27 | -12 | 18   | 5   | 6 | 27 | 27  | 2    | -4  | 9  | 27 | 0   | 2    | 0   | 1  | 28 | 29   | 36   |
| 7   | 2 | 27 | 2   | 0    | 4   | 4 | 27 | 9   | 23   | 6   | 6 | 27 | -10 | 2    | -3  | 9  | 27 | 9   | 0    | 1   | 1  | 28 | 171  | 182  |
| 8   | 2 | 27 | -7  | 11   | 5   | 4 | 27 | -17 | 3    | 7   | 6 | 27 | -44 | 2    | -2  | 9  | 27 | 7   | 10   | 2   | 1  | 28 | 45   | 20   |
| 9   | 2 | 27 | 27  | 36   | 6   | 4 | 27 | -23 | 42   | 8   | 6 | 27 | 39  | 1    | -1  | 9  | 27 | 17  | 0    | 3   | 1  | 28 | 188  | 199  |
| 10  | 2 | 27 | 27  | 1    | 7   | 4 | 27 | 27  | 2    | 9   | 6 | 27 | 41  | 4    | 0   | 9  | 27 | 33  | 0    | 4   | 1  | 28 | 16   | 50   |
| 11  | 2 | 27 | 27  | 12   | 8   | 4 | 27 | 9   | 8    | 10  | 6 | 27 | 123 | 2    | 1   | 9  | 27 | 11  | 1    | 5   | 1  | 28 | 2    | 1    |
| 12  | 2 | 27 | 15  | 5    | 9   | 4 | 27 | -15 | 10   | 11  | 6 | 27 | -48 | 1    | 2   | 9  | 27 | 8   | 11   | 6   | 1  | 28 | 21   | 23   |
| 13  | 2 | 27 | 115 | 29   | 10  | 4 | 27 | -33 | 25   | 12  | 6 | 27 | 129 | 0    | 3   | 9  | 27 | 4   | 14   | 7   | 1  | 28 | 34   | 71   |
| 14  | 2 | 27 | -15 | 9    | 11  | 4 | 27 | 93  | 6    | 13  | 6 | 27 | -22 | 1    | 4   | 9  | 27 | 18  | 8    | 8   | 1  | 28 | 19   | 1    |
| 15  | 2 | 27 | 48  | 1    | 12  | 4 | 27 | 49  | 23   | 14  | 6 | 27 | 35  | 14   | 5   | 9  | 27 | -16 | 0    | 9   | 1  | 28 | 30   | 17   |
| -19 | 3 | 27 | 92  | 2    | 13  | 4 | 27 | 15  | 0    | -14 | 7 | 27 | 88  | 18   | 6   | 9  | 27 | 1   | 15   | 10  | 1  | 28 | 39   | 21   |
| -18 | 3 | 27 | 86  | 1    | 14  | 4 | 27 | 81  | 14   | -13 | 7 | 27 | -6  | 7    | 7   | 9  | 27 | 42  | 1    | 11  | 1  | 28 | 8    | 7    |
| -17 | 3 | 27 | 21  | 29   | 15  | 4 | 27 | 4   | 7    | -12 | 7 | 27 | 43  | 15   | -7  | 10 | 27 | -38 | 3    | 12  | 1  | 28 | 35   | 4    |
| -16 | 3 | 27 | 93  | 29   | -17 | 5 | 27 | -27 | 13   | -11 | 7 | 27 | 2   | 1    | -6  | 10 | 27 | -38 | 2    | 13  | 1  | 28 | 65   | 8    |
| -15 | 3 | 27 | 9   | 9    | -16 | 5 | 27 | -45 | 1    | -10 | 7 | 27 | 41  | 38   | -5  | 10 | 27 | 16  | 2    | 14  | 1  | 28 | 42   | 12   |
| -14 | 3 | 27 | 37  | 13   | -15 | 5 | 27 | 109 | 92   | -9  | 7 | 27 | 18  | 49   | -4  | 10 | 27 | 27  | 5    | -19 | 2  | 28 | 18   | 2    |
| -13 | 3 | 27 | 127 | 72   | -14 | 5 | 27 | 6   | 0    | -8  | 7 | 27 | 20  | 22   | -3  | 10 | 27 | 58  | 2    | -18 | 2  | 28 | 62   | 25   |
| -12 | 3 | 27 | 56  | 9    | -13 | 5 | 27 | 65  | 10   | -7  | 7 | 27 | 17  | 20   | -2  | 10 | 27 | 99  | 0    | -17 | 2  | 28 | 52   | 14   |
| -11 | 3 | 27 | 48  | 14   | -12 | 5 | 27 | 47  | 13   | -6  | 7 | 27 |     |      |     |    |    |     |      |     |    |    |      |      |

Table B.3, continued

| M   | K | L  | Obs | Calc | M   | K | L  | Obs  | Calc | M   | K  | L  | Obs | Calc | M   | K | L  | Obs | Calc |
|-----|---|----|-----|------|-----|---|----|------|------|-----|----|----|-----|------|-----|---|----|-----|------|
| -18 | 3 | 28 | 152 | 29   | -15 | 5 | 28 | 188  | 77   | -6  | 7  | 28 | -30 | 22   | -19 | 0 | 29 | 11  | 26   |
| -17 | 3 | 28 | 96  | 17   | -14 | 5 | 28 | 115  | 63   | -5  | 7  | 28 | 31  | 15   | -17 | 0 | 29 | -60 | 15   |
| -16 | 3 | 28 | -9  | 16   | -13 | 5 | 28 | 2    | 4    | -4  | 7  | 28 | 59  | 39   | -15 | 0 | 29 | -34 | 60   |
| -15 | 3 | 28 | -25 | 8    | -12 | 5 | 28 | -34  | 4    | -3  | 7  | 28 | 62  | 20   | -13 | 0 | 29 | -6  | 57   |
| -14 | 3 | 28 | 24  | 1    | -11 | 5 | 28 | 34   | 1    | -2  | 7  | 28 | 24  | 4    | -11 | 0 | 29 | 70  | 42   |
| -13 | 3 | 28 | 10  | 10   | -10 | 5 | 28 | 45   | 7    | -1  | 7  | 28 | 65  | 8    | -9  | 0 | 29 | 250 | 278  |
| -12 | 3 | 28 | 20  | 23   | -9  | 5 | 28 | 102  | 52   | 0   | 7  | 28 | 41  | 15   | -7  | 0 | 29 | 62  | 5    |
| -11 | 3 | 28 | -23 | 3    | -8  | 5 | 28 | 93   | 58   | 1   | 7  | 28 | 10  | 30   | -5  | 0 | 29 | 295 | 306  |
| -10 | 3 | 28 | 62  | 29   | -7  | 5 | 28 | 37   | 20   | 2   | 7  | 28 | 24  | 2    | -3  | 0 | 29 | 11  | 10   |
| -9  | 3 | 28 | -22 | 1    | -6  | 5 | 28 | 52   | 33   | 3   | 7  | 28 | 88  | 56   | -1  | 0 | 29 | -1  | 0    |
| -8  | 3 | 28 | 36  | 28   | -5  | 5 | 28 | -5   | 7    | 4   | 7  | 28 | 63  | 9    | 1   | 0 | 29 | 10  | 3    |
| -7  | 3 | 28 | 40  | 13   | -4  | 5 | 28 | 28   | 19   | 5   | 7  | 28 | 94  | 77   | 3   | 0 | 29 | 27  | 24   |
| -6  | 3 | 28 | 39  | 15   | -3  | 5 | 28 | 5    | 5    | 6   | 7  | 28 | 66  | 49   | 5   | 0 | 29 | 122 | 2    |
| -5  | 3 | 28 | 15  | 4    | -2  | 5 | 28 | 24   | 12   | 7   | 7  | 28 | 27  | 37   | 7   | 0 | 29 | 46  | 29   |
| -4  | 3 | 28 | 134 | 126  | -1  | 5 | 28 | 14   | 0    | 8   | 7  | 28 | -29 | 0    | 9   | 0 | 29 | 177 | 10   |
| -3  | 3 | 28 | 15  | 49   | 0   | 5 | 28 | 34   | 15   | 9   | 7  | 28 | -23 | 18   | 11  | 0 | 29 | 49  | 5    |
| -2  | 3 | 28 | 39  | 34   | 1   | 5 | 28 | 41   | 2    | 10  | 7  | 28 | 21  | 7    | 13  | 0 | 29 | 103 | 7    |
| -1  | 3 | 28 | 29  | 20   | 2   | 5 | 28 | 25   | 18   | 11  | 7  | 28 | -9  | 10   | -19 | 1 | 29 | 74  | 40   |
| 0   | 3 | 28 | 35  | 23   | 3   | 5 | 28 | 39   | 0    | 12  | 7  | 28 | -31 | 9    | -18 | 1 | 29 | 23  | 13   |
| 1   | 3 | 28 | 3   | 3    | 4   | 5 | 28 | 31   | 30   | -11 | 0  | 29 | 74  | 0    | -17 | 1 | 29 | 19  | 55   |
| 2   | 3 | 28 | 141 | 113  | 5   | 5 | 28 | 2    | 1    | -10 | 0  | 29 | 2   | 10   | -16 | 1 | 29 | 102 | 0    |
| 3   | 3 | 28 | 18  | 31   | 6   | 5 | 28 | -31  | 7    | -9  | 0  | 29 | 11  | 1    | -15 | 1 | 29 | 9   | 0    |
| 4   | 3 | 28 | 193 | 185  | 7   | 5 | 28 | 79   | 25   | -8  | 0  | 29 | 8   | 31   | -14 | 1 | 29 | 36  | 15   |
| 5   | 3 | 28 | 19  | 0    | 8   | 5 | 28 | 38   | 20   | -7  | 8  | 28 | 7   | 1    | -13 | 1 | 29 | -19 | 42   |
| 6   | 3 | 28 | 37  | 1    | 9   | 5 | 28 | -55  | 1    | -6  | 8  | 28 | -8  | 0    | -12 | 1 | 29 | 26  | 47   |
| 7   | 3 | 28 | 212 | 191  | 10  | 5 | 28 | 19   | 9    | -5  | 8  | 28 | -8  | 17   | -11 | 1 | 29 | 66  | 28   |
| 8   | 3 | 28 | 289 | 261  | 11  | 5 | 28 | 32   | 0    | -4  | 8  | 28 | 11  | 6    | -10 | 1 | 29 | 263 | 261  |
| 9   | 3 | 28 | 39  | 23   | 12  | 5 | 28 | 17   | 4    | -3  | 8  | 28 | 54  | 30   | -9  | 1 | 29 | 191 | 221  |
| 10  | 3 | 28 | -2  | 9    | 13  | 5 | 28 | -21  | 0    | -2  | 8  | 28 | 50  | 1    | -8  | 1 | 29 | -18 | 5    |
| 11  | 3 | 28 | -10 | 7    | 14  | 5 | 28 | 37   | 2    | -1  | 0  | 29 | 5   | 14   | -7  | 1 | 29 | 33  | 58   |
| 12  | 3 | 28 | 9   | 33   | -15 | 6 | 28 | 32   | 1    | 0   | 0  | 29 | -2  | 8    | -6  | 1 | 29 | 83  | 68   |
| 13  | 3 | 28 | 2   | 0    | -14 | 6 | 28 | 32   | 4    | 1   | 8  | 28 | 53  | 0    | -5  | 1 | 29 | 118 | 122  |
| 14  | 3 | 28 | -43 | 24   | -13 | 6 | 28 | 0    | 2    | 2   | 8  | 28 | 0   | 10   | -4  | 1 | 29 | 200 | 196  |
| 15  | 3 | 28 | 70  | 35   | -12 | 6 | 28 | 60   | 29   | 3   | 8  | 28 | 28  | 4    | -3  | 1 | 29 | 9   | 20   |
| 16  | 3 | 28 | -34 | 0    | -11 | 6 | 28 | -40  | 2    | 4   | 8  | 28 | -20 | 13   | -2  | 1 | 29 | 160 | 194  |
| 17  | 3 | 28 | 18  | 19   | -10 | 6 | 28 | 49   | 7    | 5   | 8  | 28 | 11  | 1    | -1  | 1 | 29 | 27  | 103  |
| 18  | 3 | 28 | 30  | 2    | -9  | 6 | 28 | 27   | 76   | 6   | 8  | 28 | 47  | 17   | 0   | 1 | 29 | 125 | 103  |
| 19  | 3 | 28 | 56  | 3    | -8  | 6 | 28 | 67   | 7    | 7   | 8  | 28 | 20  | 0    | 1   | 1 | 29 | 216 | 211  |
| 20  | 3 | 28 | -20 | 2    | -7  | 6 | 28 | 19   | 4    | 8   | 8  | 28 | -40 | 3    | 2   | 1 | 29 | 209 | 167  |
| 21  | 3 | 28 | -7  | 11   | -6  | 6 | 28 | 11   | 1    | 9   | 8  | 28 | -12 | 3    | 3   | 1 | 29 | 133 | 145  |
| 22  | 3 | 28 | -11 | 11   | -5  | 6 | 28 | 26   | 1    | -8  | 9  | 28 | -12 | 0    | 4   | 1 | 29 | 46  | 1    |
| 23  | 3 | 28 | -23 | 22   | -4  | 6 | 28 | 21   | 18   | -7  | 9  | 28 | 8   | 5    | 5   | 1 | 29 | -30 | 0    |
| 24  | 3 | 28 | 1   | 5    | -3  | 6 | 28 | 6    | 19   | -6  | 9  | 28 | -8  | 6    | 6   | 1 | 29 | 44  | 46   |
| 25  | 3 | 28 | -22 | 0    | -2  | 6 | 28 | 50   | 18   | -5  | 9  | 28 | 25  | 3    | 7   | 1 | 29 | -29 | 17   |
| 26  | 3 | 28 | 13  | 36   | -13 | 6 | 28 | -11  | 5    | 6   | 8  | 28 | -45 | 0    | 4   | 1 | 30 | 107 | 122  |
| 27  | 3 | 28 | 93  | 8    | -12 | 6 | 28 | 17   | 0    | 7   | 8  | 28 | 27  | 5    | 5   | 1 | 30 | 42  | 5    |
| 28  | 3 | 28 | 95  | 3    | -11 | 6 | 28 | 39   | 3    | 8   | 8  | 28 | -23 | 1    | 6   | 1 | 30 | 10  | 0    |
| 29  | 3 | 28 | -93 | 4    | -10 | 6 | 28 | 4    | 0    | 9   | 8  | 28 | -18 | 0    | 7   | 1 | 30 | 45  | 37   |
| 30  | 3 | 28 | -57 | 21   | -9  | 6 | 28 | 33   | 1    | -7  | 9  | 28 | 126 | 19   | 8   | 1 | 30 | 363 | 38   |
| 31  | 3 | 28 | 86  | 0    | -8  | 6 | 28 | 6    | 0    | -6  | 9  | 28 | 22  | 12   | 10  | 1 | 30 | 87  | 5    |
| 32  | 3 | 28 | 163 | 13   | -7  | 6 | 28 | 23   | 1    | -5  | 9  | 28 | 49  | 14   | 11  | 1 | 30 | 20  | 23   |
| 33  | 3 | 28 | 35  | 4    | -6  | 6 | 28 | 16   | 14   | -4  | 9  | 28 | 50  | 11   | 12  | 1 | 30 | 15  | 27   |
| 34  | 3 | 28 | 75  | 32   | -5  | 6 | 28 | 48   | 15   | -3  | 9  | 28 | 32  | 1    | -19 | 2 | 30 | 16  | 16   |
| 35  | 3 | 28 | 12  | 17   | -4  | 6 | 28 | 20   | 6    | -2  | 9  | 28 | -2  | 45   | -18 | 2 | 30 | -73 | 5    |
| 36  | 3 | 28 | 43  | 2    | -3  | 6 | 28 | 183  | 72   | -1  | 9  | 28 | 15  | 6    | -17 | 2 | 30 | 102 | 6    |
| 37  | 3 | 28 | 25  | 15   | -2  | 6 | 28 | 3    | 2    | 0   | 9  | 28 | 44  | 1    | -16 | 2 | 30 | 25  | 19   |
| 38  | 3 | 28 | 11  | 32   | -1  | 6 | 28 | 87   | 19   | 1   | 9  | 28 | 48  | 1    | -15 | 2 | 30 | -34 | 3    |
| 39  | 3 | 28 | 110 | 36   | 0   | 6 | 28 | 19   | 12   | 2   | 9  | 28 | -6  | 17   | -14 | 2 | 30 | 84  | 1    |
| 40  | 3 | 28 | 4   | 38   | 1   | 6 | 28 | 35   | 17   | 3   | 9  | 28 | 98  | 35   | -13 | 2 | 30 | 19  | 3    |
| 41  | 3 | 28 | 38  | 5    | 2   | 6 | 28 | 65   | 45   | 4   | 9  | 28 | 5   | 0    | -12 | 2 | 30 | -11 | 1    |
| 42  | 3 | 28 | 8   | 37   | 3   | 6 | 28 | 35   | 0    | 5   | 9  | 28 | 55  | 1    | -11 | 2 | 30 | 70  | 58   |
| 43  | 3 | 28 | 53  | 15   | 4   | 6 | 28 | 84   | 41   | 6   | 9  | 28 | 4   | 2    | -10 | 2 | 30 | -23 | 4    |
| 44  | 3 | 28 | 50  | 60   | 5   | 6 | 28 | -24  | 9    | -3  | 10 | 28 | 32  | 1    | -9  | 2 | 30 | 39  | 1    |
| 45  | 3 | 28 | 7   | 26   | 6   | 6 | 28 | 23   | 1    | -2  | 10 | 28 | -80 | 0    | -8  | 2 | 30 | -19 | 1    |
| 46  | 3 | 28 | -16 | 7    | 7   | 6 | 28 | -3   | 0    | -1  | 10 | 28 | -19 | 1    | -7  | 2 | 30 | 96  | 51   |
| 47  | 3 | 28 | 9   | 1    | 8   | 6 | 28 | -59  | 8    | 0   | 10 | 28 | 122 | 1    | -6  | 2 | 30 | 16  | 9    |
| 48  | 3 | 28 | 35  | 65   | 9   | 6 | 28 | 54   | 0    | 1   | 10 | 28 | 89  | 3    | -5  | 2 | 30 | 29  | 0    |
| 49  | 3 | 28 | 22  | 1    | 10  | 6 | 28 | -12  | 3    | 2   | 10 | 28 | 35  | 3    | -4  | 2 | 30 | -5  | 13   |
| 50  | 3 | 28 | 22  | 20   | 11  | 6 | 28 | -38  | 7    | 3   | 10 | 28 | 383 | 3    | -3  | 2 | 30 | 21  | 3    |
| 51  | 3 | 28 | 5   | 13   | 12  | 6 | 28 | 1224 | 8    | -20 | 0  | 30 | 726 | 1    | -2  | 2 | 30 | 28  | 0    |
| 52  | 3 | 28 | 32  | 21   | -12 | 7 | 28 | 54   | 0    | -18 | 0  | 30 | -88 | 14   | -1  | 2 | 30 | 100 | 65   |
| 53  | 3 | 28 | -31 | 7    | -11 | 7 | 28 | 2    | 13   | -16 | 0  | 30 | -54 | 20   | 0   | 2 | 30 | -22 | 30   |
| 54  | 3 | 28 | 48  | 57   | -10 | 7 | 28 | 32   | 46   | -14 | 0  | 30 | -47 | 0    | 1   | 2 | 30 | 1   | 1    |
| 55  | 3 | 28 | 24  | 5    | -9  | 7 | 28 | -9   | 1    | -12 | 0  | 30 | 53  | 1    | 2   | 2 | 30 | 1   | 19   |
| 56  | 3 | 28 | 22  | 10   | -8  | 7 | 28 | -7   | 1    | -10 | 0  | 30 | 18  | 29   | 3   | 2 | 30 | -16 | 18   |
| 57  | 3 | 28 | 66  | 5    | -7  | 7 | 28 | 24   | 9    | -8  | 0  | 30 | 137 | 179  | 4   | 2 | 30 | 45  | 44   |
| 58  | 3 | 28 | 3   | 11   | -6  | 7 | 28 | 13   | 13   | -6  | 0  | 30 | 62  | 31   | 5   | 2 | 30 | 44  | 33   |
| 59  | 3 | 28 | 10  | 4    | -5  | 7 | 28 | -10  | 0    | -4  | 0  | 30 | 47  | 68   | 6   | 2 | 30 | -20 | 7    |
| 60  | 3 | 28 | 71  | 0    | -4  | 7 | 28 | -8   | 7    | -2  | 0  | 30 | 100 | 32   | 7   | 2 | 30 | 16  | 41   |
| 61  | 3 | 28 | 158 | 2    | -3  | 7 | 28 | -2   | 2    | 0   | 0  | 30 | -23 | 4    | 8   | 2 | 30 | -9  | 7    |
| 62  | 3 | 28 | 89  | 13   | -2  | 7 | 28 | 13   | 10   | 2   | 0  | 30 | 36  | 9    | 9   | 2 | 30 | 28  | 3    |
| 63  | 3 | 28 | -26 | 1    | -1  | 7 | 28 | 58   | 29   | 4   | 0  | 30 | 6   | 2    | 10  | 2 | 30 | -37 | 9    |
| 64  | 3 | 28 | 70  | 11   | 0   | 7 | 28 | 20   | 14   | 6   | 0  | 30 | -45 | 0    | 11  | 2 | 30 | 63  | 1    |
| 65  | 3 | 28 | 49  | 4    | 1   | 7 | 28 | 80   | 19   | 8   | 0  | 30 | 41  | 5    | 12  | 2 | 30 | 64  | 0    |
| 66  | 3 | 28 | -10 | 1    | 2   | 7 | 28 | -13  | 1    | 10  | 0  | 30 | -37 | 0    | -18 | 3 | 30 | 128 | 7    |
| 67  | 3 | 28 | 40  | 12   | 3   | 7 | 28 | 39   | 3    | 12  | 0  | 30 | -27 | 6    | -17 | 3 | 30 | 56  | 0    |
| 68  | 3 | 28 | 76  | 44   | 4   | 7 | 28 | 13   | 10   | -20 | 1  | 30 | -1  | 8    | -16 | 3 | 30 | 2   | 18   |
| 69  | 3 | 28 | 2   | 2    | 5   | 7 | 28 | 68   | 8    | -19 | 1  | 30 | -34 | 0    | -15 | 3 | 30 | 49  | 2    |
| 70  | 3 | 28 | 38  | 75   | 6   | 7 |    |      |      |     |    |    |     |      |     |   |    |     |      |

Table B.3, continued

| M   | K | L  | Obs | Calc | M   | K | L  | Obs | Calc | M   | K | L  | Obs | Calc | M   | K | L  | Obs | Calc | M   | K | L  | Obs | Calc |
|-----|---|----|-----|------|-----|---|----|-----|------|-----|---|----|-----|------|-----|---|----|-----|------|-----|---|----|-----|------|
| 8   | 5 | 29 | -14 | 1    | -1  | 0 | 29 | 18  | 15   | -3  | 1 | 30 | 97  | 100  | 1   | 3 | 30 | 43  | 1    | -13 | 6 | 30 | -31 | 0    |
| 9   | 5 | 29 | -7  | 0    | 0   | 0 | 29 | 45  | 6    | -2  | 1 | 30 | -12 | 2    | 2   | 3 | 30 | 129 | 162  | -12 | 6 | 30 | 82  | 2    |
| 10  | 5 | 29 | -33 | 1    | 1   | 0 | 29 | -10 | 21   | -1  | 1 | 30 | 46  | 50   | 3   | 3 | 30 | 36  | 11   | -11 | 6 | 30 | 3   | 0    |
| 11  | 5 | 29 | 23  | 1    | 2   | 0 | 29 | -14 | 0    | 0   | 1 | 30 | 32  | 25   | 4   | 3 | 30 | 37  | 65   | -10 | 6 | 30 | -18 | 0    |
| 12  | 5 | 29 | 73  | 0    | 3   | 0 | 29 | 18  | 9    | 1   | 1 | 30 | 39  | 4    | 5   | 3 | 30 | 58  | 13   | -9  | 6 | 30 | 46  | 12   |
| 13  | 5 | 29 | 24  | 2    | 4   | 0 | 29 | -44 | 2    | 2   | 1 | 30 | 212 | 206  | 6   | 3 | 30 | -12 | 1    | -8  | 6 | 30 | -1  | 0    |
| -14 | 6 | 29 | 15  | 15   | 5   | 0 | 29 | 51  | 41   | 3   | 1 | 30 | 15  | 12   | 7   | 3 | 30 | 97  | 43   | -7  | 6 | 30 | -17 | 2    |
| -6  | 6 | 30 | 41  | 1    | 4   | 9 | 30 | -23 | 1    | -2  | 1 | 31 | -22 | 2    | 7   | 4 | 31 | 67  | 0    | 6   | 7 | 31 | -10 | 2    |
| -5  | 6 | 30 | -8  | 0    | 5   | 9 | 30 | 37  | 9    | -1  | 2 | 31 | 53  | 5    | 8   | 4 | 31 | 54  | 0    | 7   | 7 | 31 | -9  | 2    |
| -4  | 6 | 30 | 34  | 69   | -19 | 0 | 31 | 119 | 7    | 0   | 2 | 31 | 46  | 4    | 9   | 4 | 31 | 32  | 1    | 8   | 7 | 31 | 38  | 1    |
| -3  | 6 | 30 | 50  | 42   | -17 | 0 | 31 | 725 | 3    | 1   | 2 | 31 | 18  | 36   | 10  | 4 | 31 | 1   | 0    | -6  | 8 | 31 | 52  | 8    |
| -2  | 6 | 30 | 25  | 15   | -15 | 0 | 31 | 7   | 1    | 2   | 2 | 31 | 70  | 21   | 11  | 4 | 31 | -19 | 5    | -5  | 8 | 31 | 8   | 10   |
| -1  | 6 | 30 | 20  | 1    | -13 | 0 | 31 | -24 | 1    | 3   | 2 | 31 | 13  | 16   | -14 | 5 | 31 | 6   | 17   | -4  | 8 | 31 | 63  | 0    |
| 0   | 6 | 30 | -9  | 1    | -11 | 0 | 31 | 25  | 1    | 4   | 2 | 31 | 38  | 40   | -13 | 5 | 31 | -23 | 33   | -3  | 8 | 31 | -2  | 1    |
| 1   | 6 | 30 | 44  | 16   | -9  | 0 | 31 | 165 | 221  | 5   | 2 | 31 | -3  | 3    | -12 | 5 | 31 | 12  | 0    | -2  | 8 | 31 | 6   | 1    |
| 2   | 6 | 30 | 11  | 8    | -7  | 0 | 31 | 38  | 43   | 6   | 2 | 31 | -3  | 40   | -11 | 5 | 31 | 31  | 7    | -1  | 8 | 31 | 76  | 0    |
| 3   | 6 | 30 | 46  | 5    | -5  | 0 | 31 | -42 | 21   | 7   | 2 | 31 | -6  | 1    | -10 | 5 | 31 | 44  | 37   | 0   | 8 | 31 | 0   | 2    |
| 4   | 6 | 30 | 33  | 11   | -3  | 0 | 31 | 37  | 9    | 8   | 2 | 31 | 104 | 12   | -9  | 5 | 31 | 21  | 40   | 1   | 8 | 31 | 6   | 7    |
| 5   | 6 | 30 | 10  | 1    | -1  | 0 | 31 | -12 | 22   | 9   | 2 | 31 | 75  | 2    | -8  | 5 | 31 | -28 | 2    | 2   | 8 | 31 | 18  | 8    |
| 6   | 6 | 30 | 55  | 0    | 1   | 0 | 31 | 24  | 55   | 10  | 2 | 31 | 2   | 0    | -7  | 5 | 31 | -23 | 37   | 3   | 8 | 31 | 24  | 1    |
| 7   | 6 | 30 | -1  | 1    | 3   | 0 | 31 | 96  | 19   | 11  | 2 | 31 | -5  | 0    | -6  | 5 | 31 | 80  | 41   | 4   | 8 | 31 | 36  | 5    |
| 8   | 6 | 30 | -3  | 3    | 5   | 0 | 31 | -60 | 9    | -17 | 3 | 31 | 97  | 12   | -5  | 5 | 31 | 40  | 46   | 5   | 8 | 31 | 27  | 2    |
| 9   | 6 | 30 | -11 | 0    | 7   | 0 | 31 | 117 | 20   | -16 | 3 | 31 | 162 | 9    | -4  | 5 | 31 | 15  | 3    | 6   | 8 | 31 | 19  | 1    |
| 10  | 6 | 30 | 0   | 4    | 9   | 0 | 31 | 16  | 18   | -15 | 3 | 31 | -38 | 1    | -3  | 5 | 31 | 34  | 17   | -1  | 9 | 31 | 65  | 5    |
| 11  | 6 | 30 | 11  | 1    | 11  | 0 | 31 | 48  | 7    | -14 | 3 | 31 | 141 | 27   | -2  | 5 | 31 | -30 | 3    | 0   | 9 | 31 | -35 | 1    |
| -11 | 7 | 30 | 90  | 10   | -19 | 1 | 31 | 280 | 6    | -13 | 3 | 31 | 20  | 3    | -1  | 5 | 31 | 10  | 7    | 1   | 9 | 31 | -20 | 14   |
| -10 | 7 | 30 | -20 | 10   | -18 | 1 | 31 | 4   | 39   | -12 | 3 | 31 | 41  | 6    | 0   | 5 | 31 | -10 | 2    | 2   | 9 | 31 | -39 | 0    |
| -9  | 7 | 30 | 63  | 71   | -17 | 1 | 31 | -26 | 2    | -11 | 3 | 31 | -14 | 11   | 1   | 5 | 31 | 51  | 11   | -18 | 0 | 32 | 99  | 4    |
| -8  | 7 | 30 | 7   | 0    | -16 | 1 | 31 | 61  | 52   | -10 | 3 | 31 | 48  | 5    | 2   | 5 | 31 | -3  | 2    | -16 | 0 | 32 | -2  | 25   |
| -7  | 7 | 30 | 15  | 22   | -15 | 1 | 31 | -27 | 5    | -9  | 3 | 31 | 53  | 14   | 5   | 3 | 31 | 28  | 5    | -14 | 0 | 32 | 83  | 1    |
| -6  | 7 | 30 | 15  | 0    | -14 | 1 | 31 | 38  | 66   | -8  | 3 | 31 | 54  | 32   | 4   | 5 | 31 | 14  | 2    | -12 | 0 | 32 | 18  | 0    |
| -5  | 7 | 30 | 75  | 51   | -13 | 1 | 31 | 11  | 17   | -7  | 3 | 31 | 0   | 48   | 5   | 5 | 31 | -15 | 17   | -10 | 0 | 32 | 29  | 3    |
| -4  | 7 | 30 | 40  | 5    | -12 | 1 | 31 | 172 | 115  | -6  | 3 | 31 | 20  | 6    | 6   | 5 | 31 | 3   | 1    | -8  | 0 | 32 | 51  | 97   |
| -3  | 7 | 30 | 37  | 29   | -11 | 1 | 31 | -14 | 6    | -5  | 3 | 31 | 50  | 6    | 7   | 5 | 31 | 178 | 33   | -6  | 0 | 32 | 9   | 13   |
| -2  | 7 | 30 | 17  | 16   | -10 | 1 | 31 | 157 | 143  | -4  | 3 | 31 | -20 | 2    | 8   | 5 | 31 | 20  | 17   | -4  | 0 | 32 | 174 | 191  |
| -1  | 7 | 30 | 74  | 28   | -9  | 1 | 31 | 80  | 137  | -3  | 3 | 31 | 19  | 11   | 9   | 5 | 31 | -38 | 2    | -2  | 0 | 32 | 46  | 30   |
| 0   | 7 | 30 | 29  | 8    | -8  | 1 | 31 | -7  | 25   | -2  | 3 | 31 | -3  | 3    | 10  | 5 | 31 | -6  | 4    | 0   | 0 | 32 | 66  | 0    |
| 1   | 7 | 30 | 6   | 32   | -7  | 1 | 31 | 16  | 0    | -1  | 3 | 31 | 24  | 2    | -11 | 6 | 31 | -13 | 15   | 2   | 0 | 32 | 236 | 158  |
| 2   | 7 | 30 | 44  | 1    | -6  | 1 | 31 | 79  | 48   | 0   | 3 | 31 | 1   | 1    | -10 | 6 | 31 | 26  | 4    | 4   | 0 | 32 | 51  | 3    |
| 3   | 7 | 30 | 0   | 38   | -5  | 1 | 31 | 130 | 110  | 1   | 3 | 31 | 128 | 40   | -9  | 6 | 31 | 16  | 11   | 6   | 0 | 32 | 2   | 59   |
| 4   | 7 | 30 | -10 | 19   | -4  | 1 | 31 | 148 | 144  | 2   | 3 | 31 | -24 | 18   | 8   | 6 | 31 | 0   | 36   | 8   | 0 | 32 | 22  | 7    |
| 5   | 7 | 30 | 3   | 0    | -3  | 1 | 31 | 79  | 54   | 3   | 3 | 31 | 98  | 97   | -7  | 6 | 31 | 45  | 8    | 10  | 0 | 32 | 210 | 29   |
| 6   | 7 | 30 | -23 | 5    | -2  | 1 | 31 | 127 | 108  | 4   | 3 | 31 | 15  | 34   | -6  | 6 | 31 | 70  | 4    | -18 | 1 | 32 | 134 | 4    |
| 7   | 7 | 30 | -9  | 17   | -1  | 1 | 31 | 11  | 0    | 5   | 3 | 31 | 32  | 33   | -5  | 6 | 31 | 1   | 0    | -17 | 1 | 32 | 33  | 32   |
| 8   | 7 | 30 | -1  | 0    | 0   | 1 | 31 | 9   | 33   | 6   | 3 | 31 | 30  | 15   | -4  | 6 | 31 | -7  | 8    | -16 | 1 | 32 | 5   | 0    |
| 9   | 7 | 30 | 32  | 8    | 1   | 1 | 31 | 32  | 4    | 7   | 3 | 31 | 69  | 7    | -3  | 6 | 31 | 3   | 10   | -15 | 1 | 32 | 41  | 14   |
| 10  | 7 | 30 | -13 | 3    | 2   | 1 | 31 | 46  | 50   | 8   | 3 | 31 | 113 | 82   | -2  | 6 | 31 | 22  | 41   | -14 | 1 | 32 | -47 | 2    |
| -8  | 8 | 30 | 123 | 2    | 3   | 1 | 31 | -13 | 10   | 9   | 3 | 31 | -19 | 4    | -1  | 6 | 31 | 41  | 59   | -13 | 1 | 32 | 66  | 42   |
| -7  | 8 | 30 | 86  | 17   | 4   | 1 | 31 | 120 | 46   | 10  | 3 | 31 | -28 | 6    | 0   | 6 | 31 | 18  | 47   | -12 | 1 | 32 | 113 | 24   |
| -6  | 8 | 30 | 16  | 7    | 5   | 1 | 31 | -28 | 14   | 11  | 3 | 31 | 44  | 6    | 1   | 6 | 31 | -20 | 15   | -11 | 1 | 32 | 41  | 49   |
| -5  | 8 | 30 | 30  | 5    | 6   | 1 | 31 | 93  | 117  | -16 | 4 | 31 | 29  | 20   | 2   | 6 | 31 | 25  | 27   | -10 | 1 | 32 | 45  | 20   |
| -4  | 8 | 30 | 35  | 0    | 7   | 1 | 31 | -9  | 0    | -15 | 4 | 31 | 75  | 4    | 3   | 6 | 31 | 36  | 31   | -9  | 1 | 32 | 52  | 42   |
| -3  | 8 | 30 | -5  | 11   | 8   | 1 | 31 | -50 | 33   | -14 | 4 | 31 | 0   | 0    | 4   | 6 | 31 | 30  | 0    | -8  | 1 | 32 | 103 | 88   |
| -2  | 8 | 30 | 31  | 12   | 9   | 1 | 31 | -27 | 11   | -13 | 4 | 31 | -23 | 0    | 5   | 6 | 31 | 67  | 32   | -7  | 1 | 32 | 21  | 1    |
| -1  | 8 | 30 | 9   | 2    | 10  | 1 | 31 | -42 | 12   | -12 | 4 | 31 | 87  | 40   | 6   | 6 | 31 | -28 | 8    | -6  | 1 | 32 | 21  | 34   |
| 0   | 8 | 30 | -14 | 7    | 11  | 1 | 31 | -19 | 0    | -11 | 4 | 31 | -37 | 1    | 7   | 6 | 31 | 4   | 6    | -5  | 1 | 32 | 77  | 112  |
| 1   | 8 | 30 | -10 | 3    | -19 | 2 | 31 | 85  | 11   | -10 | 4 | 31 | -10 | 5    | 8   | 6 | 31 | -41 | 0    | -4  | 1 | 32 | 41  | 6    |
| 2   | 8 | 30 | -20 | 16   | -18 | 2 | 31 | 0   | 12   | -9  | 4 | 31 | 17  | 1    | 9   | 6 | 31 | 15  | 3    | -3  | 1 | 32 | 94  | 53   |
| 3   | 8 | 30 | -34 | 0    | -17 | 2 | 31 | -10 | 3    | -8  | 4 | 31 | 8   | 5    | -9  | 7 | 31 | 63  | 3    | -2  | 1 | 32 | 70  | 11   |
| 4   | 8 | 30 | -16 | 0    | -16 | 2 | 31 | 85  | 0    | -7  | 4 | 31 | 31  | 7    | -8  | 7 | 31 | 64  | 0    | -1  | 1 | 32 | 31  | 42   |
| 5   | 8 | 30 | 54  | 7    | -15 | 2 | 31 | -31 | 1    | -6  | 4 | 31 | 0   | 0    | -7  | 7 | 31 | 34  | 3    | 0   | 1 | 32 | 87  | 48   |
| 6   | 8 | 30 | 0   | 7    | -14 | 2 | 31 | 13  | 21   | -5  | 4 | 31 | 40  | 12   | -6  | 7 | 31 | 28  | 8    | 1   | 1 | 32 | 49  | 23   |
| 7   | 8 | 30 | 109 | 0    | -13 | 2 | 31 | -21 | 1    | -4  | 4 | 31 | -12 | 0    | -5  | 7 | 31 | 0   | 3    | 2   | 1 | 32 | 17  | 55   |
| 8   | 8 | 30 | -15 | 2    | -12 | 2 | 31 | 84  | 8    | -3  | 4 | 31 | 33  | 1    | -4  | 7 | 31 | -31 | 0    | 3   | 3 | 32 | 32  | 32   |
| -5  | 9 | 30 | 97  | 0    | -11 | 2 | 31 | 18  | 0    | -2  | 3 | 31 | 8   | 7    | -3  | 7 | 31 | 32  | 0    | 4   | 1 | 32 | 95  | 1    |
| -4  | 9 | 30 | 10  | 10   | -10 | 2 | 31 | -27 | 6    | -1  | 4 | 31 | -22 | 0    | -2  | 7 | 31 | 11  | 0    | 5   | 1 | 32 | 73  | 39   |
| -3  | 9 | 30 | 1   | 2    | -9  | 2 | 31 | 15  | 15   | 0   | 4 | 31 | -6  | 3    | -1  | 7 | 31 | -30 | 7    | 6   | 1 | 32 | 58  | 1    |
| -2  | 9 | 30 | -30 | 2    | -8  | 2 | 31 | 21  | 13   | 1   | 4 | 31 | 15  | 18   | 0   | 7 | 31 | -33 | 3    | 7   | 1 | 32 | 45  | 27   |
| -1  | 9 | 30 | 19  | 1    | -7  | 2 | 31 | 40  | 12   | 2   | 4 | 31 | 10  | 1    | 1   | 7 | 31 | 55  | 0    | 8   | 1 | 32 | -7  | 0    |
| 0   | 9 | 30 | 5   | 12   | -6  | 2 | 31 | 72  | 83   | 3   | 4 | 31 | -15 | 0    | 2   | 7 | 31 | -7  | 6    | 9   | 1 | 32 | -2  | 4    |
| 1   | 9 | 30 | 77  | 4    | -5  | 2 | 31 | 3   | 50   | 4   | 4 | 31 | 20  | 25   | 3   | 7 | 31 | -46 | 7    | 10  | 1 | 32 | 198 | 2    |
| 2   | 9 | 30 | -33 | 0    | -4  | 2 | 31 | 2   | 3    | 5   | 4 | 31 | -14 | 13   | 4   | 7 | 31 | 17  | 23   | -18 | 2 | 32 | 17  | 5    |
| 3   | 9 | 30 | 86  | 4    | -3  | 2 |    |     |      |     |   |    |     |      |     |   |    |     |      |     |   |    |     |      |

Table B.3, continued

| M   | K | L  | Obs | Calc | M   | K | L  | Obs | Calc | M   | K | L  | Obs | Calc | M   | K | L  | Obs | Calc | M   | K  | L  | Obs | Calc |    |
|-----|---|----|-----|------|-----|---|----|-----|------|-----|---|----|-----|------|-----|---|----|-----|------|-----|----|----|-----|------|----|
| -14 | 3 | 32 | 45  | 11   | 4   | 5 | 32 | -18 | 6    | -12 | 1 | 33 | -50 | 28   | 2   | 3 | 33 | 75  | 3    | 5   | 6  | 33 | -5  | 4    |    |
| -13 | 3 | 32 | 53  | 29   | 5   | 5 | 32 | 216 | 22   | -11 | 1 | 33 | 65  | 8    | 3   | 3 | 33 | 174 | 24   | -7  | 7  | 33 | 74  | 1    |    |
| -12 | 3 | 32 | 11  | 6    | 6   | 5 | 32 | -13 | 24   | -10 | 1 | 33 | 133 | 76   | 4   | 3 | 33 | -48 | 0    | -6  | 7  | 33 | 5   | 9    |    |
| -11 | 3 | 32 | -5  | 0    | 7   | 5 | 32 | 16  | 0    | -9  | 1 | 33 | 173 | 32   | 5   | 3 | 33 | 40  | 9    | -5  | 7  | 33 | -15 | 11   |    |
| -10 | 3 | 32 | 137 | 165  | 8   | 5 | 32 | 26  | 30   | -8  | 1 | 33 | 92  | 41   | 6   | 3 | 33 | -16 | 17   | -4  | 7  | 33 | -10 | 28   |    |
| -9  | 3 | 32 | 32  | 48   | -11 | 6 | 32 | 116 | 2    | -7  | 1 | 33 | 32  | 1    | 7   | 3 | 33 | 14  | 16   | -3  | 7  | 33 | -56 | 0    |    |
| -8  | 3 | 32 | -26 | 9    | -10 | 6 | 32 | 32  | 9    | -6  | 1 | 33 | 49  | 44   | 8   | 3 | 33 | 31  | 5    | -2  | 7  | 33 | 53  | 1    |    |
| -7  | 3 | 32 | -11 | 22   | -9  | 6 | 32 | 53  | 2    | -5  | 1 | 33 | -10 | 5    | -15 | 4 | 33 | 0   | 24   | -1  | 7  | 33 | 51  | 1    |    |
| -6  | 3 | 32 | 4   | 23   | -8  | 6 | 32 | -23 | 1    | -4  | 1 | 33 | 84  | 94   | -14 | 4 | 33 | -34 | 10   | 1   | 7  | 33 | 24  | 9    |    |
| -5  | 3 | 32 | 35  | 45   | -7  | 6 | 32 | -1  | 4    | -3  | 1 | 33 | 27  | 1    | -13 | 4 | 33 | -41 | 8    | 2   | 7  | 33 | -1  | 21   |    |
| -4  | 3 | 32 | 138 | 116  | -6  | 6 | 32 | 29  | 12   | -2  | 1 | 33 | 23  | 37   | -12 | 4 | 33 | -39 | 30   | 3   | 7  | 33 | 37  | 2    |    |
| -3  | 3 | 32 | 28  | 12   | -5  | 6 | 32 | 15  | 25   | -1  | 1 | 33 | 20  | 2    | -11 | 4 | 33 | 39  | 2    | -3  | 8  | 33 | -58 | 9    |    |
| -2  | 3 | 32 | 187 | 136  | -4  | 6 | 32 | 30  | 23   | 0   | 1 | 33 | 9   | 17   | -10 | 4 | 33 | -24 | 21   | 0   | 8  | 33 | -52 | 7    |    |
| -1  | 3 | 32 | 16  | 3    | -3  | 6 | 32 | 0   | 21   | 1   | 1 | 33 | 11  | 4    | -9  | 4 | 33 | 21  | 11   | -1  | 8  | 33 | 48  | 19   |    |
| 0   | 3 | 32 | 54  | 58   | -2  | 6 | 32 | 51  | 19   | 2   | 1 | 33 | 52  | 18   | -8  | 4 | 33 | 1   | 14   | 0   | 8  | 33 | 7   | 0    |    |
| 1   | 3 | 32 | -27 | 1    | -1  | 6 | 32 | 20  | 11   | 3   | 1 | 33 | 62  | 25   | -7  | 4 | 33 | 69  | 15   | 1   | 8  | 33 | -5  | 2    |    |
| 2   | 3 | 32 | 56  | 53   | 0   | 6 | 32 | 7   | 5    | 5   | 1 | 33 | -36 | 9    | -5  | 4 | 33 | -10 | 25   | -16 | 0  | 34 | 271 | 22   |    |
| 3   | 3 | 32 | 11  | 0    | 1   | 6 | 32 | 33  | 17   | 6   | 1 | 33 | 8   | 25   | -3  | 4 | 33 | -44 | 1    | -12 | 0  | 34 | 64  | 17   |    |
| 4   | 3 | 32 | -36 | 45   | 2   | 6 | 32 | 23  | 0    | 7   | 1 | 33 | 97  | 12   | -2  | 4 | 33 | 8   | 2    | -10 | 0  | 34 | 52  | 1    |    |
| 5   | 3 | 32 | 143 | 46   | 3   | 6 | 32 | -43 | 9    | 8   | 1 | 33 | 34  | 12   | -2  | 4 | 33 | 8   | 1    | -8  | 0  | 34 | -1  | 64   |    |
| 6   | 3 | 32 | 42  | 6    | 4   | 6 | 32 | -56 | 2    | 9   | 1 | 33 | 16  | 0    | -1  | 4 | 33 | -36 | 44   | 0   | -4 | 0  | 34  | 6    | 27 |
| 7   | 3 | 32 | -52 | 9    | 5   | 6 | 32 | 18  | 1    | -17 | 2 | 33 | 42  | 1    | 0   | 4 | 33 | -44 | 41   | 6   | -4 | 0  | 34  | -4   | 34 |
| 8   | 3 | 32 | 9   | 58   | 6   | 6 | 32 | 9   | 1    | -16 | 2 | 33 | 9   | 0    | 1   | 4 | 33 | 44  | 2    | -2  | 0  | 34 | 2   | 1    |    |
| 9   | 3 | 32 | -2  | 1    | -8  | 7 | 32 | 35  | 10   | -14 | 2 | 33 | -33 | 0    | 3   | 4 | 33 | -71 | 3    | 0   | 0  | 34 | -3  | 5    |    |
| -15 | 4 | 32 | 214 | 2    | -7  | 7 | 32 | 61  | 1    | -13 | 2 | 33 | 39  | 0    | 4   | 4 | 33 | 2   | 6    | 2   | 0  | 34 | -3  | 5    |    |
| -14 | 4 | 32 | 64  | 0    | -6  | 7 | 32 | -19 | 12   | -12 | 2 | 33 | 147 | 10   | 5   | 4 | 33 | 5   | 67   | 2   | 0  | 34 | -69 | 27   |    |
| -13 | 4 | 32 | -13 | 0    | -5  | 7 | 32 | 7   | 0    | -11 | 2 | 33 | 37  | 0    | 6   | 4 | 33 | 47  | 1    | -16 | 1  | 34 | -32 | 17   |    |
| -12 | 4 | 32 | -47 | 0    | -4  | 7 | 32 | 52  | 32   | -10 | 2 | 33 | -10 | 0    | 7   | 4 | 33 | 148 | 1    | -15 | 1  | 34 | -20 | 1    |    |
| -11 | 4 | 32 | 46  | 5    | -4  | 7 | 32 | 52  | 15   | -6  | 2 | 33 | 61  | 57   | -12 | 5 | 33 | 292 | 2    | -14 | 1  | 34 | -67 | 1    |    |
| -10 | 4 | 32 | 42  | 0    | -3  | 7 | 32 | 69  | 0    | -7  | 2 | 33 | 33  | 72   | -11 | 5 | 33 | 2   | 24   | -14 | 1  | 34 | -49 | 5    |    |
| -9  | 4 | 32 | 11  | 33   | -2  | 7 | 32 | -5  | 7    | -6  | 2 | 33 | 71  | 27   | -10 | 5 | 33 | 16  | 0    | -13 | 1  | 34 | -67 | 1    |    |
| -8  | 4 | 32 | 58  | 148  | 0   | 7 | 32 | 19  | 0    | -5  | 2 | 33 | 13  | 9    | -9  | 5 | 33 | 10  | 1    | -11 | 1  | 34 | -18 | 26   |    |
| -7  | 4 | 32 | -33 | 2    | -1  | 7 | 32 | 55  | 21   | -4  | 2 | 33 | -7  | 5    | -8  | 5 | 33 | -65 | 2    | -1  | 1  | 36 | -47 | 2    |    |
| -6  | 4 | 32 | 14  | 19   | 1   | 7 | 32 | 97  | 0    | -1  | 0 | 35 | 52  | 31   | -12 | 4 | 35 | -22 | 0    | 0   | 1  | 36 | -28 | 18   |    |
| -5  | 4 | 32 | 38  | 2    | 2   | 7 | 32 | 24  | 10   | 5   | 0 | 35 | 45  | 27   | -10 | 4 | 35 | 35  | 7    | 2   | 1  | 36 | 100 | 1    |    |
| -4  | 4 | 32 | 43  | 16   | 3   | 7 | 32 | 25  | 30   | -15 | 1 | 35 | 128 | 14   | -9  | 4 | 35 | 116 | 2    | -14 | 2  | 36 | 62  | 9    |    |
| -3  | 4 | 32 | 107 | 15   | -13 | 4 | 34 | 53  | 0    | -1  | 0 | 35 | 96  | 22   | -13 | 4 | 35 | 0   | 2    | -1  | 1  | 36 | -19 | 16   |    |
| -2  | 4 | 32 | 119 | 17   | -12 | 4 | 34 | -31 | 0    | 1   | 0 | 35 | 52  | 31   | -12 | 4 | 35 | -22 | 0    | 0   | 1  | 36 | -47 | 2    |    |
| -1  | 4 | 32 | 107 | 78   | -11 | 4 | 34 | 57  | 3    | 3   | 0 | 35 | -36 | 20   | -11 | 4 | 35 | 65  | 7    | 1   | 1  | 36 | 28  | 18   |    |
| 0   | 4 | 32 | -40 | 1    | -10 | 4 | 34 | 170 | 10   | 5   | 0 | 35 | 45  | 27   | -10 | 4 | 35 | 35  | 2    | 2   | 1  | 36 | 100 | 1    |    |
| 1   | 4 | 32 | 12  | 0    | -9  | 4 | 34 | 125 | 30   | -15 | 1 | 35 | 135 | 14   | -8  | 4 | 35 | -14 | 24   | -14 | 2  | 36 | 62  | 9    |    |
| 2   | 4 | 32 | 8   | 9    | -8  | 4 | 34 | -12 | 6    | -14 | 1 | 35 | 128 | 14   | -8  | 4 | 35 | -14 | 24   | -14 | 2  | 36 | 62  | 9    |    |
| 3   | 4 | 32 | 50  | 0    | -7  | 4 | 34 | 8   | 22   | -13 | 1 | 35 | 30  | 4    | -12 | 1 | 35 | -11 | 23   | -13 | 2  | 36 | 22  | 6    |    |
| 4   | 4 | 32 | 47  | 1    | -6  | 4 | 34 | 30  | 4    | -12 | 1 | 35 | 28  | 23   | -6  | 4 | 35 | 25  | 31   | -12 | 2  | 36 | 35  | 2    |    |
| 5   | 4 | 32 | -12 | 1    | -4  | 4 | 34 | 85  | 7    | -11 | 1 | 35 | -4  | 0    | -5  | 4 | 35 | 142 | 1    | -11 | 2  | 36 | 11  | 1    |    |
| 6   | 4 | 32 | 94  | 20   | -3  | 4 | 34 | -14 | 31   | -10 | 1 | 35 | 23  | 32   | -4  | 4 | 35 | -37 | 19   | -10 | 2  | 36 | -30 | 7    |    |
| 7   | 4 | 32 | 5   | 5    | -2  | 4 | 34 | 47  | 6    | -9  | 1 | 35 | 9   | 0    | -3  | 4 | 35 | 0   | 0    | -9  | 2  | 36 | 89  | 1    |    |
| 8   | 4 | 32 | 98  | 3    | -1  | 4 | 34 | -4  | 0    | -8  | 1 | 35 | 84  | 19   | -2  | 4 | 35 | 42  | 3    | -8  | 2  | 36 | 79  | 3    |    |
| 9   | 4 | 32 | 115 | 23   | 0   | 4 | 34 | 38  | 0    | -7  | 1 | 35 | 47  | 36   | -1  | 4 | 35 | -31 | 9    | -7  | 2  | 36 | 92  | 9    |    |
| 10  | 4 | 32 | 137 | 2    | 1   | 4 | 34 | 62  | 4    | -6  | 1 | 35 | -34 | 5    | 0   | 4 | 35 | 90  | 2    | -6  | 2  | 36 | -11 | 18   |    |
| 11  | 4 | 32 | 20  | 37   | 2   | 4 | 34 | 9   | 4    | -5  | 1 | 35 | 38  | 10   | 1   | 4 | 35 | 37  | 13   | -5  | 2  | 36 | 95  | 8    |    |
| 12  | 4 | 32 | 56  | 0    | 3   | 4 | 34 | 160 | 0    | -4  | 1 | 35 | -24 | 5    | 2   | 4 | 35 | 21  | 10   | -4  | 2  | 36 | 49  | 4    |    |
| 13  | 4 | 32 | 61  | 24   | 4   | 4 | 34 | -38 | 0    | -3  | 1 | 35 | 91  | 11   | 3   | 4 | 35 | 20  | 10   | -4  | 2  | 36 | 169 | 1    |    |
| 14  | 4 | 32 | 118 | 8    | 5   | 4 | 34 | 59  | 3    | -2  | 1 | 35 | -1  | 11   | -11 | 5 | 35 | -14 | 0    | -2  | 2  | 36 | 53  | 3    |    |
| 15  | 4 | 32 | -3  | 0    | 6   | 4 | 34 | -12 | 9    | 0   | 1 | 35 | -4  | 19   | -10 | 5 | 35 | 77  | 0    | -1  | 2  | 36 | 29  | 0    |    |
| 16  | 4 | 32 | -20 | 0    | -12 | 5 | 34 | 53  | 22   | 1   | 1 | 35 | 104 | 1    | -8  | 5 | 35 | 62  | 2    | 1   | 2  | 36 | -33 | 16   |    |
| 17  | 4 | 32 | 6   | 1    | -11 | 5 | 34 | 35  | 3    | 2   | 1 | 35 | 84  | 12   | -7  | 5 | 35 | 9   | 7    | 2   | 2  | 36 | 214 | 0    |    |
| 18  | 4 | 32 | 40  | 2    | -10 | 5 | 34 | 66  | 75   | 3   | 1 | 35 | 88  | 0    | -6  | 5 | 35 | -19 | 4    | 3   | 2  | 36 | -56 | 0    |    |
| 19  | 4 | 32 | 20  | 7    | -9  | 5 | 34 | -28 | 7    | 4   | 1 | 35 | -54 | 7    | -5  | 5 | 35 | 7   | 1    | -13 | 3  | 36 | -18 | 3    |    |
| 20  | 4 | 32 | 93  | 3    | -8  | 5 | 34 | 81  | 7    | 5   | 1 | 35 | -17 | 2    | -4  | 5 | 35 | 166 | 20   | -12 | 3  | 36 | -49 | 0    |    |
| 21  | 4 | 32 | -56 | 1    | -7  | 5 | 34 | 135 | 2    | -15 | 2 | 35 | -12 | 3    | -3  | 5 | 35 | -30 | 2    | -11 | 3  | 36 | -11 | 0    |    |
| 22  | 4 | 32 | 65  | 0    | -6  | 5 | 34 | 92  | 27   | -14 | 2 | 35 | -35 | 0    | -2  | 5 | 35 | 43  | 8    | -10 | 3  | 36 | 144 | 51   |    |
| 23  | 4 | 32 | 70  | 15   | -5  | 5 | 34 | 55  | 1    | -13 | 2 | 35 | 75  | 4    | -1  | 5 | 35 | 32  | 7    | -9  | 3  | 36 | -68 | 22   |    |
| 24  | 4 | 32 | 15  | 24   | -4  | 5 | 34 | 20  | 24   | -12 | 2 | 35 | 113 | 26   | 0   | 5 | 35 | -29 | 17   | -8  | 3  | 36 | 657 | 0    |    |
| 25  | 4 | 32 | 12  | 5    | -3  | 5 | 34 | 0   | 0    | -11 | 2 | 35 | -15 | 2    | 1   | 5 | 35 | 37  | 6    | -7  | 3  | 36 | 146 | 8    |    |
| 26  | 4 | 32 | 63  | 14   | -2  | 5 | 34 | 142 | 29   | -10 | 2 | 35 | 101 | 45   | 2   | 5 | 35 | -31 | 50   | -6  | 3  | 36 | 14  | 0    |    |
| 27  | 4 | 32 | 70  | 0    | -1  | 5 | 34 | 28  | 3    | -9  | 2 | 35 | 123 | 10   | -8  | 6 | 35 | 54  | 9    | -5  | 3  | 36 | -40 | 17   |    |
| 28  | 4 | 32 | -24 | 20   | 0   | 5 | 34 | 63  | 40   | -8  | 2 | 35 | 82  | 11   | -7  | 6 | 35 | 32  | 4    | -4  | 3  | 36 | 30  | 10   |    |
| 29  | 4 | 32 | 36  | 1    | 1   | 5 | 34 | 57  | 0    | -7  | 2 | 35 | -33 | 7    | -6  | 6 | 35 | 20  | 10   | -3  | 3  | 36 | -12 | 20   |    |
| 30  | 4 | 32 | 0   | 9    | 2   | 5 | 34 | 80  | 39   | -6  | 2 | 35 | 102 | 7    | -5  | 6 | 35 | 26  | 6    | -2  | 3  | 36 | 49  | 4    |    |
| 31  | 4 | 32 | 23  | 3    | 3   | 5 | 34 | 62  | 4    | -5  | 2 | 35 | -22 | 1    | -4  | 6 | 35 | 196 | 3    | -1  | 3  | 36 | 49  | 1    |    |
| 32  | 4 | 32 | -65 | 22   | 4   | 5 | 34 | 22  | 0    | -4  | 2 | 35 | 0   | 6    | -3  | 6 | 35 | 597 | 21   | 0   | 3  | 36 | -53 | 2    |    |
|     |   |    |     |      |     |   |    |     |      |     |   |    |     |      |     |   |    |     |      |     |    |    |     |      |    |

Table B.3, continued

| H   | K | L  | Obs  | Calc | H  | K | L  | Obs  | Calc | H | K | L | Obs | Calc | H | K | L | Obs | Calc |
|-----|---|----|------|------|----|---|----|------|------|---|---|---|-----|------|---|---|---|-----|------|
| -4  | 6 | 36 | -61  | 1    | -5 | 1 | 30 | -13  | 3    | - | - | - | -   | -    | - | - | - | -   | -    |
| -3  | 6 | 36 | 34   | 0    | -4 | 1 | 30 | 19   | 0    | - | - | - | -   | -    | - | - | - | -   | -    |
| -2  | 6 | 36 | 32   | 0    | -3 | 1 | 30 | -103 | 1    | - | - | - | -   | -    | - | - | - | -   | -    |
| -1  | 6 | 36 | -69  | 0    | -7 | 2 | 30 | 67   | 22   | - | - | - | -   | -    | - | - | - | -   | -    |
| -9  | 0 | 37 | -11  | 11   | -6 | 2 | 30 | -43  | 8    | - | - | - | -   | -    | - | - | - | -   | -    |
| -7  | 0 | 37 | -21  | 10   | -5 | 2 | 30 | 46   | 0    | - | - | - | -   | -    | - | - | - | -   | -    |
| -5  | 0 | 37 | 360  | 7    | -4 | 2 | 30 | -30  | 1    | - | - | - | -   | -    | - | - | - | -   | -    |
| -3  | 0 | 37 | 96   | 0    | -7 | 3 | 30 | 98   | 1    | - | - | - | -   | -    | - | - | - | -   | -    |
| -1  | 0 | 37 | 29   | 0    | -6 | 3 | 30 | 283  | 1    | - | - | - | -   | -    | - | - | - | -   | -    |
| 1   | 0 | 37 | -21  | 1    | -5 | 3 | 30 | -100 | 0    | - | - | - | -   | -    | - | - | - | -   | -    |
| -11 | 1 | 37 | 36   | 14   | -6 | 4 | 30 | 0    | 0    | - | - | - | -   | -    | - | - | - | -   | -    |
| -10 | 1 | 37 | -55  | 0    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -9  | 1 | 37 | -20  | 14   | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -8  | 1 | 37 | 74   | 1    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -7  | 1 | 37 | 63   | 0    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -6  | 1 | 37 | -11  | 4    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -5  | 1 | 37 | 30   | 2    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -4  | 1 | 37 | -51  | 0    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -3  | 1 | 37 | 14   | 1    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -2  | 1 | 37 | 200  | 0    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -1  | 1 | 37 | 19   | 1    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| 0   | 1 | 37 | 21   | 0    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| 1   | 1 | 37 | 85   | 2    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -11 | 2 | 37 | 80   | 0    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -10 | 2 | 37 | 139  | 12   | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -9  | 2 | 37 | 59   | 7    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -8  | 2 | 37 | -36  | 4    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -7  | 2 | 37 | 148  | 4    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -6  | 2 | 37 | 325  | 0    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -5  | 2 | 37 | 49   | 5    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -4  | 2 | 37 | 96   | 10   | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -3  | 2 | 37 | -3   | 0    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -2  | 2 | 37 | -14  | 10   | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -1  | 2 | 37 | 30   | 0    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| 0   | 2 | 37 | 107  | 1    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -12 | 3 | 37 | -57  | 6    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -11 | 3 | 37 | 150  | 9    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -10 | 3 | 37 | -33  | 5    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -9  | 3 | 37 | 49   | 38   | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -8  | 3 | 37 | 48   | 1    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -7  | 3 | 37 | 253  | 1    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -6  | 3 | 37 | -100 | 0    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -5  | 3 | 37 | 49   | 10   | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -4  | 3 | 37 | -36  | 3    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -3  | 3 | 37 | 199  | 0    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -2  | 3 | 37 | 56   | 1    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -1  | 3 | 37 | -65  | 1    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| 0   | 3 | 37 | 10   | 1    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -10 | 4 | 37 | 118  | 2    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -9  | 4 | 37 | 48   | 0    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -8  | 4 | 37 | 67   | 0    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -7  | 4 | 37 | 21   | 0    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -6  | 4 | 37 | -27  | 34   | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -5  | 4 | 37 | -28  | 2    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -4  | 4 | 37 | 375  | 4    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -3  | 4 | 37 | 85   | 6    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -2  | 4 | 37 | 100  | 7    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -1  | 4 | 37 | -15  | 1    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -8  | 5 | 37 | 111  | 2    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -7  | 5 | 37 | -52  | 2    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -6  | 5 | 37 | 17   | 2    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -5  | 5 | 37 | -39  | 5    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -4  | 5 | 37 | -39  | 2    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -3  | 5 | 37 | 80   | 4    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |
| -4  | 6 | 37 | -57  | 0    | -  | - | -  | -    | -    | - | - | - | -   | -    | - | - | - | -   | -    |

a Reflections flagged with an asterisk were considered unobserved.

Table B.4. Atomic multiplicities for [Cu(tmp)<sub>2</sub>]BPh<sub>4</sub>.

| Name   | Multiplicity | Name   | Multiplicity | Name   | Multiplicity |
|--------|--------------|--------|--------------|--------|--------------|
| Cu     | 1.000        | N(11)  | 1.000        | N(21)  | 1.000        |
| N(112) | 1.000        | N(212) | 1.000        | C(12)  | 1.000        |
| C(13)  | 1.000        | C(14)  | 1.000        | C(15)  | 1.000        |
| C(16)  | 1.000        | C(17)  | 1.000        | C(18)  | 1.000        |
| C(19)  | 1.000        | C(22)  | 1.000        | C(23)  | 1.000        |
| C(24)  | 1.000        | C(25)  | 1.000        | C(26)  | 1.000        |
| C(27)  | 1.000        | C(28)  | 1.000        | C(29)  | 1.000        |
| C(31)  | 1.000        | C(32)  | 1.000        | C(33)  | 1.000        |
| C(34)  | 1.000        | C(35)  | 1.000        | C(36)  | 1.000        |
| C(41)  | 1.000        | C(42)  | 1.000        | C(43)  | 1.000        |
| C(44)  | 1.000        | C(45)  | 1.000        | C(46)  | 1.000        |
| C(51)  | 1.000        | C(52)  | 1.000        | C(53)  | 1.000        |
| C(54)  | 1.000        | C(55)  | 1.000        | C(56)  | 1.000        |
| C(61)  | 1.000        | C(62)  | 1.000        | C(63)  | 1.000        |
| C(64)  | 1.000        | C(65)  | 1.000        | C(66)  | 1.000        |
| C(110) | 1.000        | C(111) | 1.000        | C(113) | 1.000        |
| C(114) | 1.000        | C(115) | 1.000        | C(116) | 1.000        |
| C(117) | 1.000        | C(118) | 1.000        | C(210) | 1.000        |
| C(211) | 1.000        | C(213) | 1.000        | C(214) | 1.000        |
| C(215) | 1.000        | C(216) | 1.000        | C(217) | 1.000        |
| C(218) | 1.000        | B      | 1.000        | H(12)  | 1.000        |
| H(16)  | 1.000        | H(17)  | 1.000        | H(22)  | 1.000        |
| H(26)  | 1.000        | H(27)  | 1.000        | H(32)  | 1.000        |
| H(33)  | 1.000        | H(34)  | 1.000        | H(35)  | 1.000        |
| H(36)  | 1.000        | H(42)  | 1.000        | H(43)  | 1.000        |
| H(44)  | 1.000        | H(45)  | 1.000        | H(46)  | 1.000        |
| H(52)  | 1.000        | H(53)  | 1.000        | H(54)  | 1.000        |
| H(55)  | 1.000        | H(56)  | 1.000        | H(62)  | 1.000        |
| H(63)  | 1.000        | H(64)  | 1.000        | H(65)  | 1.000        |
| H(66)  | 1.000        | H(111) | 1.000        | H(11A) | 1.000        |
| H(11B) | 1.000        | H(11C) | 1.000        | H(11D) | 1.000        |
| H(11E) | 1.000        | H(11F) | 1.000        | H(11G) | 1.000        |
| H(11H) | 1.000        | H(11I) | 1.000        | H(11J) | 1.000        |
| H(11K) | 1.000        | H(11L) | 1.000        | H(211) | 1.000        |
| H(21A) | 1.000        | H(21B) | 1.000        | H(21C) | 1.000        |
| H(21D) | 1.000        | H(21E) | 1.000        | H(21F) | 1.000        |
| H(21G) | 1.000        | H(21H) | 1.000        | H(21I) | 1.000        |
| H(21J) | 1.000        | H(21K) | 1.000        | H(21L) | 1.000        |



### Appendix C: Crystal Data for [Cu(dipp)<sub>2</sub>]TFPB

**Table C.1. Anisotropic temperature factor coefficients - U's<sup>a</sup> for [Cu(dipp)<sub>2</sub>]TFPB.**

| Name   | U(1,1)    | U(2,2)    | U(3,3)    | U(1,2)     | U(1,3)     | U(2,3)     |
|--------|-----------|-----------|-----------|------------|------------|------------|
| Cu     | 0.0759(5) | 0.0646(5) | 0.0557(5) | 0.0267(4)  | 0.0361(4)  | 0.0232(4)  |
| N(11)  | 0.063(3)  | 0.069(3)  | 0.059(3)  | 0.029(2)   | 0.028(2)   | 0.023(2)   |
| N(21)  | 0.073(3)  | 0.060(3)  | 0.065(3)  | 0.022(2)   | 0.034(3)   | 0.029(2)   |
| N(112) | 0.107(4)  | 0.070(3)  | 0.069(3)  | 0.041(3)   | 0.053(3)   | 0.037(3)   |
| N(212) | 0.072(3)  | 0.053(3)  | 0.061(3)  | 0.022(2)   | 0.032(2)   | 0.022(2)   |
| C(12)  | 0.081(4)  | 0.059(4)  | 0.084(5)  | 0.017(3)   | 0.033(4)   | 0.018(3)   |
| C(13)  | 0.123(7)  | 0.064(5)  | 0.104(6)  | 0.020(4)   | 0.044(5)   | 0.010(4)   |
| C(14)  | 0.127(7)  | 0.073(5)  | 0.079(5)  | 0.031(5)   | 0.029(5)   | 0.006(4)   |
| C(15)  | 0.106(5)  | 0.101(6)  | 0.051(4)  | 0.054(5)   | 0.024(4)   | 0.014(4)   |
| C(16)  | 0.196(11) | 0.127(8)  | 0.070(5)  | 0.080(8)   | 0.068(6)   | 0.028(5)   |
| C(17)  | 0.261(15) | 0.159(10) | 0.080(6)  | 0.103(11)  | 0.110(8)   | 0.052(7)   |
| C(18)  | 0.223(11) | 0.134(8)  | 0.103(6)  | 0.093(8)   | 0.115(8)   | 0.076(6)   |
| C(19)  | 0.38(2)   | 0.166(12) | 0.165(12) | 0.113(14)  | 0.209(15)  | 0.098(10)  |
| C(22)  | 0.075(4)  | 0.092(5)  | 0.073(4)  | 0.033(4)   | 0.028(3)   | 0.040(4)   |
| C(23)  | 0.099(6)  | 0.138(7)  | 0.087(5)  | 0.052(5)   | 0.027(5)   | 0.057(5)   |
| C(24)  | 0.115(7)  | 0.114(7)  | 0.072(5)  | 0.037(5)   | 0.017(5)   | 0.043(5)   |
| C(25)  | 0.124(6)  | 0.067(4)  | 0.056(4)  | 0.027(4)   | 0.038(4)   | 0.028(3)   |
| C(26)  | 0.156(8)  | 0.074(5)  | 0.059(4)  | 0.026(5)   | 0.049(5)   | 0.026(4)   |
| C(27)  | 0.148(8)  | 0.070(5)  | 0.070(5)  | 0.027(5)   | 0.067(5)   | 0.023(4)   |
| C(28)  | 0.104(5)  | 0.053(4)  | 0.076(4)  | 0.021(3)   | 0.055(4)   | 0.023(3)   |
| C(29)  | 0.112(6)  | 0.084(5)  | 0.111(7)  | 0.038(4)   | 0.077(5)   | 0.031(5)   |
| C(110) | 0.38(2)   | 0.139(10) | 0.204(14) | 0.101(13)  | 0.216(16)  | 0.119(10)  |
| C(111) | 0.183(9)  | 0.097(6)  | 0.119(7)  | 0.056(6)   | 0.105(7)   | 0.068(5)   |
| C(113) | 0.106(5)  | 0.101(5)  | 0.065(4)  | 0.055(4)   | 0.049(4)   | 0.046(4)   |
| C(114) | 0.073(4)  | 0.078(4)  | 0.053(3)  | 0.039(3)   | 0.018(3)   | 0.023(3)   |
| C(115) | 0.125(6)  | 0.065(4)  | 0.108(6)  | 0.019(4)   | 0.075(5)   | 0.033(4)   |
| C(116) | 0.149(11) | 0.257(18) | 0.183(13) | -0.014(11) | 0.106(11)  | 0.027(12)  |
| C(117) | 0.269(19) | 0.39(3)   | 0.189(14) | 0.19(2)    | 0.154(14)  | 0.211(18)  |
| C(118) | 0.256(14) | 0.079(6)  | 0.163(10) | 0.063(8)   | 0.149(11)  | 0.070(6)   |
| C(119) | 0.34(2)   | 0.162(12) | 0.255(18) | 0.169(15)  | 0.201(18)  | 0.120(13)  |
| C(120) | 0.24(2)   | 0.147(13) | 0.222(18) | 0.004(13)  | 0.089(15)  | 0.022(12)  |
| C(210) | 0.089(5)  | 0.091(5)  | 0.109(6)  | 0.040(4)   | 0.055(5)   | 0.029(5)   |
| C(211) | 0.076(4)  | 0.068(4)  | 0.084(4)  | 0.032(3)   | 0.044(4)   | 0.029(3)   |
| C(213) | 0.083(4)  | 0.043(3)  | 0.066(4)  | 0.019(3)   | 0.044(3)   | 0.022(3)   |
| C(214) | 0.084(4)  | 0.048(3)  | 0.055(3)  | 0.017(3)   | 0.033(3)   | 0.020(3)   |
| C(215) | 0.079(5)  | 0.148(8)  | 0.085(5)  | 0.052(5)   | 0.036(4)   | 0.054(5)   |
| C(216) | 0.148(10) | 0.133(10) | 0.183(12) | 0.043(8)   | 0.092(9)   | 0.003(8)   |
| C(217) | 0.106(7)  | 0.194(12) | 0.185(12) | 0.022(8)   | 0.083(8)   | 0.077(10)  |
| C(218) | 0.085(5)  | 0.117(6)  | 0.098(6)  | 0.055(5)   | 0.037(4)   | 0.048(5)   |
| C(219) | 0.146(10) | 0.198(13) | 0.107(8)  | -0.024(9)  | 0.019(7)   | 0.045(8)   |
| C(220) | 0.232(15) | 0.207(13) | 0.143(10) | 0.150(12)  | 0.078(10)  | 0.098(10)  |
| F(331) | 0.310(11) | 0.128(5)  | 0.125(5)  | 0.090(6)   | 0.010(6)   | 0.072(4)   |
| F(332) | 0.145(5)  | 0.223(8)  | 0.388(14) | 0.122(6)   | 0.128(7)   | 0.229(9)   |
| F(333) | 0.166(5)  | 0.080(3)  | 0.224(7)  | 0.006(3)   | -0.004(5)  | 0.090(4)   |
| F(351) | 0.193(8)  | 0.156(7)  | 0.357(15) | -0.101(7)  | -0.162(10) | 0.138(9)   |
| F(352) | 0.051(3)  | 0.59(3)   | 0.140(6)  | 0.015(7)   | 0.003(4)   | -0.068(10) |
| F(353) | 0.105(4)  | 0.281(10) | 0.167(6)  | -0.056(5)  | -0.045(4)  | 0.134(7)   |
| F(431) | 0.107(4)  | 0.205(6)  | 0.157(5)  | 0.092(4)   | 0.048(3)   | 0.119(5)   |
| F(432) | 0.122(5)  | 0.514(18) | 0.199(7)  | 0.185(8)   | 0.111(5)   | 0.219(10)  |
| F(433) | 0.091(4)  | 0.138(6)  | 0.382(15) | 0.002(4)   | -0.102(7)  | 0.068(7)   |
| F(451) | 0.279(10) | 0.344(13) | 0.107(4)  | 0.180(10)  | 0.119(6)   | 0.121(6)   |
| F(452) | 0.415(14) | 0.164(6)  | 0.097(4)  | -0.064(8)  | -0.006(6)  | 0.100(5)   |
| F(453) | 0.129(5)  | 0.342(11) | 0.101(4)  | 0.011(6)   | 0.008(4)   | 0.144(6)   |
| F(531) | 0.124(4)  | 0.199(6)  | 0.080(3)  | 0.010(4)   | 0.055(3)   | 0.051(4)   |
| F(532) | 0.076(3)  | 0.227(6)  | 0.111(4)  | 0.011(3)   | 0.044(3)   | 0.081(4)   |
| F(533) | 0.286(9)  | 0.243(8)  | 0.354(12) | 0.155(8)   | 0.247(10)  | 0.258(10)  |
| F(551) | 0.086(3)  | 0.147(5)  | 0.114(4)  | -0.029(3)  | 0.028(3)   | 0.017(3)   |
| F(552) | 0.137(5)  | 0.219(7)  | 0.093(4)  | -0.089(5)  | -0.040(3)  | 0.080(4)   |
| F(553) | 0.144(5)  | 0.073(3)  | 0.192(6)  | -0.015(3)  | 0.051(4)   | 0.024(3)   |
| F(631) | 0.486(16) | 0.342(12) | 0.537(18) | 0.343(13)  | 0.454(16)  | 0.402(14)  |

Table C.1, continued

| Name   | U(1,1)    | U(2,2)    | U(3,3)    | U(1,2)    | U(1,3)    | U(2,3)    |
|--------|-----------|-----------|-----------|-----------|-----------|-----------|
| ----   | -----     | -----     | -----     | -----     | -----     | -----     |
| F(632) | 0.306(11) | 0.109(5)  | 0.168(6)  | 0.013(5)  | 0.086(7)  | 0.084(5)  |
| F(633) | 0.176(6)  | 0.269(10) | 0.265(9)  | 0.045(6)  | 0.050(6)  | 0.235(9)  |
| F(651) | 0.175(6)  | 0.303(9)  | 0.269(8)  | 0.188(7)  | 0.172(6)  | 0.217(8)  |
| F(652) | 0.177(7)  | 0.64(3)   | 0.262(10) | 0.205(13) | 0.179(8)  | 0.321(16) |
| F(653) | 0.187(8)  | 0.170(7)  | 0.62(3)   | 0.047(6)  | 0.298(14) | 0.102(11) |
| C(31)  | 0.050(3)  | 0.047(3)  | 0.044(3)  | 0.012(2)  | 0.022(2)  | 0.016(2)  |
| C(32)  | 0.055(3)  | 0.056(3)  | 0.060(3)  | 0.018(3)  | 0.025(3)  | 0.024(3)  |
| C(33)  | 0.065(4)  | 0.048(3)  | 0.071(4)  | 0.013(3)  | 0.027(3)  | 0.021(3)  |
| C(34)  | 0.077(4)  | 0.052(3)  | 0.087(4)  | 0.008(3)  | 0.035(4)  | 0.027(3)  |
| C(35)  | 0.058(3)  | 0.066(4)  | 0.060(3)  | 0.002(3)  | 0.019(3)  | 0.014(3)  |
| C(36)  | 0.055(3)  | 0.061(3)  | 0.046(3)  | 0.013(3)  | 0.020(2)  | 0.018(3)  |
| C(41)  | 0.048(3)  | 0.051(3)  | 0.045(3)  | 0.010(2)  | 0.014(2)  | 0.023(2)  |
| C(42)  | 0.049(3)  | 0.073(4)  | 0.046(3)  | 0.014(3)  | 0.016(2)  | 0.029(3)  |
| C(43)  | 0.048(3)  | 0.089(4)  | 0.070(4)  | 0.018(3)  | 0.022(3)  | 0.041(3)  |
| C(44)  | 0.066(4)  | 0.093(5)  | 0.078(4)  | 0.025(3)  | 0.043(3)  | 0.044(4)  |
| C(45)  | 0.064(4)  | 0.074(4)  | 0.058(3)  | 0.022(3)  | 0.031(3)  | 0.034(3)  |
| C(46)  | 0.054(3)  | 0.064(3)  | 0.050(3)  | 0.018(3)  | 0.019(2)  | 0.027(3)  |
| C(51)  | 0.054(3)  | 0.043(3)  | 0.048(3)  | 0.014(2)  | 0.019(2)  | 0.020(2)  |
| C(52)  | 0.054(3)  | 0.062(3)  | 0.050(3)  | 0.010(3)  | 0.018(2)  | 0.028(3)  |
| C(53)  | 0.067(4)  | 0.080(4)  | 0.047(3)  | 0.012(3)  | 0.024(3)  | 0.029(3)  |
| C(54)  | 0.078(4)  | 0.078(4)  | 0.042(3)  | 0.007(3)  | 0.016(3)  | 0.021(3)  |
| C(55)  | 0.064(3)  | 0.060(3)  | 0.051(3)  | 0.001(3)  | 0.014(3)  | 0.019(3)  |
| C(56)  | 0.063(3)  | 0.052(3)  | 0.054(3)  | 0.007(3)  | 0.021(3)  | 0.025(3)  |
| C(61)  | 0.053(3)  | 0.052(3)  | 0.041(3)  | 0.012(2)  | 0.015(2)  | 0.019(2)  |
| C(62)  | 0.061(3)  | 0.055(3)  | 0.058(3)  | 0.019(3)  | 0.026(3)  | 0.026(3)  |
| C(63)  | 0.078(4)  | 0.064(4)  | 0.068(4)  | 0.028(3)  | 0.034(3)  | 0.034(3)  |
| C(64)  | 0.083(4)  | 0.089(5)  | 0.087(4)  | 0.050(4)  | 0.043(4)  | 0.052(4)  |
| C(65)  | 0.065(4)  | 0.091(5)  | 0.086(4)  | 0.039(3)  | 0.043(3)  | 0.053(4)  |
| C(66)  | 0.059(3)  | 0.073(4)  | 0.071(4)  | 0.024(3)  | 0.032(3)  | 0.045(3)  |
| C(331) | 0.090(5)  | 0.063(5)  | 0.119(7)  | 0.022(4)  | 0.022(5)  | 0.042(4)  |
| C(351) | 0.062(5)  | 0.107(6)  | 0.087(5)  | -0.021(4) | 0.018(4)  | 0.030(5)  |
| C(431) | 0.053(4)  | 0.177(9)  | 0.114(7)  | 0.032(5)  | 0.037(5)  | 0.079(7)  |
| C(451) | 0.093(5)  | 0.133(7)  | 0.074(5)  | 0.040(5)  | 0.048(4)  | 0.065(5)  |
| C(531) | 0.083(5)  | 0.143(8)  | 0.053(4)  | 0.003(5)  | 0.018(3)  | 0.045(5)  |
| C(551) | 0.091(5)  | 0.079(5)  | 0.059(4)  | -0.012(4) | 0.018(4)  | 0.018(4)  |
| C(631) | 0.126(6)  | 0.088(6)  | 0.121(6)  | 0.070(5)  | 0.076(6)  | 0.072(5)  |
| C(651) | 0.106(7)  | 0.175(10) | 0.165(9)  | 0.076(7)  | 0.094(7)  | 0.130(8)  |
| B      | 0.047(3)  | 0.054(3)  | 0.047(3)  | 0.014(3)  | 0.018(3)  | 0.025(3)  |

a The form of the anisotropic temperature factor is:  
 $\exp[-2\pi \{h^2a'^2U(1,1) + k^2b'^2U(2,2) + l^2c'^2U(3,3) + 2hka'b'U(1,2) + 2hla'c'U(1,3) + 2klb'c'U(2,3)\}]$  where  $a'$ ,  $b'$ , and  $c'$  are reciprocal lattice constants.

Table C.2. Torsion angles in degrees for [Cu(dipp)<sub>2</sub>]TFPB.

| Atom 1 | Atom 2 | Atom 3 | Atom 4 | Angle           |
|--------|--------|--------|--------|-----------------|
| N(21)  | Cu     | N(11)  | C(12)  | 57.04 ( 0.70)   |
| N(21)  | Cu     | N(11)  | C(114) | -120.21 ( 0.47) |
| N(112) | Cu     | N(11)  | C(12)  | -179.95 ( 0.82) |
| N(112) | Cu     | N(11)  | C(114) | 2.81 ( 0.48)    |
| N(212) | Cu     | N(11)  | C(12)  | -42.79 ( 0.72)  |
| N(212) | Cu     | N(11)  | C(114) | 139.97 ( 0.45)  |
| N(11)  | Cu     | N(21)  | C(22)  | 59.68 ( 0.71)   |
| N(11)  | Cu     | N(21)  | C(214) | -116.65 ( 0.45) |
| N(112) | Cu     | N(21)  | C(22)  | -39.61 ( 0.73)  |
| N(112) | Cu     | N(21)  | C(214) | 144.06 ( 0.44)  |
| N(212) | Cu     | N(21)  | C(22)  | -176.64 ( 0.68) |
| N(212) | Cu     | N(21)  | C(214) | 7.03 ( 0.44)    |
| N(11)  | Cu     | N(112) | C(111) | -179.40 ( 0.84) |
| N(11)  | Cu     | N(112) | C(113) | -2.80 ( 0.51)   |
| N(21)  | Cu     | N(112) | C(111) | -61.28 ( 0.89)  |
| N(21)  | Cu     | N(112) | C(113) | 115.32 ( 0.50)  |
| N(212) | Cu     | N(112) | C(111) | 51.55 ( 0.90)   |
| N(212) | Cu     | N(112) | C(113) | -131.85 ( 0.51) |
| N(11)  | Cu     | N(212) | C(211) | -63.57 ( 0.71)  |
| N(11)  | Cu     | N(212) | C(213) | 110.93 ( 0.46)  |
| N(21)  | Cu     | N(212) | C(211) | 178.11 ( 0.68)  |
| N(21)  | Cu     | N(212) | C(213) | -7.39 ( 0.45)   |
| N(112) | Cu     | N(212) | C(211) | 49.63 ( 0.75)   |
| N(112) | Cu     | N(212) | C(213) | -135.87 ( 0.44) |
| Cu     | N(11)  | C(12)  | C(13)  | -179.32 ( 0.63) |
| Cu     | N(11)  | C(12)  | C(115) | -0.77 ( 1.06)   |
| C(114) | N(11)  | C(12)  | C(13)  | -2.28 ( 1.11)   |
| C(114) | N(11)  | C(12)  | C(115) | 176.27 ( 0.71)  |
| Cu     | N(11)  | C(114) | C(15)  | 178.09 ( 0.61)  |
| Cu     | N(11)  | C(114) | C(113) | -2.33 ( 0.82)   |
| C(12)  | N(11)  | C(114) | C(15)  | 0.49 ( 1.07)    |
| C(12)  | N(11)  | C(114) | C(113) | -179.93 ( 0.74) |
| Cu     | N(21)  | C(22)  | C(23)  | -175.67 ( 0.70) |
| Cu     | N(21)  | C(22)  | C(215) | 4.10 ( 1.11)    |
| C(214) | N(21)  | C(22)  | C(23)  | 0.41 ( 1.17)    |
| C(214) | N(21)  | C(22)  | C(215) | -179.83 ( 0.73) |
| Cu     | N(21)  | C(214) | C(25)  | 175.99 ( 0.59)  |
| Cu     | N(21)  | C(214) | C(213) | -5.63 ( 0.74)   |
| C(22)  | N(21)  | C(214) | C(25)  | -0.87 ( 1.03)   |
| C(22)  | N(21)  | C(214) | C(213) | 177.51 ( 0.66)  |
| Cu     | N(112) | C(111) | C(110) | 173.02 ( 1.10)  |
| Cu     | N(112) | C(111) | C(118) | -3.38 ( 1.52)   |
| C(113) | N(112) | C(111) | C(110) | -3.32 ( 1.68)   |
| C(113) | N(112) | C(111) | C(118) | -179.72 ( 0.99) |
| Cu     | N(112) | C(113) | C(18)  | -176.15 ( 0.81) |
| Cu     | N(112) | C(113) | C(114) | 2.43 ( 0.89)    |
| C(111) | N(112) | C(113) | C(18)  | 0.79 ( 1.33)    |
| C(111) | N(112) | C(113) | C(114) | 179.37 ( 0.84)  |
| Cu     | N(212) | C(211) | C(210) | 173.81 ( 0.64)  |
| Cu     | N(212) | C(211) | C(218) | -7.24 ( 1.11)   |
| C(213) | N(212) | C(211) | C(210) | -0.37 ( 1.15)   |
| C(213) | N(212) | C(211) | C(218) | 178.58 ( 0.71)  |
| Cu     | N(212) | C(213) | C(28)  | -174.92 ( 0.55) |
| Cu     | N(212) | C(213) | C(214) | 6.58 ( 0.77)    |
| C(211) | N(212) | C(213) | C(28)  | 0.32 ( 1.03)    |
| C(211) | N(212) | C(213) | C(214) | -178.19 ( 0.67) |
| N(11)  | C(12)  | C(13)  | C(14)  | 2.57 ( 1.36)    |
| C(115) | C(12)  | C(13)  | C(14)  | -175.94 ( 0.90) |
| C(12)  | C(13)  | C(14)  | C(15)  | -0.98 ( 1.51)   |
| C(13)  | C(14)  | C(15)  | C(16)  | 179.56 ( 1.05)  |
| C(13)  | C(14)  | C(15)  | C(114) | -0.72 ( 1.38)   |
| C(14)  | C(15)  | C(16)  | C(17)  | 179.93 ( 1.09)  |
| C(114) | C(15)  | C(16)  | C(17)  | 0.22 ( 1.77)    |
| C(14)  | C(15)  | C(114) | N(11)  | 1.02 ( 1.20)    |

Table C.2, continued

| Atom 1 | Atom 2 | Atom 3 | Atom 4 | Angle           |
|--------|--------|--------|--------|-----------------|
| C(14)  | C(15)  | C(114) | C(113) | -178.55 ( 0.81) |
| C(16)  | C(15)  | C(114) | N(11)  | -179.25 ( 0.89) |
| C(16)  | C(15)  | C(114) | C(113) | 1.19 ( 1.29)    |
| C(15)  | C(16)  | C(17)  | C(18)  | -0.99 ( 2.21)   |
| C(16)  | C(17)  | C(18)  | C(19)  | 177.34 ( 1.63)  |
| C(16)  | C(17)  | C(18)  | C(113) | 0.35 ( 2.10)    |
| C(17)  | C(18)  | C(19)  | C(110) | 179.90 ( 1.64)  |
| C(113) | C(18)  | C(19)  | C(110) | -3.11 ( 2.57)   |
| C(17)  | C(18)  | C(113) | N(112) | 179.63 ( 1.04)  |
| C(17)  | C(18)  | C(113) | C(114) | 1.08 ( 1.63)    |
| C(19)  | C(18)  | C(113) | N(112) | 2.37 ( 1.78)    |
| C(19)  | C(18)  | C(113) | C(114) | -176.18 ( 1.25) |
| C(18)  | C(19)  | C(110) | C(111) | 0.77 ( 2.88)    |
| N(21)  | C(22)  | C(23)  | C(24)  | 0.75 ( 1.53)    |
| C(215) | C(22)  | C(23)  | C(24)  | -179.00 ( 0.98) |
| N(21)  | C(22)  | C(215) | C(216) | -97.82 ( 0.97)  |
| C(23)  | C(22)  | C(215) | C(216) | 81.95 ( 1.14)   |
| C(22)  | C(23)  | C(24)  | C(25)  | -1.46 ( 1.61)   |
| C(23)  | C(24)  | C(25)  | C(26)  | -178.46 ( 0.97) |
| C(23)  | C(24)  | C(25)  | C(214) | 0.99 ( 1.39)    |
| C(24)  | C(25)  | C(26)  | C(27)  | 179.14 ( 0.92)  |
| C(214) | C(25)  | C(26)  | C(27)  | -0.30 ( 1.29)   |
| C(24)  | C(25)  | C(214) | N(21)  | 0.18 ( 1.17)    |
| C(24)  | C(25)  | C(214) | C(213) | -178.14 ( 0.76) |
| C(26)  | C(25)  | C(214) | N(21)  | 179.67 ( 0.70)  |
| C(26)  | C(25)  | C(214) | C(213) | 1.35 ( 1.13)    |
| C(25)  | C(26)  | C(27)  | C(28)  | -1.39 ( 1.35)   |
| C(26)  | C(27)  | C(28)  | C(29)  | -176.96 ( 0.85) |
| C(26)  | C(27)  | C(28)  | C(213) | 2.02 ( 1.22)    |
| C(27)  | C(28)  | C(29)  | C(210) | 179.51 ( 0.88)  |
| C(213) | C(28)  | C(29)  | C(210) | 0.50 ( 1.23)    |
| C(27)  | C(28)  | C(213) | N(212) | -179.43 ( 0.69) |
| C(27)  | C(28)  | C(213) | C(214) | -0.93 ( 1.05)   |
| C(29)  | C(28)  | C(213) | N(212) | -0.38 ( 1.07)   |
| C(29)  | C(28)  | C(213) | C(214) | 178.12 ( 0.70)  |
| C(28)  | C(29)  | C(210) | C(211) | -0.58 ( 1.45)   |
| C(36)  | C(31)  | C(32)  | C(33)  | 0.19 ( 0.87)    |
| B      | C(31)  | C(32)  | C(33)  | 179.91 ( 0.55)  |
| C(32)  | C(31)  | C(36)  | C(35)  | -0.79 ( 0.81)   |
| B      | C(31)  | C(36)  | C(35)  | 179.52 ( 0.54)  |
| C(32)  | C(31)  | B      | C(41)  | -77.03 ( 0.59)  |
| C(32)  | C(31)  | B      | C(51)  | 45.16 ( 0.67)   |
| C(32)  | C(31)  | B      | C(61)  | 159.99 ( 0.49)  |
| C(36)  | C(31)  | B      | C(41)  | 102.65 ( 0.60)  |
| C(36)  | C(31)  | B      | C(51)  | -135.15 ( 0.54) |
| C(36)  | C(31)  | B      | C(61)  | -20.32 ( 0.73)  |
| C(31)  | C(32)  | C(33)  | C(34)  | 0.79 ( 1.01)    |
| C(32)  | C(33)  | C(34)  | C(35)  | -1.17 ( 1.04)   |
| C(33)  | C(34)  | C(35)  | C(36)  | 0.60 ( 1.04)    |
| C(33)  | C(34)  | C(35)  | C(351) | 179.81 ( 0.70)  |
| C(34)  | C(35)  | C(36)  | C(31)  | 0.41 ( 0.96)    |
| C(351) | C(35)  | C(36)  | C(31)  | -178.80 ( 0.62) |
| C(34)  | C(35)  | C(351) | F(351) | 11.52 ( 1.34)   |
| C(34)  | C(35)  | C(351) | F(353) | 134.69 ( 0.98)  |
| C(36)  | C(35)  | C(351) | F(351) | -169.26 ( 0.96) |
| C(36)  | C(35)  | C(351) | F(353) | -46.09 ( 1.19)  |
| C(46)  | C(41)  | C(42)  | C(43)  | -1.35 ( 0.98)   |
| B      | C(41)  | C(42)  | C(43)  | -175.93 ( 0.65) |
| C(42)  | C(41)  | C(46)  | C(45)  | 3.28 ( 0.96)    |
| B      | C(41)  | C(46)  | C(45)  | 177.92 ( 0.61)  |
| C(42)  | C(41)  | B      | C(31)  | 91.01 ( 0.65)   |
| C(42)  | C(41)  | B      | C(51)  | -27.41 ( 0.85)  |
| C(42)  | C(41)  | B      | C(61)  | -147.21 ( 0.58) |
| C(46)  | C(41)  | B      | C(31)  | -83.17 ( 0.70)  |

Table C.2, continued

| Atom 1 | Atom 2 | Atom 3 | Atom 4 | Angle           |
|--------|--------|--------|--------|-----------------|
| -----  | -----  | -----  | -----  | -----           |
| C(46)  | C(41)  | B      | C(51)  | 158.41 ( 0.57)  |
| C(46)  | C(41)  | B      | C(61)  | 38.61 ( 0.80)   |
| C(41)  | C(42)  | C(43)  | C(44)  | -1.52 ( 1.14)   |
| C(42)  | C(43)  | C(44)  | C(45)  | 2.56 ( 1.17)    |
| C(43)  | C(44)  | C(45)  | C(46)  | -0.70 ( 1.13)   |
| C(43)  | C(44)  | C(45)  | C(451) | -179.75 ( 0.80) |
| C(44)  | C(45)  | C(46)  | C(41)  | -2.37 ( 1.07)   |
| C(451) | C(45)  | C(46)  | C(41)  | 176.66 ( 0.75)  |
| C(44)  | C(45)  | C(451) | F(451) | -39.29 ( 1.22)  |
| C(44)  | C(45)  | C(451) | F(452) | 78.05 ( 1.23)   |
| C(44)  | C(45)  | C(451) | F(453) | -147.56 ( 0.93) |
| C(46)  | C(45)  | C(451) | F(451) | 141.65 ( 0.87)  |
| C(46)  | C(45)  | C(451) | F(452) | -101.00 ( 1.12) |
| C(46)  | C(45)  | C(451) | F(453) | 33.38 ( 1.31)   |
| C(56)  | C(51)  | C(52)  | C(53)  | -0.19 ( 0.93)   |
| B      | C(51)  | C(52)  | C(53)  | 174.09 ( 0.62)  |
| C(52)  | C(51)  | C(56)  | C(55)  | -3.15 ( 0.90)   |
| B      | C(51)  | C(56)  | C(55)  | -177.13 ( 0.58) |
| C(52)  | C(51)  | B      | C(31)  | 35.36 ( 0.71)   |
| C(52)  | C(51)  | B      | C(41)  | 151.65 ( 0.57)  |
| C(52)  | C(51)  | B      | C(61)  | -83.82 ( 0.64)  |
| C(56)  | C(51)  | B      | C(31)  | -150.93 ( 0.56) |
| C(56)  | C(51)  | B      | C(41)  | -34.64 ( 0.82)  |
| C(56)  | C(51)  | B      | C(61)  | 89.89 ( 0.66)   |
| C(51)  | C(52)  | C(53)  | C(54)  | 2.29 ( 1.13)    |
| C(51)  | C(52)  | C(53)  | C(531) | -177.98 ( 0.71) |
| C(52)  | C(53)  | C(54)  | C(55)  | -1.00 ( 1.17)   |
| C(531) | C(53)  | C(54)  | C(55)  | 179.28 ( 0.77)  |
| C(52)  | C(53)  | C(531) | F(531) | 157.42 ( 0.73)  |
| C(52)  | C(53)  | C(531) | F(532) | 46.04 ( 1.13)   |
| C(52)  | C(53)  | C(531) | F(533) | -79.90 ( 1.03)  |
| C(54)  | C(53)  | C(531) | F(531) | -22.85 ( 1.18)  |
| C(54)  | C(53)  | C(531) | F(532) | -134.23 ( 0.84) |
| C(54)  | C(53)  | C(531) | F(533) | 99.83 ( 1.04)   |
| C(53)  | C(54)  | C(55)  | C(56)  | -2.33 ( 1.12)   |
| C(53)  | C(54)  | C(55)  | C(551) | 179.67 ( 0.74)  |
| C(54)  | C(55)  | C(56)  | C(51)  | 4.56 ( 1.05)    |
| C(551) | C(55)  | C(56)  | C(51)  | -177.46 ( 0.67) |
| C(54)  | C(55)  | C(551) | F(551) | -151.46 ( 0.77) |
| C(54)  | C(55)  | C(551) | F(552) | -28.07 ( 1.10)  |
| C(54)  | C(55)  | C(551) | F(553) | 92.36 ( 0.90)   |
| C(56)  | C(55)  | C(551) | F(551) | 30.51 ( 1.11)   |
| C(56)  | C(55)  | C(551) | F(552) | 153.90 ( 0.73)  |
| C(56)  | C(55)  | C(551) | F(553) | -85.66 ( 0.87)  |
| C(66)  | C(61)  | C(62)  | C(63)  | 3.22 ( 0.84)    |
| B      | C(61)  | C(62)  | C(63)  | 178.50 ( 0.54)  |
| C(62)  | C(61)  | C(66)  | C(65)  | -0.40 ( 0.85)   |
| B      | C(61)  | C(66)  | C(65)  | -175.98 ( 0.56) |
| C(62)  | C(61)  | B      | C(31)  | 135.86 ( 0.55)  |
| C(62)  | C(61)  | B      | C(41)  | 17.95 ( 0.76)   |
| C(62)  | C(61)  | B      | C(51)  | -107.05 ( 0.58) |
| C(66)  | C(61)  | B      | C(31)  | -49.06 ( 0.64)  |
| C(66)  | C(61)  | B      | C(41)  | -166.97 ( 0.49) |
| C(66)  | C(61)  | B      | C(51)  | 68.03 ( 0.63)   |
| C(61)  | C(62)  | C(63)  | C(64)  | -3.66 ( 0.97)   |
| C(61)  | C(62)  | C(63)  | C(631) | 176.88 ( 0.64)  |
| C(62)  | C(63)  | C(64)  | C(65)  | 1.05 ( 1.02)    |
| C(631) | C(63)  | C(64)  | C(65)  | -179.50 ( 0.70) |
| C(62)  | C(63)  | C(631) | F(631) | -18.83 ( 1.34)  |
| C(62)  | C(63)  | C(631) | F(632) | 109.39 ( 1.01)  |
| C(62)  | C(63)  | C(631) | F(633) | -141.63 ( 0.86) |
| C(64)  | C(63)  | C(631) | F(631) | 161.72 ( 1.03)  |
| C(64)  | C(63)  | C(631) | F(632) | -70.06 ( 1.16)  |
| C(64)  | C(63)  | C(631) | F(633) | 38.92 ( 1.16)   |

Table C.2, continued

| Atom 1 | Atom 2 | Atom 3 | Atom 4 | Angle           |
|--------|--------|--------|--------|-----------------|
| =====  | =====  | =====  | =====  | =====           |
| C(63)  | C(64)  | C(65)  | C(66)  | 1.69 ( 1.05)    |
| C(64)  | C(65)  | C(66)  | C(61)  | -2.07 ( 1.00)   |
| C(19)  | C(110) | C(111) | N(112) | 2.57 ( 2.44)    |
| C(19)  | C(110) | C(111) | C(118) | 178.92 ( 1.60)  |
| N(112) | C(113) | C(114) | N(11)  | -0.02 ( 1.20)   |
| N(112) | C(113) | C(114) | C(15)  | 179.58 ( 0.71)  |
| C(18)  | C(113) | C(114) | N(11)  | 178.58 ( 0.87)  |
| C(18)  | C(113) | C(114) | C(15)  | -1.83 ( 1.29)   |
| C(29)  | C(210) | C(211) | N(212) | 0.52 ( 1.43)    |
| C(29)  | C(210) | C(211) | C(218) | -178.41 ( 0.90) |
| N(212) | C(213) | C(214) | N(21)  | -0.55 ( 0.95)   |
| N(212) | C(213) | C(214) | C(25)  | 177.86 ( 0.67)  |
| C(28)  | C(213) | C(214) | N(21)  | -179.13 ( 0.61) |
| C(28)  | C(213) | C(214) | C(25)  | -0.72 ( 1.05)   |

Table C.3. Structure factors ( $F^2_{\text{obs}}$  &  $F^2_{\text{calc}}$ )<sup>a</sup> for  $[\text{Cu}(\text{dipp})_2]\text{TFPB}$ .

| H   | K | L | Obs   | Calc  | H   | K  | L | Obs  | Calc | H   | K | L | Obs  | Calc | H   | K  | L    | Obs  | Calc | H   | K   | L  | Obs | Calc |
|-----|---|---|-------|-------|-----|----|---|------|------|-----|---|---|------|------|-----|----|------|------|------|-----|-----|----|-----|------|
| 4   | 0 | 0 | 276   | 402   | -4  | 3  | 0 | 1373 | 1314 | -12 | 6 | 0 | 95   | 68   | 3   | 8  | 0    | 778  | 801  | 0   | 11  | 0  | 251 | 259  |
| 5   | 0 | 0 | 547   | 374   | -3  | 3  | 0 | 1950 | 1354 | -11 | 6 | 0 | 16   | 46   | 4   | 8  | 0    | 27   | 30   | 1   | 11  | 0  | 4   | 4    |
| 6   | 0 | 0 | 704   | 542   | 2   | 3  | 0 | 906  | 890  | -10 | 6 | 0 | 335  | 407  | 5   | 8  | 0    | 429  | 412  | 2   | 11  | 0  | 18  | 22   |
| 7   | 0 | 0 | 18    | 31    | 3   | 3  | 0 | 244  | 272  | -9  | 6 | 0 | 278  | 302  | 6   | 8  | 0    | 92   | 122  | 3   | 11  | 0  | 19  | 2    |
| 8   | 0 | 0 | 161   | 106   | 4   | 3  | 0 | 367  | 306  | -8  | 6 | 0 | 543  | 604  | 7   | 8  | 0    | 5    | 1    | 4   | 11  | 0  | 128 | 82   |
| 9   | 0 | 0 | 665   | 628   | 5   | 3  | 0 | 7517 | 6735 | -7  | 6 | 0 | 511  | 392  | 8   | 8  | 0    | 90   | 52   | 5   | 11  | 0  | 18  | 28   |
| 10  | 0 | 0 | 46    | 33    | 6   | 3  | 0 | 80   | 62   | -6  | 6 | 0 | 2040 | 2125 | 9   | 8  | 0    | 35   | 48   | 6   | 11  | 0  | 197 | 191  |
| 11  | 0 | 0 | 297   | 269   | 7   | 3  | 0 | 426  | 409  | -5  | 6 | 0 | 474  | 655  | -14 | 9  | 0    | 24   | 30   | 7   | 11  | 0  | 30  | 33   |
| 12  | 0 | 0 | 12    | 6     | 8   | 3  | 0 | 339  | 238  | -4  | 6 | 0 | 122  | 89   | -13 | 9  | 0    | -7   | 0    | -12 | 12  | 0  | 65  | 66   |
| 13  | 0 | 0 | 35    | 23    | 9   | 3  | 0 | 3    | 2    | -3  | 6 | 0 | 463  | 837  | -12 | 9  | 0    | 306  | 316  | -11 | 12  | 0  | 6   | 0    |
| 14  | 0 | 0 | 0     | 0     | 10  | 3  | 0 | 18   | 6    | -2  | 6 | 0 | 2959 | 2561 | -11 | 9  | 0    | 28   | 3    | -10 | 12  | 0  | 12  | 1    |
| -14 | 1 | 0 | 85    | 103   | 11  | 3  | 0 | 14   | 1    | -1  | 6 | 0 | 2095 | 2487 | -10 | 9  | 0    | 239  | 177  | -9  | 12  | 0  | 3   | 0    |
| -13 | 1 | 0 | 230   | 228   | 12  | 3  | 0 | 13   | 25   | 0   | 6 | 0 | 111  | 96   | -9  | 9  | 0    | 73   | 104  | -8  | 12  | 0  | 33  | 12   |
| -12 | 1 | 0 | 9     | 1     | -14 | 4  | 0 | 2    | 3    | 1   | 6 | 0 | 724  | 530  | -8  | 9  | 0    | 772  | 627  | -7  | 12  | 0  | 218 | 237  |
| -11 | 1 | 0 | 39    | 56    | -13 | 4  | 0 | 50   | 45   | 2   | 6 | 0 | 289  | 343  | -7  | 9  | 0    | 383  | 577  | -6  | 12  | 0  | 47  | 23   |
| -10 | 1 | 0 | 19    | 16    | -12 | 4  | 0 | 100  | 92   | 3   | 6 | 0 | 216  | 270  | -6  | 9  | 0    | 16   | 72   | -5  | 12  | 0  | 333 | 300  |
| -9  | 1 | 0 | 1017  | 972   | -11 | 4  | 0 | -1   | 1    | 4   | 6 | 0 | 247  | 139  | -5  | 9  | 0    | 1864 | 1401 | -4  | 12  | 0  | 3   | 16   |
| -8  | 1 | 0 | 200   | 187   | -10 | 4  | 0 | 615  | 501  | 5   | 6 | 0 | 23   | 43   | -4  | 9  | 0    | 223  | 208  | -3  | 12  | 0  | 507 | 631  |
| -7  | 1 | 0 | 1085  | 1117  | -9  | 4  | 0 | 246  | 227  | 6   | 6 | 0 | 8    | 14   | -3  | 9  | 0    | 692  | 650  | -2  | 12  | 0  | 198 | 220  |
| -6  | 1 | 0 | 530   | 439   | -8  | 4  | 0 | 1308 | 992  | 7   | 6 | 0 | 1405 | 1484 | -2  | 9  | 0    | 37   | 1    | -1  | 12  | 0  | 43  | 18   |
| -5  | 1 | 0 | 1853  | 1549  | -7  | 4  | 0 | 79   | 33   | 8   | 6 | 0 | 30   | 17   | -1  | 9  | 0    | 427  | 496  | 0   | 12  | 0  | 6   | 18   |
| -4  | 1 | 0 | 13875 | 15538 | -6  | 4  | 0 | 24   | 39   | 9   | 6 | 0 | 23   | 32   | 0   | 9  | 0    | -5   | 0    | 1   | 12  | 0  | 21  | 20   |
| -3  | 1 | 0 | 2     | 732   | -5  | 4  | 0 | 4855 | 4113 | 10  | 6 | 0 | 12   | 25   | 1   | 9  | 0    | 1183 | 971  | 2   | 12  | 0  | 86  | 53   |
| -2  | 1 | 0 | 2     | 559   | -4  | 4  | 0 | 913  | 1172 | 11  | 6 | 0 | 9    | 11   | 2   | 9  | 0    | 121  | 64   | 3   | 12  | 0  | 1   | 1    |
| -1  | 1 | 0 | 677   | 807   | -3  | 4  | 0 | 201  | 419  | -14 | 7 | 0 | 1    | 7    | 3   | 9  | 0    | 157  | 135  | 4   | 12  | 0  | 20  | 17   |
| 0   | 1 | 0 | 9711  | 9290  | 0   | 4  | 0 | 7112 | 7906 | -13 | 7 | 0 | 25   | 2    | 4   | 9  | 0    | 8    | 1    | 5   | 12  | 0  | 80  | 103  |
| 1   | 1 | 0 | 111   | 74    | 1   | 4  | 0 | 25   | 10   | -12 | 7 | 0 | 9    | 26   | 5   | 9  | 0    | 36   | 69   | -11 | 13  | 0  | 49  | 67   |
| 2   | 1 | 0 | 54    | 42    | 2   | 4  | 0 | 289  | 290  | -11 | 7 | 0 | 12   | 0    | 6   | 9  | 0    | 25   | 32   | -10 | 13  | 0  | 37  | 26   |
| 3   | 1 | 0 | 507   | 564   | 3   | 4  | 0 | 6    | 7    | -10 | 7 | 0 | 5    | 5    | 7   | 9  | 0    | 84   | 94   | -9  | 13  | 0  | 280 | 279  |
| 4   | 1 | 0 | 408   | 432   | 4   | 4  | 0 | 1214 | 996  | -9  | 7 | 0 | 56   | 33   | 8   | 9  | 0    | 128  | 118  | -8  | 13  | 0  | 147 | 139  |
| 5   | 1 | 0 | 16    | 9     | 5   | 4  | 0 | 495  | 835  | -8  | 7 | 0 | 63   | 40   | 9   | 9  | 0    | 38   | 13   | -7  | 13  | 0  | 160 | 187  |
| 6   | 1 | 0 | 11    | 10    | 6   | 4  | 0 | 23   | 16   | -7  | 7 | 0 | 1249 | 1030 | -13 | 10 | 0    | 4    | 0    | -6  | 13  | 0  | 50  | 57   |
| 7   | 1 | 0 | 11    | 1     | 7   | 4  | 0 | 8    | 19   | -6  | 7 | 0 | 446  | 421  | -12 | 10 | 0    | 95   | 99   | -5  | 13  | 0  | 39  | 89   |
| 8   | 1 | 0 | 12    | 2     | 8   | 4  | 0 | 3    | 19   | -5  | 7 | 0 | 1595 | 1284 | -11 | 10 | 0    | 0    | 3    | -4  | 13  | 0  | 175 | 127  |
| 9   | 1 | 0 | 0     | 2     | 9   | 4  | 0 | 1387 | 1277 | -4  | 7 | 0 | 1958 | 1528 | -10 | 10 | 0    | 570  | 453  | -3  | 13  | 0  | 473 | 477  |
| -13 | 2 | 0 | 17    | 4     | 10  | 4  | 0 | 12   | 4    | -3  | 7 | 0 | 44   | 42   | -9  | 10 | 0    | 28   | 32   | -2  | 13  | 0  | 307 | 251  |
| -12 | 2 | 0 | 6     | 11    | 11  | 4  | 0 | 80   | 84   | -2  | 7 | 0 | 589  | 623  | -8  | 10 | 0    | 585  | 631  | -1  | 13  | 0  | 513 | 469  |
| -11 | 2 | 0 | 337   | 329   | 12  | 4  | 0 | 17   | 25   | -1  | 7 | 0 | 832  | 999  | -7  | 10 | 0    | -2   | 13   | 0   | 13  | 0  | 146 | 155  |
| -10 | 2 | 0 | 50    | 93    | -14 | 5  | 0 | 0    | 0    | 0   | 7 | 0 | 1715 | 1882 | -6  | 10 | 0    | 306  | 419  | 1   | 13  | 0  | 347 | 335  |
| -9  | 2 | 0 | 250   | 263   | -13 | 5  | 0 | 27   | 6    | 1   | 7 | 0 | 23   | 62   | -5  | 10 | 0    | 0    | 11   | 2   | 13  | 0  | 18  | 21   |
| -8  | 2 | 0 | 1288  | 1428  | -12 | 5  | 0 | 299  | 267  | 2   | 7 | 0 | 989  | 1030 | -4  | 10 | 0    | 39   | 67   | 3   | 13  | 0  | 82  | 77   |
| -7  | 2 | 0 | 13    | 1     | -11 | 5  | 0 | 266  | 250  | 3   | 7 | 0 | 781  | 409  | -3  | 10 | 0    | 243  | 147  | 4   | 13  | 0  | 70  | 86   |
| -6  | 2 | 0 | 156   | 94    | -10 | 5  | 0 | 73   | 49   | 4   | 7 | 0 | 50   | 113  | -2  | 10 | 0    | 188  | 169  | -10 | 14  | 0  | 2   | 1    |
| -5  | 2 | 0 | 2629  | 2155  | -9  | 5  | 0 | 138  | 134  | 5   | 7 | 0 | 952  | 729  | -1  | 10 | 0    | 311  | 288  | -9  | 14  | 0  | 5   | 9    |
| -4  | 2 | 0 | 103   | 124   | -8  | 5  | 0 | 531  | 633  | 6   | 7 | 0 | 395  | 510  | 0   | 10 | 0    | 34   | 65   | -8  | 14  | 0  | 33  | 57   |
| -3  | 2 | 0 | 861   | 938   | -7  | 5  | 0 | 767  | 475  | 7   | 7 | 0 | 302  | 322  | 1   | 10 | 0    | 255  | 170  | -7  | 14  | 0  | 449 | 447  |
| -2  | 2 | 0 | 2732  | 2150  | -6  | 5  | 0 | 1448 | 1661 | 8   | 7 | 0 | 3    | 5    | 2   | 10 | 0    | 0    | 2    | -6  | 14  | 0  | 17  | 11   |
| -1  | 2 | 0 | 418   | 604   | -5  | 5  | 0 | 2446 | 2204 | 9   | 7 | 0 | 70   | 51   | 3   | 10 | 0    | 204  | 204  | -5  | 14  | 0  | 171 | 123  |
| 0   | 2 | 0 | 4525  | 4359  | -4  | 5  | 0 | 1697 | 1667 | 10  | 7 | 0 | 28   | 23   | 4   | 10 | 0    | 11   | 45   | -4  | 14  | 0  | 106 | 108  |
| 1   | 2 | 0 | 96    | 83    | -3  | 5  | 0 | 204  | 310  | -14 | 8 | 0 | 76   | 82   | 5   | 10 | 0    | 19   | 2    | -3  | 14  | 0  | 82  | 120  |
| 2   | 2 | 0 | 178   | 97    | -2  | 5  | 0 | 171  | 162  | -13 | 8 | 0 | 216  | 226  | 6   | 10 | 0    | 6    | 12   | -2  | 14  | 0  | 77  | 99   |
| 3   | 2 | 0 | 392   | 392   | -1  | 5  | 0 | 195  | 155  | -12 | 8 | 0 | 7    | 3    | 7   | 10 | 0    | -5   | 3    | -1  | 14  | 0  | 31  | 19   |
| 4   | 2 | 0 | 50    | 64    | 0   | 5  | 0 | 1147 | 893  | -11 | 8 | 0 | -1   | 25   | 8   | 10 | 0    | 79   | 73   | 0   | 14  | 0  | 236 | 202  |
| 5   | 2 | 0 | 116   | 141   | 1   | 5  | 0 | 441  | 380  | -10 | 8 | 0 | 125  | 125  | -13 | 11 | 0    | 1    | 8    | 1   | 14  | 0  | 19  | 15   |
| 6   | 2 | 0 | 29    | 29    | 2   | 5  | 0 | 1980 | 2349 | -9  | 8 | 0 | 105  | 80   | -12 | 11 | 0    | 195  | 232  | 2   | 14  | 0  | 6   | 0    |
| 7   | 2 | 0 | 27    | 12    | 3   | 5  | 0 | 2213 | 1987 | -8  | 8 | 0 | 751  | 643  | -11 | 11 | 0    | -2   | 6    | -9  | 15  | 0  | 9   | 10   |
| 8   | 2 | 0 | 6     | 2     | 4   | 5  | 0 | 1373 | 1218 | -7  | 8 | 0 | 129  | 100  | -10 | 11 | 0    | 55   | 44   | -8  | 15  | 0  | -12 | 0    |
| -13 | 3 | 0 | 92    | 60    | 5   | 5  | 0 | 1290 | 1158 | -6  | 8 | 0 | 2158 | 1928 | -9  | 11 | 0    | 124  | 155  | -7  | 15  | 0  | 167 | 118  |
| -12 | 3 | 0 | 0     | 1     | 6   | 5  | 0 | -3   | 0    | -5  | 8 | 0 | -7   | 43   | -8  | 11 | 0    | 163  | 172  | -6  | 15  | 0  | -10 | 2    |
| -11 | 3 | 0 | 26    | 47    | 7   | 5  | 0 | 2211 | 1738 | -4  | 8 | 0 | 266  | 437  | -7  | 11 | 0    | 422  | 319  | -5  | 15  | 0  | 192 | 111  |
| -10 | 3 | 0 | 255   | 273   | 8   | 5  | 0 | 38   | 42   | -3  | 8 | 0 | 919  | 952  | -6  | 11 | 0    | 120  | 90   | -4  | 15  | 0  | 8   | 0    |
| -9  | 3 | 0 | 207   | 289   | 9   | 5  | 0 | -3   | 6    | -2  | 8 | 0 | 85   | 99   | -5  | 11 | 0    | 423  | 441  | -3  | 15  | 0  | 16  | 32   |
| -8  | 3 | 0 | 65    | 4     | 10  | 5  | 0 | 88   | 112  | -1  | 8 | 0 | 2825 | 2960 | -4  | 11 | 0    | 331  | 250  | -2  | 15  | 0  | 191 | 161  |
| -7  | 3 | 0 | 4869  | 5068  | 11  | 5  | 0 | 3    | 1    | 0   | 8 | 0 | 28   | 55   | -3  | 11 | 0    | 344  | 385  | -1  | 15  | 0  | 93  | 101  |
| -6  | 3 | 0 | 246   | 286   | -14 | 6  | 0 | 1    | 0    | 1   | 8 | 0 | 1314 | 1426 | -2  | 11 | 0    | 6    | 4    | 0   | 15  | 0  | 1   | 0    |
| -5  | 3 | 0 | 61    | 57    | -13 | 6  | 0 | 118  | 90   | 2   | 8 | 0 | 217  | 140  | -1  | 11 | 0    | 526  | 445  | 2   | -16 | 1  | 7   | 4    |
| -4  | 3 | 0 | 1     | 22    | -6  | 11 | 1 | 27   | 7    | -10 | 8 | 1 | 9    | 4    | -6  | 1  | 4490 | 5045 | -9   | -3  | 1   | 24 | 10  |      |
| -3  | 3 | 0 | 18    | 11    | -5  | 11 | 1 | 110  | 105  | -9  | 8 | 1 | 177  | 202  | -8  | 11 | 0    | 4235 | 3510 | -8  | -3  | 1  | 75  | 63   |
| -2  | 3 | 0 | 8     | 1     | -4  | 11 | 1 | -2   | 12   | -8  | 8 | 1 | 184  | 203  | -6  | -6 | 1    | 194  | 139  | -7  | -3  | 1  | 5   | 2    |
| -1  | 3 | 0 | 55    | 31    | -3  | 11 | 1 | 57   | 33   | -7  | 8 | 1 | 105  | 84   | -7  | -6 | 1    | 1076 | 1103 | -6  | -3  | 1  | 69  | 27   |
| 0   | 3 | 0 | 17    | 7     | -2  | 11 | 1 |      |      |     |   |   |      |      |     |    |      |      |      |     |     |    |     |      |

Table C.3, continued

| M      | K | L | Obs  | Calc | M     | K | L | Obs   | Calc  | M     | K | L | Obs  | Calc | M     | K | L | Obs  | Calc | M      | K | L | Obs   | Calc  |
|--------|---|---|------|------|-------|---|---|-------|-------|-------|---|---|------|------|-------|---|---|------|------|--------|---|---|-------|-------|
| 3-13   | 1 |   | 62   | 86   | 9-10  | 1 |   | 259   | 421   | 1-7   | 1 |   | 130  | 95   | 14-5  | 1 |   | 49   | 57   | 11-2   | 1 |   | 38    | 61    |
| 4-13   | 1 |   | 160  | 190  | 10-10 | 1 |   | 242   | 356   | 2-7   | 1 |   | 1721 | 1521 | -12-4 | 1 |   | 9    | 4    | 12-2   | 1 |   | 313   | 278   |
| 5-13   | 1 |   | 97   | 79   | 11-10 | 1 |   | 81    | 79    | 3-7   | 1 |   | 1832 | 1861 | -11-4 | 1 |   | 366  | 326  | 13-2   | 1 |   | 20    | 33    |
| 6-13   | 1 |   | 328  | 365  | 12-10 | 1 |   | 92    | 129   | 4-7   | 1 |   | 742  | 581  | -10-4 | 1 |   | 7    | 8    | 14-2   | 1 |   | 2     | 7     |
| 7-13   | 1 |   | 185  | 151  | 13-10 | 1 |   | 65    | 68    | 5-7   | 1 |   | 402  | 296  | -9-4  | 1 |   | 134  | 149  | -14-1  | 1 |   | 31    | 29    |
| 8-13   | 1 |   | 79   | 50   | -8-9  | 1 |   | 12    | 17    | 6-7   | 1 |   | 150  | 38   | -8-4  | 1 |   | 321  | 215  | -13-1  | 1 |   | -5    | 4     |
| 9-13   | 1 |   | 66   | 59   | -8-9  | 1 |   | 3     | 1     | 7-7   | 1 |   | 132  | 87   | -7-4  | 1 |   | 893  | 875  | -12-1  | 1 |   | -5    | 0     |
| 10-13  | 1 |   | 0    | 1    | -7-9  | 1 |   | 197   | 153   | 8-7   | 1 |   | 40   | 18   | -6-4  | 1 |   | 557  | 379  | -11-1  | 1 |   | 10    | 13    |
| 11-13  | 1 |   | 11   | 3    | -6-9  | 1 |   | 4     | 1     | 9-7   | 1 |   | 782  | 612  | -5-4  | 1 |   | 397  | 377  | -10-1  | 1 |   | 179   | 226   |
| -6-12  | 1 |   | 6    | 0    | -5-9  | 1 |   | 14    | 17    | 10-7  | 1 |   | 45   | 66   | -4-4  | 1 |   | 3488 | 3238 | -9-1   | 1 |   | 65    | 62    |
| -5-12  | 1 |   | 182  | 210  | -4-9  | 1 |   | 463   | 584   | 11-7  | 1 |   | 694  | 704  | -3-4  | 1 |   | 1479 | 1472 | -8-1   | 1 |   | 231   | 227   |
| -4-12  | 1 |   | 42   | 24   | -3-9  | 1 |   | 217   | 221   | 12-7  | 1 |   | 8    | 18   | -2-4  | 1 |   | 6153 | 6700 | -7-1   | 1 |   | 39    | 103   |
| -3-12  | 1 |   | 24   | 7    | -2-9  | 1 |   | 21    | 59    | 13-7  | 1 |   | 33   | 51   | -1-4  | 1 |   | 1388 | 1592 | -6-1   | 1 |   | 120   | 163   |
| -2-12  | 1 |   | 222  | 205  | -1-9  | 1 |   | 878   | 1123  | 14-7  | 1 |   | 15   | 1    | 3-4   | 1 |   | 4605 | 6182 | -5-1   | 1 |   | 156   | 53    |
| -1-12  | 1 |   | 468  | 498  | 0-9   | 1 |   | 760   | 905   | -11-6 | 1 |   | 218  | 219  | 4-4   | 1 |   | 445  | 254  | -4-1   | 1 |   | 3958  | 3832  |
| 0-12   | 1 |   | 28   | 24   | 1-9   | 1 |   | 37    | 14    | -10-6 | 1 |   | 131  | 156  | 5-4   | 1 |   | 1116 | 1433 | 4-1    | 1 |   | 1762  | 1542  |
| 1-12   | 1 |   | 11   | 1    | 2-9   | 1 |   | 199   | 214   | -9-6  | 1 |   | 773  | 638  | 6-4   | 1 |   | 379  | 263  | 5-1    | 1 |   | 11716 | 11202 |
| 2-12   | 1 |   | -3   | 1    | 3-9   | 1 |   | 53    | 36    | -8-6  | 1 |   | 28   | 14   | 7-4   | 1 |   | 3    | 3    | 6-1    | 1 |   | 164   | 161   |
| 3-12   | 1 |   | 24   | 32   | 4-9   | 1 |   | 716   | 671   | -7-6  | 1 |   | -3   | 1    | 8-4   | 1 |   | 8    | 2    | 7-1    | 1 |   | 57    | 141   |
| 4-12   | 1 |   | 351  | 245  | 5-9   | 1 |   | 1504  | 1364  | -6-6  | 1 |   | 1000 | 1142 | 9-4   | 1 |   | 142  | 117  | 8-1    | 1 |   | 8     | 2     |
| 5-12   | 1 |   | 99   | 57   | 6-9   | 1 |   | 1685  | 1187  | -5-6  | 1 |   | 3    | 7    | 10-4  | 1 |   | 1100 | 907  | 9-1    | 1 |   | 120   | 92    |
| 6-12   | 1 |   | 1005 | 762  | 7-9   | 1 |   | 115   | 156   | -4-6  | 1 |   | 1221 | 1468 | 11-4  | 1 |   | 38   | 46   | 10-1   | 1 |   | 274   | 199   |
| 7-12   | 1 |   | 9    | 10   | 8-9   | 1 |   | 822   | 939   | -3-6  | 1 |   | 369  | 264  | 12-4  | 1 |   | 385  | 296  | 11-1   | 1 |   | 7     | 6     |
| 8-12   | 1 |   | 270  | 317  | 9-9   | 1 |   | 5     | 1     | -2-6  | 1 |   | 7200 | 7136 | 13-4  | 1 |   | 85   | 91   | 12-1   | 1 |   | 6     | 2     |
| 9-12   | 1 |   | 90   | 117  | 10-9  | 1 |   | 222   | 177   | -1-6  | 1 |   | 2577 | 2711 | 14-4  | 1 |   | 11   | 28   | 13-1   | 1 |   | 4     | 4     |
| 10-12  | 1 |   | 208  | 198  | 11-9  | 1 |   | 254   | 239   | 0-6   | 1 |   | 3546 | 4149 | -13-3 | 1 |   | 126  | 94   | 14-1   | 1 |   | 33    | 51    |
| 11-12  | 1 |   | 45   | 28   | 12-9  | 1 |   | 38    | 28    | 1-6   | 1 |   | 357  | 373  | -12-3 | 1 |   | 38   | 55   | -14-0  | 1 |   | 24    | 27    |
| 12-12  | 1 |   | 13   | 5    | 13-9  | 1 |   | 12    | 22    | 2-6   | 1 |   | 150  | 180  | -11-3 | 1 |   | 69   | 42   | -13-0  | 1 |   | -2    | 4     |
| -7-11  | 1 |   | 52   | 51   | 14-9  | 1 |   | 15    | 17    | 3-6   | 1 |   | 420  | 440  | -10-3 | 1 |   | 5    | 1    | -12-0  | 1 |   | 400   | 359   |
| -11-10 | 1 |   | 30   | 8    | -14-3 | 1 |   | 25    | 23    | 1-5   | 1 |   | 300  | 287  | 9-8   | 1 |   | 1330 | 1190 | -10-11 | 1 |   | 53    | 68    |
| -10-10 | 1 |   | 359  | 193  | -13-3 | 1 |   | 63    | 64    | 2-5   | 1 |   | 478  | 273  | -8-8  | 1 |   | 49   | 29   | -9-11  | 1 |   | -5    | 3     |
| -9-10  | 1 |   | 154  | 192  | -12-3 | 1 |   | 7     | 6     | 3-5   | 1 |   | 3509 | 3365 | -7-8  | 1 |   | 2315 | 2359 | -8-11  | 1 |   | 138   | 137   |
| -8-10  | 1 |   | 53   | 26   | -11-3 | 1 |   | 275   | 195   | 4-5   | 1 |   | 1704 | 1580 | -6-8  | 1 |   | 653  | 508  | -7-11  | 1 |   | 144   | 210   |
| -7-10  | 1 |   | 979  | 1301 | -10-3 | 1 |   | 251   | 181   | 5-5   | 1 |   | 0    | 0    | -5-8  | 1 |   | 1763 | 1453 | -6-11  | 1 |   | 29    | 24    |
| -6-10  | 1 |   | 775  | 996  | -9-3  | 1 |   | 1     | 1     | 6-5   | 1 |   | 86   | 74   | -4-8  | 1 |   | 52   | 129  | -5-11  | 1 |   | 58    | 63    |
| -5-10  | 1 |   | 404  | 660  | -8-3  | 1 |   | 630   | 619   | 7-5   | 1 |   | 453  | 405  | -3-8  | 1 |   | 2214 | 2233 | -4-11  | 1 |   | 386   | 564   |
| -4-10  | 1 |   | 8046 | 8432 | -7-3  | 1 |   | 367   | 294   | 8-5   | 1 |   | 578  | 563  | -2-8  | 1 |   | 3    | 16   | -3-11  | 1 |   | 319   | 296   |
| -3-10  | 1 |   | 1    | 139  | -6-3  | 1 |   | 1549  | 1128  | 9-5   | 1 |   | 29   | 54   | -1-8  | 1 |   | 21   | 56   | -2-11  | 1 |   | 446   | 306   |
| 3-10   | 1 |   | 376  | 255  | -5-3  | 1 |   | 964   | 840   | 10-5  | 1 |   | 195  | 165  | 0-8   | 1 |   | 91   | 164  | -1-11  | 1 |   | 156   | 138   |
| 4-10   | 1 |   | 2687 | 2913 | -4-3  | 1 |   | -3    | 7     | 11-5  | 1 |   | 15   | 11   | 1-8   | 1 |   | 124  | 136  | 0-11   | 1 |   | 9     | 7     |
| 5-10   | 1 |   | 364  | 308  | -3-3  | 1 |   | 8622  | 8669  | -14-6 | 1 |   | 54   | 43   | 2-8   | 1 |   | 183  | 265  | 1-11   | 1 |   | 73    | 74    |
| 6-10   | 1 |   | 3564 | 3854 | -2-3  | 1 |   | 9043  | 9989  | -13-6 | 1 |   | 60   | 78   | 3-8   | 1 |   | 144  | 117  | 2-11   | 1 |   | 27    | 29    |
| 7-10   | 1 |   | 42   | 81   | 2-3   | 1 |   | 877   | 621   | -12-6 | 1 |   | 535  | 458  | 4-8   | 1 |   | 322  | 364  | 3-11   | 1 |   | 198   | 206   |
| 8-10   | 1 |   | 60   | 48   | 3-3   | 1 |   | 39    | 57    | -11-6 | 1 |   | 77   | 104  | 5-8   | 1 |   | 82   | 88   | 4-11   | 1 |   | 433   | 434   |
| 9-10   | 1 |   | 5    | 4    | 4-3   | 1 |   | 196   | 227   | -10-6 | 1 |   | 170  | 170  | 6-8   | 1 |   | 148  | 171  | 5-11   | 1 |   | 52    | 42    |
| 10-10  | 1 |   | 246  | 169  | 5-3   | 1 |   | 1853  | 1908  | -9-6  | 1 |   | 270  | 274  | 7-8   | 1 |   | 208  | 205  | 6-11   | 1 |   | 65    | 62    |
| 11-10  | 1 |   | 45   | 45   | 6-3   | 1 |   | 1598  | 1098  | -8-6  | 1 |   | 13   | 1    | 8-8   | 1 |   | 58   | 23   | -12-12 | 1 |   | -4    | 0     |
| 12-10  | 1 |   | 74   | 78   | 7-3   | 1 |   | 1147  | 1267  | -7-6  | 1 |   | 55   | 21   | 9-8   | 1 |   | 9    | 11   | -11-12 | 1 |   | 108   | 104   |
| 13-10  | 1 |   | 60   | 66   | 8-3   | 1 |   | 754   | 650   | -6-6  | 1 |   | 502  | 523  | -14-9 | 1 |   | 0    | 10   | -10-12 | 1 |   | 14    | 26    |
| -14-11 | 1 |   | 7    | 0    | 9-3   | 1 |   | 3     | 5     | -5-6  | 1 |   | 1159 | 1060 | -13-9 | 1 |   | 90   | 88   | -9-12  | 1 |   | -1    | 6     |
| -13-11 | 1 |   | 4    | 0    | 10-3  | 1 |   | 84    | 77    | -4-6  | 1 |   | 137  | 150  | -12-9 | 1 |   | 27   | 27   | -8-12  | 1 |   | 62    | 102   |
| -12-11 | 1 |   | 52   | 61   | 11-3  | 1 |   | 2     | 6     | -3-6  | 1 |   | 169  | 215  | -11-9 | 1 |   | 285  | 302  | -7-12  | 1 |   | 89    | 125   |
| -11-11 | 1 |   | 47   | 48   | 12-3  | 1 |   | 116   | 111   | -2-6  | 1 |   | 332  | 240  | -10-9 | 1 |   | 9    | 22   | -6-12  | 1 |   | 124   | 87    |
| -10-11 | 1 |   | 625  | 677  | -14-4 | 1 |   | 41    | 47    | -1-6  | 1 |   | 272  | 153  | -9-9  | 1 |   | 552  | 652  | -5-12  | 1 |   | 291   | 279   |
| -9-11  | 1 |   | 71   | 39   | -13-4 | 1 |   | 17    | 21    | 0-6   | 1 |   | 1151 | 922  | -8-9  | 1 |   | 31   | 3    | -4-12  | 1 |   | 441   | 310   |
| -8-11  | 1 |   | 10   | 25   | -12-4 | 1 |   | 726   | 641   | 1-6   | 1 |   | 3648 | 3283 | -7-9  | 1 |   | 2359 | 1875 | -3-12  | 1 |   | 65    | 37    |
| -7-11  | 1 |   | 1369 | 1116 | -11-4 | 1 |   | 124   | 111   | 2-6   | 1 |   | 3017 | 3689 | -6-9  | 1 |   | 2    | 18   | -2-12  | 1 |   | 643   | 787   |
| -6-11  | 1 |   | 2288 | 2532 | -10-4 | 1 |   | 128   | 150   | 3-6   | 1 |   | 35   | 64   | -5-9  | 1 |   | 649  | 637  | -1-12  | 1 |   | 27    | 59    |
| -5-11  | 1 |   | 3652 | 4119 | -9-4  | 1 |   | 276   | 216   | 4-6   | 1 |   | 116  | 169  | -4-9  | 1 |   | 419  | 462  | 0-12   | 1 |   | 201   | 249   |
| -4-11  | 1 |   | 4729 | 5009 | -8-4  | 1 |   | 418   | 417   | 5-6   | 1 |   | 19   | 37   | -3-9  | 1 |   | 58   | 90   | 1-12   | 1 |   | 171   | 164   |
| 3-11   | 1 |   | 1152 | 754  | -7-4  | 1 |   | 426   | 440   | 6-6   | 1 |   | 9    | 10   | -2-9  | 1 |   | 352  | 384  | 2-12   | 1 |   | 524   | 529   |
| 4-11   | 1 |   | 1002 | 1072 | -6-4  | 1 |   | 938   | 1045  | 7-6   | 1 |   | 5    | 23   | -1-9  | 1 |   | 873  | 722  | 3-12   | 1 |   | 136   | 114   |
| 5-11   | 1 |   | 929  | 919  | -5-4  | 1 |   | 206   | 237   | 8-6   | 1 |   | 597  | 600  | 0-9   | 1 |   | 1    | 3    | 12-1   | 1 |   | 30    | 21    |
| 6-11   | 1 |   | 1236 | 1313 | -4-4  | 1 |   | 1090  | 928   | 9-6   | 1 |   | 37   | 46   | 1-9   | 1 |   | 458  | 403  | 5-12   | 1 |   | 23    | 24    |
| 7-11   | 1 |   | 2222 | 2052 | -3-4  | 1 |   | 1360  | 1732  | 10-6  | 1 |   | 4    | 3    | 2-9   | 1 |   | 414  | 293  | -11-13 | 1 |   | -6    | 1     |
| 8-11   | 1 |   | 1310 | 1529 | -2-4  | 1 |   | 2876  | 3583  | -14-7 | 1 |   | 13   | 14   | 3-9   | 1 |   | 7    | 7    | -10-13 | 1 |   | 65    | 94    |
| 9-11   | 1 |   | 84   | 94   | -1-4  | 1 |   | 7290  | 7993  | -13-7 | 1 |   | 222  | 262  | 4-9   | 1 |   | 200  | 148  | -9-13  | 1 |   | 66    | 39    |
| 10-11  | 1 |   | 17   | 23   | 0-4   | 1 |   | 1350  | 1512  | -12-7 | 1 |   | 52   | 34   | 5-9   | 1 |   | 7    | 7    | -8-13  | 1 |   | 60    | 33    |
| 11-11  | 1 |   | 10   | 14   | 1-4   | 1 |   | 789   | 759   | -11-7 | 1 |   | 729  | 773  | 6-9   | 1 |   | 63   | 90   | -7-13  | 1 |   | 8     | 4     |
| 12-11  | 1 |   | 218  | 235  | 2-4   | 1 |   | 18301 | 17560 | -10-7 | 1 |   | 34   | 44   | 7-9   | 1 |   | 5    | 5    | -6-13  | 1 |   |       |       |



Table C.3, continued

| H     | K | L     | Obs   | Calc  | H | K    | L    | Obs   | Calc | H    | K    | L     | Obs | Calc  | H     | K      | L | Obs   | Calc  | H | K | L | Obs | Calc |
|-------|---|-------|-------|-------|---|------|------|-------|------|------|------|-------|-----|-------|-------|--------|---|-------|-------|---|---|---|-----|------|
| 5-16  | 2 | 15    | 9     | 12-12 | 2 | 84   | 81   | 10-9  | 2    | 11   | 9    | -1-6  | 2   | 541   | 355   | 12-4   | 2 | 20    | 16    |   |   |   |     |      |
| 6-16  | 2 | 160   | 209   | -8-11 | 2 | 61   | 50   | 11-9  | 2    | 8    | 11   | 0-6   | 2   | 5758  | 5150  | 13-4   | 2 | 4     | 2     |   |   |   |     |      |
| 7-16  | 2 | -1    | 2     | -7-11 | 2 | 0    | 1    | 12-9  | 2    | 188  | 191  | 1-6   | 2   | 27    | 40    | 14-4   | 2 | 21    | 16    |   |   |   |     |      |
| -2-15 | 2 | 72    | 63    | -6-11 | 2 | 33   | 50   | 13-9  | 2    | -6   | 1    | 2-6   | 2   | 1538  | 1054  | -13-3  | 2 | -2    | 0     |   |   |   |     |      |
| -1-15 | 2 | 60    | 21    | -5-11 | 2 | 36   | 24   | -10-8 | 2    | 25   | 16   | 3-6   | 2   | 216   | 106   | -12-3  | 2 | 16    | 14    |   |   |   |     |      |
| 0-15  | 2 | 225   | 206   | -4-11 | 2 | 1    | 2    | -9-8  | 2    | 90   | 45   | 4-6   | 2   | 1328  | 1187  | -11-3  | 2 | 0     | 11    |   |   |   |     |      |
| 1-15  | 2 | 19    | 27    | -3-11 | 2 | 135  | 115  | -8-8  | 2    | 221  | 208  | 5-6   | 2   | 7170  | 5750  | -10-3  | 2 | 242   | 265   |   |   |   |     |      |
| 2-15  | 2 | 193   | 192   | -2-11 | 2 | 353  | 395  | -7-8  | 2    | 39   | 28   | 6-6   | 2   | 5     | 4     | -9-3   | 2 | 57    | 24    |   |   |   |     |      |
| 3-15  | 2 | 122   | 118   | -1-11 | 2 | 6    | 18   | -6-8  | 2    | 291  | 236  | 7-6   | 2   | 419   | 378   | -8-3   | 2 | 11    | 2     |   |   |   |     |      |
| 4-15  | 2 | 4     | 28    | 0-11  | 2 | 54   | 25   | -5-8  | 2    | 5    | 2    | 8-6   | 2   | 300   | 336   | -7-3   | 2 | 2     | 6     |   |   |   |     |      |
| 5-15  | 2 | 23    | 30    | 1-11  | 2 | 113  | 98   | -4-8  | 2    | 51   | 22   | 9-6   | 2   | 118   | 92    | -6-3   | 2 | 127   | 179   |   |   |   |     |      |
| 6-15  | 2 | 154   | 173   | 2-11  | 2 | 254  | 223  | -3-8  | 2    | 27   | 22   | 10-6  | 2   | 515   | 565   | -5-3   | 2 | 1481  | 1346  |   |   |   |     |      |
| 7-15  | 2 | -8    | 9     | 3-11  | 2 | 45   | 83   | -2-8  | 2    | 1800 | 1716 | 11-6  | 2   | 8     | 16    | -4-3   | 2 | 809   | 860   |   |   |   |     |      |
| 8-15  | 2 | 81    | 45    | 4-11  | 2 | -1   | 1    | -1-8  | 2    | 128  | 149  | 12-6  | 2   | 18    | 10    | -3-3   | 2 | 2146  | 1687  |   |   |   |     |      |
| 9-15  | 2 | 19    | 12    | 5-11  | 2 | 727  | 740  | 0-8   | 2    | 5892 | 6308 | 13-6  | 2   | 24    | 54    | 1-3    | 2 | 1735  | 1774  |   |   |   |     |      |
| -4-14 | 2 | 7     | 18    | 6-11  | 2 | 132  | 225  | 1-8   | 2    | 5657 | 5034 | 14-6  | 2   | 0     | 1     | 3-3    | 2 | 7443  | 8400  |   |   |   |     |      |
| -3-14 | 2 | 44    | 52    | 7-11  | 2 | 365  | 388  | 2-8   | 2    | 0    | 0    | -12-5 | 2   | 93    | 100   | 4-3    | 2 | 11732 | 11211 |   |   |   |     |      |
| -2-14 | 2 | 302   | 274   | 8-11  | 2 | 132  | 165  | 3-8   | 2    | 82   | 110  | -11-5 | 2   | 18    | 18    | 5-3    | 2 | 2222  | 2018  |   |   |   |     |      |
| -1-14 | 2 | 10    | 1     | 9-11  | 2 | 168  | 176  | 4-8   | 2    | 1055 | 996  | -10-5 | 2   | 261   | 263   | 6-3    | 2 | 4663  | 5321  |   |   |   |     |      |
| 0-14  | 2 | 100   | 59    | 10-11 | 2 | 3    | 2    | 5-8   | 2    | 38   | 27   | -9-5  | 2   | 24    | 22    | 7-3    | 2 | 1567  | 1310  |   |   |   |     |      |
| 1-14  | 2 | 75    | 111   | 11-11 | 2 | 212  | 176  | 6-8   | 2    | 689  | 583  | -8-5  | 2   | 139   | 112   | 8-3    | 2 | 3468  | 2958  |   |   |   |     |      |
| 2-14  | 2 | 13    | 5     | 12-11 | 2 | 79   | 109  | 7-8   | 2    | 981  | 794  | -7-5  | 2   | 5     | 5     | 9-3    | 2 | 561   | 583   |   |   |   |     |      |
| 3-14  | 2 | 12    | 16    | 13-11 | 2 | -7   | 1    | 8-8   | 2    | 26   | 37   | -6-5  | 2   | 1659  | 1383  | 10-3   | 2 | 222   | 160   |   |   |   |     |      |
| 4-14  | 2 | -1    | 10    | -9-10 | 2 | 29   | 36   | 9-8   | 2    | 126  | 151  | -5-5  | 2   | 698   | 726   | -11-3  | 2 | 111   | 102   |   |   |   |     |      |
| 5-14  | 2 | 15    | 0     | -8-10 | 2 | 15   | 19   | 10-8  | 2    | 44   | 34   | -4-5  | 2   | 729   | 557   | 12-3   | 2 | 265   | 297   |   |   |   |     |      |
| 6-14  | 2 | 83    | 44    | -7-10 | 2 | 10   | 9    | 11-8  | 2    | 6    | 1    | -3-5  | 2   | 129   | 124   | 13-3   | 2 | 18    | 10    |   |   |   |     |      |
| 7-14  | 2 | 130   | 160   | -6-10 | 2 | 71   | 81   | 12-8  | 2    | 21   | 20   | -2-5  | 2   | 10585 | 10224 | 14-3   | 2 | 29    | 49    |   |   |   |     |      |
| 8-14  | 2 | 148   | 183   | -5-10 | 2 | 71   | 59   | 13-8  | 2    | 47   | 57   | -1-5  | 2   | 18068 | 16741 | -14-2  | 2 | 5     | 4     |   |   |   |     |      |
| 9-14  | 2 | 70    | 54    | -4-10 | 2 | 119  | 113  | 14-8  | 2    | 8    | 3    | 0-5   | 2   | 203   | 117   | -13-2  | 2 | -3    | 2     |   |   |   |     |      |
| 10-14 | 2 | 24    | 28    | -3-10 | 2 | 7    | 4    | -11-7 | 2    | 30   | 22   | 1-5   | 2   | 3378  | 4071  | -12-2  | 2 | 441   | 428   |   |   |   |     |      |
| -5-13 | 2 | -4    | 3     | -2-10 | 2 | 1553 | 1550 | -10-7 | 2    | 30   | 0    | 2-5   | 2   | 947   | 1093  | -11-2  | 2 | 89    | 102   |   |   |   |     |      |
| -4-13 | 2 | 6     | 4     | -1-10 | 2 | 329  | 426  | -9-7  | 2    | 281  | 340  | 3-5   | 2   | 1539  | 2173  | -10-2  | 2 | 17    | 14    |   |   |   |     |      |
| -3-13 | 2 | 7     | 0     | 0-10  | 2 | 80   | 78   | -8-7  | 2    | 1166 | 994  | 4-5   | 2   | 68    | 128   | -9-2   | 2 | 336   | 341   |   |   |   |     |      |
| -2-13 | 2 | 77    | 75    | 1-10  | 2 | 2549 | 2580 | -7-7  | 2    | 168  | 190  | 5-5   | 2   | 1664  | 1486  | -8-2   | 2 | 77    | 141   |   |   |   |     |      |
| -1-13 | 2 | -1    | 1     | 2-10  | 2 | 453  | 526  | -6-7  | 2    | 286  | 298  | 6-5   | 2   | 698   | 570   | -7-2   | 2 | 405   | 421   |   |   |   |     |      |
| 0-13  | 2 | 7     | 15    | 3-10  | 2 | 914  | 802  | -5-7  | 2    | 3    | 1    | 7-5   | 2   | 845   | 797   | -6-2   | 2 | 2249  | 1902  |   |   |   |     |      |
| 1-13  | 2 | 31    | 44    | 4-10  | 2 | 9    | 36   | -4-7  | 2    | 0    | 1    | 8-5   | 2   | 1389  | 1126  | -5-2   | 2 | 3494  | 3366  |   |   |   |     |      |
| 2-13  | 2 | 333   | 255   | 5-10  | 2 | 262  | 151  | -3-7  | 2    | 202  | 324  | 9-5   | 2   | 107   | 99    | -4-2   | 2 | 1264  | 1295  |   |   |   |     |      |
| 3-13  | 2 | 163   | 174   | 6-10  | 2 | 67   | 71   | -2-7  | 2    | 64   | 181  | 10-5  | 2   | 282   | 268   | -3-2   | 2 | -2    | 44    |   |   |   |     |      |
| 4-13  | 2 | 147   | 115   | 7-10  | 2 | 933  | 780  | -1-7  | 2    | 3379 | 3215 | 11-5  | 2   | 2     | 1     | -2-2   | 2 | 2     | 1     |   |   |   |     |      |
| 5-13  | 2 | 12    | 1     | 8-10  | 2 | 1    | 1    | 0-7   | 2    | -6   | 5    | 12-5  | 2   | 615   | 466   | 2-2    | 2 | 2     | 314   |   |   |   |     |      |
| 6-13  | 2 | 5     | 2     | 9-10  | 2 | 298  | 195  | 1-7   | 2    | 966  | 868  | 13-5  | 2   | 52    | 56    | 3-2    | 2 | 17286 | 16116 |   |   |   |     |      |
| 7-13  | 2 | 361   | 374   | 10-10 | 2 | 69   | 98   | 2-7   | 2    | 579  | 485  | 14-5  | 2   | 28    | 21    | 4-2    | 2 | 114   | 96    |   |   |   |     |      |
| 8-13  | 2 | 170   | 151   | 11-10 | 2 | 7    | 107  | 3-7   | 2    | 4450 | 4785 | -13-4 | 2   | 19    | 27    | 5-2    | 2 | 4698  | 4639  |   |   |   |     |      |
| 9-13  | 2 | 289   | 235   | 12-10 | 2 | 3    | 8    | 4-7   | 2    | 5667 | 5224 | -12-4 | 2   | 54    | 54    | 6-2    | 2 | 7909  | 6868  |   |   |   |     |      |
| 10-13 | 2 | 15    | 1     | 13-10 | 2 | -2   | 1    | 5-7   | 2    | 839  | 838  | -11-4 | 2   | 74    | 58    | 7-2    | 2 | 82    | 82    |   |   |   |     |      |
| 11-13 | 2 | 54    | 46    | -10-9 | 2 | 49   | 45   | 6-7   | 2    | 606  | 619  | -10-4 | 2   | 255   | 181   | 8-2    | 2 | 823   | 790   |   |   |   |     |      |
| -7-12 | 2 | 3     | 0     | -9-9  | 2 | 43   | 41   | 7-7   | 2    | 2    | 41   | -9-4  | 2   | 53    | 35    | 9-2    | 2 | 1373  | 1105  |   |   |   |     |      |
| -6-12 | 2 | 42    | 54    | -8-9  | 2 | 123  | 109  | 8-7   | 2    | 126  | 113  | -8-4  | 2   | 7     | 1     | 10-2   | 2 | 121   | 142   |   |   |   |     |      |
| -5-12 | 2 | 56    | 39    | -7-9  | 2 | 193  | 181  | 9-7   | 2    | 247  | 212  | -7-4  | 2   | 36    | 25    | 11-2   | 2 | 2     | 0     |   |   |   |     |      |
| -4-12 | 2 | 390   | 373   | -6-9  | 2 | 307  | 258  | 10-7  | 2    | -2   | 3    | -6-4  | 2   | 90    | 81    | 12-2   | 2 | 65    | 49    |   |   |   |     |      |
| -3-12 | 2 | 4     | 0     | -5-9  | 2 | 45   | 22   | 11-7  | 2    | 26   | 16   | -5-4  | 2   | 190   | 156   | 13-2   | 2 | 13    | 1     |   |   |   |     |      |
| -2-12 | 2 | 51    | 44    | -4-9  | 2 | 218  | 127  | 12-7  | 2    | 2    | 1    | -4-4  | 2   | 127   | 174   | -14-1  | 2 | 45    | 35    |   |   |   |     |      |
| -1-12 | 2 | 235   | 242   | -3-9  | 2 | 344  | 333  | 13-7  | 2    | 19   | 13   | -3-4  | 2   | 3021  | 3748  | -13-1  | 2 | 111   | 134   |   |   |   |     |      |
| 0-12  | 2 | 9     | 1     | -2-9  | 2 | 427  | 738  | 14-7  | 2    | 25   | 21   | -2-4  | 2   | 2973  | 2564  | -12-1  | 2 | 6     | 10    |   |   |   |     |      |
| 1-12  | 2 | 620   | 556   | -1-9  | 2 | 476  | 253  | -12-6 | 2    | 8    | 0    | 1-4   | 2   | 2778  | 2543  | -11-1  | 2 | 17    | 19    |   |   |   |     |      |
| 2-12  | 2 | 0     | 14    | 0-9   | 2 | 40   | 30   | -11-6 | 2    | 30   | 19   | 2-4   | 2   | 6928  | 8000  | -10-1  | 2 | 394   | 391   |   |   |   |     |      |
| 3-12  | 2 | 954   | 921   | 1-9   | 2 | 93   | 271  | -10-6 | 2    | 17   | 3    | 3-4   | 2   | 1876  | 1821  | -9-1   | 2 | 501   | 576   |   |   |   |     |      |
| 4-12  | 2 | 705   | 820   | -9-8  | 2 | 600  | 640  | 3-8   | 2    | 71   | 116  | -9-7  | 2   | 72    | 77    | -11-10 | 2 | 27    | 32    |   |   |   |     |      |
| 5-12  | 2 | 472   | 380   | -8-8  | 2 | 885  | 831  | 4-4   | 2    | 320  | 213  | -8-7  | 2   | 846   | 787   | -10-10 | 2 | 42    | 15    |   |   |   |     |      |
| 6-12  | 2 | 2     | 13    | -7-8  | 2 | 3658 | 3753 | 5-4   | 2    | 16   | 28   | -7-7  | 2   | 1118  | 942   | -9-10  | 2 | 66    | 82    |   |   |   |     |      |
| 7-12  | 2 | 53    | 41    | -6-8  | 2 | 536  | 448  | 6-4   | 2    | 63   | 61   | -6-7  | 2   | 498   | 337   | -8-10  | 2 | 676   | 632   |   |   |   |     |      |
| 8-12  | 2 | 2294  | 1939  | -5-8  | 2 | 638  | 743  | 7-4   | 2    | 432  | 364  | -5-7  | 2   | 676   | 643   | -7-10  | 2 | 8     | 21    |   |   |   |     |      |
| 9-12  | 2 | 1     | 87    | -4-8  | 2 | 784  | 1039 | 8-4   | 2    | 13   | 18   | -4-7  | 2   | 4216  | 4139  | -6-10  | 2 | 441   | 323   |   |   |   |     |      |
| 10-12 | 2 | 18470 | 17467 | -3-8  | 2 | 1373 | 1855 | 9-4   | 2    | 288  | 240  | -3-7  | 2   | 5     | 2     | -5-10  | 2 | 94    | 35    |   |   |   |     |      |
| 11-12 | 2 | 6000  | 5861  | -2-8  | 2 | 5446 | 5055 | 10-4  | 2    | 56   | 17   | -2-7  | 2   | 25    | 10    | -4-10  | 2 | 414   | 514   |   |   |   |     |      |
| 12-12 | 2 | 817   | 1015  | 0-8   | 2 | 2337 | 6503 | 11-4  | 2    | 16   | 6    | -1-7  | 2   | 102   | 163   | -3-10  | 2 | 543   | 460   |   |   |   |     |      |
| 13-12 | 2 | 675   | 542   | 1-8   | 2 | 5    | 44   | -15-5 | 2    | 10   | 1    | 0-7   | 2   | -2    | 7     | -2-10  | 2 | 336   | 469   |   |   |   |     |      |
| 14-12 | 2 | 2859  | 2421  | 2-8   | 2 | 775  | 738  | -14-5 | 2    | -2   | 0    | 1-7   | 2   | 134   | 70    | -1-10  | 2 | 42    | 26    |   |   |   |     |      |
| 15-12 | 2 | 574   | 497   | 3-8   | 2 | 974  | 1048 | -13-5 | 2    | 198  | 176  | 2-7   | 2   | 979   | 1223  | 0-10   | 2 | 339   | 393   |   |   |   |     |      |
| 16-12 | 2 | 185   |       |       |   |      |      |       |      |      |      |       |     |       |       |        |   |       |       |   |   |   |     |      |



Table C.3, continued

| M   | K  | L | Obe  | Calc  | M   | K  | L | Obe  | Calc | M   | K  | L | Obe  | Calc | M   | K  | L | Obe  | Calc | M   | K  | L | Obe  | Calc |
|-----|----|---|------|-------|-----|----|---|------|------|-----|----|---|------|------|-----|----|---|------|------|-----|----|---|------|------|
| 3   | -1 | 3 | 1491 | 1353  | -7  | 2  | 3 | 13   | 16   | 4   | 4  | 3 | 31   | 16   | -7  | 7  | 3 | 10   | 2    | -9  | 10 | 3 | 168  | 193  |
| 4   | -1 | 3 | 61   | 62    | -6  | 2  | 3 | 1785 | 1296 | 5   | 4  | 3 | 100  | 121  | -6  | 7  | 3 | 359  | 388  | -8  | 10 | 3 | 62   | 80   |
| 5   | -1 | 3 | 688  | 909   | -5  | 2  | 3 | 3724 | 2868 | 6   | 4  | 3 | 76   | 103  | -5  | 7  | 3 | 1829 | 1531 | -7  | 10 | 3 | 268  | 254  |
| 6   | -1 | 3 | 11   | 31    | -4  | 2  | 3 | 2637 | 2995 | 7   | 4  | 3 | 751  | 723  | -4  | 7  | 3 | 432  | 424  | -6  | 10 | 3 | 67   | 33   |
| 7   | -1 | 3 | 565  | 476   | -3  | 2  | 3 | 4817 | 5630 | 8   | 4  | 3 | 100  | 78   | -3  | 7  | 3 | 4479 | 4043 | -5  | 10 | 3 | 413  | 259  |
| 8   | -1 | 3 | 64   | 40    | -2  | 2  | 3 | 639  | 871  | 9   | 4  | 3 | 56   | 33   | -2  | 7  | 3 | 331  | 174  | -4  | 10 | 3 | 654  | 580  |
| 9   | -1 | 3 | 173  | 157   | -1  | 2  | 3 | 1123 | 872  | 10  | 4  | 3 | 96   | 113  | -1  | 7  | 3 | 11   | 7    | -3  | 10 | 3 | 235  | 198  |
| 10  | -1 | 3 | 3    | 0     | 0   | 2  | 3 | 276  | 297  | 11  | 4  | 3 | 10   | 4    | 0   | 7  | 3 | 36   | 23   | -2  | 10 | 3 | 117  | 107  |
| 11  | -1 | 3 | 51   | 51    | 1   | 2  | 3 | 959  | 1110 | -15 | 5  | 3 | 42   | 59   | 1   | 7  | 3 | 528  | 521  | -1  | 10 | 3 | 125  | 194  |
| 12  | -1 | 3 | 72   | 87    | 2   | 2  | 3 | 767  | 724  | -14 | 5  | 3 | 263  | 238  | 2   | 7  | 3 | 440  | 526  | 0   | 10 | 3 | 110  | 110  |
| 13  | -1 | 3 | 28   | 9     | 3   | 2  | 3 | 641  | 685  | -13 | 5  | 3 | 214  | 193  | 3   | 7  | 3 | 726  | 776  | 1   | 10 | 3 | 67   | 72   |
| -14 | 0  | 3 | -4   | 5     | 4   | 2  | 3 | 488  | 350  | -12 | 5  | 3 | 93   | 74   | 4   | 7  | 3 | 1108 | 1358 | 2   | 10 | 3 | 309  | 309  |
| -13 | 0  | 3 | 171  | 233   | 5   | 2  | 3 | 3828 | 4067 | -11 | 5  | 3 | 2154 | 1892 | 5   | 7  | 3 | 1028 | 1031 | 3   | 10 | 3 | 44   | 44   |
| -12 | 0  | 3 | 338  | 334   | 6   | 2  | 3 | 1    | 8    | -10 | 5  | 3 | 794  | 709  | 6   | 7  | 3 | 17   | 4    | 4   | 10 | 3 | 24   | 24   |
| -11 | 0  | 3 | 12   | 21    | 7   | 2  | 3 | 713  | 885  | -9  | 5  | 3 | 62   | 62   | 7   | 7  | 3 | 22   | 35   | 5   | 10 | 3 | 21   | 20   |
| -10 | 0  | 3 | 103  | 186   | 8   | 2  | 3 | 26   | 10   | -8  | 5  | 3 | 1485 | 1614 | 8   | 7  | 3 | 1    | 6    | 6   | 10 | 3 | 125  | 111  |
| -9  | 0  | 3 | 108  | 149   | 9   | 2  | 3 | 2    | 7    | -7  | 5  | 3 | 353  | 213  | 9   | 7  | 3 | -5   | 3    | -13 | 11 | 3 | 103  | 98   |
| -8  | 0  | 3 | 356  | 346   | 10  | 2  | 3 | 80   | 84   | -6  | 5  | 3 | 1716 | 1416 | -14 | 8  | 3 | 23   | 29   | -12 | 11 | 3 | 6    | 5    |
| -7  | 0  | 3 | 690  | 760   | 11  | 2  | 3 | 1    | 4    | -5  | 5  | 3 | 534  | 390  | -13 | 8  | 3 | 291  | 259  | -11 | 11 | 3 | 15   | 5    |
| -6  | 0  | 3 | 7217 | 6296  | 12  | 2  | 3 | 60   | 67   | -4  | 5  | 3 | 734  | 724  | -12 | 8  | 3 | 101  | 73   | -10 | 11 | 3 | 283  | 259  |
| -5  | 0  | 3 | 52   | 71    | -15 | 3  | 3 | 0    | 2    | -3  | 5  | 3 | 2772 | 2429 | -11 | 8  | 3 | 0    | 1    | -9  | 11 | 3 | 17   | 3    |
| -4  | 0  | 3 | 7057 | 8638  | -14 | 3  | 3 | 113  | 139  | -2  | 5  | 3 | 803  | 920  | -10 | 8  | 3 | 598  | 617  | -8  | 11 | 3 | 21   | 3    |
| -3  | 0  | 3 | 1696 | 2324  | -13 | 3  | 3 | 12   | 16   | -1  | 5  | 3 | 8096 | 7213 | -9  | 8  | 3 | 137  | 238  | -7  | 11 | 3 | 171  | 185  |
| -2  | 0  | 3 | 4    | 15    | -12 | 3  | 3 | 162  | 233  | 0   | 5  | 3 | 114  | 146  | -8  | 8  | 3 | 78   | 162  | -6  | 11 | 3 | 0    | 6    |
| -1  | 0  | 3 | 7    | 4     | -11 | 3  | 3 | 575  | 622  | 1   | 5  | 3 | 2491 | 2383 | -7  | 8  | 3 | 30   | 54   | -5  | 11 | 3 | 111  | 33   |
| 0   | 0  | 3 | 7677 | 6468  | -10 | 3  | 3 | 568  | 567  | 2   | 5  | 3 | 201  | 142  | -6  | 8  | 3 | 40   | 52   | -4  | 11 | 3 | 46   | 57   |
| 1   | 0  | 3 | 81   | 156   | -9  | 3  | 3 | 249  | 313  | 3   | 5  | 3 | 1727 | 1507 | -5  | 8  | 3 | 1615 | 1445 | -3  | 11 | 3 | 38   | 19   |
| 2   | 0  | 3 | 579  | 643   | -8  | 3  | 3 | 1705 | 1328 | 4   | 5  | 3 | 313  | 281  | -4  | 8  | 3 | 56   | 20   | -2  | 11 | 3 | 26   | 46   |
| 3   | 0  | 3 | -2   | 0     | -7  | 3  | 3 | 344  | 333  | 5   | 5  | 3 | 56   | 66   | -3  | 8  | 3 | 1058 | 1025 | -1  | 11 | 3 | 95   | 98   |
| 4   | 0  | 3 | 325  | 332   | -6  | 3  | 3 | 79   | 70   | 6   | 5  | 3 | 660  | 697  | -2  | 8  | 3 | 440  | 449  | 0   | 11 | 3 | 23   | 20   |
| 5   | 0  | 3 | 16   | 19    | -5  | 3  | 3 | 49   | 59   | 7   | 5  | 3 | 21   | 35   | -1  | 8  | 3 | 316  | 296  | 1   | 11 | 3 | 171  | 164  |
| 6   | 0  | 3 | 70   | 72    | -4  | 3  | 3 | 1128 | 1374 | 8   | 5  | 3 | 148  | 148  | 0   | 8  | 3 | 204  | 225  | 2   | 11 | 3 | 87   | 85   |
| 7   | 0  | 3 | 146  | 115   | -3  | 3  | 3 | 1172 | 1149 | 9   | 5  | 3 | 47   | 30   | 1   | 8  | 3 | 280  | 234  | 3   | 11 | 3 | 2    | 3    |
| 8   | 0  | 3 | 11   | 17    | -2  | 3  | 3 | 936  | 722  | 10  | 5  | 3 | 58   | 70   | 2   | 8  | 3 | 181  | 211  | 4   | 11 | 3 | 40   | 35   |
| 9   | 0  | 3 | 48   | 52    | -1  | 3  | 3 | 242  | 191  | -15 | 6  | 3 | 20   | 29   | 3   | 8  | 3 | 6    | 2    | -12 | 12 | 3 | 21   | 33   |
| 10  | 0  | 3 | 3    | 0     | 0   | 3  | 3 | 1071 | 1467 | -14 | 6  | 3 | 106  | 108  | 4   | 8  | 3 | 659  | 627  | -11 | 12 | 3 | 35   | 45   |
| 11  | 0  | 3 | 11   | 1     | 1   | 3  | 3 | 952  | 1159 | -13 | 6  | 3 | 45   | 40   | 5   | 8  | 3 | 28   | 10   | -10 | 12 | 3 | 287  | 266  |
| 12  | 0  | 3 | 358  | 249   | 2   | 3  | 3 | 757  | 858  | -12 | 6  | 3 | 105  | 104  | 6   | 8  | 3 | 9    | 4    | -9  | 12 | 3 | 141  | 134  |
| 13  | 0  | 3 | 40   | 53    | 3   | 3  | 3 | 1462 | 1453 | -11 | 6  | 3 | 212  | 152  | 7   | 8  | 3 | -1   | 0    | -8  | 12 | 3 | 37   | 20   |
| 14  | 0  | 3 | 30   | 47    | 4   | 3  | 3 | 322  | 212  | -10 | 6  | 3 | 142  | 148  | 8   | 8  | 3 | 25   | 18   | -7  | 12 | 3 | 139  | 159  |
| 15  | 0  | 3 | 41   | 46    | 5   | 3  | 3 | 2285 | 2435 | -9  | 6  | 3 | 113  | 102  | -14 | 9  | 3 | 9    | 1    | -6  | 12 | 3 | 8    | 30   |
| 16  | 0  | 3 | 158  | 204   | 6   | 3  | 3 | 100  | 96   | -8  | 6  | 3 | 65   | 83   | -13 | 9  | 3 | 17   | 21   | -5  | 12 | 3 | 125  | 117  |
| 17  | 0  | 3 | 1    | 4     | 7   | 3  | 3 | 12   | 4    | -7  | 6  | 3 | 1176 | 1239 | -12 | 9  | 3 | 3    | 9    | -4  | 12 | 3 | 86   | 84   |
| 18  | 0  | 3 | 1211 | 1114  | 8   | 3  | 3 | 129  | 114  | -6  | 6  | 3 | 461  | 408  | -11 | 9  | 3 | 425  | 386  | -3  | 12 | 3 | 34   | 25   |
| 19  | 0  | 3 | 1556 | 1736  | 9   | 3  | 3 | 47   | 25   | -5  | 6  | 3 | 3991 | 4149 | -10 | 9  | 3 | 318  | 242  | -2  | 12 | 3 | 51   | 35   |
| 20  | 0  | 3 | 1180 | 17290 | 10  | 3  | 3 | 14   | 6    | -4  | 6  | 3 | 8460 | 6948 | -9  | 9  | 3 | 81   | 60   | -1  | 12 | 3 | 55   | 56   |
| 21  | 0  | 3 | 716  | 31517 | 11  | 3  | 3 | 34   | 27   | -3  | 6  | 3 | 2257 | 2023 | -8  | 9  | 3 | 105  | 108  | 0   | 12 | 3 | 420  | 394  |
| 22  | 0  | 3 | 209  | 205   | -15 | 4  | 3 | 23   | 20   | -2  | 6  | 3 | 1282 | 1149 | -7  | 9  | 3 | 155  | 148  | 1   | 12 | 3 | 1    | 1    |
| 23  | 0  | 3 | 787  | 935   | -14 | 4  | 3 | 0    | 10   | -1  | 6  | 3 | 950  | 1265 | -6  | 9  | 3 | 121  | 219  | 2   | 12 | 3 | 17   | 4    |
| 24  | 0  | 3 | 2314 | 2162  | -13 | 4  | 3 | 0    | 0    | 0   | 6  | 3 | 384  | 154  | -5  | 9  | 3 | 1089 | 878  | 3   | 12 | 3 | 15   | 1    |
| 25  | 0  | 3 | 90   | 46    | 0   | 13 | 4 | 519  | 479  | 3   | 10 | 4 | 313  | 291  | -6  | 7  | 4 | 569  | 610  | 7   | -5 | 4 | 166  | 243  |
| 26  | 0  | 3 | 29   | 20    | 1   | 13 | 4 | 102  | 110  | 4   | 10 | 4 | 303  | 273  | -5  | 7  | 4 | 104  | 47   | 8   | -5 | 4 | 179  | 245  |
| 27  | 0  | 3 | 87   | 73    | 2   | 13 | 4 | 902  | 801  | 5   | 10 | 4 | 24   | 72   | -4  | 7  | 4 | 21   | 45   | 9   | -5 | 4 | 147  | 202  |
| 28  | 0  | 3 | 219  | 191   | 3   | 13 | 4 | 456  | 242  | 6   | 10 | 4 | 59   | 82   | -3  | 7  | 4 | 42   | 67   | 10  | -5 | 4 | 358  | 300  |
| 29  | 0  | 3 | 27   | 36    | 4   | 13 | 4 | -4   | 3    | 7   | 10 | 4 | 784  | 652  | -2  | 7  | 4 | 6    | 9    | 11  | -5 | 4 | 198  | 236  |
| 30  | 0  | 3 | 159  | 161   | 5   | 13 | 4 | 8    | 25   | 8   | 10 | 4 | 24   | 6    | -1  | 7  | 4 | 2790 | 2967 | 12  | -5 | 4 | 124  | 89   |
| 31  | 0  | 3 | 14   | 22    | 6   | 13 | 4 | 56   | 69   | 9   | 10 | 4 | 145  | 129  | 0   | 7  | 4 | 3224 | 2574 | 13  | -5 | 4 | 96   | 94   |
| 32  | 0  | 3 | 10   | 7     | 7   | 13 | 4 | 77   | 52   | 10  | 10 | 4 | 21   | 38   | 1   | 7  | 4 | 3320 | 2547 | -13 | -4 | 4 | 137  | 137  |
| 33  | 0  | 3 | 5    | 1     | 8   | 13 | 4 | 82   | 78   | 11  | 10 | 4 | 64   | 60   | 2   | 7  | 4 | 125  | 120  | -12 | -4 | 4 | 217  | 257  |
| 34  | 0  | 3 | 86   | 56    | 9   | 13 | 4 | 145  | 174  | 12  | 10 | 4 | 46   | 50   | 3   | 7  | 4 | 40   | 29   | -11 | -4 | 4 | 198  | 167  |
| 35  | 0  | 3 | 2    | 5     | 10  | 13 | 4 | 90   | 114  | 13  | 10 | 4 | 2    | 6    | 2   | 10 | 4 | 1    | 2    | -10 | -4 | 4 | 70   | 81   |
| 36  | 0  | 3 | 7    | 7     | 11  | 13 | 4 | 30   | 19   | -10 | 9  | 4 | 89   | 95   | 5   | 7  | 4 | 1078 | 835  | -9  | -4 | 4 | 69   | 45   |
| 37  | 0  | 3 | 100  | 77    | -7  | 12 | 4 | 73   | 62   | -9  | 9  | 4 | 35   | 39   | 6   | 7  | 4 | 188  | 76   | -8  | -4 | 4 | 492  | 801  |
| 38  | 0  | 3 | 15   | 6     | -6  | 12 | 4 | 102  | 129  | -8  | 9  | 4 | 110  | 83   | 7   | 7  | 4 | 445  | 487  | -7  | -4 | 4 | 10   | 3    |
| 39  | 0  | 3 | 2    | 2     | -5  | 12 | 4 | 93   | 109  | -7  | 9  | 4 | 11   | 1    | 8   | 7  | 4 | 327  | 365  | -6  | -4 | 4 | 340  | 418  |
| 40  | 0  | 3 | 110  | 108   | -4  | 12 | 4 | 3    | 13   | -6  | 9  | 4 | 69   | 87   | 9   | 7  | 4 | 11   | 20   | -5  | -4 | 4 | 1214 | 1178 |
| 41  | 0  | 3 | 23   | 21    | -3  | 12 | 4 | 259  | 206  | -5  | 9  | 4 | 15   | 7    | 10  | 7  | 4 | -1   | 3    | -4  | -4 | 4 | 975  | 1014 |
| 42  | 0  | 3 | 49   | 26    | -2  | 12 | 4 | 252  | 161  | -4  | 9  | 4 | 22   | 53   | 11  | 7  | 4 | 6    | 2    | -3  | -4 | 4 | 1939 | 1706 |
| 43  | 0  | 3 | 63   | 45    | -1  | 12 | 4 | 12   | 19   | -3  | 9  | 4 | 952  | 611  | 12  | 7  | 4 | 23   | 25   | -2  | -4 | 4 | 160  | 187  |
| 44  | 0  | 3 | 200  | 199   | 0   | 12 | 4 | 486  | 506  | -2  | 9  | 4 | 7231 | 6636 | 13  | 7  | 4 | 54   | 61   | 1   | -4 | 4 | 1775 | 1589 |
| 45  | 0  | 3 |      |       |     |    |   |      |      |     |    |   |      |      |     |    |   |      |      |     |    |   |      |      |

Table C.3, continued

| M     | K | L    | Obe  | Calc  | M | K    | L    | Obe   | Calc | M    | K    | L     | Obe | Calc | M    | K      | L | Obe  | Calc | M | K | L | Obe | Calc |
|-------|---|------|------|-------|---|------|------|-------|------|------|------|-------|-----|------|------|--------|---|------|------|---|---|---|-----|------|
| 4-14  | 4 | 17   | 2    | 12-11 | 4 | 82   | 55   | 7-8   | 4    | 1227 | 920  | -6-5  | 4   | 134  | 141  | 11-3   | 4 | 21   | 35   |   |   |   |     |      |
| 5-14  | 4 | 526  | 492  | -9-10 | 4 | -6   | 0    | 8-8   | 4    | 24   | 9    | -5-5  | 4   | 3    | 8    | 12-3   | 4 | 240  | 222  |   |   |   |     |      |
| 6-14  | 4 | 46   | 35   | -9-10 | 4 | 123  | 126  | 9-8   | 4    | 412  | 289  | -4-5  | 4   | 620  | 802  | 13-3   | 4 | 3    | 5    |   |   |   |     |      |
| 7-14  | 4 | 131  | 137  | -7-10 | 4 | 18   | 41   | 10-8  | 4    | -1   | 1    | -3-5  | 4   | 0    | 15   | -14-2  | 4 | 2    | 4    |   |   |   |     |      |
| 8-14  | 4 | 25   | 51   | -6-10 | 4 | 49   | 47   | 11-8  | 4    | 33   | 43   | -2-5  | 4   | 4905 | 4473 | -13-2  | 4 | 104  | 123  |   |   |   |     |      |
| 9-14  | 4 | 99   | 84   | -5-10 | 4 | 21   | 8    | 12-8  | 4    | 41   | 56   | -1-5  | 4   | 604  | 669  | -12-2  | 4 | 96   | 70   |   |   |   |     |      |
| 10-14 | 4 | 32   | 29   | -4-10 | 4 | 544  | 454  | 13-8  | 4    | 14   | 6    | 0-5   | 4   | 495  | 464  | -11-2  | 4 | 23   | 13   |   |   |   |     |      |
| -6-13 | 4 | -3   | 0    | -3-10 | 4 | 17   | 6    | -12-7 | 4    | 13   | 35   | 1-5   | 4   | 2122 | 2093 | -10-2  | 4 | 652  | 556  |   |   |   |     |      |
| -5-13 | 4 | 163  | 175  | -2-10 | 4 | 1264 | 1149 | -11-7 | 4    | 22   | 3    | 2-5   | 4   | 1546 | 1473 | -9-2   | 4 | 582  | 505  |   |   |   |     |      |
| -4-13 | 4 | 13   | 5    | -1-10 | 4 | 9    | 5    | -10-7 | 4    | 332  | 339  | 3-5   | 4   | 147  | 64   | -8-2   | 4 | 546  | 621  |   |   |   |     |      |
| -3-13 | 4 | 12   | 4    | 0-10  | 4 | 1513 | 1453 | -9-7  | 4    | 87   | 96   | 4-5   | 4   | 1635 | 1452 | -7-2   | 4 | 304  | 272  |   |   |   |     |      |
| -2-13 | 4 | 82   | 113  | 1-10  | 4 | 474  | 469  | -8-7  | 4    | 42   | 113  | 5-5   | 4   | 5561 | 4704 | -6-2   | 4 | 2750 | 2698 |   |   |   |     |      |
| -1-13 | 4 | 140  | 70   | 2-10  | 4 | 246  | 213  | -7-7  | 4    | 18   | 28   | 6-5   | 4   | 157  | 134  | -5-2   | 4 | 4394 | 5084 |   |   |   |     |      |
| -4-2  | 4 | 7893 | 7173 | -15-1 | 4 | 21   | 23   | -4-3  | 4    | 393  | 814  | 9-5   | 4   | 10   | 14   | 3-8    | 4 | 226  | 166  |   |   |   |     |      |
| -3-2  | 4 | 3818 | 4844 | -14-1 | 4 | 209  | 219  | -3-3  | 4    | 2024 | 2384 | -15-6 | 4   | 11   | 7    | 4-8    | 4 | 67   | 86   |   |   |   |     |      |
| -2-2  | 4 | 6102 | 6787 | -13-1 | 4 | 40   | 36   | -2-3  | 4    | 148  | 123  | -14-6 | 4   | 2    | 1    | 5-8    | 4 | 26   | 22   |   |   |   |     |      |
| -1-2  | 4 | 954  | 1126 | -12-1 | 4 | 1354 | 1183 | -1-3  | 4    | 142  | 234  | -13-6 | 4   | 40   | 54   | 6-8    | 4 | -3   | 3    |   |   |   |     |      |
| 2-2   | 4 | 4155 | 4004 | -11-1 | 4 | 814  | 653  | 0-3   | 4    | 353  | 341  | -12-6 | 4   | 122  | 125  | 7-8    | 4 | 80   | 101  |   |   |   |     |      |
| 3-2   | 4 | 137  | 104  | -10-1 | 4 | 352  | 262  | 1-3   | 4    | 80   | 20   | -11-6 | 4   | 150  | 144  | -14-9  | 4 | -4   | 12   |   |   |   |     |      |
| 4-2   | 4 | 528  | 564  | -9-1  | 4 | 2368 | 2597 | 2-3   | 4    | 4444 | 4305 | -10-6 | 4   | 267  | 311  | -13-9  | 4 | 45   | 50   |   |   |   |     |      |
| 5-2   | 4 | 3061 | 2850 | -8-1  | 4 | 104  | 57   | 3-3   | 4    | 1373 | 1318 | -9-6  | 4   | 841  | 972  | -12-9  | 4 | 30   | 32   |   |   |   |     |      |
| 6-2   | 4 | 108  | 64   | -7-1  | 4 | 210  | 153  | 4-3   | 4    | 1049 | 1768 | -8-6  | 4   | 316  | 262  | -11-9  | 4 | 703  | 669  |   |   |   |     |      |
| 7-2   | 4 | 469  | 388  | -6-1  | 4 | 46   | 50   | 5-3   | 4    | 213  | 163  | -7-6  | 4   | 849  | 938  | -10-9  | 4 | 0    | 7    |   |   |   |     |      |
| 8-2   | 4 | 210  | 189  | -5-1  | 4 | 8216 | 7634 | 6-3   | 4    | 685  | 676  | -6-6  | 4   | 373  | 437  | -9-9   | 4 | 207  | 142  |   |   |   |     |      |
| 9-2   | 4 | 5    | 15   | -4-1  | 4 | 52   | 81   | 7-3   | 4    | 16   | 50   | -5-6  | 4   | 1451 | 935  | -8-9   | 4 | 163  | 194  |   |   |   |     |      |
| 10-2  | 4 | 55   | 74   | -3-1  | 4 | 984  | 806  | 8-3   | 4    | 0    | 3    | -4-6  | 4   | 1784 | 1938 | -7-9   | 4 | 200  | 225  |   |   |   |     |      |
| 11-2  | 4 | -1   | 2    | -2-1  | 4 | 1110 | 1240 | 9-3   | 4    | 34   | 34   | -3-6  | 4   | 1373 | 1385 | -6-9   | 4 | 345  | 407  |   |   |   |     |      |
| 12-2  | 4 | -6   | 2    | -1-1  | 4 | 6643 | 8068 | 10-3  | 4    | 5    | 0    | -2-6  | 4   | 544  | 531  | -5-9   | 4 | 18   | 7    |   |   |   |     |      |
| 13-2  | 4 | 5    | 0    | 0-1   | 4 | 610  | 684  | 11-3  | 4    | 9    | 1    | -1-6  | 4   | 469  | 494  | -4-9   | 4 | 685  | 556  |   |   |   |     |      |
| -14-1 | 4 | 93   | 93   | 1-1   | 4 | 1237 | 1081 | -15-4 | 4    | 51   | 33   | 0-6   | 4   | 137  | 134  | -3-9   | 4 | 14   | 1    |   |   |   |     |      |
| -13-1 | 4 | 128  | 166  | 2-1   | 4 | 879  | 882  | -14-4 | 4    | 19   | 34   | 1-6   | 4   | 64   | 36   | -2-9   | 4 | 0    | 2    |   |   |   |     |      |
| -12-1 | 4 | 706  | 681  | 3-1   | 4 | 4526 | 4757 | -13-4 | 4    | 29   | 19   | 2-6   | 4   | 166  | 288  | -1-9   | 4 | 279  | 260  |   |   |   |     |      |
| -11-1 | 4 | 425  | 541  | 4-1   | 4 | 746  | 616  | -12-4 | 4    | 190  | 176  | 3-6   | 4   | 310  | 226  | 0-9    | 4 | 20   | 23   |   |   |   |     |      |
| -10-1 | 4 | 778  | 736  | 5-1   | 4 | 83   | 63   | -11-4 | 4    | 701  | 629  | 4-6   | 4   | 65   | 79   | 1-9    | 4 | 31   | 7    |   |   |   |     |      |
| -9-1  | 4 | 13   | 23   | 6-1   | 4 | 447  | 347  | -10-4 | 4    | 82   | 79   | 5-6   | 4   | 349  | 335  | 2-9    | 4 | 29   | 49   |   |   |   |     |      |
| -8-1  | 4 | 828  | 800  | 7-1   | 4 | 278  | 332  | -9-4  | 4    | 1070 | 976  | 6-6   | 4   | 386  | 384  | 3-9    | 4 | 81   | 108  |   |   |   |     |      |
| -7-1  | 4 | 33   | 512  | 8-1   | 4 | 618  | 611  | -8-4  | 4    | 572  | 557  | 7-6   | 4   | 154  | 151  | 4-9    | 4 | 51   | 48   |   |   |   |     |      |
| -6-1  | 4 | 0    | 9    | 9-1   | 4 | 22   | 19   | -7-4  | 4    | 238  | 102  | 8-6   | 4   | 0    | 3    | 6-9    | 4 | 0    | 1    |   |   |   |     |      |
| -5-1  | 4 | 585  | 868  | 10-1  | 4 | 20   | 35   | -6-4  | 4    | 54   | 92   | 9-6   | 4   | 0    | 6    | -13-10 | 4 | 63   | 76   |   |   |   |     |      |
| -4-1  | 4 | 4563 | 3960 | 11-1  | 4 | 56   | 53   | -5-4  | 4    | 1003 | 1156 | -14-7 | 4   | 6    | 116  | -12-10 | 4 | 3    | 7    |   |   |   |     |      |
| -3-1  | 4 | 1041 | 1320 | 12-1  | 4 | 0    | 13   | -4-4  | 4    | 1311 | 1367 | -13-7 | 4   | 130  | 13   | -11-10 | 4 | 142  | 171  |   |   |   |     |      |
| -2-1  | 4 | 2142 | 2235 | -15-2 | 4 | 45   | 43   | -3-4  | 4    | 307  | 257  | -12-7 | 4   | 13   | 75   | -10-10 | 4 | 5    | 14   |   |   |   |     |      |
| -1-1  | 4 | 1075 | 1019 | -14-2 | 4 | 27   | 31   | -2-4  | 4    | 876  | 757  | -11-7 | 4   | 129  | 33   | -9-10  | 4 | 185  | 177  |   |   |   |     |      |
| 2-1   | 4 | 1731 | 1951 | -13-2 | 4 | 430  | 348  | -1-4  | 4    | 1781 | 1664 | -10-7 | 4   | 33   | 6    | -8-10  | 4 | 319  | 311  |   |   |   |     |      |
| 3-1   | 4 | 6517 | 6378 | -12-2 | 4 | 341  | 337  | 0-4   | 4    | 6271 | 6242 | -9-7  | 4   | 13   | 220  | -7-10  | 4 | 15   | 3    |   |   |   |     |      |
| 4-1   | 4 | 75   | 76   | -11-2 | 4 | 177  | 190  | 1-4   | 4    | 7790 | 7333 | -8-7  | 4   | 362  | 185  | -6-10  | 4 | 144  | 182  |   |   |   |     |      |
| 5-1   | 4 | 5    | 12   | -10-2 | 4 | 14   | 21   | 2-4   | 4    | 813  | 727  | -7-7  | 4   | -4   | 2    | -5-10  | 4 | 87   | 21   |   |   |   |     |      |
| 6-1   | 4 | 78   | 80   | -9-2  | 4 | 489  | 633  | 3-4   | 4    | 1767 | 1665 | -5-7  | 4   | -6   | 12   | -4-10  | 4 | 5    | 6    |   |   |   |     |      |
| 7-1   | 4 | 0    | 0    | -8-2  | 4 | 401  | 5817 | 5-4   | 4    | 32   | 6    | -4-7  | 4   | 103  | 73   | -3-10  | 4 | 30   | 0    |   |   |   |     |      |
| 8-1   | 4 | 685  | 639  | -7-2  | 4 | 5533 | 477  | 6-4   | 4    | 355  | 296  | -2-7  | 4   | 986  | 739  | -1-10  | 4 | 401  | 341  |   |   |   |     |      |
| 9-1   | 4 | 143  | 95   | -6-2  | 4 | 657  | 3200 | 7-4   | 4    | 85   | 107  | -1-7  | 4   | 2    | 22   | 0-10   | 4 | 528  | 488  |   |   |   |     |      |
| 10-1  | 4 | 86   | 93   | -5-2  | 4 | 3602 | 3691 | 8-4   | 4    | 0    | 3    | 0-7   | 4   | 559  | 548  | 1-10   | 4 | 175  | 166  |   |   |   |     |      |
| 11-1  | 4 | 18   | 15   | -4-2  | 4 | 3336 | 83   | 9-4   | 4    | 19   | 21   | 1-7   | 4   | 81   | 55   | 2-10   | 4 | 187  | 176  |   |   |   |     |      |
| 12-1  | 4 | 334  | 411  | -3-2  | 4 | 70   | 640  | 10-4  | 4    | 19   | 42   | 2-7   | 4   | 622  | 540  | 3-10   | 4 | 156  | 137  |   |   |   |     |      |
| -14-0 | 4 | 5    | 8    | -1-2  | 4 | 559  | 1882 | -15-5 | 4    | 102  | 42   | -14-5 | 4   | 10   | 33   | 4-10   | 4 | 60   | 40   |   |   |   |     |      |
| -13-0 | 4 | 38   | 48   | -1-2  | 4 | 1598 | 42   | -14-5 | 4    | 102  | 42   | -14-5 | 4   | 10   | 33   | 4-10   | 4 | 60   | 40   |   |   |   |     |      |
| -12-0 | 4 | 230  | 177  | 0-2   | 4 | 27   | 5388 | -13-5 | 4    | 102  | 108  | 4-7   | 4   | 149  | 117  | 5-10   | 4 | 5    | 0    |   |   |   |     |      |
| -11-0 | 4 | 99   | 101  | 1-2   | 4 | 4928 | 5388 | -13-5 | 4    | 102  | 67   | 5-7   | 4   | 102  | 169  | -12-11 | 4 | 19   | 8    |   |   |   |     |      |
| -10-0 | 4 | 967  | 1072 | 2-2   | 4 | 113  | 170  | -12-5 | 4    | 50   | 832  | 6-7   | 4   | 26   | 35   | -11-11 | 4 | 382  | 367  |   |   |   |     |      |
| -9-0  | 4 | 592  | 498  | 3-2   | 4 | 1421 | 1476 | -11-5 | 4    | 848  | 19   | 7-7   | 4   | 37   | 44   | -10-11 | 4 | 152  | 98   |   |   |   |     |      |
| -8-0  | 4 | 195  | 196  | 4-2   | 4 | 1376 | 1465 | -10-5 | 4    | 55   | 188  | 8-7   | 4   | 8    | 8    | -9-11  | 4 | 55   | 32   |   |   |   |     |      |
| -7-0  | 4 | 2532 | 2461 | 5-2   | 4 | 171  | 246  | -9-5  | 4    | 258  | 185  | -14-8 | 4   | 1    | 195  | -7-11  | 4 | 64   | 54   |   |   |   |     |      |
| -6-0  | 4 | 682  | 1016 | 6-2   | 4 | 787  | 885  | -8-5  | 4    | 255  | 30   | -13-8 | 4   | 405  | 388  | -6-11  | 4 | 133  | 92   |   |   |   |     |      |
| -5-0  | 4 | 785  | 767  | 7-2   | 4 | 0    | 2    | -7-5  | 4    | 30   | 2319 | -11-8 | 4   | 42   | 24   | -5-11  | 4 | 51   | 18   |   |   |   |     |      |
| -4-0  | 4 | 9246 | 9191 | 8-2   | 4 | 506  | 591  | -6-5  | 4    | 25   | 242  | -10-8 | 4   | 112  | 160  | -4-11  | 4 | 61   | 52   |   |   |   |     |      |
| -3-0  | 4 | 1953 | 1983 | 9-2   | 4 | 1    | 6    | -5-5  | 4    | 1926 | 5319 | -9-8  | 4   | 96   | 131  | -3-11  | 4 | 2    | 1    |   |   |   |     |      |
| -2-0  | 4 | 6498 | 7982 | 10-2  | 4 | 3    | 7    | -4-5  | 4    | 4645 | 711  | -8-8  | 4   | 171  | 166  | -2-11  | 4 | 96   | 97   |   |   |   |     |      |
| -1-0  | 4 | 2692 | 2801 | 11-2  | 4 | 45   | 8    | -3-5  | 4    | 4645 | 1638 | -7-8  | 4   | 538  | 318  | -1-11  | 4 | 104  | 114  |   |   |   |     |      |
| 0-0   | 4 | 823  | 1032 | -15-3 | 4 | -6   | 354  | -1-5  | 4    | 1725 | 477  | -6-8  | 4   | 122  | 180  | 0-11   | 4 | 38   | 18   |   |   |   |     |      |
| 1-0   | 4 | 4763 | 4404 | -14-3 | 4 | 429  | 10   | 0-5   | 4    | 695  | 5    | -5-8  | 4   | 149  | 114  | 1-11   | 4 | 31   | 29   |   |   |   |     |      |
| 2-0   | 4 |      |      |       |   |      |      |       |      |      |      |       |     |      |      |        |   |      |      |   |   |   |     |      |

Table C.3, continued

| M      | K | L    | Obs  | Calc  | M | K     | L     | Obs   | Calc | M    | K    | L     | Obs | Calc | M    | K     | L | Obs   | Calc  |
|--------|---|------|------|-------|---|-------|-------|-------|------|------|------|-------|-----|------|------|-------|---|-------|-------|
| 2-17   | 5 | 10   | 12   | -6-12 | 5 | 22    | 2     | -8-9  | 5    | 43   | 32   | 8-7   | 5   | 56   | 7    | -6-4  | 5 | 1112  | 1032  |
| 3-17   | 5 | 51   | 53   | -8-12 | 5 | 105   | 111   | -7-9  | 5    | 30   | 64   | 9-7   | 5   | 396  | 390  | -5-4  | 5 | 3950  | 3351  |
| 4-17   | 5 | 48   | 50   | -4-12 | 5 | 178   | 232   | -6-9  | 5    | 8    | 24   | 10-7  | 5   | 469  | 416  | -4-4  | 5 | 70    | 120   |
| 5-17   | 5 | 38   | 21   | -3-12 | 5 | 279   | 269   | -5-9  | 5    | 548  | 609  | 11-7  | 5   | 109  | 93   | -3-4  | 5 | 7905  | 7530  |
| -2-16  | 5 | 52   | 22   | -2-12 | 5 | 1161  | 1276  | -4-9  | 5    | 20   | 34   | 12-7  | 5   | 333  | 488  | -2-4  | 5 | 2633  | 3004  |
| -1-16  | 5 | 9    | 0    | -1-12 | 5 | 299   | 230   | -3-9  | 5    | 3250 | 3228 | 13-7  | 5   | 46   | 51   | -1-4  | 5 | 78    | 60    |
| 0-16   | 5 | 62   | 84   | 0-12  | 5 | 16    | 6     | -2-9  | 5    | 446  | 338  | -12-6 | 5   | 18   | 5    | 0-4   | 5 | 218   | 277   |
| 1-16   | 5 | 135  | 121  | 1-12  | 5 | 197   | 154   | -1-9  | 5    | 617  | 914  | -11-6 | 5   | 246  | 217  | 1-4   | 5 | 424   | 294   |
| 2-16   | 5 | 68   | 70   | 2-12  | 5 | 129   | 74    | 0-9   | 5    | 28   | 66   | -10-6 | 5   | 333  | 216  | 2-4   | 5 | 10    | 15    |
| 3-16   | 5 | 29   | 37   | 3-12  | 5 | 20    | 32    | 1-9   | 5    | 439  | 586  | -9-6  | 5   | 211  | 298  | 3-4   | 5 | 1906  | 2152  |
| 4-16   | 5 | 15   | 31   | 4-12  | 5 | 178   | 182   | 2-9   | 5    | 503  | 756  | -8-6  | 5   | 318  | 173  | 4-4   | 5 | 136   | 267   |
| 5-16   | 5 | 193  | 150  | 5-12  | 5 | 35    | 52    | 3-9   | 5    | 591  | 484  | -7-6  | 5   | 23   | 58   | 5-4   | 5 | 65    | 87    |
| 6-16   | 5 | 7    | 2    | 6-12  | 5 | 40    | 55    | 4-9   | 5    | 369  | 337  | -6-6  | 5   | 57   | 90   | 6-4   | 5 | 919   | 972   |
| 7-16   | 5 | -4   | 14   | 7-12  | 5 | 529   | 431   | 5-9   | 5    | 533  | 307  | -5-6  | 5   | 3    | 4    | 7-4   | 5 | 3     | 17    |
| 8-16   | 5 | 26   | 9    | 8-12  | 5 | 188   | 208   | 6-9   | 5    | 71   | 149  | -4-6  | 5   | 908  | 478  | 8-4   | 5 | 144   | 173   |
| -4-15  | 5 | 59   | 42   | 9-12  | 5 | 423   | 397   | 7-9   | 5    | 233  | 218  | -3-6  | 5   | 96   | 93   | 9-4   | 5 | 143   | 135   |
| -3-15  | 5 | 85   | 75   | 10-12 | 5 | 1     | 16    | 8-9   | 5    | 256  | 236  | -2-6  | 5   | 8729 | 7804 | 10-4  | 5 | 4     | 1     |
| -2-15  | 5 | 89   | 78   | 11-12 | 5 | 11    | 6     | 9-9   | 5    | -1   | 5    | -1-6  | 5   | 998  | 927  | 11-4  | 5 | 103   | 96    |
| -1-15  | 5 | -5   | 12   | -9-11 | 5 | 1     | 2     | 10-9  | 5    | 242  | 193  | 0-6   | 5   | 2609 | 2974 | 12-4  | 5 | 7     | 0     |
| 0-15   | 5 | 8    | 2    | -8-11 | 5 | -3    | 4     | 11-9  | 5    | 21   | 7    | 1-6   | 5   | 770  | 674  | -14-3 | 5 | 19    | 13    |
| 1-15   | 5 | 35   | 18   | -7-11 | 5 | 15    | 18    | 12-9  | 5    | 10   | 2    | 2-6   | 5   | 1906 | 2111 | -13-3 | 5 | 160   | 202   |
| 2-15   | 5 | 43   | 46   | -6-11 | 5 | 496   | 430   | -11-8 | 5    | 7    | 3    | 3-6   | 5   | 72   | 91   | -12-3 | 5 | 698   | 558   |
| 3-15   | 5 | 812  | 676  | -5-11 | 5 | 597   | 633   | -10-8 | 5    | 5    | 1    | 4-6   | 5   | 783  | 715  | -11-3 | 5 | 116   | 97    |
| 4-15   | 5 | 7    | 6    | -4-11 | 5 | 54    | 38    | -9-8  | 5    | 341  | 301  | 5-6   | 5   | 627  | 489  | -10-3 | 5 | 461   | 402   |
| 5-15   | 5 | 7    | 6    | -3-11 | 5 | 684   | 775   | -8-8  | 5    | 125  | 91   | 6-6   | 5   | 441  | 380  | -9-3  | 5 | 401   | 250   |
| 6-15   | 5 | 37   | 21   | -2-11 | 5 | 476   | 352   | -7-8  | 5    | 119  | 76   | 7-6   | 5   | 21   | 24   | -8-3  | 5 | 55    | 34    |
| 7-15   | 5 | -8   | 9    | -1-11 | 5 | 834   | 841   | -6-8  | 5    | 341  | 301  | 8-6   | 5   | 1351 | 1140 | -7-3  | 5 | 1536  | 1406  |
| 8-15   | 5 | 15   | 2    | 0-11  | 5 | 143   | 218   | -5-8  | 5    | 465  | 424  | 9-6   | 5   | 0    | 0    | -6-3  | 5 | 79    | 60    |
| 9-15   | 5 | -4   | 1    | 1-11  | 5 | 238   | 305   | -4-8  | 5    | 0    | 1    | 10-6  | 5   | 25   | 2    | -5-3  | 5 | 287   | 152   |
| -5-14  | 5 | 12   | 0    | 2-11  | 5 | 431   | 334   | -3-8  | 5    | -3   | 23   | 11-6  | 5   | 165  | 155  | -4-3  | 5 | 2518  | 2633  |
| -4-14  | 5 | 179  | 188  | 3-11  | 5 | 802   | 922   | -2-8  | 5    | 1027 | 1032 | 12-6  | 5   | 16   | 25   | -3-3  | 5 | 1119  | 916   |
| -3-14  | 5 | 145  | 172  | 4-11  | 5 | 119   | 158   | -1-8  | 5    | 476  | 652  | 13-6  | 5   | 8    | 4    | -2-3  | 5 | 18011 | 17039 |
| -2-14  | 5 | 274  | 295  | 5-11  | 5 | 80    | 99    | 0-8   | 5    | -2   | 2    | -13-5 | 5   | 83   | 83   | -1-3  | 5 | 5169  | 5629  |
| -1-14  | 5 | 46   | 43   | 6-11  | 5 | 1     | 12    | 1-8   | 5    | 163  | 177  | -12-5 | 5   | 59   | 37   | 0-3   | 5 | 6506  | 7220  |
| 0-14   | 5 | 12   | 2    | 7-11  | 5 | 68    | 35    | 2-8   | 5    | 161  | 250  | -11-5 | 5   | 319  | 344  | 1-3   | 5 | 2508  | 1808  |
| 1-14   | 5 | 325  | 310  | 8-11  | 5 | 37    | 39    | 3-8   | 5    | 4706 | 4151 | -10-5 | 5   | 267  | 285  | -9-3  | 5 | 4258  | 4608  |
| 2-14   | 5 | 19   | 12   | 9-11  | 5 | 0     | 28    | 4-8   | 5    | 2    | 35   | -9-5  | 5   | 497  | 479  | 3-3   | 5 | 1234  | 1384  |
| 3-14   | 5 | 69   | 63   | 10-11 | 5 | 85    | 60    | 5-8   | 5    | 816  | 826  | -8-5  | 5   | 79   | 122  | 4-3   | 5 | 407   | 368   |
| 4-14   | 5 | 84   | 58   | 11-11 | 5 | 9     | 18    | 6-8   | 5    | 783  | 782  | -7-5  | 5   | 1349 | 1301 | 5-3   | 5 | 72    | 77    |
| 5-14   | 5 | 57   | 69   | 12-11 | 5 | 21    | 5     | 7-8   | 5    | 2    | 21   | -6-5  | 5   | 294  | 145  | 6-3   | 5 | 37    | 42    |
| 6-14   | 5 | 32   | 60   | -9-0  | 5 | 305   | 358   | 3-2   | 5    | 2188 | 2206 | -9-5  | 5   | 13   | 22   | -13-8 | 5 | 0     | 1     |
| 7-14   | 5 | 119  | 111  | -8-0  | 5 | 52    | 85    | 4-2   | 5    | 161  | 170  | -8-5  | 5   | 1415 | 1400 | -12-8 | 5 | 643   | 510   |
| 8-14   | 5 | 16   | 7    | -7-0  | 5 | 51    | 68    | 5-2   | 5    | 27   | 31   | -7-5  | 5   | 45   | 13   | -11-8 | 5 | 329   | 314   |
| 10-13  | 5 | 9    | 10   | -6-0  | 5 | 11818 | 12355 | 6-2   | 5    | 203  | 260  | -6-5  | 5   | 1069 | 930  | -10-8 | 5 | 128   | 145   |
| 11-13  | 5 | 24   | 18   | -5-0  | 5 | 4180  | 5101  | 7-2   | 5    | 721  | 597  | -5-5  | 5   | 1325 | 1327 | -9-8  | 5 | 98    | 79    |
| 12-13  | 5 | 20   | 14   | -4-0  | 5 | 1     | 25    | 8-2   | 5    | 0    | 1    | -4-5  | 5   | 3    | 91   | -8-8  | 5 | 161   | 167   |
| -14-12 | 5 | 23   | 25   | -3-0  | 5 | 1356  | 1878  | 9-2   | 5    | 74   | 59   | 3-5   | 5   | 547  | 848  | -7-7  | 5 | 157   | 59    |
| -13-12 | 5 | 376  | 361  | -2-0  | 5 | 53    | 19    | 10-2  | 5    | 3    | 1    | -2-5  | 5   | 119  | 75   | -6-8  | 5 | 643   | 414   |
| -12-12 | 5 | 774  | 710  | -1-0  | 5 | 702   | 620   | 11-2  | 5    | 16   | 19   | -1-5  | 5   | 5    | 16   | -5-8  | 5 | 1478  | 1279  |
| -11-12 | 5 | 224  | 258  | 0-0   | 5 | 115   | 88    | -15-3 | 5    | 64   | 60   | 0-5   | 5   | 939  | 996  | -4-8  | 5 | 270   | 211   |
| -10-12 | 5 | 88   | 60   | 1-0   | 5 | 2293  | 2558  | -14-3 | 5    | 95   | 69   | 1-5   | 5   | 235  | 304  | -3-8  | 5 | 18    | 35    |
| -9-12  | 5 | 140  | 224  | 2-0   | 5 | 2097  | 2085  | -13-3 | 5    | 690  | 614  | 2-5   | 5   | 45   | 87   | -2-8  | 5 | 291   | 285   |
| -8-12  | 5 | 300  | 262  | 3-0   | 5 | 2323  | 1966  | -12-3 | 5    | 22   | 25   | 3-5   | 5   | 305  | 277  | -1-8  | 5 | 31    | 38    |
| -7-12  | 5 | 1162 | 1234 | 4-0   | 5 | 2998  | 3004  | -11-3 | 5    | 273  | 362  | 4-5   | 5   | 106  | 106  | 0-8   | 5 | 66    | 98    |
| -6-12  | 5 | 3397 | 3506 | 5-0   | 5 | 92    | 84    | -10-3 | 5    | 527  | 483  | 5-5   | 5   | 23   | 36   | 1-8   | 5 | 5     | 3     |
| -5-12  | 5 | 5793 | 5760 | 6-0   | 5 | 447   | 455   | -9-3  | 5    | 257  | 200  | 6-5   | 5   | 248  | 224  | 2-8   | 5 | 202   | 236   |
| -4-12  | 5 | 84   | 38   | 7-0   | 5 | 0     | 11    | -8-3  | 5    | 3    | 27   | 7-5   | 5   | 26   | 34   | 3-8   | 5 | 3     | 7     |
| -3-12  | 5 | 143  | 176  | 8-0   | 5 | 41    | 31    | -7-3  | 5    | 164  | 199  | 8-5   | 5   | 9    | 4    | 4-8   | 5 | 85    | 71    |
| -2-12  | 5 | 790  | 1172 | 9-0   | 5 | 156   | 94    | -6-3  | 5    | 2955 | 2869 | 9-5   | 5   | 104  | 81   | 5-8   | 5 | 140   | 165   |
| -1-12  | 5 | 4    | 7    | 10-0  | 5 | 75    | 87    | -5-3  | 5    | 2254 | 2158 | -15-6 | 5   | 12   | 11   | 6-8   | 5 | 17    | 14    |
| 0-12   | 5 | 7299 | 7303 | 11-0  | 5 | 199   | 180   | -4-3  | 5    | 1140 | 881  | -14-6 | 5   | 253  | 284  | -13-9 | 5 | 10    | 13    |
| 1-12   | 5 | 1503 | 1191 | -15-1 | 5 | 18    | 1     | -3-3  | 5    | 355  | 236  | -13-6 | 5   | 138  | 125  | -12-9 | 5 | 100   | 67    |
| 2-12   | 5 | 5    | 13   | -14-1 | 5 | 28    | 11    | -2-3  | 5    | 7    | 50   | -12-6 | 5   | 333  | 352  | -11-9 | 5 | 27    | 16    |
| 3-12   | 5 | 330  | 371  | -13-1 | 5 | 9     | 5     | -1-3  | 5    | 7    | 11   | -11-6 | 5   | 815  | 812  | -10-9 | 5 | 215   | 223   |
| 4-12   | 5 | 95   | 111  | -12-1 | 5 | 385   | 379   | 0-3   | 5    | 3592 | 3950 | -10-6 | 5   | 23   | 18   | -9-9  | 5 | 146   | 146   |
| 5-12   | 5 | 535  | 565  | -11-1 | 5 | 29    | 55    | 1-3   | 5    | 209  | 236  | -9-6  | 5   | 110  | 111  | -8-9  | 5 | 104   | 140   |
| 6-12   | 5 | 2902 | 3031 | -10-1 | 5 | 472   | 322   | 2-3   | 5    | 3802 | 3167 | -8-6  | 5   | 456  | 435  | -7-9  | 5 | 95    | 72    |
| 7-12   | 5 | 60   | 42   | -9-1  | 5 | 1155  | 987   | 3-3   | 5    | 1319 | 1305 | -7-6  | 5   | 387  | 330  | -6-9  | 5 | 91    | 53    |
| 8-12   | 5 | 31   | 55   | -8-1  | 5 | 528   | 410   | 4-3   | 5    | 252  | 256  | -6-6  | 5   | 392  | 320  | -5-9  | 5 | 59    | 47    |
| 9-12   | 5 | 6    | 1    | -7-1  | 5 | 34    | 14    | 5-3   | 5    | 473  | 504  | -4-6  | 5   | 2141 | 1871 | -4-9  | 5 | 79    | 87    |
| 10-12  | 5 | 15   | 0    | -6-1  | 5 | 1525  | 1296  | 6-3   | 5    | 86   | 78   | -4-6  | 5   | 86   | 3    | -3-9  | 5 | 109   | 166   |
| 11-12  | 5 | 173  | 223  | -5-1  | 5 | 233   | 277   | 7-3   | 5    | 5    | 4    | -3-6  | 5   | 1    | 31   | -2-9  | 5 | 18    | 53    |
| 12-12  | 5 | 16   | 16   | -4-1  | 5 | 4904  | 5624  | 8-3   | 5    | 55   | 58   | -2-6  | 5   | 1017 | 1114 | -1-9  | 5 | 622   | 654   |
| -14-11 | 5 | 4    | 0    | -3-1  | 5 | 71    | 107   | 9-3   | 5    | 11   | 10   | -1-6  | 5   | 138  | 278  | 0-9   | 5 | 10    | 1     |
| -13-11 | 5 | 67   | 55   | -2-1  | 5 | 2177  | 2266  | 10-3  | 5    | 38   | 56   | 0-6   | 5   | 526  | 550  | 1-9   | 5 | 719   | 611   |
| -12-11 | 5 | 325  | 284  | -1-1  | 5 | 540   | 413   | -15-4 | 5    | 73   | 61   | 1-6   | 5   | 318  | 302  | 2-9   | 5 | 42    | 55    |
| -11-11 | 5 | 96   | 69   | 0-1   | 5 | 676   | 808   | -14-4 | 5    | 131  | 103  | 2-6   | 5   | 150  | 203  | 3-9   | 5 | 17    | 4     |
| -10-11 | 5 | 181  | 163  | 1-1   | 5 | 35    | 28    | -13-4 | 5    | 10   | 21   | 3-6   | 5   | 375  | 403  | 4-9   | 5 | 61    | 67    |
| -9-11  | 5 | 701  | 495  | 2-1   | 5 | 2403  | 2090  | -12-4 | 5    | 333  | 387  | 4-6   | 5   | 585  | 542  | 5-9   | 5 | 67    | 72    |
| -8-11  | 5 | 879  | 681  | 3-1   | 5 | 728   | 787   | -11-4 | 5    | 215  |      |       |     |      |      |       |   |       |       |

Table C.3, continued

| M   | K   | L | Obs  | Calc | M   | K   | L | Obs  | Calc | M   | K   | L | Obs  | Calc | M   | K  | L | Obs  | Calc |
|-----|-----|---|------|------|-----|-----|---|------|------|-----|-----|---|------|------|-----|----|---|------|------|
| -10 | 0   | 5 | 34   | 21   | 2   | 2   | 5 | 2830 | 2852 | -10 | 5   | 5 | 1013 | 1197 | -14 | 8  | 5 | 143  | 108  |
| -3  | 11  | 5 | 85   | 72   | 4   | -14 | 6 | 61   | 51   | 11  | -11 | 6 | 1    | 0    | 7   | -8 | 6 | 186  | 255  |
| -2  | 11  | 5 | 0    | 1    | 5   | -14 | 6 | 19   | 0    | -10 | -10 | 6 | 17   | 28   | 0   | -8 | 6 | 62   | 59   |
| 0   | 11  | 5 | 664  | 590  | 6   | -14 | 6 | 12   | 21   | -9  | -10 | 6 | 4    | 3    | 9   | -8 | 6 | 58   | 64   |
| 0   | 11  | 5 | 32   | 35   | 7   | -14 | 6 | -4   | 1    | -8  | -10 | 6 | 71   | 55   | 10  | -8 | 6 | 47   | 38   |
| 1   | 11  | 5 | 66   | 86   | 8   | -14 | 6 | 121  | 114  | -7  | -10 | 6 | 108  | 103  | 11  | -8 | 6 | 289  | 300  |
| 2   | 11  | 5 | 56   | 54   | 9   | -14 | 6 | 14   | 1    | -6  | -10 | 6 | 141  | 92   | 12  | -8 | 6 | 115  | 112  |
| -11 | 12  | 5 | 15   | 18   | 10  | -14 | 6 | 58   | 74   | -5  | -10 | 6 | 149  | 141  | -12 | -7 | 6 | 1    | 1    |
| -10 | 12  | 5 | 4    | 2    | -7  | -13 | 6 | 34   | 26   | -4  | -10 | 6 | 144  | 135  | -11 | -7 | 6 | 1    | 1    |
| -9  | 12  | 5 | 85   | 68   | -6  | -13 | 6 | 26   | 42   | -3  | -10 | 6 | 59   | 90   | -10 | -7 | 6 | 101  | 89   |
| -8  | 12  | 5 | 14   | 10   | -5  | -13 | 6 | 30   | 5    | -2  | -10 | 6 | 560  | 382  | -9  | -7 | 6 | 127  | 153  |
| -7  | 12  | 5 | 42   | 17   | -4  | -13 | 6 | 512  | 445  | 0   | -10 | 6 | 1003 | 799  | -7  | -7 | 6 | 753  | 572  |
| -6  | 12  | 5 | 14   | 14   | -3  | -13 | 6 | 513  | 597  | 1   | -10 | 6 | 34   | 49   | -6  | -7 | 6 | 268  | 184  |
| -5  | 12  | 5 | 87   | 47   | -2  | -13 | 6 | 513  | 597  | 1   | -10 | 6 | 34   | 49   | -6  | -7 | 6 | 268  | 184  |
| -4  | 12  | 5 | 0    | 27   | -1  | -13 | 6 | 16   | 4    | 2   | -10 | 6 | 231  | 204  | -5  | -7 | 6 | 1673 | 1199 |
| -3  | 12  | 5 | 89   | 53   | 0   | -13 | 6 | 1170 | 1047 | 3   | -10 | 6 | 99   | 131  | -4  | -7 | 6 | 1022 | 1188 |
| -2  | 12  | 5 | 18   | 1    | 1   | -13 | 6 | 426  | 501  | 4   | -10 | 6 | 13   | 2    | -3  | -7 | 6 | 4440 | 3514 |
| -1  | 12  | 5 | 8    | 5    | 2   | -13 | 6 | 417  | 335  | 5   | -10 | 6 | 82   | 102  | -2  | -7 | 6 | 2022 | 2073 |
| 0   | 12  | 5 | 9    | 5    | 3   | -13 | 6 | 523  | 508  | 6   | -10 | 6 | 317  | 253  | -1  | -7 | 6 | 1340 | 1408 |
| 1   | 12  | 5 | 30   | 41   | 4   | -13 | 6 | 163  | 140  | 7   | -10 | 6 | 109  | 106  | 0   | -7 | 6 | 1019 | 838  |
| -9  | 13  | 5 | 42   | 30   | 5   | -13 | 6 | 122  | 79   | 8   | -10 | 6 | 48   | 20   | 1   | -7 | 6 | 138  | 273  |
| -8  | 13  | 5 | 84   | 75   | 6   | -13 | 6 | 238  | 202  | 9   | -10 | 6 | 30   | 18   | 2   | -7 | 6 | 31   | 41   |
| -7  | 13  | 5 | 223  | 220  | 7   | -13 | 6 | 40   | 51   | 10  | -10 | 6 | 30   | 18   | 3   | -7 | 6 | 317  | 298  |
| -6  | 13  | 5 | 12   | 3    | 8   | -13 | 6 | 85   | 106  | 11  | -10 | 6 | 51   | 61   | 4   | -7 | 6 | 68   | 79   |
| -5  | 13  | 5 | 186  | 196  | 9   | -13 | 6 | 26   | 26   | 12  | -10 | 6 | 9    | 1    | 5   | -7 | 6 | 12   | 7    |
| -4  | 13  | 5 | 4    | 0    | 10  | -13 | 6 | 148  | 158  | -11 | -9  | 6 | 64   | 58   | 6   | -7 | 6 | 243  | 250  |
| -3  | 13  | 5 | 288  | 263  | 11  | -13 | 6 | 25   | 5    | -10 | -9  | 6 | 13   | 6    | 7   | -7 | 6 | 4    | 19   |
| -2  | 13  | 5 | 10   | 3    | -8  | -12 | 6 | -5   | 0    | -9  | -9  | 6 | 124  | 149  | 8   | -7 | 6 | 157  | 97   |
| -1  | 17  | 6 | 53   | 70   | -7  | -12 | 6 | 132  | 163  | -8  | -9  | 6 | 15   | 36   | 9   | -7 | 6 | 195  | 200  |
| 2   | -17 | 6 | -2   | 0    | -6  | -12 | 6 | 2    | 0    | -7  | -9  | 6 | 722  | 652  | 10  | -7 | 6 | 17   | 9    |
| 3   | -17 | 6 | 24   | 2    | -5  | -12 | 6 | 141  | 118  | -6  | -9  | 6 | 47   | 52   | 11  | -7 | 6 | 6    | 5    |
| 4   | -17 | 6 | 55   | 72   | -4  | -12 | 6 | 165  | 193  | -5  | -9  | 6 | 101  | 86   | 12  | -7 | 6 | 346  | 399  |
| 5   | -17 | 6 | 4    | 1    | -3  | -12 | 6 | 151  | 145  | -4  | -9  | 6 | 220  | 0    | -12 | -6 | 6 | 21   | 16   |
| -2  | -16 | 6 | 27   | 19   | -2  | -12 | 6 | 675  | 850  | -3  | -9  | 6 | 699  | 696  | -11 | -6 | 6 | 26   | 20   |
| -1  | -16 | 6 | 39   | 33   | -1  | -12 | 6 | 1    | 98   | -1  | -9  | 6 | 39   | 75   | -10 | -6 | 6 | 92   | 72   |
| 0   | -16 | 6 | 10   | 0    | 0   | -12 | 6 | 164  | 98   | 0   | -9  | 6 | 1520 | 915  | -9  | -6 | 6 | 137  | 74   |
| 1   | -16 | 6 | 71   | 62   | 1   | -12 | 6 | 39   | 50   | 0   | -9  | 6 | 16   | 22   | -8  | -6 | 6 | 1735 | 1564 |
| 2   | -16 | 6 | 33   | 35   | 2   | -12 | 6 | 941  | 824  | 1   | -9  | 6 | 16   | 22   | -7  | -6 | 6 | 164  | 118  |
| 3   | -16 | 6 | 26   | 34   | 3   | -12 | 6 | 10   | 2    | 2   | -9  | 6 | 247  | 72   | -6  | -6 | 6 | 2009 | 1717 |
| 4   | -16 | 6 | 5    | 2    | 4   | -12 | 6 | 641  | 664  | 3   | -9  | 6 | -5   | 6    | -6  | -6 | 6 | 9    | 12   |
| 5   | -16 | 6 | -3   | 9    | 5   | -12 | 6 | 31   | 40   | 4   | -9  | 6 | 64   | 76   | -5  | -6 | 6 | 1565 | 1613 |
| 6   | -16 | 6 | 33   | 14   | 6   | -12 | 6 | 688  | 577  | 5   | -9  | 6 | 711  | 619  | -4  | -6 | 6 | 1436 | 1294 |
| 7   | -16 | 6 | 6    | 1    | 7   | -12 | 6 | 9    | 21   | 6   | -9  | 6 | 67   | 34   | -3  | -6 | 6 | 299  | 203  |
| -4  | -15 | 6 | 25   | 17   | 8   | -12 | 6 | 212  | 169  | 7   | -9  | 6 | 67   | 64   | -2  | -6 | 6 | 126  | 155  |
| -3  | -15 | 6 | 240  | 272  | 9   | -12 | 6 | 23   | 16   | 8   | -9  | 6 | 180  | 147  | 0   | -6 | 6 | 820  | 490  |
| -2  | -15 | 6 | 25   | 12   | 10  | -12 | 6 | 1    | 1    | 9   | -9  | 6 | 11   | 31   | 1   | -6 | 6 | 1312 | 1536 |
| -1  | -15 | 6 | 505  | 474  | 11  | -12 | 6 | 1    | 1    | 10  | -9  | 6 | 10   | 10   | 2   | -6 | 6 | 5654 | 5196 |
| 0   | -15 | 6 | 55   | 110  | -9  | -11 | 6 | 108  | 112  | 11  | -9  | 6 | 26   | 36   | 3   | -6 | 6 | 325  | 201  |
| 1   | -15 | 6 | 291  | 303  | -8  | -11 | 6 | 13   | 15   | 12  | -9  | 6 | 32   | 53   | 4   | -6 | 6 | 6    | 1    |
| 2   | -15 | 6 | 128  | 97   | -7  | -11 | 6 | 15   | 2    | -11 | -8  | 6 | 7    | 2    | 5   | -6 | 6 | 130  | 200  |
| 3   | -15 | 6 | 87   | 68   | -6  | -11 | 6 | -3   | 1    | -10 | -8  | 6 | 248  | 197  | 6   | -6 | 6 | 87   | 149  |
| 4   | -15 | 6 | 69   | 49   | -5  | -11 | 6 | 99   | 80   | -9  | -8  | 6 | 655  | 537  | 7   | -6 | 6 | 675  | 625  |
| 5   | -15 | 6 | 3    | 8    | -4  | -11 | 6 | 261  | 294  | -8  | -8  | 6 | 22   | 5    | 8   | -6 | 6 | -4   | 2    |
| 6   | -15 | 6 | 213  | 209  | -3  | -11 | 6 | 13   | 10   | -7  | -8  | 6 | 290  | 287  | 9   | -6 | 6 | 544  | 407  |
| 7   | -15 | 6 | 9    | 1    | -2  | -11 | 6 | 942  | 782  | -6  | -8  | 6 | 241  | 137  | 10  | -6 | 6 | 123  | 106  |
| 8   | -15 | 6 | 143  | 212  | -1  | -11 | 6 | 65   | 52   | -5  | -8  | 6 | 25   | 42   | 11  | -6 | 6 | 121  | 107  |
| 9   | -15 | 6 | 14   | 3    | 0   | -11 | 6 | 359  | 293  | -4  | -8  | 6 | 365  | 338  | 12  | -6 | 6 | 75   | 88   |
| -6  | -14 | 6 | -6   | 0    | 1   | -11 | 6 | 43   | 14   | -3  | -8  | 6 | 147  | 68   | -13 | -5 | 6 | 7    | 1    |
| -5  | -14 | 6 | 43   | 37   | 2   | -11 | 6 | 394  | 560  | -2  | -8  | 6 | 589  | 449  | -12 | -5 | 6 | 8    | 0    |
| -4  | -14 | 6 | 71   | 84   | 3   | -11 | 6 | 253  | 281  | -1  | -8  | 6 | 1649 | 1531 | -11 | -5 | 6 | 131  | 19   |
| -3  | -14 | 6 | 604  | 562  | 4   | -11 | 6 | 216  | 265  | 0   | -8  | 6 | 1282 | 1047 | -10 | -5 | 6 | 151  | 97   |
| -2  | -14 | 6 | 99   | 78   | 5   | -11 | 6 | 13   | 7    | 1   | -8  | 6 | 349  | 232  | -9  | -5 | 6 | 130  | 166  |
| -1  | -14 | 6 | 216  | 187  | 6   | -11 | 6 | 59   | 76   | 2   | -8  | 6 | 60   | 48   | -8  | -5 | 6 | 334  | 234  |
| 0   | -14 | 6 | 53   | 96   | 7   | -11 | 6 | 25   | 46   | 3   | -8  | 6 | 673  | 625  | -7  | -5 | 6 | 114  | 46   |
| 1   | -14 | 6 | 102  | 106  | 8   | -11 | 6 | 64   | 41   | 4   | -8  | 6 | 14   | 10   | -6  | -5 | 6 | 79   | 93   |
| 2   | -14 | 6 | 30   | 33   | 9   | -11 | 6 | 76   | 309  | 6   | -8  | 6 | 63   | 44   | -5  | -5 | 6 | 27   | 30   |
| 3   | -14 | 6 | -1   | 2    | 10  | -11 | 6 | 297  | 405  | -4  | -8  | 6 | 137  | 169  | -4  | -5 | 6 | 529  | 555  |
| 8   | -3  | 6 | 209  | 168  | -7  | 0   | 6 | 6617 | 5672 | 7   | 2   | 6 | 283  | 287  | -3  | 5  | 6 | 132  | 117  |
| 9   | -3  | 6 | 15   | 7    | -6  | 0   | 6 | 66   | 41   | 8   | 2   | 6 | 49   | 40   | -2  | 5  | 6 | 116  | 94   |
| 10  | -3  | 6 | 76   | 47   | -5  | 0   | 6 | 995  | 989  | 9   | 2   | 6 | 35   | 26   | 0   | 5  | 6 | 104  | 75   |
| 11  | -3  | 6 | 90   | 81   | -4  | 0   | 6 | 16   | 5    | 10  | 2   | 6 | -4   | 4    | 1   | 5  | 6 | 173  | 245  |
| -14 | -2  | 6 | 186  | 153  | -2  | 0   | 6 | 69   | 91   | -15 | 3   | 6 | 129  | 129  | 2   | 5  | 6 | 693  | 825  |
| -13 | -2  | 6 | 76   | 81   | -1  | 0   | 6 | 8123 | 7468 | -14 | 3   | 6 | 10   | 14   | 3   | 5  | 6 | 1157 | 1145 |
| -12 | -2  | 6 | 640  | 559  | 0   | 0   | 6 | 77   | 66   | -13 | 3   | 6 | 49   | 22   | 4   | 5  | 6 | 233  | 230  |
| -11 | -2  | 6 | 551  | 466  | 1   | 0   | 6 | 4937 | 4598 | -12 | 3   | 6 | 166  | 168  | 6   | 5  | 6 | 37   | 39   |
| -10 | -2  | 6 | 306  | 417  | 2   | 0   | 6 | 503  | 604  | -11 | 3   | 6 | 167  | 326  | 7   | 5  | 6 | 10   | 4    |
| -9  | -2  | 6 | 508  | 296  | 3   | 0   | 6 | 250  | 294  | -10 | 3   | 6 | 463  | 339  | 8   | 5  | 6 | 57   | 45   |
| -8  | -2  | 6 | 674  | 821  | 4   | 0   | 6 | 220  | 383  | -8  | 3   | 6 | 382  | 17   | -14 | 6  | 6 | 0    | 0    |
| -7  | -2  | 6 | 156  | 126  | 5   | 0   | 6 | 344  | 388  | -7  | 3   | 6 | 16   | 927  | -13 | 6  | 6 | 48   | 34   |
| -6  | -2  | 6 | 2988 | 2698 | 6   | 0   | 6 | 280  | 373  | -6  | 3   | 6 | 651  | 5786 | -12 | 6  | 6 | 91   | 121  |
| -5  | -2  | 6 | 113  | 196  | 7   | 0   | 6 | 57   | 74   | -5  | 3   | 6 | 5690 | 1717 | -11 | 6  | 6 | 992  | 908  |
| -4  | -2  | 6 | 2752 | 2532 | 8   | 0   | 6 | 364  | 376  | -4  | 3   | 6 | 4    | 5    | -10 | 6  | 6 | 10   | 35   |
| -3  | -2  | 6 | 71   | 50   | 9   | 0   | 6 | 10   | 0    | -3  | 3   | 6 | 4    | 187  | -9  | 6  | 6 | 220  | 330  |
| -2  | -2  | 6 | 171  | 152  | 10  | 0   | 6 | 15   | 14   | -2  | 3   | 6 | 315  | 746  | -8  | 6  | 6 | 338  | 365  |
| -1  | -2  | 6 | 13   | 12   | 11  | 0   | 6 | 12   | 1    | -1  | 3   | 6 | 1171 | 961  | -7  | 6  | 6 | 90   | 86   |
| 0   | -2  | 6 | 46   | 48   | -15 | 1   | 6 | -5   | 2    | 0   | 3   | 6 | 199  | 233  | -6  | 6  | 6 | 39   | 65   |
| 1   | -2  | 6 | 3    | 6    | -14 | 1   | 6 | 11   | 9    | 1   | 3   | 6 | 679  | 693  | -5  | 6  | 6 | 16   | 24   |
| 2   | -2  | 6 | 3455 |      |     |     |   |      |      |     |     |   |      |      |     |    |   |      |      |

Table C.3, continued

| M   | K  | L | Obs   | Calc | M    | K   | L | Obs  | Calc | M   | K  | L | Obs  | Calc | M   | K   | L  | Obs  | Calc | M   | K  | L  | Obs  | Calc | M    | K    | L  | Obs  | Calc | M    | K   | L   | Obs  | Calc |      |
|-----|----|---|-------|------|------|-----|---|------|------|-----|----|---|------|------|-----|-----|----|------|------|-----|----|----|------|------|------|------|----|------|------|------|-----|-----|------|------|------|
| -8  | -1 | 6 | 711   | 832  | 4    | 1   | 6 | 103  | 76   | -7  | 4  | 6 | 307  | 464  | -11 | 7   | 6  | 145  | 173  | -2  | 10 | 6  | 173  | 181  | -1   | 1    | 6  | 307  | 464  | -11  | 7   | 6   | 145  | 173  |      |
| -7  | -1 | 6 | 3155  | 1875 | 5    | 1   | 6 | 1323 | 1115 | -6  | 4  | 6 | 36   | 55   | -10 | 7   | 6  | 66   | 50   | -1  | 10 | 6  | 42   | 16   | -1   | 1    | 6  | 301  | 241  | 0    | 10  | 6   | 221  | 195  |      |
| -6  | -1 | 6 | 10987 | 9874 | 6    | 1   | 6 | 982  | 1058 | -5  | 4  | 6 | 1144 | 1071 | -9  | 7   | 6  | 301  | 241  | 0   | 10 | 6  | 221  | 195  | -1   | 1    | 6  | 301  | 241  | 0    | 10  | 6   | 221  | 195  |      |
| -5  | -1 | 6 | 5006  | 4524 | 7    | 1   | 6 | 112  | 74   | -4  | 4  | 6 | 1337 | 849  | -8  | 7   | 6  | 63   | 50   | 1   | 10 | 6  | 25   | 18   | -3   | -1   | 6  | 5121 | 5324 | 9    | 1   | 6   | 67   | 39   |      |
| -4  | -1 | 6 | 82    | 82   | 8    | 1   | 6 | 29   | 28   | -3  | 4  | 6 | 103  | 85   | -7  | 7   | 6  | 1080 | 1253 | 2   | 10 | 6  | 67   | 39   | -2   | -1   | 6  | 4375 | 3972 | 10   | 1   | 6   | 26   | 21   |      |
| -3  | -1 | 6 | 5121  | 5324 | 9    | 1   | 6 | 185  | 139  | -2  | 4  | 6 | 460  | 286  | -6  | 7   | 6  | 19   | 42   | 3   | 10 | 6  | 26   | 21   | -1   | -1   | 6  | 21   | 10   | -15  | 2   | 6   | 110  | 101  |      |
| -2  | -1 | 6 | 4375  | 3972 | 10   | 1   | 6 | 5    | 22   | -1  | 4  | 6 | 207  | 268  | -5  | 7   | 6  | 163  | 167  | -11 | 11 | 6  | 110  | 101  | 0    | -1   | 6  | 292  | 421  | -14  | 2   | 6   | 320  | 304  |      |
| -1  | -1 | 6 | 21    | 10   | -15  | 2   | 6 | 20   | 23   | 0   | 4  | 6 | 8    | 17   | -3  | 7   | 6  | 277  | 220  | -10 | 11 | 6  | 1    | 7    | 54   | 1    | -1 | 6    | 5775 | 6321 | -13 | 2   | 6    | 50   | 47   |
| 0   | -1 | 6 | 292   | 421  | -14  | 2   | 6 | 320  | 304  | 1   | 4  | 6 | -6   | 17   | -3  | 7   | 6  | 277  | 220  | -10 | 11 | 6  | 1    | 7    | 54   | 2    | -1 | 6    | 3318 | 3125 | -12 | 2   | 6    | 21   | 8    |
| 1   | -1 | 6 | 5775  | 6321 | -13  | 2   | 6 | 50   | 47   | 2   | 4  | 6 | 254  | 259  | -2  | 7   | 6  | 260  | 290  | -8  | 11 | 6  | 146  | 152  | 3    | -1   | 6  | 13   | 3    | -11  | 2   | 6   | 441  | 448  |      |
| 2   | -1 | 6 | 3318  | 3125 | -12  | 2   | 6 | 21   | 8    | 3   | 4  | 6 | 666  | 810  | -1  | 7   | 6  | 809  | 858  | -7  | 11 | 6  | 0    | 2    | 31   | -1   | 6  | 758  | 782  | -10  | 2   | 6   | 200  | 250  |      |
| 3   | -1 | 6 | 13    | 3    | -11  | 2   | 6 | 441  | 448  | 4   | 4  | 6 | 28   | 15   | 0   | 7   | 6  | 218  | 219  | -6  | 11 | 6  | 38   | 31   | 4    | -1   | 6  | 43   | 69   | -9   | 2   | 6   | 781  | 937  |      |
| 4   | -1 | 6 | 758   | 782  | -10  | 2   | 6 | 200  | 250  | 5   | 4  | 6 | 12   | 5    | 1   | 7   | 6  | 851  | 1019 | -5  | 11 | 6  | 6    | 2    | 6    | -1   | 6  | 442  | 488  | -8   | 2   | 6   | 33   | 29   |      |
| 5   | -1 | 6 | 43    | 69   | -9   | 2   | 6 | 781  | 937  | 6   | 4  | 6 | 31   | 16   | 2   | 7   | 6  | 60   | 51   | -4  | 11 | 6  | 70   | 128  | 6    | -1   | 6  | 223  | 253  | -7   | 2   | 6   | 1270 | 1380 |      |
| 6   | -1 | 6 | 442   | 488  | -8   | 2   | 6 | 33   | 29   | 7   | 4  | 6 | 7    | 108  | 4   | 7   | 6  | 86   | 95   | -2  | 11 | 6  | 10   | 19   | 7    | -1   | 6  | 46   | 41   | -6   | 2   | 6   | 44   | 33   |      |
| 7   | -1 | 6 | 223   | 253  | -7   | 2   | 6 | 1270 | 1380 | 8   | 4  | 6 | 228  | 108  | 4   | 7   | 6  | 86   | 95   | -2  | 11 | 6  | 10   | 19   | 7    | -1   | 6  | 72   | 52   | -5   | 2   | 6   | 6034 | 6270 |      |
| 8   | -1 | 6 | 46    | 41   | -6   | 2   | 6 | 44   | 33   | 9   | 4  | 6 | 15   | 21   | 5   | 7   | 6  | 16   | 12   | 0   | 11 | 6  | 19   | 29   | 9    | -1   | 6  | 14   | 4    | -4   | 2   | 6   | 73   | 131  |      |
| 9   | -1 | 6 | 72    | 52   | -5   | 2   | 6 | 6034 | 6270 | 10  | 4  | 6 | 15   | 21   | 5   | 7   | 6  | 16   | 12   | 0   | 11 | 6  | 19   | 29   | 10   | -1   | 6  | 8    | 1    | -3   | 2   | 6   | 1127 | 957  |      |
| 10  | -1 | 6 | 14    | 4    | -4   | 2   | 6 | 73   | 131  | -15 | 0  | 6 | 152  | 179  | -14 | 8   | 6  | 18   | 18   | 1   | 11 | 6  | 11   | 3    | -15  | 0    | 6  | 101  | 107  | -2   | 2   | 6   | 13   | 36   |      |
| 11  | -1 | 6 | 8     | 1    | -3   | 2   | 6 | 1127 | 957  | -14 | 0  | 6 | 152  | 179  | -14 | 8   | 6  | 18   | 18   | 1   | 11 | 6  | 11   | 3    | -14  | 0    | 6  | 235  | 273  | -1   | 2   | 6   | 1143 | 947  |      |
| -13 | 0  | 6 | 7     | 2    | 0    | 2   | 6 | 726  | 633  | -13 | 0  | 6 | 133  | 67   | -10 | 8   | 6  | 5    | 199  | -6  | 12 | 6  | 7    | 10   | 1    | -13  | 0  | 6    | 1    | 6    | 1   | 2   | 6    | 3638 | 3361 |
| -12 | 0  | 6 | 1     | 6    | 1    | 2   | 6 | 3638 | 3361 | -12 | 0  | 6 | 133  | 67   | -10 | 8   | 6  | 5    | 199  | -6  | 12 | 6  | 7    | 10   | 1    | -12  | 0  | 6    | 1    | 6    | 1   | 2   | 6    | 726  | 645  |
| -11 | 0  | 6 | 1     | 6    | 1    | 2   | 6 | 726  | 645  | -11 | 0  | 6 | 133  | 67   | -10 | 8   | 6  | 5    | 199  | -6  | 12 | 6  | 7    | 10   | 1    | -11  | 0  | 6    | 1    | 6    | 1   | 2   | 6    | 726  | 645  |
| -10 | 0  | 6 | 1082  | 1097 | 3    | 2   | 6 | 629  | 619  | -10 | 0  | 6 | 133  | 67   | -10 | 8   | 6  | 5    | 199  | -6  | 12 | 6  | 7    | 10   | 1    | -10  | 0  | 6    | 1    | 6    | 1   | 2   | 6    | 629  | 619  |
| -9  | 0  | 6 | 2     | 0    | 4    | 2   | 6 | 25   | 31   | -9  | 0  | 6 | 133  | 67   | -10 | 8   | 6  | 5    | 199  | -6  | 12 | 6  | 7    | 10   | 1    | -9   | 0  | 6    | 1    | 6    | 1   | 2   | 6    | 629  | 619  |
| -8  | 0  | 6 | 1213  | 1174 | 5    | 2   | 6 | 159  | 115  | -8  | 0  | 6 | 133  | 67   | -10 | 8   | 6  | 5    | 199  | -6  | 12 | 6  | 7    | 10   | 1    | -8   | 0  | 6    | 1    | 6    | 1   | 2   | 6    | 629  | 619  |
| -7  | 12 | 6 | 2     | 2    | -8   | -12 | 7 | 6    | 12   | -8  | -9 | 7 | 41   | 17   | 8   | -7  | 7  | 0    | 13   | -5  | -4 | 7  | 70   | 10   | -7   | 12   | 6  | 14   | 15   | -6   | -12 | 7   | 135  | 122  |      |
| -6  | 13 | 6 | 50    | 4    | -7   | -12 | 7 | 28   | 28   | -7  | -9 | 7 | 111  | 53   | 9   | -7  | 7  | 74   | 49   | -4  | -4 | 7  | 383  | 349  | -6   | 13   | 6  | 14   | 15   | -6   | -12 | 7   | 135  | 122  |      |
| -5  | 13 | 6 | 14    | 15   | -6   | -12 | 7 | 135  | 122  | -5  | 13 | 6 | 14   | 15   | -6  | -12 | 7  | 135  | 122  | -5  | 13 | 6  | 14   | 15   | 349  | -5   | 13 | 6    | 14   | 15   | -6  | -12 | 7    | 135  | 122  |
| -4  | 17 | 7 | 6     | 1    | -5   | -12 | 7 | 93   | 76   | -5  | -9 | 7 | 249  | 172  | 11  | -7  | 7  | 22   | 76   | -2  | -4 | 7  | 3732 | 3549 | -4   | 17   | 7  | 21   | 16   | -4   | -12 | 7   | 521  | 439  |      |
| -3  | 17 | 7 | 21    | 16   | -4   | -12 | 7 | 521  | 439  | -3  | 17 | 7 | 21   | 16   | -4  | -12 | 7  | 521  | 439  | -3  | 17 | 7  | 21   | 16   | 1422 | -3   | 17 | 7    | 40   | 16   | -3  | -12 | 7    | 179  | 139  |
| -2  | 17 | 7 | 40    | 16   | -3   | -12 | 7 | 179  | 139  | -2  | 17 | 7 | 40   | 16   | -3  | -12 | 7  | 179  | 139  | -2  | 17 | 7  | 40   | 16   | 1422 | -2   | 17 | 7    | 8    | 3    | -2  | -12 | 7    | 96   | 83   |
| -1  | 17 | 7 | 8     | 3    | -2   | -12 | 7 | 96   | 83   | -1  | 17 | 7 | 8    | 3    | -2  | -12 | 7  | 96   | 83   | -1  | 17 | 7  | 8    | 3    | 5741 | -1   | 17 | 7    | 10   | 10   | -1  | -12 | 7    | 16   | 49   |
| 0   | 17 | 7 | 7     | 10   | -1   | -12 | 7 | 16   | 49   | 0   | 17 | 7 | 7    | 10   | -1  | -12 | 7  | 16   | 49   | 0   | 17 | 7  | 7    | 10   | 1417 | 0    | 17 | 7    | 43   | 39   | 0   | -12 | 7    | 749  | 663  |
| 1   | 17 | 7 | 43    | 39   | 0    | -12 | 7 | 749  | 663  | 1   | 17 | 7 | 43   | 39   | 0   | -12 | 7  | 749  | 663  | 1   | 17 | 7  | 43   | 39   | 5741 | 1    | 17 | 7    | 200  | 229  | 1   | -12 | 7    | 1    | 1    |
| 2   | 17 | 7 | 200   | 229  | 1    | -12 | 7 | 1    | 1    | 2   | 3  | 9 | 7    | 90   | 79  | -8  | -6 | 7    | 629  | 765 | 5  | -4 | 7    | 1905 | 1852 | 2    | 17 | 7    | 19   | 17   | 3   | -12 | 7    | 564  | 591  |
| 3   | 17 | 7 | 19    | 17   | 3    | -12 | 7 | 564  | 591  | 3   | 17 | 7 | 19   | 17   | 3   | -12 | 7  | 564  | 591  | 3   | 17 | 7  | 19   | 17   | 3    | 1852 | 3  | 17   | 2    | 6    | 4   | -12 | 7    | 41   | 20   |
| 4   | 17 | 7 | 2     | 6    | 4    | -12 | 7 | 41   | 20   | 4   | 17 | 7 | 2    | 6    | 4   | -12 | 7  | 41   | 20   | 4   | 17 | 7  | 2    | 6    | 3    | 1852 | 4  | 17   | 37   | 36   | 5   | -12 | 7    | 33   | 42   |
| 5   | 17 | 7 | 37    | 36   | 5    | -12 | 7 | 33   | 42   | 5   | 17 | 7 | 37   | 36   | 5   | -12 | 7  | 33   | 42   | 5   | 17 | 7  | 37   | 36   | 17   | 5    | 17 | 13   | 2    | 6    | -12 | 7   | 46   | 45   |      |
| 6   | 17 | 7 | 13    | 2    | 6    | -12 | 7 | 46   | 45   | 6   | 17 | 7 | 13   | 2    | 6   | -12 | 7  | 46   | 45   | 6   | 17 | 7  | 13   | 2    | 17   | 6    | 17 | 39   | 19   | 7    | -12 | 7   | 187  | 197  |      |
| 7   | 17 | 7 | 39    | 19   | 7    | -12 | 7 | 187  | 197  | 7   | 17 | 7 | 39   | 19   | 7   | -12 | 7  | 187  | 197  | 7   | 17 | 7  | 39   | 19   | 5741 | 7    | 17 | 57   | 78   | 8    | -12 | 7   | 3    | 0    |      |
| 8   | 17 | 7 | 57    | 78   | 8    | -12 | 7 | 3    | 0    | 8   | -9 | 7 | 151  | 170  | -2  | -6  | 7  | 950  | 955  | 11  | -4 | 7  | 4    | 12   | 12   | 8    | 17 | 80   | 78   | 9    | -12 | 7   | 79   | 157  |      |
| 9   | 17 | 7 | 80    | 78   | 9    | -12 | 7 | 79   | 157  | 9   | 17 | 7 | 80   | 78   | 9   | -12 | 7  | 79   | 157  | 9   | 17 | 7  | 80   | 78   | 19   | 9    | 17 | 52   | 47   | 10   | -12 | 7   | 15   | 20   |      |
| 10  | 17 | 7 | 52    | 47   | 10   | -12 | 7 | 15   | 20   | 10  | 17 | 7 | 52   | 47   | 10  | -12 | 7  | 15   | 20   | 10  | 17 | 7  | 52   | 47   | 39   | 10   | 17 | 30   | 53   | 11   | -12 | 7   | -2   | 4    |      |
| 11  | 17 | 7 | 30    | 53   | 11   | -12 | 7 | -2   | 4    | 11  | -9 | 7 | 8    | 12   | 1   | -6  | 7  | 154  | 236  | -12 | -3 | 7  | -5   | 1    | 39   | 11   | 17 | 36   | 45   | -9   | -11 | 7   | 6    | 0    |      |
| -4  | 15 | 7 | 36    | 45   | -9   | -11 | 7 | 6    | 0    | 12  | -9 | 7 | 72   | 82   | 2   | -6  | 7  | 1716 | 1494 | -11 | -3 | 7  | 618  | 635  | -4   | 15   | 7  | 10   | 13   | -8   | -11 | 7   | 31   | 25   |      |
| -3  | 15 | 7 | 10    | 13   | -8   | -11 | 7 | 31   | 25   | -3  | 15 | 7 | 10   | 13   | -8  | -11 | 7  | 31   | 25   | -3  | 15 | 7  | 10   | 13   | 46   | -3   | 15 | 7    | 19   | 14   | -7  | -11 | 7    | 21   | 14   |
| -2  | 15 | 7 | 19    | 14   | -7   | -11 | 7 | 21   | 14   | -2  | 15 | 7 | 19   | 14   | -7  | -11 | 7  | 21   | 14   | -2  | 15 | 7  | 19   | 14   | 446  | -2   | 15 | 7    | 6    | 8    | -6  | -11 | 7    | 21   | 8    |
| -1  | 15 | 7 | 6     | 8    | -6   | -11 | 7 | 21   | 8    | -1  | 15 | 7 | 6    | 8    | -6  | -11 | 7  | 21   | 8    | -1  | 15 | 7  | 6    | 8    | 31   | 1    | 15 | 7    | 211  | 235  | -5  | -11 | 7    | 3    | 14   |
| 0   | 15 | 7 | 211   | 235  | -5   | -11 | 7 | 3    | 14   | 0   | 15 | 7 | 211  | 235  | -5  | -11 | 7  | 3    | 14   | 0   | 15 | 7  | 211  | 235  | 31   | 0    | 15 | 91   | 106  | -4   | -11 | 7   | 177  | 129  |      |
| 1   | 15 | 7 | 91    | 106  | -4</ |     |   |      |      |     |    |   |      |      |     |     |    |      |      |     |    |    |      |      |      |      |    |      |      |      |     |     |      |      |      |

Table C.3, continued

| M   | K  | L | Obs   | Calc  | M   | K  | L | Obs  | Calc | M   | K  | L | Obs  | Calc | M   | K  | L   | Obs  | Calc | M   | K   | L | Obs   | Calc  |
|-----|----|---|-------|-------|-----|----|---|------|------|-----|----|---|------|------|-----|----|-----|------|------|-----|-----|---|-------|-------|
| -7  | -1 | 7 | 1547  | 1654  | 6   | 1  | 7 | 618  | 768  | -4  | 4  | 7 | 123  | 189  | -4  | 7  | 7   | 837  | 730  | -4  | 11  | 7 | 9     | 1     |
| -6  | -1 | 7 | 537   | 380   | 7   | 1  | 7 | 1    | 0    | -3  | 4  | 7 | 7    | 19   | -3  | 7  | 7   | 93   | 44   | -3  | 11  | 7 | 153   | 160   |
| -5  | -1 | 7 | 13259 | 13329 | 8   | 1  | 7 | 341  | 317  | -2  | 4  | 7 | 18   | 56   | -2  | 7  | 7   | 199  | 203  | -2  | 11  | 7 | 24    | 8     |
| -4  | -1 | 7 | 79    | 31    | 9   | 1  | 7 | -2   | 1    | -1  | 4  | 7 | 349  | 272  | -1  | 7  | 7   | 1    | 1    | -1  | 11  | 7 | 77    | 63    |
| -3  | -1 | 7 | 1381  | 1750  | 10  | 1  | 7 | 36   | 95   | 0   | 4  | 7 | 304  | 437  | 0   | 7  | 7   | 49   | 55   | 0   | 11  | 7 | 43    | 51    |
| -2  | -1 | 7 | 2726  | 2830  | -15 | 2  | 7 | 61   | 45   | 1   | 4  | 7 | 741  | 863  | 1   | 7  | 7   | 3    | 3    | -8  | 12  | 7 | 86    | 65    |
| -1  | -1 | 7 | 7     | 10    | -14 | 2  | 7 | 0    | 10   | 3   | 4  | 7 | 41   | 87   | 2   | 7  | 7   | 107  | 50   | -7  | 12  | 7 | 43    | 44    |
| 0   | -1 | 7 | 7337  | 7682  | -13 | 2  | 7 | 511  | 437  | 4   | 4  | 7 | 484  | 431  | 3   | 7  | 7   | 54   | 43   | -6  | 12  | 7 | 70    | 43    |
| 1   | -1 | 7 | 554   | 542   | -12 | 2  | 7 | 598  | 598  | 5   | 4  | 7 | 369  | 276  | 5   | 7  | 7   | 64   | 37   | -4  | 12  | 7 | 212   | 199   |
| 2   | -1 | 7 | 4033  | 3380  | -11 | 2  | 7 | 13   | 42   | 6   | 4  | 7 | 40   | 38   | -13 | 8  | 7   | 169  | 166  | -3  | 12  | 7 | 44    | 48    |
| 3   | -1 | 7 | 5     | 534   | -9  | 2  | 7 | 542  | 550  | 7   | 4  | 7 | 216  | 227  | -12 | 8  | 7   | 258  | 280  | 0   | -17 | 8 | -9    | 1     |
| 4   | -1 | 7 | 564   | 542   | -10 | 2  | 7 | 451  | 446  | 8   | 4  | 7 | 6    | 6    | -11 | 8  | 7   | 171  | 137  | 1   | -17 | 8 | 3     | 9     |
| 5   | -1 | 7 | 12    | 274   | -7  | 2  | 7 | 86   | 64   | -14 | 5  | 7 | 20   | 25   | -10 | 8  | 7   | 26   | 19   | 3   | -17 | 8 | 21    | 25    |
| 6   | -1 | 7 | 323   | 435   | -5  | 2  | 7 | 7    | 128  | -13 | 5  | 7 | 105  | 97   | -9  | 8  | 7   | 26   | 195  | 4   | -17 | 8 | 0     | 1     |
| 7   | -1 | 7 | 5     | 13    | -4  | 2  | 7 | 420  | 468  | -11 | 5  | 7 | 14   | 13   | -8  | 8  | 7   | 292  | 51   | -3  | -16 | 8 | -5    | 1     |
| 8   | -1 | 7 | 473   | 228   | -3  | 2  | 7 | 937  | 821  | -10 | 5  | 7 | 221  | 306  | -7  | 8  | 7   | 130  | 391  | -2  | -16 | 8 | 63    | 60    |
| 9   | -1 | 7 | 6     | 228   | -2  | 2  | 7 | 652  | 827  | -9  | 5  | 7 | 66   | 63   | -5  | 8  | 7   | 76   | 85   | -1  | -16 | 8 | 41    | 72    |
| 10  | -1 | 7 | 185   | 79    | -1  | 2  | 7 | 45   | 32   | -8  | 5  | 7 | 728  | 509  | -4  | 8  | 7   | 395  | 342  | 0   | -16 | 8 | 112   | 130   |
| 11  | -1 | 7 | 8     | 102   | 0   | 2  | 7 | 269  | 209  | -7  | 5  | 7 | 12   | 18   | -3  | 8  | 7   | 7    | 9    | 1   | -16 | 8 | 42    | 68    |
| -15 | 0  | 7 | 37    | 42    | 0   | 2  | 7 | 1589 | 1110 | -6  | 5  | 7 | 182  | 227  | -2  | 8  | 7   | 113  | 72   | 2   | -16 | 8 | 49    | 23    |
| -14 | 0  | 7 | 106   | 76    | 1   | 2  | 7 | 277  | 179  | -5  | 5  | 7 | 201  | 129  | -1  | 8  | 7   | 74   | 102  | 3   | -16 | 8 | 94    | 87    |
| -13 | 0  | 7 | 318   | 365   | 2   | 2  | 7 | 32   | 6    | -4  | 5  | 7 | 516  | 507  | 0   | 8  | 7   | 159  | 98   | 4   | -16 | 8 | 32    | 67    |
| -12 | 0  | 7 | 20    | 19    | 3   | 2  | 7 | 272  | 364  | -3  | 5  | 7 | 8    | 3    | 1   | 8  | 7   | 7    | 7    | 5   | -16 | 8 | 19    | 2     |
| -10 | 0  | 7 | 611   | 590   | 4   | 2  | 7 | 335  | 356  | -2  | 5  | 7 | 3691 | 3092 | 2   | 8  | 7   | 44   | 36   | 6   | -16 | 8 | 34    | 34    |
| -9  | 0  | 7 | 104   | 130   | 5   | 2  | 7 | 34   | 19   | -1  | 5  | 7 | 189  | 243  | 3   | 8  | 7   | 158  | 190  | 7   | -16 | 8 | 49    | 53    |
| -8  | 0  | 7 | 28    | 8     | 6   | 2  | 7 | 72   | 68   | 0   | 5  | 7 | 845  | 918  | 4   | 8  | 7   | 22   | 6    | -5  | -15 | 8 | 30    | 21    |
| -7  | 0  | 7 | 11    | 18    | 7   | 2  | 7 | 17   | 139  | 1   | 5  | 7 | 588  | 393  | -13 | 9  | 7   | 93   | 102  | -4  | -15 | 8 | 21    | 30    |
| -6  | 0  | 7 | 5995  | 4376  | 8   | 2  | 7 | 140  | 139  | 1   | 5  | 7 | 185  | 155  | -12 | 9  | 7   | 4    | 2    | -3  | -15 | 8 | 136   | 155   |
| -5  | 0  | 7 | 8712  | 8313  | 9   | 2  | 7 | 128  | 114  | 3   | 5  | 7 | 348  | 264  | -11 | 9  | 7   | 108  | 66   | -2  | -15 | 8 | 16    | 23    |
| -4  | 0  | 7 | 16    | 29    | -15 | 3  | 7 | 25   | 37   | 4   | 5  | 7 | 7    | 12   | -10 | 9  | 7   | 465  | 378  | -1  | -15 | 8 | 113   | 159   |
| -3  | 0  | 7 | 868   | 620   | -14 | 3  | 7 | 117  | 86   | 5   | 5  | 7 | 107  | 71   | -9  | 9  | 7   | 14   | 17   | 0   | -15 | 8 | 19    | 32    |
| -2  | 0  | 7 | 468   | 233   | -13 | 3  | 7 | 141  | 122  | 6   | 5  | 7 | 10   | 2    | -8  | 9  | 7   | 190  | 160  | 1   | -15 | 8 | 192   | 245   |
| -1  | 0  | 7 | 49    | 31    | -12 | 3  | 7 | 72   | 64   | 7   | 5  | 7 | 2    | 0    | -7  | 9  | 7   | 72   | 29   | 2   | -15 | 8 | 7     | 11    |
| 0   | 0  | 7 | 3426  | 3179  | -11 | 3  | 7 | 24   | 9    | -14 | 6  | 7 | 94   | 82   | -6  | 9  | 7   | 60   | 52   | 4   | -15 | 8 | 99    | 93    |
| 1   | 0  | 7 | 2304  | 1786  | -10 | 3  | 7 | 524  | 589  | -13 | 6  | 7 | 293  | 313  | -5  | 9  | 7   | 14   | 2    | 5   | -15 | 8 | 293   | 252   |
| 2   | 0  | 7 | 1846  | 1632  | -9  | 3  | 7 | 490  | 464  | -12 | 6  | 7 | 571  | 508  | -4  | 9  | 7   | 35   | 58   | 6   | -15 | 8 | 44    | 68    |
| 3   | 0  | 7 | 378   | 405   | -8  | 3  | 7 | 1263 | 1418 | -11 | 6  | 7 | 418  | 437  | -3  | 9  | 7   | 144  | 83   | 7   | -15 | 8 | 49    | 37    |
| 4   | 0  | 7 | 656   | 686   | -7  | 3  | 7 | 1683 | 1313 | -10 | 6  | 7 | 129  | 75   | -2  | 9  | 7   | 38   | 32   | 8   | -15 | 8 | 88    | 57    |
| 5   | 0  | 7 | 120   | 94    | -6  | 3  | 7 | 181  | 146  | -9  | 6  | 7 | -5   | 6    | -1  | 9  | 7   | 24   | 16   | -6  | -14 | 8 | 15    | 2     |
| 6   | 0  | 7 | 213   | 235   | -5  | 3  | 7 | 1398 | 2111 | -8  | 6  | 7 | 548  | 607  | 0   | 9  | 7   | 6    | 5    | -5  | -14 | 8 | 17    | 0     |
| 7   | 0  | 7 | 126   | 107   | -4  | 3  | 7 | 61   | 29   | -7  | 6  | 7 | 147  | 107  | 1   | 9  | 7   | 40   | 50   | -4  | -14 | 8 | 168   | 174   |
| 8   | 0  | 7 | 284   | 254   | -3  | 3  | 7 | 2142 | 2239 | -6  | 6  | 7 | 498  | 439  | 2   | 9  | 7   | 40   | 50   | -4  | -14 | 8 | 10    | 14    |
| 9   | 0  | 7 | 33    | 28    | -2  | 3  | 7 | 29   | 85   | -5  | 6  | 7 | 6    | 4    | 3   | 9  | 7   | 66   | 44   | -3  | -14 | 8 | 21    | 10    |
| 10  | 0  | 7 | 67    | 90    | -1  | 3  | 7 | 1296 | 1156 | -4  | 6  | 7 | 23   | 72   | -12 | 10 | 7   | 116  | 133  | -2  | -14 | 8 | 79    | 78    |
| -15 | 0  | 7 | 11    | 19    | 0   | 3  | 7 | 1336 | 1281 | -3  | 6  | 7 | 11   | 31   | -11 | 10 | 7   | 36   | 50   | -1  | -14 | 8 | 0     | 1     |
| -14 | 1  | 7 | 131   | 150   | 1   | 3  | 7 | 31   | 25   | -2  | 6  | 7 | 432  | 399  | -10 | 10 | 7   | 124  | 110  | 0   | -14 | 8 | 227   | 205   |
| -13 | 1  | 7 | 68    | 100   | 2   | 3  | 7 | 3    | 3    | -1  | 6  | 7 | 145  | 98   | -9  | 10 | 7   | 77   | 53   | 1   | -14 | 8 | 44    | 68    |
| -12 | 1  | 7 | 147   | 134   | 3   | 3  | 7 | 156  | 147  | 0   | 6  | 7 | 330  | 254  | -8  | 10 | 7   | 34   | 51   | 3   | -14 | 8 | 480   | 408   |
| -11 | 1  | 7 | 214   | 162   | 4   | 3  | 7 | 122  | 103  | 1   | 6  | 7 | 428  | 398  | -7  | 10 | 7   | 95   | 82   | 4   | -14 | 8 | 11    | 0     |
| -10 | 1  | 7 | 3     | 3     | 5   | 3  | 7 | 87   | 73   | 2   | 6  | 7 | 931  | 405  | -6  | 10 | 7   | 101  | 114  | 5   | -14 | 8 | 18    | 27    |
| -9  | 1  | 7 | 230   | 304   | 6   | 3  | 7 | 7    | 13   | 3   | 6  | 7 | 29   | 715  | -5  | 10 | 7   | 36   | 40   | 6   | -14 | 8 | 11    | 16    |
| -8  | 1  | 7 | 1006  | 1383  | 7   | 3  | 7 | 137  | 138  | 4   | 6  | 7 | 29   | 24   | -4  | 10 | 7   | 61   | 68   | 7   | -14 | 8 | 13    | 19    |
| -7  | 1  | 7 | 2845  | 3276  | 8   | 3  | 7 | 47   | 44   | 5   | 6  | 7 | 51   | 14   | -3  | 10 | 7   | 61   | 68   | 7   | -14 | 8 | 13    | 19    |
| -6  | 1  | 7 | 860   | 770   | 9   | 3  | 7 | 3    | 2    | 6   | 6  | 7 | 76   | 69   | -2  | 10 | 7   | 137  | 116  | 8   | -14 | 8 | 123   | 140   |
| -5  | 1  | 7 | 1999  | 1801  | -15 | 4  | 7 | 3    | 2    | -9  | 7  | 8 | 1262 | 1241 | 7   | -5 | 8   | 28   | 25   | -4  | -2  | 8 | 7671  | 7276  |
| -4  | 1  | 7 | 40    | 44    | -4  | 10 | 8 | 2    | 257  | -8  | -7 | 8 | 9    | 43   | 8   | -5 | 8   | 25   | 11   | -3  | -2  | 8 | 1253  | 1243  |
| -3  | 1  | 7 | 68    | 60    | -3  | 10 | 8 | 247  | 360  | -7  | -7 | 8 | 917  | 1025 | 9   | -5 | 8   | 25   | 31   | -2  | -2  | 8 | 10317 | 10543 |
| -2  | 1  | 7 | 32    | 16    | -2  | 10 | 8 | 357  | 316  | -6  | -7 | 8 | 19   | 148  | 11  | -5 | 8   | 26   | 36   | -1  | -2  | 8 | 225   | 244   |
| -1  | 1  | 7 | 33    | 16    | -1  | 10 | 8 | 204  | 220  | -5  | -7 | 8 | 125  | 148  | 11  | -5 | 8   | 26   | 46   | 0   | -2  | 8 | 1451  | 1835  |
| 0   | 1  | 7 | 55    | 76    | 0   | 10 | 8 | 170  | 135  | -4  | -7 | 8 | 2    | 4    | -14 | -4 | 8   | 26   | 12   | 1   | -2  | 8 | 11541 | 10218 |
| 1   | 1  | 7 | 68    | 58    | 1   | 10 | 8 | 170  | 135  | -3  | -7 | 8 | 328  | 201  | -13 | -4 | 8   | 11   | 39   | 2   | -2  | 8 | 166   | 74    |
| 2   | 1  | 7 | 51    | 66    | 2   | 10 | 8 | 51   | 77   | -2  | -7 | 8 | 1686 | 1264 | -12 | -4 | 8   | 40   | 39   | 2   | -2  | 8 | 271   | 182   |
| 3   | 1  | 7 | 409   | 445   | 3   | 10 | 8 | 118  | 137  | -1  | -7 | 8 | 3047 | 2245 | -11 | -4 | 8   | 37   | 35   | 3   | -2  | 8 | 95    | 235   |
| 4   | 1  | 7 | 466   | 476   | 4   | 10 | 8 | 28   | 32   | 0   | -7 | 8 | 311  | 443  | -10 | -4 | 8   | 0    | 2    | 4   | -2  | 8 | 249   | 235   |
| 5   | 1  | 7 | 1422  | 1434  | 5   | 10 | 8 | 244  | 365  | 1   | -7 | 8 | 1536 | 1384 | -9  | -4 | 8   | 315  | 367  | 5   | -2  | 8 | 7     | 18    |
| 6   | 1  | 7 | 70    | 59    | 6   | 10 | 8 | 123  | 117  | 2   | -7 | 8 | 774  | 839  | -8  | -4 | 8   | 7    | 1    | 6   | -2  | 8 | 965   | 909   |
| 7   | 1  | 7 | 193   | 187   | 7   | 10 | 8 | 9    | 1    | 3   | -7 | 8 | 53   | 46   | -7  | -4 | 8   | 1796 | 1859 | 7   | -2  | 8 | 34    | 32    |
| 8   | 1  | 7 | 23    | 39    | 8   | 10 | 8 | 24   | 8    | 4   | -7 | 8 | 637  | 519  | -6  | -4 | 8   | 296  | 149  | 8   | -2  | 8 | 92    | 118   |
| 9   | 1  | 7 | 336   | 202   | 10  | 10 | 8 | 38   | 31   | 5   | -7 | 8 | 1271 | 1022 | -5  | -4 | 8   | 2568 | 2317 | 10  | -2  | 8 | 30    | 32    |
| 10  | 1  | 7 | 7     | 3     | 11  | 10 | 8 | 46   | 31   | 6   | -7 | 8 | 376  | 424  | -4  | -4 | 8   | 157  | 239  | -14 | -1  | 8 | 103   | 135   |
| 11  | 1  | 7 | 77    | 45    | -11 | -9 | 8 | 91   | 57   | 7   | -7 | 8 | 336  | 315  | -3  | -4 | 8</ |      |      |     |     |   |       |       |



Table C.3, continued

| M     | K | L    | Obs  | Calc    | M    | K    | L       | Obs   | Calc  | M       | K    | L    | Obs      | Calc | M    | K      | L | Obs  | Calc | M       | K    | L    | Obs     | Calc |      |         |      |      |          |      |      |
|-------|---|------|------|---------|------|------|---------|-------|-------|---------|------|------|----------|------|------|--------|---|------|------|---------|------|------|---------|------|------|---------|------|------|----------|------|------|
| -1-11 | 0 | 761  | 616  | -4-0-0  | 342  | 361  | -12-5-0 | 42    | 31    | 2-3-0   | 3468 | 3082 | -9-0-0   | 1463 | 1286 | 0-11   | 0 | 22   | 0    | -3-0-0  | 109  | 126  | -11-5-0 | 342  | 311  | 3-3-0   | 1284 | 1345 | -8-0-0   | 1235 | 905  |
| 0-11  | 0 | 22   | 0    | -3-0-0  | 109  | 126  | -11-5-0 | 342   | 311   | 3-3-0   | 1284 | 1345 | -8-0-0   | 1235 | 905  | 1-11   | 0 | 501  | 538  | -2-0-0  | 879  | 1109 | -10-5-0 | 29   | 27   | 4-3-0   | 221  | 258  | -7-0-0   | 45   | 67   |
| 1-11  | 0 | 501  | 538  | -2-0-0  | 879  | 1109 | -10-5-0 | 29    | 27    | 4-3-0   | 221  | 258  | -7-0-0   | 45   | 67   | 2-11   | 0 | 289  | 251  | -1-0-0  | 286  | 456  | -9-5-0  | 444  | 512  | 5-3-0   | 122  | 77   | -6-0-0   | 202  | 180  |
| 2-11  | 0 | 289  | 251  | -1-0-0  | 286  | 456  | -9-5-0  | 444   | 512   | 5-3-0   | 122  | 77   | -6-0-0   | 202  | 180  | 3-11   | 0 | 88   | 65   | 0-0-0   | 1804 | 1299 | -8-5-0  | 121  | 55   | 6-3-0   | 161  | 144  | -5-0-0   | 37   | 1    |
| 4-11  | 0 | 88   | 65   | 0-0-0   | 1804 | 1299 | -8-5-0  | 121   | 55    | 6-3-0   | 161  | 144  | -5-0-0   | 37   | 1    | 5-11   | 0 | 68   | 114  | 2-0-0   | 890  | 652  | -7-5-0  | 256  | 352  | 7-3-0   | 6    | 3    | -4-0-0   | 444  | 270  |
| 5-11  | 0 | 68   | 114  | 2-0-0   | 890  | 652  | -7-5-0  | 256   | 352   | 7-3-0   | 6    | 3    | -4-0-0   | 444  | 270  | 6-11   | 0 | 300  | 209  | 3-0-0   | 405  | 375  | -6-5-0  | 1548 | 1467 | 8-3-0   | 126  | 133  | -3-0-0   | 769  | 586  |
| 7-11  | 0 | 143  | 219  | 4-0-0   | 76   | 111  | -4-5-0  | 7     | 0     | 10-3-0  | 0    | 0    | -1-0-0   | 2430 | 1606 | 8-11   | 0 | 140  | 164  | 5-0-0   | 104  | 154  | -3-5-0  | 741  | 587  | 11-3-0  | 27   | 17   | 0-0-0    | 888  | 996  |
| 9-11  | 0 | 9    | 11   | 6-0-0   | 321  | 360  | -2-5-0  | 958   | 1002  | -14-2-0 | 33   | 3    | 2-0-0    | 1144 | 1025 | 10-11  | 0 | 43   | 71   | 7-0-0   | 160  | 106  | -1-5-0  | 2751 | 2444 | -13-2-0 | 6    | 3    | 2-0-0    | 232  | 331  |
| 11-11 | 0 | 4    | 2    | 8-0-0   | 6    | 6    | 0-5-0   | 16319 | 15003 | -12-2-0 | 140  | 136  | 3-0-0    | 1076 | 1028 | -10-10 | 0 | 54   | 50   | 9-0-0   | 4    | 10   | 1-5-0   | 412  | 602  | -11-2-0 | 451  | 410  | 4-0-0    | 24   | 7    |
| -9-10 | 0 | 12   | 10   | 10-0-0  | 1    | 0    | 2-5-0   | 2343  | 2067  | -10-2-0 | 190  | 212  | 5-0-0    | 284  | 285  | -8-10  | 0 | 19   | 12   | 11-0-0  | 79   | 89   | 3-5-0   | 127  | 154  | -9-2-0  | 67   | 51   | 6-0-0    | 0    | 1    |
| -8-10 | 0 | 25   | 8    | -12-7-0 | 151  | 14   | 4-5-0   | 1441  | 1204  | -8-2-0  | 91   | 69   | 7-0-0    | 1936 | 1762 | -7-10  | 0 | 25   | 8    | -12-7-0 | 151  | 14   | 4-5-0   | 1441 | 1204 | -8-2-0  | 91   | 69   | 7-0-0    | 1936 | 1762 |
| -6-10 | 0 | 80   | 46   | -11-7-0 | 151  | 14   | 4-5-0   | 1441  | 1204  | -8-2-0  | 91   | 69   | 7-0-0    | 1936 | 1762 | -5-10  | 0 | 17   | 23   | -10-7-0 | 151  | 14   | 4-5-0   | 1441 | 1204 | -8-2-0  | 91   | 69   | 7-0-0    | 1936 | 1762 |
| -15-1 | 0 | 94   | 115  | 2-3-0   | 348  | 248  | 2-6-0   | 231   | 185   | -9-11-0 | 46   | 41   | 9-13-0   | 13   | 13   | -14-1  | 0 | 15   | 24   | 3-3-0   | 415  | 328  | 3-6-0   | 5    | 5    | -7-11-0 | 100  | 89   | -9-12-0  | 36   | 46   |
| -13-1 | 0 | 364  | 274  | 4-3-0   | 35   | 43   | 4-6-0   | 189   | 189   | -7-11-0 | 100  | 89   | -9-12-0  | 36   | 46   | -12-1  | 0 | 2    | 5    | 3-3-0   | 108  | 56   | 5-6-0   | 1    | 4    | -6-11-0 | 60   | 46   | -8-12-0  | 9    | 5    |
| -11-1 | 0 | 21   | 19   | 6-3-0   | 102  | 47   | -13-7-0 | 47    | 21    | -5-11-0 | 253  | 253  | -7-12-0  | 186  | 194  | -10-1  | 0 | 209  | 139  | 7-3-0   | -4   | 4    | -12-7-0 | 572  | 610  | -4-11-0 | 38   | 36   | -6-12-0  | 69   | 47   |
| -10-1 | 0 | 46   | 67   | 8-3-0   | 130  | 108  | -11-7-0 | 17    | 1     | -3-11-0 | 216  | 194  | -5-12-0  | 43   | 41   | -9-1   | 0 | 239  | 141  | -14-4-0 | 4    | 13   | -10-7-0 | 4    | 9    | -2-11-0 | 207  | 204  | -4-12-0  | 196  | 128  |
| -8-1  | 0 | 384  | 566  | -13-4-0 | 24   | 11   | -9-7-0  | 402   | 339   | 0-17-0  | 36   | 5    | -3-12-0  | 45   | 57   | -6-1   | 0 | 2334 | 2934 | -12-4-0 | 528  | 194  | -7-7-0  | 284  | 282  | 2-17-0  | 28   | 12   | -1-12-0  | 237  | 273  |
| -6-1  | 0 | 140  | 96   | -11-4-0 | 236  | 359  | -6-7-0  | 39    | 10    | 3-17-0  | -5   | 9    | 0-12-0   | 1314 | 1154 | -5-1   | 0 | 57   | 101  | -10-4-0 | 447  | 359  | -6-7-0  | 39   | 10   | 3-17-0  | -5   | 9    | 0-12-0   | 1314 | 1154 |
| -4-1  | 0 | 939  | 902  | -9-4-0  | 116  | 144  | -5-7-0  | 203   | 178   | -3-16-0 | 15   | 4    | 1-12-0   | 236  | 263  | -2-1   | 0 | 3693 | 3536 | -8-4-0  | 416  | 388  | -4-7-0  | 33   | 7    | -1-16-0 | 19   | 18   | 2-12-0   | 1130 | 759  |
| -2-1  | 0 | 3693 | 3536 | -8-4-0  | 416  | 388  | -4-7-0  | 33    | 7     | -1-16-0 | 19   | 18   | 2-12-0   | 1130 | 759  | -1-1   | 0 | 151  | 303  | -7-4-0  | 40   | 31   | -3-7-0  | 444  | 569  | -1-16-0 | 19   | 18   | 2-12-0   | 1130 | 759  |
| 0-1   | 0 | 9    | 9    | -6-4-0  | 592  | 485  | -2-7-0  | 12    | 10    | 0-16-0  | 20   | 2    | 4-12-0   | 35   | 33   | 0-1    | 0 | 433  | 373  | -5-4-0  | 305  | 197  | -1-7-0  | 194  | 186  | 1-16-0  | 10   | 2    | 5-12-0   | 63   | 84   |
| 1-1   | 0 | 433  | 373  | -5-4-0  | 305  | 197  | -1-7-0  | 194   | 186   | 1-16-0  | 10   | 2    | 5-12-0   | 63   | 84   | 2-1    | 0 | 30   | 20   | -4-4-0  | 25   | 2    | 0-7-0   | 8    | 7    | 2-16-0  | 33   | 36   | 6-12-0   | 53   | 85   |
| 3-1   | 0 | 248  | 224  | -3-4-0  | 259  | 454  | 1-7-0   | 157   | 106   | 3-16-0  | 25   | 9    | 7-12-0   | 277  | 303  | 4-1    | 0 | 42   | 52   | -2-4-0  | 191  | 181  | 2-7-0   | 12   | 1    | 4-16-0  | 117  | 178  | 8-12-0   | 32   | 8    |
| 4-1   | 0 | 42   | 52   | -2-4-0  | 191  | 181  | 2-7-0   | 12    | 1     | 4-16-0  | 117  | 178  | 8-12-0   | 32   | 8    | 5-1    | 0 | 152  | 203  | -1-4-0  | 547  | 679  | 3-7-0   | 37   | 29   | 5-16-0  | 5    | 15   | 9-12-0   | 57   | 24   |
| 6-1   | 0 | 152  | 203  | -1-4-0  | 547  | 679  | 3-7-0   | 37    | 29    | 5-16-0  | 5    | 15   | 9-12-0   | 57   | 24   | 7-1    | 0 | 24   | 23   | 1-4-0   | 85   | 122  | 4-7-0   | -8   | 0    | 6-16-0  | 7    | 13   | 10-12-0  | 13   | 2    |
| 8-1   | 0 | 19   | 12   | 2-4-0   | 254  | 166  | -12-8-0 | 144   | 139   | -4-15-0 | 10   | 18   | -9-11-0  | 1    | 11   | 9-1    | 0 | 1    | 7    | 3-4-0   | 4    | 13   | -10-8-0 | 12   | 3    | -5-15-0 | 52   | 90   | -10-11-0 | 18   | 6    |
| 9-1   | 0 | 1    | 7    | 3-4-0   | 4    | 13   | -10-8-0 | 12    | 3     | -5-15-0 | 52   | 90   | -10-11-0 | 18   | 6    | -14    | 0 | 12   | 0    | 4-4-0   | 59   | 64   | -9-8-0  | 27   | 58   | -1-15-0 | 19   | 29   | -6-11-0  | 695  | 607  |
| -15-2 | 0 | 12   | 0    | 4-4-0   | 12   | 3    | -10-8-0 | 142   | 120   | -2-15-0 | 6    | 1    | -7-11-0  | 39   | 39   | -13-2  | 0 | 277  | 374  | 6-4-0   | 12   | 13   | -8-8-0  | 47   | 45   | 0-15-0  | -2   | 0    | -5-11-0  | 243  | 228  |
| -14-2 | 0 | 87   | 86   | 5-4-0   | 59   | 64   | -9-8-0  | 27    | 58    | -1-15-0 | 19   | 29   | -6-11-0  | 695  | 607  | -12-2  | 0 | 168  | 135  | 7-4-0   | 6    | 26   | -7-8-0  | 281  | 270  | 1-15-0  | 46   | 70   | -4-11-0  | 242  | 290  |
| -11-2 | 0 | 29   | 25   | -14-5-0 | 66   | 63   | -6-8-0  | 35    | 26    | 2-15-0  | 92   | 94   | -3-11-0  | 285  | 272  | -10-2  | 0 | 347  | 250  | -13-5-0 | 1    | 1    | -5-8-0  | 26   | 29   | 3-15-0  | 45   | 49   | -2-11-0  | 30   | 9    |
| -10-2 | 0 | 347  | 250  | -13-5-0 | 1    | 1    | -5-8-0  | 26    | 29    | 3-15-0  | 45   | 49   | -2-11-0  | 30   | 9    | -9-2   | 0 | 32   | 54   | -11-5-0 | 77   | 55   | -3-8-0  | 197  | 210  | 5-15-0  | 13   | 16   | 0-11-0   | 14   | 27   |
| -8-2  | 0 | 471  | 423  | -11-5-0 | 77   | 55   | -3-8-0  | 197   | 210   | 5-15-0  | 13   | 16   | 0-11-0   | 14   | 27   | -6-2   | 0 | 126  | 140  | -10-5-0 | 109  | 110  | -2-8-0  | 31   | 27   | 6-15-0  | 79   | 71   | 1-11-0   | -2   | 0    |
| -7-2  | 0 | 126  | 140  | -10-5-0 | 109  | 110  | -2-8-0  | 31    | 27    | 6-15-0  | 79   | 71   | 1-11-0   | -2   | 0    | -5-2   | 0 | 1771 | 1783 | -9-5-0  | 685  | 548  | -1-8-0  | 129  | 38   | -6-14-0 | 0    | 11   | 2-11-0   | 103  | 142  |
| -6-2  | 0 | 1771 | 1783 | -9-5-0  | 685  | 548  | -1-8-0  | 129   | 38    | -6-14-0 | 0    | 11   | 2-11-0   | 103  | 142  | -4-2   | 0 | 343  | 251  | -8-5-0  | 224  | 343  | 0-8-0   | 27   | 38   | -5-14-0 | 45   | 55   | 4-11-0   | 1249 | 1361 |
| -5-2  | 0 | 343  | 251  | -8-5-0  | 224  | 343  | 0-8-0   | 27    | 38    | -5-14-0 | 45   | 55   | 4-11-0   | 1249 | 1361 | -3-2   | 0 | 1569 | 1809 | -7-5-0  | 583  | 562  | 1-8-0   | 357  | 272  | -5-14-0 | 45   | 55   | 4-11-0   | 1249 | 1361 |
| -2-2  | 0 | 685  | 504  | -6-5-0  | 59   | 37   | 2-8-0   | 98    | 73    | -4-14-0 | 10   | 9    | 5-11-0   | 340  | 267  | -2-2   | 0 | 122  | 103  | -5-5-0  | 117  | 184  | 3-8-0   | 37   | 26   | -3-14-0 | 2    | 8    | 6-11-0   | 11   | 1    |
| 0-2   | 0 | 830  | 895  | -4-5-0  | 707  | 614  | -12-9-0 | 70    | 85    | -2-14-0 | 26   | 48   | 7-11-0   | 85   | 56   | 1-2    | 0 | 830  | 895  | -4-5-0  | 707  | 614  | -12-9-0 | 70   | 85   | -2-14-0 | 26   | 48   | 7-11-0   | 85   | 56   |
| 0-2   | 0 | 1    | 9    | -3-5-0  | 294  | 282  | -11-9-0 | 18    | 36    | -1-14-0 | 96   | 74   | 8-11-0   | -5   | 5    | 1-2    | 0 | 239  | 207  | -2-5-0  | 301  | 402  | -10-9-0 | -3   | 1    | 0-14-0  | 53   | 65   | 9-11-0   | 68   | 78   |
| 1-2   | 0 | 239  | 207  | -2-5-0  | 301  | 402  | -10-9-0 | -3    | 1     | 0-14-0  | 53   | 65   | 9-11-0   | 68   | 78   | 2-2    | 0 | 655  | 462  | 0-5-0   | 5    | 3    | -8-9-0  | 8    | 18   | 2-14-0  | 318  | 266  | -10-10-0 | 56   | 85   |
| 2-2   | 0 | 655  | 462  | 0-5-0   | 5    | 3    | -8-9-0  | 8     | 18    | 2-14-0  | 318  | 266  | -10-10-0 | 56   | 85   | 4-2    | 0 | 53   | 63   | 1-5-0   | 220  | 116  | -7-9-0  | 314  | 287  | 3-14-0  | 42   | 31   | -9-10-0  | 19   | 20   |
| 5-2   | 0 | 867  | 816  | 2-5-0   | 614  | 565  | -6-9-0  | 7     | 5     | 4-14-0  | 76   | 76   | -8-10-0  | 42   | 32   | 6-2    | 0 | 21   | 30   | 3-5-0   | 234  | 136  | -5-9-0  | 219  | 237  | 5-14-0  | 61   | 81   | -7-10-0  | 107  | 109  |
| 7-2   | 0 | 296  | 220  | 4-5-0   | 76   | 60   | -4-9-0  | 6     | 1     | 6-14-0  | 254  | 249  | -6-10-0  | 67   | 70   | 8-2    | 0 | 52   | 48   | 5-5-0   | 4    | 8    | -3-9-0  | 119  | 114  | 7-14-0  | 2    | 10   | -4-10-0  | 55   | 59   |
| 8-2   | 0 | 52   | 48   | 5-5-0   | 4    | 8    | -3-9-0  | 119   | 114   | 7-14-0  | 2    | 10   | -4-10-0  | 55   | 59   | -13-3  | 0 | 165  | 141  | -14-6-0 | 106  | 124  | -1-9-0  | 90   | 56   | -8-13-0 | 37   | 28   | -3-10-0  | 10   | 2    |
| -15-3 | 0 | 18   | 13   | -13-6-0 | 25   | 20   | 0-9-0   | 308   | 248   | -7-13-0 | 6    | 3    | -2-10-0  | 626  | 629  | -13-3  | 0 | 104  | 107  | -12-6-0 | 325  | 351  | 1-9-0   | 29   | 29   | -6-13-0 | 80   | 107  | -1-10-0  | -3   | 1    |
| -12-3 | 0 | 104  | 107  | -12-6-0 | 325  | 351  | 1-9-0   | 29    | 29    | -6-13-0 | 80   | 107  | -1-10-0  | -3   | 1    | -10-3  | 0 | 31   | 25   | -11-6-0 | 459  | 485  | 2-9-0   | 69   | 84   | -5-13-0 | 89   | 103  | 0-10-0   | 2116 | 2017 |
| -11-3 | 0 | 31   | 25   | -11-6-0 | 459  | 485  | 2-9-0   | 69    | 84    | -5-13-0 | 89   | 103  | 0-10-0   | 2116 | 2017 | -9-3   | 0 | 41   | 118  |         |      |      |         |      |      |         |      |      |          |      |      |

Table C.3, continued

| M   | K  | L | Obe  | Calc | M   | K  | L | Obe  | Calc | M   | K   | L  | Obe  | Calc | M   | K   | L  | Obe  | Calc | M   | K  | L   | Obe  | Calc | M    | K    | L    | Obe | Calc |
|-----|----|---|------|------|-----|----|---|------|------|-----|-----|----|------|------|-----|-----|----|------|------|-----|----|-----|------|------|------|------|------|-----|------|
| -   | -  | - | -    | -    | -   | -  | - | -    | -    | -   | -   | -  | -    | -    | -   | -   | -  | -    | -    | -   | -  | -   | -    | -    | -    | -    | -    | -   |      |
| 9   | -9 | 9 | 41   | 41   | 3   | -6 | 9 | 1749 | 1549 | -5  | -3  | 9  | 137  | 117  | -13 | 0   | 9  | -1   | 1    | 7   | 2  | 9   | -14  | 19   | 6    | 6    | 6    | 6   |      |
| 10  | -9 | 9 | 59   | 29   | 4   | -6 | 9 | 405  | 399  | -4  | -3  | 9  | 1460 | 1358 | -12 | 0   | 9  | 316  | 351  | 8   | 2  | 9   | 7    | 106  | 106  | 106  | 106  | 106 |      |
| -12 | -8 | 9 | 14   | 5    | 5   | -6 | 9 | 977  | 860  | -3  | -3  | 9  | 2681 | 2446 | -11 | 0   | 9  | 262  | 336  | -14 | 3  | 9   | 92   | 30   | 30   | 30   | 30   | 30  |      |
| -11 | -8 | 9 | 10   | 14   | 6   | -6 | 9 | 34   | 59   | -2  | -3  | 9  | 6877 | 6399 | -10 | 0   | 9  | 371  | 340  | -13 | 3  | 9   | 10   | 4    | 1    | 1    | 1    | 1   |      |
| -10 | -8 | 9 | 291  | 278  | 7   | -6 | 9 | 114  | 74   | 0   | -3  | 9  | 398  | 702  | -9  | 0   | 9  | 39   | 3    | -12 | 3  | 9   | 152  | 148  | 148  | 148  | 148  |     |      |
| -9  | -8 | 9 | -2   | 2    | 8   | -6 | 9 | 114  | 74   | 0   | -3  | 9  | 398  | 264  | -8  | 0   | 9  | 31   | 4    | -11 | 3  | 9   | 5    | 1    | 1    | 1    | 1    | 1   |      |
| -8  | -8 | 9 | 165  | 113  | 9   | -6 | 9 | 96   | 44   | 1   | -3  | 9  | 218  | 150  | -7  | 0   | 9  | 358  | 267  | -10 | 3  | 9   | 926  | 874  | 874  | 874  | 874  |     |      |
| -7  | -8 | 9 | 455  | 418  | 10  | -6 | 9 | 40   | 84   | 2   | -3  | 9  | 138  | 73   | -6  | 0   | 9  | 500  | 427  | -9  | 3  | 9   | 309  | 355  | 355  | 355  | 355  |     |      |
| -6  | -8 | 9 | 563  | 470  | -13 | -5 | 9 | 7    | 54   | 3   | -3  | 9  | 734  | 678  | -5  | 0   | 9  | 932  | 999  | -8  | 3  | 9   | 2038 | 2037 | 2037 | 2037 | 2037 |     |      |
| -5  | -8 | 9 | 6    | 5    | -12 | -5 | 9 | 7    | 9    | 4   | -3  | 9  | 1102 | 1056 | -4  | 0   | 9  | 1842 | 1618 | -7  | 3  | 9   | 171  | 307  | 307  | 307  | 307  |     |      |
| -4  | -8 | 9 | 1566 | 1913 | -11 | -5 | 9 | 28   | 9    | 5   | -3  | 9  | 6    | 4    | -3  | 0   | 9  | 1636 | 2040 | -6  | 3  | 9   | 65   | 96   | 96   | 96   | 96   |     |      |
| -3  | -8 | 9 | 19   | 35   | -10 | -5 | 9 | 300  | 258  | 6   | -3  | 9  | 827  | 685  | -2  | 0   | 9  | 720  | 571  | -5  | 3  | 9   | 917  | 865  | 865  | 865  | 865  |     |      |
| -2  | -8 | 9 | 468  | 456  | -9  | -5 | 9 | 55   | 52   | 7   | -3  | 9  | 26   | 23   | -1  | 0   | 9  | 2523 | 2101 | -4  | 3  | 9   | 952  | 981  | 981  | 981  | 981  |     |      |
| -1  | -8 | 9 | 365  | 323  | -8  | -5 | 9 | 710  | 733  | 8   | -3  | 9  | 28   | 21   | 0   | 0   | 9  | 1008 | 1004 | -3  | 3  | 9   | 106  | 65   | 65   | 65   | 65   |     |      |
| 0   | -8 | 9 | 34   | 18   | -7  | -5 | 9 | 876  | 826  | 9   | -3  | 9  | 21   | 29   | 1   | 0   | 9  | 24   | 33   | -2  | 3  | 9   | 101  | 42   | 42   | 42   | 42   |     |      |
| 1   | -8 | 9 | 1609 | 1432 | -6  | -5 | 9 | 1543 | 1805 | 10  | -3  | 9  | 65   | 67   | 3   | 0   | 9  | 255  | 317  | 0   | 3  | 9   | 55   | 105  | 105  | 105  | 105  |     |      |
| 2   | -8 | 9 | 71   | 42   | -5  | -5 | 9 | 123  | 145  | -14 | -2  | 9  | 24   | 34   | 4   | 0   | 9  | 116  | 53   | 1   | 3  | 9   | 160  | 154  | 154  | 154  | 154  |     |      |
| 3   | -8 | 9 | 594  | 623  | -4  | -5 | 9 | 360  | 384  | -13 | -2  | 9  | 105  | 68   | 5   | 0   | 9  | 9    | 15   | 2   | 3  | 9   | 14   | 1    | 1    | 1    | 1    |     |      |
| 4   | -8 | 9 | 11   | 5    | -3  | -5 | 9 | 231  | 193  | -12 | -2  | 9  | 72   | 52   | 6   | 0   | 9  | 28   | 32   | 3   | 3  | 9   | 58   | 15   | 15   | 15   | 15   |     |      |
| 5   | -8 | 9 | 862  | 874  | -2  | -5 | 9 | 226  | 276  | -11 | -2  | 9  | 654  | 601  | 7   | 0   | 9  | 23   | 22   | 5   | 3  | 9   | 135  | 137  | 137  | 137  | 137  |     |      |
| 6   | -8 | 9 | 135  | 173  | -1  | -5 | 9 | 860  | 733  | -10 | -2  | 9  | 11   | 15   | 8   | 0   | 9  | 11   | 2    | 6   | 3  | 9   | 15   | 2    | 2    | 2    | 2    |     |      |
| 7   | -8 | 9 | 459  | 458  | 0   | -5 | 9 | 412  | 492  | -9  | -2  | 9  | 227  | 261  | 9   | 0   | 9  | 73   | 74   | -14 | 4  | 9   | 42   | 52   | 52   | 52   | 52   |     |      |
| 8   | -8 | 9 | 95   | 76   | 1   | -5 | 9 | 1834 | 1549 | -8  | -2  | 9  | 50   | 38   | -14 | 1   | 9  | 73   | 118  | -13 | 4  | 9   | 107  | 93   | 93   | 93   | 93   |     |      |
| 9   | -8 | 9 | 261  | 254  | 2   | -5 | 9 | 535  | 565  | -7  | -2  | 9  | 29   | 12   | -13 | 1   | 9  | 134  | 119  | -12 | 4  | 9   | 13   | 6    | 6    | 6    | 6    |     |      |
| 10  | -8 | 9 | 12   | 9    | 3   | -5 | 9 | 107  | 144  | -6  | -2  | 9  | 122  | 121  | -12 | 1   | 9  | 311  | 191  | -12 | 4  | 9   | 324  | 270  | 270  | 270  | 270  |     |      |
| 11  | -8 | 9 | 6    | 16   | 4   | -5 | 9 | 131  | 96   | -5  | -2  | 9  | 129  | 138  | -11 | 1   | 9  | 66   | 73   | -11 | 4  | 9   | 0    | 0    | 0    | 0    | 0    |     |      |
| -12 | -7 | 9 | 62   | 34   | 5   | -5 | 9 | 96   | 63   | -4  | -2  | 9  | 153  | 2159 | -10 | 1   | 9  | 20   | 58   | -10 | 4  | 9   | 646  | 603  | 603  | 603  | 603  |     |      |
| -11 | -7 | 9 | 208  | 147  | 6   | -5 | 9 | 35   | 17   | -3  | -2  | 9  | 198  | 170  | -9  | 1   | 9  | 701  | 710  | -9  | 4  | 9   | 275  | 362  | 362  | 362  | 362  |     |      |
| -10 | -7 | 9 | -1   | 6    | 7   | -5 | 9 | 250  | 224  | -1  | -2  | 9  | 7    | 22   | -8  | 1   | 9  | 747  | 685  | -8  | 4  | 9   | 696  | 662  | 662  | 662  | 662  |     |      |
| -9  | -7 | 9 | 295  | 287  | 8   | -5 | 9 | 6    | 0    | 0   | -2  | 9  | 354  | 322  | -7  | 1   | 9  | 14   | 28   | -7  | 4  | 9   | 614  | 480  | 480  | 480  | 480  |     |      |
| -8  | -7 | 9 | 77   | 121  | 9   | -5 | 9 | 2    | 2    | 1   | -2  | 9  | 49   | 49   | -6  | 1   | 9  | 66   | 83   | -6  | 4  | 9   | 276  | 405  | 405  | 405  | 405  |     |      |
| -7  | -7 | 9 | 40   | 31   | 10  | -5 | 9 | 2    | 4    | 2   | -2  | 9  | 513  | 425  | -5  | 1   | 9  | 119  | 122  | -5  | 4  | 9   | 52   | 16   | 16   | 16   | 16   |     |      |
| -6  | -7 | 9 | 376  | 443  | -13 | -4 | 9 | 38   | 22   | 3   | -2  | 9  | 49   | 86   | -4  | 1   | 9  | 719  | 650  | -4  | 4  | 9   | 516  | 316  | 316  | 316  | 316  |     |      |
| -5  | -7 | 9 | 95   | 165  | -12 | -4 | 9 | 30   | 37   | 4   | -2  | 9  | 389  | 380  | -3  | 1   | 9  | 3414 | 3424 | -3  | 4  | 9   | 129  | 151  | 151  | 151  | 151  |     |      |
| -4  | -7 | 9 | 4    | 11   | -11 | -4 | 9 | 11   | 26   | 5   | -2  | 9  | 139  | 176  | -2  | 1   | 9  | 531  | 381  | -2  | 4  | 9   | 203  | 82   | 82   | 82   | 82   |     |      |
| -3  | -7 | 9 | 123  | 85   | -10 | -4 | 9 | 251  | 313  | 6   | -2  | 9  | 43   | 73   | -1  | 1   | 9  | 2069 | 1979 | -1  | 4  | 9   | 164  | 170  | 170  | 170  | 170  |     |      |
| -2  | -7 | 9 | 108  | 68   | -9  | -4 | 9 | 146  | 109  | 7   | -2  | 9  | 1345 | 1276 | 0   | 1   | 9  | 48   | 26   | 0   | 4  | 9   | 37   | 39   | 39   | 39   | 39   |     |      |
| -1  | -7 | 9 | 972  | 937  | -8  | -4 | 9 | 430  | 480  | 8   | -2  | 9  | 258  | 190  | 1   | 1   | 9  | 1288 | 1297 | 1   | 4  | 9   | 501  | 525  | 525  | 525  | 525  |     |      |
| 1   | -7 | 9 | 2549 | 2945 | -7  | -4 | 9 | 607  | 528  | 9   | -2  | 9  | 97   | 112  | 2   | 1   | 9  | 23   | 33   | 4   | 4  | 9   | 273  | 224  | 224  | 224  | 224  |     |      |
| 2   | -7 | 9 | 74   | 6    | -5  | -4 | 9 | 7    | 9    | 10  | -2  | 9  | 12   | 9    | 3   | 1   | 9  | 35   | 264  | 5   | 4  | 9   | 129  | 94   | 94   | 94   | 94   |     |      |
| 3   | -7 | 9 | 4    | 6    | -5  | -4 | 9 | 1355 | 1358 | -14 | -1  | 9  | 162  | 176  | 4   | 1   | 9  | 292  | 96   | 6   | 4  | 9   | 55   | 51   | 51   | 51   | 51   |     |      |
| 4   | -7 | 9 | 330  | 357  | -4  | -4 | 9 | 10   | 6    | -13 | -1  | 9  | 121  | 152  | 5   | 1   | 9  | 82   | 32   | -14 | 5  | 9   | 151  | 173  | 173  | 173  | 173  |     |      |
| 5   | -7 | 9 | 283  | 231  | -3  | -4 | 9 | 53   | 38   | -12 | -1  | 9  | 313  | 268  | 6   | 1   | 9  | 33   | 2    | -13 | 5  | 9   | 24   | 31   | 31   | 31   | 31   |     |      |
| 6   | -7 | 9 | 89   | 161  | -2  | -4 | 9 | 10   | 3    | -11 | -1  | 9  | 117  | 74   | 7   | 1   | 9  | 2    | 11   | -13 | 5  | 9   | 720  | 653  | 653  | 653  | 653  |     |      |
| 7   | -7 | 9 | 15   | 9    | -1  | -4 | 9 | 3021 | 2889 | -10 | -1  | 9  | 28   | 38   | 8   | 1   | 9  | 117  | 131  | -12 | 5  | 9   | 52   | 39   | 39   | 39   | 39   |     |      |
| 8   | -7 | 9 | -4   | 2    | 0   | -4 | 9 | 1565 | 1584 | -9  | -1  | 9  | 406  | 403  | -14 | 2   | 9  | 110  | 62   | -6  | 7  | 10  | 824  | 757  | 757  | 757  | 757  |     |      |
| 9   | -7 | 9 | 18   | 9    | 1   | -4 | 9 | 4264 | 3936 | -8  | -1  | 9  | 472  | 102  | -8  | 10  | 10 | 84   | 15   | -7  | 10 | 252 | 160  | 160  | 160  | 160  |      |     |      |
| -9  | 5  | 9 | 1054 | 929  | -9  | 9  | 9 | 390  | 340  | 0   | -13 | 10 | 137  | 332  | 9   | -10 | 10 | 27   | 15   | 7   | -7 | 10  | 56   | 11   | 11   | 11   | 11   |     |      |
| -8  | 5  | 9 | 75   | 77   | -8  | 9  | 9 | 13   | 2    | 1   | -13 | 10 | 335  | 73   | 10  | -10 | 10 | 14   | 19   | 8   | -7 | 10  | 96   | 61   | 61   | 61   | 61   |     |      |
| -7  | 5  | 9 | 1244 | 1145 | -7  | 9  | 9 | 26   | 53   | 2   | -13 | 10 | 80   | 14   | -11 | -9  | 10 | 30   | 28   | 9   | -7 | 10  | 74   | 64   | 64   | 64   | 64   |     |      |
| -6  | 5  | 9 | 20   | 185  | -6  | 9  | 9 | 171  | 130  | 3   | -13 | 10 | 25   | 30   | -10 | -9  | 10 | 9    | 1    | 10  | -7 | 10  | 63   | 62   | 62   | 62   | 62   |     |      |
| -5  | 5  | 9 | 446  | 394  | -4  | 9  | 9 | 208  | 189  | 5   | -13 | 10 | 466  | 329  | -9  | -9  | 10 | 36   | 71   | -13 | -6 | 10  | 0    | 0    | 0    | 0    | 0    |     |      |
| -4  | 5  | 9 | 118  | 85   | -3  | 9  | 9 | 77   | 117  | 6   | -13 | 10 | 58   | 82   | -8  | -9  | 10 | 620  | 544  | -12 | -6 | 10  | 4    | 1    | 1    | 1    | 1    |     |      |
| -3  | 5  | 9 | 358  | 392  | -2  | 9  | 9 | 345  | 362  | 7   | -13 | 10 | 10   | 9    | -7  | -9  | 10 | 3    | 2    | -11 | -6 | 10  | 81   | 50   | 50   | 50   | 50   |     |      |
| -2  | 5  | 9 | 69   | 43   | -1  | 9  | 9 | 203  | 171  | 8   | -13 | 10 | 33   | 15   | -6  | -9  | 10 | 163  | 170  | -10 | -6 | 10  | 65   | 101  | 101  | 101  | 101  |     |      |
| 0   | 5  | 9 | 374  | 516  | 0   | 9  | 9 | 311  | 384  | -9  | -12 | 10 | 10   | 1    | -5  | -9  | 10 | 13   | 51   | -8  | -6 | 10  | 86   | 85   | 85   | 85   | 85   |     |      |
| 1   | 5  | 9 | 45   | 76   | -10 | 10 | 9 | 22   | 19   | -8  | -12 | 10 | 111  | 138  | -4  | -9  | 10 | 64   | 46   | -7  | -6 | 10  | 888  | 658  | 658  | 658  | 658  |     |      |
| 3   | 5  | 9 | 194  | 105  | -9  | 10 | 9 | 2    | 97   | -7  | -12 | 10 | 22   | 112  | -2  | -9  | 10 | 2372 | 2456 | -6  | -6 | 10  | 596  | 434  | 434  | 434  | 434  |     |      |
| 4   | 5  | 9 | 20   | 6    | -8  | 10 | 9 | 105  | 97   | -6  | -12 | 10 | 88   | 193  | -1  | -9  | 10 | 1832 | 1986 | -5  | -6 | 10  | 889  | 968  | 968  | 968  | 968  |     |      |
| 5   | 5  | 9 | 150  | 62   | -7  | 10 | 9 | 41   | 26   | -5  | -12 | 10 | 179  | 271  | 0   | -9  | 10 | 1242 | 1087 | -4  | -6 | 10  | 66   | 40   | 40   | 40   | 40   |     |      |
| -13 | 6  | 9 | 274  | 276  | -6  | 10 | 9 | 168  | 183  | -4  | -12 | 10 | 241  | 89   | 1   | -9  | 10 | 1140 | 1178 | -3  | -6 | 10  | 184  | 175  | 175  | 175  | 175  |     |      |
| -12 | 6  | 9 | 40   | 46   | -5  | 10 | 9 | -2   | 0    | -3  |     |    |      |      |     |     |    |      |      |     |    |     |      |      |      |      |      |     |      |

Table C.3, continued

| M   | K  | L  | Obs  | Calc | M   | K   | L  | Obs  | Calc | M   | K   | L  | Obs  | Calc | M   | K  | L  | Obs  | Calc | M   | K   | L  | Obs  | Calc |
|-----|----|----|------|------|-----|-----|----|------|------|-----|-----|----|------|------|-----|----|----|------|------|-----|-----|----|------|------|
| -6  | 0  | 9  | 347  | 364  | 6   | -14 | 10 | 153  | 161  | -3  | -10 | 10 | 187  | 176  | -5  | -7 | 10 | 1351 | 1169 | -11 | -4  | 10 | 709  | 713  |
| -5  | 0  | 9  | 126  | 97   | 7   | -14 | 10 | 33   | 15   | -2  | -10 | 10 | 1911 | 1630 | -4  | -7 | 10 | 66   | 69   | -10 | -4  | 10 | 3    | 4    |
| -4  | 0  | 9  | 280  | 285  | 8   | -14 | 10 | 19   | 30   | -1  | -10 | 10 | 1316 | 1339 | -3  | -7 | 10 | 449  | 532  | -9  | -4  | 10 | 275  | 227  |
| -3  | 0  | 9  | 1    | 15   | -8  | -13 | 10 | 82   | 47   | 0   | -10 | 10 | 11   | 19   | -2  | -7 | 10 | 80   | 74   | -8  | -4  | 10 | 7    | 15   |
| -2  | 0  | 9  | 537  | 517  | -7  | -13 | 10 | 30   | 21   | 1   | -10 | 10 | 1463 | 1274 | -1  | -7 | 10 | 1089 | 1001 | -7  | -4  | 10 | 34   | 23   |
| -1  | 0  | 9  | 157  | 159  | -6  | -13 | 10 | -2   | 1    | 2   | -10 | 10 | 116  | 101  | 0   | -7 | 10 | 212  | 167  | -6  | -4  | 10 | 76   | 550  |
| 0   | 0  | 9  | 5    | 7    | -5  | -13 | 10 | 25   | 23   | 3   | -10 | 10 | 146  | 146  | 1   | -7 | 10 | 3    | 6    | -5  | -4  | 10 | 496  | 548  |
| 1   | 0  | 9  | -7   | 0    | -4  | -13 | 10 | 5    | 1    | 4   | -10 | 10 | 19   | 43   | 2   | -7 | 10 | 323  | 414  | -4  | -4  | 10 | -2   | 8    |
| 2   | 0  | 9  | 9    | 4    | -3  | -13 | 10 | 0    | 15   | 5   | -10 | 10 | 724  | 857  | 3   | -7 | 10 | 41   | 86   | -3  | -4  | 10 | 2576 | 2157 |
| -11 | 9  | 9  | 82   | 2    | -2  | -13 | 10 | 13   | 1    | 6   | -10 | 10 | 99   | 91   | 4   | -7 | 10 | 797  | 780  | -2  | -4  | 10 | 482  | 279  |
| -10 | 9  | 9  | 119  | 129  | -1  | -13 | 10 | 20   | 10   | 7   | -10 | 10 | 38   | 37   | 5   | -7 | 10 | -2   | 8    | -1  | -4  | 10 | 1083 | 1093 |
| 0   | -4 | 10 | 770  | 705  | -6  | -1  | 10 | 366  | 489  | -8  | 2   | 10 | 129  | 113  | -4  | 5  | 10 | 913  | 920  | -2  | -16 | 11 | 15   | 7    |
| 1   | -4 | 10 | 3023 | 3149 | -5  | -1  | 10 | 66   | 46   | -7  | 2   | 10 | 7    | 27   | -3  | 5  | 10 | 429  | 417  | -1  | -16 | 11 | 21   | 4    |
| 2   | -4 | 10 | 480  | 463  | -4  | -1  | 10 | 1197 | 1256 | -6  | 2   | 10 | 1631 | 1407 | -2  | 5  | 10 | 128  | 125  | 0   | -16 | 11 | 2    | 1    |
| 3   | -4 | 10 | 35   | 35   | -3  | -1  | 10 | 494  | 469  | -5  | 2   | 10 | 472  | 335  | -1  | 5  | 10 | 110  | 80   | 1   | -16 | 11 | 11   | 18   |
| 4   | -4 | 10 | 30   | 21   | -2  | -1  | 10 | 941  | 543  | -4  | 2   | 10 | 1261 | 1176 | 0   | 5  | 10 | 37   | 32   | 2   | -16 | 11 | 36   | 14   |
| 5   | -4 | 10 | 139  | 214  | -1  | -1  | 10 | 89   | 49   | -3  | 2   | 10 | 332  | 435  | 1   | 5  | 10 | 46   | 40   | 3   | -16 | 11 | 137  | 103  |
| 6   | -4 | 10 | 98   | 86   | 0   | -1  | 10 | 916  | 942  | -2  | 2   | 10 | 800  | 868  | 2   | 5  | 10 | 0    | 7    | 4   | -16 | 11 | 77   | 34   |
| 7   | -4 | 10 | 87   | 94   | 1   | -1  | 10 | 10   | 3    | -1  | 2   | 10 | 25   | 26   | 3   | 5  | 10 | 244  | 245  | 5   | -16 | 11 | 3    | 6    |
| 8   | -4 | 10 | 14   | 11   | 2   | -1  | 10 | 335  | 327  | 0   | 2   | 10 | 120  | 174  | 4   | 5  | 10 | 22   | 31   | -5  | -15 | 11 | 14   | 24   |
| 9   | -4 | 10 | -3   | 0    | 3   | -1  | 10 | 785  | 852  | 1   | 2   | 10 | 22   | 8    | -13 | 6  | 10 | 59   | 111  | -4  | -15 | 11 | 11   | 3    |
| -14 | -3 | 10 | 50   | 56   | 4   | -1  | 10 | 5    | 1    | 2   | 2   | 10 | 146  | 106  | -12 | 6  | 10 | 66   | 59   | -3  | -15 | 11 | -4   | 6    |
| -13 | -3 | 10 | 227  | 214  | 5   | -1  | 10 | 22   | 42   | 3   | 2   | 10 | 69   | 72   | -11 | 6  | 10 | 85   | 107  | -2  | -15 | 11 | 7    | 3    |
| -12 | -3 | 10 | 92   | 60   | 6   | -1  | 10 | 16   | 17   | 4   | 2   | 10 | 65   | 75   | -10 | 6  | 10 | 203  | 205  | -1  | -15 | 11 | 2    | 3    |
| -11 | -3 | 10 | 177  | 181  | 7   | -1  | 10 | 35   | 8    | 5   | 2   | 10 | 123  | 85   | -9  | 6  | 10 | 329  | 360  | 0   | -15 | 11 | 20   | 23   |
| -10 | -3 | 10 | 2    | 7    | 8   | -1  | 10 | 11   | 4    | 6   | 2   | 10 | 16   | 0    | -8  | 6  | 10 | 132  | 131  | 1   | -15 | 11 | 37   | 40   |
| -9  | -3 | 10 | 243  | 253  | -14 | 0   | 10 | 4    | 3    | 7   | 2   | 10 | 6    | 13   | -7  | 6  | 10 | 37   | 24   | 2   | -15 | 11 | 53   | 45   |
| -8  | -3 | 10 | 14   | 24   | -13 | 0   | 10 | 108  | 141  | -14 | 3   | 10 | -1   | 18   | -6  | 6  | 10 | 35   | 39   | 3   | -15 | 11 | -7   | 1    |
| -7  | -3 | 10 | 108  | 202  | -12 | 0   | 10 | 39   | 26   | -13 | 3   | 10 | 117  | 104  | -5  | 6  | 10 | 81   | 99   | 4   | -15 | 11 | 47   | 49   |
| -6  | -3 | 10 | 12   | 30   | -11 | 0   | 10 | 662  | 604  | -12 | 3   | 10 | 85   | 95   | -4  | 6  | 10 | 195  | 195  | 5   | -15 | 11 | 14   | 18   |
| -5  | -3 | 10 | 165  | 233  | -10 | 0   | 10 | 40   | 33   | -11 | 3   | 10 | 191  | 204  | -3  | 6  | 10 | 1271 | 1175 | 6   | -15 | 11 | 0    | 2    |
| -4  | -3 | 10 | 154  | 121  | -9  | 0   | 10 | 67   | 28   | -10 | 3   | 10 | 490  | 495  | -2  | 6  | 10 | 69   | 76   | -6  | -14 | 11 | 26   | 24   |
| -3  | -3 | 10 | 1364 | 1422 | -8  | 0   | 10 | 224  | 254  | -9  | 3   | 10 | 62   | 91   | -1  | 6  | 10 | 654  | 657  | -5  | -14 | 11 | 38   | 20   |
| -2  | -3 | 10 | 684  | 442  | -7  | 0   | 10 | 855  | 752  | -8  | 3   | 10 | 186  | 157  | 0   | 6  | 10 | 292  | 232  | -4  | -14 | 11 | 43   | 78   |
| -1  | -3 | 10 | 825  | 681  | -6  | 0   | 10 | 22   | 23   | -7  | 3   | 10 | 213  | 224  | 1   | 6  | 10 | 48   | 46   | -3  | -14 | 11 | 114  | 86   |
| 0   | -3 | 10 | 128  | 250  | -5  | 0   | 10 | 57   | 78   | -6  | 3   | 10 | 2978 | 2196 | 2   | 6  | 10 | 57   | 62   | -2  | -14 | 11 | 42   | 25   |
| 1   | -3 | 10 | 92   | 89   | -4  | 0   | 10 | 573  | 421  | -5  | 3   | 10 | 29   | 0    | 3   | 6  | 10 | 0    | 0    | -1  | -14 | 11 | 165  | 165  |
| 2   | -3 | 10 | 193  | 219  | -3  | 0   | 10 | 0    | 25   | -4  | 3   | 10 | 2231 | 2130 | -12 | 7  | 10 | 4    | 3    | 0   | -14 | 11 | -1   | 1    |
| 3   | -3 | 10 | 3    | 0    | -2  | 0   | 10 | 833  | 962  | -3  | 3   | 10 | 12   | 5    | -11 | 7  | 10 | -5   | 0    | 1   | -14 | 11 | 165  | 171  |
| 4   | -3 | 10 | 15   | 7    | -1  | 0   | 10 | 25   | 52   | -2  | 3   | 10 | 788  | 952  | -10 | 7  | 10 | 102  | 105  | 2   | -14 | 11 | 31   | 15   |
| 5   | -3 | 10 | -2   | 1    | 0   | 0   | 10 | 1106 | 1385 | -1  | 3   | 10 | 7    | 2    | -9  | 7  | 10 | 8    | 3    | 3   | -14 | 11 | 160  | 140  |
| 6   | -3 | 10 | 196  | 181  | 1   | 0   | 10 | 93   | 71   | 0   | 3   | 10 | 248  | 190  | -8  | 7  | 10 | 144  | 109  | 4   | -14 | 11 | 19   | 44   |
| 7   | -3 | 10 | 25   | 17   | 2   | 0   | 10 | 774  | 522  | 1   | 3   | 10 | 58   | 90   | -7  | 7  | 10 | 52   | 61   | 5   | -14 | 11 | 70   | 72   |
| 8   | -3 | 10 | 142  | 184  | 3   | 0   | 10 | 60   | 86   | 2   | 3   | 10 | 187  | 93   | -6  | 7  | 10 | 61   | 61   | 6   | -14 | 11 | 4    | 11   |
| 9   | -3 | 10 | 49   | 51   | 4   | 0   | 10 | 69   | 77   | 3   | 3   | 10 | 31   | 35   | -5  | 7  | 10 | 129  | 138  | 7   | -14 | 11 | 1    | 5    |
| -14 | -2 | 10 | 22   | 18   | 5   | 0   | 10 | 12   | 5    | 4   | 3   | 10 | 30   | 34   | -4  | 7  | 10 | 42   | 51   | -7  | -13 | 11 | 50   | 46   |
| -13 | -2 | 10 | 160  | 166  | 6   | 0   | 10 | 131  | 147  | 5   | 3   | 10 | 111  | 150  | -3  | 7  | 10 | 389  | 504  | -6  | -13 | 11 | 38   | 39   |
| -12 | -2 | 10 | 65   | 75   | 7   | 0   | 10 | 46   | 46   | 6   | 3   | 10 | 18   | 7    | -2  | 7  | 10 | 111  | 132  | -5  | -13 | 11 | 31   | 49   |
| -11 | -2 | 10 | 242  | 304  | 8   | 0   | 10 | 16   | 17   | -14 | 4   | 10 | 102  | 80   | -1  | 7  | 10 | 365  | 353  | -4  | -13 | 11 | 30   | 10   |
| -10 | -2 | 10 | 0    | 8    | -14 | 1   | 10 | 64   | 81   | -13 | 4   | 10 | 70   | 69   | 0   | 7  | 10 | 13   | 4    | -3  | -13 | 11 | 224  | 288  |
| -9  | -2 | 10 | 315  | 279  | -13 | 1   | 10 | 6    | 1    | -12 | 4   | 10 | 183  | 145  | 1   | 7  | 10 | 126  | 75   | -2  | -13 | 11 | 169  | 105  |
| -8  | -2 | 10 | 536  | 688  | -12 | 1   | 10 | 6    | 45   | -11 | 4   | 10 | 10   | 6    | -2  | 7  | 10 | 13   | 3    | -1  | -13 | 11 | 779  | 800  |
| -7  | -2 | 10 | 114  | 94   | -11 | 1   | 10 | 34   | 18   | -10 | 4   | 10 | 366  | 279  | -11 | 8  | 10 | -1   | 1    | 0   | -13 | 11 | 26   | 29   |
| -6  | -2 | 10 | 83   | 69   | -10 | 1   | 10 | 259  | 249  | -9  | 4   | 10 | 299  | 215  | -10 | 8  | 10 | 500  | 452  | 1   | -13 | 11 | 2    | 0    |
| -5  | -2 | 10 | 1261 | 1231 | -9  | 1   | 10 | 71   | 83   | -8  | 4   | 10 | 1807 | 1689 | -9  | 8  | 10 | 14   | 16   | 2   | -13 | 11 | 353  | 376  |
| -4  | -2 | 10 | 136  | 178  | -8  | 1   | 10 | 1007 | 983  | -7  | 4   | 10 | 369  | 299  | -8  | 8  | 10 | 229  | 216  | 3   | -13 | 11 | 25   | 20   |
| -3  | -2 | 10 | 293  | 215  | -7  | 1   | 10 | 177  | 187  | -6  | 4   | 10 | 1146 | 1275 | -7  | 8  | 10 | 93   | 39   | 4   | -13 | 11 | 471  | 418  |
| -2  | -2 | 10 | 534  | 842  | -6  | 1   | 10 | 1356 | 936  | -5  | 4   | 10 | 32   | 24   | -6  | 8  | 10 | 172  | 157  | 5   | -13 | 11 | 112  | 118  |
| -1  | -2 | 10 | 1    | 10   | -5  | 1   | 10 | 1132 | 941  | -4  | 4   | 10 | 418  | 608  | -5  | 8  | 10 | 23   | 23   | 6   | -13 | 11 | 0    | 1    |
| 0   | -2 | 10 | 775  | 820  | -4  | 1   | 10 | 148  | 142  | -3  | 4   | 10 | 309  | 313  | -4  | 8  | 10 | 6    | 10   | 7   | -13 | 11 | 4    | 12   |
| 1   | -2 | 10 | 4    | 2    | -3  | 1   | 10 | 509  | 509  | -2  | 4   | 10 | 1131 | 1157 | -3  | 8  | 10 | 229  | 212  | 8   | -13 | 11 | 6    | 3    |
| 2   | -2 | 10 | 479  | 411  | -2  | 1   | 10 | 300  | 413  | -1  | 4   | 10 | 773  | 542  | -2  | 8  | 10 | 152  | 145  | -9  | -12 | 11 | 50   | 40   |
| 3   | -2 | 10 | 14   | 0    | -1  | 1   | 10 | 591  | 292  | 0   | 4   | 10 | 329  | 213  | -1  | 8  | 10 | 163  | 148  | -8  | -12 | 11 | 77   | 68   |
| 4   | -2 | 10 | 702  | 688  | 0   | 1   | 10 | 16   | 2    | 1   | 4   | 10 | 155  | 75   | 0   | 8  | 10 | 61   | 57   | -7  | -12 | 11 | 180  | 178  |
| 5   | -2 | 10 | 378  | 470  | 1   | 2   | 10 | 1216 | 1245 | 2   | 4   | 10 | -10  | 1    | -10 | 10 | 42 | 28   | 28   | -6  | -12 | 11 | 24   | 24   |
| 6   | -2 | 10 | 160  | 126  | 2   | 1   | 10 | 217  | 238  | 3   | 4   | 10 | -6   | 5    | -9  | 9  | 20 | 21   | 21   | -5  | -12 | 11 | 76   | 84   |
| 7   | -2 | 10 | 85   | 69   | 3   | 1   | 10 | 78   | 78   | 4   | 4   | 10 | 35   | 16   | -8  | 9  | 10 | 120  | 104  | -4  | -12 | 11 | 102  | 151  |
| 8   | -2 | 10 | 22   | 22   | 4   | 1   | 10 | 205  | 183  | 5   | 4   | 10 | 53   | 36   | -7  | 9  | 10 | 273  | 258  | -3  | -12 | 11 | 36   | 50   |
| 9   | -2 | 10 | 23   | 19   | 5   | 1   | 10 | 604  | 566  | -13 | 5   | 10 | 32   | 42   | -6  | 9  | 10 | 129  | 131  | -2  | -12 | 11 | 106  | 100  |
| -14 | -1 | 10 | 28   | 33   | 6   | 1   |    |      |      |     |     |    |      |      |     |    |    |      |      |     |     |    |      |      |

Table C.3, continued

| M         | K    | L    | Obe       | Calc | M    | K          | L    | Obe  | Calc      | M    | K    | L         | Obe  | Calc | M | K | L | Obe | Calc |
|-----------|------|------|-----------|------|------|------------|------|------|-----------|------|------|-----------|------|------|---|---|---|-----|------|
| -3-10 11  | 92   | 108  | -4 -7 11  | 270  | 233  | -7 -4 11   | 287  | 263  | -11 -1 11 | 45   | 44   | -10 2 11  | 42   | 13   |   |   |   |     |      |
| -4-10 11  | 31   | 14   | -3 -7 11  | 4    | 1    | -6 -4 11   | 576  | 589  | -10 -1 11 | 166  | 189  | -9 2 11   | 249  | 321  |   |   |   |     |      |
| -3-10 11  | 262  | 313  | -2 -7 11  | 611  | 575  | -5 -4 11   | 78   | 106  | -9 -1 11  | 71   | 76   | -8 2 11   | 665  | 560  |   |   |   |     |      |
| -2-10 11  | 745  | 797  | -1 -7 11  | 157  | 136  | -4 -4 11   | 656  | 685  | -8 -1 11  | 226  | 361  | -7 2 11   | 32   | 59   |   |   |   |     |      |
| -1-10 11  | 6    | 9    | 0 -7 11   | 54   | 56   | -3 -4 11   | 51   | 19   | -7 -1 11  | 681  | 710  | -6 2 11   | 347  | 397  |   |   |   |     |      |
| 0-10 11   | 620  | 643  | 1 -7 11   | 71   | 89   | -2 -4 11   | 1101 | 1194 | -6 -1 11  | 729  | 666  | -5 2 11   | 2378 | 2201 |   |   |   |     |      |
| 1-10 11   | 32   | 35   | 2 -7 11   | 886  | 862  | -1 -4 11   | 343  | 427  | -5 -1 11  | 142  | 190  | -4 2 11   | 205  | 217  |   |   |   |     |      |
| 2-10 11   | 176  | 162  | 3 -7 11   | 452  | 431  | 0 -4 11    | 1119 | 1164 | -4 -1 11  | 1071 | 1162 | -3 2 11   | 4089 | 3996 |   |   |   |     |      |
| 3-10 11   | 1    | 11   | 4 -7 11   | 186  | 149  | 1 -4 11    | 0    | 10   | -3 -1 11  | 51   | 82   | -2 2 11   | 3    | 7    |   |   |   |     |      |
| 4-10 11   | -6   | 1    | 5 -7 11   | 68   | 65   | 2 -4 11    | 28   | 29   | -2 -1 11  | 619  | 803  | -1 2 11   | 848  | 839  |   |   |   |     |      |
| 5-10 11   | 169  | 170  | 6 -7 11   | 319  | 335  | 3 -4 11    | 172  | 191  | -1 -1 11  | 126  | 107  | 0 2 11    | -2   | 5    |   |   |   |     |      |
| 6-10 11   | 18   | 9    | 7 -7 11   | 2    | 1    | 4 -4 11    | 0    | 1    | 0 -1 11   | 39   | 10   | 1 2 11    | 248  | 260  |   |   |   |     |      |
| 7-10 11   | 36   | 54   | 8 -7 11   | 28   | 27   | 5 -4 11    | 13   | 10   | 1 -1 11   | 814  | 795  | 2 2 11    | 59   | 31   |   |   |   |     |      |
| 8-10 11   | 25   | 28   | 9 -7 11   | 5    | 8    | 6 -4 11    | 61   | 49   | 2 -1 11   | 68   | 45   | 3 2 11    | 252  | 288  |   |   |   |     |      |
| 9-10 11   | 27   | 10   | -13 -6 11 | 4    | 8    | 7 -4 11    | 65   | 69   | 3 -1 11   | 31   | 42   | 4 2 11    | 16   | 5    |   |   |   |     |      |
| -11 -9 11 | 181  | 208  | -12 -6 11 | 31   | 38   | 8 -4 11    | 49   | 36   | 4 -1 11   | 44   | 20   | 5 2 11    | 10   | 36   |   |   |   |     |      |
| -10 -9 11 | 5    | 7    | -11 -6 11 | 4    | 10   | 9 -4 11    | 30   | 13   | 5 -1 11   | 26   | 13   | 6 2 11    | 29   | 28   |   |   |   |     |      |
| -9 -9 11  | 1    | 2    | -10 -6 11 | 419  | 365  | -14 -3 11  | 72   | 271  | 7 -1 11   | 291  | 292  | -13 3 11  | 109  | 93   |   |   |   |     |      |
| -8 -9 11  | 194  | 200  | -9 -6 11  | 34   | 39   | -13 -3 11  | 216  | 148  | -14 0 11  | 107  | 78   | -12 3 11  | 101  | 71   |   |   |   |     |      |
| -7 -9 11  | 82   | 52   | -8 -6 11  | 520  | 435  | -12 -3 11  | 194  | 27   | -13 0 11  | 9    | 15   | -11 3 11  | 220  | 220  |   |   |   |     |      |
| -6 -9 11  | 21   | 14   | -7 -6 11  | 0    | 20   | -11 -3 11  | 26   | 27   | -12 0 11  | 558  | 533  | -10 3 11  | 23   | 8    |   |   |   |     |      |
| -5 -9 11  | 35   | 87   | -6 -6 11  | 73   | 58   | -10 -3 11  | 81   | 102  | -12 0 11  | 91   | 92   | -9 3 11   | 288  | 373  |   |   |   |     |      |
| -4 -9 11  | 115  | 131  | -5 -6 11  | 24   | 39   | -9 -3 11   | 124  | 143  | -11 0 11  | 173  | 157  | -8 3 11   | 533  | 480  |   |   |   |     |      |
| -3 -9 11  | 493  | 521  | -4 -6 11  | 1623 | 1659 | -8 -3 11   | 143  | 160  | -10 0 11  | 3    | 3    | -7 3 11   | 1289 | 1367 |   |   |   |     |      |
| -2 -9 11  | 66   | 13   | -3 -6 11  | 3    | 12   | -7 -3 11   | 160  | 410  | -9 0 11   | 14   | 28   | -6 3 11   | 930  | 874  |   |   |   |     |      |
| -1 -9 11  | 55   | 55   | -2 -6 11  | 241  | 196  | -6 -3 11   | 385  | 538  | -7 0 11   | 28   | 24   | -5 3 11   | 159  | 171  |   |   |   |     |      |
| 0 -9 11   | 879  | 862  | -1 -6 11  | 0    | 1    | -5 -3 11   | 424  | 749  | -6 0 11   | 582  | 659  | -4 3 11   | 1982 | 1830 |   |   |   |     |      |
| 1 -9 11   | 8    | 6    | 0 -6 11   | 1204 | 1220 | -4 -3 11   | 694  | 184  | -5 0 11   | 216  | 215  | -3 3 11   | 11   | 14   |   |   |   |     |      |
| 2 -9 11   | 16   | 26   | 1 -6 11   | 441  | 355  | -3 -3 11   | 238  | 92   | -4 0 11   | 115  | 204  | -2 3 11   | 362  | 411  |   |   |   |     |      |
| 3 -9 11   | 295  | 320  | 2 -6 11   | 87   | 121  | -2 -3 11   | 122  | 66   | -3 0 11   | 1778 | 1420 | 1 3 11    | 109  | 90   |   |   |   |     |      |
| 4 -9 11   | 515  | 505  | 3 -6 11   | 160  | 174  | -1 -3 11   | 65   | 131  | -2 0 11   | 261  | 551  | 0 3 11    | 154  | 134  |   |   |   |     |      |
| 5 -9 11   | 223  | 179  | 4 -6 11   | 133  | 148  | 0 -3 11    | 110  | 1059 | -1 0 11   | 163  | 98   | 2 3 11    | 156  | 83   |   |   |   |     |      |
| 6 -9 11   | 446  | 428  | 5 -6 11   | 961  | 920  | 1 -3 11    | 949  | 479  | 1 0 11    | 124  | 226  | 3 3 11    | 106  | 21   |   |   |   |     |      |
| 7 -9 11   | 92   | 76   | 6 -6 11   | 1782 | 1575 | 2 -3 11    | 133  | 107  | 0 0 11    | 119  | 101  | 4 3 11    | 25   | 14   |   |   |   |     |      |
| 8 -9 11   | 45   | 56   | 7 -6 11   | 257  | 266  | 3 -3 11    | 436  | 1    | 2 0 11    | 475  | 377  | 5 3 11    | 1    | 3    |   |   |   |     |      |
| 9 -9 11   | 56   | 60   | 8 -6 11   | 3    | 2    | 4 -3 11    | 1    | 207  | 3 0 11    | 60   | 91   | -12 4 11  | 0    | 1    |   |   |   |     |      |
| -12 -8 11 | 18   | 11   | 9 -6 11   | 2    | 2    | 5 -3 11    | 232  | 147  | 4 0 11    | 60   | 75   | -13 4 11  | 20   | 39   |   |   |   |     |      |
| -11 -8 11 | 24   | 27   | -13 -5 11 | 73   | 76   | 6 -3 11    | 215  | 303  | 5 0 11    | 65   | 75   | -11 4 11  | 59   | 61   |   |   |   |     |      |
| -10 -8 11 | 33   | 50   | -12 -5 11 | 319  | 299  | 7 -3 11    | 304  | 13   | 6 -1 11   | 31   | 23   | -1 5 12   | 847  | 911  |   |   |   |     |      |
| -9 -8 11  | 92   | 87   | -11 -5 11 | 12   | 2    | 8 -3 11    | 27   | 135  | -1 0 12   | 20   | 43   | 2 -5 12   | 8    | 6    |   |   |   |     |      |
| -10 4 11  | 396  | 403  | -2 -8 11  | 12   | 10   | -8 -1 12   | 186  | 108  | 0 -8 12   | 33   | 206  | 3 -5 12   | 100  | 78   |   |   |   |     |      |
| -9 4 11   | 166  | 166  | -1 8 11   | 77   | 62   | -7 -1 12   | 132  | 3    | 1 -8 12   | 233  | 5    | 4 -5 12   | 3    | 1    |   |   |   |     |      |
| -8 4 11   | 1062 | 1016 | -6 9 11   | 21   | 20   | -6 -1 12   | 8    | 64   | 3 -8 12   | 19   | 27   | 5 -5 12   | 70   | 53   |   |   |   |     |      |
| -7 4 11   | 256  | 236  | -4 9 11   | -5   | 6    | -5 -1 12   | -6   | 8    | 4 -8 12   | 223  | 200  | 6 -5 12   | 13   | 19   |   |   |   |     |      |
| -6 4 11   | 635  | 713  | -5 9 11   | 81   | 73   | -4 -1 12   | 62   | 412  | 5 -8 12   | 72   | 118  | 7 -5 12   | -2   | 3    |   |   |   |     |      |
| -5 4 11   | 667  | 540  | -2 -16 12 | 21   | 30   | -3 -1 12   | 6    | 12   | 6 -8 12   | 56   | 50   | 8 -5 12   | 8    | 17   |   |   |   |     |      |
| -4 4 11   | 75   | 23   | -1 -16 12 | -12  | 1    | -2 -1 12   | 321  | 156  | 7 -8 12   | 61   | 75   | -13 -4 12 | 14   | 13   |   |   |   |     |      |
| -3 4 11   | 635  | 538  | 0 -16 12  | 25   | 53   | -1 -1 12   | 14   | 161  | 8 -8 12   | 14   | 5    | -12 -4 12 | 278  | 221  |   |   |   |     |      |
| -2 4 11   | 308  | 313  | 1 -16 12  | -3   | 15   | 0 -1 12    | 189  | 89   | -12 -7 12 | 47   | 57   | -11 -4 12 | 262  | 314  |   |   |   |     |      |
| -1 4 11   | 40   | 73   | 2 -16 12  | 19   | 14   | 1 -1 12    | 187  | 17   | -11 -7 12 | 100  | 84   | -10 -4 12 | 275  | 310  |   |   |   |     |      |
| 0 4 11    | 52   | 27   | 3 -16 12  | 86   | 77   | 2 -1 12    | 84   | 194  | -10 -7 12 | 86   | 78   | -9 -4 12  | 252  | 232  |   |   |   |     |      |
| 1 4 11    | 39   | 31   | 4 -15 12  | 23   | 14   | 3 -1 12    | 24   | 93   | -9 -7 12  | 358  | 309  | -8 -4 12  | 6    | 18   |   |   |   |     |      |
| 2 4 11    | 202  | 160  | -3 -15 12 | 66   | 33   | 4 -1 12    | 210  | 133  | -8 -7 12  | 350  | 348  | -7 -4 12  | 343  | 400  |   |   |   |     |      |
| 3 4 11    | 89   | 91   | -2 -15 12 | 241  | 204  | 5 -1 12    | 127  | 45   | -7 -7 12  | 101  | 137  | -6 -4 12  | 256  | 261  |   |   |   |     |      |
| 4 4 11    | 18   | 16   | -1 -15 12 | 25   | 110  | 6 -1 12    | 123  | 0    | -6 -7 12  | 116  | 111  | -5 -4 12  | 612  | 566  |   |   |   |     |      |
| -13 5 11  | 50   | 46   | 0 -15 12  | 96   | 112  | -10 -10 12 | 114  | 106  | -5 -7 12  | 193  | 158  | -4 -4 12  | 8    | 29   |   |   |   |     |      |
| -12 5 11  | 167  | 140  | 1 -15 12  | 33   | 33   | 8 -1 12    | 8    | 2    | -4 -7 12  | 111  | 110  | -3 -4 12  | 366  | 357  |   |   |   |     |      |
| -11 5 11  | 78   | 85   | 2 -15 12  | 80   | 52   | -8 -10 12  | 120  | 116  | -3 -7 12  | 397  | 274  | -2 -4 12  | 2    | 2    |   |   |   |     |      |
| -10 5 11  | 292  | 291  | 3 -15 12  | 2    | 15   | -7 -10 12  | 39   | 27   | -2 -7 12  | 18   | 25   | -1 -4 12  | 666  | 698  |   |   |   |     |      |
| -9 5 11   | 9    | 9    | 4 -15 12  | 64   | 8    | -6 -10 12  | 8    | 7    | -1 -7 12  | 951  | 776  | 0 -4 12   | 725  | 763  |   |   |   |     |      |
| -8 5 11   | 73   | 83   | 5 -15 12  | 17   | 32   | -5 -10 12  | 125  | 122  | 0 -7 12   | 70   | 83   | 1 -4 12   | 5    | 7    |   |   |   |     |      |
| -7 5 11   | 152  | 104  | -6 -14 12 | 63   | 32   | -4 -10 12  | 9    | 17   | 1 -7 12   | 93   | 86   | 2 -4 12   | 84   | 71   |   |   |   |     |      |
| -6 5 11   | 75   | 71   | -5 -14 12 | 1    | 1    | -3 -10 12  | 125  | 158  | 2 -7 12   | 1    | 3    | 3 -4 12   | 9    | 9    |   |   |   |     |      |
| -5 5 11   | 768  | 719  | -4 -14 12 | 119  | 111  | -4 -10 12  | 224  | 64   | 3 -7 12   | 570  | 475  | 4 -4 12   | 252  | 288  |   |   |   |     |      |
| -4 5 11   | 89   | 91   | -3 -14 12 | -8   | 0    | -3 -10 12  | 224  | 144  | 4 -7 12   | 35   | 26   | 5 -4 12   | 110  | 99   |   |   |   |     |      |
| -3 5 11   | 522  | 603  | -2 -14 12 | 232  | 279  | -2 -10 12  | 80   | 3    | 5 -7 12   | 216  | 204  | 6 -4 12   | 135  | 161  |   |   |   |     |      |
| -2 5 11   | 203  | 235  | -1 -14 12 | -8   | 1    | -1 -10 12  | 99   | 75   | 6 -7 12   | 658  | 598  | 7 -4 12   | 0    | 2    |   |   |   |     |      |
| -1 5 11   | 74   | 97   | 0 -14 12  | 230  | 257  | 0 -10 12   | 0    | 2    | 7 -7 12   | 72   | 93   | 8 -4 12   | 29   | 25   |   |   |   |     |      |
| 1 5 11    | 127  | 154  | 1 -14 12  | 30   | 16   | 1 -10 12   | 135  | 661  | 8 -7 12   | 21   | 31   | -13 -5 12 | 69   | 85   |   |   |   |     |      |
| 2 5 11    | 30   | 10   | 2 -14 12  | 63   | 47   | 2 -10 12   | 10   | 188  | -12 -6 12 | 117  | 117  | -12 -5 12 | 0    | 13   |   |   |   |     |      |
| 3 5 11    | -9   | 1    | 3 -14 12  | 61   | 67   | 3 -10 12   | 656  | 264  | -11 -6 12 | 46   | 53   | -11 -3 12 | 10   | 4    |   |   |   |     |      |
| -12 6 11  | 12   | 10   | 4 -14 12  | 24   | 8    | 4 -10 12   | 227  | 44   | -10 -6 12 | 26   | 33   | -10 -3 12 | 11   | 1    |   |   |   |     |      |
| -11 6 11  | 23   | 86   | 5 -14 12  | 19   | 3    | 5 -10 12   | 233  | 113  | -9 -6 12  | 13   | 32   | -9 -3 12  | 118  | 92   |   |   |   |     |      |
| -10 6 11  | 75   | 55   | 6 -14 12  | 28   | 58   | 6 -10 12   | 60   | 10   | -8 -6 12  | 172  | 110  | -8 -3 12  | 53   | 48   |   |   |   |     |      |
| -9 6 11   | 72   | 54   | -7 -13 12 | 56   | 40   | 7 -10 12   | 99   | 15   | -7 -6 12  | 2410 | 2357 | -7 -3 12  | 170  | 122  |   |   |   |     |      |
| -8 6 11   | 4    | 1    | -6 -13 12 | 55   | 45   | 8 -10 12   | 11   | 114  | -6 -6 12  | 781  | 805  | -6 -3 12  | 47   | 88   |   |   |   |     |      |
| -7 6 11   | 10   | 80   | -5 -13 12 | 60   | 39   | -11 -9 12  | 23   | 34   | -5 -6 12  | 512  | 440  | -5 -3 12  | 420  | 377  |   |   |   |     |      |
| -6 6 11   | 52   | 57   | -4 -13 12 | 4    | 6    | -10 -9 12  | 112  | 33   | -4 -6 12  | 579  | 554  | -4 -3 12  | 3    | 1    |   |   |   |     |      |
| -5 6 11   | 83   | 72   | -3 -13 12 | 23   | 31   | -9 -9 12   | 53   | 3    | -3 -6 12  | 176  | 142  | -3 -3 12  | 830  | 777  |   |   |   |     |      |
| -4 6 11   | 125  | 148  | -2 -13 12 | -3   | 4    | -8 -9 12   | 34   | 87   | -2 -6 12  | 14   | 5    | -2 -3 12  | 40   | 21   |   |   |   |     |      |
| -3 6 11   | 16   | 7    | -1 -13 12 | 508  | 593  | -7 -9 12   | -2   | 60   | -1 -6 12  | 18   | 47   | -1 -3 12  | 52   | 35   |   |   |   |     |      |
| -2 6 11   | 123  | 99   | 0 -13 12  | 173  | 209  | -6 -9 12   | 77   | 14   | 0 -6 12   | 0    | 1    | 0 -3 12   | 40   | 19   |   |   |   |     |      |
| -1 6 11   | 15   | 2    | 1 -13 12  | 53   | 38   | -5 -9 12   | 93   | 662  | 1 -6 12   | 20   | 60   | 2 -3 12   | 187  | 269  |   |   |   |     |      |
| 0 6 11    | 95   | 107  | 2 -13 12  | 115  | 110  | -4 -9 12   | 24   | 236  | -6 12     | 20   | 60   | 2 -3 12   | 187  | 269  |   |   |   |     |      |
| 1 6 11    | 21   | 7    | 3 -13 12  | -7   | 3    | -3 -9 12   | 4    | 163  | 3 -6 12   | 128  | 127  | 3 -3 12   | 1    | 2    |   |   |   |     |      |
| 2 6 11    | 151  | 155  | 4 -13 12  | 52   | 41   | -2 -9 12   | 251  | 2    | 4 -6 12   | 13   | 24   | 4 -3 12   | 527  | 549  |   |   |   |     |      |
| -11 7 11  | 279  | 251  | 5 -13 12  | 40   | 20   | -1 -9 12   | 212  | 468  | 5 -6 12   | 115  | 122  | 5 -3 12   | 29   | 14   |   |   |   |     |      |
| -10 7 11  | 32   | 51   | 6 -13 12  | 123  | 171  | 0 -9 12    | -1   | 5    | 6 -6 12   | 2    | 16   | 6 -3 12   | 35   | 13   |   |   |   |     |      |
| -9 7 11   | 284  | 234  | 7 -13 12  | 28   | 5    | 1 -9 12    | 395  | 121  | 7 -6 12   | 4    | 1    | 7 -3 12   | 36   | 40   |   |   |   |     |      |
| -8 7 11   | 5    | 2    | 8 -12 12  | 142  | 162  | 2 -9 12    | 17   | 83   | 8 -6 12   | 80   | 76   | -13 -2 12 | 7    | 4    |   |   |   |     |      |
| -7 7 11   | 562  | 488  | -7 -12 12 | 12   |      |            |      |      |           |      |      |           |      |      |   |   |   |     |      |

Table C.3, continued

| M   | K  | L  | Obs  | Calc | M   | K   | L  | Obs  | Calc | M   | K   | L  | Obs | Calc | M   | K   | L  | Obs | Calc | M   | K  | L  | Obs  | Calc | M   | K  | L  | Obs  | Calc | M   | K   | L  | Obs  | Calc |
|-----|----|----|------|------|-----|-----|----|------|------|-----|-----|----|-----|------|-----|-----|----|-----|------|-----|----|----|------|------|-----|----|----|------|------|-----|-----|----|------|------|
| -5  | 0  | 11 | 77   | 68   | 6   | -12 | 12 | 4    | 0    | -4  | -8  | 12 | 613 | 348  | -2  | -5  | 12 | 455 | 356  | -1  | -2 | 12 | 240  | 222  | -5  | 0  | 11 | 77   | 68   | 6   | -12 | 12 | 4    | 0    |
| -4  | 0  | 11 | 57   | 48   | 7   | -12 | 12 | 115  | 89   | -3  | -8  | 12 | 392 | 455  | -1  | -5  | 12 | 950 | 897  | 0   | -2 | 12 | 87   | 73   | -4  | 0  | 11 | 57   | 48   | 7   | -12 | 12 | 115  | 89   |
| -3  | 0  | 11 | 56   | 54   | -9  | -11 | 12 | 9    | 13   | -2  | -8  | 12 | 569 | 447  | 0   | -5  | 12 | 127 | 159  | 1   | -2 | 12 | 89   | 72   | -3  | 0  | 11 | 56   | 54   | -9  | -11 | 12 | 9    | 13   |
| 2   | -2 | 12 | 700  | 571  | 5   | 1   | 12 | 20   | 7    | -1  | 5   | 12 | 0   | 8    | -5  | -12 | 13 | -3  | 1    | 7   | -9 | 13 | 6    | 2    | 2   | -2 | 12 | 700  | 571  | 5   | 1   | 12 | 20   | 7    |
| 3   | -2 | 12 | 0    | 0    | -13 | 2   | 12 | 263  | 256  | 0   | 5   | 12 | 18  | 23   | -4  | -12 | 13 | 1   | 28   | -11 | -8 | 13 | 123  | 114  | 3   | -2 | 12 | 0    | 0    | -13 | 2   | 12 | 263  | 256  |
| 4   | -2 | 12 | 3    | 2    | -12 | 2   | 12 | 20   | 2    | 1   | 9   | 12 | 202 | 182  | -3  | -12 | 13 | 13  | 12   | -10 | -8 | 13 | 15   | 5    | 4   | -2 | 12 | 3    | 2    | -12 | 2   | 12 | 20   | 2    |
| 5   | -2 | 12 | 32   | 22   | -11 | 2   | 12 | 6    | 9    | 2   | 5   | 12 | 101 | 100  | -2  | -12 | 13 | 19  | 12   | -9  | -8 | 13 | 221  | 199  | 5   | -2 | 12 | 32   | 22   | -11 | 2   | 12 | 6    | 9    |
| 6   | -2 | 12 | 131  | 156  | -10 | 2   | 12 | 10   | 27   | -11 | 6   | 12 | 27  | 26   | -1  | -12 | 13 | 46  | 28   | -8  | -8 | 13 | 2    | 0    | 6   | -2 | 12 | 131  | 156  | -10 | 2   | 12 | 10   | 27   |
| 7   | -2 | 12 | 78   | 85   | -9  | 2   | 12 | 250  | 232  | -10 | 6   | 12 | 183 | 155  | 0   | -12 | 13 | 34  | 26   | -7  | -8 | 13 | 162  | 97   | 7   | -2 | 12 | 78   | 85   | -9  | 2   | 12 | 250  | 232  |
| -14 | -1 | 12 | 3    | 15   | -8  | 2   | 12 | 288  | 276  | -9  | 6   | 12 | 61  | 44   | 1   | -12 | 13 | 24  | 38   | -6  | -8 | 13 | 381  | 311  | -14 | -1 | 12 | 3    | 15   | -8  | 2   | 12 | 288  | 276  |
| -13 | -1 | 12 | 94   | 96   | -7  | 2   | 12 | 57   | 45   | -8  | 6   | 12 | 51  | 103  | 2   | -12 | 13 | 21  | 11   | -3  | -8 | 13 | 343  | 298  | -13 | -1 | 12 | 94   | 96   | -7  | 2   | 12 | 57   | 45   |
| -12 | -1 | 12 | 0    | 6    | -6  | 2   | 12 | 85   | 49   | -7  | 6   | 12 | 0   | 0    | 3   | -12 | 13 | 26  | 12   | -4  | -8 | 13 | 480  | 531  | -12 | -1 | 12 | 0    | 6    | -6  | 2   | 12 | 85   | 49   |
| -11 | -1 | 12 | 266  | 259  | -5  | 2   | 12 | 151  | 193  | -6  | 6   | 12 | 349 | 348  | 4   | -12 | 13 | 19  | 16   | -3  | -8 | 13 | 112  | 146  | -11 | -1 | 12 | 266  | 259  | -5  | 2   | 12 | 151  | 193  |
| -10 | -1 | 12 | 4    | 0    | -4  | 2   | 12 | 1634 | 1581 | -5  | 6   | 12 | 76  | 48   | 5   | -12 | 13 | 17  | 5    | -2  | -8 | 13 | 448  | 465  | -10 | -1 | 12 | 4    | 0    | -4  | 2   | 12 | 1634 | 1581 |
| -9  | -1 | 12 | 468  | 493  | -3  | 2   | 12 | 847  | 781  | -4  | 6   | 12 | 283 | 288  | 6   | -12 | 13 | 44  | 36   | -1  | -8 | 13 | 105  | 62   | -9  | -1 | 12 | 468  | 493  | -3  | 2   | 12 | 847  | 781  |
| -8  | -1 | 12 | 62   | 62   | -2  | 2   | 12 | 859  | 773  | -3  | 6   | 12 | 77  | 83   | 7   | -12 | 13 | 10  | 2    | 0   | -8 | 13 | 36   | 32   | -8  | -1 | 12 | 62   | 62   | -2  | 2   | 12 | 859  | 773  |
| -7  | -1 | 12 | 299  | 275  | -1  | 2   | 12 | 519  | 457  | -2  | 6   | 12 | 116 | 120  | -9  | -11 | 13 | 14  | 15   | 1   | -8 | 13 | 104  | 102  | -7  | -1 | 12 | 299  | 275  | -1  | 2   | 12 | 519  | 457  |
| -6  | -1 | 12 | 521  | 488  | 0   | 2   | 12 | 236  | 214  | -1  | 6   | 12 | 33  | 147  | -7  | -11 | 13 | 22  | 1    | 2   | -8 | 13 | 209  | 245  | -6  | -1 | 12 | 521  | 488  | 0   | 2   | 12 | 236  | 214  |
| -5  | -1 | 12 | 1178 | 1003 | 1   | 2   | 12 | 11   | 0    | 0   | 6   | 12 | 495 | 147  | -4  | -11 | 13 | 96  | 84   | 3   | -8 | 13 | 41   | 24   | -5  | -1 | 12 | 1178 | 1003 | 1   | 2   | 12 | 11   | 0    |
| -4  | -1 | 12 | 49   | 49   | 2   | 2   | 12 | 44   | 39   | -10 | 7   | 12 | 161 | 123  | -6  | -11 | 13 | 35  | 36   | 4   | -8 | 13 | 52   | 62   | -4  | -1 | 12 | 49   | 49   | 2   | 2   | 12 | 44   | 39   |
| -3  | -1 | 12 | 384  | 349  | 3   | 2   | 12 | 56   | 12   | -9  | 7   | 12 | 49  | 63   | -5  | -11 | 13 | 130 | 160  | 5   | -8 | 13 | 31   | 16   | -3  | -1 | 12 | 384  | 349  | 3   | 2   | 12 | 56   | 12   |
| -2  | -1 | 12 | 171  | 187  | 4   | 2   | 12 | 32   | 45   | -7  | 7   | 12 | 15  | 7    | -4  | -11 | 13 | -4  | 0    | 6   | -8 | 13 | 135  | 146  | -2  | -1 | 12 | 171  | 187  | 4   | 2   | 12 | 32   | 45   |
| -1  | -1 | 12 | 12   | 19   | 5   | 2   | 12 | 5    | 24   | -5  | 7   | 12 | -3  | 15   | -3  | -11 | 13 | 38  | 50   | 7   | -8 | 13 | 13   | 1    | -1  | -1 | 12 | 12   | 19   | 5   | 2   | 12 | 5    | 24   |
| 0   | -1 | 12 | 832  | 758  | -13 | 3   | 12 | 54   | 49   | -4  | 7   | 12 | 7   | 8    | -2  | -11 | 13 | 187 | 106  | -12 | -7 | 13 | 0    | 15   | 0   | -1 | 12 | 832  | 758  | -13 | 3   | 12 | 54   | 49   |
| 1   | -1 | 12 | 5    | 1    | -12 | 3   | 12 | 12   | 1    | -3  | 7   | 12 | 32  | 31   | 1   | -11 | 13 | 12  | 1    | -11 | -7 | 13 | 132  | 121  | 1   | -1 | 12 | 5    | 1    | -12 | 3   | 12 | 12   | 1    |
| 2   | -1 | 12 | 215  | 189  | -11 | 3   | 12 | 239  | 258  | -2  | 7   | 12 | 182 | 0    | 0   | -11 | 13 | 23  | 9    | -10 | -7 | 13 | 23   | 2    | 2   | -1 | 12 | 215  | 189  | -11 | 3   | 12 | 239  | 258  |
| 3   | -1 | 12 | 13   | 14   | -10 | 3   | 12 | 92   | 151  | -7  | 8   | 12 | -4  | 1    | 1   | -11 | 13 | 33  | 31   | -9  | -7 | 13 | 92   | 59   | 3   | -1 | 12 | 13   | 14   | -10 | 3   | 12 | 92   | 151  |
| 4   | -1 | 12 | 350  | 346  | -9  | 3   | 12 | 521  | 528  | -5  | 8   | 12 | 7   | 28   | 2   | -11 | 13 | 335 | 345  | -8  | -7 | 13 | 611  | 530  | 4   | -1 | 12 | 350  | 346  | -9  | 3   | 12 | 521  | 528  |
| 5   | -1 | 12 | 47   | 19   | -8  | 3   | 12 | 104  | 91   | -1  | -16 | 13 | 120 | 143  | 3   | -11 | 13 | 34  | 69   | -7  | -7 | 13 | 281  | 274  | 5   | -1 | 12 | 47   | 19   | -8  | 3   | 12 | 104  | 91   |
| 6   | -1 | 12 | 33   | 20   | -7  | 3   | 12 | 1172 | 896  | 0   | -16 | 13 | 1   | 1    | 4   | -11 | 13 | 31  | 17   | -6  | -7 | 13 | 49   | 109  | 6   | -1 | 12 | 33   | 20   | -7  | 3   | 12 | 1172 | 896  |
| -14 | 0  | 12 | -5   | 3    | -6  | 3   | 12 | 107  | 65   | -1  | -16 | 13 | 52  | 37   | 5   | -11 | 13 | 206 | 213  | -5  | -7 | 13 | 26   | 42   | -14 | 0  | 12 | -5   | 3    | -6  | 3   | 12 | 107  | 65   |
| -13 | 0  | 12 | 58   | 46   | -5  | 3   | 12 | 1590 | 1841 | -4  | -15 | 13 | 9   | 5    | 6   | -11 | 13 | 49  | 40   | -4  | -7 | 13 | 18   | 14   | -13 | 0  | 12 | 58   | 46   | -5  | 3   | 12 | 1590 | 1841 |
| -12 | 0  | 12 | 4    | 17   | -4  | 3   | 12 | 126  | 131  | -3  | -15 | 13 | 10  | 2    | 7   | -11 | 13 | 3   | 0    | -3  | -7 | 13 | 233  | 220  | -12 | 0  | 12 | 4    | 17   | -4  | 3   | 12 | 126  | 131  |
| -11 | 0  | 12 | -4   | 7    | -3  | 3   | 12 | 168  | 81   | -2  | -15 | 13 | 42  | 31   | -10 | -10 | 13 | 11  | 3    | -2  | -7 | 13 | 85   | 61   | -11 | 0  | 12 | -4   | 7    | -3  | 3   | 12 | 168  | 81   |
| -10 | 0  | 12 | -2   | 3    | -2  | 3   | 12 | 180  | 110  | -1  | -15 | 13 | 114 | 96   | -9  | -10 | 13 | 181 | 162  | -1  | -7 | 13 | 106  | 65   | -10 | 0  | 12 | -2   | 3    | -2  | 3   | 12 | 180  | 110  |
| -9  | 0  | 12 | 160  | 165  | -1  | 3   | 12 | 52   | 37   | 0   | -15 | 13 | 15  | 9    | -8  | -10 | 13 | 29  | 28   | 0   | -7 | 13 | 875  | 839  | -9  | 0  | 12 | 160  | 165  | -1  | 3   | 12 | 52   | 37   |
| -8  | 0  | 12 | 5    | 0    | 0   | 3   | 12 | 57   | 32   | 1   | -15 | 13 | 35  | 34   | -7  | -10 | 13 | 136 | 109  | 1   | -7 | 13 | 141  | 142  | -8  | 0  | 12 | 5    | 0    | 0   | 3   | 12 | 57   | 32   |
| -7  | 0  | 12 | 124  | 75   | 1   | 3   | 12 | 76   | 60   | 2   | -15 | 13 | 0   | 1    | -6  | -10 | 13 | 254 | 147  | 2   | -7 | 13 | 83   | 70   | -7  | 0  | 12 | 124  | 75   | 1   | 3   | 12 | 76   | 60   |
| -6  | 0  | 12 | 199  | 281  | 2   | 3   | 12 | 115  | 107  | 3   | -15 | 13 | 61  | 85   | -5  | -10 | 13 | 13  | 1    | 3   | -7 | 13 | 68   | 81   | -6  | 0  | 12 | 199  | 281  | 2   | 3   | 12 | 115  | 107  |
| -5  | 0  | 12 | 55   | 28   | 3   | 3   | 12 | -2   | 5    | 4   | -15 | 13 | 8   | 11   | -4  | -10 | 13 | 17  | 21   | 4   | -7 | 13 | 709  | 627  | -5  | 0  | 12 | 55   | 28   | 3   | 3   | 12 | -2   | 5    |
| -4  | 0  | 12 | 733  | 915  | 4   | 3   | 12 | 196  | 162  | -6  | -14 | 13 | 5   | 13   | 3   | -10 | 13 | 56  | 72   | 5   | -7 | 13 | 31   | 72   | -4  | 0  | 12 | 733  | 915  | 4   | 3   | 12 | 196  | 162  |
| -3  | 0  | 12 | 1417 | 1334 | -13 | 4   | 12 | 66   | 79   | -5  | -14 | 13 | -4  | 0    | -2  | -10 | 13 | 5   | 3    | 6   | -7 | 13 | 1    | 6    | -3  | 0  | 12 | 1417 | 1334 | -13 | 4   | 12 | 66   | 79   |
| -2  | 0  | 12 | 784  | 894  | -12 | 4   | 12 | 28   | 33   | -4  | -14 | 13 | 16  | 20   | -1  | -10 | 13 | 4   | 19   | 7   | -7 | 13 | 1    | 6    | -2  | 0  | 12 | 784  | 894  | -12 | 4   | 12 | 28   | 33   |
| -1  | 0  | 12 | 72   | 81   | -11 | 4   | 12 | 21   | 28   | -3  | -14 | 13 | 214 | 241  | 0   | -10 | 13 | 44  | 52   | -12 | -6 | 13 | 4    | 0    | -1  | 0  | 12 | 72   | 81   | -11 | 4   | 12 | 21   | 28   |
| 0   | 0  | 12 | 1173 | 920  | -10 | 4   | 12 | 75   | 53   | -2  | -14 | 13 | -2  | 4    | 1   | -10 | 13 | 215 | 210  | -11 | -6 | 13 | 82   | 66   | 0   | 0  | 12 | 1173 | 920  | -10 | 4   | 12 | 75   | 53   |
| 1   | 0  | 12 | 68   | 43   | -9  | 4   | 12 | 88   | 73   | -1  | -14 | 13 | 84  | 94   | 2   | -10 | 13 | 0   | 2    | -10 | -6 | 13 | 149  | 193  | 1   | 0  | 12 | 68   | 43   | -9  | 4   | 12 | 88   | 73   |
| 2   | 0  | 12 | 220  | 183  | -8  | 4   | 12 | 11   | 4    | 0   | -14 | 13 | 13  | 1    | 3   | -10 | 13 | 68  | 63   | -9  | -6 | 13 | 1032 | 1054 | 2   | 0  | 12 | 220  | 183  | -8  | 4   | 12 | 11   | 4    |
| 3   | 0  | 12 | 32   | 14   | -7  | 4   | 12 | 64   | 69   | 1   | -14 | 13 | 56  | 52   | 4   | -10 | 13 | 151 | 182  | -8  | -6 | 13 | 116  | 92   | 3   | 0  | 12 | 32   | 14   | -7  | 4   | 12 | 64   | 69   |
| 4   | 0  | 12 | 8    | 1    | -6  | 4   | 12 | 16   | 18   | 2   | -14 | 13 | 23  | 17   | 5   | -10 | 13 | 121 | 131  | -7  | -6 | 13 | 73   | 48   | 4   | 0  | 12 | 8    | 1    | -6  | 4   | 12 | 16   | 18   |
| 5   | 0  | 12 | 82   | 77   | -5  | 4   | 12 | 96   | 108  | 3   | -14 | 13 | 26  | 28   | 6   | -10 | 13 | 215 | 188  | -6  | -6 | 13 | 30   | 23   | 5   | 0  | 12 | 82   | 77   | -5  | 4   | 12 | 96   | 108  |
| 6   |    |    |      |      |     |     |    |      |      |     |     |    |     |      |     |     |    |     |      |     |    |    |      |      |     |    |    |      |      |     |     |    |      |      |

Table C.3, continued

| M   | K  | L  | Obs  | Calc | M   | K  | L  | Obs  | Calc | M   | K   | L  | Obs | Calc | M   | K   | L  | Obs | Calc |
|-----|----|----|------|------|-----|----|----|------|------|-----|-----|----|-----|------|-----|-----|----|-----|------|
| -7  | -4 | 13 | 71   | 89   | -7  | 0  | 13 | 423  | 359  | -9  | 4   | 13 | 244 | 219  | -5  | -12 | 14 | 273 | 203  |
| -13 | -3 | 13 | 117  | 130  | -6  | 0  | 13 | 1109 | 1330 | -8  | 4   | 13 | 14  | 3    | -4  | -12 | 14 | 260 | 216  |
| -12 | -3 | 13 | 7    | 0    | -5  | 0  | 13 | 1442 | 1334 | -6  | 4   | 13 | 3   | 8    | -3  | -12 | 14 | 14  | 26   |
| -11 | -3 | 13 | 161  | 205  | -4  | 0  | 13 | 1449 | 1264 | -5  | 4   | 13 | 26  | 6    | -2  | -12 | 14 | 8   | 8    |
| -10 | -3 | 13 | -3   | 1    | -3  | 0  | 13 | 1491 | 1468 | -4  | 4   | 13 | 15  | 30   | -1  | -12 | 14 | 87  | 85   |
| -9  | -3 | 13 | 175  | 242  | -2  | 0  | 13 | 916  | 839  | -3  | 4   | 13 | 91  | 72   | 0   | -12 | 14 | 0   | 1    |
| -8  | -3 | 13 | 53   | 21   | -1  | 0  | 13 | 3    | 28   | -2  | 4   | 13 | 95  | 103  | 1   | -12 | 14 | 267 | 232  |
| -7  | -3 | 13 | 231  | 276  | 0   | 0  | 13 | 893  | 878  | -1  | 4   | 13 | 184 | 189  | 2   | -12 | 14 | 31  | 34   |
| -6  | -3 | 13 | 166  | 134  | 1   | 0  | 13 | 432  | 387  | 0   | 4   | 13 | 38  | 4    | 3   | -12 | 14 | 56  | 61   |
| -5  | -3 | 13 | 1583 | 1649 | 2   | 0  | 13 | 186  | 192  | 1   | 4   | 13 | 84  | 51   | 4   | -12 | 14 | 148 | 126  |
| -4  | -3 | 13 | 2630 | 2312 | 3   | 0  | 13 | 15   | 25   | -11 | 5   | 13 | 1   | 24   | 5   | -12 | 14 | 4   | 7    |
| -3  | -3 | 13 | 93   | 142  | 4   | 0  | 13 | 139  | 147  | -10 | 5   | 13 | 136 | 121  | 6   | -12 | 14 | 5   | 4    |
| -2  | -3 | 13 | 422  | 291  | 5   | 0  | 13 | 32   | 35   | -9  | 5   | 13 | 10  | 4    | -9  | -11 | 14 | 47  | 37   |
| -1  | -3 | 13 | 156  | 156  | -13 | 1  | 13 | 116  | 122  | -8  | 5   | 13 | 114 | 170  | -8  | -11 | 14 | 166 | 156  |
| 0   | -3 | 13 | 335  | 380  | -12 | 1  | 13 | 220  | 204  | -7  | 5   | 13 | 9   | 18   | -7  | -11 | 14 | 44  | 23   |
| 1   | -3 | 13 | 34   | 40   | -11 | 1  | 13 | 93   | 77   | -6  | 5   | 13 | 151 | 170  | -6  | -11 | 14 | 505 | 490  |
| 2   | -3 | 13 | 6    | 2    | -10 | 1  | 13 | 78   | 82   | -5  | 5   | 13 | 138 | 152  | -5  | -11 | 14 | 171 | 152  |
| 3   | -3 | 13 | -1   | 3    | -9  | 1  | 13 | 124  | 123  | -4  | 5   | 13 | 9   | 0    | -4  | -11 | 14 | 163 | 162  |
| 4   | -3 | 13 | 11   | 11   | -8  | 1  | 13 | 7    | 4    | -3  | 5   | 13 | 168 | 146  | -3  | -11 | 14 | 43  | 56   |
| 5   | -3 | 13 | 180  | 162  | -7  | 1  | 13 | 29   | 28   | -2  | 5   | 13 | -3  | 0    | -2  | -11 | 14 | 37  | 56   |
| 6   | -3 | 13 | 4    | 2    | -6  | 1  | 13 | 54   | 100  | -1  | 5   | 13 | 276 | 252  | -1  | -11 | 14 | 26  | 15   |
| -13 | -2 | 13 | 17   | 21   | -5  | 1  | 13 | 1    | 2    | 0   | 5   | 13 | -12 | 3    | 0   | -11 | 14 | 0   | 2    |
| -12 | -2 | 13 | 69   | 72   | -4  | 1  | 13 | 90   | 111  | -10 | 6   | 13 | 78  | 101  | -1  | -11 | 14 | 0   | 2    |
| -11 | -2 | 13 | 34   | 34   | -3  | 1  | 13 | 119  | 134  | -9  | 6   | 13 | 165 | 190  | 2   | -11 | 14 | 25  | 27   |
| -10 | -2 | 13 | 2    | 1    | -2  | 1  | 13 | 381  | 424  | -8  | 6   | 13 | 65  | 72   | 3   | -11 | 14 | 30  | 24   |
| -9  | -2 | 13 | 7    | 14   | -1  | 1  | 13 | 7    | 6    | -7  | 6   | 13 | 21  | 176  | 4   | -11 | 14 | 5   | 1    |
| -8  | -2 | 13 | 359  | 385  | 0   | 1  | 13 | 146  | 132  | -6  | 6   | 13 | 45  | 26   | 5   | -11 | 14 | 152 | 140  |
| -7  | -2 | 13 | 3    | 2    | 1   | 1  | 13 | 8    | 11   | -5  | 6   | 13 | 78  | 67   | 6   | -11 | 14 | 43  | 42   |
| -6  | -2 | 13 | 815  | 780  | 2   | 1  | 13 | 199  | 165  | -4  | 6   | 13 | 94  | 127  | -9  | -10 | 14 | 26  | 29   |
| -5  | -2 | 13 | 1496 | 1353 | 3   | 1  | 13 | 76   | 67   | -3  | 6   | 13 | -17 | 1    | -8  | -10 | 14 | 10  | 6    |
| -4  | -2 | 13 | 1614 | 1725 | 4   | 1  | 13 | 118  | 9    | -2  | 6   | 13 | 17  | 13   | -7  | -10 | 14 | 16  | 11   |
| -3  | -2 | 13 | 249  | 270  | -13 | 2  | 13 | -5   | 1    | -7  | 7   | 13 | 85  | 65   | -6  | -10 | 14 | 80  | 81   |
| -11 | -6 | 14 | 17   | 16   | -2  | -3 | 14 | 5    | 21   | -6  | 1   | 14 | 38  | 74   | -2  | -13 | 15 | 130 | 118  |
| -10 | -6 | 14 | 47   | 47   | -1  | -3 | 14 | 358  | 336  | -5  | 1   | 14 | 15  | 18   | -1  | -13 | 15 | 11  | 18   |
| -9  | -6 | 14 | 24   | 34   | 0   | -3 | 14 | 21   | 36   | -4  | 1   | 14 | 15  | 18   | 0   | -13 | 15 | 11  | 0    |
| -8  | -6 | 14 | 172  | 158  | 1   | -3 | 14 | 191  | 180  | -3  | 1   | 14 | -1  | 3    | 1   | -13 | 15 | 18  | 15   |
| -7  | -6 | 14 | 276  | 303  | 2   | -3 | 14 | 82   | 68   | -2  | 1   | 14 | 67  | 62   | 2   | -13 | 15 | -5  | 11   |
| -6  | -6 | 14 | 1672 | 1544 | 3   | -3 | 14 | 27   | 16   | -1  | 1   | 14 | 197 | 150  | 3   | -13 | 15 | 31  | 17   |
| -5  | -6 | 14 | 170  | 175  | 4   | -3 | 14 | 82   | 49   | 0   | 1   | 14 | 83  | 76   | 4   | -13 | 15 | 15  | 18   |
| -4  | -6 | 14 | 913  | 923  | 5   | -3 | 14 | 30   | 24   | 1   | 1   | 14 | 117 | 49   | -7  | -12 | 15 | 25  | 45   |
| -3  | -6 | 14 | 722  | 587  | -13 | -2 | 14 | 22   | 25   | 2   | 1   | 14 | 128 | 100  | -6  | -12 | 15 | 6   | 1    |
| -2  | -6 | 14 | 98   | 93   | -12 | -2 | 14 | 4    | 2    | 3   | 1   | 14 | 1   | 18   | -5  | -12 | 15 | 3   | 2    |
| -1  | -6 | 14 | 567  | 476  | -11 | -2 | 14 | 0    | 1    | -12 | 2   | 14 | 218 | 275  | -4  | -12 | 15 | 131 | 238  |
| 0   | -6 | 14 | 138  | 112  | -10 | -2 | 14 | 12   | 7    | -11 | 2   | 14 | 101 | 83   | -3  | -12 | 15 | 518 | 579  |
| 1   | -6 | 14 | 714  | 709  | -9  | -2 | 14 | 18   | 15   | -10 | 2   | 14 | 79  | 123  | -2  | -12 | 15 | 90  | 97   |
| 2   | -6 | 14 | 37   | 39   | -8  | -2 | 14 | 184  | 1    | -9  | 2   | 14 | 236 | 180  | -1  | -12 | 15 | 180 | 210  |
| 3   | -6 | 14 | 8    | 17   | -7  | -2 | 14 | 184  | 197  | -8  | 2   | 14 | 1   | 1    | 0   | -12 | 15 | 78  | 79   |
| 4   | -6 | 14 | 8    | 42   | -6  | -2 | 14 | 741  | 706  | -7  | 2   | 14 | 898 | 929  | 1   | -12 | 15 | 136 | 118  |
| 5   | -6 | 14 | 0    | 16   | -5  | -2 | 14 | 1562 | 1385 | -6  | 2   | 14 | 21  | 10   | 2   | -12 | 15 | 36  | 24   |
| 6   | -6 | 14 | 0    | 16   | -4  | -2 | 14 | -2   | 1    | -5  | 2   | 14 | 12  | 13   | 3   | -12 | 15 | 35  | 39   |
| -12 | -5 | 14 | 31   | 27   | -2  | -2 | 14 | 72   | 50   | -4  | 2   | 14 | 47  | 35   | 4   | -12 | 15 | 12  | 8    |
| -11 | -5 | 14 | 5    | 4    | -1  | -2 | 14 | 75   | 101  | -3  | 2   | 14 | 29  | 37   | -8  | -11 | 15 | 0   | 0    |
| -10 | -5 | 14 | 200  | 185  | 0   | -2 | 14 | 34   | 24   | -2  | 2   | 14 | 63  | 28   | -7  | -11 | 15 | 0   | 11   |
| -9  | -5 | 14 | 5    | 5    | 1   | -2 | 14 | 271  | 274  | -1  | 2   | 14 | 0   | 0    | -6  | -11 | 15 | 542 | 476  |
| -8  | -5 | 14 | 271  | 299  | 2   | -2 | 14 | 11   | 47   | 0   | 2   | 14 | 123 | 56   | -5  | -11 | 15 | 35  | 36   |
| -7  | -5 | 14 | 235  | 179  | 3   | -2 | 14 | 378  | 353  | 1   | 2   | 14 | 19  | 7    | -4  | -11 | 15 | 22  | 39   |
| -6  | -5 | 14 | 40   | 35   | 4   | -2 | 14 | 18   | 42   | 2   | 1   | 14 | 71  | 66   | 3   | -11 | 15 | 9   | 9    |
| -5  | -5 | 14 | 44   | 28   | 5   | -2 | 14 | 27   | 55   | -11 | 3   | 14 | 426 | 474  | -2  | -11 | 15 | 100 | 78   |
| -4  | -5 | 14 | 97   | 160  | -13 | -1 | 14 | 14   | 6    | -10 | 3   | 14 | 21  | 28   | -1  | -11 | 15 | 18  | 7    |
| -3  | -5 | 14 | 6    | 16   | -12 | -1 | 14 | 145  | 169  | -9  | 3   | 14 | 83  | 61   | 0   | -11 | 15 | 47  | 58   |
| -2  | -5 | 14 | 11   | 5    | -11 | -1 | 14 | 1    | 7    | -8  | 3   | 14 | 151 | 138  | 1   | -11 | 15 | 22  | 32   |
| -1  | -5 | 14 | 450  | 461  | -10 | -1 | 14 | 81   | 127  | -7  | 3   | 14 | 2   | 2    | 2   | -11 | 15 | 34  | 45   |
| 0   | -5 | 14 | 9    | 1    | -9  | -1 | 14 | 63   | 46   | -6  | 3   | 14 | 37  | 56   | 3   | -11 | 15 | 67  | 69   |
| 1   | -5 | 14 | 2    | 6    | -8  | -1 | 14 | 199  | 222  | -5  | 3   | 14 | 1   | 2    | 4   | -11 | 15 | 4   | 2    |
| 2   | -5 | 14 | 118  | 115  | -7  | -1 | 14 | 103  | 49   | -4  | 3   | 14 | 19  | 15   | 5   | -11 | 15 | 63  | 53   |
| 3   | -5 | 14 | 35   | 331  | -6  | -1 | 14 | 91   | 86   | -3  | 3   | 14 | 110 | 92   | -9  | -10 | 15 | 27  | 58   |
| 4   | -5 | 14 | 3    | 3    | -5  | -1 | 14 | 703  | 495  | -2  | 3   | 14 | 134 | 191  | -8  | -10 | 15 | 227 | 242  |
| 5   | -5 | 14 | 24   | 39   | -4  | -1 | 14 | 1133 | 1239 | -1  | 3   | 14 | 26  | 41   | -7  | -10 | 15 | 166 | 173  |
| 6   | -5 | 14 | 1    | 78   | -3  | -1 | 14 | 53   | 74   | 0   | 3   | 14 | 87  | 98   | -6  | -10 | 15 | 144 | 135  |
| -12 | -4 | 14 | 61   | 78   | -2  | -1 | 14 | 72   | 69   | 1   | 3   | 14 | 17  | 9    | -5  | -10 | 15 | 571 | 571  |
| -11 | -4 | 14 | 76   | 78   | -1  | -1 | 14 | 1049 | 1108 | -10 | 4   | 14 | 10  | 6    | -4  | -10 | 15 | 34  | 35   |
| -10 | -4 | 14 | 164  | 200  | 0   | -1 | 14 | 46   | 41   | -9  | 4   | 14 | 199 | 243  | -3  | -10 | 15 | 649 | 738  |
| -9  | -4 | 14 | 263  | 234  | 1   | -1 | 14 | 456  | 324  | -8  | 4   | 14 | 1   | 0    | -2  | -10 | 15 | 4   | 0    |
| -8  | -4 | 14 | 10   | 3    | 2   | -1 | 14 | 25   | 21   | -7  | 4   | 14 | 174 | 263  | -1  | -10 | 15 | 987 | 900  |
| -7  | -4 | 14 | 150  | 138  | 3   | -1 | 14 | 171  | 185  | -6  | 4   | 14 | 7   | 1    | 0   | -10 | 15 | 14  | 7    |
| -6  | -4 | 14 | 2027 | 1980 | 4   | -1 | 14 | 104  | 84   | -5  | 4   | 14 | 289 | 212  | 1   | -10 | 15 | 264 | 200  |
| -5  | -4 | 14 | 2868 | 2472 | -12 | 0  | 14 | 48   | 53   | -4  | 4   | 14 | 43  | 54   | 2   | -10 | 15 | 17  | 16   |
| -4  | -4 | 14 | 2018 | 1715 | -11 | 0  | 14 | 54   | 32   | -3  | 4   | 14 | 50  | 54   | 3   | -10 | 15 | 47  | 53   |
| -3  | -4 | 14 | 775  | 787  | -10 | 0  | 14 | 99   | 102  | -2  | 4   | 14 | 52  | 71   | 4   | -10 | 15 | 49  | 53   |
| -2  | -4 | 14 | 102  | 65   | -9  | 0  | 14 | 962  | 932  | -1  | 4   | 14 | 48  | 49   | -10 | -9  | 15 | 50  | 56   |
| -1  | -4 | 14 | 3    | 11   | -8  | 0  | 14 | 363  | 290  | -9  | 5   | 14 | 46  | 62   | -9  | -9  | 15 | 0   | 0    |
| 0   | -4 | 14 | 13   | 9    | -7  | 0  | 14 | 789  | 752  | -8  | 5   | 14 | 74  | 76   | -8  | -9  | 15 | 1   | 1    |
| 1   | -4 | 14 | 19   | 27   | -5  | 0  | 14 | 84   | 32   | -6  | 5   | 14 | 173 | 174  | -7  | -9  | 15 | 130 | 91   |
| 2   | -4 | 14 | 82   | 99   | -4  | 0  | 14 | 16   | 11   | -5  | 5   | 14 | 134 | 113  | -6  | -9  | 15 | 8   | 3    |
| 3   | -4 | 14 | 9    | 18   | -3  | 0  | 14 | 1    | 20   | -4  | 5   | 14 | 12  | 3    | -5  | -9  | 15 | 72  | 63   |
| 4   | -4 | 14 | 48   | 46   | -2  | 0  | 14 | 203  | 223  | -3  | 5   | 14 | 37  | 45   | -4  | -9  | 15 | 4   | 2    |
| 5   | -4 | 14 | 74   | 86   | -1  | 0  | 14 | 191  | 180  | -4  | -14 | 15 | 3   | 7    | -3  | -9  | 1  |     |      |

Table C.3, continued

| M   | K  | L  | Obs | Calc | M   | K  | L  | Obs | Calc | M   | K   | L  | Obs | Calc | M   | K  | L  | Obs | Calc |
|-----|----|----|-----|------|-----|----|----|-----|------|-----|-----|----|-----|------|-----|----|----|-----|------|
| -6  | -4 | 15 | 278 | 278  | -6  | 0  | 15 | 5   | 5    | 0   | -12 | 16 | -4  | 0    | 0   | -7 | 16 | 178 | 221  |
| -5  | -4 | 15 | 32  | 11   | -5  | 0  | 15 | 126 | 85   | 1   | -12 | 16 | 19  | 7    | 1   | -7 | 16 | 9   | 30   |
| -4  | -4 | 15 | 195 | 140  | -4  | 0  | 15 | 1   | 1    | 2   | -12 | 16 | 60  | 39   | 2   | -7 | 16 | 198 | 191  |
| -3  | -4 | 15 | 12  | 35   | -3  | 0  | 15 | 78  | 57   | 3   | -12 | 16 | 2   | 1    | 3   | -7 | 16 | 16  | 20   |
| -2  | -4 | 15 | 72  | 33   | -2  | 0  | 15 | 21  | 52   | -7  | -11 | 16 | 53  | 79   | 4   | -7 | 16 | 9   | 5    |
| -1  | -4 | 15 | 374 | 266  | -1  | 0  | 15 | 16  | 0    | -6  | -11 | 16 | 15  | 3    | -10 | -6 | 16 | 0   | 1    |
| 0   | -4 | 15 | 121 | 109  | 0   | 0  | 15 | 16  | 1    | -5  | -11 | 16 | 332 | 316  | -9  | -6 | 16 | 39  | 49   |
| 1   | -4 | 15 | 2   | 5    | 1   | 0  | 15 | 0   | 1    | -4  | -11 | 16 | 102 | 115  | -8  | -6 | 16 | -4  | 2    |
| 2   | -4 | 15 | 8   | 9    | 2   | 0  | 15 | 14  | 16   | -3  | -11 | 16 | 20  | 28   | -7  | -6 | 16 | 79  | 69   |
| 3   | -4 | 15 | 6   | 6    | -11 | 1  | 15 | 206 | 222  | -2  | -11 | 16 | 513 | 489  | -6  | -6 | 16 | 415 | 501  |
| 4   | -4 | 15 | 18  | 15   | -10 | 1  | 15 | 78  | 70   | -1  | -11 | 16 | 93  | 73   | -5  | -6 | 16 | 126 | 125  |
| -12 | -3 | 15 | 67  | 53   | -9  | 1  | 15 | 242 | 245  | 0   | -11 | 16 | 298 | 335  | -4  | -6 | 16 | 161 | 146  |
| -11 | -3 | 15 | 17  | 10   | -8  | 1  | 15 | 423 | 350  | 1   | -11 | 16 | 72  | 91   | -3  | -6 | 16 | 9   | 0    |
| -10 | -3 | 15 | 5   | 3    | -7  | 1  | 15 | 7   | 13   | 2   | -11 | 16 | 45  | 28   | -2  | -6 | 16 | 7   | 12   |
| -9  | -3 | 15 | 11  | 8    | -6  | 1  | 15 | 367 | 309  | 3   | -11 | 16 | 14  | 32   | -1  | -6 | 16 | 90  | 138  |
| -8  | -3 | 15 | 27  | 36   | -5  | 1  | 15 | 32  | 36   | -8  | -10 | 16 | 44  | 67   | 0   | -6 | 16 | 20  | 14   |
| -7  | -3 | 15 | 95  | 86   | -4  | 1  | 15 | 3   | 15   | -7  | -10 | 16 | 79  | 87   | 1   | -6 | 16 | 193 | 201  |
| -6  | -3 | 15 | 141 | 122  | -3  | 1  | 15 | 11  | 18   | -6  | -10 | 16 | 62  | 49   | 2   | -6 | 16 | 69  | 114  |
| -5  | -3 | 15 | 57  | 63   | -2  | 1  | 15 | 165 | 145  | -5  | -10 | 16 | 145 | 133  | 3   | -6 | 16 | 102 | 81   |
| -4  | -3 | 15 | 699 | 629  | -1  | 1  | 15 | 21  | 9    | -4  | -10 | 16 | 189 | 179  | 4   | -6 | 16 | 7   | 0    |
| -3  | -3 | 15 | 5   | 3    | 0   | 1  | 15 | 35  | 13   | -3  | -10 | 16 | 67  | 46   | -11 | -5 | 16 | 36  | 53   |
| -2  | -3 | 15 | 279 | 314  | 1   | 1  | 15 | 109 | 96   | -2  | -10 | 16 | 14  | 14   | -10 | -5 | 16 | 158 | 143  |
| -1  | -3 | 15 | 24  | 34   | -11 | 2  | 15 | 13  | 14   | -1  | -10 | 16 | 2   | 2    | -9  | -5 | 16 | 77  | 61   |
| 0   | -3 | 15 | 131 | 142  | -10 | 2  | 15 | 263 | 269  | 0   | -10 | 16 | -1  | 1    | -8  | -5 | 16 | 303 | 339  |
| 1   | -3 | 15 | 34  | 40   | -9  | 2  | 15 | 86  | 88   | 1   | -10 | 16 | 33  | 51   | -7  | -5 | 16 | 66  | 33   |
| 2   | -3 | 15 | 966 | 941  | -8  | 2  | 15 | 44  | 79   | 2   | -10 | 16 | 16  | 9    | -6  | -5 | 16 | 22  | 24   |
| 3   | -3 | 15 | 55  | 65   | -7  | 2  | 15 | 19  | 14   | 3   | -10 | 16 | 11  | 18   | -5  | -5 | 16 | 527 | 473  |
| 4   | -3 | 15 | 202 | 199  | -6  | 2  | 15 | 82  | 96   | -4  | -10 | 16 | 26  | 28   | -4  | -5 | 16 | 123 | 50   |
| -12 | -2 | 15 | 24  | 9    | -5  | 2  | 15 | 21  | 69   | -9  | -9  | 16 | -5  | 1    | -3  | -5 | 16 | 51  | 72   |
| -11 | -2 | 15 | 114 | 101  | -4  | 2  | 15 | 27  | 21   | -8  | -9  | 16 | 51  | 20   | -2  | -5 | 16 | 185 | 164  |
| -10 | -2 | 15 | 3   | 2    | -3  | 2  | 15 | 71  | 51   | -7  | -9  | 16 | 221 | 222  | -1  | -5 | 16 | 30  | 39   |
| -9  | -2 | 15 | 221 | 167  | -2  | 2  | 15 | 36  | 32   | -6  | -9  | 16 | 141 | 145  | 0   | -5 | 16 | 5   | 6    |
| -8  | -2 | 15 | 24  | 9    | -1  | 2  | 15 | 36  | 50   | -5  | -9  | 16 | 211 | 261  | 1   | -5 | 16 | 22  | 6    |
| -7  | -2 | 15 | 674 | 584  | 0   | 2  | 15 | 4   | 8    | -4  | -9  | 16 | 264 | 271  | 2   | -5 | 16 | 43  | 199  |
| -6  | -2 | 15 | 13  | 13   | -10 | 3  | 15 | 113 | 163  | -3  | -9  | 16 | 5   | 7    | 3   | -5 | 16 | 27  | 39   |
| -5  | -2 | 15 | 29  | 46   | -9  | 3  | 15 | 3   | 1    | -2  | -9  | 16 | 666 | 612  | -11 | -4 | 16 | 179 | 159  |
| -4  | -2 | 15 | 76  | 69   | -8  | 3  | 15 | 198 | 154  | -1  | -9  | 16 | 6   | 4    | -10 | -4 | 16 | 93  | 85   |
| -3  | -2 | 15 | 26  | 23   | -7  | 3  | 15 | 1   | 7    | 0   | -9  | 16 | 402 | 379  | -9  | -4 | 16 | 62  | 40   |
| -2  | -2 | 15 | 42  | 54   | -6  | 3  | 15 | 246 | 292  | 1   | -9  | 16 | 2   | 5    | -8  | -4 | 16 | 3   | 1    |
| -1  | -2 | 15 | 18  | 6    | -5  | 3  | 15 | 120 | 129  | -2  | -9  | 16 | 2   | 37   | -7  | -4 | 16 | 275 | 287  |
| 0   | -2 | 15 | 174 | 184  | -4  | 3  | 15 | 141 | 139  | -9  | -9  | 16 | 2   | 0    | -6  | -4 | 16 | 78  | 45   |
| 1   | -2 | 15 | 0   | 1    | -3  | 3  | 15 | 15  | 1    | 4   | -9  | 16 | 44  | 34   | -5  | -4 | 16 | 27  | 7    |
| 2   | -2 | 15 | 104 | 104  | -2  | 3  | 15 | 320 | 173  | -10 | -8  | 16 | -1  | 2    | -4  | -4 | 16 | 52  | 27   |
| 3   | -2 | 15 | 11  | 14   | -1  | 3  | 15 | 43  | 44   | -9  | -8  | 16 | 338 | 394  | -3  | -4 | 16 | 30  | 28   |
| -12 | -1 | 15 | -8  | 1    | -8  | 4  | 15 | 83  | 96   | -8  | -8  | 16 | 50  | 58   | -2  | -4 | 16 | 72  | 101  |
| -11 | -1 | 15 | 138 | 114  | -7  | 4  | 15 | 37  | 36   | -7  | -8  | 16 | 80  | 69   | -1  | -4 | 16 | 47  | 51   |
| -10 | -1 | 15 | 60  | 108  | -6  | 4  | 15 | 59  | 70   | -6  | -8  | 16 | 636 | 644  | 0   | -4 | 16 | 94  | 77   |
| -9  | -1 | 15 | 204 | 239  | -5  | 4  | 15 | 41  | 19   | -5  | -8  | 16 | 2   | 1    | -4  | -4 | 16 | 116 | 195  |
| -8  | -1 | 15 | 283 | 380  | -4  | 4  | 15 | 58  | 48   | -4  | -8  | 16 | 363 | 422  | 2   | -4 | 16 | 5   | 2    |
| -7  | -1 | 15 | 8   | 9    | -2  | 4  | 15 | 16  | 20   | -3  | -8  | 16 | 29  | 9    | 3   | -4 | 16 | 169 | 196  |
| -6  | -1 | 15 | 361 | 291  | -1  | 4  | 15 | 120 | 129  | -2  | -8  | 16 | 9   | 14   | -11 | -3 | 16 | 7   | 3    |
| -5  | -1 | 15 | 248 | 269  | 0   | 4  | 15 | 29  | 42   | -1  | -8  | 16 | 58  | 35   | -10 | -3 | 16 | 272 | 247  |
| -4  | -1 | 15 | 33  | 19   | -5  | 4  | 15 | 6   | 4    | 0   | -8  | 16 | 2   | 1    | -9  | -3 | 16 | 7   | 5    |
| -3  | -1 | 15 | 28  | 28   | -4  | 4  | 15 | 6   | 3    | 1   | -8  | 16 | 16  | 30   | -8  | -3 | 16 | 328 | 313  |
| -2  | -1 | 15 | 3   | 10   | -3  | 4  | 15 | 9   | 8    | 2   | -8  | 16 | 0   | 1    | -7  | -3 | 16 | 278 | 234  |
| -1  | -1 | 15 | 41  | 49   | -2  | 4  | 15 | 196 | 215  | 4   | -8  | 16 | 38  | 30   | -6  | -3 | 16 | 65  | 37   |
| 0   | -1 | 15 | 132 | 119  | -1  | 4  | 15 | 16  | 9    | -10 | -7  | 16 | 74  | 72   | -5  | -3 | 16 | 461 | 497  |
| 1   | -1 | 15 | 12  | 47   | 0   | 4  | 15 | 254 | 261  | -9  | -7  | 16 | 2   | 1    | -4  | -3 | 16 | 130 | 135  |
| 2   | -1 | 15 | 185 | 164  | 1   | 4  | 15 | 207 | 233  | -8  | -7  | 16 | 107 | 106  | -3  | -3 | 16 | 47  | 61   |
| 3   | -1 | 15 | 51  | 68   | 2   | 4  | 15 | 103 | 119  | -7  | -7  | 16 | 5   | 11   | -2  | -3 | 16 | 195 | 207  |
| -12 | 0  | 15 | 51  | 57   | -6  | 4  | 15 | -4  | 0    | -6  | -7  | 16 | 218 | 173  | -1  | -3 | 16 | 264 | 235  |
| -11 | 0  | 15 | 18  | 31   | -8  | -5 | 17 | 2   | 6    | -1  | -10 | 17 | 10  | 6    |     |    |    |     |      |
| -10 | 0  | 15 | 58  | 103  | -7  | -5 | 17 | 139 | 114  | -6  | -9  | 18 | 28  | 22   |     |    |    |     |      |
| -9  | 0  | 15 | 15  | 9    | -6  | -5 | 17 | -4  | 4    | -5  | -9  | 18 | 40  | 36   |     |    |    |     |      |
| -8  | 0  | 15 | 21  | 18   | -5  | -5 | 17 | 12  | 18   | -4  | -9  | 18 | 14  | 10   |     |    |    |     |      |
| -7  | 0  | 15 | 69  | 59   | -4  | -5 | 17 | 12  | 11   | -3  | -9  | 18 | 20  | 13   |     |    |    |     |      |
| -6  | 0  | 15 | 47  | 42   | -3  | -5 | 17 | 361 | 329  | -2  | -9  | 18 | 9   | 13   |     |    |    |     |      |
| -5  | 0  | 15 | 18  | 10   | -2  | -5 | 17 | 9   | 2    | -1  | -9  | 18 | 128 | 97   |     |    |    |     |      |
| -4  | 0  | 15 | 19  | 6    | -1  | -5 | 17 | 272 | 256  | 0   | -9  | 18 | 17  | 6    |     |    |    |     |      |
| -3  | 0  | 15 | 274 | 307  | 0   | -5 | 17 | 0   | 3    | -7  | -8  | 18 | 3   | 7    |     |    |    |     |      |
| -2  | 0  | 15 | 124 | 79   | 2   | -5 | 17 | 8   | 2    | -6  | -8  | 18 | 38  | 27   |     |    |    |     |      |
| -1  | 0  | 15 | 10  | 3    | -10 | -4 | 17 | 79  | 74   | -5  | -8  | 18 | 13  | 3    |     |    |    |     |      |
| 0   | 0  | 15 | 103 | 75   | -9  | -4 | 17 | 175 | 172  | -4  | -8  | 18 | 10  | 19   |     |    |    |     |      |
| 1   | 0  | 15 | 11  | 3    | -8  | -4 | 17 | 289 | 214  | -3  | -8  | 18 | 114 | 106  |     |    |    |     |      |
| 2   | 0  | 15 | 7   | 5    | -7  | -4 | 17 | 80  | 114  | -2  | -8  | 18 | 53  | 64   |     |    |    |     |      |
| 3   | 0  | 15 | 7   | 7    | -6  | -4 | 17 | 40  | 36   | -1  | -8  | 18 | 0   | 2    |     |    |    |     |      |
| 4   | 0  | 15 | 24  | 13   | -5  | -4 | 17 | 12  | 9    | 0   | -8  | 18 | 151 | 176  |     |    |    |     |      |
| 5   | 0  | 15 | 2   | 5    | -4  | -4 | 17 | 45  | 36   | -8  | -7  | 18 | 20  | 0    |     |    |    |     |      |
| 6   | 0  | 15 | 33  | 25   | -3  | -4 | 17 | 221 | 203  | -7  | -7  | 18 | 45  | 74   |     |    |    |     |      |
| 7   | 0  | 15 | 400 | 415  | -2  | -4 | 17 | 90  | 143  | -6  | -7  | 18 | 10  | 3    |     |    |    |     |      |
| 8   | 0  | 15 | 71  | 76   | -1  | -4 | 17 | 95  | 82   | -5  | -7  | 18 | 30  | 23   |     |    |    |     |      |
| 9   | 0  | 15 | 472 | 434  | 0   | -4 | 17 | 154 | 179  | -4  | -7  | 18 | 7   | 19   |     |    |    |     |      |
| 10  | 0  | 15 | 33  | 49   | 1   | -4 | 17 | 78  | 105  | -3  | -7  | 18 | 22  | 13   |     |    |    |     |      |
| 11  | 0  | 15 | 13  | 5    | -10 | -3 | 17 | 56  | 36   | -2  | -7  | 18 | 102 | 101  |     |    |    |     |      |
| 12  | 0  | 15 | 316 | 269  | -9  | -3 | 17 | 149 | 112  | -1  | -7  | 18 | 28  | 45   |     |    |    |     |      |
| 13  | 0  | 15 | 101 | 139  | -8  | -3 | 17 | 69  | 42   | 0   | -7  | 18 | 20  | 7    |     |    |    |     |      |
| 14  | 0  | 15 | 28  | 0    | -7  | -3 | 17 | 375 | 315  | -8  | -6  | 18 | 21  | 26   |     |    |    |     |      |
| 15  | 0  | 15 | 7   | 4    | -6  | -3 | 17 | 142 | 113  | -7  | -6  | 18 | 139 | 157  |     |    |    |     |      |
| 16  | 0  | 15 | 6   | 3    | -5  | -3 | 17 | 360 | 362  | -6  | -6  | 18 | 41  | 14   |     |    |    |     |      |
| 17  | 0  | 15 | 1   | 19   | -4  | -3 | 17 | 1   | 3    | -5  | -6  | 18 | 39  | 12   |     |    |    |     |      |
| 18  | 0  | 15 | 79  | 64   | -3  | -3 | 17 | 65  | 120  | -4  | -6  | 18 | 169 |      |     |    |    |     |      |

Table C.3, continued

| H   | K  | L  | Obs | Calc | H  | K   | L  | Obs | Calc | H  | K  | L  | Obs | Calc | H | K | L | Obs | Calc |
|-----|----|----|-----|------|----|-----|----|-----|------|----|----|----|-----|------|---|---|---|-----|------|
| -7  | -7 | 17 | 129 | 127  | 0  | -2  | 17 | 32  | 26   | -8 | -4 | 18 | 35  | 53   | - | - | - | -   | -    |
| -6  | -7 | 17 | -6  | 10   | -9 | -1  | 17 | 51  | 77   | -7 | -4 | 18 | 11  | 27   | - | - | - | -   | -    |
| -5  | -7 | 17 | 19  | 2    | -8 | -1  | 17 | -3  | 2    | -6 | -4 | 18 | 258 | 270  | - | - | - | -   | -    |
| -4  | -7 | 17 | 25  | 22   | -7 | -1  | 17 | 123 | 98   | -5 | -4 | 18 | 28  | 112  | - | - | - | -   | -    |
| -3  | -7 | 17 | 79  | 33   | -6 | -1  | 17 | 49  | 20   | -4 | -4 | 18 | 62  | 88   | - | - | - | -   | -    |
| -2  | -7 | 17 | 81  | 54   | -5 | -1  | 17 | 263 | 262  | -3 | -4 | 18 | 4   | 6    | - | - | - | -   | -    |
| -1  | -7 | 17 | 119 | 135  | -4 | -1  | 17 | 4   | 0    | -2 | -4 | 18 | 109 | 112  | - | - | - | -   | -    |
| 0   | -7 | 17 | 14  | 12   | -3 | -1  | 17 | 45  | 50   | -1 | -4 | 18 | 0   | 0    | - | - | - | -   | -    |
| 1   | -7 | 17 | 43  | 59   | -2 | -1  | 17 | 113 | 105  | -8 | -3 | 18 | 84  | 96   | - | - | - | -   | -    |
| 2   | -7 | 17 | 74  | 98   | -1 | -1  | 17 | 13  | 5    | -7 | -3 | 18 | 22  | 20   | - | - | - | -   | -    |
| -9  | -6 | 17 | -2  | 4    | -8 | 0   | 17 | 16  | 7    | -6 | -3 | 18 | 70  | 55   | - | - | - | -   | -    |
| -8  | -6 | 17 | 207 | 155  | -7 | 0   | 17 | 52  | 46   | -5 | -3 | 18 | 12  | 5    | - | - | - | -   | -    |
| -7  | -6 | 17 | 10  | 1    | -6 | 0   | 17 | -1  | 0    | -4 | -3 | 18 | 172 | 153  | - | - | - | -   | -    |
| -6  | -6 | 17 | 178 | 221  | -5 | 0   | 17 | 68  | 75   | -3 | -3 | 18 | 1   | 1    | - | - | - | -   | -    |
| -5  | -6 | 17 | 180 | 168  | -4 | 0   | 17 | 69  | 99   | -2 | -3 | 18 | 163 | 138  | - | - | - | -   | -    |
| -4  | -6 | 17 | 80  | 75   | -3 | 0   | 17 | 6   | 24   | -7 | -2 | 18 | 1   | 0    | - | - | - | -   | -    |
| -3  | -6 | 17 | 0   | 5    | -6 | 1   | 17 | 33  | 32   | -6 | -2 | 18 | 50  | 85   | - | - | - | -   | -    |
| -2  | -6 | 17 | 16  | 30   | -5 | 1   | 17 | 3   | 1    | -5 | -2 | 18 | 20  | 15   | - | - | - | -   | -    |
| -1  | -6 | 17 | 24  | 18   | -3 | -11 | 18 | 33  | 26   | -4 | -2 | 18 | 26  | 26   | - | - | - | -   | -    |
| 0   | -6 | 17 | 1   | 0    | -2 | -11 | 18 | -5  | 2    | -3 | -2 | 18 | 0   | 0    | - | - | - | -   | -    |
| 1   | -6 | 17 | 5   | 0    | -5 | -10 | 18 | 1   | 1    | -  | -  | -  | -   | -    | - | - | - | -   | -    |
| 2   | -6 | 17 | 34  | 53   | -4 | -10 | 18 | 27  | 7    | -  | -  | -  | -   | -    | - | - | - | -   | -    |
| -10 | -5 | 17 | 61  | 52   | -3 | -10 | 18 | 66  | 97   | -  | -  | -  | -   | -    | - | - | - | -   | -    |
| -9  | -5 | 17 | 212 | 177  | -2 | -10 | 18 | 105 | 90   | -  | -  | -  | -   | -    | - | - | - | -   | -    |

a Reflections flagged with an asterisk were considered unobserved.



Table C.4. Atomic multiplicities for [Cu(dipp)<sub>2</sub>]TFPB.

| Name   | Multiplicity | Name   | Multiplicity | Name   | Multiplicity |
|--------|--------------|--------|--------------|--------|--------------|
| Cu     | 1.000        | F(331) | 1.000        | F(332) | 1.000        |
| F(333) | 1.000        | F(351) | 1.000        | F(352) | 1.000        |
| F(353) | 1.000        | F(431) | 1.000        | F(432) | 1.000        |
| F(433) | 1.000        | F(451) | 1.000        | F(452) | 1.000        |
| F(453) | 1.000        | F(531) | 1.000        | F(532) | 1.000        |
| F(533) | 1.000        | F(551) | 1.000        | F(552) | 1.000        |
| F(553) | 1.000        | F(631) | 1.000        | F(632) | 1.000        |
| F(633) | 1.000        | F(651) | 1.000        | F(652) | 1.000        |
| F(653) | 1.000        | N(11)  | 1.000        | N(21)  | 1.000        |
| N(112) | 1.000        | N(212) | 1.000        | C(12)  | 1.000        |
| C(13)  | 1.000        | C(14)  | 1.000        | C(15)  | 1.000        |
| C(16)  | 1.000        | C(17)  | 1.000        | C(18)  | 1.000        |
| C(19)  | 1.000        | C(22)  | 1.000        | C(23)  | 1.000        |
| C(24)  | 1.000        | C(25)  | 1.000        | C(26)  | 1.000        |
| C(27)  | 1.000        | C(28)  | 1.000        | C(29)  | 1.000        |
| C(31)  | 1.000        | C(32)  | 1.000        | C(33)  | 1.000        |
| C(34)  | 1.000        | C(35)  | 1.000        | C(36)  | 1.000        |
| C(41)  | 1.000        | C(42)  | 1.000        | C(43)  | 1.000        |
| C(44)  | 1.000        | C(45)  | 1.000        | C(46)  | 1.000        |
| C(51)  | 1.000        | C(52)  | 1.000        | C(53)  | 1.000        |
| C(54)  | 1.000        | C(55)  | 1.000        | C(56)  | 1.000        |
| C(61)  | 1.000        | C(62)  | 1.000        | C(63)  | 1.000        |
| C(64)  | 1.000        | C(65)  | 1.000        | C(66)  | 1.000        |
| C(110) | 1.000        | C(111) | 1.000        | C(113) | 1.000        |
| C(114) | 1.000        | C(115) | 1.000        | C(116) | 1.000        |
| C(117) | 1.000        | C(118) | 1.000        | C(119) | 1.000        |
| C(120) | 1.000        | C(210) | 1.000        | C(211) | 1.000        |
| C(213) | 1.000        | C(214) | 1.000        | C(215) | 1.000        |
| C(216) | 1.000        | C(217) | 1.000        | C(218) | 1.000        |
| C(219) | 1.000        | C(220) | 1.000        | C(331) | 1.000        |
| C(351) | 1.000        | C(431) | 1.000        | C(451) | 1.000        |
| C(531) | 1.000        | C(551) | 1.000        | C(631) | 1.000        |
| C(651) | 1.000        | B      | 1.000        | H(13)  | 1.000        |
| H(14)  | 1.000        | H(16)  | 1.000        | H(17)  | 1.000        |
| H(19)  | 1.000        | H(23)  | 1.000        | H(24)  | 1.000        |
| H(26)  | 1.000        | H(27)  | 1.000        | H(29)  | 1.000        |
| H(32)  | 1.000        | H(34)  | 1.000        | H(36)  | 1.000        |
| H(42)  | 1.000        | H(44)  | 1.000        | H(46)  | 1.000        |
| H(52)  | 1.000        | H(54)  | 1.000        | H(56)  | 1.000        |
| H(62)  | 1.000        | H(64)  | 1.000        | H(66)  | 1.000        |
| H(110) | 1.000        | H(115) | 1.000        | H(118) | 1.000        |
| H(11A) | 1.000        | H(11B) | 1.000        | H(11C) | 1.000        |
| H(11D) | 1.000        | H(11E) | 1.000        | H(11F) | 1.000        |
| H(11G) | 1.000        | H(11H) | 1.000        | H(11I) | 1.000        |
| H(12A) | 1.000        | H(12B) | 1.000        | H(12C) | 1.000        |
| H(210) | 1.000        | H(215) | 1.000        | H(218) | 1.000        |
| H(21A) | 1.000        | H(21B) | 1.000        | H(21C) | 1.000        |
| H(21D) | 1.000        | H(21E) | 1.000        | H(21F) | 1.000        |
| H(21G) | 1.000        | H(21H) | 1.000        | H(21I) | 1.000        |
| H(22A) | 1.000        | H(22B) | 1.000        | H(22C) | 1.000        |

VITA

## VITA

Corey Thomas Cunningham was born on April 4, 1973 in Danville, Indiana to Stephen and Brenda Cunningham. He spent his childhood in the nearby village of Pittsboro, Indiana. He graduated from Northwest Hendricks Junior Senior High School in Lizton, Indiana in June 1991. He then enrolled at Purdue University, in West Lafayette, Indiana where he stayed for the next 7 years. In May 1995 he completed the bachelors program and graduated with a B.S. in Chemistry. He spent the summer continuing his research under Dr. David R. McMillin and in early August of 1995 he married Dr. Kurstan Cunningham. In late August of 1995 he began his graduate career at Purdue University. While at Purdue, his research focused on the synthesis and photochemistry of transition metal coordination compounds. A little over three years later he defended his Doctor of Philosophy in Inorganic Chemistry under the supervision of Dr. David R. McMillin. He is currently (and forever more) remodeling a 90 year old house in Terre Haute, Indiana with his wife and their two dogs.

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